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## Article

# Chemical Bonding and Dynamic Structural Fluxionality of a Boron-Based $B_8Al_3^+$ Cluster

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**Abstract:** We studied the boron-based composite cluster  $B_8Al_3^+$  doped with Al atoms. The global minimum structure of the  $B_8Al_3^+$  cluster is a three-layer structure, consisting of three parts:  $Al_2$  unit,  $B_8$  ring and isolated Al atom. Charge calculations analysis shows that the cluster can be expressed as  $[Al]^+[B_8]^{2-}[Al_2]^{2+}$ , has  $6\pi/6\sigma$  double aromaticity, and follows the  $(4n+2)$  Hückel rule. Born–Oppenheimer molecular dynamics (BOMD) simulation shows that,  $B_8Al_3^+$  cluster has dynamic fluxionality properties. Remarkably, at the single-point CCSD(T) level, the energy barrier for intramolecular rotation is merely 0.19 kcal mol<sup>-1</sup>.  $[B_8]^{2-}$  molecular wheels has magical  $6\pi/6\sigma$  double aromaticity properties, providing a continuous cloud of delocalized electrons, which is a key factor in the dynamic fluxionality of the cluster. The  $B_8Al_3^+$  cluster provides a new example of dynamic structural fluxionality in molecular systems.

**Keywords:** dual  $\pi/\sigma$  aromaticity; dynamic structural fluxionality; chemical bonding; theoretical chemistry

## 1. Introduction

Boron, positioned nearest to carbon in the periodic table, shares various structural attributes and represents a typical electron-deficient element. Experimental and theoretical investigations of elemental boron clusters have been ongoing since the 1980s [1–15]. Systematic experimental and computational analyses have revealed the propensity of boron clusters to exhibit planar or quasi-planar structures across diverse size scales. Owing to the electron deficiency, boron-based clusters possess a unique electron distribution orbital structure, enabling the formation of distinct chemical bonds. Within these clusters, chemical bonding is influenced by  $\pi/\sigma$  aromaticity, antiaromaticity, and conflicting aromaticity, necessitating electron delocalization to counterbalance boron's inherent electronic deficiencies [4–6,9]. Additionally, the unusual bonding mode also leads to dynamic structural fluxionality of bare boron clusters and related compound systems.

Metal atoms are introduced into boron clusters to create boron-based alloy clusters. The approach proves effective in exploring structural diversity, adjusting electronic properties, and uncovering new chemical bonds within these clusters [16–20]. Utilizing intramolecular charge transfer allows precise electron counting in alloy clusters, facilitating the deliberate design of new cluster structures and deeper investigation into their bonding and dynamic attributes. Structural fluxionality is an extraordinary attribute inherent in boron clusters, manifesting as dynamic flexibility. The electron deficiency of boron contributes significantly to this distinct dynamic behavior. Researchers have consistently designed and documented a range of pure boron clusters showcasing dynamic fluxionality, including  $B_{11}^-$ ,  $B_{13}^+$ ,  $B_{15}^+$ , and  $B_{19}^-$  [21–24]. Subsequent research revealed that blending different metals enables the deliberate design of boron-based cluster nanomachines exhibiting dynamic fluxionality. In 2017, Zhai and colleagues identified nearly isoenergetic three-layer and spiral structures within the  $Be_6B_{11}^-$  cluster [25]. The former sandwich structure demonstrates two dynamic rotation/twisting modes, resembling structural fluidity akin to the nanoscale Earth-Moon system. Furthermore, researchers have observed magical dynamic

fluxionality in a range of binary boron-based nanoclusters, including  $\text{Na}_5\text{B}_7$ ,  $\text{V}_2\text{B}_7^-$ ,  $\text{Be}_3\text{B}_{11}^-$  [26–28], among others.

