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DFT Calculation of the Electronic Properties of Cubic Ti₃Sb Crystals with Adsorbed and/or Partially Substituted Nitrogen

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Abstract

Due to their chemical structure and convenient, tunable physicochemical properties, intermetallic alloys and materials are promising for use in various fields, such as gas sensors. The aim of this study was to perform DFT GGAS calculations of the adsorption energy of atomic nitrogen and the properties of partially substituted metal atoms with nitrogen in Ti₃Sb supercells with an A15 cubic structure. Adsorption and doping at various adsorption sites and crystallographic orientations (110; 111; 100), as well as their electronic properties, were studied in 2 × 2, 3 × 3, and 5 × 5 supercells. The density of states (DOS) of Ti₃Sb–N supercells with two different positions of partial substitution of nitrogen for Ti₃Sb metal atoms was calculated: N/Ti and N/Sb. Comparative data show that the structural and energetic properties of Ti₃Sb–N vary compared to pure Ti₃Sb. Controlled incorporation of nitrogen atoms and partial substitution of Ti₃Sb atoms allow for tuning of the properties of Ti₃Sb–N. These data can be used to optimize and predict the electronic structure and response characteristics of such materials for electronics and catalysis. They are also important as potential sensor materials with exceptional properties and promising applications for nitrogen detection in targeted developments

Keywords: calculation of electronic properties; cubic structure; Ti₃Sb supercell; nitrogen adsorption; partial substitution with nitrogen; DFT method

1. Introduction

Intermetallic compounds (IC) possess a unique ability to bond with other elements, resulting in the creation of practically important structures for a wide range of applications. One way to improve the performance of materials is through adsorption and doping with metals and non-metallic elements. Understanding these processes requires considering, in particular, the role of electron affinity, orbital chemistry, band gap chemistry, conductivity, bond type, and spin redistribution. Therefore, gaining fundamental knowledge about the relationship between the electronic, physical, and chemical properties of materials and their structural features remains an important task. ICs are a promising alternative to, for example, superconductors and catalysts based on metals or metal oxides. ICs offer advantages such as low cost, structural flexibility beyond the atomic scale, excellent electronic conductivity, high specific surface area, and good stability.

Electron ICs such as the Laves phase and Hume-Rothery phase have structures characteristic of metallic elements. In these compounds, the structure of the resulting phases is primarily determined by the electron concentration, i.e., the ratio of the number of valence electrons to the number of atoms

in the unit cell. When these compounds form, transition metals exhibit variable valence, due to the overlap of the d- and s-levels.

When the ratio of the number of valence electrons to the number of atoms in the lattice changes, intermetallic compounds form various structures, including those with a cubic lattice (e.g., Ti_3Sb, FeAl, CoAl, NiAl and alloys based on them). These intermetallic compounds possess metallic properties, but the participation of d-electrons in the interatomic bonding predetermines the appearance of a covalent component.

From the above, it follows that the electronic structure of intermetals can be tuned using different types of adsorbates and doping. This makes them attractive for use in various fields, such as electronics, catalysis, and so on. The change in properties upon adsorption and alloying significantly alters the structures with a multivalent element, where the lattice symmetry changes, allowing such compounds to be used as functional materials in electronics and industry.

As a result, absorption and doping has become a common strategy for controlling the properties of source materials. First, let's review some results from studies of nitrogen adsorption on the surfaces of alloys and intermetallic compounds. We'll focus on solving the problem using DFT calculations and new methods.

The authors of work [1] studied the adsorption of N_2 and atomic N on the ZrMnFe(110) surface using the DFT method, including the barriers of dissociation and penetration of the atom into the surface. It was indicated that the best adsorption site is "vacancy Hollow 1 composed of 4Zr1Fe". The adsorption energy of the N atom is $E_{ads}(N) \approx 6.057$ eV, and N_2 $E_{ads}(N_2) \approx 10.215$ eV, the barriers are 1.129 eV (dissociation) and 0.766 eV (penetration).

The influence of atomic composition and environment on nitrogen adsorption on high-entropy alloy (HEA) surfaces is examined in [2]. The authors investigate the adsorption of molecular N_2 on HEA surfaces from the perspective of the influence of the local environment (the first and second shells of neighboring atoms) on the bond strength. DFT calculations with van der Waals corrections and Bayesian error estimation methods are used. The main conclusion is that the d-band of the active atom's center is regulated by neighboring atoms, and this "influence shell" can be used as a "designer" for tuning nitrogen binding.

In order to model the influence of local structural variations on the adsorption of nitrogen atoms, the authors of work [3] studied the adsorption of atomic nitrogen on the bimetallic surface Ni/Pt(111) with different Ni configurations (on the surface, in the subsurface, in clusters). The proposed model is: binding energy = base (on Pt) + linear correction from Ni neighbors to the third nearest order. The model was used to parameterize the adsorption energy as a perturbation of the adsorption energy on the host metal relative to the coordination number of the guest metal. The model was applied to N adsorption on the Ni/Pt(111) system, using a parameterization with a small number of surface and subsurface Ni structures on Pt(111) and Ni clusters in the first and/or second Pt layer.

The DFT-D3 method was used to study the chemisorption of H_2 and N_2 on cobalt-promoted Ta_3N_5-(100), (010), and (001) surfaces [4]. The adsorption (including molecular, with the possibility of activation) of N_2 on the faces of the nitride surface of Ta_3N_5, with the participation of added Co, is considered. It is shown that N_2 is adsorbed molecularly (not completely dissociated) in various orientations (side-on, end-on, tilt), and the interaction with transition elements of Co is discussed. It was shown that the formation energies of nitrogen vacancies were relatively high compared to other metal nitrides and were 2.89 eV, 2.32 eV, and 1.95 eV for cobalt coadsorbed on the surface and cobalt coadsorbed under the surface of Ta_3N_5-(010).

The authors of work [5] use a combination of DFT and machine learning to screen HEA catalytic surfaces (Co, Mo, Fe, Ni, Cu) for H, N, NH_χ adsorption properties. They attempt to find a composition at which the binding of N (and intermediate nitrogen species) is not stringent, but sufficient for activation. Using a computational approach based on first-principles calculations, combined with data analytics and machine learning, a model is proposed for rapidly calculating the adsorption energies of H, N, and NHx ions (x = 1, 2, 3) on CoMoFeNiCu alloy surfaces with different alloy compositions and atomic arrangements. A Co/Mo ratio of 25/45, experimentally identified as the most

active for ammonia decomposition, increases the probability that the surface adsorbs nitrogen equivalent to the adsorption

The study in [6] examines the influence of interstitial nitrogen on oxygen adsorption on the iron surface. It is shown that the presence of N atoms within the Fe lattice alters the surface electron density and enhances/weakens the adsorption of other atoms [7–10].

Intermetallic compounds, including type A_3B A15, form the basis of industrial alloys due to their variable composition, unique active-site properties, and adjustable crystal structure with a characteristic electronic spectrum (cubic, tetragonal, and hexagonal structure).

However, the electronic structure affecting the catalytic activity of pure binary A_3B A15 compounds in reactions that evolve gases such as nitrogen has been poorly studied. This problem can be addressed by DFT calculations involving the doping of A_3B A15 crystals. Studying the doping process allows for the adjustment of the electronic structure of the material, the Gibbs free energy of phase formation, and the structure of the d-band center to improve the kinetics of catalytic reactions.

Therefore, for example, atomic doping of Ti_3Sb crystals with nitrogen is of scientific and practical interest. Let us briefly review some similar studies on nitrogen doping of alloys. This is important for the development and creation of highly effective intermetallic materials, for example, for catalytic processes.

