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Article

A Chopper for the Injection Line of the SPES Project Cyclotron: Solutions and Design

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Abstract: This paper presents the design and the solutions of the chopper for the injection line of the cyclotron of the SPES project at Laboratori Nazionali di Legnaro. The device aims to precisely modulate the average current injected into the cyclotron, thereby controlling the current it delivers. A precise control of the beam current is essential for many experiments foreseen for the cyclotron. Due to safety constraints and limited space, an innovative design has been developed. The chopper features a Wien filter configuration, where the electric field is pulsed and the magnetic field is generated by permanent magnets.

Keywords: chopper; cyclotron; SPES; permanent magnet

1. Introduction

One of the main goals of the SPES project [1,2] is the production of exotic nuclei using the new ISOL target [3,4]. This system requires precise balancing of its heating load to maintain the operational temperature. The power sources for this heating are the Ohmic effect and the proton beam. Therefore, the beam current on the target must be carefully increased from 0 μA to approximately 200 μA . One of the most effective ways to achieve precise control of the target current is to vary the current injected from the ion source into the accelerator, which is a cyclotron in the SPES project.

To vary the injected current, several options are available: adjusting the settings of the source, the inflector, or the cyclotron cavities, or introducing an aperture, an de-phased buncher, or a chopper in the injection line. Among these, a promising solution is the chopper, as implemented in other similar facilities, such as Arronax [5].

A chopper can operate at frequencies lower than the cyclotron cavities (approximately 56 MHz), allowing it to modify the average current delivered by the cyclotron by selecting the number of bunches within a given period, while keeping the charge per bunch constant.

The chopper to be introduced in the injection line of the SPES cyclotron must also meet additional requirements, necessitating an innovative design. Specifically, it must ensure fail safe operations and be very compact due to the limited space available in the injection line. The first requirement can be addressed by using the magnetic field of a permanent magnet, periodically compensated by an electric field, while the second requirement necessitates overlapping the magnetic and electric fields to create a Wien filter.

This document outlines the requirements for the chopper, describes the solutions developed to meet them, and presents the final design along with the expected performance based on numerical simulations.

2. The Injection Beam Line of the SPES Cyclotron

The cyclotron for the SPES project is capable of accelerating H^- ions up to 70 MeV with a maximum current of 750 μA (52 kW of extracted power). Further details can be found in [6].

The injection beam line is located below the cyclotron, in a pit, and its main components include: source, beam stopper, two solenoids, two quadrupoles, two steering magnets, and a collimator. A schematic, detailing the distances between these elements, is presented in Figure 1(a).

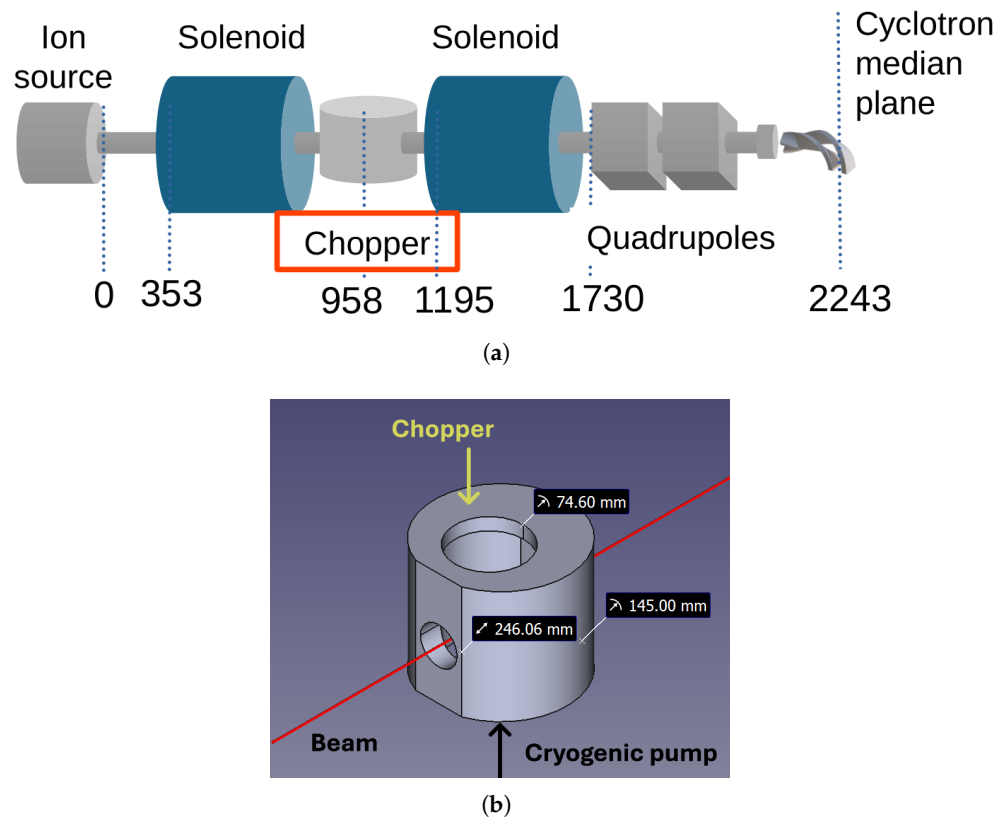


Figure 1. (a) The scheme representing the elements composing the injection line. (b) The design of the diagnostic chamber located at 958 mm from the source output. In the picture there are also the principal measures, the foreseen location of the chopper and the cryogenic pump.