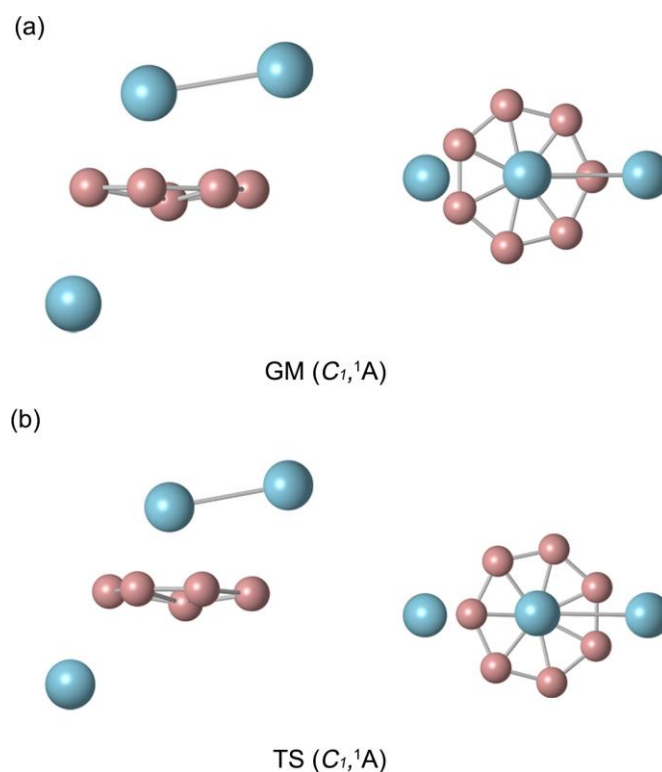
To diminish the dynamic energy barrier associated with fluxionality, researchers started incorporating multiple metal atoms to alter the electron distribution within boron clusters. Compass-like clusters  $\text{MB}_7\text{X}_2$  and  $\text{MB}_8\text{X}_2$  (where X stands for Zn or Cd and M represents Be, Ru, or Os) [29], the  $\text{X}_2$  needle undergoes rotation along the  $\text{B}_8$  wheel. The central  $\text{B}_6$  ring within the boron-based ternary  $\text{Rb}_6\text{Be}_2\text{B}_6$  cluster [30], featuring a distinct sandwich structure, emerges as exposed bare B enclosed by two tetrahedral  $\text{BeRb}_3$  ligands. The bonding pattern within the vast sandwich cluster encourages distinctive dual-mode dynamic fluxionality. The study aims to examine the structure of the ternary cluster  $\text{B}_8\text{Al}_3^+$ , analyze its structural stability, and determine if it presents novel instances of dynamic structural fluxionality. The GM structure of the  $\text{B}_8\text{Al}_3^+$  was determined using CK search. The  $\text{B}_8\text{Al}_3^+$  cluster exhibits a three-layer structure. Its geometric configuration resembles a "clock": the middle  $\text{B}_8$  ring create the dial, while the two aluminums above it atoms act as pointer, with an Al unit below it. Chemical bonding analysis indicates that the  $\text{B}_8\text{Al}_3^+$  cluster exhibits  $6\pi/6\sigma$  dual aromaticity, with a double delocalized electron cloud facilitating a continuous "orbit," enabling unrestricted rotation of the  $\text{Al}_2$  unit above the  $\text{B}_8$  ring. Charge calculations reveal evident charge transfer among the  $\text{Al}_2$  unit, Al atom, and the  $\text{B}_8$  ring, presenting a formal description as a  $[\text{Al}]^+[\text{B}_8]^{2-}[\text{Al}_2]^{2+}$  ion complex.

## 2. Results

### 2.1. Global-Minimum of $\text{B}_8\text{Al}_3^+$ Cluster

Figure 1a show the GM  $C_1$  ( $^1\text{A}$ ) structure of  $\text{B}_8\text{Al}_3^+$  cluster. The relative energies of the top 20 low-lying isomers, including zero-point energy correction (ZPE), are provided in Figure S1. The  $\text{B}_8\text{Al}_3^+$  cluster exhibits  $C_1$  symmetry, signifying the global minimum on the potential energy surface. Initial computations using PBE0/def2-TZVP on the top 20 structures revealed the GM cluster to be 1.01 kcal mol $^{-1}$  lower in energy than its nearest competitor. It is worth noting that within the DFT method, the PBE0 and B3LYP functionals are widely acknowledged for their complementarity in molecular systems. To ensure computational consistency across density functionals concerning geometry and energetics, we completed a comparison at the B3LYP/def2-TZVP method level, revealing the GM cluster to be 7.71 kcal mol $^{-1}$  lower in energy than its closest competitor. Subsequent calculations conducted at the CCSD(T)/def2-TZVP//PBE0/def2-TZVP and complementary CCSD(T)/def2-TZVP//B3LYP/def2-TZVP levels indicated energy advantages of 5.61 kcal mol $^{-1}$  and 4.65 kcal mol $^{-1}$ , respectively, for the GM structure. Hence, based on the aforementioned data, the GM  $C_1$  ( $^1\text{A}$ ) structure of  $\text{B}_8\text{Al}_3^+$  cluster is confirmed to be a really minimal structure on the potential energy surface.

Figure 1a displays the top and side views of the GM  $\text{B}_8\text{Al}_3^+$  cluster, representing a closed-shell electronic system. The GM  $\text{B}_8\text{Al}_3^+$  cluster comprises three layers, resembling a clock: the middle  $\text{B}_8$  ring create the dial, while the two aluminums above it atoms act as pointer, with an Al unit below it. Figure 1b demonstrates the similarity between the TS structure and the GM structure, where the Al–Al pointer rotates approximately 25.7° to achieve the TS structure. Currently, the Al–Al pointer is positioned between the two B atoms on the dial. The cartesian coordinates of GM cluster and TS structure at PBE0/def2-TZVP are presented in Table S1.

