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*Article*

# Digital Twins Verification and Validation Approach Through the Quintuple Helix Conceptual Framework

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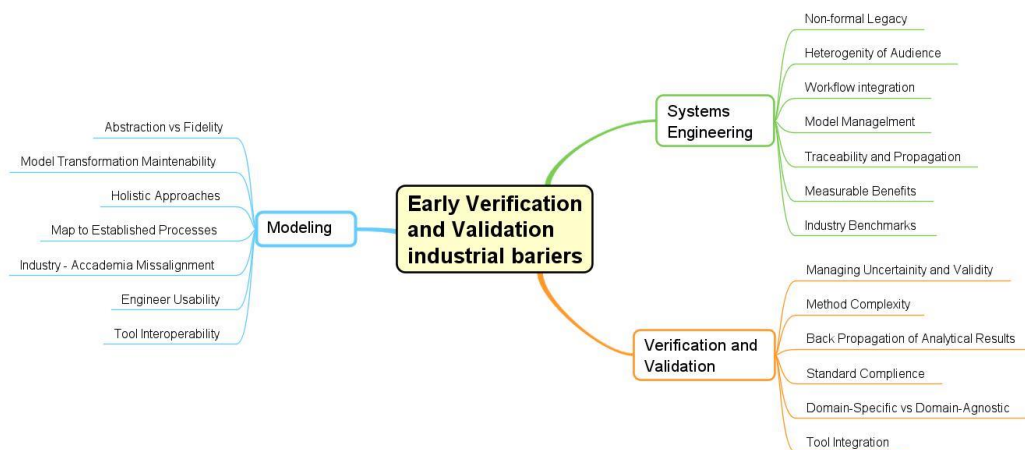
**Abstract:** The concept of Digital Twins has been in the field for a long time, constantly challenging the specification, modeling, design, implementation, and exploitation of complex cyber-physical systems. Despite the various foundations, standards, and platforms in Systems Engineering, there are ongoing challenges with Verification and Validation methodology. This study aims to establish a generic framework that addresses the various aspects of Digital Twinning. The multifaceted nature of the problem requires raising the abstraction level in both the Real (Actual) and Virtual domains, effective dissemination of information resources, and a design inspired by verification and validation. The proposed framework combines the Quintuple Helix model with the Problem and Operational Domains of a Real (Actual) Twin, the Solution and Implementation Domains of a Virtual Twin, and the Execution Domain as the bridge that links them. Verification and Validation dimensions follow the Meta Object Facility abstraction layers (Instance, Model, Meta-model, and Meta-meta-model) mapping over five Helices. Embedding the complexity reduction mechanisms in the proposed framework builds a suite for extendible and verifiable digital twinning in simulation and real-time scenarios.

**Keywords:** verification; validation; digital twins; system of systems; domain specific modeling; verification frameworks; helix models; quintuple helix model; cyber-critical systems; meta object facility

## 1. Introduction

Verification and validation of complex cyber-critical systems are challenging aspects that require extensive engineering and scientific research. They are essential for assessing the maturity level of the engineering process and the sustainability of the coexistence of real-world systems and their digital counterparts. From an engineering process perspective, design involves a forward-looking combination of specification, modeling, design, and implementation activities, methods, techniques, and platforms. Verification and validation are backward-looking activities performed to confirm the proper alignment of the vision and solution and to assess the quality of operation according to the system's metrics. Process management involves guiding the overall life cycle stages of cyber-critical systems. Frameworks that support creativity in forward-looking and critical thinking in backward-chaining cognition are highly desirable in complex engineering efforts. Although raising the abstraction level decreases the reuse capacity of engineered artifacts, it is a powerful characteristic of a mature mental model. This research aims to combine digital twinning, multidimensional cognition processes, and systems engineering methodology to build an extendable, generic, configurable, and usable framework that supports the specification, modeling, design, verification, and validation of sustainable cyber-critical systems. Model-based approaches require careful integration into the systems engineering process. Defining the granularity level of a particular model presents two opposite challenges. If the model is coarse-grained, it is not well-suited for analytical evaluation and the generation of reliable guidelines for further implementation. The development of a detailed

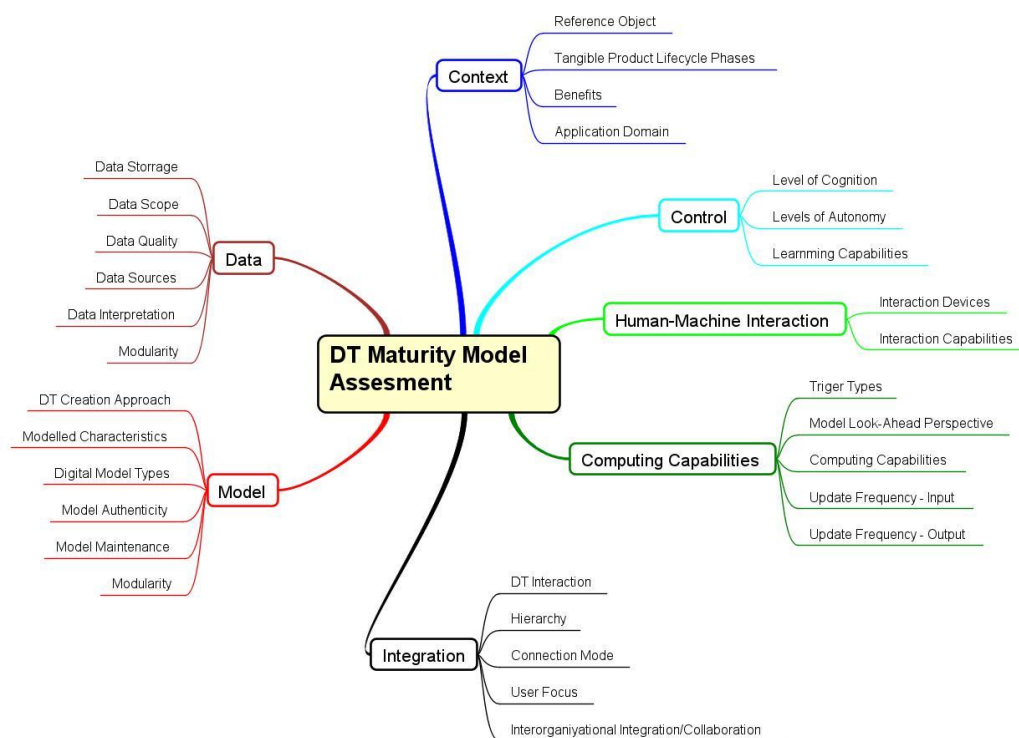
model requires significant effort to convert it into a usable implementation [1]. Modeling systems based on their delivered values provides new perspectives on verification and validation. The continuous delivery of value throughout the system's lifecycle, in accordance with the system values model, is crucial in various domains [2]. There is still a lack of common understanding regarding the formality level that justifies the incorporation of verification and validation in the early stages of Model-Based Systems Engineering. Research has shown that Systems Modeling Language (SysML) is the most commonly used formalism for specifying system descriptions [3]. The study also indicates that the requirements specification is significantly less focused on than the design phase, with reducing the risk of late defect detection being the major motivating factor [3]. Currently, there are various formalisms that rely on transforming behavioral models into corresponding analytical models. While these formalisms offer flexibility due to the range of analytical languages and notations available, it is widely agreed that they introduce additional complexity and require proper handling. The interoperability of different tools, general-purpose or domain-specific languages, and integrated production environments supporting simulations is one of the most challenging issues for further research and engineering directions. Our approach to the proposed framework model specification has been directly influenced by general findings adopted from [3] and visualized as a Mind-map diagram (Figure 1).



