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Article

Can Uncertainty Metrics Guide Search? Evaluating Search-Time Decision-Making in Large Language Models

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Abstract: Sampling-based search methods for Large Language Models (LLMs), such as Chain of Thought (CoT) and Tree of Thought (ToT), improve accuracy by exploring multiple reasoning paths. These approaches can be enhanced by search algorithms like Monte Carlo Tree Search (MCTS) and Bandit strategies, which rely on effective uncertainty estimation. While many uncertainty metrics have been proposed for LLMs, we argue that most of them are primarily *descriptive*, as they capture model confidence rather than *prescriptive* tools for guiding search toward correct answers. In this study, we evaluate whether existing uncertainty metrics can support search-time decision-making through two diagnostic tasks: *Answer Selection* and *Answer Refinement*. Our results show that while current metrics help flag risky or error-prone responses, they fall short in guiding search toward correctness. This highlights the need for optimization-aware uncertainty metrics explicitly designed to support correctness-driven decisions. Code is available at https://anonymous.4open.science/r/llm-uncertainty-search-D185.

Keywords: langauge model; uncertainty

1. Introduction

Sampling-based search methods for large language models (LLMs) involve generating multiple responses, either in parallel, sequentially, or through hybrid approaches, and aggregating them into a final answer. Techniques such as Chain-of-Thought (CoT) [34], Tree-of-Thoughts (ToT) [39], and ReAct [40] have demonstrated that structured reasoning through intermediate steps can significantly enhance LLM performance. These approaches can be further extended with search algorithms, including Monte Carlo Tree Search (e.g., LATS, STaR) [42,43], bandit-based methods (e.g., LongPO) [7], and gradient-based optimization (e.g., OPRO) [38].

A crucial component in these search and optimization strategies is *uncertainty estimation*, which is vital for guiding decisions, balancing exploration and exploitation. Uncertainty estimation techniques, such as those used in Bandit algorithms or Bayesian optimization, can dynamically adjust learning rates or hyperparameters. In combinatorial optimization (e.g., genetic algorithms), uncertainty estimation informs heuristic decisions like mutation rates or temperature adjustments. Thus, developing robust methods for quantifying uncertainty in LLMs is essential for enabling more effective search behavior.

Prior work on LLM uncertainty estimation has primarily focused on methods based on generation likelihoods [1,12,18], verbalized confidence [11,15], and response consistency [9,37]. These methods have shown utility for tasks like hallucination detection and risk assessment. However, we argue that these metrics primarily serve a *descriptive role*: they reflect the model's confidence in a given query but are not designed to guide or influence the generation process. For example, a model uncertainty score of 0.8 indicates a 20% estimated error rate when sampling multiple responses to a query, but it does not help determine which of those candidate responses is correct or should be preferred.

In contrast, search-based tasks demand a more *prescriptive role* from uncertainty estimators: rather than passively measuring confidence, they must actively guide decision-making during search. For

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instance, in multi-step generation or tree-based reasoning, uncertainty scores should inform which candidate answers to select, which nodes to expand, and which paths to prune or refine. An effective prescriptive estimator should provide fine-grained, local feedback that incrementally reduces error. Without this capability, even a well-calibrated estimator can lead to misleading decisions during search.

In this study, we evaluate whether existing LLM uncertainty metrics can fulfill a prescriptive role in search-based tasks by introducing two diagnostic tasks: (1) *Answer Selection*—choosing the best answer from a set of candidates; and (2) *Answer Refinement*—identifying which response most needs refinement. Our empirical results show that while current uncertainty metrics are useful for flagging risky or error-prone responses, they struggle to reliably guide search toward correctness. This highlights the need for optimization-aware uncertainty metrics explicitly designed to support decision-making in correctness-driven search.

2. Diagnostic Tests

Search-based methods for LLMs typically involve generating multiple candidate responses—either in parallel, sequentially, or both—and then aggregating them into a final answer. Within this process, two fundamental actions frequently occur: *selection* and *refinement*. *Selection* refers to choosing which candidate responses to explore, exploit, or use in final aggregation—usually in a parallel setting. *Refinement*, often used in sequential settings, involves generating follow-up outputs based on earlier responses, such as self-reflection [20], verification [35], or correction [19]. Based on these two fundamental actions, we design two diagnostic tests to evaluate whether existing uncertainty metrics can meaningfully guide the search process. These tests aim to answer the question: *Can uncertainty metrics be reliably linked to correctness in a way that makes them useful for decision-making?*

Test 1: Answer Selection

This test examines whether an uncertainty metric can help select the best answer among candidates. For each question, the LLM generates multiple responses. Responses that yield the same answer (regardless of surface form) are grouped into answer clusters. The uncertainty metric ranks these answer groups, under the assumption that correct answers should appear less uncertain (i.e., the lowest uncertainty score group is selected as the final answer). We measure how well the metric prioritizes correctness using three evaluation criteria: PAIRWISE-WIN-RATE (prefer correct answers over an incorrect ones), TOP-1 ACCURACY (whether the top-ranked candidate is correct), and MEAN-RECIPROCAL-RANK (how high correct answers appear on average).