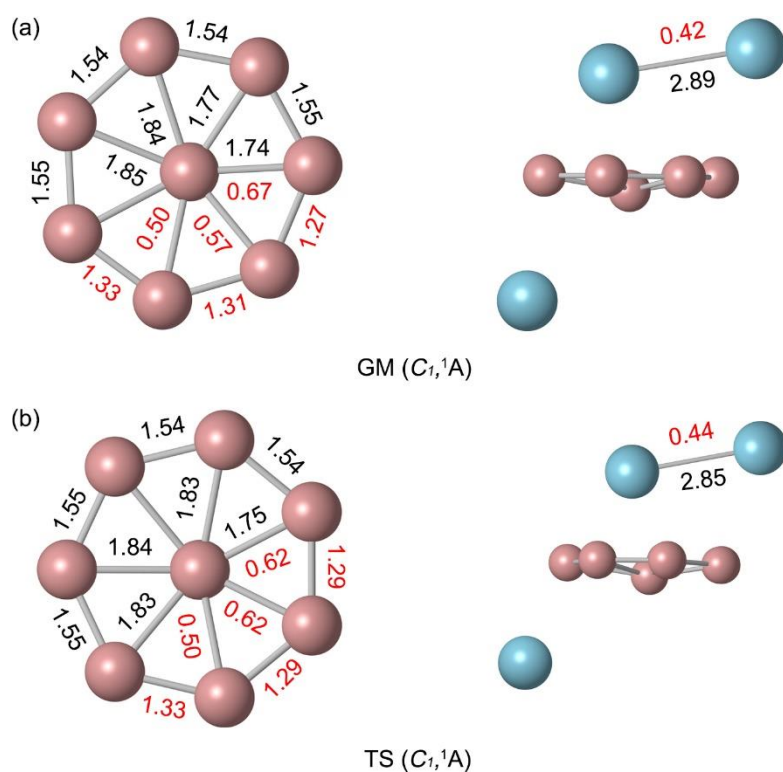


**Figure 1.** Optimized (a)  $C_1$  global-minimum (GM) and (b)  $C_1$  transition-state (TS) structures of  $B_8Al_3^+$  cluster at the PBE0/def2-TZVP level. Presented in top and side views.

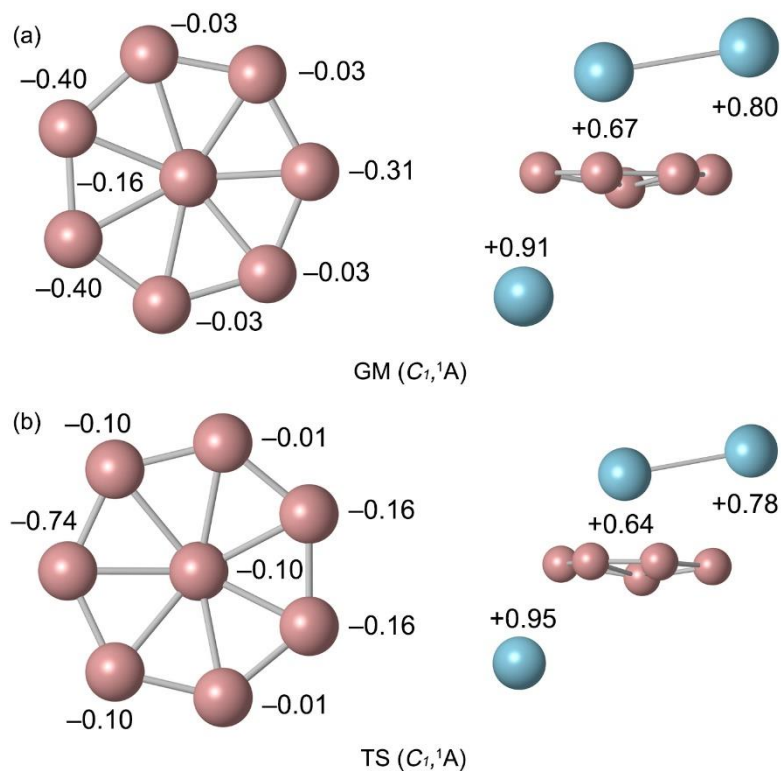
## 2.2. Bond Distances, Wiberg Bond Indices, and Natural Atomic Charges

Figure 2a displays the bond distances and bond orders for GM  $B_8Al_3^+$  cluster. The boron ring's peripheral bond distances are 1.54–1.55 Å, below the upper-bound of 1.70 Å for B–B single bonds. It suggests a force between the B atoms involving both covalent single bonds and delocalized electrons, the bond orders of the  $B_8$  ring are greater than 1, which also illustrates this essence. Radial B–B links are much longer (1.74–1.85 Å), the links are in line with delocalized  $\pi/\sigma$  bonding, which are weaker than single bond. Indeed, their calculated WBIs amount to 0.50–0.67. The distance between the two Al atoms, 2.89 Å, is close to the upper limit of the Al–Al single bond (2.52 Å), and the corresponding Al–Al bond order is 0.42, indicating the presence of an Al–Al single bond.

