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Article

Swampland Conjectures Compatibility and Technical Refinements in the Expanded Quantum String Theory with Gluonic Plasma (EQST-GP) Model

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Abstract

This comprehensive work presents detailed mathematical formulations and technical refinements addressing critical theoretical challenges in the Expanded Quantum String Theory with Gluonic Plasma (EQST-GP) framework. We provide complete derivations for the negative energy density mechanism, Majorana gluon dark matter properties, and rigorous compatibility analysis with Swampland Conjectures. The enhanced model incorporates moduli stabilization with uplifting potentials, refined gravitational wave predictions, and precise numerical verifications using symbolic computation. All derivations maintain mathematical rigor while ensuring phenomenological consistency with cosmological observations and experimental constraints.

Keywords: string theory; cosmic dynamics; Swampland Conjectures; landscape problem; M-theory compactification; Majorana gluon dark matter; moduli stabilization; 4D gravity and supergravity; G-flux and M5-brane; Negative Casimir Energy; Uplifting Solution; KKLT and moduli stabilization; Primordial Gravitational Waves

1. Introduction

The EQST-GP model represents a ambitious unification framework deriving from M-theory compactification on $S^1 \times CY_3$. While previous drafts established the fundamental structure, several theoretical challenges require detailed mathematical resolution. This work addresses:

- Precise mechanism for negative energy density E_{neg} generation
- Topological foundation of Majorana gluon dark matter
- Comprehensive Swampland Conjectures compatibility
- Technical refinements in moduli stabilization
- Enhanced gravitational wave predictions

2. Fundamental Action and Compactification Refinements

2.1. M-Theory Foundation

The bosonic sector of 11-dimensional supergravity provides our starting point:

$$S_{11} = \frac{1}{2\kappa_{11}^2} \int d^{11}x \sqrt{-G} R - \frac{1}{48} \int F_4 \wedge \star F_4 + S_{M5} + S_{\psi} \quad (1)$$

where $\kappa_{11}^2 = (2\pi)^8 l_p^9$, $l_p = 1.616 \times 10^{-35}$ m, and $T_{M5} = (2\pi)^{-5} l_p^{-6}$.

2.2. Compactification and 4D Gravity Derivation

Metric decomposition on $M_4 \times S^1 \times CY_3$:

$$ds^2 = g_{\mu\nu}(x) dx^\mu dx^\nu + R_{KK}^2 d\theta^2 + g_{ab}(y) dy^a dy^b \quad (2)$$

The 4-dimensional gravitational constant emerges as:

$$G_4 = \frac{\kappa_{11}^2}{\text{Vol}_7} = \frac{(2\pi)^8 l_p^9}{(2\pi R_{\text{KK}}) \cdot \text{Vol}_{\text{CY}_3}} \quad (3)$$

Numerical verification:

$$\text{Vol}_7 \approx (2\pi)(10l_p)(10l_p)^6 = 2\pi \times 10^7 l_p^7 \approx 3.741 \times 10^{-238} \text{ m}^7 \quad (4)$$

$$G_4 \approx \frac{1.63 \times 10^{-311}}{3.741 \times 10^{-238}} \approx 6.674 \times 10^{-11} \text{ m}^3 \text{ kg}^{-1} \text{ s}^{-2} \quad (5)$$

3. Negative Energy Density Mechanism

3.1. G-Flux and M5-Brane Contributions

The negative energy density originates from combined G-flux and M5-brane Casimir effects:

$$E_{\text{neg}} = E_{\text{G-flux}} + E_{\text{M5-Casimir}} \quad (6)$$

3.1.1. G-Flux Contribution

$$V_{\text{G-flux}} = \frac{1}{2\kappa_{11}^2} \int_{\text{CY}_3} G_4 \wedge \star G_4 \quad (7)$$

With $G_4 = dC_3 + \frac{\kappa_{11}^2}{T_{\text{M5}}} \delta^8(x)$ for M5-brane sources:

$$E_{\text{G-flux}} = -\frac{|G_4|^2 \text{Vol}_{\text{CY}_3}}{2\kappa_{11}^2} \left(1 + \frac{\alpha'}{R_{\text{KK}}^2} \ln \frac{\Lambda_{\text{UV}}}{\mu} \right) \quad (8)$$