2. Materials and Methods

A. General Settings

Density functional theory (DFT) calculations [11–24] of Ti_3Sb–N supercells with a cubic structure (a = 5.2228 Å, A15 phase, Cr_3Si prototype, $Pm\bar{3}n$ space group, no. 223) were performed using the Vienna Ab initio Simulation Package (VASP) based on plane waves and the Atomistic Toolkit (ATK) [25,26]. The threshold value of the plane wave kinetic energy was fixed at 500 eV. Γ-centered grids (2 × 2 × 1, 3 × 3 × 3, 5 × 5 × 5) with the same k-point spacing were used to select the Brillouin zones. Energy band calculations for A_3B A15 were performed along L–Γ–X trajectories. Noncollinear calculations took into account the spin–orbit coupling (SOC) effect.

The electron configurations of the atoms had the following valence states of the orbitals in the calculations: Ti–[Ar] $3d^24s^2$, Sb–[Kr] $4d^{10}5s^25p^3$, and N–[He] $2s^22p^3$. Integration over the Brillouin zone was performed using the Monkhorst–Pack scheme with a grid step of 0.03 Å^{-1}. The convergence threshold for the kinetic energy of the wave functions was less than 0.1 meV/atom. The BFGS minimization scheme [26] was used for geometric optimization of the crystal A15 structure.

The following threshold values were used for the calculations: maximum residual force acting on an atom of 1 × 10^{-7} eV, maximum displacement of atoms of 1 × 10^{-4} eV/Å and maximum stress of less than 0.001 GPa along the crystallographic directions to optimize the A15 structure, respectively. The lattice constant of Ti_3Sb optimized by the DFT GGA PBE method was found to be a = 5.215 Å, which is in good agreement with the known value [26].

B. Calculating Adsorption Energy

Adsorption Energy

Calculated values of the mechanical properties of metals typically differ from experimental data depending on the crystal orientation and the locations where adsorbed particles can be located on the facet surface (top-T, bridge-B, hollow-H). DFT calculations of Ti_3Sb–N adsorption showed that the difference in the calculated adsorption energies (per potential adsorption barrier) between the different crystallographic surfaces of the cubic Ti_3Sb crystal is insignificant. For ease of comparison of the calculated nitrogen atom adsorption energies across crystal sites, only the (110) surface of the A15 cubic cell of the Ti_3Sb compound was considered (Figure 1).
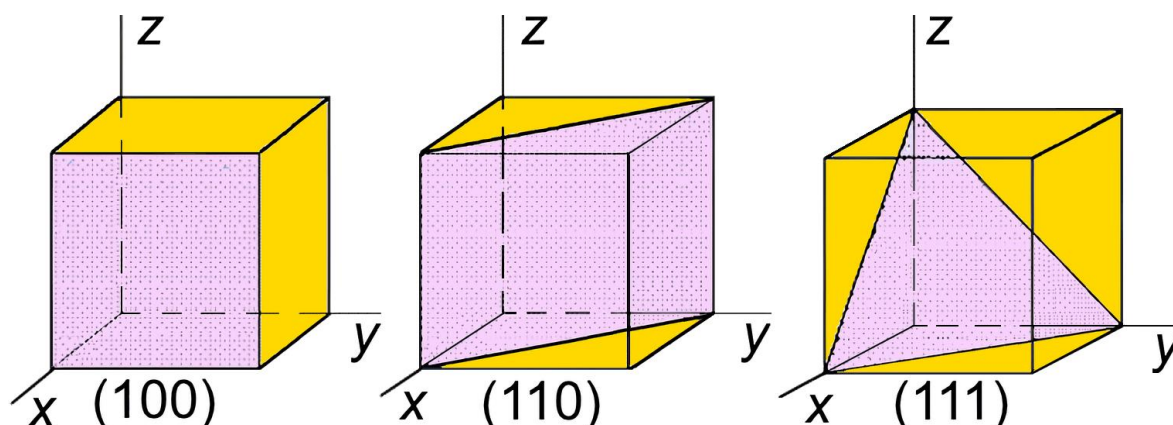
Figure 1. The arrangement of different planes in a cubic unit cell.

In the (100; 110; 111) planes of an ideal cubic lattice, the number of particles should be the same, since crystal anisotropy is absent. The surface energy of crystals with an ideal cubic lattice depends primarily on the valence, electron charge, lattice constant, ionic radius, and electron work function. The surface energies calculated by the DFT method for different orientations (100; 110; 111) of cubic crystals, depending on the number of layers in the crystal plate, differ little from each other, and there is no surface energy anisotropy [26].

Atomic nitrogen N was used as the adsorbate rather than molecular nitrogen N_2 for the following reasons:

1. Simplicity of modeling. Atomic nitrogen is easier to model due to its simpler electronic structure. The N_2 molecule consists of two atoms with additional electronic interactions, which are more difficult to describe in the context of adsorption.

2. Reaction kinetics. Nitrogen adsorption on a surface can occur in atomic form, since N_2 molecules can dissociate at the surface, converting into atomic nitrogen. This is relevant for processes such as nitrogen diffusion, catalytic reactions, or nitration reactions, where atomic nitrogen can participate in the reaction.

3. Energetic considerations. Adsorption of atomic nitrogen should be more stable than adsorption of molecular N_2, since N_2 can dissociate at the active sites of catalysts or other surfaces.

4. Simplification of calculations. In DFT calculations, it was assumed that the adsorbed nitrogen particles (atom or molecule) had already gone through intermediate stages (dissociation, etc.), and only the atomic form of nitrogen actively interacts with the surface.

Surface coverage

Dependence of adsorption energy on surface coverage θ. This is one of the fundamental factors influencing adsorption energy. Surface coverage, usually expressed as a fraction of a monolayer (ML), determines the number of adsorbed atoms (in our case, nitrogen) per unit surface area.

Interaction between adsorbate particles. At high coverage (approximately 1 ML), adsorbed atoms can begin to interact with each other (repulsion or attraction), changing the overall energy of the system.

Occupancy of various active sites. At low coverages, nitrogen can only occupy energetically favorable (active) sites, but as coverage increases, it can occupy less favorable sites, which increases the adsorption energy (in absolute terms, it will decrease–that is, adsorption is less favorable).

Charge and structural effects. A large number of adsorbate atoms can alter the charge distribution, local electronic structure, and even lead to changes in surface symmetry. Taking this into account, we determined the optimal coverage, which characterizes the adsorption capacity of Ti_3Sb. A low coverage (θ = 1/9 ML in the supercell) minimizes interactions between adsorbed atoms and allows energy to be obtained for a single adsorbed atom near the ideal location. In this case, the

dependence of the adsorption energy on the degree of coverage has a minimum, which is the optimal coverage for the stable phase.

In the calculations, a series of models were constructed for different coatings based on adsorption configurations at different sites. The (001), (100), or (110) adsorption planes were selected.

To study the most densely packed and stable surface, the (111) plane in Ti₃Sb was chosen. The properties of the (111) plane is well known. It is energetically stable. In many cubic structures (FCC, cubic intermetallic), (111) is one of the most stable surfaces.

3. Results and Discussion

The creation of nanoscale materials based on A15 phases, particularly those containing Ti, is important for improving their physicochemical properties. Such doped materials could be important for superconducting and adsorption-catalytic systems.

A. Adsorption energy

A literature review (2022–2025) revealed no DFT data on the adsorption energy of atomic nitrogen on titanium alloys. The existing studies consider either metals, alloys with other metals, molecular nitrogen, or conditions different from those for atomic nitrogen adsorption on the titanium alloy surface. Furthermore, to compare adsorption data with existing studies, the nitrogen adsorption conditions (temperature, coating, surface structure) must be similar. We are interested in the adsorption energy of atomic nitrogen N on the surface of titanium-containing alloys. For example, the adsorption and diffusion of atomic nitrogen in cubic α-Ti (α-Ti(0001)) were studied in [27]. It was shown that the N atom is adsorbed on the surface of α-Ti(0001) in FCC and HCP structures. The FCC structure has a lower adsorption energy for nitrogen N atom. Doping α-Ti with aluminum (Al) reduces the adsorption capacity. However, the adsorption energy of N in α-Ti was not reported.