As shown in the schematic, there is a small chamber located between the two solenoids, approximately 1.3 meters below the cyclotron median plane, designed to host one device at a time. The current plan is to install either a buncher, a chopper, or a pepper pot device, depending on the target requirements. This chamber is roughly cylindrical, measuring about 250 mm in length and 145 mm in radius, with its axis orthogonal to the beam direction. It has two access points: one is occupied by a cryogenic pump, while the other is available for inserting the required device. The radius of this latter flange is 75 mm.

A simplified design of the chamber is given in Figure 1(b).

3. The Chopper Setup

The ISOL target requirements include ramping the beam current up or down from 0 to 200 μA with an increment step of 0.5 μA or less. Additionally, to prevent unexpected beam current increases due to controller failure, the system should be fail safe, i.e. *normally deflecting*.

Since short beam trips are not problematic for the ISOL target (numerical analysis indicates that beam trips lasting up to 1 second are sustainable), the average current can be varied by adjusting the number of bunches within a fixed period, rather than altering the charge of each bunch. This approach allows the current controller to operate at a fraction of the cyclotron cavities frequency, creating *trains* of bunches separated by empty intervals. The ratio between the lengths of the bunch trains and the empty intervals determines the average current. The resulting time plot of the bunches is schematically shown in Figure 2(a).

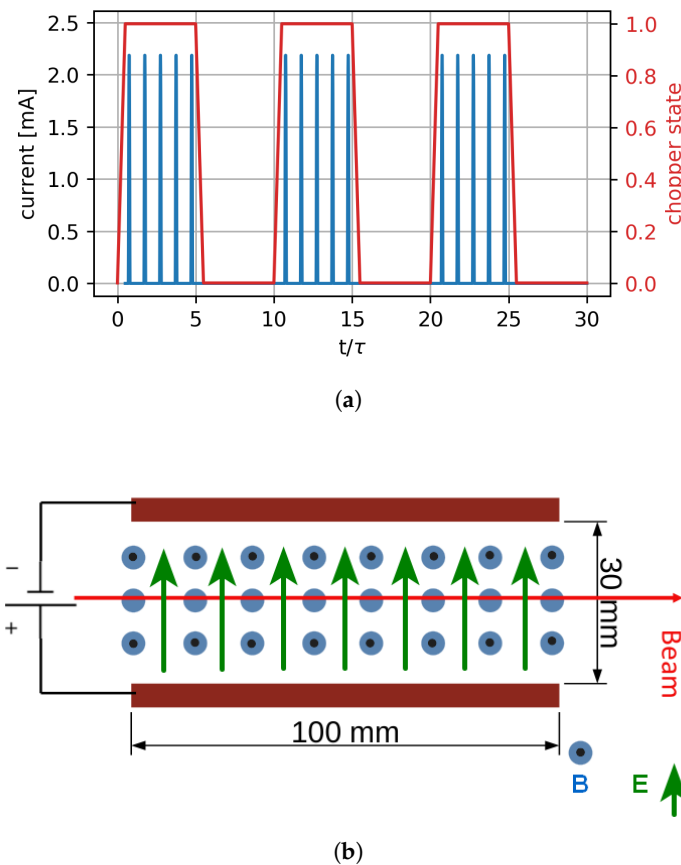


Figure 2. (a) A schematic timeline for the bunches sent by the cyclotron to the target (blue curve, right axis) when the chopper operates with a duty cycle equals to 50 % (the red curve represents the chopper state: 1 is on, 0 is off. Left axis). In this example the chopper has a frequency of one tenth of the cyclotron, which is equal to 56.16 MHz. (b) The simplified scheme that allows to compute the deflection of the beam as a function of the magnetic flux density and then the electric field as a function of the magnetic flux density.

In this context, a single bunch represents the smallest amount of current. Consequently, with this type of controller, the number of bunches within one operational interval dictates the minimum possible increment in current. For instance, a controller frequency of 560 kHz, which is 1/100th of the cyclotron frequency, allows for trains with a maximum of 100 bunches, resulting in a resolution of 1%. To achieve a sufficiently high current resolution, the operating frequency should be less than 1/400th of the cyclotron frequency, leading to a maximum theoretical frequency of 140 kHz.

As mentioned earlier, this device must be capable of stopping the beam even in the event of a power supply failure. One solution is to provide a constant deflection using a permanent magnet, while an alternating electrostatic field provides the counter-deflection. For compactness, the electric and magnetic fields should be overlapped, creating a Wien filter configuration. The dimensions are also crucial, as the device must be easily removable.

