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Article

Pressure-Induced Graphene-like Si Layer in Ductile RuSi₂ with Ambient-Pressure Superconductivity and High Hardness

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Abstract: Of particular interest is the serendipity of distinctive nonmetallic layered frameworks with the stoichiometry of 1:2 in the binary metallic compounds within inorganic chemistry and materials science. This not only gives rise to the unexpected properties, especially the distinguished superconductivity, as reflected in MgB₂, MoB₂, NaC₂, LaP₂ and CeP₂, but also strengthens the cognition of the elemental contributions. Although various investigations on the superconducting performances in the alkali, alkaline-earth and rare-earth metal disilicides containing the silicon layers have been reported, the pursuit of superconductors with silicon-planar framework in transition metal disilicides remain unknown up to now. In the present work, crystal structure searches and first-principles calculations were thoroughly conducted in RuSi₂ within the pressure range of 0–300 GPa to uncover the novel structures, incredible silicon building block and the amazing properties. The ground orthorhombic *Cmca*-RuSi₂ phase at ambient pressure is a semiconductor with the band gap of 0.485 eV, whose hardness can reach 31.7 GPa. Even more intriguingly, the high-pressure orthorhombic *Cmcm*-RuSi₂ configuration with the fabulous graphene-like silicon-layer, which can be theoretically stabilized with the transformation pressure of 50.97 GPa, can be unexpectedly recovered to ambient pressure. Electron-phonon coupling calculations unravels that it possesses the metallic trait with an estimated *T_c* value of 1.43 K at 75 GPa, which increases to 10.07 K under ambient pressure. The enhanced *T_c* stems from the increased density of states at the Fermi level and associated with the coupled vibrations between Ru and the planar Si layer. Meanwhile, the hardness value for *Cmcm*-RuSi₂ is 26.8 GPa under ambient pressure, which further results from the three-dimensional covalent Ru-Si and Si-Si building blocks. The coexistence of superconductivity and high hardness in the *Cmcm*-RuSi₂ configuration under ambient pressure will pave the way for delving into more binary transition-metal silicides and correlated ternary silicides with the profound silicon layers.

Keywords: transition metal disilicide; 2D silicon layer; first principles; electronic property; superconductivity; hardness

Introduction

Last decade has witnessed the exuberant development of superconductor, which discloses a variety of advanced superconductor materials. Among these superconductors, a class of binary compound constituted by rich nonmetallic and metallic elements has garnered climbing interest from academic and industrial communities not only due to the considerable superconducting transition temperature *T_c* but also owing to the unprecedented nonmetallic polymetric configurations. In the binary hydride superconductors, the special H₂₄, H₂₉, H₃₂ and H₃₆ clathrate structures were verified in CaH₆ [1,2], YH₉ [3,4], LaH₁₀ [5,6] and CeH₁₈ [7] with the near or even above room-temperature *T_c* values of 205 K (172 GPa), 262 K (182 GPa), 250 K (170 GPa), and 329 K (350 GPa), respectively. Recently, another A-15 type structure of *Pm-3n*-Lu₄H₂₃ [8] was further proposed with a measured *T_c* value of 71 K (218 GPa), which consists of a combined clathrate structure of H₂₀ and H₂₄ cage. This

idea stems from the Si clathrate structures in $\text{Ba}_8\text{Si}_{46}$ [9,10] with the low-temperature properties. The high temperature T_c s in these hydrogen clathrate structures are closely associated with sodalite H clathrate structure, because the stretching and rocking vibrations of H atoms within H-cage contribute to strong electron-phonon coupling. Apart from the three dimensional (3D) hydrogen cage structure in the binary hydrogen-rich superconductor, two unpredictable hydrogen configurations with high T_c s enter into the scientists' horizon, which not only contains one-dimensional (1D) nanotubes in HfH_9 (110 K, 200 GPa) [11] and H_7 chains in GaH_7 (~100 K, 200–300 GPa) [12], but also consists of the momentous two-dimensional (2D) layered configurations. These 2D layered structures can be typified by the wavy H layer containing the edge-sharing pea-like H_{18} ring in LiH_4 (93.6 K, 100 GPa) [13], exotic layered structure composed of quasimolecular H_2 and linear H_3 units in KH_6 (58.6–69.8 K, 166 GPa) [14], puckered hexagonal honeycomb of H atoms sandwiched between slabs of atomic Fe and H atoms in FeH_5 (51 K, 130 GPa) [15], hydrogen pentagraphenelike structure in HfH_{10} (213–234 K, 250 GPa) [16] and H_9 nonagon in XH_{15} ($X = \text{Ca, Sr, Y and La}$) [17] with the estimated high T_c values of 189 K at 200 GPa, 139 K at 300 GPa, 208 K at 220 GPa and 113 K at 200 GPa, respectively. Although the breakthroughs in achieving high transition temperature T_c have breathed new life into the pursuit of room-temperature superconductivity, the extremely high pressures (usually surpassing 100 GPa) in synthesizing these hydride-based superconductors involving diamond anvil cell (DAC) necessitates the use of culet with the small sample size ranging from 40 to 80 μm [18]. Nevertheless, the small sample size conduces to the weak magnetic measurements challenging and makes precise temperature control difficult. On the other hand, the DAC for the synthesis were always broken during depressurization owing to the hydrogen embrittlement [19,20]. Both aspects are expected to get rid of the hydride superconductor under high pressure, which portends the advent of other non-H building blocks in binary metal compounds under lower or even atmospheric pressures.

In the binary compounds containing metal and non-H light element (B, C, N and P), a variety of researchers endeavored to dig into their superconductivity and extraordinary nonmetallic frameworks, especially for 2D planar motifs. The planar nonmetallic skeleton is of great interest due to the spectacular properties, such as distinct superconductivity. Starting from metal borides, MgB_2 (at 1 atm) [21] and MoB_2 (under 100 GPa) [22] within the identical $P6/mmm$ symmetry possess the highest and second highest T_c s of corresponding 39 and 32 K because of the 2D graphitic boron layer among the metal borides. In the metal carbides, the predicted superconducting critical temperature T_c for NaC_2 [23] could approach ~42 K at 80 GPa with the existence of hexagonal rings, which is slightly higher than that of MgB_2 [21]. Moreover, YC_2 was also theoretically verified to be a good superconductor with the estimated T_c value of 2.9 K [24], characterized by the 2D graphite sheet. Importantly, the KN_2 [25] monolayer presents a unique superconducting trait with an estimated critical temperature (T_c) of 4.3 K under ambient condition. Furthermore, the particular novel planar N_4 unit gives rise to the phonon-mediated superconductivity with the T_c value of 4–8 K in $P6_3/mcm$ - FeN_2 [26]. Last but not least, the $I4/mmm$ - KP_2 [27] configuration with puckered phosphorus layer is predicted to have the superconducting critical temperature T_c of 22 K under 5 GPa. Moreover, the calculated T_c values for CeP_2 [28] under ambient pressure ($T_c = 30.77$ K) and LaP_2 [29] at 11 GPa ($T_c = 22.2$ K), regarded as the the highest and second highest T_c s among those of already known binary transition-metal phosphorus, which should be attributed to the graphene-like P layer. From the anterior discussions, two recognizable traits for these binary metal compounds with superb superconductivity fade into our sight, the stoichiometry of 1: 2 and the nonmetallic layered framework (B, C, N and P). In consequence, to uncover more marvelous superconductors, we need to achieve more fresh structures containing the nonmetallic layer fabrications in this category of compounds.