No such data are available for the Ti₃Sb–N system. DFT calculations of N adsorption in the Ti₃Sb–N supercell were considered at different surface sites (T, B, H-site). We considered four different N adsorption sites on the Ti₃Sb surface. They were located: (i) directly above the surface titanium atom (T-site); (ii) midway between two nearest neighboring surface titanium atoms (bridge site); (iii) in the hollow above the titanium atom in the second layer (H-site); and (iv) in the hollow above the titanium atom in the third layer.

The nitrogen adsorption energy E_{ads} (N) was calculated as the difference between the total energy of the supercell with the adsorbed nitrogen atom Ti₃Sb–N, the energies of the Ti₃Sb surface and the nitrogen atom N in vacuum:

$$E_{\text{ads}}(\text{N}) = \frac{1}{n} E\big(\text{Ti}_3\text{Sb} + n(\text{N})\big) - E(\text{Ti}_3\text{Sb}) - nE(\text{N}) \quad (1)$$

where $E\big(\text{Ti}_3\text{Sb} + n(\text{N})\big)$ is the total energy of the Ti₃Sb–N system with an adsorbed N atom, $E(\text{Ti}_3\text{Sb})$ is the energy of the Ti₃Sb plate surface, *n* is the number of adsorbed N atoms, $E(\text{N})$ is the energy of N atoms, respectively.

Lower adsorption energies E_{ads} of N atoms on the Ti₃Sb surface correspond to more stable adsorption centers or sites. N adsorption on the Ti₃Sb surface has a negative E_{ads} value.

Nitrogen-containing cubic metallic structures are known to have two highly symmetric interstitial positions (octahedral (O) and tetrahedral (T)). These positions are energetically more probable for the location of adsorbed or doping nitrogen in the cubic lattice. The arrangement of the various planes in a cubic unit cell is shown in Figure 1.

As noted above, the adsorbate coverage θ is a key parameter in adsorption studies. Monolayer fractions ($0 \le \theta \le 1$) were used in DFT calculations. The coverage was determined by the number of adsorbed atoms on the model surface

$$\theta = \frac{N_{\text{ads}}}{N_{\text{sites}}} \quad (2)$$

where N_{ads} is the number of adsorbed nitrogen atoms, and N_{sites} is the total number of active sites on the surface. Using the cubic Ti₃Sb surface cell model, the number of sites suitable for adsorption was determined, and nitrogen atoms N 1, 2, 3, etc., were added to these sites. Each added N atom corresponded to its own θ = 1/n, 2/n, etc. The periodicity of the cell model was taken into account. Adding one N atom to a given region, for example, a 2 × 2 cell, results in a coverage of θ = 0.25 ML. Experimental methods for determining coverage are often used in surface physical chemistry. Coverage is determined, for example, by pressure and Langmuir isotherms

$$\theta = \frac{KP}{1+KP} \quad (3)$$

where K is the adsorption equilibrium constant, and P is the partial pressure of the adsorbate (in our case, nitrogen).

We investigated the adsorption energy E_{ads} on the Ti₃Sb surface at low nitrogen concentrations. The equilibrium adsorption parameters of Ti₃Sb–N are presented in Table 1 for a 2 × 2 supercell and a coverage of θ = 0.25 ML. The E_{ads} values for relaxed Ti₃Sb–N structures differ from the E_{ads} of hydrogen in the Ti₃Sb–H supercell [26].

Table 1. Calculated equilibrium energy of nitrogen absorption for the 2 × 1 × 1 Ti₃Sb(111) supercell. θ = 0.25 ML.

Supercell	E_{ads}, eV
Ti₃Sb(111)–N	-3.11
Ti₃Sb(110)–H [26]	-0.55

Using the Nudged Elastic Band (NEB) method [28], the transition state energy of nitrogen atom adsorption was determined. The distance from the Ti₃Sb surface for the adsorption of nitrogen atoms was varied in the range of 1–3 Å. The transition state structures were localized as the structures with the highest energy along the reaction coordinate, characterized by a single imaginary frequency. The adsorption activation energies differ for different faces. The activation energies for adsorption on Ti₃Sb (111), Ti₃Sb (110), and Ti₃Sb(100) are negative and are -0.07, 0.17, and -0.11 eV, respectively.

Thus, the stable N adsorption configuration on the studied Ti₃Sb faces is N adsorption on top of Ti₃Sb (111), with an adsorption energy of –3.11 eV. The N adsorption energies on Ti₃Sb (100) and Ti₃Sb (110) are –0.87 and –0.15 eV, respectively. For the Ti₃Sb (100) and (110) crystallographic faces, the energetically favorable N adsorption trajectory is the bridged adsorption form (located near two adjacent Ti₃Sb atoms).

The adsorption energy E_{ads} of atomic nitrogen on Ti₃Sb is significantly lower than that of hydrogen (Table 1). This may be due to several physicochemical factors.

1. Different nature of the chemical bond. Atomic nitrogen has five valence e⁻ orbitals ($2s^2 2p^3$ configuration), making it nucleophilic and allowing it to form a variety of bonds, including triple bonds. However, efficient nitrogen adsorption on the surface requires accessible d-orbitals with a specific energy and spatial orientation. Hydrogen, in contrast, has one electron orbital ($1s$), which interacts more readily with the surface, even on a metal with a low-activity substrate. It readily adsorbs on many metallic surfaces through simple donor-acceptor interactions. Conclusion: atomic nitrogen has difficulty finding a compatible orbital on the Ti₃Sb surface, while hydrogen atoms easily do so.

2. Composition and electronic structure of Ti₃Sb. Ti₃Sb is an intermetallic compound, where Ti, a transition metal, produces d-orbitals; Sb is a semimetal with high electronegativity (~2.05), which can be considered a "sink" for Ti's electron density. As a result, the Ti₃Sb surface may be charge- and orbitally suboptimal for strong nitrogen adsorption. The d-orbitals of Ti may be partially filled and may not be available for strong bonding with N. Conclusion: the electronic state of Ti on the surface is not capable of effectively capturing and stabilizing nitrogen (including due to the strong π-electron nature of N).

3. Differences in radii and steric effects. Atomic nitrogen is larger than hydrogen but has a lower tendency to form strained bonds. However, steric effects and the arrangement of the Ti and Sb atoms may not favor a stable geometry for N. Conclusion: geometrically, Ti₃Sb can be considered a substrate that does not prefer N (no convenient sites, weak orbital match, steric hindrance).

4. Thermodynamic properties of N and H. Nitrogen prefers to form N_2, a molecule with high bound energy (~9.8 eV), so atomic nitrogen is very unstable and does not tend to remain alone. Hydrogen H does not have this problem, and its atomic form is easily adsorbed, in some ways "preferably" than H_2. Conclusion: even if atomic N is brought to the surface, it energetically prefers to leave it or form an N_2 molecule rather than create a stable adsorption configuration.

Taking into account the above reasons for the low $E_{ads}(N)$ on Ti₃Sb, we can conclude. There is weak orbital bonding between the N and *d*-orbitals of Ti, and therefore the accessibility of donor-acceptor orbitals is low. Energetically, nitrogen prefers to remain in its molecular form (N_2) rather than in its atomic form. Hydrogen is more easily adsorbed on various types of surfaces. Therefore, the Ti3Sb surface is a site for very weak fixation of atomic nitrogen.

Based on these data, it can be concluded that Ti₃Sb is selective and resistant to surface poisoning. Weak N adsorption means that the Ti₃Sb surface will be resistant to nitrogen-containing pollutants such as NO, NO_2, NH_3, etc. Therefore, Ti₃Sb may be a suitable material for gas-selective sensors, such as water sensors in the presence of N_2, NO, NH_3, etc.

On the other hand, hydrogen will be readily captured by the Ti₃Sb surface, which is important for systems requiring selective H_2 capture. In other words, strong H_2 adsorption on the surface may indicate the potential of Ti₃Sb as a material for hydrogen storage (if desorption is possible under suitable conditions) or for water separation in membrane systems.