An indicative estimation of the magnetic flux density can be derived from the basic scheme shown in Figure 2(b), where the electric field is generated by two electrodes 30 mm apart and 100 mm long, while the magnetic field exits the picture and is present only between the two electrodes. The length and distance of the electrodes are initial guesses.

Based on these simplified assumptions, a beam deflection between 7 to 14 mm, which is the average transversal size of the beam, corresponds to a magnetic field ranging from 0.04 T to 0.08 T. Given a 30 mm distance between the electrodes, the electrostatic potential must range from a minimum of 3.5 kV to a maximum of 7 kV.

The design of the chopper should ensure that the magnetic field is homogeneous in all directions (longitudinal and transverse), sharply edged at the borders, with a zero value outside the yoke, and

capable of inducing adequate beam deflection. Additionally, the magnetic field must be kept as low as possible to minimize the electrostatic potential required to generate the counter-deflecting electric field.

To meet these requirements, an iron yoke must be introduced. We have preliminarily evaluated several configurations, such as C-shaped or H-shaped yokes, ultimately selecting the configuration shown in Figure 3(a). The iron yoke guides and homogenizes the magnetic field in the central gap, with its width determining the field value: enlarging the yoke decreases the magnetic flux density and vice versa.

To shape properly the magnetic field along the beam path, ensuring a sharp drop to zero outside the region of interest, two iron masks are added, one before and one after the yoke. An additional benefit of the masks is that they also confine the electric field within the yoke, as their electric potential will be zero. Moreover, the entrance mask protects the chopper components, while the exit mask dumps the beams. Moreover, adjusting their distance from the yoke allows for changes in the magnetic flux density within the chopper; moving the masks closer to the yoke decreases the magnetic flux density in the beam path.

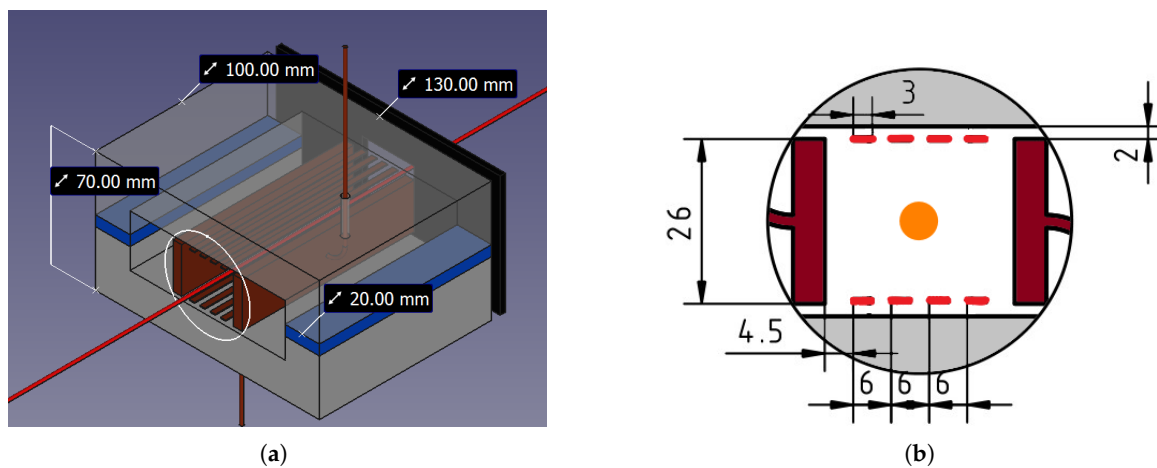


Figure 3. (a) The final configuration of the chopper: the permanent magnets are in blue, the iron yoke in gray, the electrodes in brown and one of the two masks is in black (the other, on the opposite side, is hidden). The red line represents the beam trajectory while the white circle is the border of the section depicted in (b). In this second picture the two main electrodes are in brown, the sub-electrodes in red, the yoke is gray and the orange dot is the beam position. All the distances are in mm.

In order to uniform the electric field, besides the two main electrodes eight more *sub*-electrodes are introduced, four above and four below the beam path, in the same way explained in [7]. They can be seen in Figure 3(b).

4. Numerical Analysis for the Chopper Evaluation

To determine the optimal dimension of each component, several numerical analyses were conducted. These studies involved an iterative process.

The first analysis aimed to obtain the magnetic flux density generated by the permanent magnets. The second analysis computed the electric field produced by the electrodes. Finally, the third analysis assessed the behavior of a beam traveling in the previously obtained fields.

4.1. Magnetic Field

The magnetic field can be determined using Finite Element Analysis (FEA). We employed the ElmerFEM code [8] for this purpose. This method requires a simplified CAD design of the device, along with the selection of materials and properties such as magnetization. In this case, the chosen material for the yoke is iron, conforming to the XC06 standard. The B-H curve for this material is easily available online [9].

As regards magnets, for the specified magnetic flux density Neodymium magnets has been selected.

The final model to determine the magnetic field is shown in Figure 3(a). In the model there are several parameters that allow to tune the magnetic field, one is the yoke width, as stated above, another is the permanent magnet width or thickness.