**Figure 1.** Verification and Validation MBSE Challenges (*Adapted from [3]*).

The concept of Digital Twins (DT) has been around for quite some time, continuously challenging the specification, modeling, design, implementation, and exploitation of complex Cyber-critical systems [4,5]. With the rise of the Smart Internet of Things (IoT) and the use of machine learning models, there are several challenging research and engineering directions such as Cyber-physical systems (CPS), data science, optimization, and security and privacy [6,7]. Current research questions about DT revolve around the impact of modeling, different data sources, communication between Real (Actual) and Digital (Virtual) twins, problem domains, purpose, validation principles, and the elements and their potential reusability [8,9]. The practical aspects of DT, such as state synchronization and deployment within the DT network, deserve particular attention from a dynamic (behavioral) modeling perspective [10]. These characteristics position DT as a potential analytical framework that focuses on modeling and model-based engineering through integrated modeling environments. DT, as the virtual representation of a physical asset, is directly influenced by different problem domains, catering to the interests of specific stakeholders. While DT holds the promise of revolutionizing the operations, support, and sustainability of deployed systems, it faces several industrial barriers. The development time and costs associated with building a DT and particular domain expertise make it difficult to undertake for many organizations [11]. Digital Engineering Strategy (DES) positions DTs as a natural framework for tracking and reporting the engineered system's physical condition. It enables employing prediction and health management (PHM) technology principles to transform systems sustainability support by condition-based maintenance (CBM) platforms. One of the problems of having two systems (the physical one and its

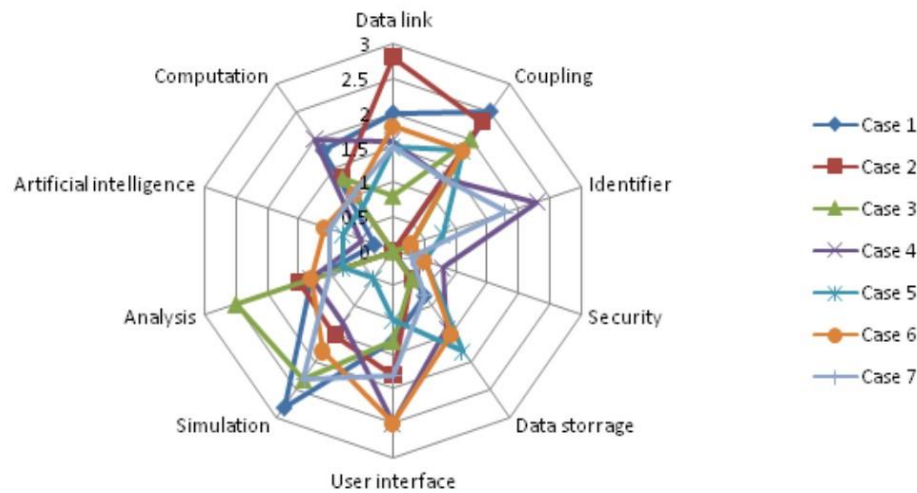
digital replica) is that their behavior may not always be consistent. The fact is that physical systems possess inherent uncertainty, and it is a challenging endeavor to determine the actual cause of potential differences considering the possible uncertainties built in their digital counterpart. Engineering adaptive systems (systems that regularly change their structural and behavioral characteristics to cope with context disorders) additionally question the applicability of DTs [12]. Concerning the DT maturity model [13], the highest maturity level corresponds to Intelligent DT as a virtual system model of the physical twin with adaptive AI and reinforcement learning. The comprehensive study of the DT Maturity Model foundation [14] assesses Digital Twins in seven categories (context, data, computing capabilities, model, integration, control, and human-machine interface) with 31 ranked characteristics. It is a generalized model for Digital Twins evaluation purposes (Figure 2).



**Figure 2.** DT Maturity Model (Adapted from [14]).

Dealing with multilevel uncertainty is a significant challenge when relying on Digital Twins (DTs) as part of Verification and Validation frameworks or when trying to verify and validate their structure and behavior. An important question arises: who validates the Validator and verifies the Verifier? Another source of uncertainty in DTs is their human-centric nature. While technology aims to replace human involvement in repetitive tasks through procedural-declarative specifications [15], integrating human cognition with technology frameworks remains unavoidable. With a focus on humans, DT-based frameworks can become non-deterministic, discrete socio-technical systems. Incorporating robots into production systems demands enhanced collaboration between intelligent robots and human operators [16]. In recent research, DT development frameworks have used various virtual concepts, including mirror space models, product agents, product avatars, digital threads, prototypes, workshops, data, and features. Feature-based DT analysis (FEDA) identifies essential features that may exist in the DT of a specific asset, such as data link, coupling, identifier, security, data storage, user interface, simulation model, analysis, artificial intelligence, and computation. These features serve as the foundation for the assessment methodology of conceptual DT frameworks based on a holistic score scale (see Figure 3) [17].

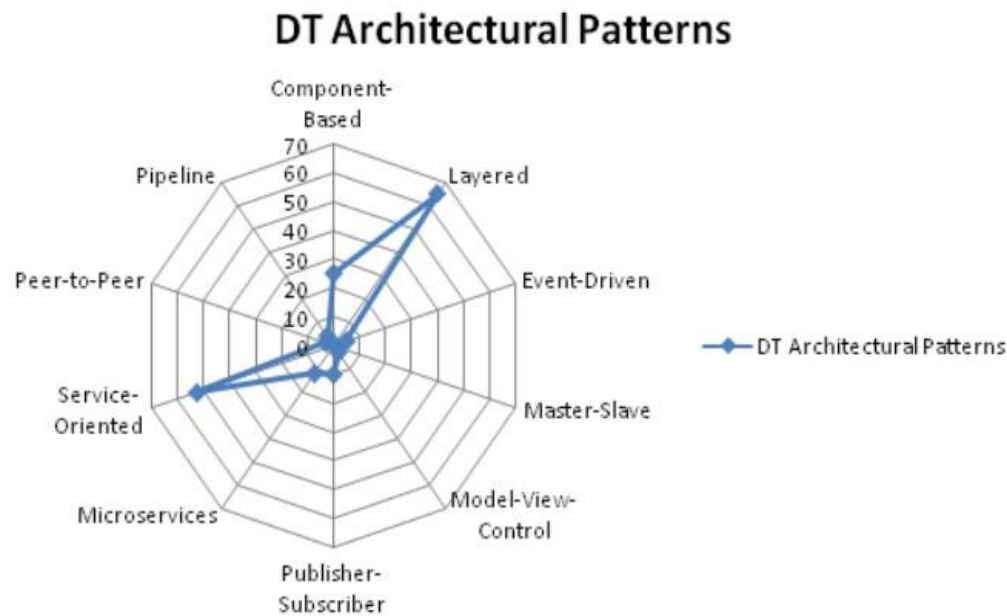




**Figure 3.** Feature-Based DT assesment heuristics (*Adapted from [17]*).

Regarding DT architecting, two main approaches direct contemporary research activities. One relies on Systems Architecting, while the other favors Software Architecting with a noticeable shift from Systems to Software Architecting approach. The research in DT architecting usually starts with a Referent Architecture Model (RAM) validated with a Validation by Example method [18]. DTs are software-intensive systems with a broad set of Quality Attributes (QAs), with possibly hidden interdependences that affect the assessment process and results. As such, they justify the application of existing software architectural patterns as DT core architectural models, reducing the need for reinventing the novel RAMs. Although there is a lack of widely accepted architectural solutions for digital twins, the dominant ones are the layered and service-oriented architectural patterns (Figure 4).

The digital transformation of contemporary business systems justifies the combination of Enterprise and Service-Oriented Architectures. The Enterprise Architecture Modeling approach integrates the heterogeneous elements of a business system, while Service-Oriented-Architecture tends to harmonize business and Information Technology (IT) dimensions [19]. With the current proliferation of micro-services scripting as an challenging, language based, technology for the distributed architectures, the requirement-driven DT Microservice framework architectures bust. In [20], the authors propose DT tree-tired Microservice framework architecture, composed of the Business Layer (modeled with the Business Process Modeling Notation - BPMN), the Functional Layer (Message Broker Architecture), and the Information Layer (Smart Data Services supported by the Federated SPARQL Endpoint - with Resource Description Framework format). Each layer is formally specified through the set of functional and nonfunctional requirements extracted from the RAMI 4.0 Reference Architectural Model for Industry 4.0 [21].

