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Article

A New Paradigm in AC Drive Control: Data Driven Based Control by Learning of the High Efficiency Data Set. Generalizations and Applications to a PMSM Drive Control System

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Abstract: This paper presents a new means to control the processes, which involve the electric energy conversion. Electric machines fed by electronic converters provide the useful power defined by the inner product of two generalized energetic variables: the effort and the speed. The novelty of the paper idea is to control the desired energetics variables by a direct Data Driven Control (DDC) law in terms of the pair effort, speed and corresponding voltage controls of the electronic converter. It must be mentioned that the same desired useful power might be obtained with different controls at different efficiencies. The regularization problem was solved by selecting from a knowledge database, the maximum efficiency operation points. Knowing a reasonable number of optimal efficiency operation points, an interpolative Radial Base Function (RBF) control was built up. The RBF algorithm can find by interpolation the optimal controls for any admissible operation points of the process. The control scheme developed for this purpose has an inner DDC loop, that perform the converter control based on measured speed and demanded torque by the outer loop which handles the speed. A comparison of the DDC with the Model Predictive Control (MPC) schemas highlights the advantages of the new proposed control.

Keywords: data driven control (DDC); model predictive control (MPC); permanent magnet synchronous machine (PMSM); searching algorithm; radial basis function (RBF) neural networks (NN); interpolation technique.

1. Introduction

Electric Drive Systems (EDSs) have getting a real interest in the least decades by developing advanced technologies in digital processors, signals proceedings and power systems. The main benefits provide by developing EDSs can be summarized as follows: fast transients, high power density, large range of speed and power, low cost, safety operation, robustness, modular components etc.

Increasing number of EDSs applications (see automotive) implies new control techniques to improve the performances of the energy conversion process. Firstly, the efficiency improving of the EDSs can be done from the conception phase, when there is selected the Permanent Magnet Synchronous Machine (PMSM) that presents a high efficiency as a consequence of the using of modern technologies of manufacturing of permanent magnets. Secondly, the increasing of the EDSs with PMSM may be obtained by using an adequate optimal control law designed by a certain methodology.

The traditional control strategies are based on the physical equations of the process model, for example the common used in EDSs are: Field Oriented Control (FOC) with the mathematical model in an appropriate coordination frame which it is used by an adequate decoupled control changes for torque and flux, the loops being usually designed with classical PI linear controllers [1,2], Direct

Torque Control (DTC) – a bang to bang control implemented by hysteresis controllers [2] and Model Predictive control (MPC) which uses a future control sequence obtained by the process model predictor in the aim to find the best control law sequence by minimising a known objective function [3].

The specific particularity of the advanced EDSs is that the input voltage and frequency are not directly applied from the power grid, which presents fixed values. The command is obtained by using a power interface represented by a power electronic inverter, which allows the giving variable values of voltage and frequency for obtaining the imposed performances [4]. This task is crucial for meet the advanced results, which can improve the close loop performance of the EDSs [5,6].

In the last years, the MPC control strategy has been extensively developed and improved, being an actual motivation for research and industry [7-11]

]]. More advanced studies are dedicated to improve the control results, taking into account the nonlinear magnetic circuit [12], advanced optimization method [13], robustness [14] or fault tolerant capability [15], respectively. However, MPC strategy is strongly based on the model of the process, which in practice can differs from the one of the real system, leading to the worsening of the control performances.

In EDSs, the Artificial Intelligence Methods (AIMs) are well approached on control system. Thus, the torque minimization was successfully obtained by using Neural Network (NN) method [16], the Radial Basis Function Proportional-Integral-Derivative (RBF-PID) controller developed in [17] leads to improve the tracking results and an iterative learning control strategy reduce the torque ripple [18]. More advanced AIMs can be founded in the survey [19].

The Reinforcement Learning (RL) is an advance popular framework used to control systems and devices in a wide range of applications because of its ability to autonomously find control policies to achieve a desired goal without assuming that the environment are known. Thus, in [20] it is proved that the actual methods of deep RL leads to obtain a suitable control structure of the adaptive controller. Further, a low-complexity gradient descent solution with backtracking iteration approach for MPC Quadratic Programming (QP) problem leads by minimizing to reduce the number of the searched control inputs and improve the control performances [21]. In spite of the various benefits obtained by AIMs, these control advanced algorithms require a large amount of hardware and software resources.

A new trend in the control theory applications is based on data-driven control (DDC) that discusses the transition from Model-Based Control (MBC) applications to Model-Free Control (MFC) adaptive structures, involving the learning in a given control framework context [22–25]. The DDC method is an advanced strategy that can learn the dynamics [26], or can let to obtain different formulations via regularizations and relaxations methods, bridging the direct and indirect data driving control [27]. Indirect data driven control is formulated as bi-level optimization problem. That is, first a model fitted from the data in the inner identification, before the model is used to control the outer problem. Model is used for many reasons: first is the availability of powerful analysis and design of the control methods. Another advantages is that the models are very compressed compared to the data driven representation. At least, for more details about stabilization, optimality, and robustness behavior of DDC see [28].

Also, it can be mention that there can be obtained predictive control applications, which are directly obtained from the data set, which does not include all the main features of the classical predictive control strategy, as: integrator that ensure a offset-free control, the constraint handling, feed forward action, and disturbance control model, which make the strategy to be more versatile for real-time applications [29]. Furthermore, an algorithm designed for control an unknown stochastic linear time-invariant systems illustrate the high closed-loop performance obtained by data-enabled predictive control strategy which has a novel robust distribution [30]. A simultaneous MPC and DDC strategy with relaxed assumption on the model in a proper framework shows how a no convex optimal problem is transformed into a one with convex constraints [31]. The input-mapping based data-driven model predictive control is successful used for systems with bounded disturbance [32] or for advance learning [33]. For generalization, in [34] is discussed a data-enabled predictive control

parametric algorithm that combined the identification method obtained by a learning procedure and a control one of the dynamical systems, resulting in an equivalent MPC formulation, which is valid for both linear time-invariant system, which is directly applied, and for nonlinear systems, that requires a regularization procedure.

As expected, an emerging technology on control system development may be based on both DDC and MPC strategies. Although, EDSs with represent a rapid process for control applications, with the help of the advance sensors and adequate numerical signal processing there can be collected and processed a large amount of data that is sufficient for implementing the DDC solution. Thus, based on White-Box (WB) modeling estimation by least squares technique, in [35] a DDC-MPC method is proposed for current controlling of PMSM, that leads to compensate the modeling errors and, to improve the control performance for both dynamic and steady-state regimes. In relatively recent paper [36,37], it has been shown the transition from the classical model-based approach towards data-driven optimal control strategies, which take into account the model predictive control paradigm, leading to develop the data-enabled predictive control. At least, in the reference [38] it is shown that a fractional PI controller for a PMSM drive can be obtained by a DDC algorithm in certain practical conditions.

MPC strategy and then recently starting by DDC have done many successfully solved problems. An important issue in the EDSs with PMSM is related on the efficiency improving by control means. In literature [39–41] can be founded various solution for improving the efficiency of EDSs with PMSM. Most of them are based on the modeling of the power losses with algebraic relation, taking into account some specific constants of materials. The minimize of an analytic cost function with constraints will give the optimal solution that ensures a high efficiency. This approach has an elegant mathematical description, but also many limitations: the constants of the materials depend of the magnetic/electric fields, there are losses that cannot be modeled analytically (abnormal losses) and many methods are designed for partial losses.

Finally, there is an extensive literature focusing on the MFC strategy (philosophy). Research started early in 1956 through the project [42] *"A proposal for the Dartmouth Summer Research Project on Artificial Intelligence"* by J. McCarthy, Dartmouth College, M. L. Minsky, Harvard University, N. Rochester, IBM Corporation, C. E. Shannon, Bell Telephone Corporation. It is concluded in this research project: *"if a machine can do a job, then an automatic calculator can be programmed to simulate the machine"*. Paraphrasing we can say mutatis mutandis: *if a classic automatic control based on a physical model can control a process, then an informatic system can control the same process without a physical model*. This is the main philosophy followed in the paper to show how a MBC strategy offers good enough possibilities to develop a MFC in certain energetic constraint. The addressing paper made a transion from the MBC to MFC in the DDC paradigme for high performance objective.

For a large set of the phisical processes the main controlled quantities are effort and flow. Their product represents the useful power. In the paper we develop a new technique to find adequate controls of the effort and flow in terms of maximum efficiency, that is the minimum losses. These appropriates controls are extracted from an aprioric DataBase (DB) in terms of required effort and measured speed. The aprioric DB contains mainly the steady state measurements in the open loop tests for: the speed, the effort and the corresponding controls. An RBF interpolativ system is trained so that, based on an few set of the optimal experimental data, to extract the controls for any desired speed and flow. In the on line operation of the process the initial DB is adaptive. An on line optimisation system search the new optimal controls when the process parameters are changed. DB are free from process parameters and in consecace from the process model.

The paper shows that an informatic system based on an experimental database, without knowing the parameters of the process, can do the same job as a MPC control system with multiple advantages. Thus, we propose a new combined linear PID and DDC, where the control variables are directly obtained from an experimental database by a RBF methodology. The key of DDC is to find the relation of the energetic variables with the control variables, by a RBF -NN interpolative surfaces. These surfaces are built with a set of the optimal experimental support points extracted from a large knowledge database.

In the following, we demonstrate that the proposed combined linear PID and the RBF-NN methodology can successfully dynamically simulate EDSs with PMSM, controlled by the MPC methodology, without knowing any parameters of the motor or driven process.

Respecting the state of art, in the paper there are proposed the following new contributions:

- (i) A new combined linear and DDC control methodology that uses the process control variables obtained from an experimental database built by a RBF methodology.
- (ii) In the case of the EDSs, the combined control methodology is in terms of an outer time domain PID control of speed and an inner implicit RBF control loop.
- (iii) The inner control loop is based on an experimental database, which contains the optimal controls corresponding to any speed and torque of process operation points. The control law is in implicit form that is a set a steady state process operation points.
- (iv) The RBF methodology compresses the set of all admissible operation points by network architecture, with a few optimal data basis functions.
- (v) We present a novel control scheme in which the demanded effort by the PI controller and measured speed are the input for the RBF inner loop. The output of the inner loop is the inverter's modulator input, which select the proper inverter's voltage vector sequence of the inverter.
- (vi) The inner RBF control loop is adaptive, that is the inverter control is temperature dependent because the parameters of the process changes with motor is temperature.

The organization of this paper is structured as follows. Thus, in the Section II is presented how is obtained a data free control algorithm based on the physical modeling of the processes. The section III is dedicated to DDC of AC drives, where the illustrative application of PMSM drive control is done. The comparative results obtained by MPC and DDC techniques are presented in Section IV. At last, in Section V there were summarized the main benefits obtained by the proposed novelty control method.

2. Problem Statement. From Classical Physical Modeling of Energy Conversion Flow to Data Free Model Control

2.1. Problem Statement

The energy conversion flow is an essential objective for ensuring of the social and economic stability. In industry and residence, many applications are designed to deal with the macroscopic energy conversion that implies three main types of fields: electromagnetics, mechanics and thermodynamics (Figure 1).

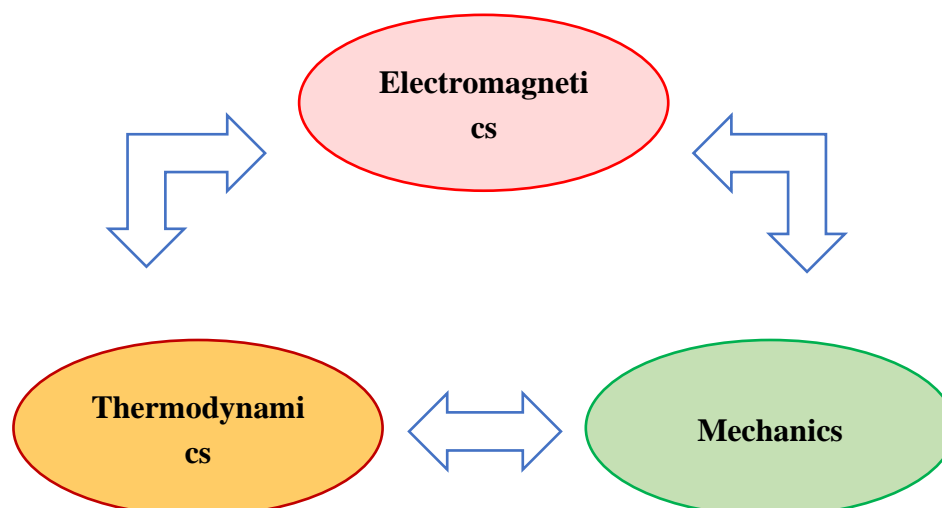


Figure 1. The diagram of the macroscopic energy flow conversion.

Starting from these energy conversion possibilities, in practice there can be developed different conversion processes subject of adequate constraints.

In the various physical processes like electrical, mechanical, hydro- or thermal, the desired useful work is universally characterized by a pair of energetic variables: the effort $e(t)$ and flow $s(t)$. The inner product of these generalized variables is the instantaneous useful power:

$$p_2(t) = e(t) \cdot s(t). \quad (1)$$

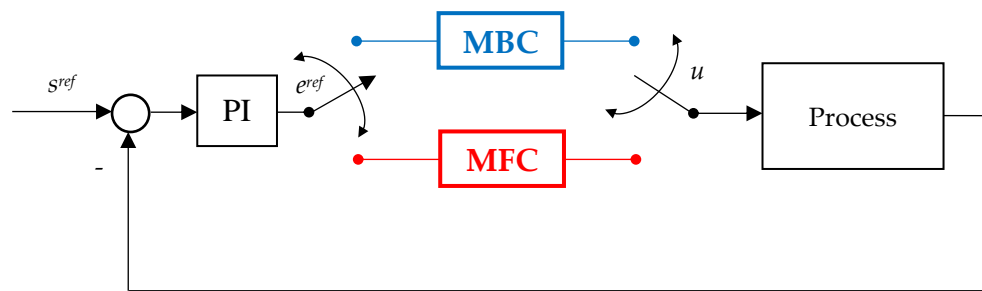
The different forms of primary power $p_1(t)$, can be converted in useful forms by various means. Let be η the efficiency of the power conversion process. Then, primary power $p_1(t)$ is easily obtained:

$$p_1(t) = p_2(t) / \eta. \quad (2)$$

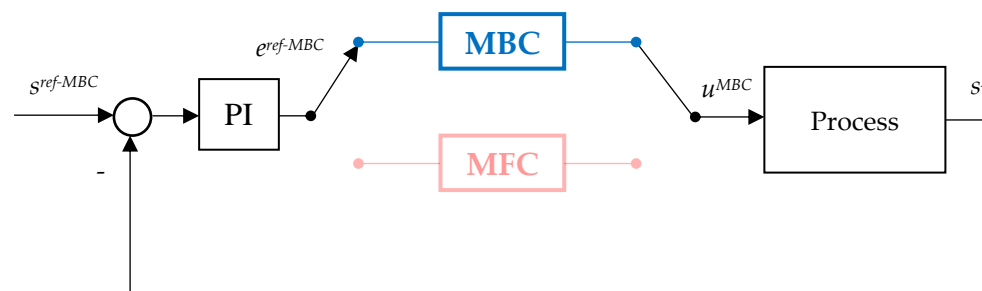
If, for example, we refer to a mechanical process of motion which develop a useful force f_u and a linear velocity v , the motion being described in external (cartesian) coordinates, then we have $e = f_u$, and $s = v$. If the motion is rated to the drive motor shaft, then $e = m$ and $s = \omega$, where m is the developed torque and ω the angular speed. In the case of an electrical process, the electrical voltage represented in the complex domain, $e = \underline{u}$ and the corresponding current $s = \underline{i}$. Similarly, in the case of Hydro, Ventilation, Air Conditioning (HVAC) processes, the pressure $e = P$ and the flow rate $s = Q$.

Usually, the above energetic macroscopic process are well-modeled by the actual intrinsic physical theories. In the control theory, the using of this model with lumped parameters have some vulnerabilities: high sensitivity to parameter variations, incomplete modeling of some loss components, linearity on a small range, low control accuracy at high frequencies etc. However, the analytic modeling has the advantage of simplicity, being in many approaches a starting point in the developing of advanced control methods.

The transition from MBC to model MFC is illustrated in Figure 2. For this aim it is considerate a combined PI and inner control (cascaded or not) for a given process described by adequate physical model equations.



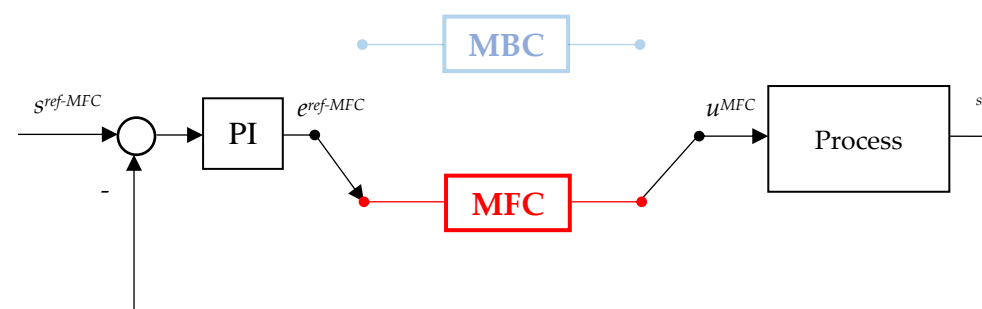
a) The basis control scheme.



b) Stored data from MPC running.



c) Designing of MFC strategy: training phase



d) Designing of MFC strategy: testing phase

Figure 2. The transition from MBC to MFC.

The inner control is switched from MBC to MFC whenever is necessary, giving on the output the control u as is suggested in Figure 2(a).

In the first stage exposed in Figure 2(b), the inner control is switched to MBC. At this step, there selected a collection of the main data in steady-state regime that corresponds to the high efficiency, grouped in:

$$\mathbf{d}^{MBC} = \begin{bmatrix} u^{MBC} & y^{MBC} & e^{MBC} & s^{MBC} \end{bmatrix}^T, \quad (3)$$

where has been considerate that in steady-state regime we have $e^{ref}=e$.

Now, the next step is the designing of the MFC controller. This controller has a interpolative-adaptive structure with a variable structure, being able to learn from MBC data, having as input the data stored (3) in a sufficient number, and the output u^{*MFC} as is shown in Figure 2(c). The MFC algorithm is trained in a open structure, and has the ability to learn from the experience given by MBC

Having closed the training phase of MFC, the testing phase is done in the close loop structure as is indicated in Figure 2(d).

The transition from MBC to MFC depends of the process that is subject of control strategy. This procedure may be applied to the process with complex, nonlinear and multivariable structure.

2.2. The DDC Strategy of the Energy Conversion Process

The MFC technique represents a modern approach with a large applicability in practice. From MFC control techniques, a particular direction are described by DDC strategy which is developed in the following.

The numerical processing of the signals that refers to the training phase are carried out with the MBC strategy, which is why the MBC acronym will be ignored in the symbolization of signals, distinguishing between the acronyms DDC and MPC whenever is necessary.

The state model of this nonlinear deterministic conversion processes is described by:

$$\begin{cases} \dot{\mathbf{x}} = \mathbf{f}(\mathbf{x}(t), \mathbf{u}(t), \boldsymbol{\theta}(t)) \\ \mathbf{y} = \mathbf{g}(\mathbf{x}, \mathbf{u}) \end{cases} \quad (4)$$

The state \mathbf{x} , control input \mathbf{u} and output \mathbf{y} , respectively, are restricted to the sets of adequate dimensions: $\mathbf{x}(t) \in \mathbf{X} \subset \mathbb{R}^N$, $\mathbf{u}(t) \in \mathbf{U} \subset \mathbb{R}^M$ and $\mathbf{y}(t) \in \mathbf{Y} \subset \mathbb{R}^P$. Further, in the vector $\boldsymbol{\theta}(t)$ there are comprised the parameter of the process. The nonlinearity of the state model (3) is emphasizes by the nonlinear functions \mathbf{f} and \mathbf{g} .

Let us to adopt the following outputs variables:

$$\begin{aligned} \mathbf{y} &= \begin{bmatrix} e & s & p_1 & p_2 \end{bmatrix}^T \\ h(\mathbf{x}, \mathbf{u}) &= p_1 \end{aligned} \quad (5)$$

By usually discretizing techniques, the corresponding discrete state space model of the plant (4) becomes:

$$\begin{cases} \mathbf{x}(k) = \mathbf{f}(\mathbf{x}(k-1), \mathbf{u}(k-1), \boldsymbol{\theta}, T_s) + \boldsymbol{\xi} \\ \mathbf{y}(k) = \mathbf{g}(\mathbf{x}(k), \mathbf{u}(k)) \end{cases} \quad (6)$$

where the discrete states $\mathbf{x}(k)$, control inputs $\mathbf{u}(k)$, and outputs $\mathbf{y}(k)$ are matrices of appropriate sizes.

Also, in (6) $\boldsymbol{\xi}$ is the discrete noise of the process, while T_s represents the sampling time period.