B. Relationship between adsorption energy and activation energy

Let us consider the relationship between the nitrogen adsorption energy and the activation energy of the surface of a cubic Ti₃Sb crystal. The adsorption and surface activation energies are related through the electron-structural changes in the crystal during adsorption. This demonstrates how nitrogen interacts with the surface of the Ti₃Sb crystal lattice.

It is known that adsorption energy E_{ads} is the energy released (or absorbed) when an atom or molecule (in our case, nitrogen) attaches to a surface. E_{ads} depends on the nature of the surface (coordination numbers, local electron density), the type of adsorbent (N atom, N_2 molecule), the presence of defects, doping, etc.

The activation energy E_a of a surface is the barrier for a certain reaction (e.g., dissociation of N_2, migration of atoms, or further doping). The stronger the nitrogen atom's bond to the surface (the higher the E_{ads}), the greater the contribution of its orbitals to the local electronic structure of the Ti₃Sb surface. This can alter (decrease or increase) E_a for the next step (reaction or nitrogen atom migration), depending on the nature of the bond (covalent, ionic, donor-acceptor).

For some simple surface reactions (especially on metals and semiconductors), there is a so-called linear Brønsted–Evans–Polanyi (BEP) relationship:

$$E_a = \alpha_1 \Delta E_1 + \beta_1 \qquad (4)$$

where ΔE_1 is the energy effect of the reaction (can be related to E_{ads}), α_1, β_1 are empirical constants for a given material and reaction.

In the case of nitrogen doping, if nitrogen is adsorbed with high energy and readily diffuses into the crystal, this can be considered a low activation energy for doping. For example, on the surface of cubic TiN or ZrN, where nitrogen is adsorbed with strong covalent bonds, a low energy barrier to nitrogen diffusion into the crystal bulk can be expected. On inert surfaces (e.g., oxides), weak nitrogen adsorption can correspond to a high energy barrier to N_2 dissociation.

Thus, there is a relationship between E_{ads} and E_a via the local electron structure and the BEP rules. However, this relationship is usually nonlinear and depends on the reaction context.

B. Alloying

Alloying and heat treatment are known to significantly improve the mechanical properties (e.g., antifriction) of titanium alloys. However, chemical-thermal nitriding can improve these properties [19–21].

Ti$_3$Sb 2×1×1 supercells were modeled by doping with N atoms, where N atoms individually replace Sb (Figure 2) and Ti (Figure 3) atoms.
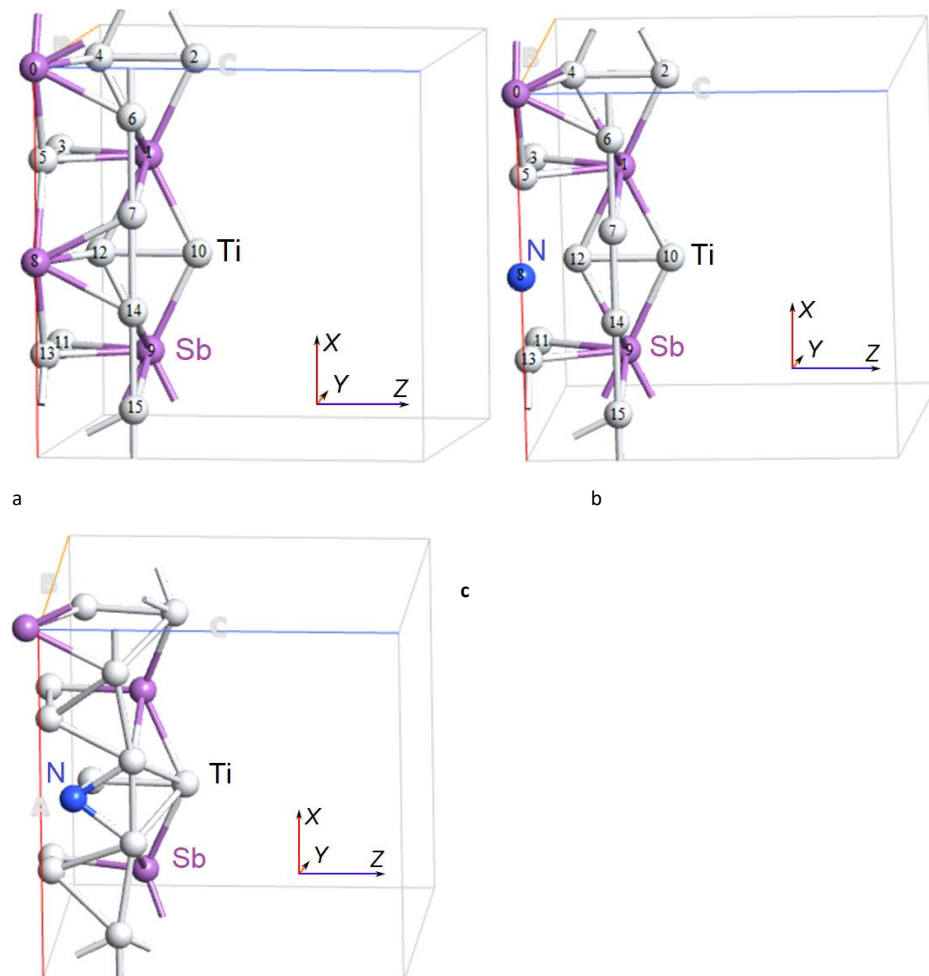

Figure 2. Atomic structure of the cubic Ti$_3$Sb supercell 2 × 2 × 1: a) supercell of pure Ti$_3$Sb; supercell of Ti$_3$Sb doped with N (Sb), b) before relaxation and c) after relaxation of the structure corresponding to the minimum energy of the Ti$_3$Sb–N lattice.
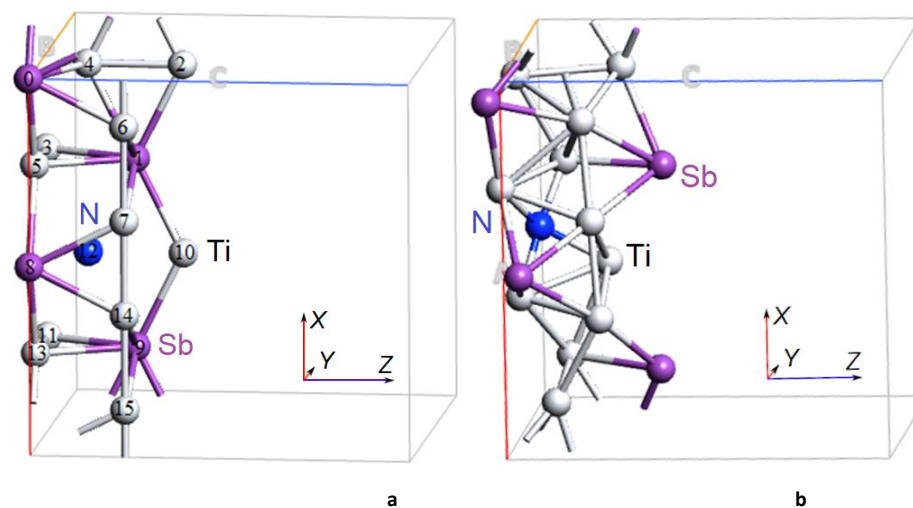
Figure 3. Atomic structure of the Ti₃Sb 2×2×1 supercell doped with N (Ti), a) before relaxation and b) after relaxation of the Ti₃Sb–N structure.

The cubic three-dimensional structure of Ti₃Sb A15 can be represented as a single Ti atom bonded to two other Ti atoms and four Sb atoms in a lattice. The Ti–Ti bond length is 2.61 Å, and the Ti–Sb bond length is 2.92 Å. In this lattice, a given Sb atom is bonded to twelve Ti atoms, forming SbTi₁₂ cuboctahedra that share edges and faces.