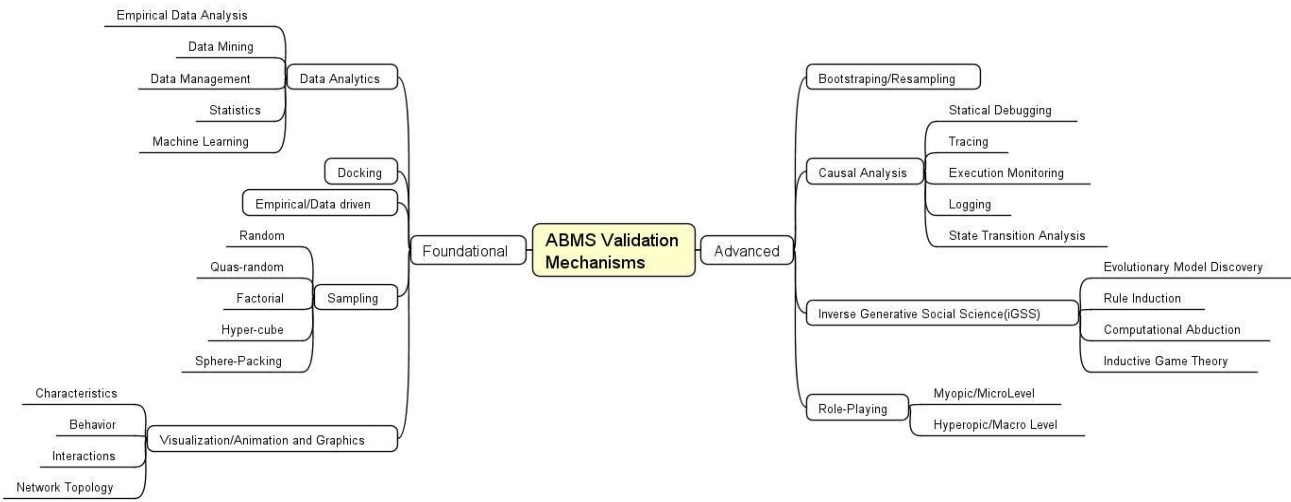


**Figure 4.** DT Architectural Patterns utilization (*Adopted from [18]*).

Systems Engineering and System-of-Systems paradigms are well-suited contexts for model-based decision-making concerning the requirements phase of DT development [22]. The issue with complex systems is not the complexity if one assumes the deterministic behavior in fulfilling their specified mission while producing desired outcomes. The main problem with complex systems is the discreet nature with configuration (context) dependent emergent properties and non-proportional relation between applied stimulus and the reflected outcomes. It may result in potentially dramatic failures without a prior warning or even an indirect announcement. The potential benefits of DT are that, through modeling and simulation over virtual twins, it is possible to catch and explore the emergent system properties without exposing the physical twin to potentially harmful outcomes [23]. *The unavoidable role of prototyping in mission-critical systems design exhibits a perspective approach for a prototyping framework based on verifiable formal specifications involving meta-meta, meta, and modeling abstractions [24].* The Artificial Intelligence (AI) principles and methods play a significant role in DT framework development and enable constant improvement through integrated transfer learning capabilities [25,26]. The enhancement of design, verification, validation, and continuous improvement of AI-controlled cyber-critical systems demands novel methodologies that leverage machine learning while coping with their inherent non-linearity and complexity [27]. Engineering cognitive and intelligent systems currently lack suitable formalisms that enable specification, modeling, and formal verification at multiple abstraction levels while combining the open and closed principles on informational and functional domains [28]. The traditional Verification and Validation methods of safety-critical systems, with AI components in their software core, seem inappropriate and thereby crucially demand the development of novel approaches [29].

Digital Twins-based Verification and Validation ranges from functional to non-functional and safety-critical requirements. The survey [30] cross-relates the essential elements of Digital Twins that serve as a foundation for Verification and Validation purposes. Modeling and models are founded as fundamental sources, while simulations and operational data usage appear significantly less utilized. The growing reliance on modeling and simulation results coupled with operational data to guide system design and operational Verification and Validation increases the importance of making those results reliable in different contexts. The collaborative safety-critical systems demand parallelism modeling and bring the System-of-Systems (SoS) Verification and Validation to contemporary research focus, particularly with IoT, and synchronization of reactive components of complex cyber-physical systems [31–34]. With the proliferation of Agent-Based Modeling and Simulation (ABMS) methods, the lack of mutually accepted approaches and standards for assessing the simulation is a

significant obstacle. The main question is how to select the relevant subset of validation-supporting mechanisms and raise the credibility level of applied models from different stakeholders' aspects [35]. The addressed mechanisms cluster into two main groups. One is the Foundation group, which clusters mandatory mechanisms, and the other is the Advanced group, which clusters the exceptional ones (Figure 5).



**Figure 5.** ABMS Validation Mechanisms (*Adapted from [35]*).

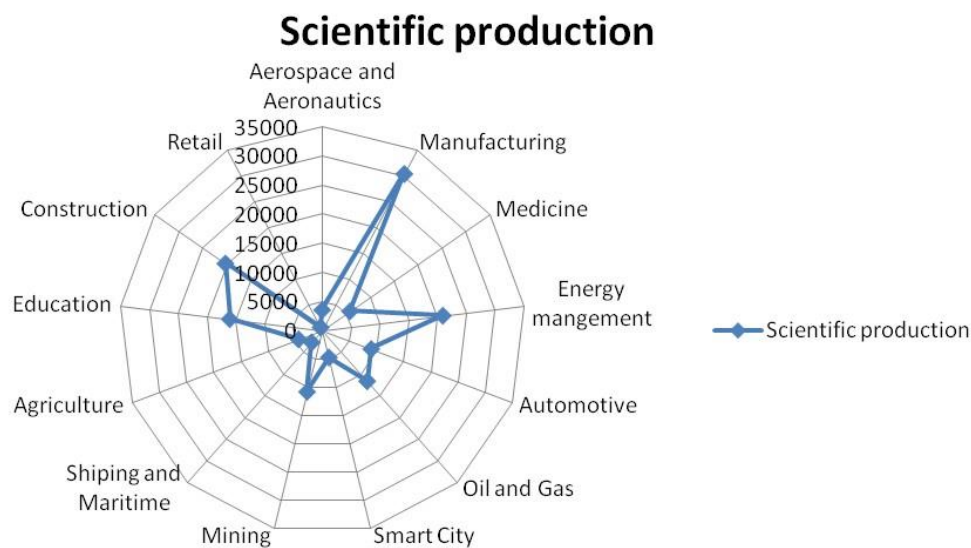
The validation of DT models demands a creative combination of expert knowledge gained through critical analysis, with the operational data gathered from the sparse network of IoT sensor devices incorporated into the architecture of an actual system. DT modeling needs a balanced combination of sufficient details that bust the resolution level and high enough fidelity to mimic the actual system properly. DT servicing layer demands the effective acquisition of real-time data, responsive analytics, and the efficient dissemination of feedback. The current lack of a systematic framework for DT validation is the main obstacle but, at the same time, a challenging issue. In [36], the authors elaborate on the general validation strategies (manual/visual inspections, property testing, model-based testing, and machine learning) and the opened problems (modeling realism, data uncertainty, system dynamics, use case alignment, and reporting invalid models). They end up with the conceptual DT validation framework/strategy that relies on the synergy of expert knowledge and the combination of historical and operational data.

The framework-based approach to engineering complex systems has a long tradition that favors top-down architecting with early-stage verification and validation capabilities. A framework is either a physical or a conceptual skeleton that guides a particular artifact construction by expanding and specializing the generic structure that specifies a family of interrelated products or procedures. It favors reusability by managing the control flow and orchestration of dynamically configured components in an inversion of control manner. The conceptual framework is an analytical tool that enables critical analysis of various concepts to develop new ones. It focuses solely on concepts and lacks factors and variables that naturally belong to the conceptual model successor. There are two major categories of contemporary frameworks: non-software empowered (usually represented as a set of structured and semi-structured documents), and software empowered (software-supported collaborative/cooperative environments supporting the digital transformation of problem domain) [37]. Software-empowered interoperability frameworks are of greater importance for this research perspective. They demand intensive, time-consuming specification, modeling, and meta-modeling activities performed and managed within the scope of related projects or portfolios. The development of the verification framework usually incorporates the mechanism for statistical correlations and parametric space search, with probabilistic coverage guarantees, to determine potential parameter regions (configurations) that complies or violate predefined specifications [38,39]. Regarding the role and importance of early verification in engineering complex systems, the confidence level in verification methodology and obtained results may vary due to the experiences gained through the