The control problem to be solved is defined according to: seek for a control $\mathbf{u}(t)$ that will bring a desired useful work:

$$E_2(t) = \int_{t_0}^{t_1} p_2(t) dt, \quad (7)$$

when the input of the system is supplied by the energy:

$$E_1(t) = \int_{t_0}^{t_1} p_1(t) dt, \quad (8)$$

with a natural condition resulted from (2):

$$E_1(t) = E_2(t) / \eta \Big|_{\eta < 1} \Rightarrow E_2(t) < E_1(t), \quad (9)$$

such as for any other control $\hat{\mathbf{u}}(t)$, which also bring the same work E_2 , the energy E_1 is larger:

$$\int_{t_0}^{t_1} \mathbf{h}(\hat{\mathbf{u}}, \mathbf{x}) dt < \int_{t_0}^{t_1} \mathbf{h}(\mathbf{u}, \mathbf{x}) dt. \quad (10)$$

In other words, we assume that for a given desired pair of the generalized variables $e(t)$ and $s(t)$, there exist a bounded control $u(t)$ and a bounded cost criterion, which can be expressed either in a continuous set formulation:

$$\mathbf{C}_c = \left\{ \int_{t_0}^{t_1} \boldsymbol{\varepsilon}^2 dt; \int_{t_0}^{t_1} \mathbf{h}(\mathbf{u}, \mathbf{x}) dt; THD_e \mid E_2(t) = cst. \right\}, \quad (11)$$

or in a discrete representation:

$$\mathbf{C}_d = \left\{ \sum_{k=1}^N \boldsymbol{\varepsilon}^2(k) T_s; \sum_{k=1}^N \mathbf{h}(k) T_s; THD_e \mid E_2(k) = cst. \right\}, \quad (12)$$

where there has been used the mean square error: $\boldsymbol{\varepsilon}^2 = (e^{ref} - e)^2 + (s^{ref} - s)^2$.

Also, in the cost formulation (11)-(12) there is used the Total Harmonic Distorsion THD factor that is a measure of harmonic distortion, computed by:

$$THD_e = \frac{\sqrt{\sum_{n=2}^{\infty} E_{n,RMS}^2}}{E_{f,RMS}}, \quad (13)$$

where $E_{f,RMS}$ and $E_{n,RMS}$ represent the Root Mean Square (RMS) values of fundamental and harmonics components of the effort e , respectively.

For the same desired work (7) the final cost \mathbf{C} which is lower, has better control u . The interval (t_1-t_0) length is a time window with the required energy E_2 (6), where $t_{1/0}$ represents the end/start time.

It can be mention that the input power may be either positive $p_1 > 0$ or negative $p_1 < 0$, as the power is delivered or received by the process.

The first term from (11)-(12) refers at the control quality in the control horizon N length and the second terms, respectively, refers to the input energy.

The numerical computation has a large apicalbility in data computation. For our approach we define cost – solving problem based on (12) as follows:

$$\begin{aligned} \mathbf{C}_{\min} &= \arg \min_{\mathbf{u}, \mathbf{x}} \mathbf{C}_d \\ \text{s.t. :} & \begin{cases} E_2 = cst. \\ \eta(k) = \max \end{cases}, \end{aligned} \quad (14)$$

where the constraints E_2 and η ensure the uniqueness of the optimal cost problem.

The process model (4) is in time domain, having an explicit form. A more convenient approach is developed in the following.

We introduce the implicit control law:

$$\begin{cases} \mathbf{G}(\bar{\mathbf{y}}, \bar{\mathbf{u}}) = 0 \\ \bar{\mathbf{y}} = [e \quad s]^T \end{cases}. \quad (15)$$

In the model (15) the output of the process $\tilde{\mathbf{y}}$ was reduced in terms of the generalized variables pair (e,s) , and the corresponding input is $\tilde{\mathbf{u}}$. In consequence, the output variables p_1, p_2 are free, being unconstrained, which shows the control law \mathbf{G} is not unique. A regularization procedure is effectuated by selecting from the set (e,s) corresponding to the maximum efficiency power operation points.

The command law of the process results from the explicit model (15):

$$\begin{cases} \mathbf{u} = \mathbf{F}(e, s) \\ \mathbf{F} = \mathbf{G}^{-1} \end{cases} \quad (16)$$

Let consider a time window $[t_0, t_1]$ for requested output trajectories of the both generalized variables:

$$\begin{cases} g_1(t) = e(t) \\ g_2(t) = s(t) \end{cases} \quad t \in [t_0, t_1]. \quad (17)$$

By eliminate the time from relations (16) we have the implicit representation:

$$f_e(e, s) = 0. \quad (18)$$

Each discrete point kT_s , with $k=1, \dots, N_{obs}$, where N_{obs} is the number of observations points, on the trajectory (17) in the generalized variables (e, s) plane, has the input controls which represents the supports points for the control surfaces:

$$\begin{aligned} \tilde{\mathbf{u}}(k) &= \mathbf{f}(e(k), s(k)) \\ \tilde{\mathbf{u}} &= [\tilde{u}_1 \quad \tilde{u}_2] \\ \mathbf{f} &= [f_1 \quad f_2] \end{aligned} \quad (19)$$

The surfaces (19) in the continuous domain represent the endless set of steady state operation points. Any stable operating point (e,s) is correlated with the corresponding's controls (u_1, u_2) . A trajectory of motion (16) in the permissible range, beginning in a stable initial state (e_0, s_0) and reaching the final state (e_f, s_f) , passes through an countless set of intermediate energy states, since in classical physics it is admitted that states of physical processes can vary only continuously. By using digital process control techniques, the set of states travelled from the initial state to the final state becomes countable due to sampling operations. An exhaustive condition of stability of process controlled by the two fundamental energy quantities, effort e and velocity (flow) s is as follows: if the speed control loop is stable in the sense that the required effort e^{ref} is on the control surfaces (19), the operating points on the motion path will be stable. Through the sampling process, stability is reduced, the longer the sampling period.

Generalizing we can say that the multivariable control law (19) can be generated with the required precision, by means of a known set \mathcal{M}_F of operating points of the process:

$$\mathcal{M}_F = [\tilde{\mathbf{y}} \quad \tilde{\mathbf{u}}]^T. \quad (20)$$

Through an interpolation algorithm \mathcal{A}_F associated with the \mathcal{M}_F database, for any current value $\tilde{\mathbf{y}} \in \mathbf{Y}$, a value $\tilde{\mathbf{u}} \in \mathbf{U}$ is generated which approximates the control law $\mathbf{F}(\tilde{\mathbf{y}})$ relation (15), so that:

$$\tilde{\mathbf{u}} = \mathcal{A}_F(\tilde{\mathbf{y}}). \quad (21)$$

The control law is determined by means of an experimental data set \mathcal{M}_F and some continuity and smoothing properties of the surfaces (15), which are specific properties of energetic inertial processes.

In summary, the control law has the form:

$$\begin{aligned} \tilde{\mathbf{u}} &= \mathcal{A}_F(\tilde{\mathbf{y}}), \\ \tilde{\mathbf{u}}, \tilde{\mathbf{y}} &\in \mathcal{M}_F \end{aligned} \quad (22)$$

with properties:

$$\begin{aligned} \tilde{\mathbf{u}}(k) &= \mathcal{A}_F(\tilde{\mathbf{y}}(k)), \quad \forall (\tilde{\mathbf{u}}(k), \tilde{\mathbf{y}}(k)) \in \mathcal{M}_F, \\ k &= 1, 2, \dots, N_{obs} \end{aligned} \quad (23)$$

The RBF-NN is largely used in control system [1]. A typical RBF-NN structure used for obtaining the input plant command is depicted in Figure 3.

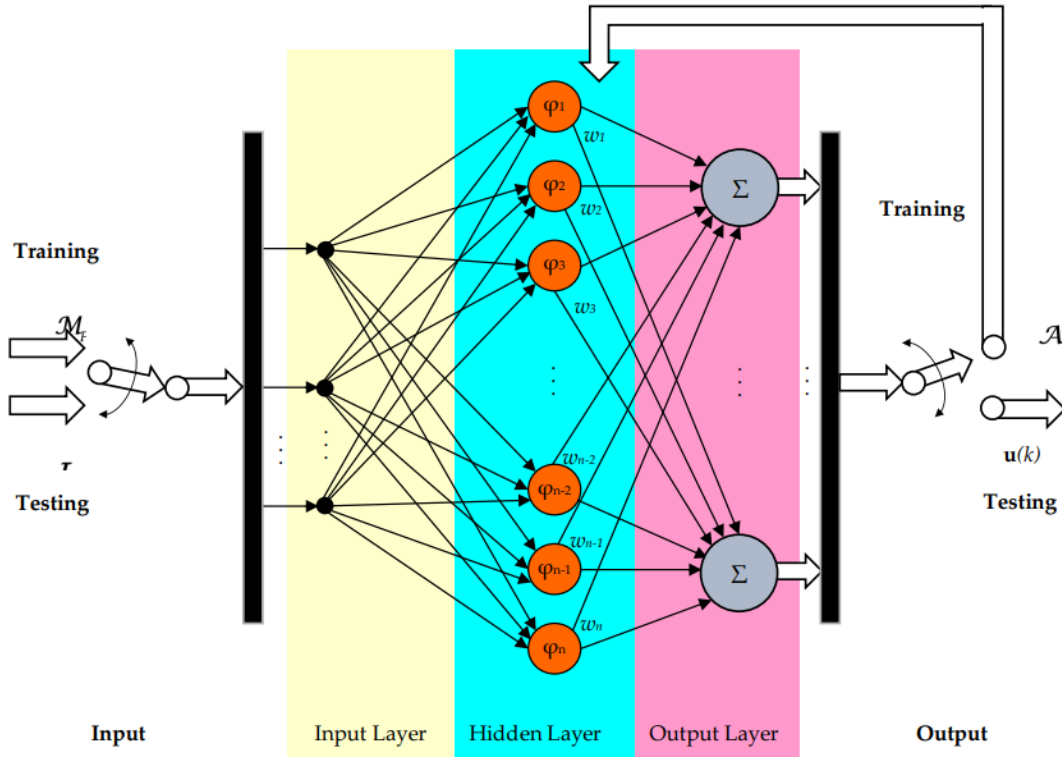


Figure 3. The RBF-NN used for obtaining the plant input.

The RBF-NN is used for two objectives, as training and testing:

$$\begin{aligned} \text{Training: } \mathcal{A}_F &= \text{RBF}(\mathcal{M}_F) \\ \text{Testing: } \mathbf{u}^{\text{RBF}}(k) &= \text{RBF}(\mathcal{A}_F, (e(k), s(k))). \end{aligned} \quad (24)$$

← Input ← Output →

where by RBF has been denoted the function of the neural network.

Having a classical structure, the RBF is organized in three levels of layers as input, hidden and output, respectively. Moreover, the weights obtained in the testing step are grouped in:

$$\mathcal{A}_F = [w_1 \ w_2 \ \dots \ w_{n-1} \ w_n]^T. \quad (25)$$

The output of the RBF-NN is given by a linear combination:

$$\mathbf{u}^{\text{RBF}}(k) = \mathcal{A}_F^T \boldsymbol{\varphi} = w_1 \varphi_1 + w_2 \varphi_2 + \dots + w_n \varphi_n, \quad (26)$$

where the activation function is given by Gaussian distribution

$$\varphi_i = e^{-\frac{\|x_i - \mu_i\|^2}{\sigma_i^2}}, \quad i = 1, n. \quad (27)$$

having the parameters σ and μ which are the basis width vector and center points of Gaussian function, respectively.

Also, the input Gaussian function is represented by set:

$$I = \{\mathcal{A}_F, e^{ref}(k), s(k)\}. \quad (28)$$

Enhancing the RBF depicted in Figure 3, in Figure 4 is illustrated the combined control structure of a generic process, that involves an outer explicit flow control loop and a inner multivariable data driven control loop.

The fundamental operation key of the DDC schema is the knowlage database. This database contains a large set of process operation points, from which are limited steady-state ones. In the block scheme from Figure 3, the actual values $\mathbf{d}^{MBC}(k)$ of control, output, effort and flow is comprised in the set:

$$\mathbf{d}^{MBC}(k) = [\mathbf{u}(k) \quad \mathbf{y}(k) \quad e(k) \quad s(k)]^T, \quad (29)$$

where $\mathbf{y}(k)$ is the output of the process, and N is the number of collected data.

The next task is to select a sufficient number of steady-state points $\mathbf{d}^{\circ MBC}(k)$ from all the operation points from $\mathbf{d}^{MBC}(k)$,

$$\mathbf{d}^{\circ MBC}(k) = [\mathbf{u}^{\circ}(k) \quad \mathbf{y}^{\circ}(k) \quad e^{\circ}(k) \quad s^{\circ}(k)]^T, \quad (30)$$

with:
$$\begin{cases} \mathbf{d}^{\circ MBC}(k) \subset \mathbf{d}^{MBC}(k) \\ \frac{\partial \mathbf{d}^{\circ MBC}(k)}{\partial t} \equiv \mathbf{0}(k) \\ \mathbf{0}(k) = [0(k) \quad 0(k) \quad 0(k) \quad 0(k)]^T \end{cases},$$

For obtaining the sufficient number of steady-state points contained in the set $\mathbf{d}^{\circ MBC}(k)$, the operator used for data extraction will be symbolized by “ \circ ”.

Supplimentary, as input data, there are considered the aprioric informations included in the set:

$$\mathcal{K}_{db} = \{\mathbf{R}_N; \mathbf{E}_N; \mathbf{H}_N\}, \quad (31)$$

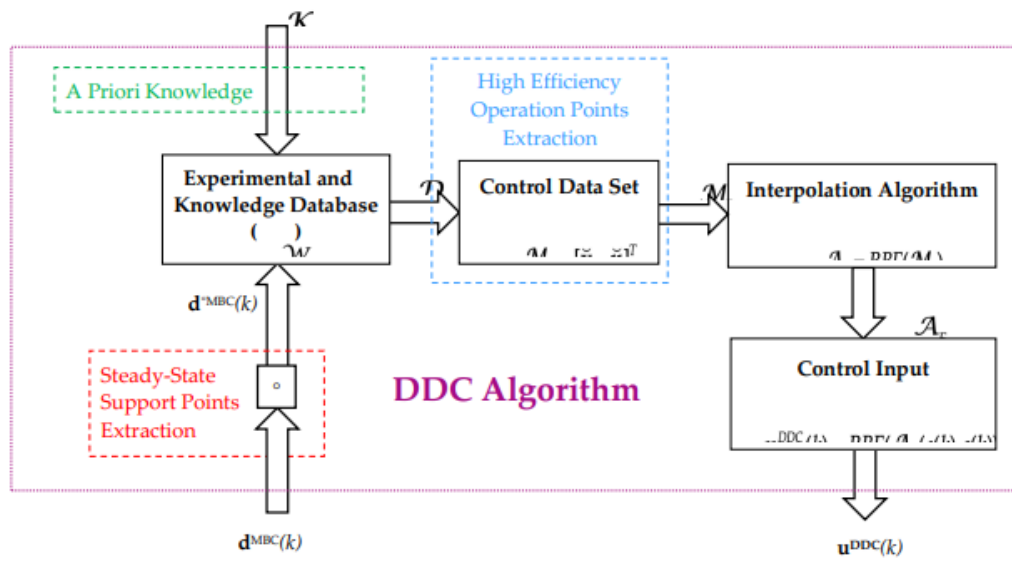
where: rated specification of the process are contained in the set \mathbf{R}_N , environment and design requirments which are contained in the sets \mathbf{E}_N and \mathbf{H}_N , respectively.

The input control data set will be computed based on both aprioric information and process data. In fact, the design of the required database is quite complex, and will be presented in the next section for the case of a concrete application. However, stating from the inputs of knowledges \mathcal{K}_{DB} and data $\mathbf{d}^{\circ}(k)$ the output of the database is

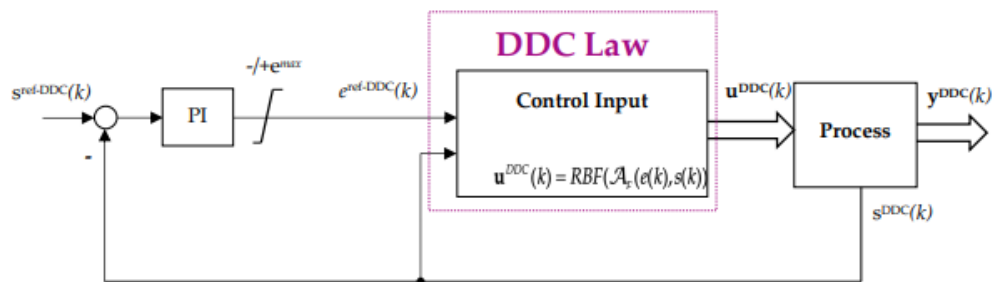
$$\mathcal{D}_F = \mathcal{W}\{\mathcal{K}_{db}; \mathbf{d}^{\circ MBC}(k)\}, \quad (32)$$

where by \mathcal{W} has been represented a numerical operator used for data processing in the database.

The proposed PI and combined DCC structure is illustrated ub Figure 4.



a) Designing of DDC strategy: training phase.



b) Designing of DDC strategy: testing phase.

3

Figure 4. A combined control structure with linear PI outer control loop and DDC inner control.

The training phase designing of DDC strategy is depicted in Figure 4(a), where are highlighted the main steps of DDC algorithm, while the testing phase made in close loop structure is represented in Figure 4(b).

The DDC control structure from Figure 4(b) is desined for tracking the output of the process $s^{\text{DDC}}(k)$ to its reference $s^{\text{ref-DDC}}(k)$ by using a linear PI controller, having the output $e^{\text{ref-DDC}}(k)$ bounded into the limits $-/+e^{\text{max}}$.

The control data set \mathcal{M}_f contains the maximum efficiency operation points selected from the knowledge database. The interpolation algorithm \mathcal{A}_f find the actual control $u(k)$ based on demanded effort $e(k)^{\text{ref}}$ and the measured flow $s(k)$.

We assume that all points \mathcal{M}_f (19), also referred as nodes, or “support points” are distinct and not collinear. Due to the intrinsic nature of the energy conversion process, the DDC law (15) is geometrically represented as continuous differentiable surfaces which allows to find an interpolation algorithm \mathcal{A}_f such that these surfaces passes exactly through each experimental points \mathcal{M}_f (18). The maximum efficiency operation points (e,s) is selected from the knoulogy database by a grid (direct) search method. These methodology involve setting up of grids in the input space (e,s) and evaluating the power efficiency of each grid point. The operation point that corresponds to the maimum efficiency was considered the best solution.

Two interpolation methods that are widely used in different application fields (in areas such as computer graphics, physical modeling, geographic information systems, medical imaging, and more), have been adopted. We used two basic methods: Delaunay triangulation and related methods and RBF-NN interpolation.

Let be a set of data and we want to find a rule which allows us to deduce information about the process we are studying at locations different from those at which we are obtained our measurements.

The interpolated value of a point, other than support points, was obtained by local interpolation techniques with the three nearby points. One widely used approach is Delaunay triangulation of data and the Voronoi diagram of a set of points, which is the dual of the first approach (Delaunay triangulation).

The RBF network has its origin in performing the interpolation of a set of data points in a multidimensional compact domain to an arbitrary accuracy, given sufficient number of data points. It has a network architecture with weighed basis functions. The solution is optimal by minimizing a functional containing a regularization terms. The RBF method compresses a very large volume of data, with the help of a much smaller number of weighted basic functions in the training process. In the exam (assessing) stage, the RBF network returns any point in the field covered by the data used in the training stage by an interpolation process of the weighted basis function. The discrete model of the control law is practically non-inertial, because the control $u(k)$ at the current step k is obtained by accessing the fast interpolation algorithm \mathcal{A}_f :

$$\begin{aligned} \mathbf{u}(k) &= \mathcal{A}_f(\mathbf{y}(k)), \\ k &= 1, 2, \dots, N, \\ N &= T_d / T_s, \end{aligned} \quad (33)$$

where T_d is the desired final time of the motion trajectories.

The new control methodology of the energy conversion process in terms of the effort and flow was represented in Figure 4. The objectives (10)-(11) are accomplished by two control loops: a MIMO inner control loop in terms of desired effort $e^{ref}(t)$ and measured flow $s(t)$ and an outer classical PI speed control loop.

3. The DDC of AC drive. Illustrative Case Study: The DDC of a PMSM Drive System

The control method proposed in the previous section has the ability to offers a new alternative of the classical methods which are based on the model accuracy. The novel approach is model free, being suitable for a large class of applications.

In the following, we begin with the principle of the DDC scheme applied to AC drives. Afterwards, there is done an illustrative application for a PMSM driving systems controlled according to the methodology developed in this paper. As MBC method has been selected the MPC strategy due to benefits of providing an optimal solution without any frequency modulator.

3.1. The DDC Principle of AC Drives

AC drives are founded in a large area of applications due to their high-performances resulted in dynamic regime.

Usually, the cascade control structure of AC drives is used to separate the different dynamics of electrical and mechanical parts, respectively, and then to have an independent control of each loop.

In addition to the advance control law, an important attention is paid for the electronic power inverter used to obtain the voltage supply. This aspect will be largely approached in the following sections.

This section is dedicated to the DDC principle applied to AC drives.

As mention in the second section, the DDC method is based on a learning technique. For our approach, the learning is based on the collected data from MPC strategy running.

The stages on DDC design are illustrated in Figure 5.