Surrounded by B, C, N and P elements in the periodic table of elements, Si is a common but useful element for a great number of fields, such as integrated circuits and solar cells. Contrary to the semiconductor properties of silicon at ambient pressure, the metal silicides possess the superconducting properties in consequence of its various intriguing motifs (e.g. 3D cages and 2D buckled layers). In the 3D silicon cage system, $\text{Ba}_8\text{Si}_{46}$ [30] consists of a combination of Si_{20} and Si_{24}

cages linked by sharing a pentagonal face with the estimated T_c of 8 K at ambient pressure while $\text{Ba}_{24}\text{Si}_{100}$ [31] contains Si_{20} cage with the T_c value of 1.4 K at the pressure of 1.5 GPa. Subsequent experiment proposed that LaSi_{10} [32] is deemed as a superconductor with $T_c = 6.7$ K. Moreover, the superconducting critical temperature of $P6/m\text{-NaSi}_6$ [33] is estimated to be 13.1 K with the silicon clathrate configuration, in which all Si atoms form simple hexagonal open channels and guest Na atoms fill the channels. Apart from the 3D silicon clathrate configurations, another extraordinary example of graphite-like 2D-structured sub-network are metal disilicides in the form of MSi_2 , where M represents the metal atom. This kind compound is very stable and multifunctional and can be chemically modified by oxidation, which further could induce novel silicon framework such as layered silicon, silicon clathrates and other silicon allotropes after removing the metals. More interestingly, the superconducting phenomenon can be achieved in such layered silicides, which hence stimulate the experimental and theoretical discoveries of the interesting superconductivity in MSi_2 . In the alkali-metal disilicides, RbSi_2 [34] with the trigonal EuGe_2 -type phase (space group: $P\bar{3}m1$, 164), characterized by the hexagonal honeycomb structure, was predicted to have the T_c value of 9 K. For the alkaline-earth metal disilicides, three layered phases in MgSi_2 [35,36] namely, the $R\bar{3}m$ phase at 0 GPa, $Imma$ phase at 10 GPa and $P6/mmm$ phase at 20 GPa were predicted to possess the superconducting critical temperature T_c values of ~ 7 , ~ 6.9 and ~ 7 K, respectively. CaSi_2 [37,38] is transformed to the hexagonal AlB_2 -type structure (space group: $P6/mmm$, 191) with the graphite-like Si layers at 15 GPa in experiment, which displays a superconducting transition at 14 K. Moreover, the high pressure of BaSi_2 [39] with the EuGe_2 -type layered configuration is a superconductor with the experimentally measured T_c value of 6.8 K. In rare-earth metal disilicides, LaSi_2 [40] is considered as a superconductor with the tetragonal ThSi_2 -type ($I4_1/amd$, 141) layered structure, which has the superconducting T_c value of 2.5 K. Recently, another theoretical group studied the superconductivity of the binary Y–Si system and pointed out that the estimated T_c value of $Imma\text{-YSi}_2$ [41] with the apparent layered structure is 0.5 K at 50 GPa. Based on the anterior superconductivity discussions, the layered structures in metal disilicides MSi_2 cover alkali, alkaline-earth and rare-earth metal disilicides. Nevertheless, a distinct category of metal disilicides, namely, transition metal disilicides may be neglected in previous investigations, which arouses our interest in the quest for the layered structures with exceptional superconductivity in transition-metal disilicides.

Chemical substitution is one of the diverse routes in chemical pressure, which can tune the structures and properties of materials [42,43]. Following on this method, we replace alkali, alkaline-earth and rare-earth metal with the considered transition metal in MSi_2 . As is generally known, ruthenium element is located in the VIII group of the periodic table and is a typical transition metal element, which is selected as a representative transition metal. According to the experiment, there are four compounds (e.g., RuSi [44,45], Ru_2Si_3 [45–47], Ru_4Si_3 [45,46] and RuSi_2 [48]) in the binary Ru–Si system under atmospheric pressure. Zhang et al. theoretically predicted three stable compounds in the binary Ru–Si system at ambient pressure, namely, RuSi , Ru_2Si_3 and RuSi_2 through the CALYPSO crystal structure prediction method in combination with first-principles [49]. Both experiment and theory confirm the stable existence of RuSi , Ru_2Si_3 and RuSi_2 in Ru–Si system under ambient pressure, which exhibit the semiconductor characters with narrow band gaps. RuSi consists of two polymorphic types, in other words, the FeSi -type phase with space group of $P2_13$ at low temperature and the CsCl -type phase with space group of $Pm\bar{3}m$ at high temperature [50]. Ru_2Si_3 crystallizes in the orthorhombic $Pbcn$ configuration [45–47]. More importantly, RuSi_2 was reported experimentally for the first time and analyzed theoretically with three possible phases, tetragonal $\alpha\text{-RuSi}_2$ ($P4/mmm$), orthorhombic $\beta\text{-RuSi}_2$ ($Cmca$) and cubic $\gamma\text{-RuSi}_2$ ($Fm\bar{3}m$) [51]. Recently, Zhang et al. theoretically confirmed that the component RuSi_2 with the $Cmca$ phase is stable in the convex hull of the binary Ru–Si system based on the CALYPSO crystal research method and first-principles [49]. However, the exploration on RuSi_2 has focused only on the structures and electronic properties under the atmospheric pressure in spite of the fantastic silicon framework and unexpected properties possibly existing under the high pressure condition, for example, the novel structures with superconductivity. High pressure is an effective methodology to induce the structural transition of materials, bringing about the variation of the properties [52,53], for instance, the evolution from insulator or

semiconductor to metallicity or superconductivity. Moreover, RuSi undergoes a structural transition from FeSi-type to CsCl-type cubic structure at 0.28 GPa, accompanied by the semiconductor-metal conversion [50]. These two aspects enhance our confidence in pursuing the novel structures with superconductivity in RuSi₂ under high pressure. Impressed by the layered structures with the alkali, alkaline-earth and rare-earth metal disilicides discussed above, two questions has been lingering in my mind. could the novel phases appear for RuSi₂ under high pressure? Furthermore, if novel structures could stabilized under high pressure, could the high-pressure phases contain the layered silicon motifs with the superconductivity and superb hardness?

To resolve the aforementioned two problems, we performed an extensive study on the potential RuSi₂ configurations over the pressure range of 0–300 GPa by applying an unbiased CALYPSO method combined with first-principles calculations. Herein, we report an absolutely novel RuSi₂ configuration with the orthorhombic *Cmcm* symmetry under high pressure, composed of a graphene-like silicon-layer with one centered ruthenium atom. More intriguingly, this configuration can be quenchable after releasing the pressure down to ambient pressure. The *Cmcm*-RuSi₂ structure exhibits the superconducting character with the superconducting critical temperature of 10.07 K at ambient pressure, which is the second highest temperature among the MSi₂ (M = metal) silicides (*R*-3*m*-CaSi₂, 14 K) [38]. In addition, its Vicker hardness value can reach 26.76 GPa, makes it become a rarely hybrid material that simultaneously behaves the superconducting property and high hardness under atmospheric pressure. This investigation provide a new pathway for the design of hard superconductors in transition-metal silicides, which will arouse the interest of the experimental researchers in synthesizing transition metal disilicides and measuring related properties.

2. Computational Method

The structure searches of RuSi₂ materials under high pressure are based on the particle swarm optimization (PSO) algorithm as implemented in the crystal structure prediction CALYPSO code [54,55], which has successfully predicted the ambient-pressure and high-pressure structures of various systems [56–59]. In the pressure range of 0–300 GPa, we implemented the structure searches with unit cells including up to four formula units (f.u.). The structural geometrical optimization, electronic structure, Bader charge, electron localization functions (ELF) [60,61] and elastic constants calculations were performed through density functional theory in the Vienna ab initio simulation package (VASP) [62] within the Perdew–Burke–Ernzerhof (PBE) exchange correlation function of generalized gradient approximation (GGA) [63,64]. The Projector-Augmented Wave (PAW) [65] method was adopted to treat $4d^75s^1$ and $3s^23p^2$ as valence electrons for Ru and Si atoms, respectively. In addition, the cutoff energy of 800 eV for the plane-wave basis expansion of the electronic wave functions was implemented and appropriate Monkhorst–Pack *k* meshes for sampling in the Brillouin zone were set to ensure that all the enthalpy calculations were well converged to better than 1 meV/atom [66]. The crystal orbital Hamilton population (COHP) method was applied in LOBSTER code [67,68]. The phonon and electron-phonon coupling (EPC) matrix elements were calculated within density functional perturbation theory (DFPT) as implemented in the QUANTUM ESPRESSO package [69] with a kinetic cutoff energy of 80 Ry. In the first Brillouin zone, we have selected *k*-point meshes for *Cmcm*-RuSi₂ phase of $12 \times 12 \times 12$ at 1 atm and $10 \times 10 \times 10$ at 25, 50 and 75 GPa, respectively. The *q*-point meshes for *Cmcm*-RuSi₂ phase were set to $3 \times 3 \times 3$ at 1 atm and $5 \times 5 \times 5$ at 25, 50 and 75 GPa, respectively.