previous design phases. That is why it is essential to adapt the optimal verification strategy selection mechanisms through a belief-based model [40] or AI mechanisms that aid the critical analysis phase in deductive reasoning [41,42]. Integrating digital twin technology in cyber-physical systems (CPS) and the Internet of Things (IoT) boosts their intelligence and enables DT model refinements without disrupting the operation of an Actual System. The promising networking platforms (5G and 6G) with highly connected cells enable collaborative model improvements like blockchain middleware as a framework (CoTwin) [43] and Zero-Touch Network management secured framework [44]. Visual analytics for DT play a critical role in effectively navigating humans through twin data but currently lacks guidance to fully integrate human domain experience and cognitive abilities into the intelligent decision-making process of digital twin systems [45]. DT framework operation mechanism crucially depends on the quality of the data integration layer and the means used in Twin Model verification and validation processes. Twin data origins from heterogeneous sources need explicit marking by the spatial-temporal and modal qualifiers, are naturally multidimensional, and serve as a foundation for application services in optimization, model construction, interaction, and decision feedback frameworks' states. The Tensor-Based representation of heterogeneous, multidimensional data instances, with different orders of tensor [46], represents a challenging formalism for data fusion in DT data models and instances. Data Analysis Workflows (DAWs) represent the structured specifications that guide data sets' analytical processes. Their popularity emerges with the rise of dataset complexity, progressive growth of interdependencies, and the number of individual data instances. With the proliferation of Not-only-SQL (NoSQL) repositories and the possibility of topological and operational distribution, locating the data handling mechanisms outside the actual code busts the dynamic multiplatform execution abilities. Formal, conceptual model of logical and physical DAWs, the infrastructure and execution semantics, and static and dynamic DAWs validity constraints abstractions, defined in [47], serve as the foundation for concrete Validity Constraints (VCs) specification (setup-related, task-related, and file-related). In the verification prototype, the authors have extended the NextFlow (a Domain Specific Language (DSL) for creating scalable, portable, and reproducible workflows [48]) with two directives (*require* and *promise*), thereby avoiding a novel VC specification language. The utilization of well-known scripting platforms, like Apache Groovy [49], and the associated frameworks, like Gradle [50] and Grails [51], has influenced the platform-oriented abstraction with the bridge for the concrete platforms extendibility as an architectural foundation of our conceptual framework.

The industrial applications of digital transformation (DT) generate a lot of interest in both academic and production settings. The rise of Industry 4.0, 5.0, and 6.0 paradigms continues to influence methodologies, methods, and technologies in modern industries. Virtually every industrial sector is heavily involved in digital transformation [52]. Research in the most significant domains (Figure 6) indicates uneven coverage, with Manufacturing, Construction, Energy management, and Education being the most significant in that order.





**Figure 6.** Scientific production over industrial sectors (*Adapted from [52]*).

Intelligent systems in any industrial sector can greatly benefit from the automatic generation of DT simulation models that are updated in real-time. This can lead to increased productivity, cost reduction, improved decision-making, safety, better design, planning, maintenance, remote access, and optimization in various engineering stages. The need for rapid decision-making support is growing, requiring a high level of automation in the decision-making process. There are four main decision-driving forces: table-driven (fast, event-driven with static connectivity between event and appropriate event handler), process-driven (strategy building, algorithmic, rule-based, with dynamic binding), data-driven (parametric, dynamic, adaptive, with binding over external data sources) [53], and knowledge-based (evolutionary, adaptive, generative, with continuous improvement). Providing support for different core decision-making strategies is crucial for creating a sustainable DT verification and validation framework specification.

The operation of a real-time system requires continuous optimization of strategies and configurations, along with support for leveraging the structure and behavior of the Digital Twin (DT) [54–56]. Model-based simulations, enhanced by learning mechanisms and big data utilization, involve gradual tuning of the Actual System Model (ASM). Due to the diverse applications and complex models of DT, there is a focus on developing a surrogate modeling approach for building the ASM, leading to the development of the DT Mediator (DTM) as a core component of the proposed framework [57]. The DTM facilitates communication between the Actual System (AS) and its corresponding Digital Twin (DT), handling the collaboration responsibilities.

The acquisition, storage, retrieval, and visualization of key performance indicators related to domain-specific Digital Twins represents an important set of framework features. Modern software tools primarily rely on Graphical User Interface (GUI), which is typically implemented as parameterized dashboards with an extendible set of views [58]. Digital Twins that support the product assembly process heavily rely on the accuracy and compliance of actual assembling geometry and its 3D model. Currently, there is a lack of efficient model-sharing and management mechanisms [59]. In the construction sector, the spatial arrangement of different construction equipment and their interaction shows a higher dynamic level over the stages of building environment progression, in correlation with the built facilities, compared with manufacturing (production) lines. This ultimately demands Digital Twin integration with 6D Building Information Management (BIM), Geographic Information System, corresponding Enterprise Information System [60,61], Six M (Machine, Manpower, Material, Measurement, Milieu, and Method) strategy [62], and emerging Digital Twins Information Systems [63]. Some obstacles in the currently available solutions

for Digital Twins applications in Building and Construction Engineering are the lack of sustainable support for data integration and interoperability, data accuracy and completeness, scalability and complexity issues, privacy and security, and standards and governance support [64]. Automated visual quality assessment in virtual and augmented reality extends Digital Twin visualization capabilities and aids framework visualization, simulation, and animation quality [65].

The main focus of analyzed references is on the real-time aspects of applying Digital Twins. However, there is little attention given to systems built on event-driven architectures in socio-technical domains. By raising the level of abstraction, we believe it is possible to elevate the Digital Twin paradigm beyond the traditional real-time and sensor-focused connection with the actual system. This can be done by abstracting the event coupling mechanisms which hide the physical characteristics of the specific coupling through mediator services. This leads to a challenging concept of Virtual Twins that offer end-to-end infrastructure that accelerates the collaboration of the actual systems at arbitrary abstraction or hierarchy levels.

The previously discussed challenges have directly influenced our research approach. Our ultimate motivation is to formally and conceptually specify the extensible hyper-framework for the verification and validation of Digital Twins through multilevel and multidimensional virtual or digital twinning.

2. Materials and Methods

The analysis indicates a lack of framework-based integration of DT Design, DT Verification, DT Validation, and DT Operation. DT Design frameworks usually focus on various aspects of the DT design process, including formalisms, models [66], and mimicking object-oriented software development integrated environments [67]. The reference architecture of network aggregated DTs and service orchestration, with six steps and four stages, represents a challenging starting point [68]. We argue that Verification and Validation are not isolated steps in the DT Design and Operation processes, similar to testing in software development. When integrated into design activities, they form a mental discipline that ensures the lowest possible risk level for utilizing an engineered system. We have defined DT Competence ontology, a Quintuple Helix generative architecture, Meta-object-facility layered architecture, standards and standardization, and bridging of the abstraction and implementation in favor of heterogeneity as five main pillars of the proposed conceptual framework specification.

The first pillar relies on the Digital Twin Consortium's Digital Twin Ecosystem Capabilities Periodic Table, containing a systematic collection of referent capabilities and the associated semantics. Developed to bust the acquisition process and the comparative analysis of different DT use cases, it enables leveraging the quality level of the domain-specific DT requirement models. From our perspective, it represents an unavoidable starting point in building the generative conceptual framework architecture, fully compliant with relevant referent specifications. We have reorganized the original Periodic Table as a Hub-Mind map diagram, with general groups presented in Figure 7.

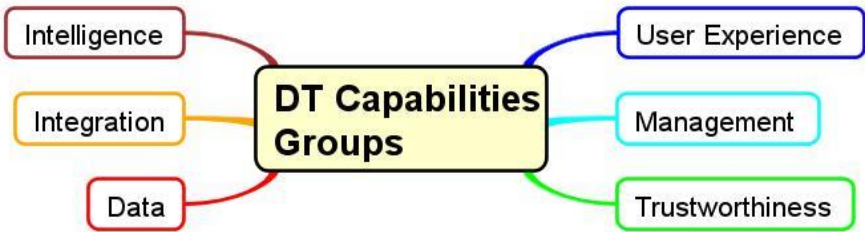


Figure 7. Digital Twin Capabilities Hub (Adapted from [69]).