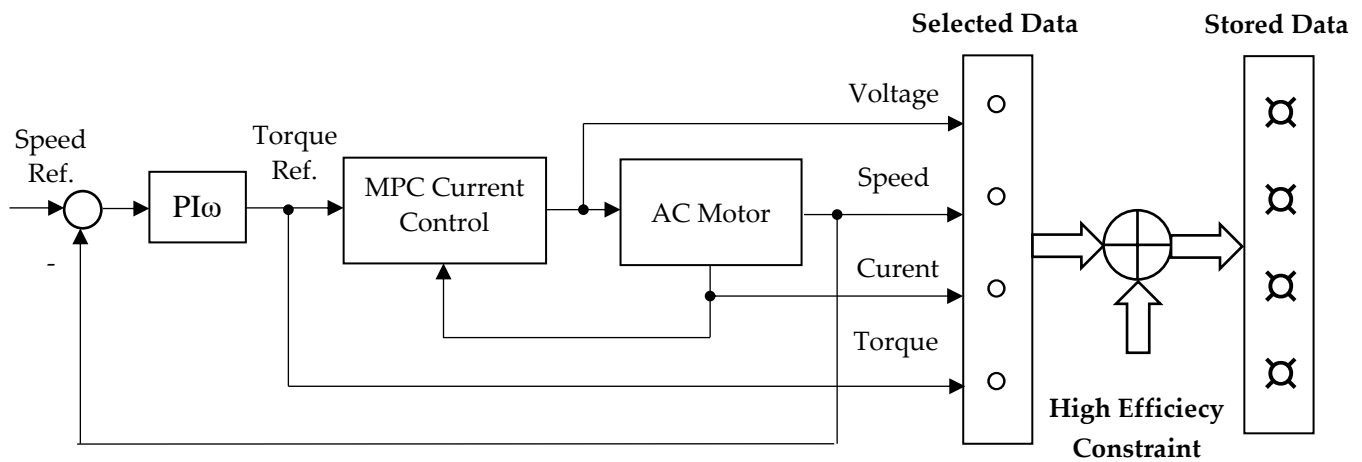
It is starting from a cascade structure, having the well-known quantities: speed (actual and reference), torque (reference), voltage and current (components). A brief description of each stage can be done as follows:

- a. Stage I: Stored data from MPC cascade control running. In this stage there are selected a limited data obtained from MPC cascade running in steady-state regime for: speed, torque, voltage and current. Further, from this there is imposed the constraint of high efficiency, resulting in the stored data;
- b. Stage II: Training of DDC strategy. The stored data obtained on the previous stage serves as a base in this training stage for DDC design which is done in a open structure. Usually, the stored data are numerically processed in the order to improve the main features: efficiency, robustness, tracking and disturbance rejection. This objectives are done by using a DB which offers multiple possibilities of data processing;
- c. Stage III: Testing of DDC method. Learning from the previous stage, the DDC strategy is able to operate in any point required by the application of AC drive. The DDC method are implemented with no cascade control structure as is shown in the figure.

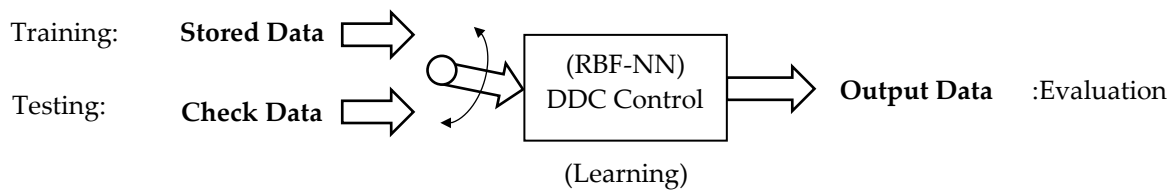
The DDC strategy may be a emergence solution in the actual AC drives whose model parameters sensitivity is still reported as an open problem.

Nevertheless, an important objective it represented by the improving of the efficiency in various scenarios.

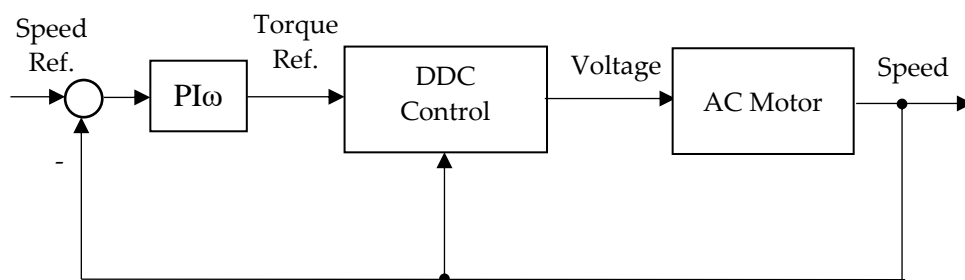
Usually, the electrical parameters of the model of AC drives are subject of variations as dependence of exogenous conditions that can differ with environment conditions: temperature, external fields, altitude etc. In this can there must be studied the robustness of the DDC strategy under these circumstances.



a) Stage I: Stored data from MPC cascade control running.



b) Stage II: Training of testing the RBF-NN DDC control



c) Stage III: Testing of the DDC control

Figure 5. The principle of the DDC strategy applied to an AC motor.

3.2. DDC of the PMSM Drive System

The PMSM drives are largely used in the adjustable applications that require high performance control performances and high efficiency. A conventional structure used in practice includes a two level power electronic inverter as in Figure 6. On this input of the power electronic inverter is usually

ensured a constant DC bus voltage U_{DC} which is provided by a DC bus circuit that contains a DC link voltage and a voltage rectifier. The main feature of this power structure is that the discrete logic command $S_{abc}=\{S_a,S_b,S_c\}$ applied on the top switches $\{1,3,5\}$ is negated applied to the bottom switches $\{4,6,2\}$.

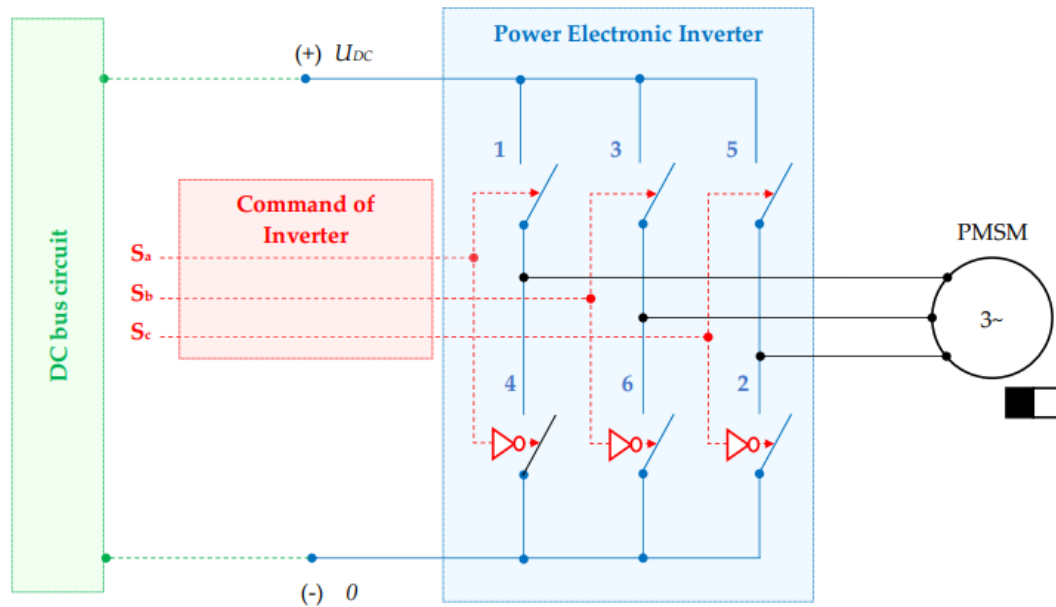


Figure 6. Power structure of the PMSM drive. .

The power inverter discrete command is provided by the control structure that is developed in the following.

3.2.1. Plant Modeling: PMSM and Power Inverter

Naturally, the model of PMSM is developed in the three-phase coordinates (a,b,c) . This model has a complex structure, being difficult to be used in the practical close-loop control applications. A first approach to avoid this drawback is to use orthogonal fixed coordinate (α,β) that offer some improvements. At last, the orthogonal transformation in a moving system reference frame (d,q) provides the highest benefits of the model of PMSM for close loop applications. Indeed, the usual FOC technique applied to PMSM is done by align the space vector of PM flux $\bar{\psi}_{PM}$ with a north pole of the rotor of PMSM.

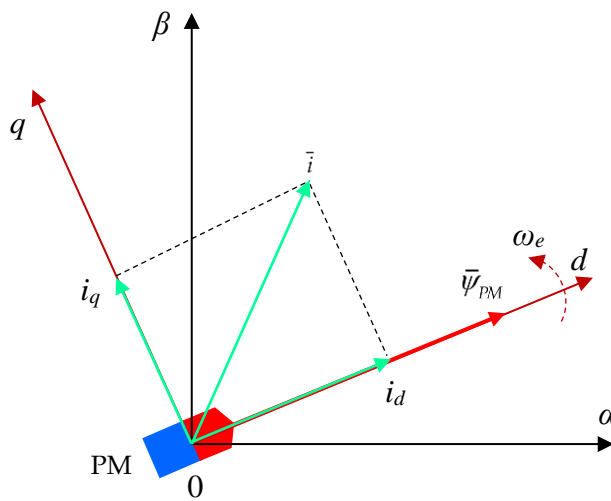


Figure 7. Space vector diagram of a PMSM with rotor system frame orientation .

In addition, the stator current components (i_d, i_q) of space vector current \bar{i} admits to be colinear and perpendicular with the PM flux direction. The both space vectors as PM flux $\bar{\psi}_{PM}$ and current \bar{i} rotates with the electrical speed ω_e .

For this kind of application, the pair of flow and effort mention above in the previous section it corresponds to torque and angular speed:

$$(e, s) \mapsto (m, \omega_m) . \quad (34)$$

The PMSM model obtained by FOC principle is composed by the currents and the motion equations [8]:

$$\begin{aligned} \frac{di_d(t)}{dt} &= \frac{1}{L_d} (u_d(t) - R_s i_d(t) + L_q \omega_e(t) i_q(t)) \\ \frac{di_q(t)}{dt} &= \frac{1}{L_q} (u_q(t) - R_s i_q(t) - L_d \omega_e(t) i_d(t) - \omega_e(t) \psi_{PM}) \end{aligned} , \quad (35)$$

$$\frac{d\omega_m(t)}{dt} = \frac{1}{J} \left(m(t) - \frac{\mu_f}{z_p} \omega_m(t) - m_\ell(t) \right) , \quad (36)$$

where: $(u_d, u_q), (i_d, i_q)$ and (L_d, L_q) are voltages, currents and inductances, all expressed in (d, q) coordinates, (ω_e, ω_m) are electrical and mechanical angular speed, respectively, R_s denoted the stator resistance, ψ_{PM} represents the permanent magnet flux, m and m_ℓ are the electromagnetic and load torques, respectively, and the group of constants represented by z_p, J and μ_f that are poles pairs, total inertia of drive and friction factor, respectively.

The system (35) – (36) was completed by introducing the expressions of the electromagnetic torque, magnetic flux components, input and output power, respectively, as follows:

$$m(t) = \frac{3}{2} z_p \left[(L_d - L_q) i_d(t) i_q(t) + \psi_{PM} i_q(t) \right] , \quad (37)$$

$$\begin{aligned} \psi_d(t) &= L_d i_d(t) + \psi_{PM} , \\ \psi_q(t) &= L_q i_q(t) \end{aligned} , \quad (38)$$

$$\begin{aligned} p_1(t) &= \text{Re}\{\underline{u}\underline{i}^*\} = \text{Re}\{(u_d(t) + ju_q(t))(i_d(t) - ji_q(t))\}, \\ p_2(t) &= m(t) \cdot \omega_m(t) \end{aligned} \quad (39)$$

where \underline{u} and \underline{i} are the phasors of voltage and current, respectively, \underline{i}^* represents the complex-conjugate phasor of current, and by $\text{Re}\{\circ\}$ is denoted the real part of the applied quantity.

The equivalent circuit scheme of the PMSM based on the dq current model (35) is depicted in Figure 8, where has been introduced the total ElectroMotive Force (EMF) force components:

$$\begin{aligned} e_d(t) &= -L_q \omega_e(t) i_q(t) \\ e_q(t) &= L_d \omega_e(t) i_d(t) + \omega_e(t) \psi_{PM} \end{aligned} \quad (40)$$

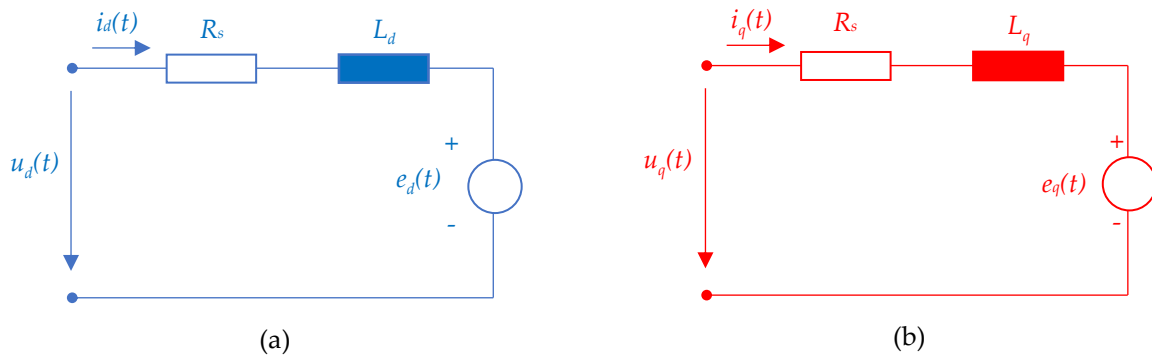


Figure 8. The dq equivalent circuit scheme of PMSM.

The Equations (34) – (38) describe the so-called dq model of the PMSM drive system. Based on the dq model there is designed the control structure in a proper manner. However, the physical operation of PMSM is done in the natural three-phase system reference frame. To obtain the desired quantities there are used the Clarke and Park direct/indirect transformations, respectively, of the quantity $\lambda = u, i, \psi$, as follows:

$$\begin{aligned} \lambda_{\alpha\beta} &= \mathbf{T}_{\alpha\beta} \lambda_{abc} \\ \lambda_{abc} &= \mathbf{T}_{\alpha\beta}^{-1} \lambda_{\alpha\beta} \end{aligned} \quad (41)$$

$$\begin{aligned} \lambda_{dq} &= \mathbf{T}_{dq} \lambda_{\alpha\beta} \\ \lambda_{\alpha\beta} &= \mathbf{T}_{dq}^{-1} \lambda_{dq} \end{aligned} \quad (42)$$

where vector-matrix quantities used are:

$$\begin{aligned} \lambda_{abc} &= [\lambda_a \quad \lambda_b \quad \lambda_c]^T, \\ \lambda_{\alpha\beta} &= [\lambda_d \quad \lambda_q]^T, \\ \lambda_{dq} &= [\lambda_d \quad \lambda_q]^T. \end{aligned} \quad (43)$$

and the involved matrix-transformations are given by:

$$\mathbf{T}_{\alpha\beta} = \frac{2}{3} \begin{bmatrix} 1 & -\frac{1}{2} & -\frac{1}{2} \\ 0 & \frac{\sqrt{3}}{2} & -\frac{\sqrt{3}}{2} \end{bmatrix}; \mathbf{T}_{\alpha\beta}^{-1} = \frac{2}{3} \begin{bmatrix} 1 & 0 & 1 \\ 0 & -\frac{1}{2} & \frac{\sqrt{3}}{2} \end{bmatrix};$$

$$\mathbf{T}_{dq} = \frac{2}{3} \begin{bmatrix} \cos \alpha_m & \cos \left(\alpha_m - \frac{2\pi}{3} \right) & \cos \left(\alpha_m + \frac{2\pi}{3} \right) \\ \sin \alpha_m & \sin \left(\alpha_m - \frac{2\pi}{3} \right) & \sin \left(\alpha_m + \frac{2\pi}{3} \right) \end{bmatrix}; \mathbf{T}_{dq}^{-1} = \frac{2}{3} \begin{bmatrix} \cos \alpha_m & \sin \alpha_m & 1 \\ \cos \left(\alpha_m - \frac{2\pi}{3} \right) & \sin \left(\alpha_m - \frac{2\pi}{3} \right) & \frac{\sqrt{3}}{2} \end{bmatrix}. \quad (44)$$

The power inverter command will be supplied by the finite set values \mathbf{S}_{abc} which contains the optimal logical values required for obtaining inverter control.

Based on finite set values \mathbf{S}_{abc} the model of the two-level power inverter provides the three-phase voltages:

$$\mathbf{u}_{abc} = \frac{1}{3} U_{DC} \mathbf{T}_I \mathbf{S}_{abc}, \quad (45)$$

where the power inverter matrix model is:

$$\mathbf{T}_I = \begin{bmatrix} 2 & -1 & -1 \\ -1 & 2 & -1 \\ -1 & -1 & 2 \end{bmatrix}. \quad (46)$$

3.2.2. MPC with Finite Set

The DDC method is developed by using the main features of the MPC strategy that provides a command law which corresponds to voltage of the inverter, computed by a switching functions set. In this strategy, the main variables as current, voltage and electromagnetic torque are discretized on every time instant T_s by forward Euler forward method, that gives to a generic variable $z(t)$ the next first-time derivative linear approximation:

$$\left. \frac{dz(t)}{dt} \right|_{z=z(k+1)} \approx \frac{z(k+1) - z(k)}{T_s}, \quad (47)$$

Taking into account Euler forward approximation method, the first-time derivate of current (35) becomes:

$$i_d(k+1) = \left(1 - \frac{T_s R_s}{L_d} \right) i_d(k) + \frac{L_q}{L_d} T_s \omega_e(k) i_q(k) + \frac{T_s}{L_d} u_d(k)$$

$$i_q(k+1) = \left(1 - \frac{T_s R_s}{L_q} \right) i_q(k) - \frac{L_d}{L_q} T_s \omega_e(k) i_d(k) - \frac{T_s}{L_q} \omega_e(k) \psi_{PM} + \frac{T_s}{L_q} u_q(k), \quad (48)$$

Now, from the first-time derivate of current (37), the predictive electromagnetic torque results:

$$m(k+1) = \frac{3}{2} z_p \left[(L_d - L_q) i_d(k+1) i_q(k+1) + \psi_{PM} i_q(k+1) \right], \quad (49)$$

The one-step-ahead MPC law is an optimal solving problem defined as follows:

$$g^* = \min_{\mathbf{S}_{abc}} g_i$$

$$\text{s.t.} \left\{ \begin{array}{l} g_i = \begin{cases} |m^{ref} - m(k+1)| + i_d(k), \\ |m^{ref} - m(k+1)| + |emf^{rated} - (\psi_{PM} + L_d i_d(k))|, \end{cases} \\ i = 1 \div 8; k = 1 \div N \end{array} \right. \cdot \begin{array}{l} \omega_m \leq \omega_m^{rated} \\ \omega_m > \omega_m^{rated} \end{array} \quad (50)$$

where emf^{rated} is the rated back motion EMF computed by:

$$emf = k_e \omega_m. \quad (51)$$

with the back EMF constant:

$$k_e = z_p \psi_{PM}, \quad (52)$$

the index i corresponds to the combination of switching state \mathbf{S}_{abc} (see below the Table 1).

Table 1. The voltage space vector according to their corresponding switching function.

Index i	\mathbf{S}_{abc}	Voltage space vector
1	(0,0,0)	$\underline{v}_1 = 0$
2	(1,0,0)	$\underline{v}_2 = 2/3 U_{DC}$
3	(1,1,0)	$\underline{v}_3 = 1/3 U_{DC} + j\sqrt{3} U_{DC}$
4	(0,1,0)	$\underline{v}_4 = -1/3 U_{DC} + j\sqrt{3} U_{DC}$
5	(0,1,1)	$\underline{v}_5 = -2/3 U_{DC}$
6	(0,0,1)	$\underline{v}_6 = -1/3 U_{DC} - j\sqrt{3} U_{DC}$
7	(0,1,0)	$\underline{v}_7 = 1/3 U_{DC} + j\sqrt{3} U_{DC}$
8	(1,0,1)	$\underline{v}_8 = 0$

A better illustration of the voltage space vector of the power inverter and their hexagonal bounds is done in Figure 9.

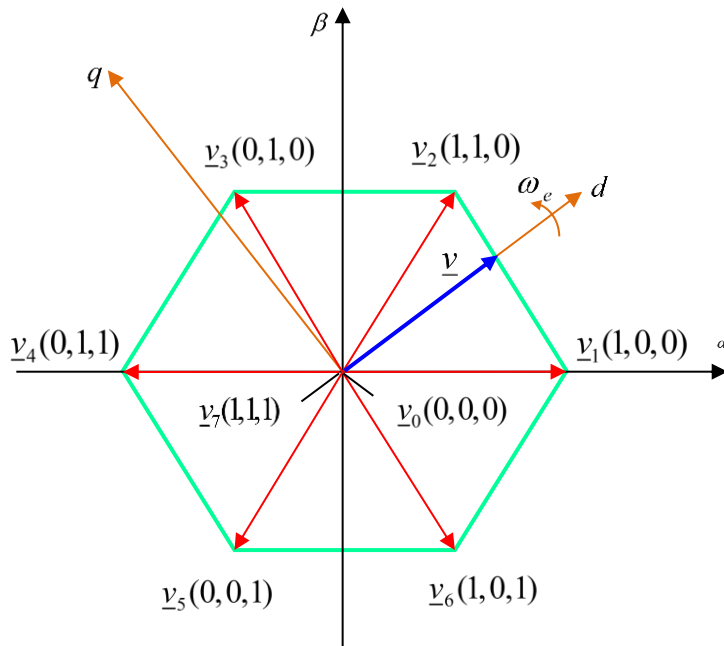


Figure 9. The voltage space vector according to their corresponding switching states.

In the dq system reference frame, the components of the space vector \underline{v} for the eight possible states are obtained in a vector-matrix representation:

$$\begin{aligned} \mathbf{v}_d &= \begin{bmatrix} 0 & 2 & 1 & -1 & 2 & -1 & 1 & 0 \end{bmatrix} \frac{U_{DC}}{3} \\ \mathbf{v}_q &= \begin{bmatrix} 0 & 0 & 1 & -1 & 0 & -1 & -1 & 0 \end{bmatrix} \frac{\sqrt{3}}{3} U_{DC} \end{aligned} \quad (53)$$

Further, in Figure 10 is presented the cascade control structure, with a PI speed control in an outer loop and a MPC multivariable inner current control loop for the electronic power converter which supply the PMSM. The PI speed control is designed via the classical pole placement method [45].

The electrical energy provided from the power grid is of fixed values of voltage and frequency. By and adevate rectifer there is obtained a DC voltage. The DC-bus voltage U_{DC} is filtered by a passive Low Pass Filter (LPF) represented by a high value capacitor C , obtaining a constant value of the DC-bus voltage $U_{DC} = \text{cst}$.