The natural atomic charges were calculated by natural bond orbital (NBO) analysis as shown in Figure 3. The Al atom below the B ring carry a positive charge of +0.91 |e|. This natural atomic charge data indicate that there is one electron transfers from Al atom to the  $B_8$  ring. The rightmost B atom near the pointer Al<sub>2</sub> carry a charge of –0.31 |e|, indicating an electrostatic interaction between the B and Al atoms (Figure 3a). The B atoms are negatively charged from –0.03 to –0.40 |e| in GM and from –0.01 to –0.74 |e| in TS. The charge carried by Al<sub>2</sub> unit is +1.47 |e|, which can be approximately regarded as transferring two electrons to the  $B_8$  ring. The bond distances and bond order of TS and GM are similar. Due to the deflection of the Al needle, the natural atomic charge changes slightly. Overall, the charge transfer case is identical. The similarity in structure and chemical bonding of GM and TS implies a lower energy barrier between them. Thus, both the GM and TS structures of  $B_8Al_3^+$  cluster are essential charge transfer complexes of  $[Al]^+[B_8]^{2-}[Al_2]^{2+}$ .



**Figure 2.** Calculated bond distances (in Å, black color) and Wiberg bond indices (WBIs, in red color) for GM  $B_8Al_3^+$  cluster at the PBE0/def2-TZVP level. The WBIs are obtained from the natural bond orbital (NBO) analysis at PBE0/def2-TZVP.



**Figure 3.** Natural atomic charges (in  $|e|$ ) for (a)  $C_1 (^1A)$  GM and (b)  $C_1 (^1A)$  TS structures of  $B_8Al_3^+$  cluster. The data are obtained from the NBO analyses at PBE0/def2-TZVP.



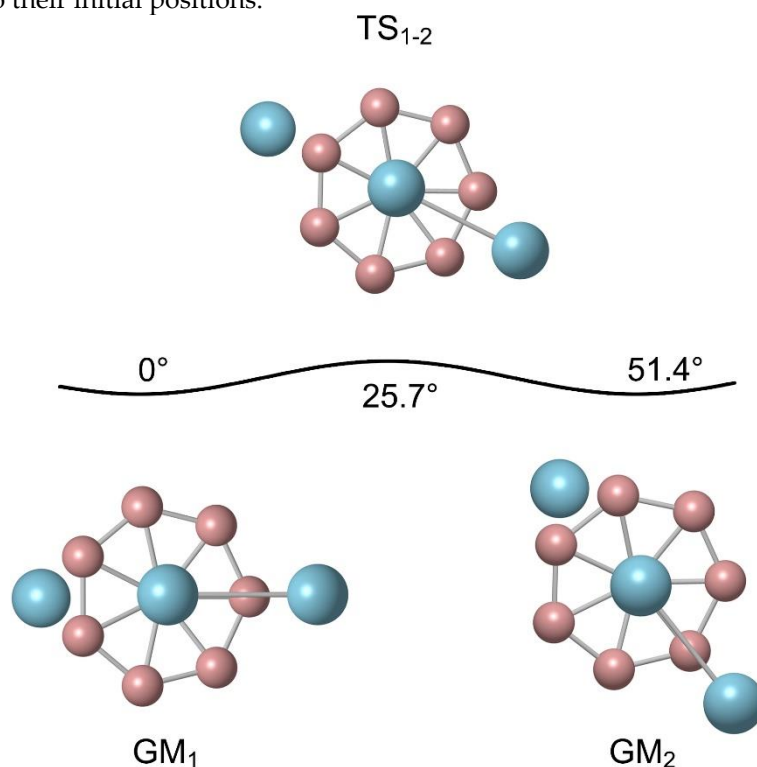
### 3. Discussion

#### 3.1. Dynamic Structural Fluxionality

Vibration frequency analysis was conducted on the GM and TS structures of  $B_8Al_3^+$  cluster at PBE0 level, as illustrated in Figure S2. The GM  $B_8Al_3^+$  cluster exhibits a vibration soft mode at  $30.43\text{ cm}^{-1}$ , correspond the tangential reverse motion involving the  $Al_2$  unit and the  $B_8$  ring. The movement along the vibration soft mode vector leads to the formation of the corresponding TS structure. The TS structure's vibration soft mode is  $29.48i\text{ cm}^{-1}$ . Both exhibit similar rotation modes that facilitate the relative rotation of the  $Al_2$  unit above the  $B_8$  ring. These soft vibrational modes are perfectly in line with dynamic structural fluxionality of the system as a molecular rotor.