3. Results and Discussion

3.1. Structural Transition and Dynamical Stability

In the first instance, in order to determine the structural transition sequence and potential stable structures for RuSi₂ under high pressure, we carried out the CALYPSO code for thoroughly crystal structure searches. As a result, nine candidate low-energy structures with space groups of *Cmca*, *Cmcm*, *P2₁/m*, *Immm*, *Cm*, *P3₂12*, *Imm2*, *C2* and *P2₁/m* were predicted at the pressure range of 0–300 GPa. The structural diagrams, together with detailed structural parameters of nine candidate phases

under ambient pressure are summarized in Figure S1 and Table S1 of the Supplementary Information (SI). The previously known *Cmca* [49,70] and *Immm* [71] structures of transition metal disilicide RuSi_2 were successfully reproduced by our structure searches, demonstrating the reliability of the CALYPSO method. Subsequently, we constructed the enthalpy-pressure (H-P) curves of the low-energy phases and presented two possible decomposition routes ($\text{Ru} + 2\text{Si}$ and $\text{RuSi} + \text{Si}$) with respect to *Cmca* phase, as shown in Figure 1. The phase stability of RuSi_2 compound is established at various pressures by judging the enthalpy difference relative to the solid constituent elements and stable compounds (i.e. Ru, Si solid phase, and RuSi compound). The corresponding known stable elements *P6₃/mmc* for Ru [72], *Fd-3m*, *P6₃/mmc*, and *Fm-3m* for Si [73], and compounds *P2₁3* and *Pm-3m* for RuSi [44,45,74] under corresponding pressures were achieved from the previous literature. According to Figure 1, RuSi_2 adopts the orthorhombic $\beta\text{-FeSi}_2$ type configuration (space group: *Cmca*) as ground-state structure under ambient pressure, which is consistent with the previous experimental observations and theoretical researches [49,51,75]. As the pressure increases, the RuSi_2 is found to crystallize in another orthorhombic *Cmcm* phase, which is energetically favored over the *Cmca*- RuSi_2 above 50.97 GPa and maintains its stability up to 79.15 GPa. Noticeably, this *Cmcm*- RuSi_2 configuration is absolutely distinctive from previously reported metal disilicides MSi_2 , such as hexagonal *P6₃/mmc*-type phase in MgSi_2 [35,36] and CaSi_2 [37,38], trigonal *P-3m1* phase in RbSi_2 [34] and alkaline-earth metal disilicides, trigonal *I4₁/amd* phase in LaSi_2 [40], rhombohedral *R-3m* phase in MgSi_2 [35,36], and orthorhombic *Imma* in MgSi_2 [35,36] and YSi_2 [41]. Hence, this orthorhombic *Cmcm* phase is predicted to be a high-pressure ground-state structure in metal disilicides in the present work for the first time. Above 79.15 GPa, the RuSi_2 compound decomposes into $\text{RuSi} + \text{Si}$. Additionally, the considered pressure dependence of RuSi_2 decomposition reaction proves that RuSi_2 will not decompose into $\text{Ru} + 2\text{Si}$ within the pressure range of 0–78.48 GPa (see Figure 1). Thus, compressing RuSi and Si is a potential synthetic route for RuSi_2 crystal. The above analysis demonstrates the thermodynamical stability of *Cmca*- RuSi_2 and *Cmcm*- RuSi_2 phases and provides their potential synthetic routes, which will stimulate the experimental synthesis. Subsequently, we focus on the structural, chemical bonding, electronic, superconducting and mechanical characters for the *Cmca*- RuSi_2 and *Cmcm*- RuSi_2 phases.

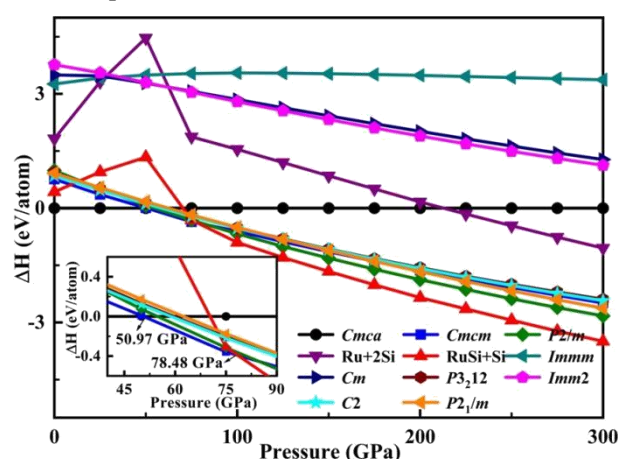


Figure 1. The enthalpy curves for nine low-energy candidate phases and two considered decomposition routes with respect to *Cmca* phase. The inset shows the specific decomposition pressure of RuSi_2 .

To probe into the dynamical stability of two thermodynamical stable structures under specific pressures, we have computed their phonon dispersion curves (see Figures S2 and 7). It is evidently found that both the *Cmca*- RuSi_2 phase at atmospheric pressure and the *Cmcm*- RuSi_2 phase at the pressure range of 0–75 GPa are dynamically stable, as there is no imaginary frequency in the whole Brillouin zone. Although the *Cmcm*- RuSi_2 structure can be acquired under high pressure, it can be recovered to ambient pressure condition, thereby render it applicable in practical settings.

Subsequently, we mainly focus on the the structural, chemical bonding, electronic, superconducting and mechanical features for the *Cmca*-RuSi₂ and *Cmcm*-RuSi₂ phases under atmospheric pressure.

3.2. Structural Character and Bonding Essence

The crystal structure diagrams for the *Cmca*-RuSi₂ phase at 1 atm and the *Cmcm*-RuSi₂ phase at 75 GPa were distinctly depicted in Figure 2 and homologous structural parameters were tabulated in Table S2. From Table S2, the lattice parameters ($a = 10.170$ Å, $b = 8.108$ Å, and $c = 8.209$ Å) of *Cmca*-RuSi₂ excellently align with previous results ($a = 10.223$ Å, $b = 8.133$ Å, and $c = 8.250$ Å) [49,51,75]. In this structure, there are two inequivalent Si atoms located at the Wyckoff sites 16g (0.372, -0.778, 0.057) and 16g (0.127, -0.551, 0.225), respectively, with Si-Si separations varying from 2.54 to 2.62 Å. All the Si atoms form a ladder-like Si-network framework with the planar quadrangle along the b axis and the angle between the nearest three Si atoms is nearly 90°. The shortest Si-Si distance (2.54 Å) is marginally longer than the those of Si (2.22 Å) atoms, d -Si (2.35 Å) [76], and allotrope *Cmcm*-Si₂₄ (2.33-2.41 Å) [76], but comparable to those of C49-WSi₂ [77] (2.56 Å) and B31-RhSi (2.53-2.69 Å) [78], expounding the contribution of Si-Si covalent bond to the structure construction. This result can be evidenced by the electron localization function (ELF) for the *Cmca*-RuSi₂ under ambient pressure, as displayed in Figure 3(a) and 3(b), which precisely describes the electron localization between Si atoms. Besides, each Ru atom is coordinated by eight Si atoms, forming a “RuSi₈” building block with Ru-Si separation range of 2.45-2.52 Å. The shortest Ru-Si distance (2.45 Å) is slightly longer than the sum of the covalent bond radii of Ru (1.25 Å) and Si (1.11 Å) atoms, indicating the covalent Ru-Si bond, which can be demonstrated by ELF in Figures 3(a) and 3(b) as well. For the *Cmcm*-RuSi₂ phase at 75 GPa, the lattice parameters are $a = 6.693$ Å, $b = 4.052$ Å and $c = 3.866$ Å, where Ru atoms occupying the Wyckoff sites 4c (-0.500, 0.307, 0.750) are neighbored by equivalent Si atoms locating at 8g (-0.832, 0.316, 0.750) sites. More charmingly, the *Cmcm*-RuSi₂ phase contains two interpenetrating honeycomb-like silicon-layer along the c -axis, which forms the silicon hexagonal ring with one metal atom Ru located at the center of hexagonal ring in the a - b plane, disclosing that metallic atom and nonmetallic silicon layer are in the same flat. This layered feature is distinct from previously reported planar structures, such as MgB₂ [21], MoB₂ [22], NaC₂ [23], YC₂ [24], CeP₂ [28] and LaP₂ [29], where the hexagonal-ring nonmetallic layer and metallic atom generate two alternate layers and are distributed in different flats. In silicon hexagonal-ring, the there are two kinds of Si-Si bond lengths, corresponding to 2.298 and 2.461 Å, while the Si-Si bond length between the silicon layers is 2.456 Å. These three Si-Si bond lengths are elongated into 2.417, 2.668 and 2.655 Å, respectively, when the pressure decreases to the ambient pressure. Additionally, ten silicon atoms are coordinated around one Ru atom, forming a distorted RuSi₁₀ dodecahedron with four different Ru-Si bond lengths of 2.347, 2.431, 2.435 and 2.440 Å at 75 GPa, compared with the elongated Ru-Si bond separations of 2.523, 2.615, 2.554 and 2.683 Å under atmospheric pressure. Both of Si-Si and Ru-Si bond distances provide an explanation of the Si-Si and Ru-Si covalent bonds in the *Cmcm*-RuSi₂ crystal at ambient pressure and high pressure, which can also be substantiated by the electron localization in the intermediate regions of the Si-Si and Ru-Si bonds, as depicted in Figures 3(c), 3(d), 3(e) and 3(f). In short, based on the overall analyses of bond length and ELF, the *Cmca*-RuSi₂ and *Cmcm*-RuSi₂ phases under ambient pressures as well as the *Cmcm*-RuSi₂ phase under high pressure are characterized by a combination of the covalent Ru-Si and Si-Si bonds.