The PI controller is used for trackig the mechanical speed ω_m^{MPC} its reference $\omega_m^{ref-MPC}$. For the MPC formulation of the inner loop, there are measured the three-phase current (a, b, c), and then by the Park/Clarke transformations are successively obtained the dq MPC current $\mathbf{i}_{dq}^{MPC}(k) = [i_d^{MPC}(k) \ i_q^{MPC}(k)]^T$. Further, based on (48) is obtained the current prediction $\mathbf{i}_{dq}^{MPC}(k+1) = [i_d^{MPC}(k+1) \ i_q^{MPC}(k+1)]^T$. Now, the MPC problem defined according to (50) will give optimal switching combinations S_{abc}^{MPC} . For the future computations, there is additionally calculated the voltages $\mathbf{u}_{dq}^{MPC}(k) = [u_d^{MPC}(k) \ u_q^{MPC}(k)]^T$ based on a switch-voltage transformation S/u .

It can be mentioned that the mecanical speed ω_m^{MPC} is not directly measured. Firstly, there is measured the postion of the rotor $\alpha_m^{MPC}(k)$ by an encoder (E), and then by derivation is obtained the actual mechanical speed $\omega_m^{MPC}(k)$.

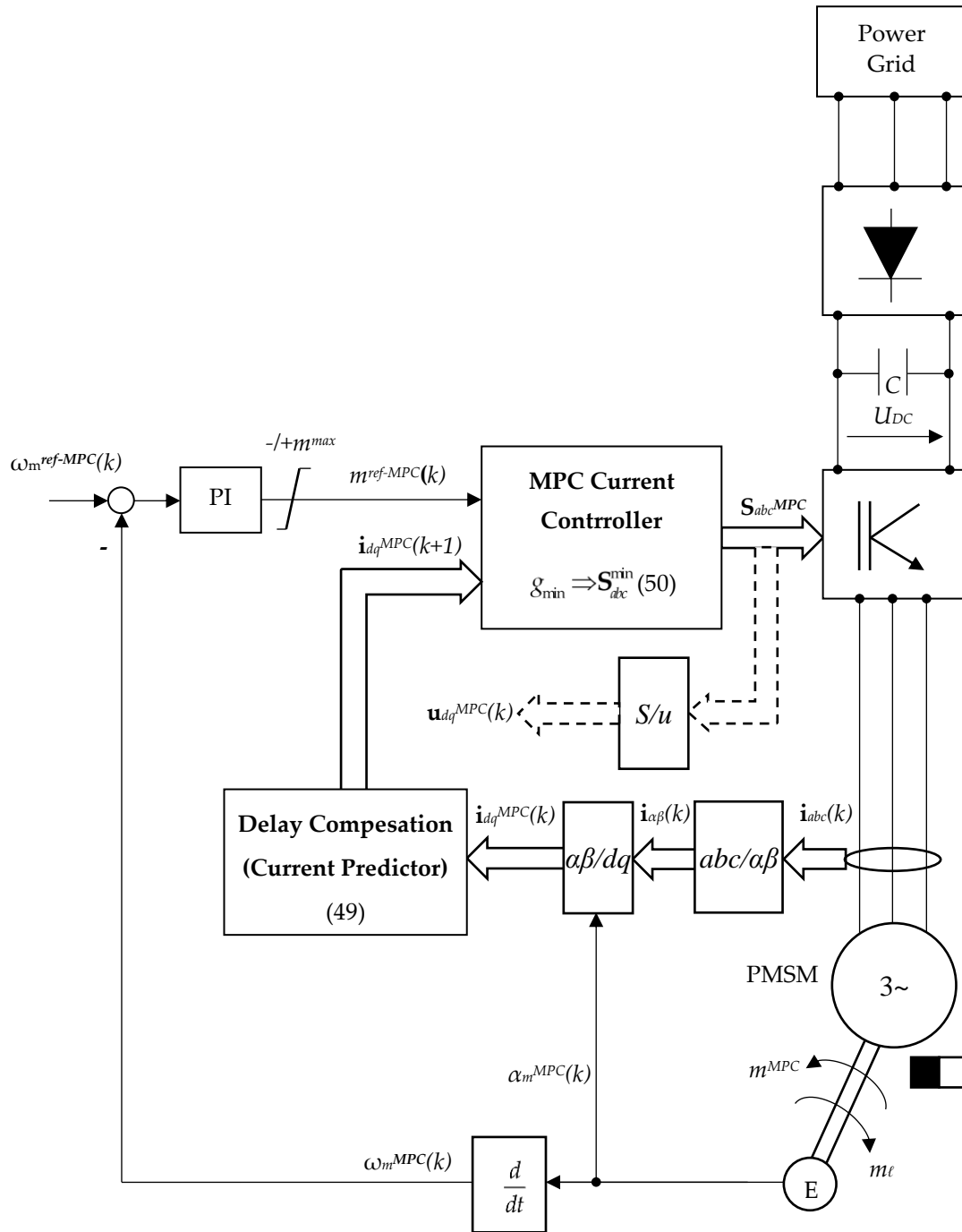


Figure 10. The MPC control PMSM drive.

3.2.3. DDC Law of PMSM

The main idea of DDC strategy is to learn from a well-known MBC method whose performances has been already proved. In this sense, the DDC method of a PMSM drive is developed by selecting a DB containing the data provided by MPC law. Following the methodology developed for DDC in the sens of the maximum energy conversion process objective, for PMSM the output is given by speed and torque $\mathbf{y}(k) = [\omega_m^{MPC}(k) \quad m^{MPC}(k)]^T$, while the control by dq voltage $\mathbf{u}(k) \equiv \mathbf{u}_{dq}^{MPC}(k)$. In this context, the training sequence becomes:

$$\mathbf{d}^{MPC}(k) = [\mathbf{u}_{dq}^{MPC}(k) \quad \omega_m^{MPC}(k) \quad m^{MPC}(k)]^T, \quad (54)$$

Also, for the PMSM drive the training matrix of the RBF-NN is composed by speed and dq volage of the reduced model (high efficiency points extraction):

$$\begin{aligned}\mathcal{M}_F &= [\tilde{\mathbf{y}} \quad \tilde{\mathbf{u}}]^T, \\ \tilde{\mathbf{y}} &= [\tilde{\omega}_m^{MPC}(k) \quad \tilde{m}^{MPC}(k)]^T, \\ \tilde{\mathbf{u}} &= \tilde{\mathbf{u}}_{dq}^{MPC}(k),\end{aligned}\quad (55)$$

The training phase of the DDC controller is depicted in Figure 11. As mention above, the entire methodology is based on the the learning of the experience of the high-value efficiency steady-state data provided by MPC strategy.

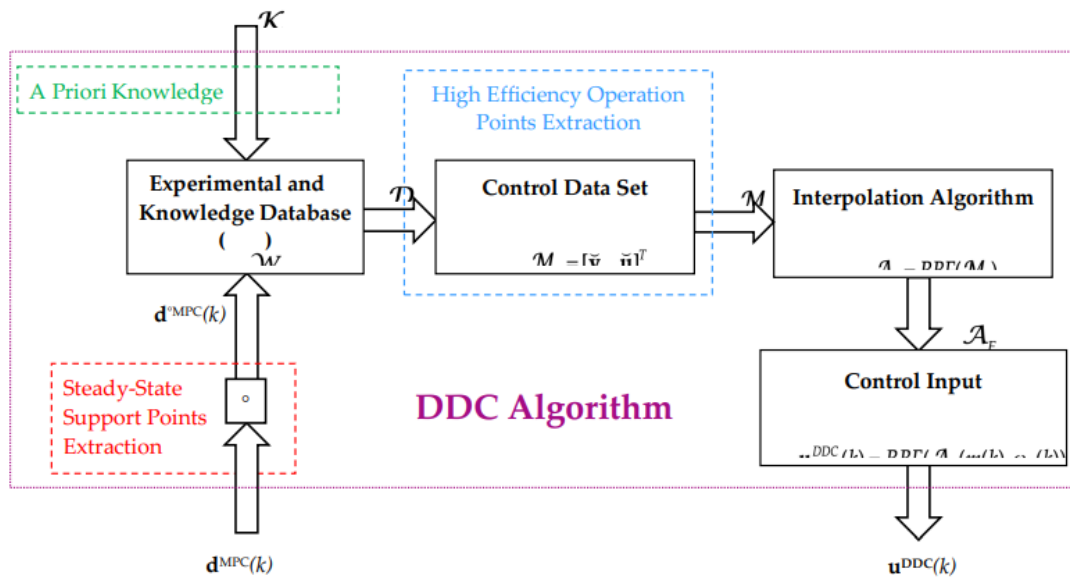


Figure 11. Training phase of the DDC controller of PMSM.

The set of aprioric informations \mathcal{K}_{DB} includes rated data of PMSM, power inverter load and other components, environment and design requirements of EDSs.

Once training is done, the DDC control structure may be done as in Figure 12. The output of the DDC controller is given by the dq voltage $\mathbf{u}_{dq}^{DDC}(k)$. The optimal set of the switching functions combinations \mathbf{S}_{abc}^{DDC} is then obtained by a command shaping block.

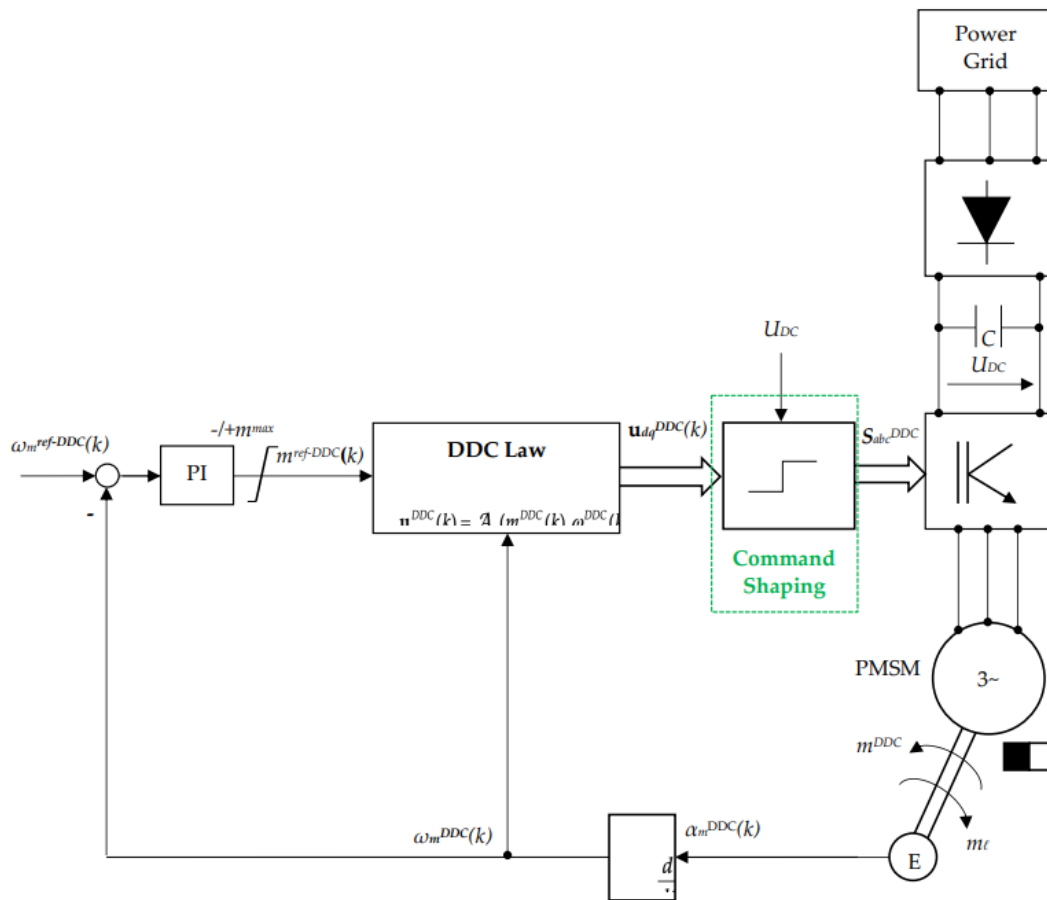


Figure 12. The DDC control structure of a PMSM drive.

To have a succinct description, in Figure 13 is depicted a schematic representation of the DDC control structure. The main controllers as PI and DDC are highlighted. The DDC algorithm is represented in a sequential structure, where the command shaping has an internal computing loop. The DDC algorithm has a complex structure. A first stage is the searching on the DB the corresponding command $\mathbf{u}_{dq}^{ref-DDC}$. Once found, an internal computing programming loop is designed. Further, there are compared the command $\mathbf{u}_{dq}^{ref-DDC}(k)$ and the feedback $\mathbf{v}_{dq}^{opt-DDC}(k)$ (that is also an optimal value), resulting an error which is then integrated obtaining the the voltage control $\mathbf{v}_{dq}^{c-DDC}(k)$ that acts as input in the searching block. Finally, there is obtained switching functions delivered by DDC method S_{abc}^{DDC} that will feed the gate of the inverter.

More details will presented later in the pseudocode format of the DDC method.

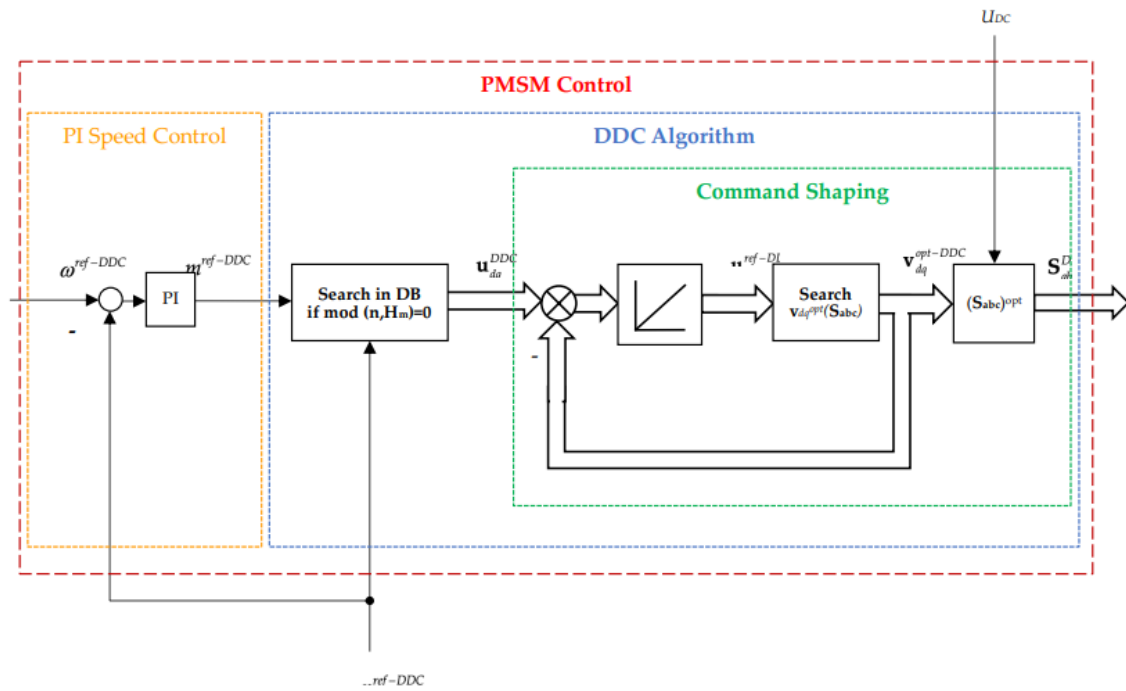


Figure 13. A schematic representation of the DDC control of the PMSM drive system.

3.2.4. Design of the DDC Database

The input data in DB is initially done from the MPC operation, selected from the high efficiency values. After that, the data are processed according to various criteria. Hence, the acronym MPC will be substituted, making the distinction between MPC and DDC whenever is necessary.

The operation of a PMSM drive depends on the required mechanical speed domain limits. Generally, there are possible three situation that show how torque and outer power varies vs. mechanical speed:

$$\omega_m = \begin{cases} \text{I. } \omega_m \in (0, \omega_{m,b}) & \Rightarrow \omega_m \nearrow \Rightarrow \left\{ \begin{array}{l} m = cst. \\ P_2 \nearrow \end{array} \right\} \text{Constant torque} \\ \text{II. } \omega_m \in (\omega_{m,b}, \omega_{m,max}) & \Rightarrow \omega_m \nearrow \Rightarrow \left\{ \begin{array}{l} m \searrow \\ P_2 = cst. \end{array} \right\} \text{Constant power ,} \\ \text{III. } \omega_m > \omega_{m,max} & \Rightarrow \omega_m \nearrow \Rightarrow \left\{ \begin{array}{l} m \searrow \\ P_2 \searrow \end{array} \right\} \text{Critical operation} \end{cases} \quad (56)$$

where: $\omega_{m,b}$ is the based mechanical speed which corresponds to the rated one ($\omega_{m,b}=\omega_{mN}$), and $\omega_{m,max}$ represent the maximal mechanical speed.

In Figure 14 are illustrated the torque – speed characteristics of a PMSM drive system. Until base speed $\omega_m < \omega_{m,b}$, the operation of PMSM is done on constant torque in region I. In the region II, where the power becomes constant, there is used field-weakening technique. At last, the critical operation done for $\omega_m > \omega_{m,max}$ must be avoided (region III) for ensuring a safety operation.

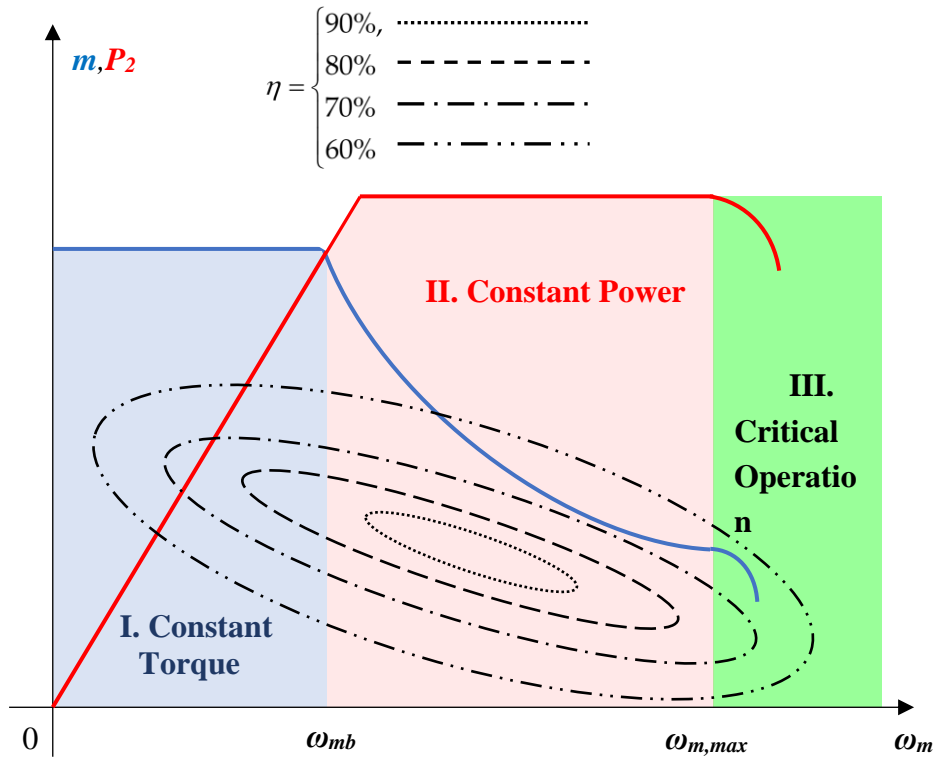


Figure 14. The torque – speed characteristics under iso-efficiency curves of a PMSM drive.

Let be $\Omega, \mathbf{M}, \mathbf{P}$ and \mathbf{H} the sets of sets of torque, power, and their corresponding efficiency:

$$\Omega = \{\omega_{m_j} \mid j = \overline{1, N_\omega}\}, \quad (57)$$

$$\mathbf{M} = \{m_j \mid j = \overline{1, N_m}\}, \quad (58)$$

$$\mathbf{P} = \{P_{2j} \mid j = \overline{1, N_p}\}, \quad (59)$$

$$\mathbf{H} = \{\eta_j \mid j = \overline{1, N_h}\}. \quad (60)$$

where $N_{\omega/m/p/h}$ is the number of points of each set.

As can be easlier observer from Figure 14, some of the different paris of speed-torque (ω_{m_j}, m_i) or speed – power (ω_{m_j}, P_{2j}) corresponds to the same value of efficiency. That means that the solution is not unique.

Considering that all the sets (57) – (60) has the same number of points $N_\omega = N_p = N_h = N$, there are introduced the next sets obtained by cartesian product:

$$\Lambda_m = \{\omega_{m_j} \times m_j \mid j = \overline{1, N}\}, \quad (61)$$

$$\Lambda_p = \{\omega_{m_j} \times P_{2j} \mid j = \overline{1, N}\}. \quad (62)$$

Now, there can be definited the following multi-valued maps:

$$\mathbf{f}_m : \Lambda_m \rightarrow \mathbf{H}, \quad (63)$$

$$\mathbf{f}_p : \Lambda_p \rightarrow \mathbf{H}, \quad (64)$$

whose points are contained in the sets:

$$\Gamma_m = \{(\Lambda_m(j), \eta_j) \mid j = \overline{1, N}\}, \quad \Gamma_m \subseteq \Lambda_m \times \mathbf{H}, \quad (65)$$

$$\Gamma_p = \{(\Lambda_p(j), \eta_j) \mid j = \overline{1, N}\}, \quad \Gamma_p \subseteq \Lambda_p \times \mathbf{H}. \quad (66)$$

To avoid the efficiency multi-valued representation, we select the high efficiency points that corresponds to each point, defining the functions:

$$\mathbf{f}_m^* : \Lambda_m \rightarrow \mathbf{H}^{\max}, \quad (67)$$

$$\mathbf{f}_p^* : \Lambda_p \rightarrow \mathbf{H}^{\max}, \quad (68)$$

where the maximal efficiency vector is :

$$\mathbf{H}^{\max} = [\eta_1^{\max} \quad \eta_2^{\max} \quad \eta_3^{\max} \quad \cdots \quad \eta_N^{\max}]^T, \quad (69)$$

and the contained sets are given by:

$$\Gamma_m^* = \{(\Lambda_m(j), \eta_j^{\max}) \mid j = \overline{1, N}\}, \quad \Gamma_m^* \subseteq \Lambda_m \times \mathbf{H}^{\max}, \quad (70)$$

$$\Gamma_p^* = \{(\Lambda_p(j), \eta_j^{\max}) \mid j = \overline{1, N}\}, \quad \Gamma_p^* \subseteq \Lambda_p \times \mathbf{H}^{\max}. \quad (71)$$

An illustrative representation of the transformation of the multi-valued map of the efficiency vs torque/power into a single-valued functions of a PMSM drive characteristics is depicted in Figure 15.