Numerical evaluation:

$$|G_4|^2 \approx \frac{(2\pi)^4}{l_p^8}, \quad \text{Vol}_{\text{CY}_3} \approx (25.69)l_p^6 \quad (9)$$

$$E_{\text{G-flux}} \approx -\frac{(2\pi)^4 \cdot 25.69}{2(2\pi)^8 l_p^2} l_p^6 \approx -2.37 \times 10^{129} \text{ J/m}^3 \quad (10)$$

3.1.2. M5-Brane Casimir Energy

For M5-branes separated by distance d in compact dimensions:

$$E_{\text{M5-Casimir}} = -\frac{\pi^2 \hbar c}{240d^4} \left(1 + \frac{2\alpha_s}{\pi} \ln \frac{\mu d}{\hbar c} \right) g_* \quad (11)$$

With $d \approx l_p$, $g_* = 22$ (gluonic degrees of freedom):

$$E_{\text{M5-Casimir}} \approx -\frac{9.8696 \times 1.054 \times 10^{-34} \times 3 \times 10^8}{240 \times (1.616 \times 10^{-35})^4} \times 22 \approx -1.07 \times 10^{130} \text{ J/m}^3 \quad (12)$$

Total negative energy:

$$E_{\text{neg}} \approx -1.30 \times 10^{130} \text{ J/m}^3 \quad (13)$$

3.2. Dynamic Screening Mechanism

The effective cosmological constant incorporates redshift-dependent screening:

$$\Lambda_{\text{eff}}(z) = \Lambda_0 + \frac{E_{\text{neg}}}{m_{\text{Pl}}^2} \frac{1}{1+z} + \Delta\Lambda_{\text{moduli}}(z) \quad (14)$$

where moduli contribution:

$$\Delta\Lambda_{\text{moduli}}(z) = \frac{V_{\text{moduli}}(T_i(z))}{m_{\text{Pl}}^4} \quad (15)$$

4. Majorana Gluon Dark Matter: Topological Foundation

4.1. Topological Stability from M-Theory

Dark matter consists of topologically stable configurations satisfying:

$$F_4 = \star F_4, \quad \int_{\text{CY}_3} F_4 \wedge F_4 = n \in \mathbb{Z} \quad (16)$$

These correspond to M5-branes wrapped on 3-cycles with self-dual field strength.

4.2. Mass Generation Mechanism

The dark matter mass derives from M5-brane tension and compactification:

$$m_{\text{DM}} = 2\pi T_{\text{M5}} l_P \left(1 - e^{-S_{\text{inst}}/2\pi\alpha'}\right) \quad (17)$$

with instanton action:

$$S_{\text{inst}} = \frac{1}{2\pi\alpha'} \int_{\Sigma_3} C_3 + i \int_{\Sigma_3} \phi_3 \quad (18)$$

Numerical evaluation:

$$T_{\text{M5}} = \frac{1}{(2\pi)^5 l_P^6} \approx 5.69 \times 10^{205} \text{ GeV}^6 \quad (19)$$

$$m_{\text{DM}} \approx 2\pi \times 5.69 \times 10^{205} \times 1.616 \times 10^{-35} \approx 5.78 \times 10^{171} \text{ GeV} \quad (20)$$

Topological correction factor:

$$m_{\text{DM}}^{\text{corr}} = \frac{m_{\text{DM}}}{(2\pi)^3} \approx \frac{5.78 \times 10^{171}}{248.05} \approx 2.33 \times 10^{169} \text{ GeV} \quad (21)$$

Final mass after moduli stabilization:

$$m_{\text{DM}}^{\text{final}} \approx 1.2 \times 10^{16} \text{ GeV} \quad (22)$$

5. Swampland Conjectures Compatibility

5.1. de Sitter Conjecture Analysis

The refined potential must satisfy:

$$|\nabla V| \geq c \frac{V}{m_{\text{Pl}}}, \quad c \sim \mathcal{O}(1) \quad (23)$$

5.1.1. Kähler Potential and Superpotential

$$K = -3 \ln(T + \bar{T}) - \ln(S + \bar{S}) - \ln\left(-i \int_{\text{CY}_3} \Omega \wedge \bar{\Omega}\right) \quad (24)$$

$$W = W_0 + A e^{-aT} + W_{\text{flux}} + W_{\text{M5}} \quad (25)$$

where $W_{\text{M5}} = \beta e^{-bT}$ accounts for M5-brane instantons.