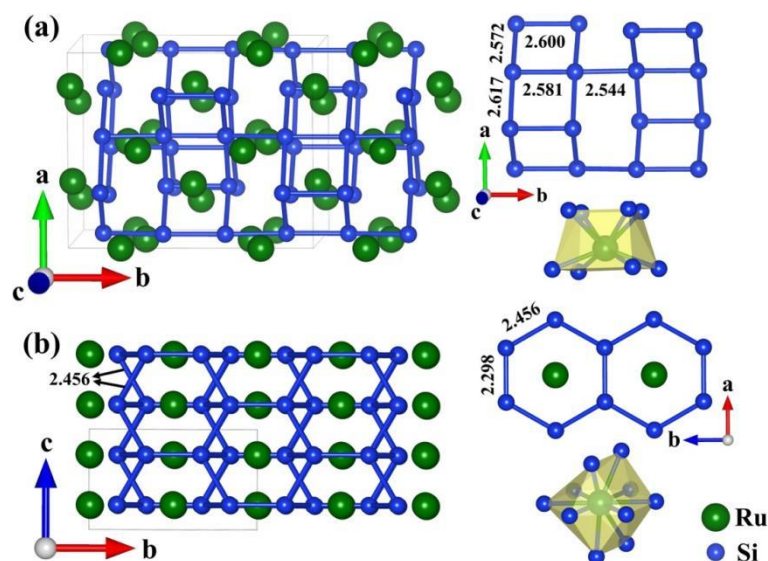


Figure 2. Crystal structures of two stable RuSi_2 phases. The green and blue spheres represent Ru and Si atoms, respectively. (a) Cmca-RuSi_2 at 1 atm, and (b) Cmcu-RuSi_2 at 75 GPa.

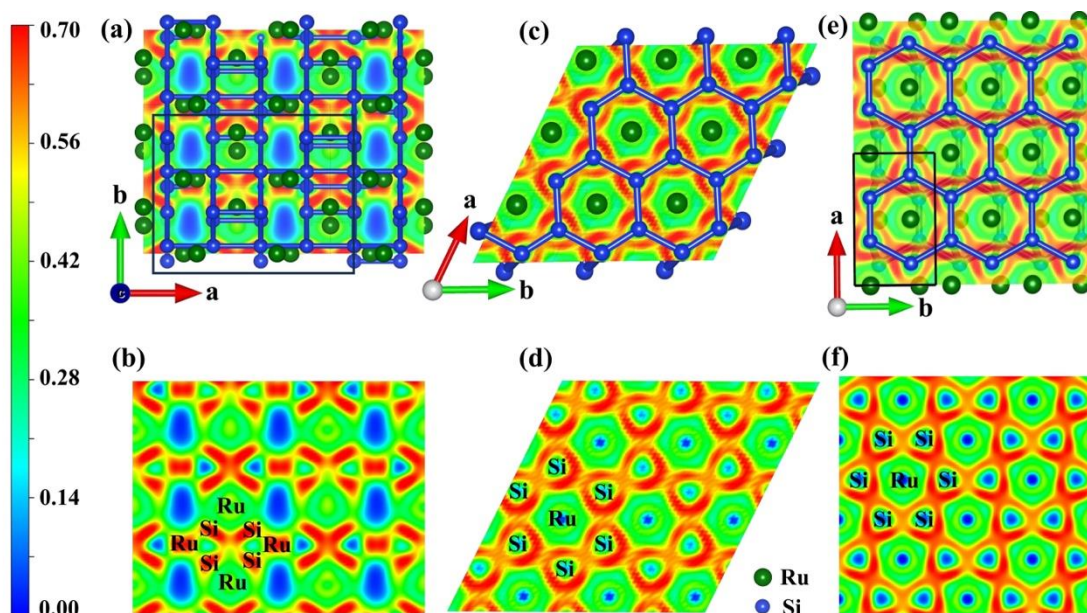


Figure 3. The 3D and 2D electron localization functions (ELF) of two stable RuSi_2 phases. (a) and (b) (001) plane for the Cmca-RuSi_2 at 1 atm, (c) and (d) (001) plane for the Cmcu-RuSi_2 at 1 atm, and (e) and (f) (001) plane for the Cmcu-RuSi_2 at 75 GPa. The green and blue spheres represent Ru and Si atoms, respectively.

The formation of strong covalent Ru–Si and Si–Si interactions in these two stable configurations of RuSi_2 can be quantitatively disclosed through the calculated crystal orbital Hamilton population (COHP) curves and integral crystal orbital Hamilton population (ICOHP) at the Fermi level, as displayed in Figure 4. The calculated ICOHP values for Ru–Si and Si–Si pairs in Cmca-RuSi_2 under 1 atm are -1.84 and -2.41 eV for per pair, respectively. Moreover, the predicted ICOHP values for the Ru–Si bonds in Cmcu-RuSi_2 at 1 atm and 75 GPa is -1.66 and -1.68 eV for per pair, respectively, with the corresponding ICOHP values of the Si–Si pairs -2.25 and -2.23 eV for per pair. Afterward, the predicted ICOHP values for the Si–Si pairs (-2.41 , -2.25 and -2.23 eV for per pair) in both RuSi_2 structures are comparable to those of covalent Si–Si pairs in $\text{Na}_4\text{Si}_{24}$ (-2.544 eV/pair) [76], P–P pairs in LaP_2 (-2.32 eV/pair) [29], P1–P2 pairs in Ce_2P_3 (-2.41 eV/pair) [28], B2–B2 pairs in LiB_4 (-2.55

eV/pair) [79] and B2–B2 pairs in NaB₄ (–2.55 eV/pair) [80], reconfirming strong covalent Si–Si bond in both configurations. From the consequences above, it can be conspicuously found summarized into two aspects. On the one hand, the strength of the covalent Si–Si bond is stronger than that of the Ru–Si covalence in both RuSi₂ configurations as the estimated ICOHP values for the Si–Si pairs are slightly lower than those of the Ru–Si pairs. On the other hand, compared with the layered *Cmcm*-RuSi₂ phase, *Cmca*-RuSi₂ possesses the stronger Ru–Si and Si–Si covalent bonds, which should be the main driving force that the *Cmca*-RuSi₂ phase have more magnificent incompressibility than the *Cmcm*-RuSi₂ structure.

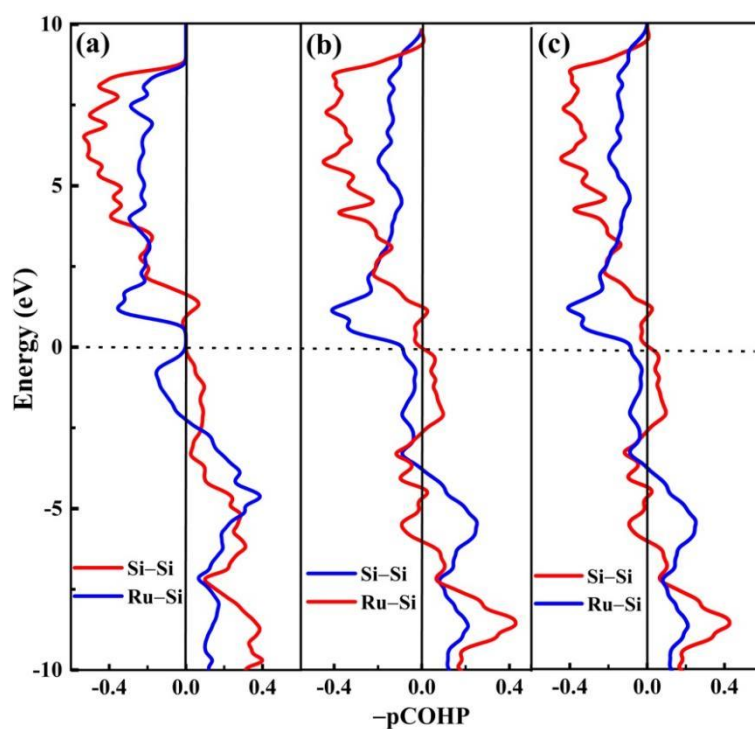


Figure 4. The crystal orbital Hamilton population (COHP) curves of two stable RuSi₂ phases. (a) *Cmca*-RuSi₂ at 1 atm, (b) *Cmcm*-RuSi₂ at 1 atm, and (c) *Cmcm*-RuSi₂ at 75 GPa. The dotted vertical line at 0 eV represents Fermi energy level.