After some attempt the magnet dimensions were set to 100 mm length, 6 mm thick and 20 mm width while the magnetization is 25EH, that is 1 T of remanent magnetization (equivalent to 800 kA/m).

The resulting magnetic flux density in the transverse direction is shown in Figure 4(a) and (b). The plot indicates that the magnetic flux density is vertical (with negligible components in other directions) and fairly uniform within the region of interest, i.e. between the two electrodes, which are positioned 15 mm from the beam axis. The magnetic flux density at the center is 0.06 T.

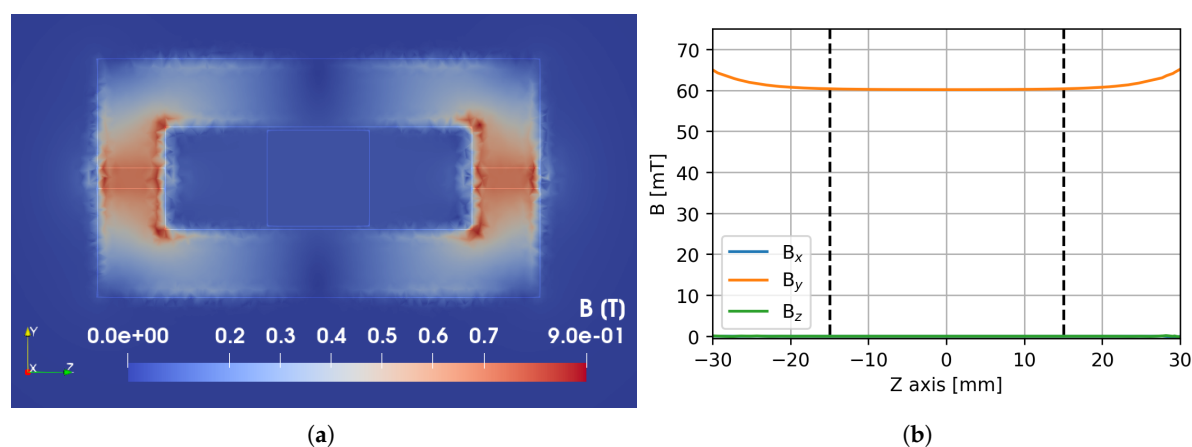


Figure 4. (a) The magnetic flux density on the transversal plane of the chopper. (c) The magnetic flux density along the horizontal transversal axis in the bap region: the orange line is the one in the vertical direction, green and blue are in the other two directions. The two dashed lines indicates the electrodes positions, the beam can pass only between them.

4.2. Electric Field

Similarly to the study of the magnetic field, we computed the electric field using a FEA software (ElmerFEM also here), applying the same 3D model described in Figure 3(a). In this model, all components are grounded except for the electrodes and sub-electrodes, which are biased symmetrically with respect to the longitudinal vertical plane. This means that if one electrode is at a positive voltage, the corresponding electrode on the opposite side has an equal magnitude of voltage but the opposite polarity.

The results are illustrated in Figure 5. The contour plot in (a) represents the electric field magnitude on the transversal plane: the effect of the eight sub-electrodes is clearly visible. In (b) there is a comparison between the Z component of the electric field taken along the axis connecting the center of the two main electrodes: the blue line represents the chopper with the sub-electrodes while the green line is the case of a chopper without them.

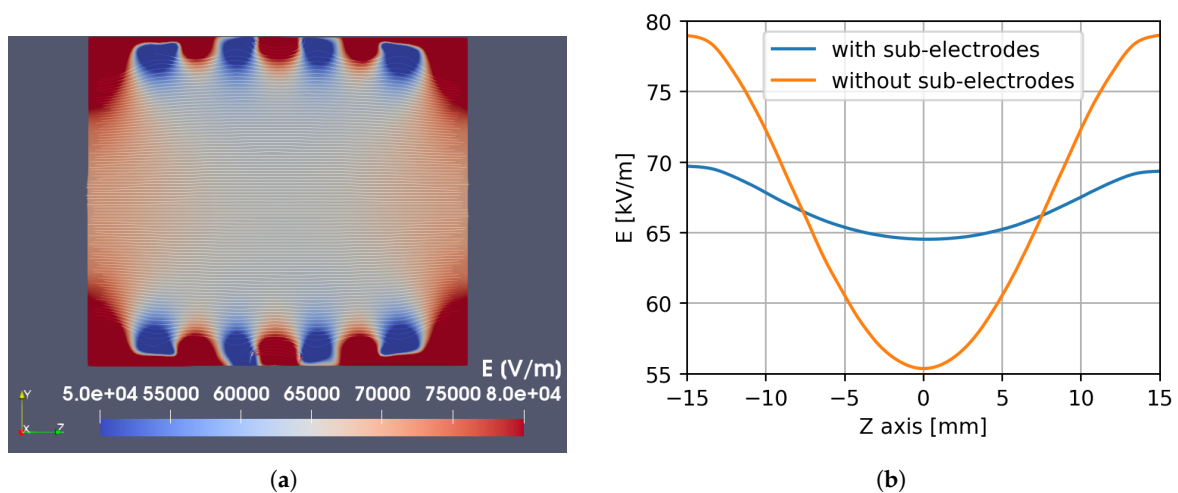


Figure 5. (a) Contour plot of the electric field magnitude in the transversal plane of the chopper when all the electrodes and sub-electrodes are turned on. (b) The electric field in the Z direction along the Z axis for with the sub-electrodes (blue line) and without (green line).