Figure 4 shows the Brillouin zone of the cubic Ti₃Sb structure, where the Γ–X–M–X plane corresponds to the k_z Fermi surface.
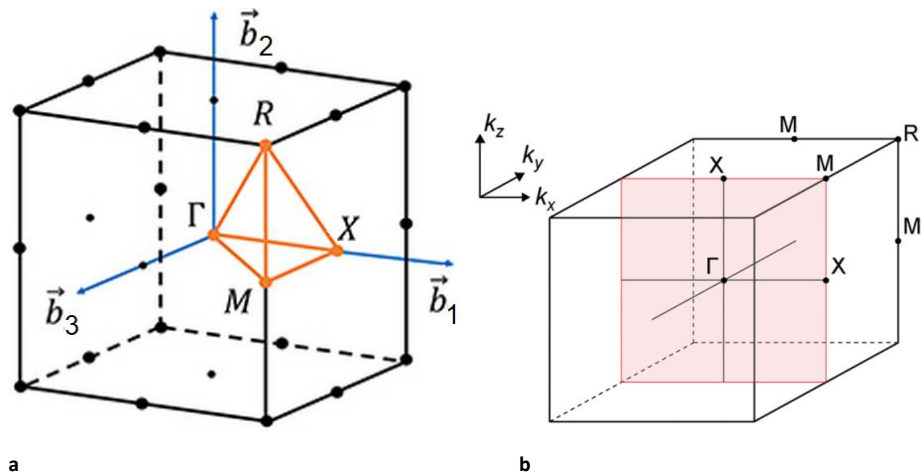

Figure 4. a) Brillouin zone of the cubic structure of Ti₃Sb with characteristic points, b) the Γ–X–M–X plane corresponds to the Fermi k_z surface.

Partial replacement of Ti or Sb atoms with nitrogen atoms at the Ti₃Sb crystal lattice sites alters the structural parameters (bond lengths, electronic properties). This may be due to differences in the oxidation states and ion sizes of the components of the Ti₃Sb–N system: Ti^{+3} (0.67 Å), Sb^{+3} (0.76 Å), and N^{+3} (0.16 Å). Thus, it has been established that partial nitrogen doping affects the interatomic distances between Ti and Sb atoms near the N atom in Ti₃Sb–N and the electronic structure (Table 2).

In the ordered crystal structure of the Ti₃Sb compound, Sb is a p-element (5 valence electrons), and Ti is a transition metal (4 valence electrons; $3d^2 4s^2$). In compounds, antimony can exhibit oxidation states of -3, +3, and +5, while Ti can exhibit oxidation states of +2, +3, and +4.

Consider doping the Ti₃Sb–N system with nitrogen N. Nitrogen has 5 valence electrons ($2s^2 2p^3$), like Sb, but the nitrogen atom is significantly smaller than the Sb atom. N has a higher electronegativity (~3.0 for N and ~2.05 for Sb). Therefore, the electron density of Ti₃Sb–N(doped) can change with partial substitution of N for Sb. In this case, N more strongly attracts electrons from Ti₃Sb, which can be considered as local electron depletion of the neighboring Sb (or Ti) atom. This nitriding can be considered as n-alloying in the Ti₃Sb crystal structure, where Ti donates electrons to the Sb atom.

As a result of partial replacement of Sb (or Ti) by nitrogen impurity N, the electron distribution in the band structure of Ti₃Sb changes. Compared to pure Ti₃Sb [26], local electron density bands appear in Ti₃Sb–N due to modification of the conduction band of Ti₃Sb (Figures 5 and 6).

Table 2. Change in atomic distances in N-doped structure based on 2×2×1 Ti₃Sb supercell.

Supercell 2×2×1 Ti₃Sb	Interatomic distance (Ti–Sb, Ti–Ti or Ti–N), Å		
	Ti–Sb	Ti–Ti	Ti–N

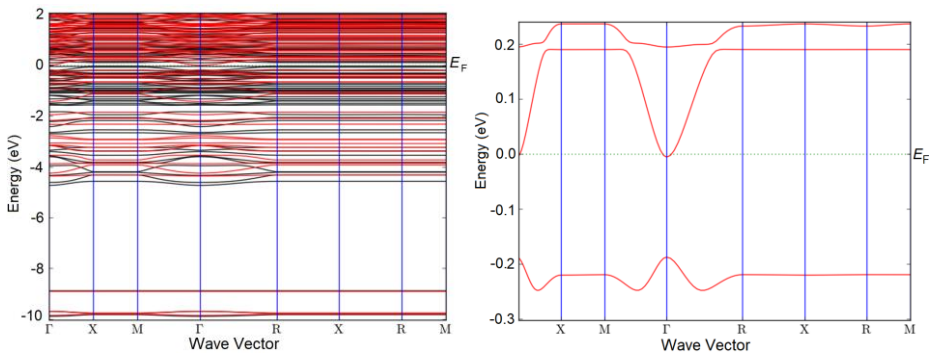| Pure Ti$_3$Sb	Ti$_7$–Sb$_8$ (2.917)	Ti$_7$–Ti$_{14}$ (2.609)	
Ti$_3$Sb–N(Sb)	Ti$_{14}$–Sb$_9$ (2.911) Ti$_{10}$–Sb$_9$ (2.971) Ti$_{12}$–Sb$_9$ (3.072)	Ti$_7$–Ti$_{14}$ (2.473) Ti$_{10}$-Ti$_{12}$ (2.757) Ti$_7$–Ti$_6$ (2.724)	Ti$_7$–N$_8$ (2.171) Ti$_{14}$–N$_8$ (2.171) Ti$_{12}$–N$_8$ (2.052)

Figure 5. Band structure of N-doped 2×2×1 Ti$_3$Sb supercell including the spin effect. a) N(Sb) and b) energy region near the Fermi level. Surface coverage θ = 0.25 ML.
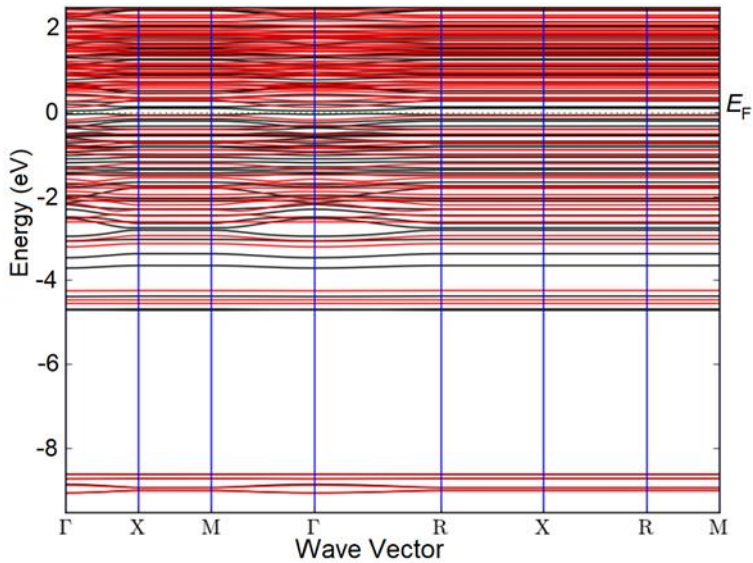

Figure 6. Band structure of N-doped 2×2×1 Ti$_3$Sb supercell including the spin effect. N partially replaces Ti in the lattice. Surface coverage θ = 0.25 ML.