To vividly demonstrate the dynamic fluxionality of  $B_8Al_3^+$  cluster, we have run a BOMD simulation at a selected set of temperatures of 300 K for a time span of 50 ps. The system dynamics trajectories were obtained by taking GM structure as the initial coordinate at PBE0 level. The BOMD data are visualized using GaussView, which vividly show that the present ternary cluster behaves closely like a functioning compass at the subnanoscale. The BOMD simulation results vividly illustrate the dynamic fluxionality process within the  $B_8Al_3^+$  cluster: the Al–Al unit rotates above the  $B_8$  ring, resembling the motion of a clock hands. Throughout the BOMD simulation, the  $B_8Al_3^+$  cluster consistently retained geometric stability without noticeable deformation. A short movie is extracted from the simulation and presented in the ESI. The animation approximately lasts for 12 ps.

Figure 4 displays the dynamic evolution process of  $B_8Al_3^+$  cluster. The rotation energy barrier for  $B_8Al_3^+$  cluster is  $0.32\text{ kcal mol}^{-1}$  at PBE0 level, refined to  $0.19\text{ kcal mol}^{-1}$  at the CCSD(T) level. The Al–Al unit, resembling a pointer, is suspended above the  $B_8$  ring. Starting from  $GM_1$  as the initial configuration, it rotates clockwise with the  $B_8$  ring's center as the axis. As the Al–Al pointer rotates  $25.7^\circ$  clockwise, surpassing the rotation energy barrier, it reaches the first transition state,  $TS_{1-2}$ , while the Al–Al pointer is perpendicular to the B–B bond of the two adjacent B atoms below at this stage. Further rotate Al–Al dimer by  $25.7^\circ$  clockwise, one recovers the GM geometry ( $GM_2$ ). Subsequently, it continues to rotate clockwise, always exceeding the reaction energy barrier. After completing the above process by six TS configurations and five GM configurations, all atoms in  $B_8Al_3^+$  cluster eventually return to their initial positions.



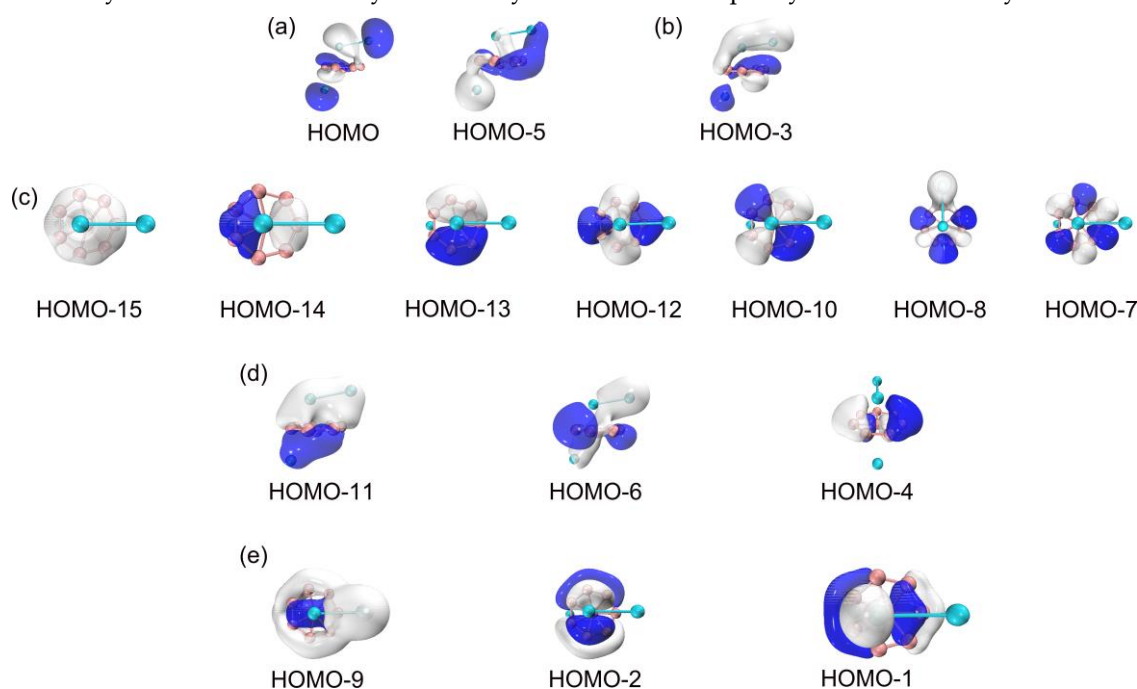
**Figure 4.** Structural evolution of  $B_8Al_3^+$  cluster during intramolecular dynamic rotation of the Al–Al dimer with respect to  $B_8$  molecular wheel.