Test 2: Answer Refinement

This test examines whether uncertainty metrics can identify which answers are most in need of refinement. For each question, the LLM first generates a set of initial answers. Refinement is then applied only to the answer cluster exhibiting the highest uncertainty score. A high uncertainty metric value suggests that an answer is more likely to be incorrect and thus a better candidate for refinement. We evaluate each metric by measuring the overall accuracy gain achieved through this targeted refinement.

Insights and Applications

The two tests highlight distinct roles for uncertainty metrics in search-based tasks. Test 1 assesses how well a metric ranks candidate answers by correctness—useful for reranking and aggregation. Test 2 evaluates the ability to prioritize answers for refinement, which is crucial in compute-limited settings like interactive systems. Together, these tests reveal how uncertainty metrics can guide specific search actions and inform their use in real-world applications.

3. Experiments

In this section, we introduce the uncertainty metrics, datasets, models, and baseline methods used in our two diagnostic experiments. Additional implementation details and prompt templates are provided in Appendix A and C.

Benchmarked Metrics

We benchmark six task-agnostic uncertainty metrics that don't require additional model training. Generation-liklihood based metrics estimate uncertainty from the predictive entropy of model's output distribution: NORMALIZED PREDICTIVE ENTROPY (NPE), LENGTH-NORMALIZED PREDICTIVE ENTROPY (LNPE) [18], and SEMANTIC ENTROPY (SE) [12]. Verbalized-based measures assess confidence by directly prompting the model to express its certainty: VERBALIZED CONFIDENCE (VC) and P(TRUE) [11]. Lexical-based metrics: LEXICAL SIMILARITY [16], evaluate uncertainty based on the consistency of lexical overlap between multiple responses. Since P(TRUE), and VC are originally formulated to express model confidence, we transform them into uncertainty measures by taking their complements: PTRUE-COMP (1-P(TRUE)), and VC-NEG (negative of VC).

Datasets and Models

We select four diverse datasets: MATH (mathematical reasoning) [6], COMMONSENSEQA (commonsense reasoning) [21], TRIVIAQA (reading comprehension) [10], and TRUTHFULQA (truthfulness) [14]. MATH and TRIVIAQA feature open-ended (free-form) answers, while COMMONSENSEQA and TRUTHFULQA use multiple-choice formats. These datasets are evaluated using three open-source language models [3,8,22] of similar sizes: LLAMA-3-8B, GEMMA-2-9B, and MISTRAL-7B-V0.3. This setup ensures diversity across task types and model architectures, enhancing the robustness of our evaluation.

Baselines

In Answer Selection test, we compare Uncertainty-Guided Selection with (1) Random Selection, where a candidate is chosen uniformly at random, and (2) Majority Voting, which selects the most frequent answer as a strong self-consistency baseline [33]. In Answer Refinement test, we test whether Uncertainty-Guided Refinement outperforms (1) refining a random answer (Random Refinement), (2) refining the majority answer (Majority Refinement), and (3) refining all answers (All Refinement). For both tests, random baselines are calculated by averaging the scores over 50 runs of sampling to estimate the expected performance when randomly selecting a choice.

4. Result and Analysis

Uncertainty Metrics Fall Short in Answer Selection

As shown in Figure 1, *Uncertainty-Guided Selection* generally outperforms *Random Selection* but underperforms compared to *Majority Voting*. This indicates the limited applicability of uncertainty metrics in answer selection, as *Majority Voting*, being computation-free, still outperforms uncertainty-guided methods.

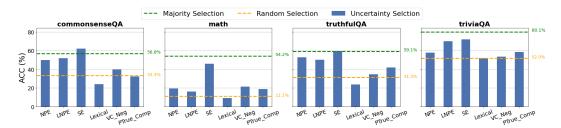


Figure 1. Diagnostic Test 1: Answer Selection Each bar plot shows the *Top-1 Accuracy* of *Uncertainty-Guided Selection* on six uncertainty metrics. Results show that uncertainty-guided selection generally underperforms majority vote (green) but better than random selection (yellow). Each value in figure is averaged across models.