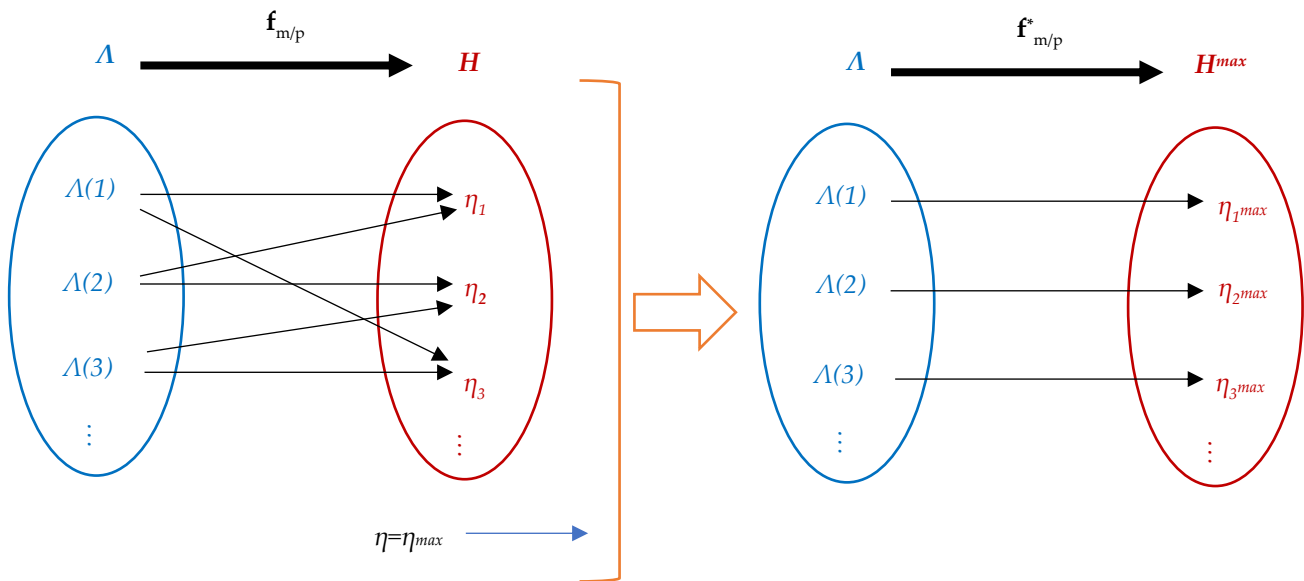


Figure 15. Transformation of the multi-valued efficiency map into a single-valued function.

An essential objective is the design of the DB. Generally, there are few steps that must be followed in the order to obtain high computation accuracy as it is suggested in Figure 16.

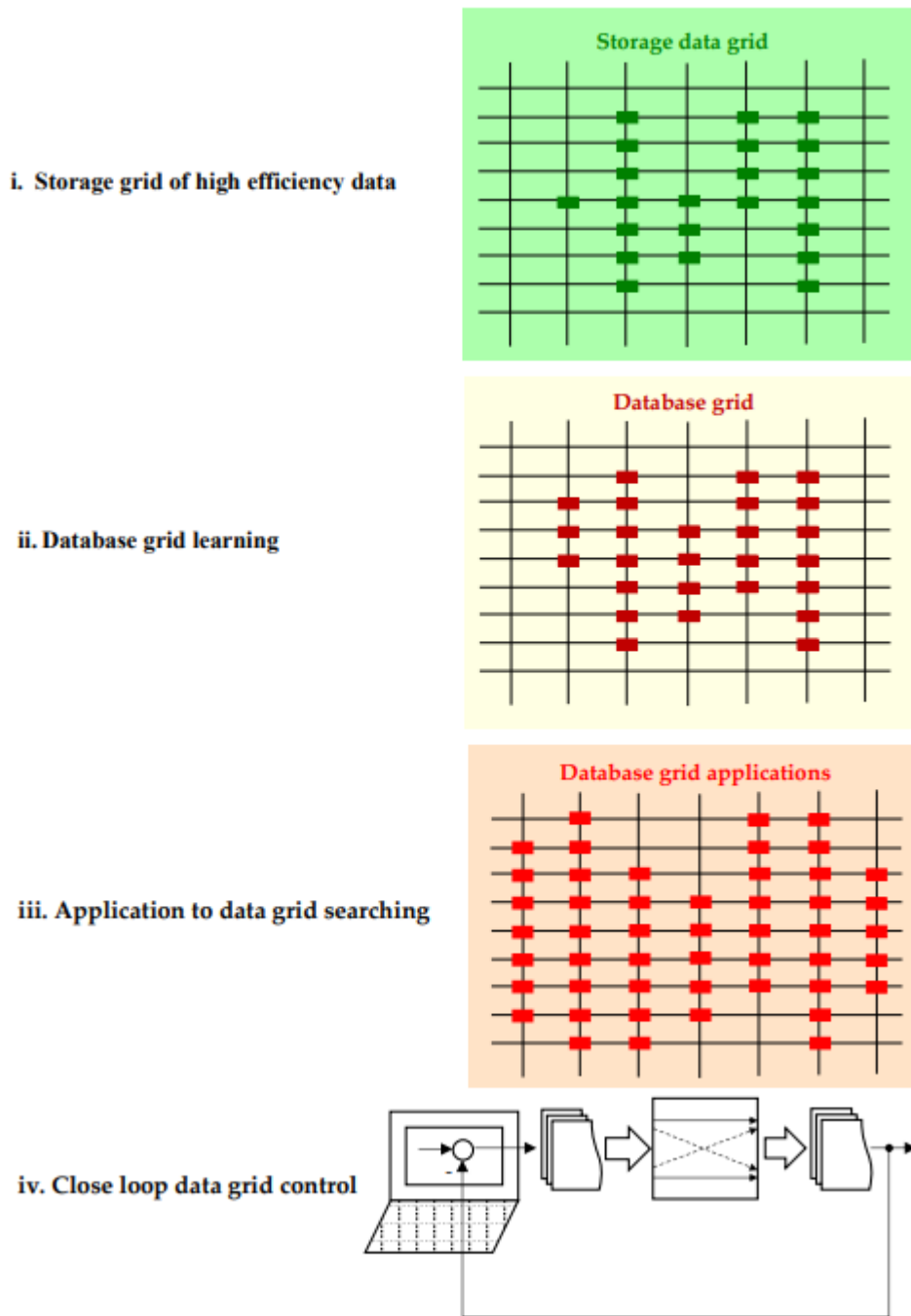


Figure 16. The database grid steps design of close loop applications.

Succinctly, the main followed steps can be described as:

- I. *Storage grid of high efficiency data.* At this step there are collected the main data set in the steady-state regime and knowledge which corresponds to a high efficiency value stored in $\mathcal{D}_F = \mathcal{W}\{\mathcal{K}_{db}; \mathbf{d}^\circ(k)\}$

$$\mathbf{d}^\circ(k) = \left[\mathbf{u}_{dq}^\circ(k) \quad \mathbf{i}_{dq}^\circ(k) \quad m^\circ(k) \quad \omega_m^\circ(k) \right]^T, \quad (72)$$

s.t. $\eta(k) = \eta_{\max}$

- II. *Database grid learning.* The database sets are extended by a learning process, adding new points contained in the set:

$$\begin{aligned} \mathbf{d}^{\circ e}(k) &\supseteq \mathbf{d}^{\circ}(k) \\ \text{s.t. } \eta(k) &= \eta_{\max} \end{aligned} \quad (73)$$

- III. *Application to data grid searching.* It is checked that the added new points corresponds to the real operation for open loop applications.
- IV. *Close loop data grid control.* Finally, the designed database grid is introduced in the desired close loop application from Figure 16.

These steps can be changed/improved depending on the desired objectives. For example, exogenous quantities may have a high influence on the system which are not on thermodynamic equilibrium.

Numerical computations of the quantities delivered by DB are affected by errors and noises. The DDC strategy is a searching discrete – interpolative method of the best solution within learning data bounds.

In the order to improve the accuracy of data processing there is used a moving window filter, whose output is given by:

$$\mathbf{y}^{ftr}[n] = \frac{1}{L_w} \sum_{k=0}^{L_w-1} \mathbf{u}^{nfr}[n-k], \quad (74)$$

where L_w is the filter length, n is the current sample, and the input samples (nonfiltered) and output samples (filtered), respectively, are:

$$\mathbf{u}^{nfr} = \left[\mathbf{u}_{dq}^{nfr}(k) \quad m^{nfr}(k) \quad \omega_m^{nfr}(k) \right]^T, \quad (75)$$

$$\mathbf{y}^{ftr} = \left[\mathbf{u}_{dq}^{ftr}(k) \quad m^{ftr}(k) \quad \omega_m^{ftr}(k) \right]^T, \quad (76)$$

where $\mathbf{u}_{dq}^{nfr/ftr}(k) = \left[u_d^{nfr/ftr}(k) \quad u_q^{nfr/ftr}(k) \right]^T$.

The moving window filter structure is represented in Figure 17. The input samples are introduced by using the unit-delay operator Δ . On the output is obtained an average value of the moving samples.

As can be observed from (75) – (76) the filtered quantities are voltage, torque and mechanical speed. Based on this, further there result the filtering of both input and output powers of PMSM. Finally, the filtered powers are used to compute the efficiency, that do not contains high numerical noises and errors.

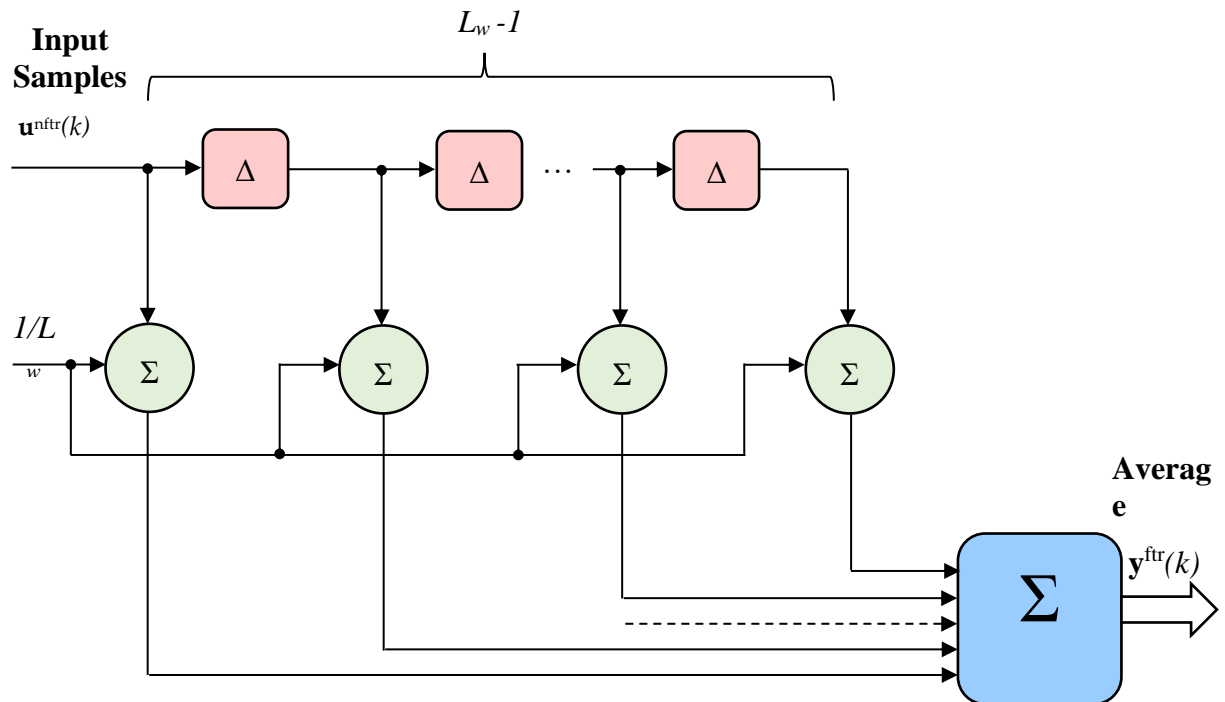


Figure 17. The moving window filter structure.

3.2.5. DDC Matlab Implementation

The DDC of the PMSM is implemented in Matlab simulation environment, taking into account the main programming features of this software package.

To obtain a high analysis, in the paper is made up a comparison between the MPC method and DDC strategy of the PMSM drive.

MPC Algorithm

The basic idea of the model predictive control for the PMSM fed by the simplest inverter with two voltage levels, having eight available state voltage switching vectors v_i (Table 1) is the following: the torque and speed can be controlled by direct selecting a proper switching inverter's voltage vector based on the machine parametric predictive model and an appropriate cost function g .

The objective of the *Algorithm 1* represented in pseudocode format from Figure 12 is to give to reader the necessary tools to understand the simulations results and to replicate the implementation of the exposed algorithms thinking in Matlab environment.

The switching vector v^{opt} , that was predicted to provide the most favourable process behaviour, i. e, the one that minimize the objective function g , is considered to be optimal and is generated by the inverter, applying directly the corresponding switch functions $svs=[S_a, S_b, S_c]$.

The parameters of the motor and the driven process are included in the vector \mathcal{P}_{em} (electromagnetic parameters). After initialisations of the finite states for the switching vector (lines 1,2) and the rated values and state variables, the main iteration loop are opened (line 8).

The model requires the actual state variables $\mathbf{x}=[i_d \quad i_q \quad \omega_m]$ to be recalled from the previous sampling period state $\mathbf{x}^{old}=[i_d^{old} \quad i_q^{old} \quad \omega_m^{old}]$.

Algorithm 1. The MPC main program

```

% Initialization for the 8 possible values of the inverter voltages
1.  $v_d=[0;2;1;-1;2;-1;1;0]*U_{dc}/3;$  %  $U_{dc}$  is DC-bus voltage [V]
2.  $v_q=[0;0;1;-1;0;-1;-1;0]*\sqrt{3}/3*U_{dc};$ 
3.  $svs=[000; 100; 110; 010; 011; 001; 101; 111];$  % Switching vector states inverter's gate control
4.  $\mathcal{P}_{em}=[m_e, J, \mu, R_s, L_d, L_q, \psi_{PM}];$  % Declare process and machine parameters
5.  $\omega^{ref}=\omega^{rated}; m^{max}=2.5*m^{rated};$  % Initialization of the desired speed and maximum torque
6.  $\omega_p^{old}=\omega^{int}; i_{dp}^{old}=0; i_{qp}^{old}=0;$  % Initialization of the state's variables of the process
7.  $T_s=1e-4; T_d=10s; N=T_d/T_s;$  % Sampling period ( $T_s$ ), Desired simulation time ( $T_d$ )
8. for n=1:N
% Call function PI_control
9.  $[m^{ref}]=PI\_control(\omega^{ref}, \omega^{old}, m^{max}, K_p, K_i);$ 
% The prediction-optimisation procedure
10. for i=1:8
% Call Model Predictive Control-(MPC_model) ( $i_{dp}^{old}, i_{qp}^{old}$  are the measured currents)
11.  $[i_d(i), i_q(i), m(i), p_1(i)]=MPC\_PMSM\_model(v_d(i), v_q(i), i_{dp}^{old}, i_{qp}^{old}, \mathcal{P}_{em}, T_s);$  % Predictor
12. if  $(\omega_p \leq \omega^{rated});$ 
13.  $g(i)=abs(m^{ref}-m(i))+i_d(i);$ 
14. else
15.  $g(i)=abs(m^{ref}-m(i))+abs(em^{rated}(i)-(\psi_{PM}+L_d*i_d(i)));$  %  $em^{rated}$  is rated bac-EMF
16. end % end if
17. % Search  $v_d^{opt}, v_q^{opt}$  such as  $g|_{min}$ 
18.  $[v_d^{opt}, v_q^{opt}, svs^{opt}]=MPC\_Command\_Shaping(g(m^{ref}, m(i), em^{rated}), p_1(i), v_d(i), v_q(i));$ 
19. end % end for
% Call Process_Model
20.  $[i_d, i_q, m, \omega, p_1, p_2]=Process\_PMSM\_Model(v_d^{opt}, v_q^{opt}, i_{dp}^{old}, i_{qp}^{old}, \omega^{old}, \mathcal{P}_{em});$ 
% Update the states
21.  $i_{dp}^{old}=i_{dp}; i_{qp}^{old}=i_{qp}; \omega^{old}=\omega;$ 
% Call Moving_Average
22.  $[u_{dd}^{ftr}, u_{dq}^{ftr}]=Moving\_Average(v_d^{opt}, v_q^{opt}, L, T_s);$  % L is the length of the moving window filter
% Save process outputs in Data_Base_1
23.  $[i_{dd}, i_{dq}, m, \omega, u_{dd}^{ftr}, u_{dq}^{ftr}, pp1, pp2]=Data\_Base\_1(i_d(n), i_q(n), m(n), \omega(n), u_{dd}^{ftr}, u_{dq}^{ftr}, p_1(n), p_2(n));$ 
24. end % end for

```

Figure 18. The pseudocode format of the MPC algorithm of a PMSM drive control.

The electrical and mechanical parameters respectively, \mathcal{P}_e and \mathcal{P}_m , of the plant are grouped in the electromechanically set of parameters \mathcal{P}_{em} , as follows:

$$\mathcal{P}_{em}(t) = \underbrace{[R_s \quad L_d \quad L_q \quad \psi_{PM}]}_{\mathcal{P}_e} \underbrace{[m_t \quad J \quad \mu_f]}_{\mathcal{P}_m} = \mathcal{P}_e \cup \mathcal{P}_m \quad (77)$$

The MPC algorithm starts with the initializing the main data used in the computing loop. A first programming syntax is developed for implement the PI speed controller:

$$\underbrace{[m^{ref}]}_{\text{Output}} = \mathbf{PI_control} \left(\underbrace{\omega^{ref}, \omega^{old}, m^{max}, K_p, K_i}_{\text{Input}} \right) \quad (78)$$

where $\omega^{ref/old}$ the reference /actual mechanical speed is, m^{max} denotes the maximal value of the electromagnetic torque, and $K_{p/i}$ are the parameters of the PI controller. **The PI_control** generates the required value of torque reference (set point) m^{ref} .

The relation (78) describes a typical programming syntax that contain the *Input/Output* sets of quantities. This type of programming syntax structure was followed in the rest of the paper.

The MPC strategy takes as input the voltages v_{dq} , the previous measured currents $i_{d/q}^{old}$, the electromechanical set of parameters $\mathcal{P}_{em}(t)$ and sampling time instant of MPC calculated around ten times higher then the simulation discretizing one:

$$[i_d^p(i), i_q^p(i), m^p(i), p_1(i)] = \mathbf{MPC_PMSM_model}(v_d(i), v_q(i), i_d^{old}, i_q^{old}, \mathcal{P}_{em}(t), 10 \cdot T_s). \quad (79)$$

Thinking in the Matlab environment implementation, the function which simulate the PMSM model has as the input the controls (u_d, u_q) - the components of the supply voltage, the old states, the load torque and the electromagnetique parameters and as the outputs - the current components (i_d, i_q) , the electromagnetique torque m and the angular velocity ω_m :

$$\underbrace{[i_d, i_q, m, \omega_m]}_{\text{Output}} = \mathbf{Plant_PMSM_model} \left[\underbrace{[u_d^{old}, u_q^{old}, i_d^{old}, i_q^{old}, \omega_m^{old}, m_t, \mathcal{P}_{em}(t), T_s]}_{\text{Input}} \right]. \quad (80)$$

Finally, the programs were grouped and compacted in a software application of the proposed control structure.

The equations of the physical model (80) are in the continuous time domain. The variables of the model take values in the real domain \mathbb{R} . In fact the PMSM is supplied by the power electronic inverter which provide in the simplest case, a eight finite switching state vector:

$$\mathbf{v}_{dq} = \{v_d(i), v_q(i)\}, \quad i = 1, \dots, 8. \quad (81)$$

The components (u_d, u_q) takes values on the set \mathbf{v}_{dq} . For this reason, these quantities must be shaped. According to the principle algorithm of the power inverter command, within each sampling period T_s , the components (v_d^{opt}, v_q^{opt}) and the duration d ($0 < d < T_s$) are calculated so that the machine currents resulting from switching supply voltage $\mathbf{v}_{dq}^{opt} = [v_d^{opt}, v_q^{opt}]$ has to be as close as possible to the ideal sinusoidal form of the three-phase currents:

$$\text{Find: } \mathbf{v}_{dq}^{opt} \text{ until } \Rightarrow THDi_{abc} = \min, \quad (82)$$

which admits the syntax:

$$[v_d^{opt}, v_q^{opt}] = \mathbf{Inverter_Command_Shaping} \left[u_d(k), u_q(k), T_s \right]. \quad (83)$$

The command algorithm used by MPC control is implicit, that is different from classical version. Within each sampling period T_s , the command algorithm looks for the optimal components (v_d^{opt}, v_q^{opt}) , which minimizes the g criterion function:

$$[v_d^{opt}, v_q^{opt}] = \mathbf{MPC_Command_Shaping} \left[g(v_d(k), v_q(k), m, m^{ref}, i_d(k), p_1(k), T_s) \right]. \quad (84)$$

This function provides the variables of the process at the current sampling period. The filter is implemented by the function *Moving_Average*, having the input the switching voltage vector

components (v_d^{opt}, v_q^{opt}) , length of the window of the filter L and the sample time period T_s , providing the output of the moving window that corresponds to the filtered inputs (u_d^{fir}, u_q^{fir}) :

$$\left[u_d^{fir}, u_q^{fir} \right] = \mathbf{Moving_Average}[v_d^{opt}, v_q^{opt}, L, T_s]. \quad (85)$$

The numerical data calculated at each step T_s are stored in the DB named *Data_Base_1*, which will continue to be used in DDC Algorithm presented in the next section.