C. Density of States

The effect of nitrogen doping on the electronic structure of Ti$_3$Sb is manifested in the density of states DOS spectra. The introduction of a nitrogen atom into the Ti$_3$Sb–N(doped) lattice alters the electronic structure of Ti$_3$Sb, leading to an increase in the binding energy difference between the Ti–N and Ti–Sb chemical bonds. Energetically, this manifests itself as a slight increase in the band gap E_g of the Ti$_3$Sb semimetal and a shift in the Fermi level (depending on the N dopant concentration) in the band structure. The partial DOS peaks of the Ti$_3$Sb–N(doped) supercells, associated with the p-orbitals of Sb atoms and/or d-orbitals of Ti, are replaced by the low-energy orbitals of the nitrogen impurity atoms (Figures 7, 8).
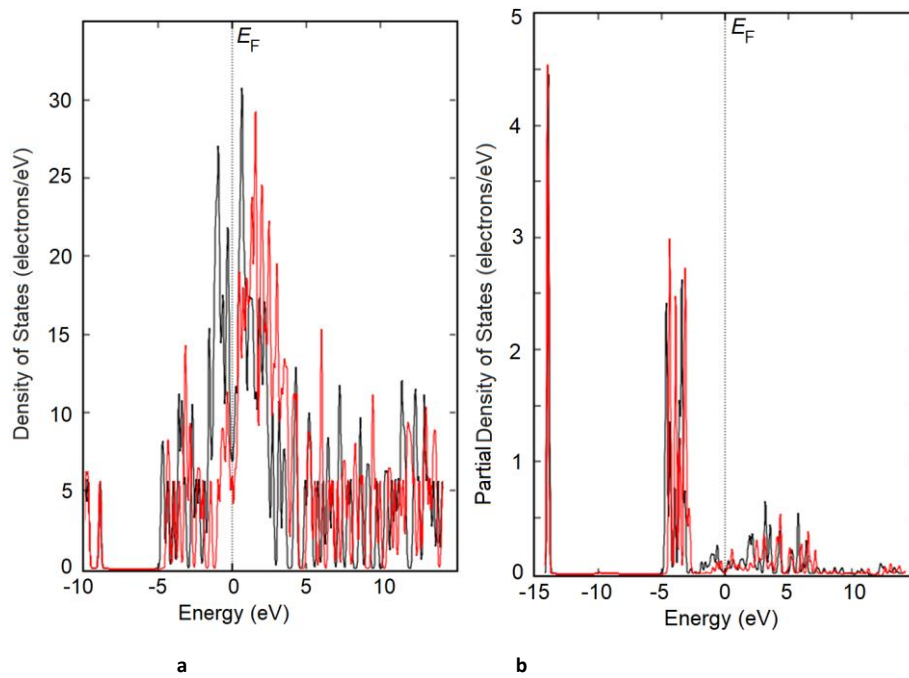
Figure 7. DOS (a) and partial PDOS (b) of a 2×2×1 Ti₃Sb supercell doped with nitrogen (N replaces Sb).

The Ti₃Sb–N DOS spectra along the Γ–X direction of the wave vector differ from each other, as can be seen in Figures 7 and 8. The Ti₃Sb–N DOS and PDOS spectra also differ from the PDOS spectra of the pure Ti₃Sb supercell [25]. The valence band contains Sb-[Kr]$4d^{10}5s^25p^3$ states, approximately 5 eV below the Fermi energy E_F. Furthermore, the Ti₃Sb–N DOS and PDOS peaks become intense near E_F at the Γ point (Figure 8). This may be due to the $3d$-t_{2g} states characteristic of Ti-[Ar]$3d^24s^2$ (Figure 9), occupied by electrons of the N-[He]$2s^22p^3$ dopant.
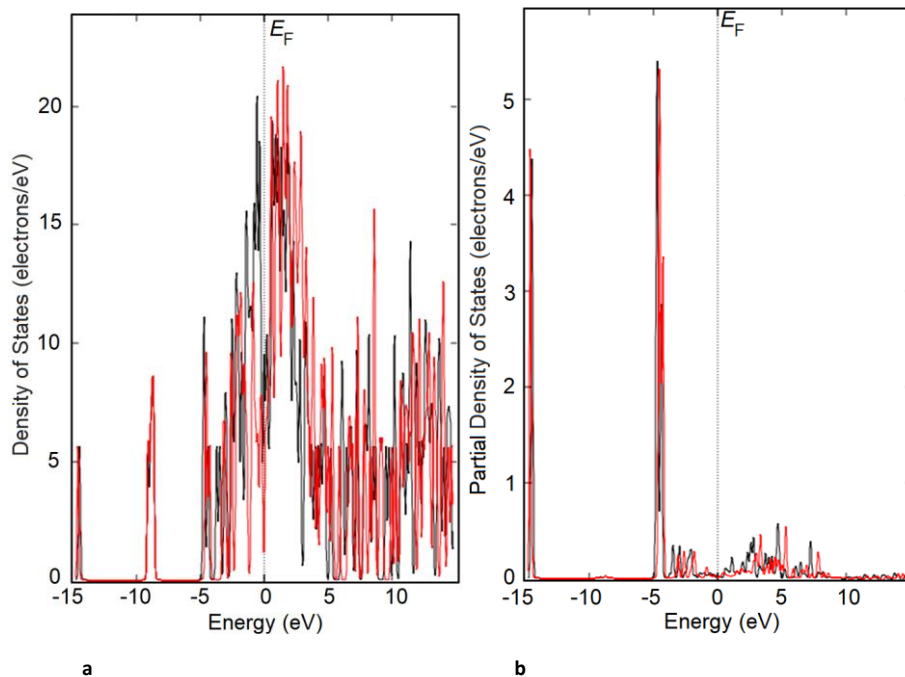

Figure 8. DOS (a) and partial PDOS (b) of a 2×2×1 Ti₃Sb supercell doped with nitrogen (N replaces Ti).
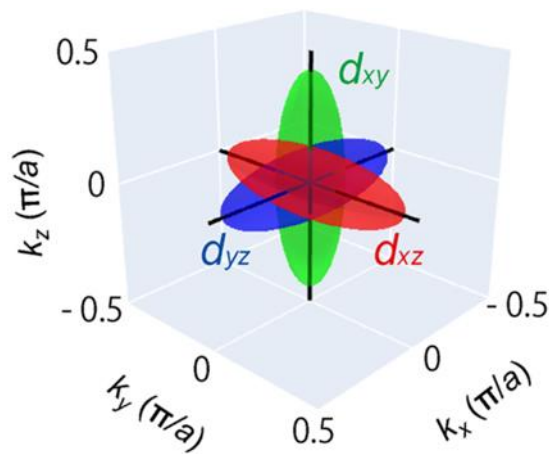
Figure 9. The location of the initial t$_{2g}$ orbital of Ti $3d$ along the x, y, z directions, where k_x, y and k_z are the wave vectors along the x, y and z directions, respectively.

D. Surface anisotropy

Surface anisotropy in cubic crystals arises from differences in the atomic structure and electronic properties of the various crystallographic faces (e.g., (100), (110), (111), even if the crystal has high symmetry in the bulk.

In general, electron anisotropy in crystals with a cubic structure can arise due to:

- anisotropy of the electron effective mass (near band minima);

- the crystal potential, which, although symmetrical on average, can lead to a directional dependence of properties (for example, due to the band structure);

- spin-orbit interaction;

- crystal deformations (mechanical stress);

- the presence of impurities or defects that break symmetry.

Cubic structures (FCC, BCC, SC, DC, NaCl, TiN, etc.) have high volumetric symmetry. Different faces have different numbers of neighbors, angular bonds, packing density, etc. As soon as the crystal is destroyed and a surface is created, the symmetry of the bulk crystal is broken. In other words, the formation of a surface disrupts the symmetry of the crystal.

As an example, let's consider the FCC structure. The (111) surface direction is the region with the highest packing density, is stable, and has a low γ_{sur} (100) is a finer packing, with more uncanceled bonds → higher γ_{sur} (110) has even more bond breaks → higher γ_{sur}. These differences lead to different surface energies γ_{sur}. This is called surface energy anisotropy.