To dive deeper, we provide a breakdown of TOP-1 ACCURACY (ACC), PAIRWISE WIN RATE (PWR), and MEAN RECIPROCAL RANK (MRR) for each uncertainty metric in Table 1. Likelihood-based metrics (NPE, LNPE, SE) typically achieve PWR and MRR above 0.6, indicating that they rank correct answers higher, though they don't always place the correct answer at the top. In contrast,

lexical- and verbalization-based metrics (LEXICAL, VC-NEG, PTRUE-COMP) perform poorly, with values often below 0.5. Notably, all metrics struggle with the MATH dataset, likely due to its complex reasoning demands and open-ended answer format, which makes it difficult for existing metrics to provide reliable signals.

Table 1. Uncertainty-Guided Selection Performance. Table present three metrics to evaluate method performance: *Top-1 Accuracy (ACC)*, the proportion of times the top-ranked answer is correct; *Pairwise Win Rate (PWR)*, the fraction of pairwise comparisons where the correct answer is ranked higher; and *Mean Reciprocal Rank (MRR)*, which reflects how early the correct answer appears in the ranked list. Each value in table is averaged across models.

Metric	COMMONSENSEQA			MATH			TruthfulQA			TRIVIAQA		
	ACC	PWR	MRR	ACC	PWR	MRR	ACC	PWR	MRR	ACC	PWR	MRR
NPE	0.500	0.604	0.723	0.197	0.615	0.391	0.529	0.660	0.726	0.578	0.526	0.744
LNPE	0.518	0.615	0.728	0.162	0.572	0.361	0.502	0.640	0.718	0.699	0.570	0.799
SE	0.622	0.706	0.789	0.460	0.729	0.597	0.595	0.707	0.765	0.719	0.562	0.827
Lexical	0.240	0.343	0.575	0.092	0.189	0.240	0.239	0.327	0.549	0.517	0.375	0.691
VC_Neg	0.401	0.481	0.668	0.216	0.309	0.387	0.347	0.432	0.630	0.535	0.419	0.717
PTrue_Comp	0.325	0.423	0.625	0.189	0.557	0.371	0.420	0.557	0.674	0.586	0.533	0.745

Uncertainty Metrics show potential to guide Answer Refinement.

As illustrated in Figure 2, *Uncertainty-Guided Refinement* leads to notable accuracy gains on COMMONSENSEQA and TRUTHFULQA, achieving performance close to *Majority Refinement* but using fewer refinement attempts. On MATH and TRIVIAQA, where accuracy gains of *All Refinement* are negative, *Uncertainty-Guided Refinement* surprisingly shows a slightly positive values, likely due to refining fewer answers and reducing unnecessary corrections.



Figure 2. Diagnostic Test 2. Answer Refinement Each bar plot shows the accuracy gain after *Uncertainty-Guided Refinement* on six uncertainty metrics. Results show that uncertainty-guided refinement leads to notable accuracy improvements with fewer attempts and even when baselines are showing negative gains. Each value in figure is averaged across models.

To analyze the refinement effect, we quantize answer candidates into four bins based on their uncertainty metric values and measure the accuracy gain achieved by refining answers in each bin. As shown in Figure 3, refining answers in the higher-uncertainty bins generally leads to larger accuracy gains—consistent with the intuition that uncertain responses are more likely to be incorrect and therefore benefit from refinement. However, we also observe positive gains from refining answers in the lowest-uncertainty bin, suggesting potential mismatch between model confidence and correctness.

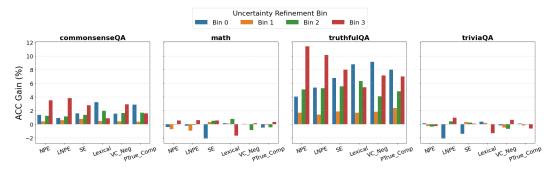


Figure 3. Uncertainty-Guided Refinement by Quantile Bins. Each bar plot shows the accuracy gain across uncertainty quantile bins. Higher-uncertainty bins tend to yield greater gains—consistent with the intuition that uncertain responses are more likely to be incorrect and therefore benefit from refinement. Refining the lowest-uncertainty bin can sometimes surprisingly result in positive gains. Each value in figure is averaged across models.

Descriptive vs. Prescriptive

From the previous analysis, we observe that current uncertainty metrics show potential in guiding answer refinement but struggle in answer selection. We argue this is because these metrics are designed for a *descriptive role*—capturing the model's confidence among outputs—rather than serving a *prescriptive role*, where uncertainty directly informs decisions during search. Additional figures in Appendix B highlight the descriptive power of these metrics.

The difference between descriptive and prescriptive roles helps explain why *Uncertainty-Guided Refinement* performs better than *Uncertainty-Guided Selection*. Refinement uses uncertainty metrics to identify low-confidence answers that are worth improving, which is a task that aligns with the descriptive strengths of the metrics. In contrast, selection assumes a mapping between confidence and correctness. This requires the model not only to recognize its uncertainty but also to correctly assess which answers are accurate.