The DT capabilities groups differ in the contained number of level-1 capabilities. Figure 8 correlates level-1 capabilities as a radar diagram and indicates the contemporary domination of Data, Intelligence, and Use Experience groups. We have additionally sub-structured the individual groups, as appropriate, to add further fidelity tuning mechanisms. For example, Figure 9 represents the sub-

structured (Data Harvesting, Data Management, and Persistency) grouping of a Data group as a Mind-map diagram.

DT Capabilities/Number of Services

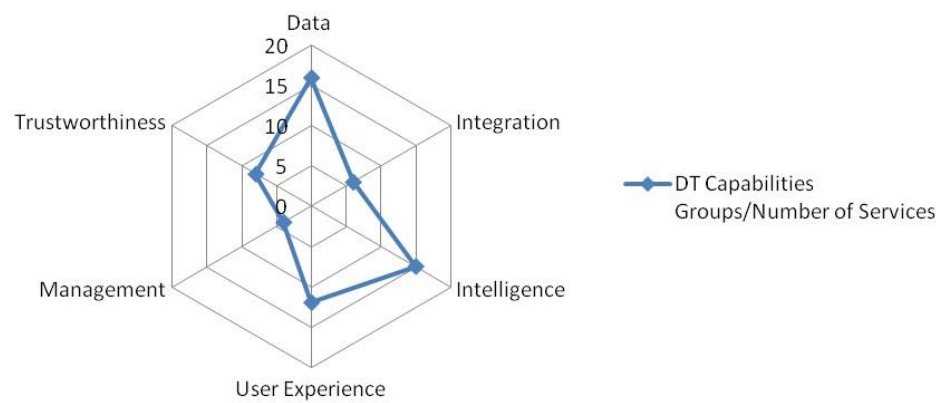


Figure 8. DT capabilities number per groups (Adapted from [69]).

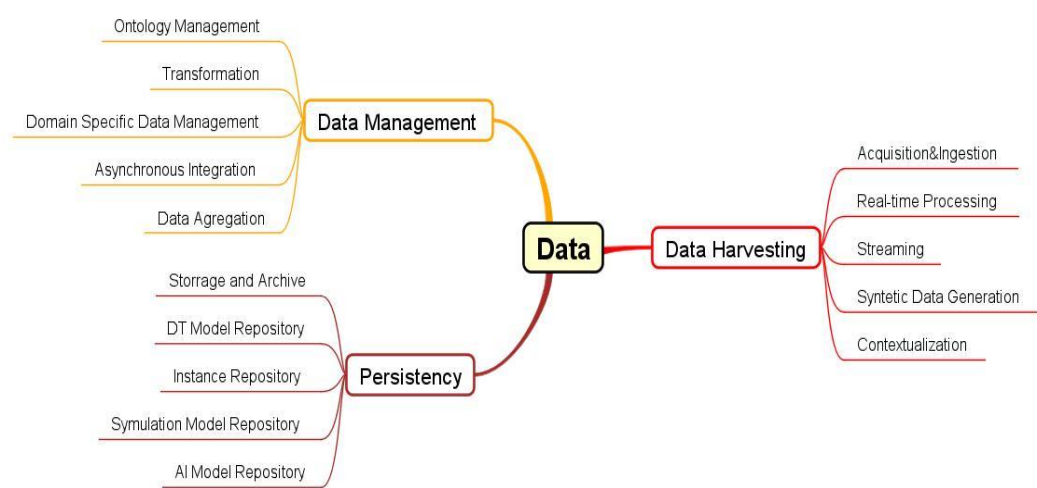


Figure 9. Detailed structure of Data group (Adapted from [69]).

The hub-mind-maps of the Management, Intelligence, User Experience, Trustworthiness, and Integration, build the reference capability model foundation (Figures 10–14, respectively).



Figure 10. Detailed structure of Management group (Adapted from [69]).

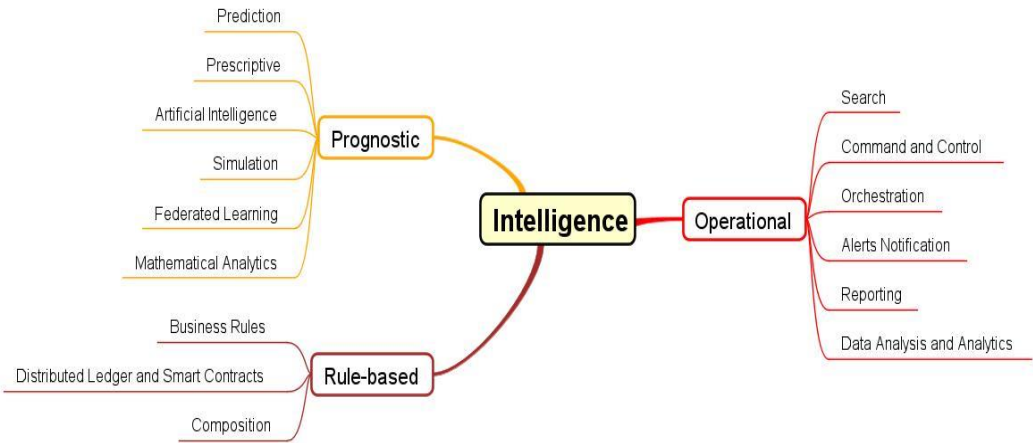


Figure 11. Detailed structure of Intelligence group (Adapted from [69]).



Figure 12. Detailed structure of User Experience group (Adapted from [69]).

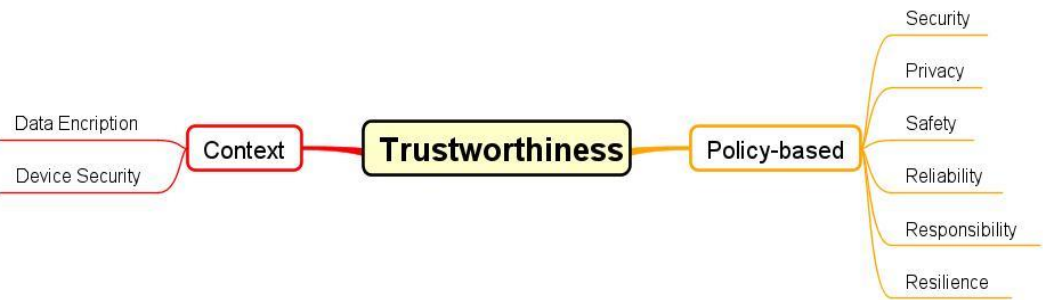


Figure 13. Detailed structure of Trustworthiness group (Adapted from [69]).

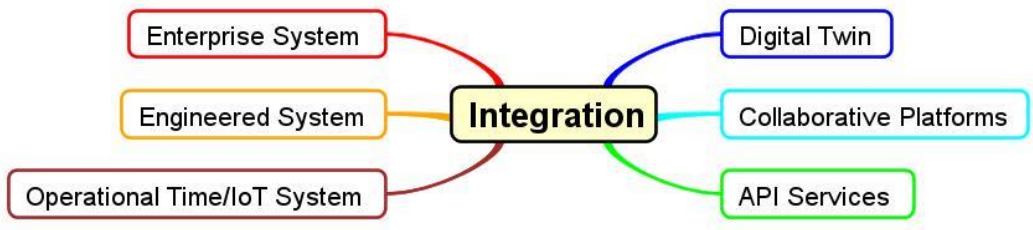


Figure 14. Detailed structure of Integration group (Adapted from [69]).

Regarding the presented capability model, it is possible to define a family of related specific frameworks or a single, generic integrated hyper-framework with the opened set of capabilities, each with extendible nesting features.



The combination of run-time pluggable, strategy-driven, DT configuration building with delegated construction of individual capabilities dimensions has inspired the use of extendible builder combined with factory method creation and strategy pattern-directed building as a core framework service.

The second pillar relies on generative potentials of the DNA helix model with the built-in combinatorial complexity replicating within two back-bones coupled by four-dimensional nucleotides (Figure 15). DNA model has inspired many research endeavors outside its natural life science domain. Operational Research, Computer Science, Economy, Knowledge, Business, Social Sciences, Education, Technology, Smart Cities, and Innovations are typical examples. With the structural expansion of the genuine DNA model either by single (Figure 16) or double (Figure 15) helixes, the family of derived higher-order models emerged (Triple, Quadruple, Quintuple, and beyond). The higher-order helix models have dominantly appeared in different socio-technical domains.