The simplest method to bias the electrodes and sub-electrodes is to connect them to a voltage divider. Given that the electric field will follow a pulse wave, the resistors in this divider must be appropriately sized to deliver a sufficiently high current, ensuring that the potential of all sub-electrodes rises as quickly as that of the main electrodes. However, this solution introduces the side effect of the current passing through the divider which is both a heating problem and a current drain that extends the rising time for the main electrodes.

To address this issue, we have considered the option of disconnecting the sub-electrodes from the main electrodes, maintaining them at their operational potential. In this scenario, since the sub-electrodes are held at a non-zero voltage, they would introduce a static electric field into the beam path. This could potentially perturb the beam dynamics and allow some particles to pass through the chopper even when it is turned off. The impact of this residual electric field on the beam dynamics will be evaluated in [subsection 4.3](#).

4.3. Beam Dynamics

To evaluate the effect of the chopper in the injection line and verify if the beam is correctly dumped, the beam line from the source to the cyclotron inflector was simulated using the Simion code [10].

Simion can both, compute electric and magnetic fields and also import external ones. In this analysis the fields related to the chopper and to the inflector, together with the magnetic field of the cyclotron, are computed with a FEA and then imported, while the other fields, that are the magnetic fields of the two solenoids and those of the quadrupoles, are computed in Simion.

A valuable feature of Simion is its ability to run the dynamics integration alongside a user programmed file in which one can create specific functions. In our case this capability has been exploited to define the impact conditions for the beam, based on the geometry of the injection line and the chopper.

The simulated beam, characterized by measured parameters, consists 10^3 particles. The outcomes of the dynamics integration are illustrated in [Figure 6](#). In panel (a), the beam interaction with the dumper (represented as a brown box) is depicted. The beam stops on the dumper when the chopper electrodes are fully deactivated (black lines) and when the sub-electrodes are maintained at their operational voltages (blue lines). These two conditions are related to alternative configurations of the chopper, as explained in [section 5](#). In both scenarios, the beam is entirely stopped by the dumper.

Panel (b) shows the beams at the inflector entrance with the chopper at its operational voltage (orange dots) and without the chopper (blue dots). All other elements of the injection line remain

unchanged. The chopper exerts a weak focusing effect and the beam remains nearly identical to the unperturbed one.

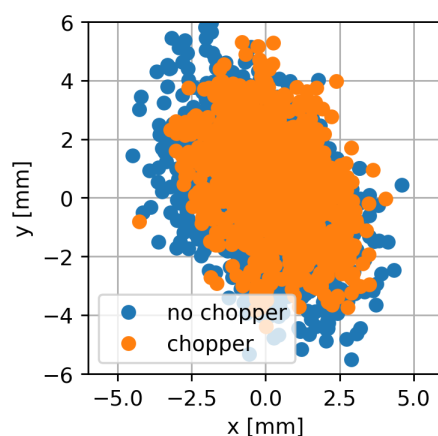
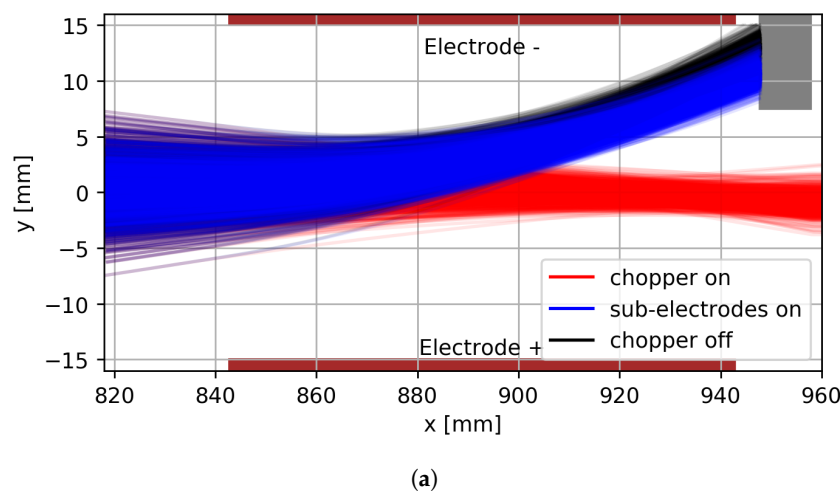


Figure 6. (a) The picture shows the beam trajectory inside the chopper. The beam color is related to the chopper setting: black is for the electrodes and sub-electrodes off, blue is for the electrodes off and the sub-electrodes on and red is for all the electrodes and sub-electrodes on. The other visible elements are the two electrodes in brown and the dumper in grey. (b) In the plot there are the simulation of the beam at the entrance of the inflector (63 mm from the median plane of the cyclotron) with the chopper at its ideal voltage (orange dots) and without the chopper.