After the surface is formed, the atoms relax, changing the interatomic distances and local electron density. The (111) face can relax differently than the (100) face; this is called electron anisotropy. In metallic systems (e.g., FCC Ni, Cu), anisotropy is formed due to d-electrons, which are distributed differently on different faces. In ionic crystals (e.g., NaCl, TiN), anisotropy is formed due to the uneven distribution of ions on different garnets. In covalent crystals (e.g., C, Si, Ge, Sb), anisotropy is formed due to the different topologies of chemical bonds (for (111) and (100)).

The higher the atomic density at the boundary (Miller indices and packing density), the higher the protection of the surface atoms and the lower the surface energy of the crystal, i.e., the more stable the facet. The general dependence of surface energy on facet and packing density for the FCC cubic structure is presented in Table 3.

Table 3. Dependence of surface energy on facet and packing density for the fcc cubic structure.

Facet	Packing Density (FCC)	Surface Energy
(111)	Maximum	Low
(100)	Medium	High

(110)	Minimum	Highest

Thus, surface anisotropy is the difference in surface energies of different planes:

$$E_a = \alpha_1 \Delta E_1 + \beta_1 \qquad (5)$$

The value of γ can be calculated using the DFT method for each plane of the supercell:

$$\gamma = \frac{1}{2A}(E_{slab} - N \cdot E_{bulk}) \qquad (6)$$

Although cubic symmetry theoretically implies isotropy, real crystals exhibit anisotropic behavior due to:

- differences in the effective mass of electrons along different directions;

- electron bands, which can have an ellipsoidal shape (for example, in silicon, the conduction bands have six ellipsoids along the [100] axes);

- spin-orbit splitting, especially in heavy elements.

Conclusion. Surface anisotropy of cubic crystals is due to differences in geometry (atomic density, bond cleavages), electronic properties (local density of states, relaxation), and crystallography (face indices).

Let's consider the DOS taking into account crystallographic directions, for example, in a cubic crystal. DOS is a scalar quantity that depends on energy but not direction. However, the anisotropy of the band structure means that the contribution to DOS from different crystallographic directions can differ.

That is, the DOS itself does not explicitly depend on direction, but the group velocity, dispersion $E(\vec{k})$, and other crystal characteristics can be significantly directional. In the isotropic case (e.g., free electrons) $DOS(E)$ is independent of direction. In a crystal, due to the complex shape of the bands, the bands can be denser in states in certain directions. For example, if the dispersion in [111] is flatter than in [100], then there are more states at the same energy.

The influence of cubic crystal directions manifests itself in the following cases: Partial density of states (PDOS) – if we consider the contribution from specific atomic directions (orbitals). Fermi surface orientation – different directions produce different surface cross-sections, which influence the electron density. Anisotropy of transport properties – for example, thermoelectric properties or thermal conductivity of the crystal.

Thus, electron anisotropy arises from differences in the dispersion of $E(\vec{k})$ despite cubic symmetry; this is determined experimentally or through band calculations. The DOS is generally a scalar, but the band shape and dispersion anisotropy contribute to the DOS, making it directionally dependent. This manifests itself in the transport properties and DOS spectra.

There is no universal formula for the DOS for anisotropic electrons. For this, we will use the theory and the effective mass tensor. The DOS for the isotropic case of free electrons with parabolic dispersion is

$$E(\vec{k}) = \frac{\hbar^2 k^2}{2m^*} \qquad (7)$$

Then in three dimensions for the kinetic energy density of an electron we can write:

$$g(E) = \frac{1}{V}\frac{dN}{dE} = \frac{1}{2\pi^2}\left(\frac{2m^*}{\hbar^2}\right)^{3/2}\sqrt{E - E_0} \qquad (8)$$

where E_0 is the bottom of the zone or the level relative to which the energy is calculated. This expression assumes that the effective mass m^* is the same in all directions.

The DOS for the anisotropic case will include the anisotropic effective mass and the mass tensor. If the dispersion is anisotropic, then for small deviations from the zone minima:

$$E(\vec{k}) = E_0 + \frac{\hbar^2}{2}\sum_{ij}(k_i - k_{0,i})\left(\frac{1}{m^*}\right)_{ij}(k_j - k_{0,j}) \qquad (9)$$

where $\left(\frac{1}{m^*}\right)_{ij}$ are the components of the inverse effective mass tensor.

If the system allows the selection of principal axes, the mass tensor becomes diagonal:

$$E = E_0 + \frac{\hbar^2}{2}\left(\frac{(k_x - k_{0,x})^2}{m_x^*} + \frac{(k_y - k_{0,y})^2}{m_y^*} + \frac{(k_z - k_{0,z})^2}{m_z^*}\right) \qquad (10)$$

where $m_x^*,\ m_y^*, m_z^*$ are the effective masses along the principal directions.

In a cubic crystal, with complete symmetry, $m_x^* = m_y^* = m_z^*$ should be true. However, due to the peculiarities of the zone, there may be cases where different directions of the crystal are poorly approximated by a single mass.

Therefore, let's consider the DOS for the anisotropic case in terms of the mass tensor. For the case with a diagonal mass tensor, the DOS expression is:

$$g(E) = \frac{1}{(2\pi)^3} \int_{S(E)} \frac{dS}{\|\nabla(\vec{k})_E (\vec{k})\|} \tag{11}$$

where the integration is over the surface of constant energy E.

Substituting the parabolic anisotropic form into this expression, we obtain:

$$g(E) = \frac{1}{(2\pi)^3} \int_{S(E)} \frac{dS}{\|\nabla(\vec{k})_E (\vec{k})\|} \tag{12}$$

After transformations, the final result for small deviations is obtained in the form:

$$g(E) = \frac{1}{2\pi^2} \left(\frac{2}{\hbar^2}\right)^{3/2} \sqrt{(E - E_0)} \left(m_x^* m_y^* m_z^*\right)^{1/2} \tag{13}$$

or:

$$g(E) = \frac{1}{2\pi^2} \left(\frac{2}{\hbar^2}\right)^{3/2} \sqrt{(E - E_0)} \cdot \sqrt{m_x^* m_y^* m_z^*} \tag{14}$$

That is, the effective DOS mass in the anisotropic case is the geometric mean of the masses in three directions in the crystal:

$$m_{\text{DOS}}^* = \left(m_x^* m_y^* m_z^*\right)^{1/3} \tag{15}$$

Taking this into account, the DOS expression in the anisotropic case can be written similarly to the isotropic case, but with the contribution of m_{DOS}^*.

Notes and limitations. This formula is valid only near the band minimum, when the dispersion can be considered parabolic in three directions of the crystal. If the dispersion is significantly non-parabolic, or if the bands are significantly curved, then exact integration over the surface $E(\vec{k})$=const or numerical methods (e.g., DFT, special packages for DOS calculations) should be used.

The DOS spectra of Ti$_3$Sb–N along the Γ–X direction of the wave vector differ from each other, as can be seen from Figures 7 and 8. They also differ from the DOS spectra of the pure Ti$_3$Sb supercell [25]. In addition to the Sb 5p valence bands located approximately 5 eV below the Fermi energy E_{F}, the intensity of the peaks near E_{F} at the Γ point (Figure 9) can be due to the 3d-t$_{2g}$ states (Figure 10) characteristic of Ti, occupied by the electrons of the N dopant.

The anisotropic dispersion of the electron pocket bands t$_{2g}$ of cubic crystals containing titanium [29] can be expressed in terms of the effective mass model:

$$E(k_x, k_y, k_z) = \frac{\hbar^2}{2m_1}\left(k_x^2 + k_y^2\right) + \frac{\hbar^2}{2m_2} k_z^2, \tag{16}$$

where $\hbar$ is the reduced Planck constant.