3.4.2. DDC Algorithm

The DDC controls (u_d, u_q) are directly obtained from DB with \mathcal{M}_F (Figure 11) by the interpolation techniques RBF – NN exposed in the second section. The control law was generated by means of a known set \mathcal{M}_F of operating points of the process (55) through an interpolation technique \mathcal{A}_F (25). The resulting Algorithm 2 of the DDC strategy in pseudocode format is depicted in Figure 19 that schematically is given by Figure 13. The main common programming syntax from MPC and DDC has the same significance.

In first line there is loaded the data from database DB1, created with the MPC algorithm (Figure 18), where the support points of the control surfaces are described by:

$$\begin{aligned} \mathbf{u}(a) &= \mathcal{F}(mm(a), \omega\omega(a)), \\ \mathbf{u} &= \left[u_d^{fir}(a) \quad u_q^{fir}(a) \right]^T, \\ \mathcal{F} &= \begin{bmatrix} F_d & F_q \end{bmatrix}^T, \\ a &= 1, \dots, N_{obs}. \end{aligned} \quad (86)$$

As mention before, the control system is designed in two stages. In the the first, by MPC software are simulated a set of motion trajectories. In database DB1 are stored in a set of grided operation points of the process. Based on DB1 is simulated the DDC algorithm with which they were obtained the results presented in the paper.

There is a particularity of the electric drive systems, because the controls $\mathbf{u}_{dq}(k)$ must be shaped by the switching vector \mathbf{v}_{dq} of the power inverter (81). The set \mathcal{M}_F of operating points of the process (55) is essential for the efficiency of the energy conversion system with power electronic converter and electric machine. In that aim we selected from a large database a few set of the optimal energy operation points defined by the speed, torque, voltltge control of power converter, input and output powers.

The parameters P_{em} (line 5) are used for the offline simulation of the process. The online operation of the control algorithm is parameters free. These is the main advantage of the DDC method.

In the main loop there are called the following functions:

- The *PI_control* which calculate the actual torque set point m^{ref} using the measured past speed ω_m^{old} and the speed set point ω_m^{ref} , and the tuning parameters K_p and K_i ;
- The matlab *RBF_Interpolant* function which interpolate the control surfaces (24) by scattered support points contained in DB 1;
- The function *Process_Model* which calculate the actual process variables (i_d, i_q, m, ω) and the powers p_1, p_2 .

Algorithm 2. The DDC main program

```

% Load Data_Base1
1. Load('DB1', $\omega\omega$ ); Load('DB1',mm); Load('DB1', $u_d^{ftr}$ ); Load('DB1', $u_q^{ftr}$ );
% Initialization for the 8 possible values of the inverter voltages components
2.  $v_d=[0;2;1;-1;2;-1;1;0]*U_{DC}/3$ ;
3.  $v_q=[0;0;1;-1;0;-1;-1;0]*\sqrt{3}/3*U_{DC}$ ;  $\underline{v}=v_d + v_q^*$ ;
% Initialization of the electromagnetic parameters
4.  $svs=[000; 100; 110; 010; 011; 001; 101; 111]$ ; %Switching vector states inverter's gate control
5.  $\mathcal{P}_{em}=[m\tau, J, \mu, R_s, L_d, L_q, \psi_{PM}]$ ; %Declare process and machine parameters (*)
6.  $\omega^{ref} = \omega^{rated}$ ;  $m^{max} = 2.5*m^{rated}$ ; % Initialization of the desired speed and maximum torque
7.  $\omega^{old} = \omega^{init}$ ;  $i_d^{old} = 0$ ;  $i_q^{old} = 0$ ;  $u_d^{old-ref} = 0$ ;  $u_q^{old-ref} = 0$ ;  $v_d^{opt} = 0$ ;  $v_q^{opt} = 0$  %Initializations
8.  $T_s = 1e-4$ ;  $T_d = 10s$ ;  $N = T_{desired}/T_s$ ;  $T_{int} = 2$  %Sampling period ( $T_s$ ), desired simulation time ( $T_{desired}$ ), integration
9.  $H_m = 8$ ;  $du_d = 0$ ;  $du_q = 0$ ;  $g-opt = 1e7$ ; %  $H_m$  is shaping horizon,  $du_d$ ,  $du_q$ , are the control corrections
10.  $\mathcal{F}_d = \text{RBF\_Interpolant}(\omega\omega, mm, u_d^{ftr})$ ;  $\mathcal{F}_q = \text{RBF\_Interpolant}(\omega\omega, mm, u_q^{ftr})$ ; % Learning algorithm
11. for n=1:N
12. if (mod(n, $H_m$ )) == 0 % the speed loop is the  $H_m$  time is slower then DDC algorithm
% Call function PI_control
13.  $[m^{ref}] = \text{PI\_control}(\omega^{ref}, \omega^{old}, m^{max}, K_p, K_i)$ ;
% Call interpolation algorithm by means of Data_Base 1 (speeds  $\omega\omega$ , torques mm and controls  $u_d^{ftr}$ ,  $u_q^{ftr}$ )
14.  $u_d = \mathcal{F}_d(\omega^{old}, m^{ref})$ ;  $u_q = \mathcal{F}_q(\omega^{old}, m^{ref})$ ; % DDC law
15. end % end if
%Shaping the finite states of inverter
16.  $u_d^{ref} = u_d^{old-ref} + T_{int}(u_d^{ref} - v_d^{opt})$ ;  $u_q^{ref} = u_q^{old-ref} + T_{int}(u_q^{ref} - v_q^{opt})$ ;
17.  $u_d^{old-ref} = u_d^{ref}$ ;  $u_q^{old-ref} = u_q^{ref}$ ;
18. for  $H_m = 1:8$ 
19.  $g = \text{abs}((u_d^{ref} + 1 * u_q^{ref}) - \underline{v}(ss))$ ;
20. if ( $g < g-opt$ )
21.  $g-opt = g$ ;
22.  $ss_{opt} = ss$ ;
23. end % end if
24. end % end for
25.  $v^{opt} = \underline{v}(ss_{opt})$ ;  $v_d^{opt} = \text{real}(v(ss_{opt}))$ ;  $v_q^{opt} = \text{imag}(v(ss_{opt}))$ . % end of shaping
% Call Proces_Model
26.  $[i_d, i_q, m, \omega, p1, p2] = \text{Proces\_Model}(v_d^{opt}, v_q^{opt}, i_d^{old}, i_q^{old}, \omega^{old}, \mathcal{P}_{em})$ ;
27.  $i_d^{old} = i_d$ ;  $i_q^{old} = i_q$ ;  $\omega^{old} = \omega$ ;
28.  $[u_d^{ftr}, u_q^{ftr}] = \text{Mouving\_Average}(v_d^{opt}, v_q^{opt}, L, T_s)$ ; % L is the length of the moving window filter
% Save process outputs in Data_Base_2
29.  $[i_{dd}(n), i_{qq}(n), mm(n), \omega\omega(n), u_{dd}^{ftr}, u_{qq}^{ftr}, pp1(n), pp2(n)] = \text{Data\_Base\_2} = (i_d, i_q, m, \omega, u_d^{ftr}, u_q^{ftr}, p1, p2)$ ;
30. end % end for

```

Figure 19. The DDOC control algorithm of a PMSM drive control.

The control $u(a) = u_d(a) + ju_q(a)$ are the query of the actual points $(\omega_m^{old}, m^{ref})$ for the surfaces \mathcal{F}_d and \mathcal{F}_q . These controls are sampled from the continuous time domain. The inverter is controlled by the finite states switching functions svs . The transformation of the controls u_d and u_q from continuous time domain in the finite states domain of the inverter's switching vectors v_d and v_q is a synthesis process.

The actual control $\underline{u}(a)$ at the step a is synthesized by a finite set of the switching vectors $\underline{v} = v_d + jv_q$ as follows

$$\begin{aligned} \mathbf{u}(a) &= \{v_k^{opt}(r), v_k^{opt}(r+1), \dots, v_k^{opt}(r+H_m)\}, \\ r &= 1, \dots, H_m, \\ a &= 1, \dots, N_{obs}. \end{aligned} \quad (87)$$

where H_m is the horizon of modulation and each $v_k^{opt}(k)$ vectors are determined with a searching procedure, minimizing the g criteria function. The dimension of the H_m horizon was chosen by analogy with the classical modulation.

4. Illustrative Case Study of DDC of a PMSM Drive System

An industrial PMSM from a drive system supplied by a power inverter is used to illustrate the proposed DDC approach by comparison with the MPC control in the order to check the optimal energy operation. The PMSM rated data are depicted in Table 2.

Table 2. PMSM rated specifications data.

Symbol	Description	Values
P_N [W]	Rated power	5500
U_N [V]	Rated voltage	325
m_N [Nm]	Rated torque	35
I_N [A]	Rated current	10.6
ω_{mN} [rad/sec]	Rated speed	157
R_s [Ω]	Rotor resistance	0.65
L_d [H]	Direct axis inductance	0.0082
L_q [H]	Quadrature axis inductance	0.0082
J [kg·m ²]	Total inertia of the PMSM drive	0.5
z_p	Stator pole pairs	2

The illustrative case study is done in Matlab-Simulink software in command-line line implementation programs. For simulation it has been adopted the sampling time period $T_s = 10^{-4}$ s. Also, the speed loop is designed by choosing a linear control law implemented by PI controller designed by pole placement method, resulting the parameters $K_{p\omega} = 30$ and $K_{i\omega} = 0.1$. As a priori data \mathcal{K}_{DB} there are considered the PMSM parameters (Table 2), rated data for a conventional power inverter with DC link voltage $U_{DC} = 520$ V, the PMSM operate in a closed loop.

A first objective is the designing of database used for DDC strategy based on the high efficiency data collected from the MPC strategy running of PMSM. The second aim is to check the results of a comparative analysis obtained by MPC and DCC in rated conditions. To study a high impact of the DDC method, a third scope is to make a comparative analysis of the results obtained via MPC and DCC strategies in mismatch conditions. Finally, a performance comparative analysis of the previous results obtained via MPC and DDC strategies for rated and mismatch conditions is done in the order to demonstrate that the developed DDC method in the paper is a relevant topic for future research.

4.1. Database Learning Design

The essential point in DDC method is the DB design. Firstly, there are the bootstrap DB obtained from process design theoretical data and parametric offline of the process.

From this large knowledge and data DB we extracted the control (working) DB. The control DB contains a few optimal efficiency steady-state operation points of the process (around 250), obtained in exogenous conditions. In our case the exogenous conditions are the ambient temperature T^0 and rated flux ψ_{PM} . Tacking into account the ambient conditios the control becomes:

$$\tilde{\mathbf{u}} = \mathcal{A}_F(\omega_m, m, T^0, \psi_{PM}). \quad (88)$$

In consequence, the control DB must be extracted, and the RBF interpolation block will have four inputs and two outputs controls.

In this paper we applied the direct searching corrections of the controls in the sens of maximum energy efficiency. This corections are global or local.

A gridded experimental data points was obtained by simulating the MPC control algorithm, providing an admissible set of the operation points of the process selected in steady-state regime for the highest efficiency values.

There were adopted voltage global correction on the entire DB:

$$\begin{cases} u_d^{DDC} = u_d^{MPC} k_d \\ u_q^{DDC} = u_q^{MPC} k_q \end{cases}, \quad (89)$$

where the factors $k_d=1.04$ and $k_q=1$ are selected in the order to improve the DDC performances.

The local DB corection are applied around a steady-state points. This kinds of corrections are applied mainly online in steady-state operation, in the sense of searching the maximum energy efficiency, in the actual exogenous conditions,

Based on this set experimental data, in Figure 20 it was built the discrete implicit surfaces of the high efficiency DDC control law $\eta^{DDC} = f(\omega_m^{DDC}, m^{DDC})$, which contains around 250 points of steady-state higher efficiency operation given by MPC strategy.

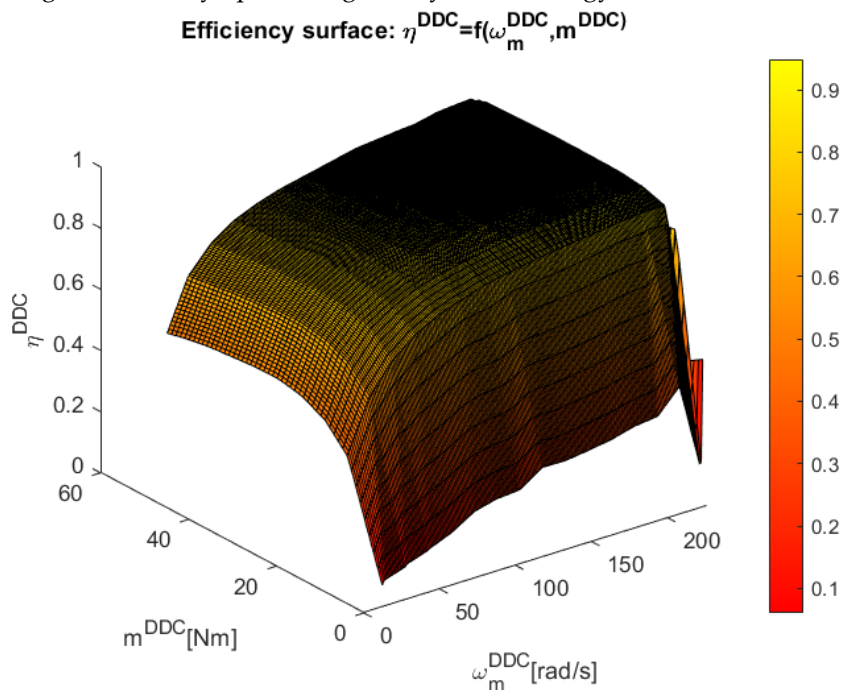


Figure 20. The efficiency surface vs. speed and torque.

A more attention must be paid for representing the control sufaces in Figure 21 and Figure 22 of the control implicit surfaces $u_{d/q} = f(\omega_m^{DDC}, m^{DDC})$.

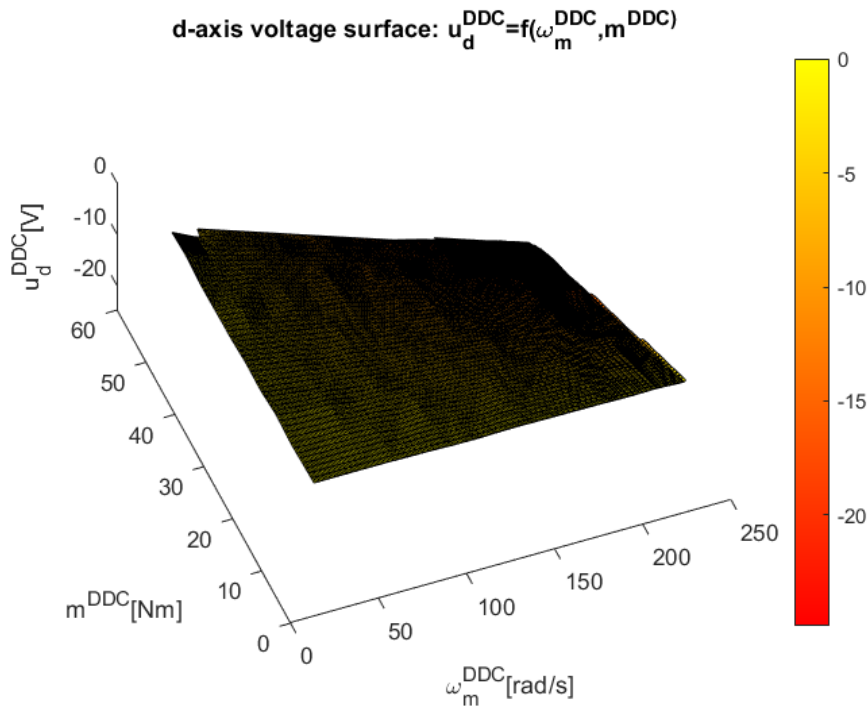


Figure 21. The d -axis voltage surface vs. speed and torque.

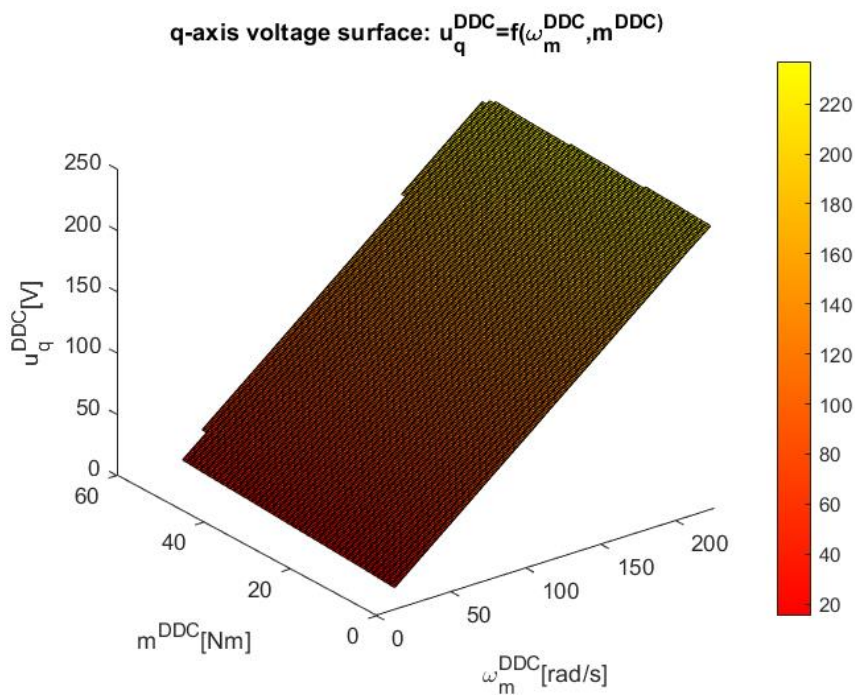


Figure 22. The q -axis voltage surface vs. speed and torque.

4.2. Study on Rated Data Conditions

In this section is provided a comparative analysis of the results obtained via MPC and DDC in rated conditions provided by the model parameters of PMSM from Table 2.

Adopting a speed step reference of $\omega_m^{ref} = 175 \text{ rad/s}$, in Figure 23 is depicted the speed tracking results obtained by MPC and DDC strategies. The speed provided by DDC method ω_m^{DDC} and MPC one ω_m^{MPC} present close responses, but the DDC has a sensible lower transient regime.

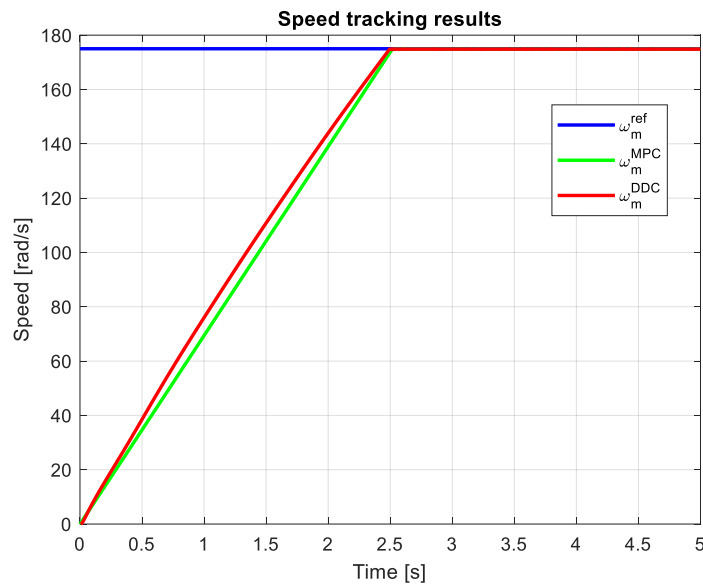


Figure 23. The speed tracking results obtained for MPC and DDC control strategies.

The current results provided by MPC and DDC strategies are illustrated in Figure 24. In the case of d -axis current component, the MPC law offers a small value then the corresponding one of DDC law in absolute values $|i_d^{MPC}| < |i_d^{DDC}|$. After a different dynamic regime, the q -axis current component presents close values in steady state regime for for both DDC and MPC controllers.

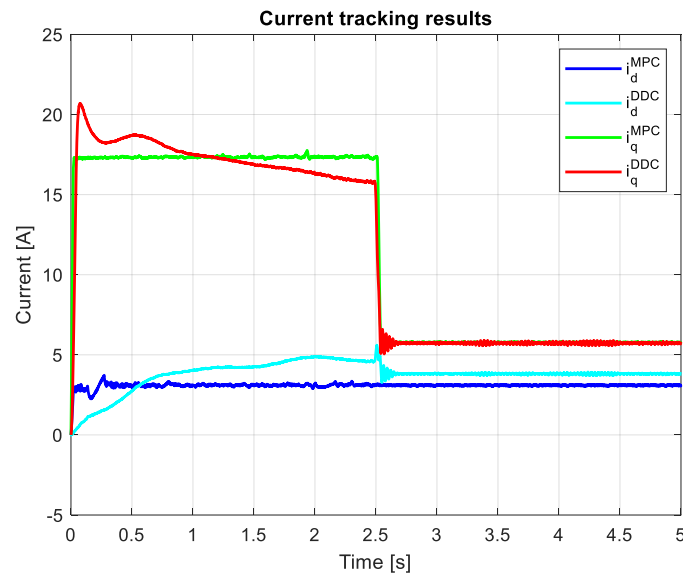


Figure 24. The current results obtained for MPC and DDC control strategies.