Figure 15. The Basic Double Helix Model.



Figure 16. Single Helix.

The relative comparison of different helix model referenced searched in favor of this article and roughly correlated over last four years, is presented in Figure 17.

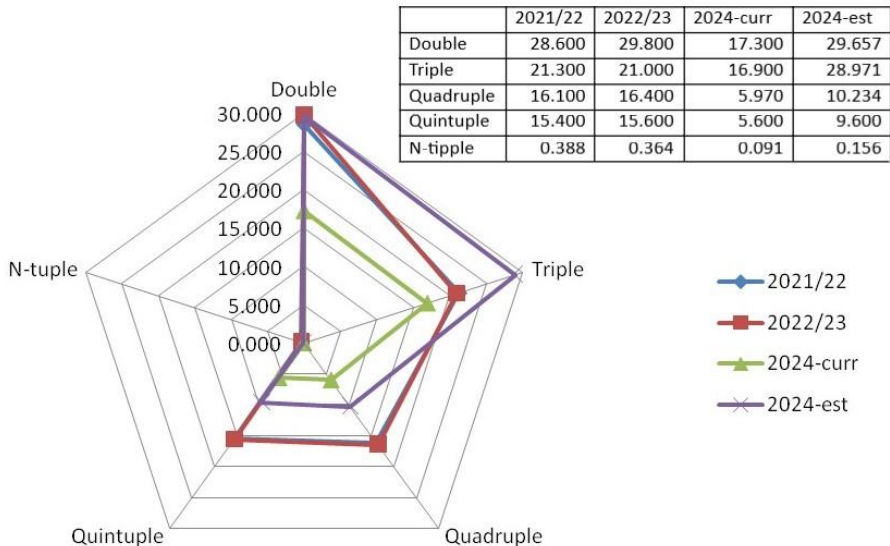
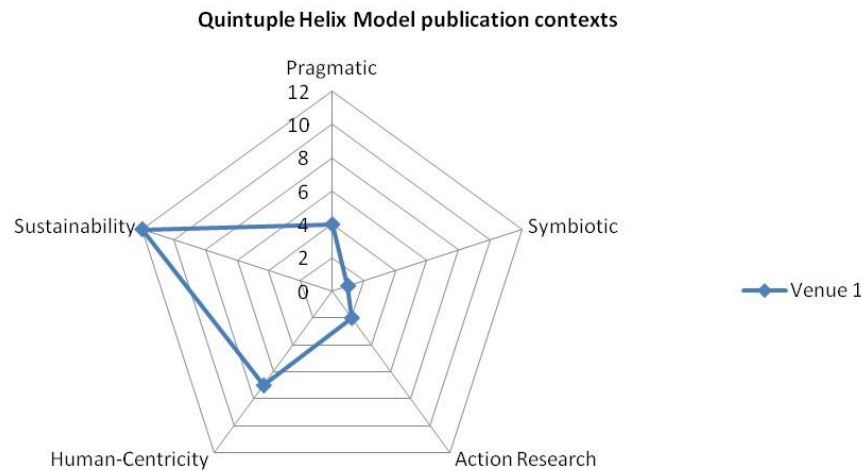


Figure 17. The relative comparison of different helix models apperiance frequency.

The results show the relative dominance of Double and Triple Helix elaborations with the stable growth of Quadruple and Quintuple instances. N-tuples helix models are beyond the scope of statistical error. The application of helix models dominantly belongs to the conceptualization of

knowledge-based economy studies and social sciences. The traditional triple helix model sublimates academia, industry, and government interactions. The transition from triple to quadruple engages the additional helix associated with democratic aspects (civil society) of a knowledge-based economy and community, while the transition from quadruple to quintuple assumes extension by additional ecology and ecological sensitivity helix [70–73]. The quintuple helix mode is additionally analyzed as a paradigm of future studies and digital technology foresight [74], promoting general sustainable development [75] and specific industries [76]. The cross-related domain analysis of the quintuple helix model application in different problem domains, adapted from [77], is represented by a radar diagram in Figure 18.



**Figure 18.** Quintuple Helix Model domains (Adapted from [77]).

We found the Quintuple Helix model the most suitable for the proposed Conceptual Framework architecting. The relevant details appear in the Results section of this article.

A third pillar relies on the unified conceptualization approach to reasoning about framework entities and stages. The assumption that human intelligence and cognitive processes build an arbitrary configuration through the dynamic instantiation of abstract concepts aligns well with commonsense reasoning [78]. With the proliferation of intelligent DTs, delegating mental tasks to an arbitrary physical or virtual automata instance is a challenging mainstream. With AI reasoning, dealing with the dynamically unpredictably ambiguities, emergent properties, and the social context of operation appoints the reflection as a currently missing mechanism. The abstracting mechanism has to be closed and self-modifiable to cope with the reflective changes in the execution context [79]. The closeness principle has to guarantee fully standardized specification and dedication of individual layers. The self-modifiability offers the inherent intra-layer transformation mechanism with the absolute (unlimited) gaining potential.

The Meta-Object-Facility (MOF) is the Object-Management-Group (OMG) standard for writing meta-models (models of models). It provides a typed system for building the architecture of complex systems in the context of model-driven engineering and fully supports closeness and self-modifiability. An advantage of meta-concepts generally is that they enable the use of concepts without prior knowledge of the concepts' specific features. There are two distinct aspects of closed-layered architectures, the intra and inter-layer. Intra-layer defines different entities at the same level of abstraction. The inter-layer specifies the same entity at the different abstraction levels. Each concept, appearing on an inner layer, is fully described by the abstract concepts from the upper layer, excluding the final layer with auto-definable properties. The OMG MOF is composed of four abstraction layers. The M0 is the instance layer (object), M1 the model layer, M2 the meta-model layer, and the self-specifiable M3 the meta-meta-model layer (aka language). The core specification of OMG MOF appears in [80]. The traditional MDE references M0 and M1 layers and appears in object-oriented modeling tools. Digital Twin Definition Language (meta-meta-model abstraction layer) is an example of a language for describing models and interfaces for IoT digital twins. It is defined as JSON-LD, leveraging JSON-based and Resource

Description Framework (RDF) systems, and contains a set of meta-model classes (Interface, Command, Component, Property, Relationship, Telemetry, and data types), and semantic type annotation [81].

The additional elaboration on the MOF as the multilayered Reference Architecture foundation for the main architectural constituents, the modeling abstraction, and the information resource abstraction appear in Section 3.

A fourth pillar relies on *the standards and standardization issues being inseparable from the engineering endeavors, virtually from their first announcements by Charles Le Maistre, a pioneer of international standardization [82]. They have been defined or prescribed with the general mission to ensure quality product and process development and are avoidable in the early stages of research or engineering projects. With the proliferation of standard organizations and domain-specific standardization, the main obstacle is to recognize what exactly Standards standardize and to what degree of formalization. In [83], the author cross-examines five relevant standards for modeling digital twins in digitalized factories. In the context of this article, the most referenced is ISO 23247 - Digital Twin Framework for Manufacturing, which provides a generic development framework with a set of standardized building blocks and assembling support for configuring specific DT implementations based on IoT [84–86]. The next referent is the IEC62541, the Open Platform Communication Unified Architecture (OPC UA), for data exchange between sensors and cloud applications [87]. Interoperability between Digital Twin standards and specifications is a challenging issue primarily motivated by the diversity in their operational use [88–90]. The interoperability within an open set of relevant related standards is a framework's must.*

Bridging the abstract specification and the diverse repertoire of implementation platforms establishes a fifth framework's pillar that favors heterogeneity instead of homogeneity while harmonizing the involved specification, development, modeling, implementation, and execution platforms. Digital Twins are software systems, and thereby ultimately specified, modeled, implemented, verified, validated, and operated having software in mind. According to the detailed enumeration [91], software vendors have recognized the opportunities to support the DT paradigm in different stages of the engineering life cycle. Although [91] elaborates on the wide range of related technologies and tools, we may conclude that there is still a lack of research articles that address the overall integration capabilities. The requirements set, derived for the comparison purposes of three commercially available integrated DT platforms [92] and evaluated through the experimental smart-room case study, shows significant compliance with the respectable number of partially or fully satisfied requirements.