3.3. Electronic Structure and Superconductive Property

To further delve into the electronic structures of the *Cmca*-RuSi₂ phase at 1 atm as well as the *Cmcm*-RuSi₂ phase at 1 atm and 75 GPa, we calculated their electronic band structure (BS) and density of states (DOS), as constructed in Figure 5. Note that the *Cmca*-RuSi₂ structure under ambient pressure displays a semiconductor behavior characterized by a direct band gap of 0.485 eV, in conformity with the preceding theoretical calculations reported by Zhang *et al* [49]. On the contrary, as the pressure increase, the conduction band and the valence band of *Cmcm*-RuSi₂ phase pass through the Fermi level (E_F) and overlap, implying its metallic character. In reality, a semiconductor-metal transformation or metallization occurs under high pressure, along with the structural transition from *Cmca*-RuSi₂ to *Cmcm*-RuSi₂. This phenomenon metallization induced by high pressure can also be appreciated in other systems, such as MgH₂ [81], CaLi₂ [82] and SiH₄ [83]. Moreover, the *Cmcm*-RuSi₂ phase still maintains the metallic characteristic when the pressure is released into the ambient pressure, as shown in Figure 5(b). On the other hand, the semi-conductive and metallic traits in *Cmca*-RuSi₂ and *Cmcm*-RuSi₂ can be elucidated in the right side of Figures 5(a), 5(b) and 5(c). On the basis of the total and partial density of states (TDOS and PDOS) of both RuSi₂ structures, it is obviously achieved that the Ru-4*d* state make the dominant contribution to TDOS. Apart from the Ru-4*d* state contribution, the Si-3*p* state also contributes to TDOS at a certain extent. The hybridization effect between the Ru-4*d* and Si-3*p* states near both sides of the E_F disclose the Ru-Si covalent bond in both RuSi₂ phases, which in excellent accord with the previous analyses of bond length, ELF, and COHP.

Eventually, the chemical bonding in the *Cmca*-RuSi₂ and *Cmcm*-RuSi₂ configurations comprises a complex combination of the covalent Ru-Si and Si-Si bonds with the Si-Si bond stronger than that of the Ru-Si bonding. More noticeably, as presented in the left sides of Figures 3(b) and 3(c), the electronic BS exhibits multiple characters in proximity to E_F , comprising of the hole pockets around *T/S/U* points, electron pockets around *Z/S* points and flat band along the *Y-S-X* direction. In view of the atypical BS, we further dig into the topological structure of Fermi surfaces (see Figure 6), which serve to unveil the electronic performance at the E_F . The emerge of three bands in *Cmcm*-RuSi₂ indicates excellent electrical conductivity and the third band should be attributed to the flat band along the *Y-S-X*, further secured by the decreased energy approaching the E_F at the ambient pressure. These electronic traits proposed from the BS and Fermi surfaces have been comprehensively investigated and deemed as imperative signs for superconductivity.

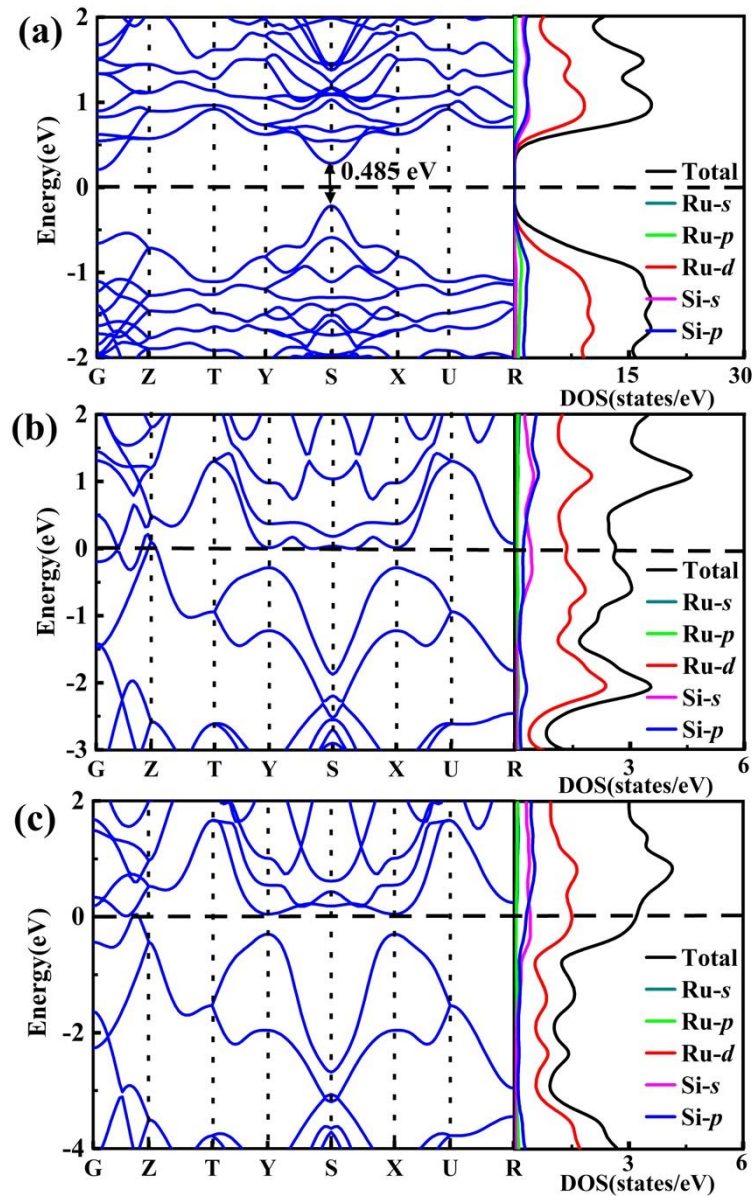


Figure 5. Electronic band structures and density of states (DOS) of two stable RuSi₂ phases. (a) *Cmca*-RuSi₂ at 1 atm, (b) *Cmcm*-RuSi₂ at 1 atm, and (c) *Cmcm*-RuSi₂ at 75 GPa.

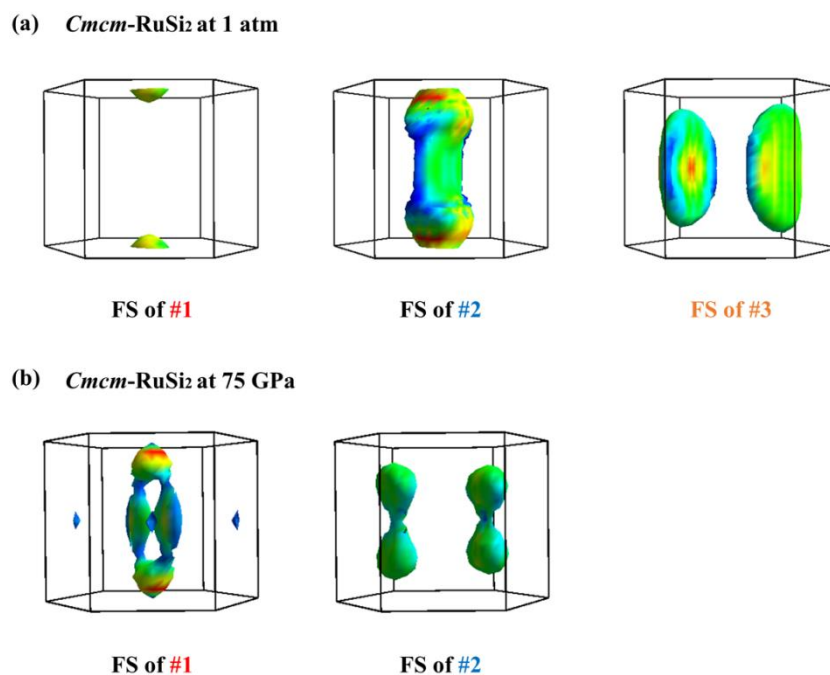


Figure 6. The nested Fermi surfaces for the *Cmcm*-RuSi₂ configuration at (a) 1atm and (b) 75 GPa.