Taking this into account, as well as the sixfold degeneracy of the t$_{2g}$ bands due to spin and orbital degrees of freedom, the electron carrier density for occupied states in Ti$_3$Sb–N can be estimated as:

$$n = \frac{1}{(2\pi)^3} \int_{E<\varepsilon_F} E(k_x, k_y, k_z)dk = \frac{2^{\frac{3}{2}}}{18\pi^2} \frac{\sqrt{m_1^2 m_2}}{\hbar^3} \varepsilon_F. \tag{17}$$

The stability of the obtained Ti$_3$Sb–N structures with partial substitution of Ti3Sb components with nitrogen was estimated by calculating the formation energy:

$$E_{\text{f}} = E_{\text{doped}} - E_{\text{pure}} - n\left(\mu_{\text{dopants}} - \mu_{\text{Ti;Sb}}\right), \tag{18}$$

where E_{f} is the formation energy, E_{doped} and E_{pure} are the total energies of nitrogen-doped Ti$_3$Sb and pure Ti$_3$Sb, respectively; μ_{dopants} $\mu_{\text{Ti;Sb}}$ are the chemical potentials of the dopant nitrogen and the Ti and/or Sb components, respectively; n is the number of Ti or Sb atoms replaced by the dopant nitrogen atom.

The calculations assume that the dopant nitrogen atoms replace Ti or Sb atoms. The ratio of the chemical potential [30] is defined as $\mu\text{Ti}_3\text{Sb} = 3\mu\text{Ti} + \mu\text{Sb}$. Calculation results showed that partial replacement of Ti or Sb in the Ti$_3$Sb lattice with nitrogen impurity atoms leads to a negative formation energy for Ti$_3$Sb–N structures. On average, E_{f} = -0.32 eV for these structures. This indicates favorable incorporation of nitrogen impurity atoms into the Ti$_3$Sb crystal lattice. DFT LSDA calculated E_{f} of pure Ti$_3$Sb is E_{f} = -0.38 eV/atom [25].

The calculated energy levels remain nearly identical for both spin-up and spin-down states in the density-of-state spectra of Ti_3Sb–N (Figures 8, 9). That is, these energies for both spin orientations differ little from each other in Ti_3Sb–N. The band gap for Ti_3Sb–N, calculated based on highly symmetric k-points, is 0.009 eV. A local magnetic moment was detected in Ti_3Sb–N using the Mulliken method (Table 4).

Table 4. DFT GGAS calculated values of the magnetic moment and total energy of N-doped 2×1×1 Ti_3Sb supercells with N/Sb and N/Ti substitution sites.

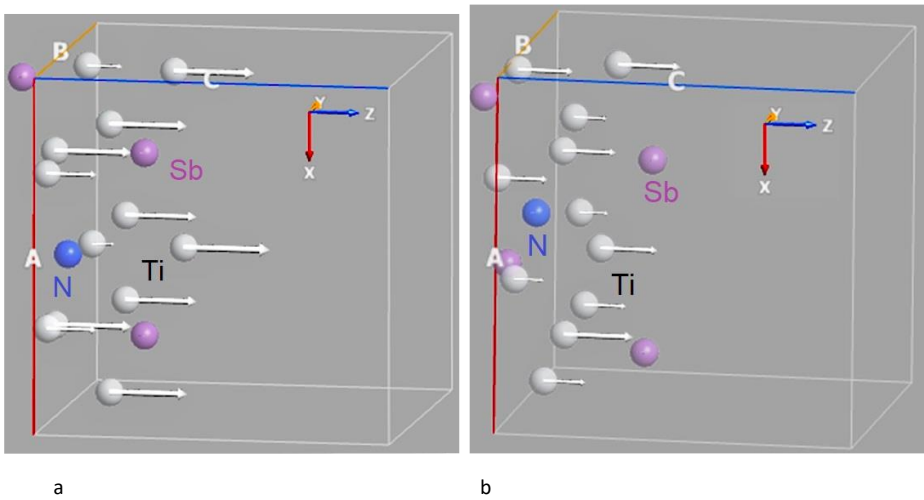| 2×2×1 supercell	M_{tot}, μ_B	E_{tot}, eV
Ti_3Sb	0.08	-1390
$Ti_3Sb_{0.9412}N_{0.0588}$	2.07	-2870
$Ti_{2.9412}SbN_{0.0588}$	2.21	-2847

a   b

Figure 10. Direction of the magnetic moment in a 2×2×1 Ti_3Sb supercell doped with nitrogen: a) N replaces Ti, b) N replaces Sb.

Both nitrogen adsorption on the surface and the incorporation of the nitrogen atom into the lattice of the cubic Ti_3Sb A15 crystal can also depend on the anisotropy and crystallographic orientation of the structural planes. These data can be used to specifically control the electronic, mechanical, and catalytic properties of Ti_3Sb-based materials. These findings are important for the development of new nitrogen-containing functional materials that are resistant to oxidation and suitable for applications such as electronics, catalysis, and sensors.

5. Conclusions

Supercell models of cubic Ti_3Sb crystals containing atomic nitrogen were created, taking into account the effects of coating, various surface orientations (111), (100), and (110), as well as the activation energy of the Ti_3Sb surface. The adsorption properties of nitrogen, as well as the partial substitution of Ti and Sb atoms by an impurity of atomic nitrogen, were calculated using the DFT GGAS PBE method taking into account the spin polarization for different parts of the Ti_3Sb surface (top – T, bridge – B, hollow – H).

1. It was shown that low coverage (e.g., $\theta(N)$ = 1/9 ML in a 3 × 3 Ti_3Sb(111)–N(ads) supercell) minimizes the interaction between adsorbed nitrogen atoms. This allows us to determine the energy for a single adsorbed N(ads) atom near a given position in the Ti_3Sb–N supercell.

2. Calculations show that the dependence of the adsorption energy on coverage has a minimum, which corresponds to the optimal nitrogen coverage on Ti_3Sb. The adsorption energy of atomic

nitrogen differs significantly from the adsorption energy of atomic hydrogen on similar 2 x 2 Ti$_3$Sb(110)–H supercells with a coating thickness of θ = 0.25 ML.

3. The activation energies of nitrogen adsorption differ for different faces: Ti$_3$Sb(111), Ti$_3$Sb(110), and Ti$_3$Sb(100). The most stable nitrogen adsorption configuration is the (111) face on Ti$_3$Sb, with an adsorption energy of –3.11 eV (nitrogen adsorption in the octahedral interstitial site in Ti$_3$Sb with an average N–Ti distance of 2.111 Å). The adsorption energies of nitrogen on Ti$_3$Sb(100) are lower than on Ti$_3$Sb(110), at –0.87 and –0.15 eV, respectively.

4. The energetically favorable adsorption trajectory for atomic N is the hollow site adsorption form located near two adjacent Ti$_3$Sb atoms.

5. It was established that, like the behavior of the nitrogen adatom on the surface, the effect of the admixture of atomic nitrogen in the bulk of the Ti$_3$Sb lattice depends on the crystallographic directions, which is associated with the anisotropy of the local atomic environment of Ti$_3$Sb–N. Partial substitution of Sb and/or Ti by nitrogen in their various positions in the Ti$_3$Sb structure leads to a change in the band structure and local magnetic moment in Ti$_3$Sb–N.

6. The calculated band gap, based on highly symmetric k-points, is 0.009 eV for Ti$_3$Sb–N. A change in the electron density distribution creates local magnetic states in Ti$_3$Sb when it is doped with atomic nitrogen. The partial magnetic moment with partial substitution of Ti sites by atomic nitrogen in Ti$_3$Sb–N was 2.21 μ_B. The partial magnetic moment with partial substitution of Sb sites by nitrogen was lower than with Ti substitution and was 2.07 μ_B.

Thus, the new data obtained on the electron density of states DOS and adsorption energy for Ti$_3$Sb–N play a key role in understanding the functions of Ti$_3$Sb–N and serve as the basis for its applied evaluation in sensors, catalysis, and energy. Furthermore, they are important for predicting the surface behavior and bulk properties of Ti$_3$Sb under real-world conditions and serve as a basis for the development of new, more effective adsorbents and doped systems.

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Conflicts of Interest: The authors declare no conflicts of interest.

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