The simulation results indicate that the beam is correctly stopped in the chopper dumper when there is no electric field. When the sub-electrodes are maintained at their operating voltage and the main electrodes are set to zero, the beam stops slightly displaced but still within the dumper, indicating that the residual electric field has a limited effect.

The optimal working voltage was determined through multiple simulations, gradually increasing the electrode bias. The best transmission after the inflector was identified as the desired spot. Figure 7(a) presents these simulation results, showing that the optimal working voltage is 2.9 kV, although partial beam transmission begins at around 1.5 kV.

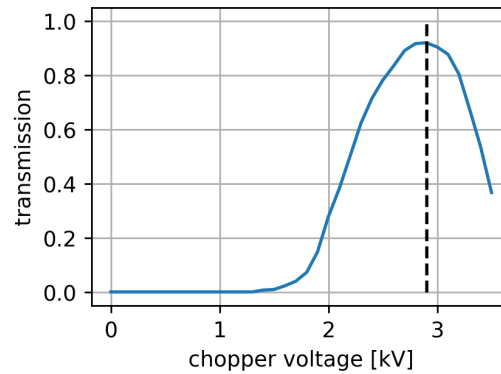


Figure 7. The transmission of the beam after the inflector as a function of the chopper voltage. The best transmission is indicated by the dashed black line.

An important result is that the optimal transmission is 90%, consistent with simulation values obtained without the chopper, suggesting that the chopper perturbations on the beam are negligible for this parameter. Additionally, an analysis of the emittance indicates that the chopper is unlikely to affect the beam quality. The emittances with and without the chopper are compared in Figure 8. The plots show that the beams are very similar, with the primary difference being the focus, represented by the α parameter, which is slightly higher with the chopper, as expected.

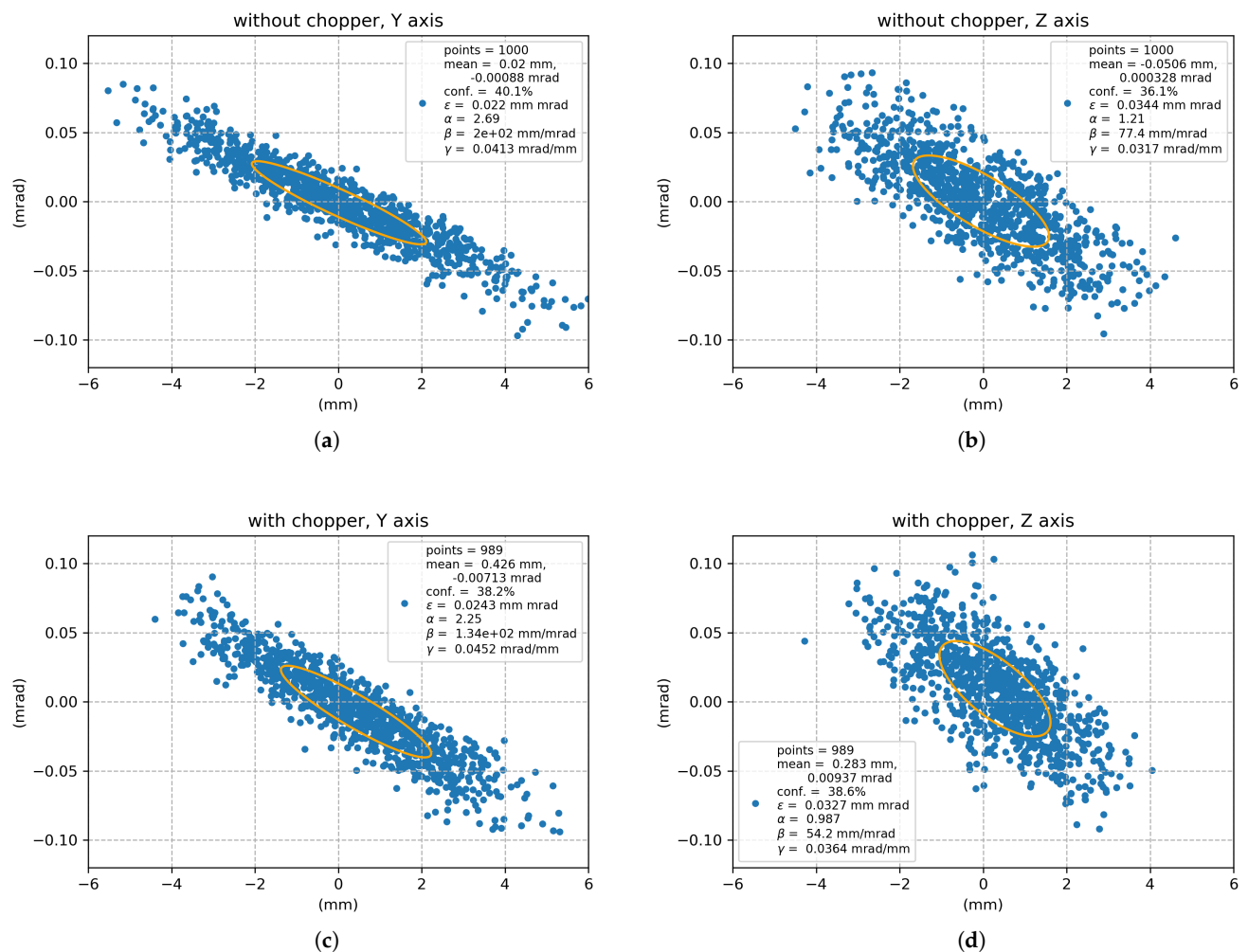


Figure 8. The emittances at the inflector entrance without the chopper (panels a and b) and with the chopper (panels c and d).