We hope the proposed conceptual framework, joined with similar approaches concerning the requirement specification of future frameworks [93], will open new perspectives in that direction.

### 3. Results

The proposed Conceptual Framework represents a novel approach to modeling and interconnecting multidimensional constituents of DT-based conceptual framework with built-in Verification and Validation features that may aid the entire life cycle stages of Cyber-physical-Systems model-driven engineering.

#### 3.1. The Requirements Modeling and Specification

We first specify the requirement model of the capabilities of a novel proposed conceptual framework. The model classifies the capabilities into three main groups: Essential, Highly Desirable, and Desirable (Figure 19). The adopted classification is neither absolute nor determines the order of components' development and integration in the assumed framework's architecture. It favors the capabilities we find novel regarding the other cross-related frameworks.

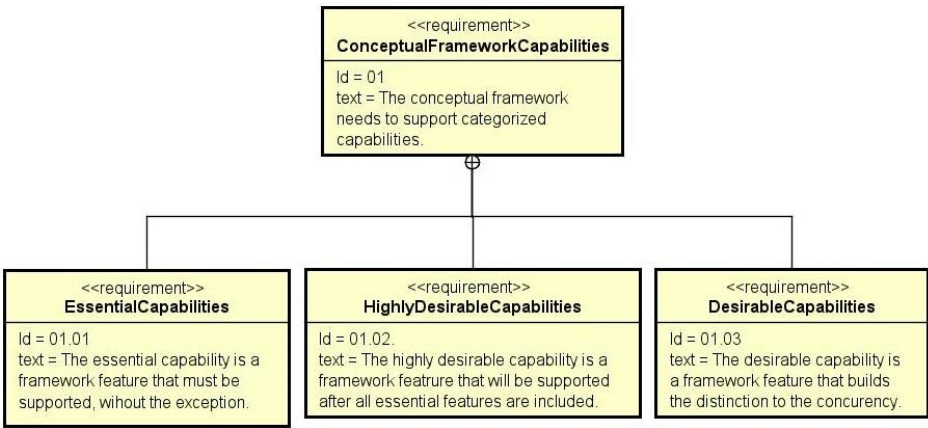


Figure 19. SySML based Conceptual Framework Capabilities Groups.

Table 1 sublimates the detailed requirements derived through the critical analysis presented in the Introduction and Materials and Methods sections and used as the foundation for the creative phase of novel conceptual framework specification development.

Table 1. The detailed conceptual framework requirements.

Category	RQ	Context/Role	Description
Essential Conceptual Framework Requirements	RQ1	Embedding the Process and product Verification and Validation.	It is essential to use digital twinning within product and process assets and integrate them into a single framework.  Process and product verification and validation through five imbued domains:
	RQ2	Quintuple Helix Model foundation.	1. Problem domain 2. Operational domain 3. Solution domain 4. Implementation domain 5. Execution domain
	RQ3	Meta Object Facility (MOF)-abstraction layered model over a quintuple helix.	(instance, model, meta-model, mete-meta-model aka language)
	RQ4	Abstract Information Resource support	Data Analysis Workflows support through Visitor Accept Interface implementation and Repository abstracting.
		with distributed heterogeneous repository handlers.	Load and store repository interface (data, information, knowledge, wisdom). Abstracting the Sources with get and put mechanisms.
	RQ5	Representation of domain specific DT as MVRC (Model, View, Repository, Control). Actual system domain (Physical system) support at different integration levels	MVRC architecture of DT mediator pattern. Micro-service orchestration, and Service-oriented architecting support.
	RQ6	(Unit, Component, Internal Configuration (System), External Configuration (System of Systems with Logistics ).	The communicating concepts are not conscious of other, potentially related concepts, existence. The mediator pattern-based approach is a must.

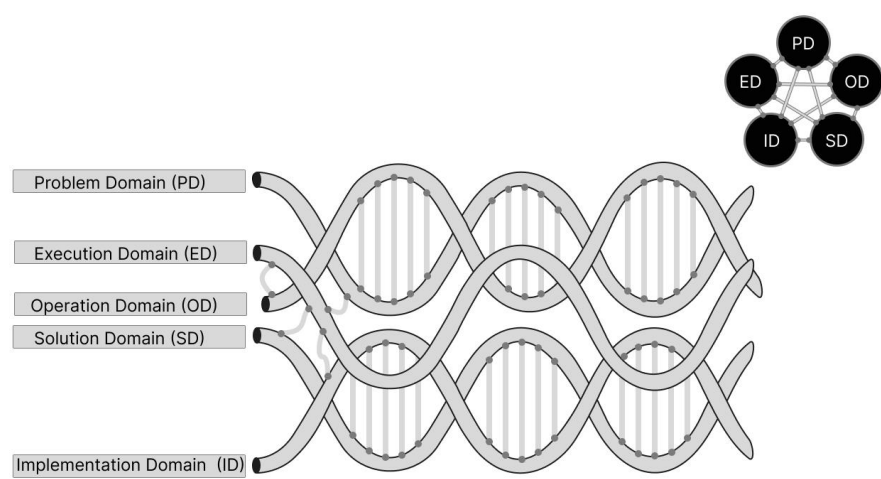


Highly Desirable	RQ7	Bridging platform independent and platform dependent mechanisms.	Splitting the Abstraction and the Implementation sides of system under consideration, with a bridge pattern, to enable undisturbed extending of both sides.
	RQ8	Abstracting the Cyber-physical and Cyber-socio-technical systems.	Universal approach to the main categories of DT application.
	RQ9	Evolutionary prototyping with continuous integration and deployment support.	The automatic, model-based generation of an initial evaluative prototype of the engineered system that evolves to deployable instances.
	RQ10	Modeling-based simulations support based on hyper-simulation model.	In favor of RQ9, the extendible simulation platforms based bridge support.
	RQ11	Version management and Configuration management support.	In support for RQ9 and RQ10.
	RQ12	Visual Analytics Support.	The extendible support for different visualization strategies is applied to the generic structure of information resource instances.
Desirable	RQ13	Standardized ontology	Regarding any dissent domain, the essential research direction assumes the universal ontology specification. Although extremely controversial, we see it as a generally desirable feature.
	RQ14	Decision-making Foundation.	The extendible support for different decision-making core strategies.
	RQ15	Reactive optimization of DT Model.	Bridging Abstract DT model and its implementations through the executable DTs.
	RQ16	Security and Privacy.	Security Policy Modeling, and Security abstraction layers bridging.

3.2. Quintuple Helix Foundation of DT Verification and Validaion Conceptual Framework

We propose five essential domains that constantly appear at the highest abstraction level of system and software engineering endeavors. The first two originate from the actual system/software specification stage. The third and fourth emerge from the engineering stage, while the fifth belongs to sustainable exploitation.

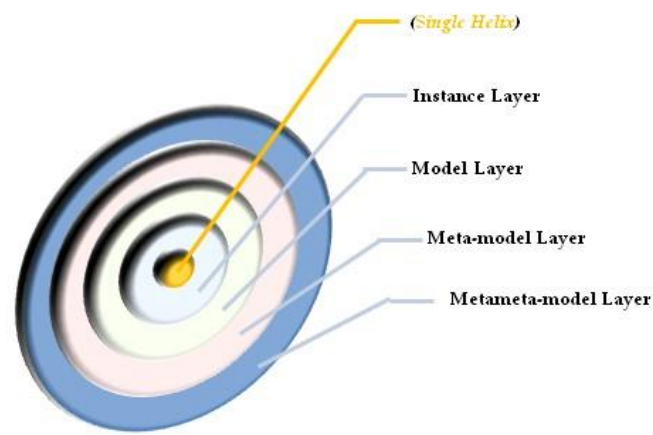
We roughly represent the Real-world system under consideration with one Double Helix composed of Problem and Operation Domains. The corresponding Digital Twin forms another Double Helix composed of a Solution and Implementation Domain. To integrate them, we need an additional Single Helix abstracting the Execution Domain. The selection of a generic Quintuple Helix Model is thereby fully justified (Figure 20).



**Figure 20.** The Integrated Quantuple Helix Model (the *Frameworks’ second pillar*).

Problem and Operation domains form the Actual Twin that models the structure and the behavior of the value chain for a concrete-engineered system. The Solution and Implementation domains build the Virtual Twin as a software counterpart of the concrete-engineered system. The Execution helix represents a real-time dimension that integrates previous helixes with the concrete deployment configuration instances of the engineered system.