On the shaft of the PMSM drive is applied a step load torque $m_\ell = 17.5 \text{ Nm}$. The load and electromagnetic torques provided by MPC/DDC laws are represented in Figure 25. Excepting the startup process, in dynamic regime the electromagnetic torque obtained by DDC is smaller than one given by MPC $m^{DDC} < m^{MPC}$. However, the speed transient leads to have a higher dynamic torque regime for DDC method.

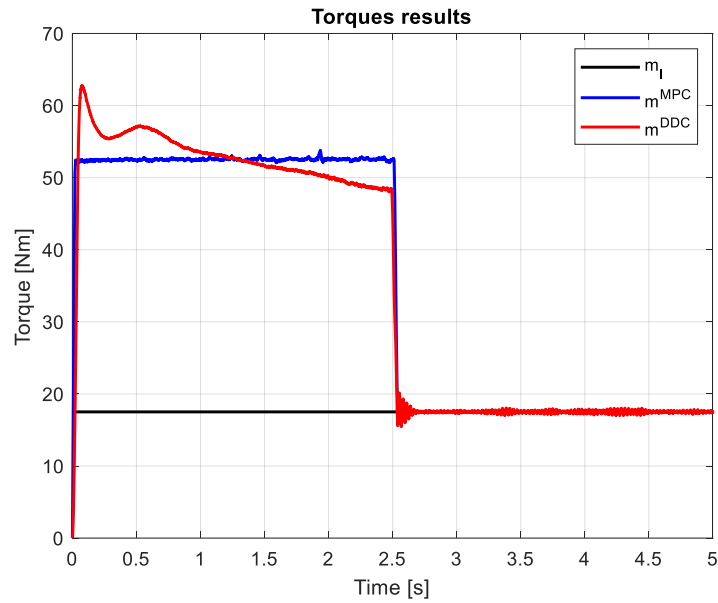


Figure 25. Load and electromagnetic torques for MPC and DDC control strategies.

Figure 26 indicates the voltages obtained by both MPC and DDC strategies $u_{d/q}^{MPC}$ and $u_{d/q}^{DDC}$. As a consequence of the increasing of the q -axis voltage component provided by DB, this difference is seen in the figure, having $u_d^{MPC} > u_d^{DDC}$. For d -axis, the voltage component have closed values for MPC and DDC strategies.

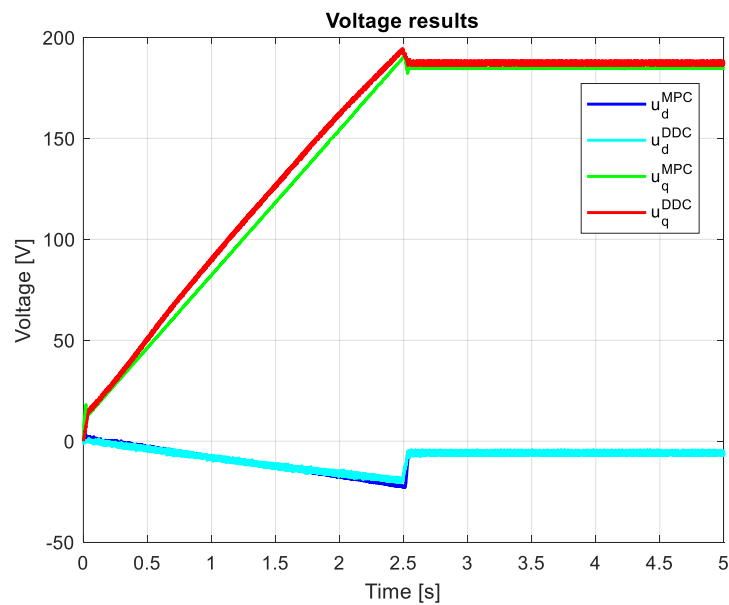


Figure 26. Voltage components for MPC and DDC control strategies.

To have a concrete appreciation of the current tracking or voltage delivered by the control system of PMSM, in the following there are evaluated the current/voltage magnitude computed according to:

$$I = \sqrt{I_d^2 + I_q^2}, \quad (90)$$

$$U = \sqrt{u_a^2 + u_q^2}, \quad (91)$$

which are graphically illustrated in Figure 27 and Figure 28. It can be seen that, after the startup, during the transient regime the DDC method provide a lower value then de corresponding one given by MPC strategy $I^{DDC} < I^{MPC}$, and in steady-state regime becomes grater $I^{DDC} > I^{MPC}$.

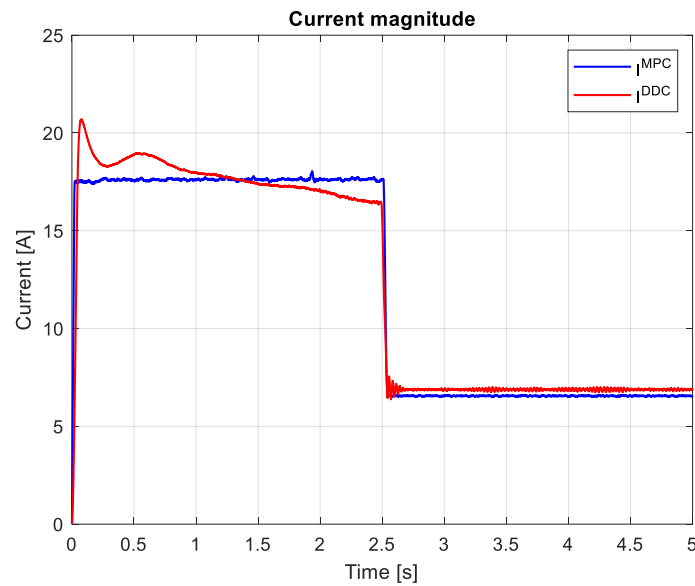


Figure 27. Current magnitude for MPC and DDC control strategies.

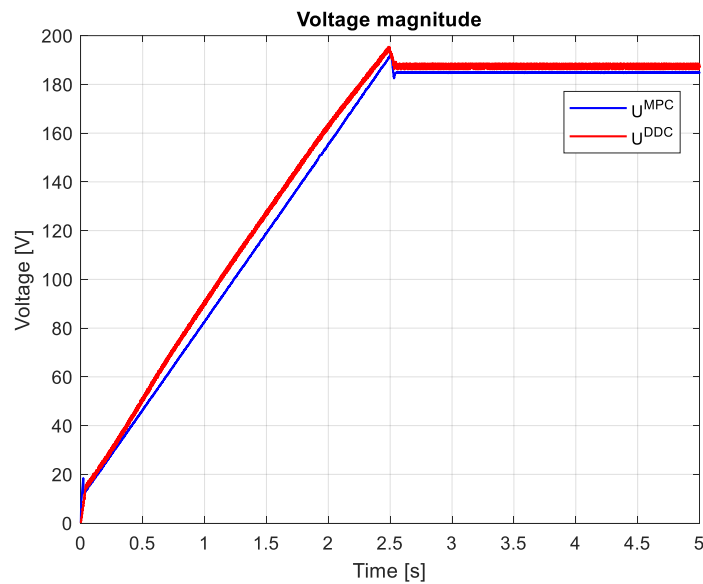


Figure 28. Voltage magnitude for MPC and DDC control strategies.

The efficiency of PMSM obtained by MPC and DDC control strategies in depicted in Figure 29. As expected, the new control technology provides advanced benefits as parameter free and high efficiency objective. Thus, the dynamic efficiency compared with the classical one steady state efficiency is greater $\eta^{DDC} > \eta^{MPC}$.

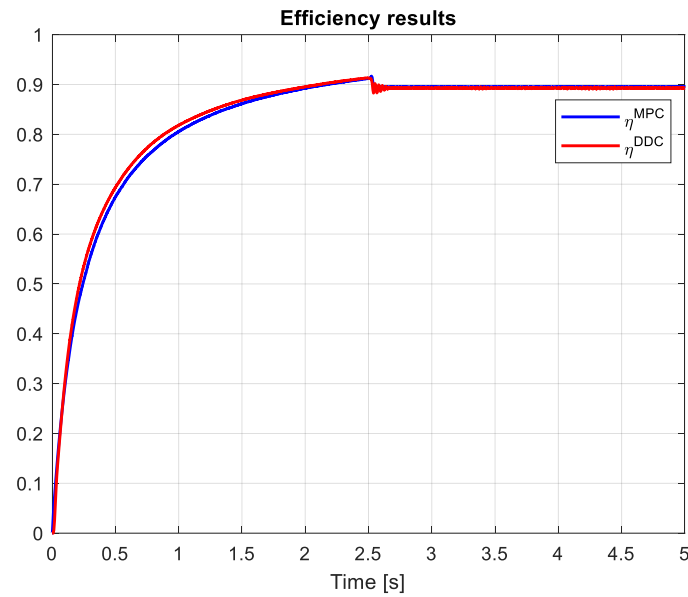


Figure 29. Efficiency of PMSM for MPC and DDC control strategies.

To evaluate the efficiency of the PMSM on the entire simulation domain, there is used the average efficiency defined according to:

$$\eta^{av} = \frac{\sum_{a=1}^{N^{obs}} \eta(a)}{N^{obs}}, \quad (92)$$

which is graphically represented in Figure 30.

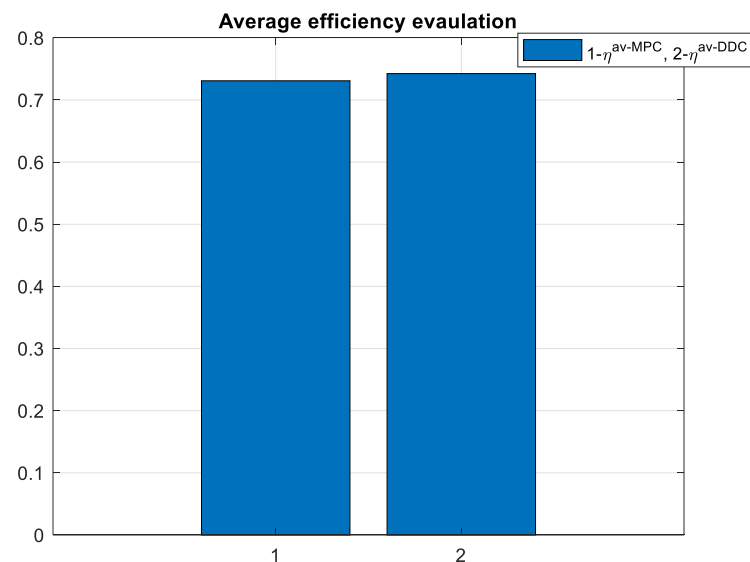


Figure 30. Average efficiency of PMSM for MPC and DDC control strategies.

Finally, it is important to use the phase currents. Since the PMSM has a symmetric mechanical and electrical structure, the system of currents is also symmetrical, which is why only the current on the first phase $i_a^{MPC/DDC}$ will be represented as in Figure 31. The peak of the phase current provided by DDC method has a high value then one given by MPC law.

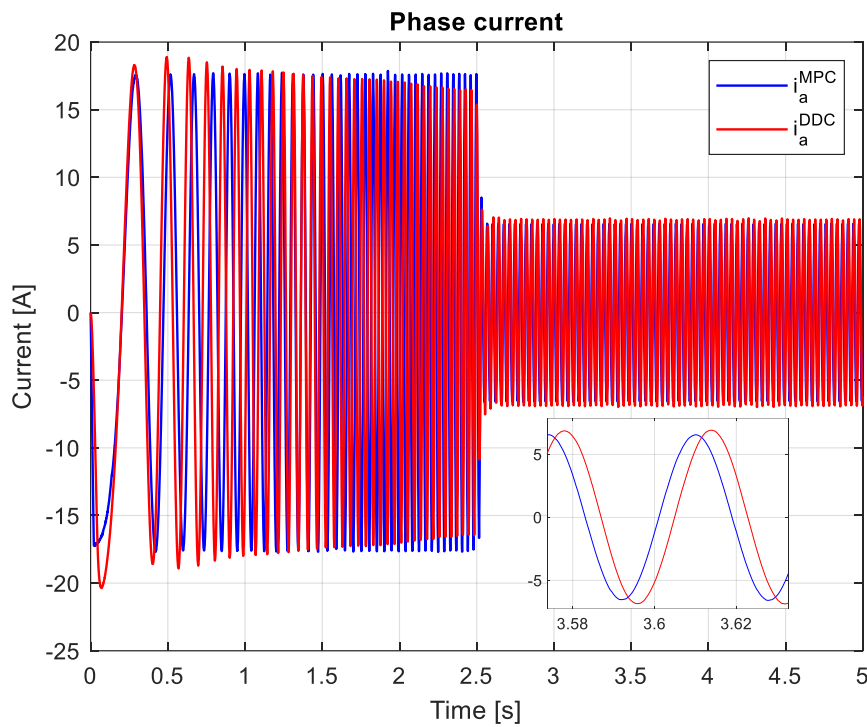


Figure 31. Phase current of PMSM for MPC and DDC control strategies.

A first conclusion is that the DDC strategy may operate without any mathematical model, being also parameter-free. The key of DDC strategy operation is related on database design, learning process and available computational resources. A more important appreciation is that DDC improve both tracking references and efficiency. However, the DDC strategy remains stable in the imposed simulation scenario.

3.3. Study on Mismatch Conditions

Often, in practice the dq PMSM model with constant lumped parameters is just an idealization which cannot always be fulfilled.

In the following is considered there the next variations of the parameters of the dq model of PMSM due to demagnetization and temperature increasing, respectively, as follows:

$$\begin{cases} \psi_{PM} \rightarrow 0.8\psi_{PM} \\ R_s \rightarrow 1.4R_s \end{cases}, \quad (93)$$

otherwise, all the conditions remain unchanged.

In this case, the speed tracking results obtained by MPC and DDC strategies are illustrated in Figure 32. Now, again, the speed obtained by DDC strategy ω_m^{DDC} has a shorter dynamic regime than the one given by MPC law ω_m^{MPC} . The speed response is even better than the one obtained in the rated scenario. For MPC strategy, the results get worse once with parameters mismatch.

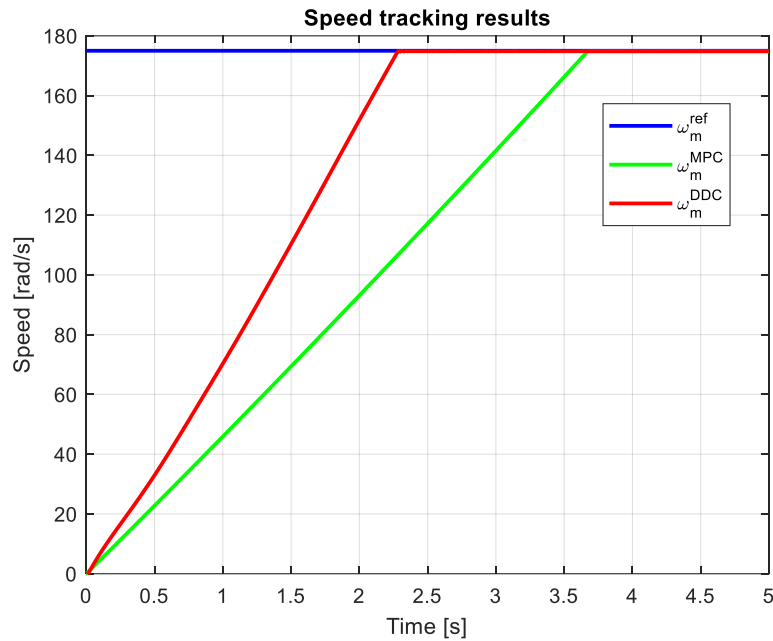


Figure 32. The tracking results of speed obtained via MPC and DDC control laws.

For current results given by MPC and DDC laws, both transient and steady-state regimes are different as is depicted in Figure 33. The d -axis current component delivered by MPC controller and the one of DDC law in have different values in dynamic regime, and closed in steady-state regime. On q -axis, the current given by MPC and DDC have different values in both dynamic and steady-state regime.

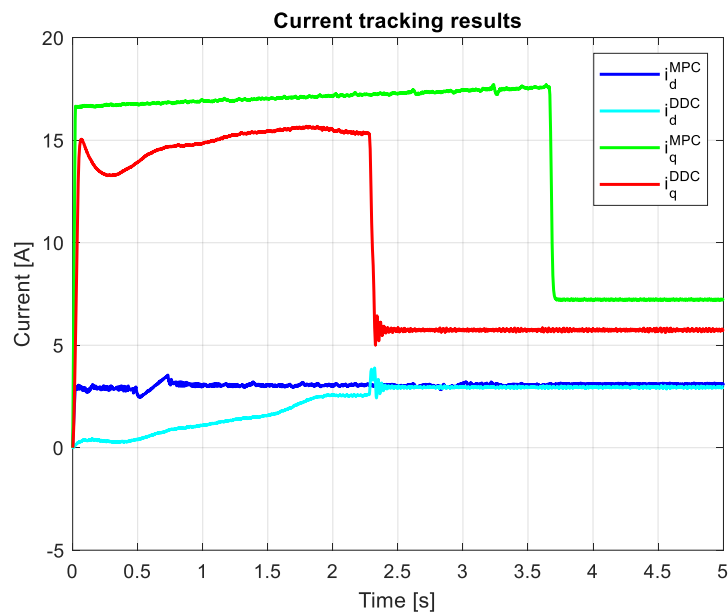


Figure 33. The dq current obtained for MPC and DDC control laws.

Applying the same step load torque $m_t = 17.5Nm$, the load and electromagnetic torques obtained by MPC/DDC strategies have different dynamics as is graphically depicted in Figure 34. The dynamic torque given by DDC has a higher value than the one provided by MPC $m^{DDC} > m^{MPC}$

, but acts in a short transient. Thus, the evolution of electromagnetic torques is done with different dynamics until the main disturbance represented of the load torque is rejected.

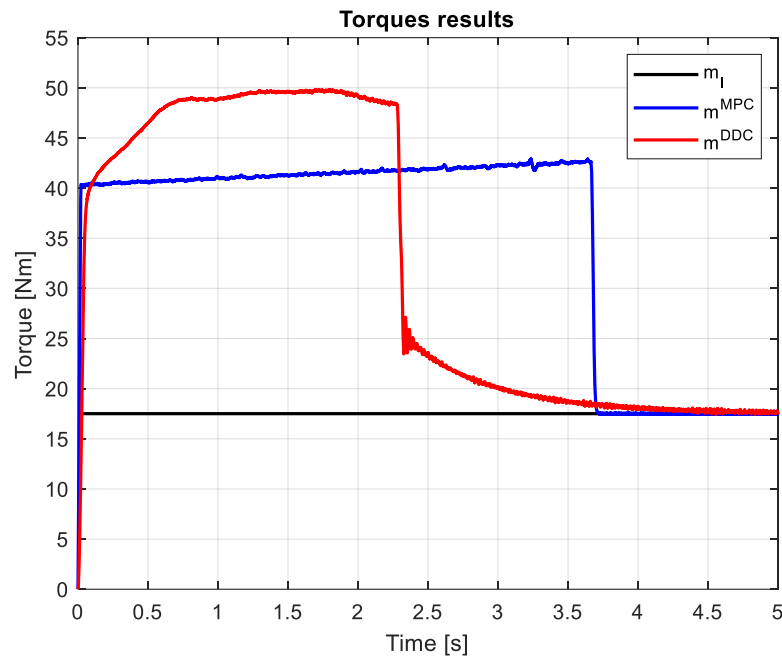


Figure 34. Load torque disturbance rejection for MPC and DDC control strategies.

The voltages provided by both MPC and DDC strategies $u_{d/q}^{MPC}$ and $u_{d/q}^{DDC}$ are shown in Figure 35. On d-axis, the voltage components present appropriate values, with small differences in dynamic regime. Important differences are founded on q -axis, where $u_d^{DDC} > u_q^{MPC}$ has a significant value, mainly in steady-state regime.

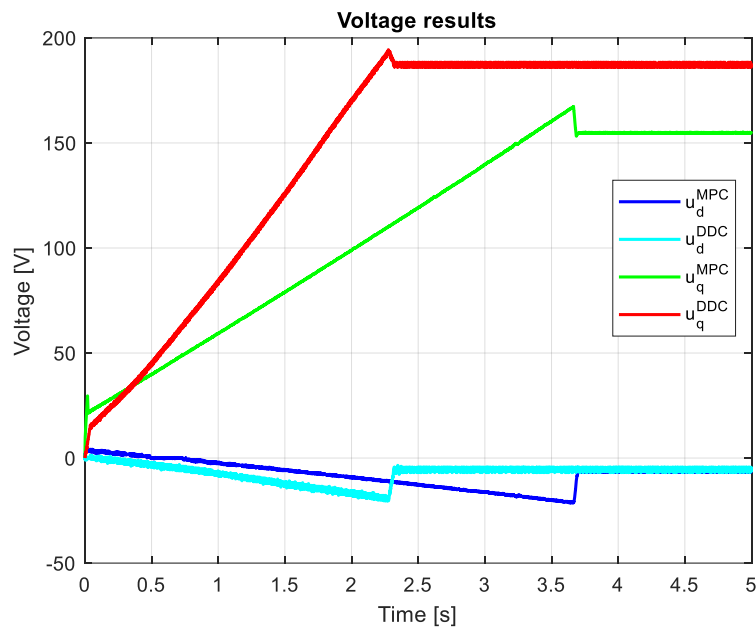


Figure 35. Voltage obtained by MPC and DDC control strategies.

The magnitude of current and voltage are represented in Figure 36 and Figure 37, respectively. The current magnitude obtained by DDC law is always smaller than the one given by MPC algorithm $I^{DDC} < I^{MPC}$. Mostly, a significant increasing of the voltage magnitude for DDC algorithm than MPC controller is obtained $U^{DDC} > U^{MPC}$.