### 3.2. Chemical Bonding

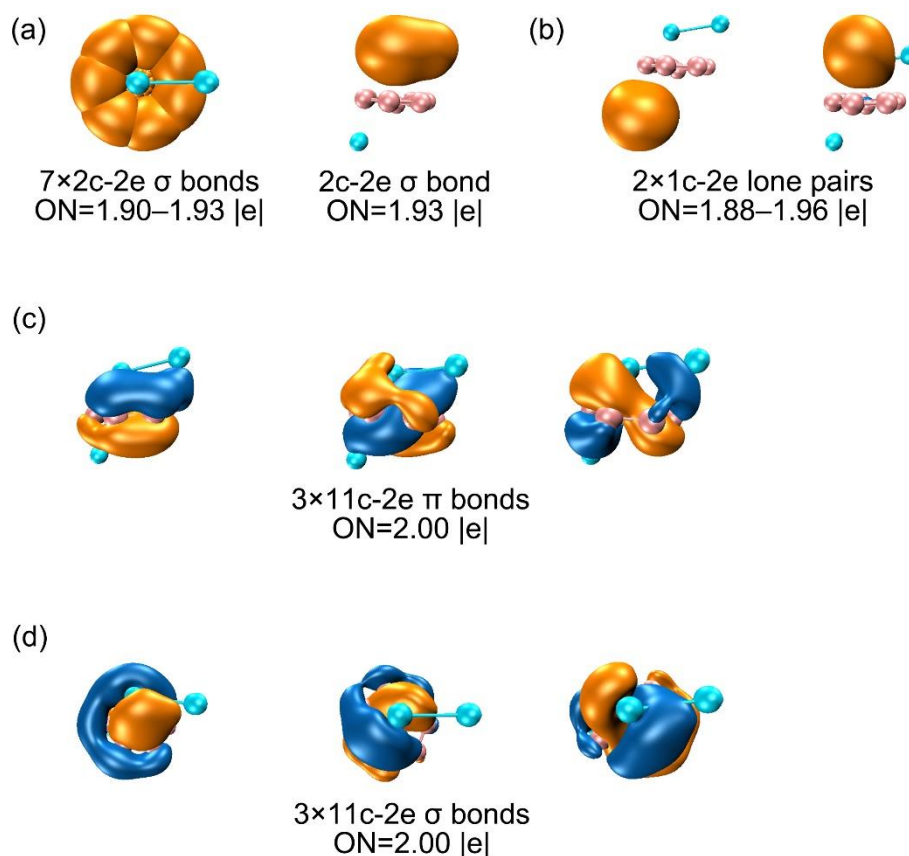
To understand the unique geometries, stability, and dynamic fluxionality of GM  $B_8Al_3^+$  cluster, it is essential to elucidate their chemical bonding. For this purpose, CMOs and AdNDP analyses are fundamental. The GM  $B_8Al_3^+$  cluster is a closed-shell cluster with 32 valence electrons. Its 16 occupied CMOs are sorted to five subsets based on their constituent atomic orbitals (AOs) as shown in Figure 5. The two CMOs in subset (a) are composed mainly of 3s/3p AOs from two aluminum atoms, in their constructive versus destructive combinations. According to the CMO construction principles, these two CMOs can be localized as the lone pairs of Al  $3s^2$ . HOMO-3 in subset (b) is responsible for interlayer Al-Al  $\sigma$  single bond, which originate from 3s AOs of two Al atoms. Meanwhile, the 14 orbital electrons in subset (c) are derived mainly from the 2s and 2p atomic orbitals of  $B_8$  ring.

There are seven CMOs in subset (c) contain HOMO-15, HOMO-14, HOMO-13, HOMO-12, HOMO-10, HOMO-8 and HOMO-7, which constitute a complete series with from 0 up to 3 nodal planes (sequentially from left to right), including 2 degenerate pairs. Upon recombination, these seven orbitals can form seven two-center two-electron (2c-2e) bonds, thereby being localized as seven B-B  $\sigma$  bonds. These Lewis-type bonds constitute the cluster's structural framework, utilizing a total of 14 electrons. Figure 6a shows the AdNDP bonding scheme, affirming the alignment between seven CMOs and the seven 2c-2e single bonds on the  $B_8$  ring. The occupation numbers (ONs) are 1.90–1.93 |e|, which generally close to ideal value of 2.00 |e|. Subset (d) is the cluster's delocalized  $\pi$  framework, primarily sourced from the 2s/2p orbitals of B atoms (Table S2). The corresponding AdNDP bonding scheme allocates three delocalized  $\pi$  orbitals into three 11c-2e bonds, with an occupation value of 2.00 |e|. Three CMOs in subset (e) constitute a delocalized  $6\sigma$  subsystem, situated on the 8 B atoms. Subsets (d) and (e) each comprise 3 orbitals and 6 delocalized electrons, satisfying the  $(4n+2)$  Hückel rule ( $n=1$ ), establishing the cluster's  $\pi/\sigma$  dual aromaticity. In Subset (b), an Al-Al  $\sigma$  orbital aligns with AdNDP bonding principles. Corresponds to the AdNDP scheme in Figure 6a (right). In the TS structure, the CMOs, AdNDP scheme, orbital compositions virtually do not alter (Figure S3 and S4, ESI<sup>†</sup>), which explain why the dynamic fluxionality process has no energy barrier.