5. Power Supply Chain

A critical aspect in this kind of devices is the power supply chain. In the present project the approach is to bias the electrodes with a solid state fast switch in a similar way seen in [5].

Simplified electric circuits representing the device are illustrated in Figure 9(a) and (b), they are implemented, with more details, in the software LTspice [11] in order to verify their behavior. In Figure 9 (a) there are the connections, one for the positive bias and another for the negative, from the power supplies to the fast switches (which should be installed as close as possible to the chopper) and from there to the chopper. Just before the fast switches there is a capacitor to ensure a rapid rise in the voltages of the main electrodes. A capacitance of 100 nF is considered a suitable value.

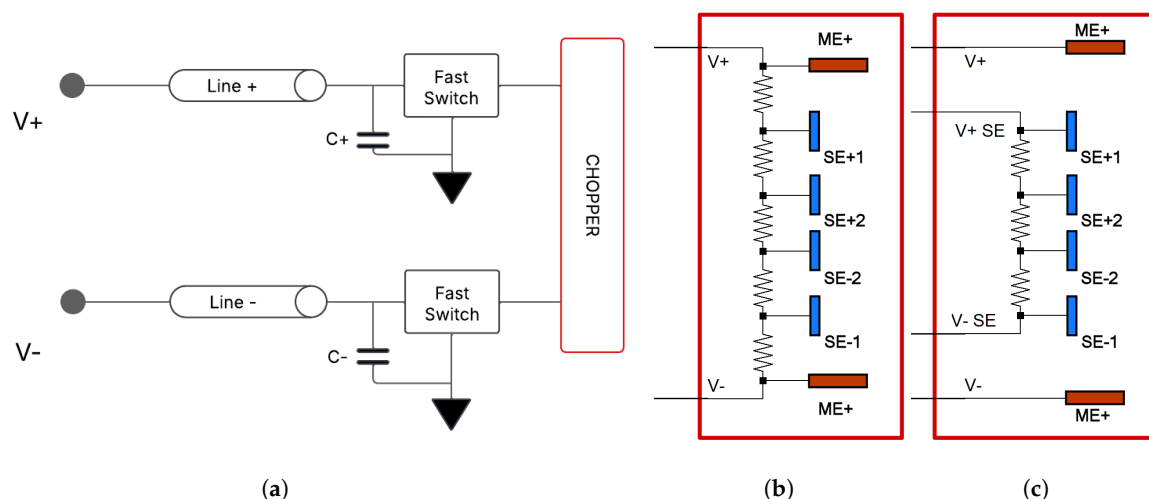


Figure 9. (a) A simplified electric scheme for the chopper power supply chain. (b) The equivalent circuit of the chopper. (c) The scheme for a chopper with a static voltage divider for the four sub-electrodes.

In Figure 9 (b) there are the components belonging to the chopper: the two main electrodes are in red while the sub-electrodes are in blue, all the electrodes are connected by a voltage divider consisting of five resistors.

From electrical point of view each electrode is a capacitor and its capacitance is estimated by FEA, their values are: 15 pF for the main electrodes, 5 pF for the sub-electrodes, and 1 pF for the mutual capacitance.

The resistances in the voltage divider should be low enough to ensure a rapid increase in the sub-electrodes voltage. However, if the resistance is too low, it will drain most of the current supplied to the chopper, resulting in significant heat generation. For example, a resistance of 3.5 k Ω will draw 330 mA and produce 1.9 kW of heating power when the chopper voltage is set to 5.8 kV. Conversely, a resistance of 15 k Ω will drain 6 mA and generate 90 W of heat.

The two power supplies, that should be positioned far from the cyclotron to avoid radiation-induced failures, are limited in both, voltage and current. In our case, a suitable power supply would have a maximum output of 3 kV and 400 mA corresponding to 1.2 kW.

Using the described circuit, the voltage dynamics for each electrode can be determined, allowing for the calculation of the rise times for both the electrodes and sub-electrodes. With a voltage divider resistance of 15 k Ω , the rise time for the sub-electrodes is approximately 136 ns, whereas with 3.5 k Ω , it is 32 ns. The main electrodes achieve their operational voltage very rapidly, in about 1 ns.

In the presented case, the cyclotron period is 18 ns, while the chopper period can be higher than 180 μ s (equivalent to 5.6 kHz), therefore a rise time of 136 ns represents less than 0.1 % of the whole cycle which is below the required resolution. Consequently a voltage divider resistance equal to 15 k Ω is considered a suitable choice.