Kindled by the metallic and significant band structure characters in *Cmcm*-RuSi₂ under ambient and high pressures coupled with the outstanding superconductivity in the layered framework in MgB₂ [21], MoB₂ [22], NaC₂ [23], KP₂ [27], CeP₂ [28], and LaP₂ [29] as well as alkali, alkaline-earth and rare-earth metal disilicides, analogous to the *Cmcm*-RuSi₂ phase, we assume that the layered *Cmcm*-RuSi₂ structure should be a promising superconductor. Subsequently, we calculated the phonon dispersion curves, the projected phonon density of states (PHDOS) and Eliashberg spectral function $\alpha^2F(\omega)$ together with the electron–phonon integral constant λ of *Cmcm*-RuSi₂ at 1 atm, 25 GPa, 50 GPa, and 75 GPa with the intention of illuminating their potential superconductivity, presented in Figure 7. As analysed above, its dynamical stability could be verified within the pressure range of 0–75 GPa as a consequence of the absence of imaginary phonon frequency throughout the whole Brillouin zone at 1 atm, 25 GPa, 50 GPa, and 75 GPa. In the PHDOS, the phonon vibrational modes of *Cmcm*-RuSi₂ can mainly be divided into three districts on the basis of the phonon region. The vibrations of Ru atoms mainly contribute to the low-frequency phonon regions (< 9 THz), while the high-frequency phonon modes (10–15 THz) are associated with silicon layers because of Ru atom heavier than Si atom. It is worthy noting that the intermediate-frequency branches stem from the coupled vibrations of Ru atom and Si layer. For the EPC parameter λ , the low-frequency vibrations by Ru atoms around below 9 THz contribute 82.4%, 77%, 74% and 67.5% at 1 atm, 25 GPa, 50 GPa and 75 GPa of the total λ , respectively, while the high-frequency phonon bands above 10 THz associated with light Si atom vibrations only account for 13.2%, 19.7%, 20.5% and 22.5% in *Cmcm*-RuSi₂, respectively. In addition, the corresponding coupled vibrations from Ru atoms and Si layer contribute 4.4%, 3.3%, 6.5% and 10% at 1 atm, 25 GPa, 50 GPa and 75 GPa of the total λ , respectively. This directly denotes that the vibrations from Ru atoms combined with the coupled vibrations between Ru atoms and Si layers play significant roles in the superconductivity of *Cmcm*-RuSi₂.

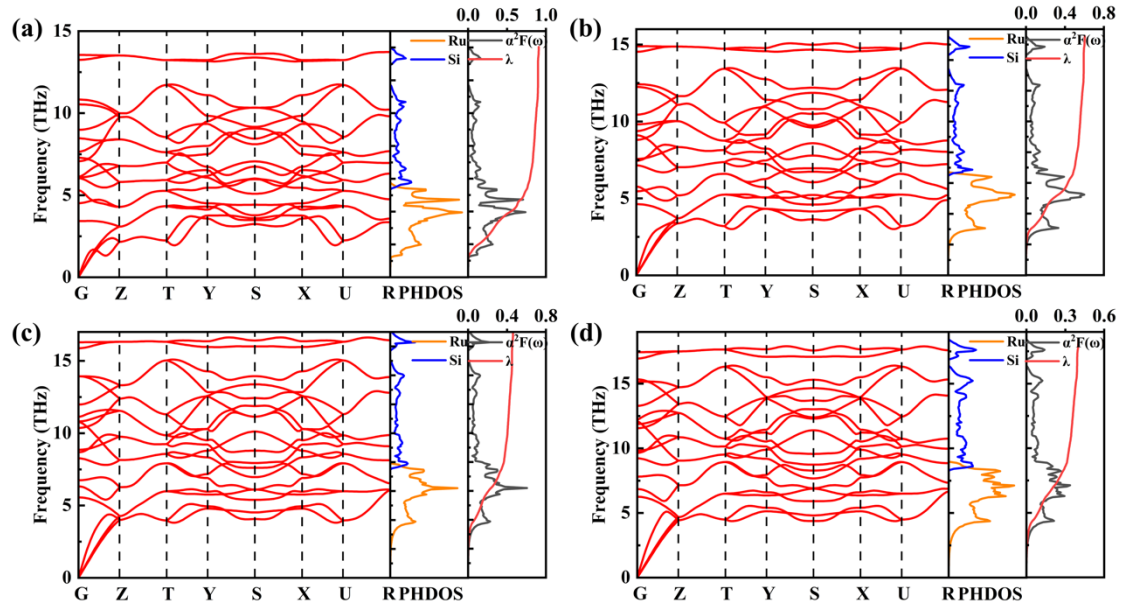


Figure 7. The phonon dispersion curves, the projected phonon density of states (PHDOS) and Eliashberg spectral function $\alpha^2F(\omega)$ together with the electron-phonon integral constants $\lambda(\omega)$ of (a) *Cmcu*-RuSi₂ at 1 atm, (b) *Cmcu*-RuSi₂ at 25 GPa, (c) *Cmcu*-RuSi₂ at 50 GPa, and (d) *Cmcu*-RuSi₂ at 75 GPa.

The electron-phonon coupling parameters λ , logarithmic average phonon frequency $\omega_{\log}$, electron density of states at the Fermi level $N(E_f)$ and superconducting transition temperature T_c of *Cmcu*-RuSi₂ at 1 atm, 25 GPa, 50 GPa and 75 GPa were also calculated in Table 1. The superconducting critical temperature T_c values are estimated by using the Allen-Dynes modified McMillan equation :

$$T_c = \frac{\omega_{\log}}{1.2} \exp \left[\frac{1.04(1+\lambda)}{\lambda - \mu^* (1+0.62\lambda)} \right]$$

where, the Coulomb pseudopotential parameters μ^* are set to typical 0.10 and 0.13, respectively. As summarized in Table 1, the predicted EPC parameter λ for the *Cmcu*-RuSi₂ crystal is 0.4 at 75 GPa and displays a monotonous decrease with the increment of the pressure. Accordingly, the maximal EPC parameter λ value of 0.91 emerges in *Cmcu*-RuSi₂ under ambient pressure, which is comparable to 0.93 for RuSi₂ at 0 GPa, 1.1 for CaSi₂ at 0 GPa, 0.92 for Al₂Si₃ at 10 GPa, 1.01 for *P6₃/mmc*-Y₃Si, but larger than 0.81 for *P6₃/mmm*-MgSi₃ at 0 GPa, 0.808 for *Cmmm*-Si₄ at ambient pressure, 0.897 for *P6₃/m*-NaSi₆ at 0 GPa, 0.799 *P6₃/m*-Si₆ at 0 GPa. To compare with the former binary conventional superconductors, we draw a overall diagram which displays a combination of the T_c and stabilized pressure for established superconductors, as shown in Figure 8. Additionally, the detailed T_c values

For the conventional superconductors at different pressures are summarized in Table S3. It is undoubtedly found that the *Cmcu*-RuSi₂ structure are estimated to be 10.07 K at atmospheric pressure, which is comparable to 13.7 K in MgSi₃, 13 K in *P6₃/m*-NaSi₆ and 12 *P6₃/m*-Si₆ at 0 GPa, 14 K for CaSi₂ at 15 GPa, 10.5 K for *P6₃/mmm*-CeP₂ at 16.5 GPa, and 13.6 K for CrB₂ at 60.7 GPa, but higher than other transition metal disilicides, such as RuSi₂ (9 K) [34], MgSi₂ (~7 K) [35,36], BaSi₂ (6.8 K) [39], LaSi₂ (2.5 K) [40] and YSi₂ (0.5 K, 50 GPa) [41]. In short, the novel *Cmcu*-RuSi₂ configuration at ambient pressure possesses the secondarily highest T_c among the binary metal disilicides, merely lower than that of CaSi₂ (14 K) under 15 GPa. In addition, it is worthy mentioning that the superconducting critical temperature T_c in *Cmcu*-RuSi₂ is significantly higher than those of the corresponding metallic *Cmcu*-Si₄ (2.2 K) [87] and Ru (0.51 K) [91,92] at ambient pressure, which tremendously advance the superconductivity for the related elemental substances.

The investigation of the variation trends with the increasing pressure serve as an appropriate pathway for a deeper understanding of the superconductivity driven in *Cmcu*-RuSi₂, as intuitively

exhibited Figure 9. Regarding the broad stable pressure range obtained in *Cmcm*-RuSi₂, we have implemented calculations to estimate its pressure-dependent superconductivity. As the pressure decreases, a successive increase presents in the T_c values, eventually reaching 10.07 K at atmospheric pressure. Manifestly, two substantial parameters (λ and ω_{og}) play a vital role in determining T_c , displaying the contrasting trends with pressure. The increment in T_c with decreasing pressure results from the synchronous enhancement in λ , which dominates the evolution of T_c with pressure. The growth in λ should be related to the increasing DOS at the Fermi energy upon the reducing pressure, which further originate from the decrease of charges of Ru-4d orbital transferred from silicon layer, as tabulated in Table S4. In the *Cmcm*-RuSi₂ phase, one Ru atom gain 1.38 e at 75 GPa and reduces to 1.06 e under ambient pressure. The charge transferred from nonmetallic Si to metallic Ru is feasible for the reason that the electronegativity value of Si (1.90) element is lower than that of Ru element according to the periodic table of the elements. The anion character in metallic element Ru is rarely seen in binary metal silicides. In contrast, the reducing process of ω_{og} with the decreasing pressure should be attributed to the elongation of Si-Si bonds within the configuration. Upon the reducing compression, the variation trend of λ (increment) and ω_{og} (diminution) is similar to those in Ce₂P₃, CeP₂ [28] and Sc₂P [93].