In summary, the chemical bonding of  $B_8Al_3^+$  cluster consists of the lone pairs of two Al atoms, a covalent Al-Al single bond, seven 2c-2e Lewis single bonds within the  $B_8$  ring, three 11-center delocalized  $\sigma$  and three 11-center delocalized  $\pi$  bonds, which establishes their two-fold  $6\pi/6\sigma$  aromaticity. This dual aromaticity collectively underlie the unique dynamic fluxionality for cluster.



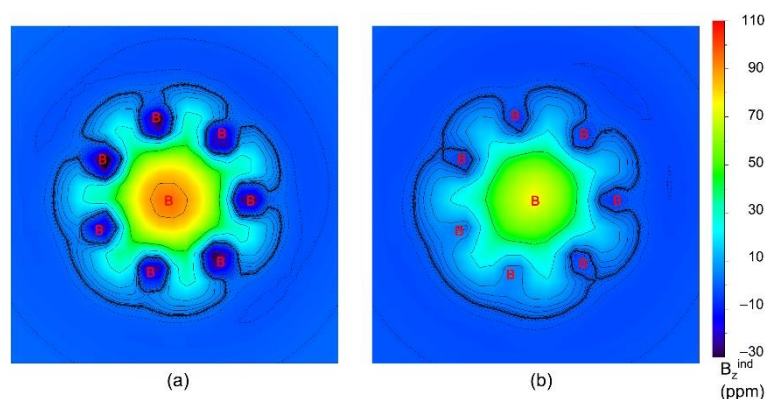
**Figure 5.** Pictures of occupied canonical molecular orbitals (CMOs) of GM  $B_8Al_3^+$  cluster. (a) Lone pairs. (b) Lewis-type Al–Al  $\sigma$  bond. (c) Seven CMOs for Lewis B–B  $\sigma$  single bonds along the periphery of disk  $B_8$  motif. (d) Three delocalized  $\pi$  CMOs. (e) Three delocalized  $\sigma$  CMOs.



**Figure 6.** AdNDP bonding scheme for GM ( $C_1$ ,  $^1A$ )  $B_8Al_3^+$  cluster. Occupation numbers (ONs) are shown.

To more intuitively observe the dual  $6\pi/6\sigma$  aromaticity, the color-filled maps of  $ICSS_{zz}$  of  $B_8Al_3^+$  cluster at 0 ( $ICSS_{zz}(0)$ ) and 1 Å ( $ICSS_{zz}(1)$ ) above the  $B_8$  ring plane are plotted in Figure 7. The green areas in (a) and (b) within the molecular wheel, in which the shielding effect is primarily concentrated, are in line with  $\sigma$  and  $\pi$  aromaticity of the cluster, respectively. Obviously, the  $[B_8]^{2-}$  unit has doubly  $6\pi/6\sigma$  aromatic, which is the key factor that causes the ground state to stabilize. In essence,  $6\pi/6\sigma$  double aromaticity of  $[B_8]^{2-}$  which is based on its charge-transfer as described previously. Nucleus-independent chemical shifts, NICS and  $NICS_{zz}$ , are calculated for GM  $B_8Al_3^+$  cluster as an additional criterion for aromaticity (Table S3, ESI). The large negative values are consistent with the assessment of  $\pi$  and  $\sigma$  double aromaticity. The NICS and  $NICS_{zz}$  values at the centre of a  $B_3$  triangle are actual helpful for understanding the aromaticity of GM  $B_8Al_3^+$ , whereas those at 1 Å below the plane probe  $\pi$  aromaticity. The electron clouds over the system are uniform and dilute facilitate dynamic fluxionality which are based on two-fold magic  $6\pi/6\sigma$  aromaticity.





**Figure 7.** The iso-chemical shielding surfaces (ICSSs) of GM B<sub>8</sub>Al<sub>3</sub><sup>+</sup> cluster. (a) ICSS<sub>zz</sub>(0) at the B<sub>8</sub> disk plane. (b) ICSS<sub>zz</sub>(1) at 1.0 Å below disk plane. For ICSSs, a positive value indicates aromaticity, and vice versa.

#### 4. Methods

The global minimum (GM) structure and low-lying isomers of the B<sub>8</sub>Al<sub>3</sub><sup>+</sup> cluster were determined through Coalescence Kick (CK) search and more than 5000 stationary points (3000 singlet and 2000 triplet) were detected on the potential energy surface with the help of artificial structure construction [31,32]. The candidate low-lying structures were subsequently reoptimized at the PBE0/def2-TZVP level [33,34]. Frequency calculations were carried out at the same level to ensure that the reported structures are true minima. To check for computational consistency of different functionals in structures and energetics, the zero-point correction energy was also calculated at the B3LYP/PBE0/def2-TZVP. In order to benchmark the relative energies, the top five low-lying isomers, were further assessed at the single-point CCSD(T)/def2-TZVP level on the basis of their PBE0/def2-TZVP and B3LYP/def2-TZVP geometries [35–37].