In Figure 10(a) three curves represent the voltages for the positive electrodes during a single pulse, with a voltage divider resistance equal to 15 k Ω and a duty period of 250 ns. The plot shows that the

main electrode (blue line) reaches its final voltage in a very short interval (about 1 ns) compared to the two sub-electrodes (orange and green lines).

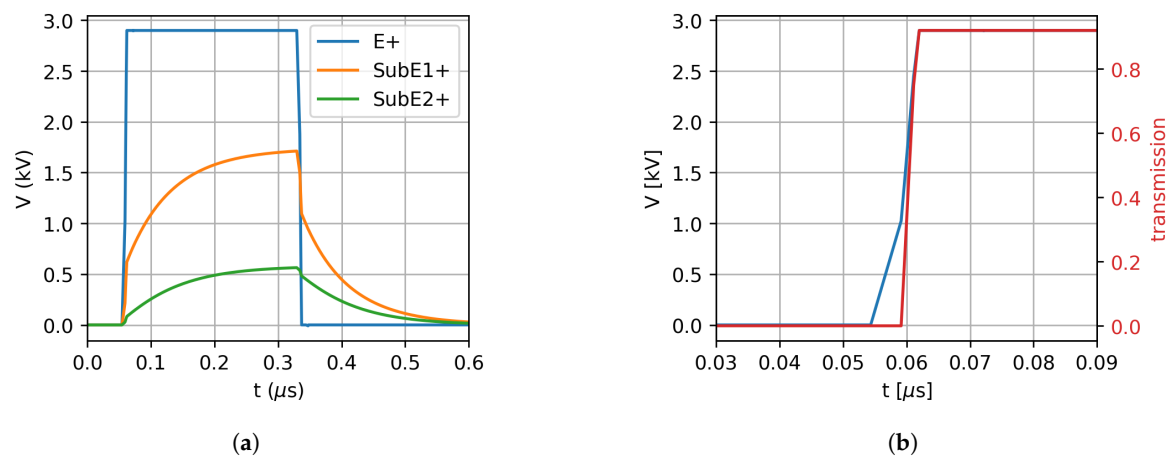


Figure 10. (a) The charging curves for the positive electrode and sub-electrodes for a short pulse. (b) The blue curve is a detail of the voltage dynamics for the positive electrode. The red curve is the consequently current transmission in the cyclotron.

In Figure 10(b), a detailed view near the ignition moment is presented, showing the main electrode voltage (blue curve) and the resulting beam transmission within the cyclotron (red curve).

As mentioned in subsection 4.3, an alternative and more efficient approach is to maintain the sub-electrodes at their operative voltages continuously. This method offers two advantages: only the main electrodes have a variable voltage, resulting in very short rising time, moreover the heating generated by the voltage divider can be significantly reduced, as its resistance can be freely incremented. The scheme representing this new alternative approach is in Figure 9 (c).

This configuration has the drawback that a residual electric field being present in the chopper also during the off period, the effect of this electric field was evaluated using Simion in subsection 4.3 and resulted compatible with the requirements.

6. Conclusions

The present document describes the chopper developed for the injection line of the cyclotron of the SPES project. The chopper has the purpose to vary the injected current in order to finely modulate the average current delivered to the ISOL target. The modulation has to ensure a control under 0.5μ A in a total current to 200μ A.

It features an innovative design to meet safety requirements, ensuring the beam is normally stopped, within a compact space. The solution involves using a Wien filter configuration to minimize bulk, with the magnetic field generated by permanent magnets to ensure reliability.

Additional design details include the homogenization of the electric field using four pairs of sub-electrodes, positioned between the main electrodes and biased with intermediate voltages. Furthermore, the magnetic and electric fields are confined by two ferromagnetic plates situated before and after the chopper.

The design is analyzed exploiting numerical simulations. Thanks to FEA we have computed the electric and the magnetic fields and with the code Simion we have evaluated their effects on the beam dynamics. From this analysis resulted that the electric and magnetic fields have a very small effect on the beam when the chopper is turned on and, in the case the chopper is turned off the beam stop correctly in the dumper.

The design was analyzed using numerical simulations. Utilizing Finite Element Analysis, we computed the electric and magnetic fields, and with the Simion code, we evaluated their effects on beam dynamics. The analysis revealed that the electric and magnetic fields have a minimal impact

on the beam when the chopper is activated, and when the chopper is deactivated, the beam correctly stops in the dumper.

Finally, to achieve a faster response and mitigate the heating issue, an improved supply configuration was defined. In this configuration, some of the chopper electrodes remain biased even when the chopper is turned off. Simulations indicate that with this setup, the beam consistently stops in the dumper.

The executive design is currently being defined, with the device construction scheduled for mid-year.

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Conflicts of Interest: “The authors declare no conflicts of interest.”

Abbreviations

The following abbreviations are used in this manuscript:

INFN	Istituto Nazionale di Fisica Nucleare
LNL	Laboratori Nazionali di Legnaro
SPES	Selective Production of Exotic Species
FEA	Finite Elements Analysis

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