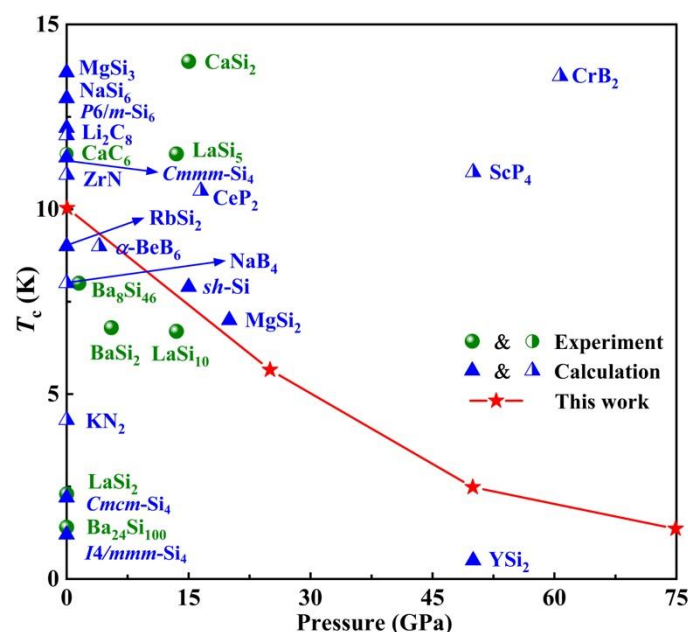


Figure 8. Pressure dependence of T_c values for typical superconductors. The green filled and half-filled circles stand for the T_c values of well-known metal silicides and other binary compounds in experiment, respectively [9-11,32,38-40,84]. The blue filled and half-filled triangles denote the T_c values of well-known metal silicides and other binary compounds in theory, respectively [25,33,35,41,43,85-90]. The red filled stars the T_c values ($\mu^* = 0.1$) of the *Cmcm*-RuSi₂ configuration at four different pressures.

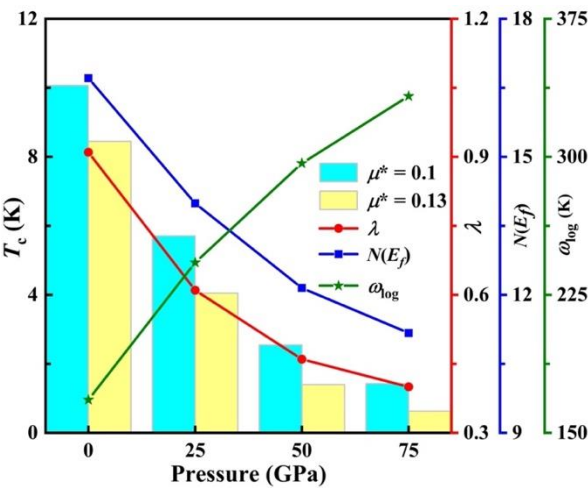


Figure 9. Calculated electron-phonon coupling parameters λ , electronic density of states at the Fermi level $N(E_f)$ (states/spin/Ry/Unit Cell), logarithmic average phonon frequency ω_{log} (K), and superconducting transition temperature T_c (K) in *Cmcm*-RuSi₂ phase as a function of pressure with μ^* = 0.10 and 0.13.

Table 1. Calculated electron-phonon coupling parameters λ , electronic density of states at the Fermi level $N(E_f)$ (states/spin/Ry/Unit Cell), logarithmic average phonon frequency ω_{log} (K), and superconducting transition temperature T_c (K) of *Cmcm*-RuSi₂ at 1 atm, 25 GPa, 50 GPa and 75 GPa, respectively.

Structure	Pressure	ω_{log}	$N(E_f)$	λ	T_c	
					$\mu^* = 0.10$	$\mu^* = 0.13$
<i>Cmcm</i> -RuSi ₂	1 atm	167.97	16.71	0.91	10.07	8.45
	25 GPa	242.56	13.99	0.61	5.71	4.05
	50 GPa	296.50	12.15	0.46	2.55	1.40
	75 GPa	332.95	11.17	0.40	1.43	0.63

As the representative superconductor in the component of 1:2 in binary metallic compounds, MgB₂ encompasses a similar honeycomb B layer, differing from *Cmcm*-RuSi₂. It is necessary to unlock the discrepancy in the structural characters, electronic properties, the superconducting mechanism and T_c values between both phases at ambient pressure. In regard to the structural trait, the honeycomb B layer and Mg atoms are located in the alternate layers along the *c* axis in MgB₂ whereas the graphene-like Si layer and the Ru atoms are in the same plane with Ru atom sited at the center of the Si hexatomic ring. In the case of the metallic character, MgB₂ mainly stems from the B-2*p* orbital while the current *Cmcm*-RuSi₂ should be ascribed to the Ru-4*d* state. The high frequency for MgB₂ derives from the graphene-like B layer with the superconductivity of MgB₂ dominated by the electron-phonon coupling of B atoms [94], while the transition Ru-4*d* orbital electrons also take part in the coupling. This comparison not only points toward a possibility to uncover different superconducting sources in the traditional prototype phases, such as H₃S, CaH₆ and LaH₁₀, but also widens the cognition of the elemental contributions in superconductivity. As for the T_c value, MgB₂ is higher than *Cmcm*-RuSi₂, which can be summarized as the following reasons: (a) The MgB₂ has an open B layer without the B–B interlayer covalence while *Cmcm*-RuSi₂ contains an closed Si layer with the interlayer covalent Si–Si bond; (b) the bond strength of Si–Si bond in *Cmcm*-RuSi₂ is weaker than that of MgB₂, as demonstrated by the calculated ICOHP (–2.25 per pair Si–Si in comparison with –6.92 per pair B–B); (c) the ω_{log} value for *Cmcm*-RuSi₂ is lower than that of MgB₂ (167.97 K with respect to 450 K) [94], which results from the lower phonon frequencies of Ru and Si atoms lower than those of Mg and B atoms, as related to the larger atomic mass of Ru and Si, respectively.

3.4. Mechanical Property and Hardness

With the high development in the superconductor, it necessitates the eminent mechanical property and hardness integrated with spectacular ductility. The elastic constants for the *Cmca*-RuSi₂ and *Cmcm*-RuSi₂ phases at 1 atm in conjunction with the *Cmcm*-RuSi₂ configuration under ambient pressure and 75 GPa were computed through the identical strain–stress means [95], as corroborated in Table 2. Both phases are dynamically stable under focused pressures as they satisfy the mechanical stability criteria for the orthorhombic crystal system [96]. Thereafter, the homologous shear modulus *G*, bulk modulus *B*, *B/G*, Young’s modulus *E* and Poisson’s ratio *ν* of both phases can be attainable from the elastic constants based on the Voigt–Reuss–Hill (VRH) method [97] (see Table 2). In the *Cmca*-RuSi₂ configuration under ambient pressure, the current estimated elastic constants *C_{ij}*, bulk modulus *B*, shear modulus *G*, Young’s modulus *E* and Poisson’s ratio *ν* are in conformity with the prior theoretical consequens [49], clarifying that the methodology utilized in present work is convincing. Generally speaking, the *C₁₁*, *C₂₂* and *C₃₃* values in material denote the resistance to compression along the corresponding *a*-, *b*- and *c*-axis. From Table 2, *Cmcm*-RuSi₂ under 75 GPa possesses ultra-high *C₁₁*, *C₂₂* and *C₃₃* values, which are much higher than those of *P6/mmm*-ScB₂ [98], explaining that this phase behaves excellent incompressibility along *a*-, *b*- and *c*-axis. The calculated *B*, *G* and *E* values of *Cmcm*-RuSi₂ under 75 GPa are 410.13, 184.99 and 482.44 GPa, respectively, which are significantly higher than those of the *Cmca*-RuSi₂ phase at ambient pressure (*B*, *G* and *E* values are 173.53 , 107.99 and 268.30 GPa, respectively), corroborating that this phase transition induced by compression enhances the mechanical properties of RuSi₂ crystal to a great extent. Moreover, the value of *B/G* can estimate the brittle or ductile manner of a solid: a high ratio of *B/G* (> 1.75) indicates the ductility, while a low ratio (< 1.75) indicates the brittleness according to the Pugh criterion [99,100]. For transition metal silicides, the improvement of ductility can greatly improve their industrial work efficiency, because their actual productions as high-temperature materials are limited by their own brittleness [101-103]. As listed in Table 2, the the *B/G* value of *Cmca*-RuSi₂ at 1 atm is 1.61, uncovering the brittle nature whereas the *B/G* values of *Cmcm*-RuSi₂ at 1 atm and 75 GPa are 2.03 and 2.22, corresponding to ductile character, respectively. This phenomenon confirms the brittle-to-ductile transformation in RuSi₂, accompanied by the structural transformation under high pressure, which is analogous to NbSi₂ [104] and MoN₂ [105].