5. Conclusions

In this study, we use two diagnostic tests to investigate the ability of LLM uncertainty metrics to guide search tasks. While these metrics are effective at identifying risky responses, they primarily capture model confidence and fall short in guiding toward correct answers. Our findings highlight the critical challenge of bridging the gap between model confidence and correctness, emphasizing the need for uncertainty metrics designed to support correctness-oriented decisions in search tasks.

Limitations

Due to computational constraints, we evaluate on a sampled subset of benchmark datasets. While bootstrapping is employed to reduce sampling bias, our findings may still be influenced by the limited scale. Additionally, our analysis focuses on a representative, but non-exhaustive, set of existing uncertainty metrics, meaning it may not capture all emerging approaches or domain-specific adaptations. Finally, our experiments are conducted using a fixed prompting and sampling strategy, so results may vary under different decoding settings or model configurations.

Use of AI Assistants

ChatGPT was utilized to refine paper writing. The authors paid careful attention to ensuring that AI generated content is accurate and aligned with the author's intentions.

Appendix A. Implementation Details

Due to computational constraints, we randomly sample 150 questions from each dataset. To ensure robustness and statistical significance, we apply bootstrapping with 500 resamples across all experiments. For benchmarked metric calculation, we use: 32 samples for NPE, LNPE, and SE; 3

samples for VC-NEG and PTRUE-COMP. For SE, we use JINAAI/JINA-EMBEDDINGS-V3 as embedding model to cluster semantic group. All experiments are conducted using a single NVIDIA GeForce RTX 3090 GPU. We use the vLLM engine for efficient inference and encoding text into vector.

Appendix B. Additional Results

To examine the descriptive power of uncertainty metrics, we assess their ability to predict hallucinations in model responses. We generate 32 responses per question, labeling those with accuracy below 70% as *uncertain* (positive class). This allows us to evaluate how well each estimator identifies low-confidence or error-prone questions driven by specific uncertainty factors.

Figures A1 and A2 report the AUROC for identifying error-prone queries and the rank correlation between uncertainty metric values and response correctness. These figures highlight the strong descriptive power of the metrics in identifying when the model is uncertain.

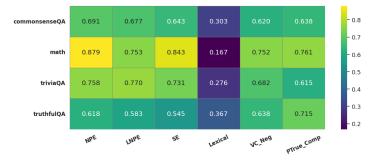


Figure A1. AUROC of uncertainty metrics across datasets. A higher value indicates that the uncertainty metric effectively distinguishes between error-prone and non-error-prone questions, capturing signals associated with potential hallucinations or inaccuracies.

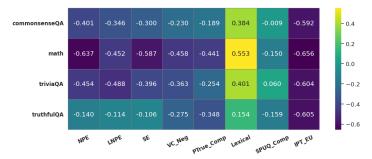


Figure A2. Rank correlation between uncertainty scores and response accuracy. Lower values (high uncertainty low correctness) indicate a stronger alignment between uncertainty estimates and actual correctness.

Appendix C. Prompt Templates

Please answer the following question. Think carefully and in a step-by-step fashion.

At the end of your solution, indicate your final answer by writing the answer choice (A, B, C, D, or E) inside a boxed environment, like:

Q: {q}
Choices: {c}
Your answer:

Figure A3. Sampling Prompt Template for MC Questions

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```
Following is your previous response to the question.
Q: {q}
Choices: {c}
Your previous response: {a}
Check your previous response carefully and solve the same question again.
At the end of your solution, indicate your final answer by writing one of the answer choice (only letter: A, B, C, D, or E) inside a boxed environment, like:

A.
Output:
```

Figure A4. Check Prompt Template for MC Questions

```
Read the following passage and answer the question.

Passage: {p}

Question: {q}

At the end of your solution, indicate your final answer inside a boxed environment, like: answer.
```

Figure A5. Sampling Prompt Template for RC Questions

```
Following is your previous response to the question:
Read the following passage and answer the question.
Passage: {p}
Question: {q}
Your previous response: {a}
Check your previous response carefully and respond the question again.
At the end of your solution, indicate your final answer inside a boxed environment, like: answer.
```

Figure A6. Check Prompt Template for RC Questions

```
Please answer the following question.

Think carefully and in a step-by-step fashion.

At the end of your solution, put your final result in a boxed environment, e.g. answer

Q: {q}
```

Figure A7. Sampling Prompt Template for Essay Questions

```
Following is your previous response to the question. Q: {q}
Your previous response: {a}
Check your previous response carefully and solve the same question again step by step.
At the end of your solution, put your final result in a boxed environment, eg. (answer).
Output:
```

Figure A8. Check Prompt Template for Essay Questions

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