At the PBE0/def2-TZVP level, orbital composition analysis was completed through NAO calculations, and Wiberg bond indices (WBIs) and natural atomic charges were obtained through natural bond orbital (NBO) calculations [38]. Chemical bonds were elucidated using canonical molecular orbital (CMO) analysis and adaptive natural density partitioning (AdNDP) [39]. Nucleus independent chemical shifts (NICSSs), Iso-chemical shielding surfaces (ICSSs) were calculated to evaluate  $\pi/\sigma$  aromaticity [40,41]. AdNDP analysis and ICSSs calculations were done with the Multifwn program [42]. We performed e Born-Oppenheimer molecular dynamics (BOMD) simulations at a temperature of 300K to study the dynamic properties of the clusters [43]. All the above calculations are done using the Gaussian 09 software package [44]. The visualization of calculation results is completed through GaussView, CYLview and VMD programs [45–47].

#### 5. Conclusions

In summary, we have designed a cationic ternary boron-based binary B–Al cluster, B<sub>8</sub>Al<sub>3</sub><sup>+</sup>, which adopt three-layered structure can be seen as subnanoscale clock in shape with a quasi-planar B<sub>8</sub> wheel. And the Al<sub>2</sub> pointer that above the wheel and another aluminum atom under it. It features dynamic structural fluxionality at 300 K. Charge calculations suggest that the cluster can be described as a charge-transfer ion complex and formulated as [Al]<sup>+</sup>[B<sub>8</sub>]<sup>2-</sup>[Al<sub>2</sub>]<sup>2+</sup>, whose three charged layers are bound via quite strong electrostatic forces. BOMD simulation indicates that the Al–Al pointer can freely rotate on the dial below, requiring an energy barrier of 0.19 kcal mol<sup>-1</sup> to facilitate its rotation. Chemical bonding analyses indicate a magic  $6\pi/6\sigma$  double aromaticity of B<sub>8</sub>Al<sub>3</sub><sup>+</sup> cluster. The dual delocalized electron clouds create a fluid “orbital” that allows the Al<sub>2</sub> unit above the B<sub>8</sub> ring to rotate freely, thus imparting dynamism to the cluster. The balance of electrostatic traction and repulsion between layers are the critical contribution to the dynamic fluxionality of the cluster.

**Supplementary Materials:** The following supporting information can be downloaded at the website of this paper posted on Preprints.org, Table S1: Cartesian coordinates for optimized global-minimum (GM) and

transition-state (TS) structures of  $B_8Al_3^+$  cluster at the PBE0/def2-TZVP level; Table S2: Orbital composition analyses for occupied canonical molecular orbitals (CMOs) of GM ( $C_i$ ,  $^1A$ )  $B_8Al_3^+$  cluster; Table S3: Calculated NICS<sub>zz</sub> and NICS (shown in italics in brackets) of GM  $B_8Al_3^+$  cluster at the PBE0/def2-TZVP level. These values are calculated at the center of  $B_3$  triangle, as well as at 1 Å above the center; Figure S1: Alternative optimized structures for  $B_8Al_3^+$  cluster at the PBE0/def2-TZVP level including zero-point energy (ZPE) corrections, along with their relative energies. Relative energies are also presented for top five lowest-energy isomers at the single-point CCSD(T)/def2-TZVP//PBE0/def2-TZVP (in parentheses) and for top two lowest-energy isomers at the B3LYP/def2-TZVP (in square brackets, with ZPE corrections), and single-point CCSD(T)/def2-TZVP//B3LYP/def2-TZVP (in curly brackets) levels of theory. All energies are shown in kcal mol<sup>-1</sup>; Figure S2: Displacement vectors of the vibrational modes of (a) GM and (b) TS structures of the  $B_8Al_3^+$  cluster at the PBE0/def2-TZVP level; Figure S3: Pictures of occupied canonical molecular orbitals (CMOs) of TS  $B_8Al_3^+$  cluster. (a) Lone pairs. (b) Lewis-type Al–Al  $\sigma$  bond. (c) Seven CMOs for Lewis B–B  $\sigma$  single bonds along the periphery of disk  $B_8$  motif. (d) Three delocalized  $\pi$  CMOs. (e) Three delocalized  $\sigma$  CMOs; Figure S4: AdNDP bonding scheme for TS ( $C_i$ ,  $^1A$ )  $B_8Al_3^+$  cluster. Occupation numbers (ONs) are shown.

**Author Contributions:** Conceptualization, S.-J.G.; methodology, S.-J.G.; validation, S.-J.G. and T.-L.Y.; investigation, S.-J.G.; writing—original draft preparation, S.-J.G.; writing—review and editing, S.-J.G. and T.-L.Y. All authors have read and agreed to the published version of the manuscript.

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**Conflicts of Interest:** The authors declare no conflict of interest.

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