Table 2. Elastic constants *C_{ij}* (GPa), shear modulus *G* (GPa), bulk elastic modulus *B* (GPa), *B/G*, Young’s modulus *E* (GPa) and Poisson’s ratio *ν* of two stable RuSi₂ structures.

Pressure	Space group	<i>C₁₁</i>	<i>C₂₂</i>	<i>C₃₃</i>	<i>C₄₄</i>	<i>C₅₅</i>	<i>C₆₆</i>	<i>C₁₂</i>	<i>C₁₃</i>	<i>C₂₃</i>	<i>G</i>	<i>B</i>	<i>B/G</i>	<i>E</i>	<i>ν</i>
1 atm	<i>Cmca</i>	271	336	327	103	111	122	115	90	112	107.99	173.53	1.61	268.30	0.24
1 atm	<i>Cmcm</i>	389	288	292	85	90	69	96	112	128	89.28	181.20	2.03	230.05	0.29
75 GPa	<i>Cmcm</i>	836	676	594	149	173	188	261	246	298	184.99	410.13	2.22	482.44	0.30

Hardness should be characterized as a substantial mechanical property of a material and can be used to measure the ability to resist local deformation, especially plastic deformation, indentation or scratches. In addition, the orientation bond in a material is an important index to measure its hardness, and it can be expressed by Pugh’s ratio *G/B* [99,100]. A larger *G/B* value corresponds to a higher hardness. As summarized in Table 2, the *G/B* values of *Cmca*-RuSi₂ and *Cmcm*-RuSi₂ phases under atmospheric pressure are 0.64 and 0.49, respectively. However, Gao *et al.* indicated that the vital problem in digging into the hardness of materials is how to describe the strength of internal bonds of the materials. Thus, we further probe into the hardness values of both structures employing the hardness model proposed by Gao et al [106,107]. The Vickers hardness could be calculated with the following formula:

$$H_v = \{ \prod_{i=1}^{\mu} [740P^{\mu}(V_b^{\mu})^{-\frac{5}{3}}]^{n^{\mu}} \}^{\frac{1}{\sum n^{\mu}}}$$

where

$$V_b^\mu = (d^\mu)^3 / \sum [(d^\nu)^3 N_b^\mu]$$

where μ labels all different types of covalent bonds in the system, P^μ is the Mulliken overlap population of the μ type bond, v_b^μ is its volume, n^μ is the number of μ type bonds, d^μ is its bond length, and N_b^μ is the bond number of type μ per unit volume. On account of the aforementioned empirical equation, the estimated hardness values of *Cmca*-RuSi₂ and *Cmcm*-RuSi₂ phases reach 31.74 and 26.76 GPa, respectively (see Table 3). The hardness value of *Cmca*-RuSi₂ under ambient pressure is consistent with the previous theoretical results [49]. The predicted H_v values of *Cmca*-RuSi₂ (31.74 GPa) and *Cmcm*-RuSi₂ (26.76 GPa) are comparable to the experimental measurements of β -SiC (34 GPa) [106], BP (33 GPa) [108], TiC (32 GPa) [109] β -Si₃N₄ (30 GPa) [109] and transition metal disilicide WSi₂ (28.5 GPa) [110], but higher than elemental solid Si (12 GPa) [106]. Hence, it can be concluded that both *Cmca*-RuSi₂ and *Cmcm*-RuSi₂ are potential high hardness materials. In comparison with *Cmcm*-RuSi₂, *Cmca*-RuSi₂ has a higher hardness, which can be ascribed to the stronger Ru–Si and Si–Si covalent bonds and better orientation than those of *Cmcm*-RuSi₂.

Table 3. Calculated bond parameters and Vickers hardness H_v (GPa) of two stable structures.

	bond	<i>P</i>	<i>n</i>	<i>d</i> (Å)	<i>V_b</i> (Å³)	<i>H_v</i> (GPa)
<i>Cmca</i>	Ru-Si	0.38	16	2.452	2.955	31.7
		0.30	16	2.458	2.977	28 ^a
		0.35	16	2.460	2.984	
		0.41	16	2.460	2.986	
		0.36	16	2.467	3.010	
		0.30	16	2.484	3.072	
		0.30	16	2.500	3.131	
		0.27	16	2.523	3.219	
	Si-Si	0.33	8	2.541	3.289	
		0.32	16	2.570	3.402	
		0.28	8	2.576	3.428	
		0.27	8	2.598	3.514	
		0.31	16	2.612	3.574	
		0.18	8	2.689	3.898	
		0.20	16	2.693	3.913	
<i>Cmcm</i>	Ru-Si	2.23	8	2.226	6.367	26.8
		0.32	4	2.242	6.513	
	Si-Si	0.37	4	2.293	6.967	
^a Reference [49].		0.76	4	2.307	7.095	

4. Conclusions

To sum up, our comprehensive first-principles structure searches in RuSi₂ within the pressure range of 0–300 GPa have disclosed the emerge of the peculiar *Cmcm*-RuSi₂ phase at 50.97 GPa. This *Cmcm*-RuSi₂ configuration contain an extraordinary graphene-like silicon layer, which is dynamically stable and simultaneously leads to exceptional superconductivity and high hardness under ambient pressure, despite it is recovered from the high pressure. On the one hand, its predicted T_c value could reach 10.07 K at ambient pressure, comparable to the previous proposed *P6/m*-NaSi₆ (13 K) and CaSi₂(14 K). On the other hand, the Vickers hardness value is 26.76 GPa, which is comparable to WSi₂(28.5 GPa). Furthermore, its excellent conductivity stem from the the strong interaction between Ru-4*d* electrons and the phonons B–B and coupled Ru–Si vibrations, while its high hardness can be ascribed to the 3D robust Ru–Si and Si–Si directional covalent framework. In addition, the *Cmcm*-

RuSi₂ phase is a ductile material. The ambient-pressure ground *Cmca* phase is a narrow-gap semiconductor with a estimated hardness of 31.7 GPa.

The special graphene-like silicon layer in the transition-metal disilicides *Cmcm*-RuSi₂ phase broaden the existing silicon-layer space beyond alkali, alkaline-earth and rare-earth metal disilicides. The removal of metal atoms can be utilized to acquire silicon framework such as layered silicon, silicon clathrates and other silicon allotropes. This mode has uncovered a succession of novel elemental structures, such as *I4/mmm*-B₄, *Pm*-B₁₇ [80] and *P6/m*-Si₆ [33], which is destined to promote the quest for the analogous silicon laminar structures and distinct silicon motifs (eg. 3D silicon clathrate framework and 1D silicon chains) in elemental silicon and transition-metal silicides. On the other hand, this layered network in *Cmcm*-RuSi₂ provide a wonderful bedding for adding light element adatoms to layered superconductors, which could enhance the superconductivity for the parent *Cmcm*-RuSi₂ configuration. This method has been practically employed recently to improve the superconductivity in very diverse ultrathin materials, ranging from monolayer MgB₂ to truly 2D atomic sheets doped graphene and transition metal dichalcogenides.

The *Cmcm*-RuSi₂ structure has the secondarily highest superconducting transition temperature among the metal disilicides, MSi₂ (M = metal), merely lower than that of CaSi₂ (14 K), which facilitate the in-depth investigation on the superconductivity mechanism in the metal disilicides in both theory and experiment.

The anion transition-metal in *Cmcm*-RuSi₂ is rarely reported in preceding binary compounds that contains metal and nonmetal elements, which widens the physical and chemical cognition.

Supplementary Materials: The following supporting information can be downloaded at the website of this paper posted on Preprints.org., Figure S1: Nine structures of RuSi₂ at ambient pressure. The red and green spheres represent Ru and Si atoms, respectively; Figure S2: The phonon dispersion curves of *Cmca*-RuSi₂ at ambient pressure.

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