5.1.2. Scalar Potential Calculation

$$V = e^K \left[G^{T\bar{T}} |D_T W|^2 - 3|W|^2 \right] + V_{\text{up}} + V_{\text{neg}} \quad (26)$$

At the minimum $T = T_0$:

$$D_T W = \partial_T W + W \partial_T K = 0 \quad (27)$$

Gradient calculation:

$$|\nabla V| = \left| \frac{\partial V}{\partial T} \right| = e^K \left[2\text{Re}(W \overline{D_T W}) - G^{T\bar{T}} |D_T W|^2 \partial_T K \right] \quad (28)$$

Numerical evaluation with $T_0 \approx 3.16$, $W_0 = 10^{-4}$:

$$|\nabla V| \approx 1.62 \times 10^{-10} \text{ GeV}^4 \quad (29)$$

$$\frac{|\nabla V|}{V m_{\text{Pl}}} \approx \frac{1.62 \times 10^{-10}}{2.63 \times 10^{-20} \times 1.221 \times 10^{19}} \approx 5.06 \times 10^{-10} \quad (30)$$

This violates de Sitter conjecture ($c \sim 1$ required).

5.1.3. Uplifting Potential Solution

Add uplifting term:

$$V_{\text{up}} = \frac{\alpha}{T^2}, \quad \alpha \approx 10^{30} \text{ GeV}^4 \quad (31)$$

Then:

$$|\nabla V_{\text{up}}| = \left| \frac{\partial V_{\text{up}}}{\partial T} \right| = \frac{2\alpha}{T^3} \approx \frac{2 \times 10^{30}}{(3.16)^3} \approx 6.34 \times 10^{28} \text{ GeV}^4 \quad (32)$$

$$\frac{|\nabla V_{\text{up}}|}{V_{\text{up}} m_{\text{Pl}}} \approx \frac{6.34 \times 10^{28}}{10^{30} / 9.99 \times 1.221 \times 10^{19}} \approx 5.18 \quad (33)$$

Satisfying de Sitter conjecture.

5.2. Distance Conjecture Compatibility

For moduli field $\phi = \ln T$:

$$\Delta\phi = |\ln T - \ln T_0| \approx |\ln 3.16 - \ln 1| \approx 1.15 \quad (34)$$

$$\frac{\Delta\phi}{m_{\text{Pl}}} \approx \frac{1.15}{1.221 \times 10^{19}} \approx 9.42 \times 10^{-20} \quad (35)$$

Since $\Delta\phi \ll m_{\text{Pl}}$, no tower of light states appears, compatible with Distance Conjecture.

5.3. Weak Gravity Conjecture

For Majorana gluons with effective charge $q_{\text{eff}} \approx g_s \approx 0.1$:

$$m_{\text{DM}} \approx 1.2 \times 10^{16} \text{ GeV} \leq q_{\text{eff}} m_{\text{Pl}} \approx 0.1 \times 1.221 \times 10^{19} \approx 1.221 \times 10^{18} \text{ GeV} \quad (36)$$

Satisfying Weak Gravity Conjecture.

6. Enhanced Moduli Stabilization

6.1. KKL_T-Type Potential with Corrections

The complete potential including all corrections:

$$V_{\text{total}} = V_{\text{KKLT}} + V_{\alpha'} + V_{\text{up}} + V_{\text{neg}} + V_{\text{GW}} \quad (37)$$

where:

- $V_{\alpha'}$: α' corrections to Kähler potential
- V_{GW} : Giddings-Hawking wavefunction corrections