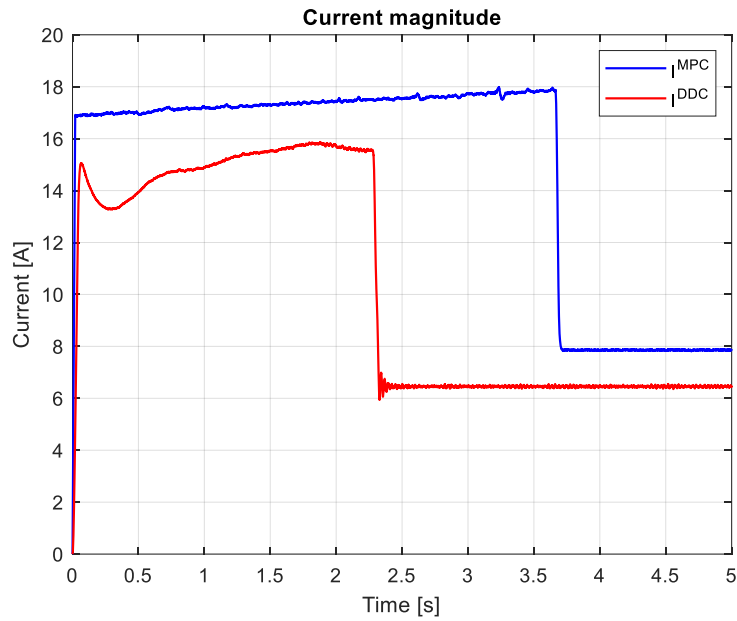


Figure 36. Current magnitude given by MPC and DDC control algorithms.

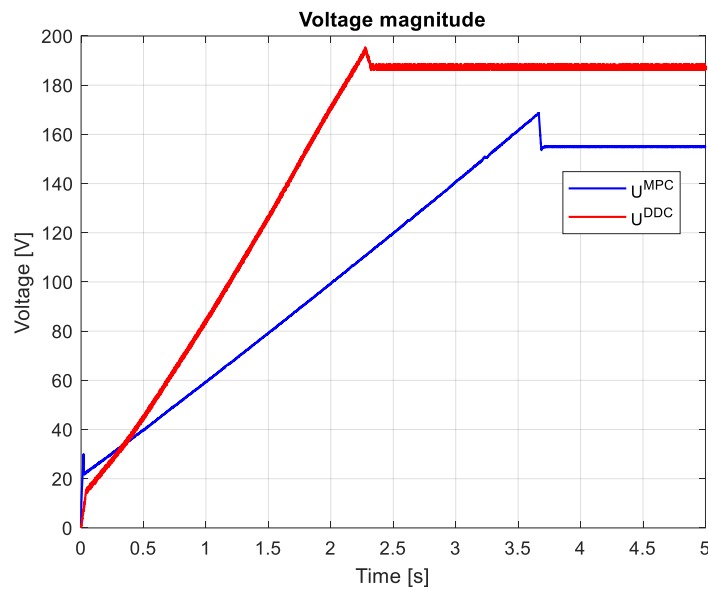


Figure 37. Voltage magnitude given by MPC and DDC control algorithms.

The efficiency of PMSM obtained by DDC law is substantially increased the the one provided by and DDC strategy $\eta^{DDC} > \eta^{MPC}$ in both dynamic and steady state regimes, as illustrated in Figure 38. This is a consequence of the fact that DDC method is designed by using the high-efficiency data collected from MPC operation. This is a major objective done in this robust scenario.

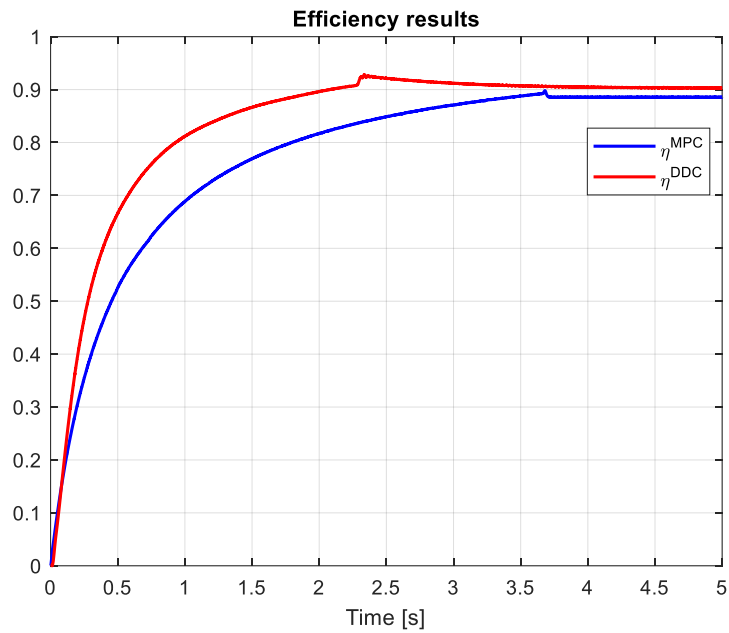


Figure 38. Efficiency of PMSM obtained by using MPC and DDC control algorithms.

As expected the average efficiency for the entire simulation time is increased for DDC method $\eta^{av-DDC} > \eta^{av-MPC}$ as is graphically depicted in Figure 39.

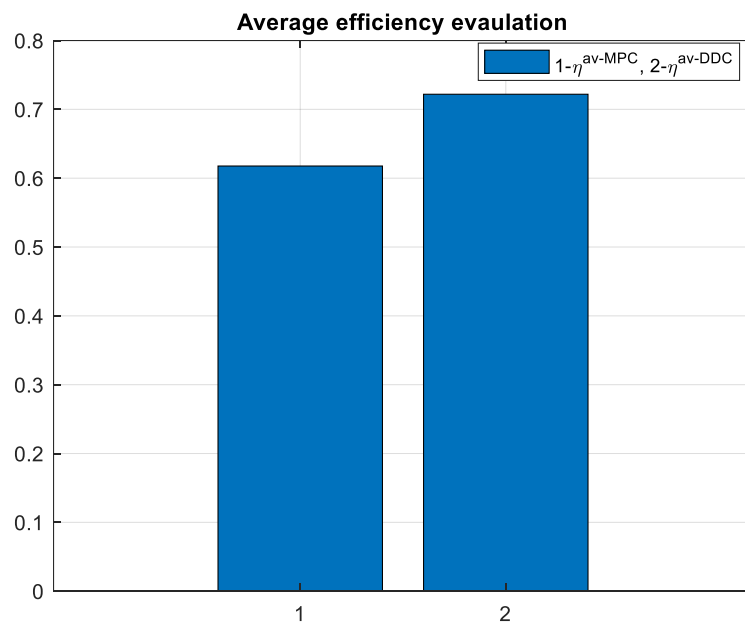


Figure 39. Average efficiency of PMSM provided by using MPC and DDC control algorithms.

In this scenario, the phase current obtained by DDC strategy has a smaller peak value than the one delivered by MPC algorithm in both transient and steady-state regimes as is shown in Figure 40. However, a small peak value will generate reduced power losses, and then the increasing of the efficiency of PMSM. The DDC strategy is designed by using a database learning that no not contain overcurrents, feature which will maintain the phase current into a minimal range.

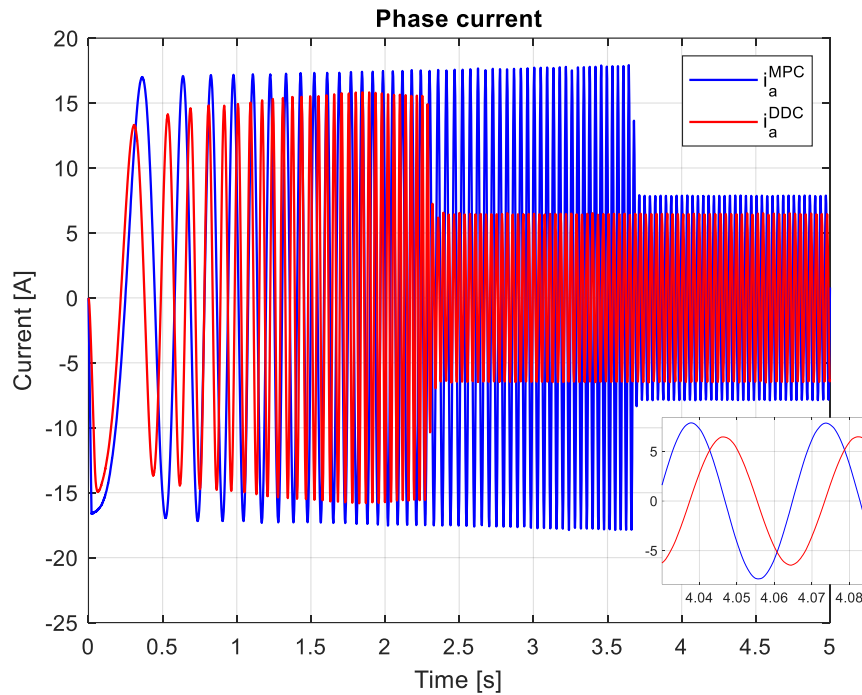


Figure 40. Phase current for MPC and DDC control algorithms.

The study developed in this section shows the results given by DDC strategy under robustness conditions of PMSM parameters mismatch. The main objective of the efficiency increasing has been successfully shown. However, this objective leads secondary to decrease the dynamic regime of speed tracking. Compared with MPC strategy, the DDC law requires a higher voltages magnitude/components which must take into account the voltage limit levels of the PMSM drive. Also, the DDC strategy leads to obtain a smaller peak value of the phase current that will generate lower level of power losses.

3.4. Comparative analysis of MPC and DDC results

The proposed DDC method proves to have a stable operation on the rated an mismatch cases and, also offers several benefits. For a relevant comparison of the above discussed cases, there are used the next criteria:

- Settling time of the mechanical speed – t^{st} ;
- Average efficiency on the entire simulation time – η^{av} ;
- Peak value of the a phase current in steady-state regime – I_a^{pk} ;
- THD of the a phase current computed in steady-state regime, for ten harmonics, including the fundamental of the frequency 55.66 Hz, for a common time domain pf MPC and DDC strategies, 4-5 s time.

The comparative results based on the above criteria of the MPC and DDC strategies are summarized in Table 3.

Table 3. The comparative evaluation of MPC and DDC strategies.

Test	Control strategy	t^{st} [s]	η^{av}	I_a^{pk} [A]	THD_a [%]
Rated conditions	MPC	2.52	0.730	6.55	0.06
	DDC	2.50	0.742	6.96	0.17
Mismatch conditions	MPC	3.68	0.612	7.86	0.08
	DDC	2.28	0.722	6.44	0.13

It is obvious that in both tests, compared with MPC law, the DDC strategy leads to decreasing of the settling time of the mechanical speed $t^{st-DDC} < t^{st-MPC}$. In rated conditions there is obtained a small difference, but in the mismatch test the DDC method leads to a setting time with 61% lower than the one obtained by MPC strategy, which is a high advantage. For rated conditions, the increasing of the average efficiency is small for DDC strategy $\eta^{av-MPC} > \eta^{av-DDC}$, being around 1.2 % from the one resulted in rated conditions with MPC controller. A high increasing of the DDC average efficiency $\eta^{av-DDC} > \eta^{av-MPC}$, about 11 % results for mismatch test, which is the major successfully, achieved objective. In addition, the peak value of the phase current for rated conditions is smaller for DDC, $I_a^{pk-DDC} < I_a^{pk-MPC}$, and higher in the mismatch case $I_a^{pk-DDC} > I_a^{pk-MPC}$. As a consequence of interpolation and digital signal processing, the THD of the phase current obtained by DDC law remains low for both rated/mismatch cases studied.

We can conclude that DDC strategy persevere better the high efficiency objective in the both rated and robust scenarios than the classical MPC law. Nevertheless, the settling of speed responses has been also improved in the both tests.

Finally, it should be noticed the results of the performances presented in Table 3 are open to be improved since the results depends on the learning process and on software and hardware available resources.

5. Conclusions

The many faces of the macroscopic energy conversion systems may be characterized by a set of generalized variables as effort and flow. This approach allows a physical – based mathematical equation modeling developed in the order to increase the efficiency of energy conversion.

In spite of the high performances of actual devices and actuators for the energy transformation, there are enough resources for the improvements of their efficiency, especially in the operation points at low effort and high flow or respectively at high effort and high flow.

A transition from MBC to MFC is required for ensuring the non-sensitive control approach.

The idea of the paper is to build the surfaces of the DDC law in terms of effort and flow. Starting from a large knowledge DB we built a control DB containing a reasonable optimal efficiency steady state operation points of the process. A RBF interpolative system has been trained in order to extract from this surfaces the controls demanded for any operation points. It results that the control efficiency is largely dependent from the consistency of the collected data.

The AC drives is a field that emphasis the largely developed fast process in industry and residence. The performances of this DDC method were evaluated based on a PMSM drive system simulated by MPC methodology. The DB was built in Matlab simulation environment using a specific algorithm for the MPC control of PMSM drive and the algorithm of DDC. The comparison criteria were the efficiency of the energy process conversion (the ratio of the output and input powers), the quality of the control for speed and effort and the current THD. Due to the PMSM windings resistance variations and to the degree of the magnetic circuit depreciations during the time, the DDC efficiency control is better than MPC control, because the MPC is model parameters dependent.

In many research papers in the field has been demonstrated that the direct DDC strategy is superior in reduction the bias whereas the indirect MPC one gives better variance. The results shown in Figure 36 and Figure 38 confirm the fact that the MPC control gives better variance but the DDC gives better efficiency and bias to process parameters modifications.

Our DDC technique, being process parameters free is more general than classical process model control as MPC, in the sense that does not depend on the nature of process (electromagnetic, thermic or mechanic). If we refer on the electric driven systems, DDC technic is the same for all type of motors (asynchronous, synchronous or others).

The DDC method with appropriately designed management make possible to realize a high level of the energy transformation quality that is fast dynamic response, high energy efficiency and low parametric sensitivity.

The multiple aspects discussed and successfully solved in the paper shows that the novel technology developed in the paper is still an open problem which can provides realistic improved results in a future promising approach.

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Data Availability Statement: Data availability is not applicable to this article as the study did not report any data.

Conflicts of Interest: The authors declare no conflict of interest.

Abbreviations

<i>AC</i>	<i>Alternative Current</i>
<i>AIMs</i>	<i>Artificial Intelligence Methods</i>
<i>DB</i>	<i>DataBase</i>
<i>DDC</i>	<i>Data Driven Control</i>
<i>DC</i>	<i>Direct-current</i>
<i>EDSs</i>	<i>Electric Drive Systems</i>
<i>EMF</i>	<i>ElectroMotive Force</i>
<i>HVAC</i>	<i>Hydro, Ventilation, Air Conditioning</i>
<i>MBC</i>	<i>Model Based Control</i>
<i>MFC</i>	<i>Model Free Control</i>
<i>MPC</i>	<i>Model Predictive Control</i>
<i>NN</i>	<i>Neural Network</i>
<i>PI</i>	<i>Proportional-Integral controller</i>
<i>LPF</i>	<i>Lower Pass Filter</i>
<i>PMSM</i>	<i>Permanent Magnet Synchronous Machine</i>
<i>RBF</i>	<i>Radial Basis Function</i>
<i>RL</i>	<i>Reinforcement Learning</i>
<i>THD</i>	<i>Total Harmonic Distorsion</i>
<i>QP</i>	<i>Quadratic Programming</i>
<i>WB</i>	<i>White-Box</i>

Nomenclature

(a,b,c)	Three phase coordinates
\mathcal{A}_F	Set of the weights of the RBF-NN
(α,β)	Fixed coordinates
α_m	Electric position of the rotor
$\mathbf{d}^{MBC/MPC}$	Set of processing data obtained by MBC/MPC
$\mathbf{d}^{oMBC/MPC}$	Steady-state set of processing data obtained by MBC/MPC
\mathbf{d}^{oe}	Set of data obtained by grid learning
$\mathbf{C}_c, \mathbf{C}_d$	Continous/discrete cost
\mathcal{D}_F	DB of knowledge and data of the process
Δ	Unit-delay
e	Effort
$e_{d/q}$	d/q electrical EMF components
$E_{f,RMS}, E_{n,RMS}$	RMS value of fundamental/ Harmonics components of the effort e
\mathbf{E}_N	Set of envirovment data
E_1, E_2	Input/output energy
emf	Motion ElectroMotive Force (EMF)
ε	Mean square error
η, η^{av}	Efficiency/Average efficiency
ζ	Discrete noise of the process state model
\mathbf{F}	Operator of control law
\mathbf{f}, \mathbf{g}	Nonlinear function of the state representation
F_i	Explicit control law
f_ε	Implicit represenation of the process model
f_u	Useful force
$f_{1/2}$	Components of surface grid representation
$\mathbf{f}_{m/p}$	Multi-valued map of torque/output power
$\mathbf{f}'_{m/p}$	Single-valued map of torque/output power
ψ_{PM}	Permanent magnet flux
φ_i	Gaussian distribution
$\Phi^{MBC/MPC}$	Training data set given by MBC/MPC
g	Cost function
G_i	Implicit control law
g_1, g_2	Generalized variables of trajectories
$\Gamma_{m/p}$	Set of speed and torque/output power and efficiency
$\Gamma'_{m/p}$	Set of speed and torque/output power and maximum efficiency
h/\mathbf{h}	Output of the space state model
H_m	Horizon of command shaping searching

H/H^{max}	<i>Set of efficiency/maximum efficiency</i>
H_N	<i>Set of design data</i>
i	<i>Index that corresponds to the combination of switching</i>
(i_d, i_q)	<i>Direct and quadrature current components</i>
\underline{i}	<i>Current phasor</i>
I_a^{pk}	<i>Peak value of the a phase current</i>
I	<i>Input of the RBF-NN</i>
J	<i>Motal inertia</i>
$k_{d/q}$	<i>Corection factor of voltage</i>
k_e	<i>Back motion EMF constant</i>
\mathcal{K}_{DB}	<i>Knowledge data</i>
l	<i>Index of the number of hidden neurons of the RBF-NN</i>
(L_d, L_q)	<i>Direct and quadrature inductances</i>
L_w	<i>Filter length</i>
LPF	<i>Lower Pass Filter</i>
λ	<i>Generalized variables for transformation of PMSM model</i>
$A_{m/p}$	<i>Set of the cartezian product of speed and torque/output power</i>
m, m_ℓ	<i>Electromagnetic/load torque</i>
M	<i>Set of electromagnetic torque</i>
\mathcal{M}_F	<i>Set of training data for RBF-NN</i>
\mathcal{K}_{ab}	<i>Set of the aprioric knowledge</i>
μ	<i>Center points of Gaussian function</i>
μ_f	<i>Friction factor of the load</i>
N	<i>Number of trajectory points</i>
$N_{\omega/m/p/h}$	<i>Number of points of the set of speed, torque, power, efficiency, respectively</i>
N_{obs}	<i>Number of observation points</i>
Q	<i>Flow rate</i>
θ	<i>Vector of parameters of the process state model</i>
P	<i>Pressure</i>
\mathbf{P}	<i>Set of output power</i>
p_1, p_2	<i>Input/output power</i>
\mathcal{P}_e	<i>Set of electrical parameters</i>
\mathcal{P}_m	<i>Set of mechanical parameters</i>
\mathcal{P}_{em}	<i>Set of electromechanical parameters</i>
\mathbf{R}_N	<i>Set of rated data</i>
R_s	<i>Stator resistance</i>

RMS	<i>Root mean square</i>
$Re\{\}, Im\{\}$	<i>Real/imaginary part of a given quantity</i>
s	<i>Flow</i>
\mathbf{S}_{abc}	<i>Set of the switching states</i>
σ	<i>Basis width vector of the Gaussian distribution</i>
t	<i>Time</i>
t_0, t_1	<i>Start/end time</i>
T_d	<i>Desired final time</i>
T_s	<i>Sampling time period</i>
T^0	<i>Temperature of stator winding of PMSM</i>
$\mathbf{T}_{\alpha\beta}, \mathbf{T}_{\alpha\beta}^{-1}$	<i>Direct/Indirect matrix of the Clarke transformation</i>
$\mathbf{T}_{dq}, \mathbf{T}_{dq}^{-1}$	<i>Direct/Indirect matrix of the Park transformation</i>
\mathbf{T}_i	<i>Power inverter matrix</i>
\mathbf{u}	<i>Control input</i>
$\hat{\mathbf{u}}$	<i>Any other control than the optimal one</i>
$\tilde{\mathbf{u}}$	<i>Control obtained via grid surface interpolation technique</i>
\mathbf{u}_{abc}	<i>Three-phase voltages</i>
\mathbf{u}_{dq}	<i>dq voltages</i>
\mathbf{u}^{ftr}	<i>Filter input</i>
\mathbf{u}^{RBF}	<i>Output of the RBF-NN</i>
\underline{u}	<i>Voltage phasor</i>
U_{DC}	<i>DC bus voltage</i>
(u_d, u_q)	<i>Direct and quadrature voltage components</i>
$(u_d^{ftr/nftr}, u_q^{ftr/nftr})$	<i>Filtred/non-filtred commande of the power inverter</i>
v	<i>Linear velocity</i>
$\mathbf{v}_{d/q}$	<i>Vectors of d/q components of power inverter</i>
$\mathbf{v}_{dq}^{c/opt-DDC}$	<i>Command/optimal voltage of the DDC algorithm</i>
ω_e, ω_m	<i>Electrical/mechanical angular speed</i>
$\omega_{m,b}$	<i>Based mechanical speed</i>
$\omega_{m,max}$	<i>Maximal mechanical speed</i>
ω_{mN}	<i>Rated mechanical speed</i>
\mathbf{x}	<i>State of the state model</i>
\mathbf{y}	<i>Output of the state model</i>
$\tilde{\mathbf{y}}$	<i>Output of the interpolation method</i>
\mathbf{y}^{ftr}	<i>Filter output</i>

z	Generic variable used for the applying of the forward Euler forward method
z_p	Stator magnetic poles pairs
w	Weights
\mathcal{W}	Database operator of data processing
Ω	Mecahical speed set

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