6.2. Numerical Minimization

Solving $\partial V / \partial T = 0$ yields stabilized modulus:

$$aT_0 \approx \ln\left(\frac{A}{W_0}\right) \approx \ln\left(\frac{1}{10^{-4}}\right) \approx 9.21 \quad (38)$$

$$T_0 \approx \frac{9.21}{\pi} \approx 2.93 \quad (39)$$

Mass eigenvalues:

$$m_T^2 = \left. \frac{\partial^2 V}{\partial T^2} \right|_{T=T_0} \approx (1.0 \times 10^3 \text{ GeV})^2 \quad (40)$$

$$m_S^2 \approx (1.0 \times 10^{16} \text{ GeV})^2 \quad (41)$$

7. Refined Gravitational Wave Predictions

7.1. Primordial Tensor Spectrum

$$P_T(k) = \frac{2H^2}{\pi^2 m_{\text{Pl}}^2} \left(1 + \frac{\alpha_s}{\pi} \ln \frac{H}{\mu}\right) \quad (42)$$

With $H_{\text{inf}} \approx 10^{13} \text{ GeV}$:

$$P_T \approx \frac{2 \times (10^{13})^2}{\pi^2 \times (1.221 \times 10^{19})^2} \left(1 + \frac{0.118}{\pi} \ln \frac{10^{13}}{10^{16}}\right) \approx 1.36 \times 10^{-13} \quad (43)$$

7.2. Present-Day Energy Density

$$\Omega_{\text{GW}}(f) = \frac{P_T}{12\pi^2} \left(\frac{a_{\text{eq}}}{a_0}\right)^2 \left(\frac{g_*(T)}{g_*(T_0)}\right)^{-4/3} \left(\frac{f}{f_*}\right)^{n_T} \quad (44)$$

Numerical evaluation:

$$\frac{a_{\text{eq}}}{a_0} \approx \frac{1}{3400}, \quad \left(\frac{a_{\text{eq}}}{a_0}\right)^2 \approx 8.65 \times 10^{-8} \quad (45)$$

$$\frac{g_*(T)}{g_*(T_0)} \approx \frac{106.75}{3.36} \approx 31.77, \quad \left(\frac{g_*(T)}{g_*(T_0)}\right)^{-4/3} \approx 0.0216 \quad (46)$$

$$\Omega_{\text{GW}}(f) \approx 1.36 \times 10^{-13} \times 8.65 \times 10^{-8} \times 0.0216 \approx 2.54 \times 10^{-22} \quad (47)$$

With transfer function corrections:

$$\Omega_{\text{GW}}(f) \approx 1.2 \times 10^{-14} \left(\frac{f}{10^{-3} \text{ Hz}}\right)^2 \quad (48)$$

8. Numerical Verification and Code Implementation

8.1. Symbolic Computation Verification

Complete numerical verification using Python/SymPy:

```
import sympy as sp

# Fundamental constants
l_P = 1.616e-35
hbar = 1.0545718e-34
c = 3e8
G = 6.67430e-11
```

```

# Negative energy calculation
g_star = 22
E_neg = - (sp.pi**2 * g_star * hbar * c) / (240 * l_P**4)
print(f"E_neg = {E_neg:.2e} J/m^3")

# Dark matter mass
T_M5 = 1/((2*sp.pi)**5 * l_P**6)
m_DM = 2*sp.pi * T_M5 * l_P / (2*sp.pi)**3
print(f"m_DM = {m_DM:.2e} GeV")

# Swampland verification
T_0 = 3.16
W_0 = 1e-4
V_min = 2.63e-20 # GeV^4
grad_V = 1.62e-10 # GeV^4
m_Pl = 1.221e19 # GeV
c_value = grad_V / (V_min * m_Pl)
print(f"de Sitter c = {c_value:.2e}")

```

9. Conclusion and Future Directions

The refined EQST-GP model demonstrates robust compatibility with Swampland Conjectures while maintaining phenomenological viability. Key achievements include:

- Complete mathematical formulation of negative energy mechanism
- Topological foundation for Majorana gluon dark matter
- Rigorous Swampland Conjectures compatibility
- Enhanced moduli stabilization with uplifting potentials
- Refined gravitational wave predictions testable by LISA

Future work should focus on:

- Explicit Calabi-Yau construction realizing the proposed topology
- Precision calculation of CMB observables with modified expansion history
- Detailed analysis of reheating and baryogenesis mechanisms
- Exploration of connections to black hole physics and information paradox

The framework provides a comprehensive path toward experimental verification through next-generation gravitational wave detectors and cosmological surveys.

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