According to the foundations presented in the Materials and Methods section, we define a Framework Helix as a link that bridges two ends of a Framework Wormhole Modeling Abstractions End (Figure 21) and the Information Resource Abstractions End (Figure 22).

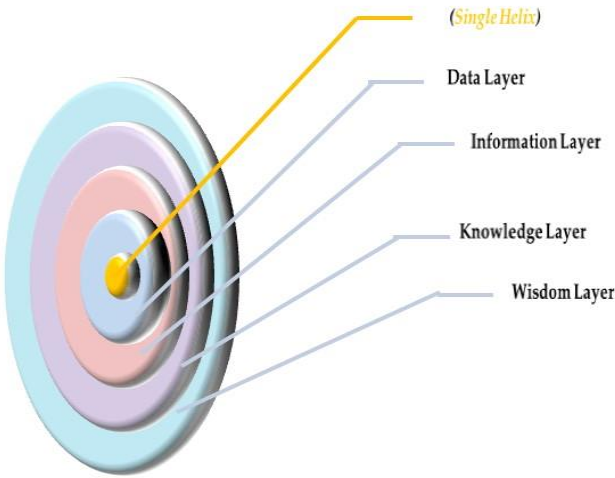


**Figure 21.** The Resource Abstractions End of a Framework Helix Wormhole.

The Resource Abstraction End model relies on the Meat-Object-Facility, Four Layers Wrapper, with the Instance layer as the lowest and the Mata-meta-model as the highest abstraction layer. Following the abstraction hierarchy, every inner layer concept derives from the abstract concepts of the upper neighboring layer. The last one is an exception, a self-defined, and thereby ends the abstraction hierarchy. The end-to-end connections of each layer instances of the encapsulated Single Helix, leading to the equivalent layer of another arbitrary Single Helix, build the communication network that enables design, management, verification, validation, and execution flows over the dynamic configuring paths.

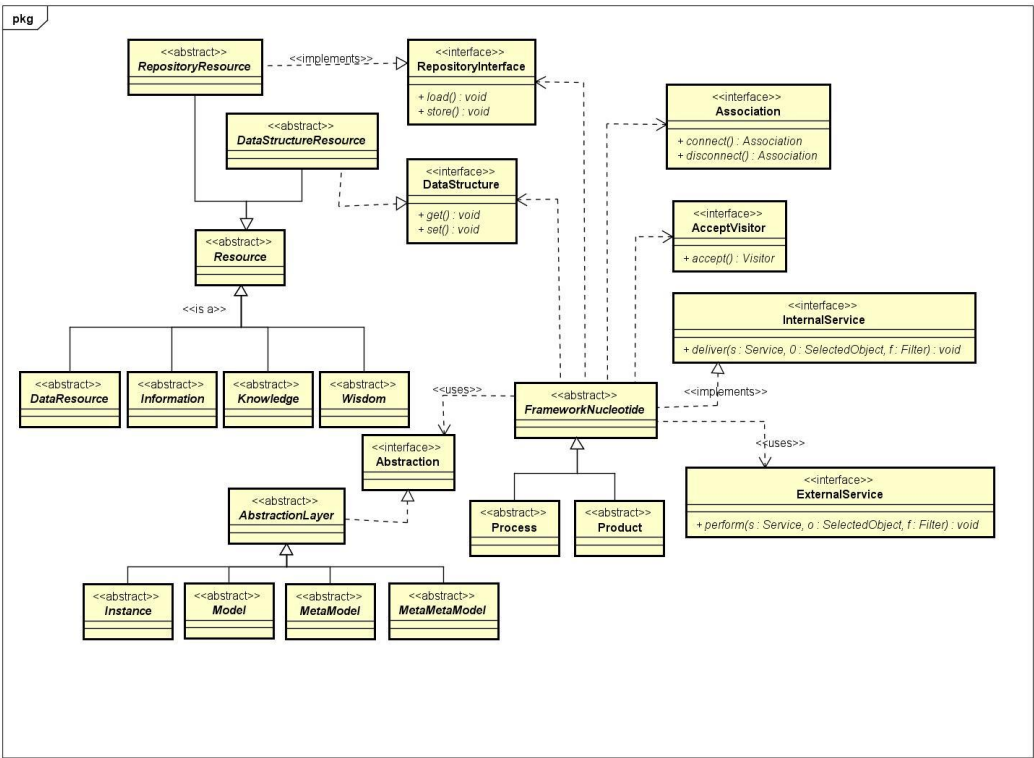
The Information Resource Abstraction concept specifies different resources that compose the essential part of DT architecture, the data. According to the MOF concept, with four abstraction

layers, with the Data Layer as the lowest and the Wisdom Layer as the highest abstraction level. The Information Resource Abstraction is a two-folded concept with persistent and dynamic sides. The persistent side abstracts storage and retrieval forms and mechanisms, while the dynamic side abstracts run-time accessible data structure representations.



**Figure 22.** The Information Resource Abstractions End of a Framework Helix Wormhole.

Additionally, we define a Framework Nucleotide as an abstract, freely associable atomic building block template (capsule) with temporal (time) and modal (type) marking abilities (Figure 23).



**Figure 23.** Framework Nukleotide conceptual object model.

The Framework Nucleotide (FN) encapsulates internal characteristics with the interfacing mechanisms and enables configuring the Core Conceptual Framework Quintuple Helix architecture instances with time and topology dimensioning of one of the currently defined specializations Process and the Product. Considering Verification and Validation as FN specializations embedded in the process and product assets, it is essential to supply the multilayered connectivity mechanisms

supporting the multipath traversals and traceability through the navigation space of associatively connected model abstractions (instance, model, meta-model, and meta-metamodel), dynamic and persistent information resource instances (data, information, knowledge, and wisdom), and externally or internally orchestrated services.

The FN specifies seven interfaces:

- Abstraction Interface - that bridges the modeling abstraction layers (Instance, Model, Meta-model, and Meta-meta-model) ;
- Data Structure Interface - that bridges the Data Structure Resource, a complex abstract concept encapsulating dynamic Resource collection representing Data, Information, Knowledge, or Wisdom abstractions;
- Repository Interface - that bridges the Repository Resource, a complex abstract concept encapsulating persistent Resource collection representing Data, Information, Knowledge, or Wisdom abstractions;
- Association Interface - that encapsulates the connectivity mechanisms (connect and disconnect services);
- Repository Interface - that bridges the Repository Resource, a complex abstract concept encapsulating persistent Resource collection representing Data, Information, Knowledge, or Wisdom abstractions;
- Association Interface - that encapsulates the connectivity mechanisms (connect and disconnect services);
- Accept Visitor Interface - that enables the hosting of external, visiting, set of services attached to the Framework Nucleotide Instance;
- Internal Service Interface - that enables the formation of an extendible set of internally implemented services, accessible through referencing the universal abstract method implemented by an arbitrary implementer *deliver*(s: Service, o: SelectedObject, f: Filter). Semantically, run a service (s: Service) on a selected object (o: SelectedObject) and restrict the delivery with security and privacy policy-based dynamic filtering (f: Filter); and
- External Service Interface - that enables access to externally offered services by referencing the universal abstract method implemented by an arbitrary external implementer *to perform*(s: Service, o: SelectedObject, f: Filter). Semantically, execute external service (s: Service) on the selected object (o: SelectedObject) and restrict the execution by the security and privacy policy-based dynamic filtering (f: Filter).

### 3.3. Quintuple Helix Conceptual Framework for DT Verification and Validation Spots

The transfer of control between participating objects in Model-Based-System-Engineering phases, mapped to the corresponding Digital Twins and supported referent resource objects that foster the interactions, relays on the Verification (red) and the Validation (black) spots embedding in the proposed conceptual framework behavior modeled as activity diagrams (Figures 24 and 25).

The behavioral model contains six vertical partitions, split into Figures 24 and 25, that correspond to the course grained phases in Model-Based-Systems-Engineering paradigm (Concept, Primary Design, Detailed Design, Implementation, Test and Evaluation, and deployed Operation and Maintenance), and three horizontal partitions that correspond to MBSE Outputs, mapping partition, and Digital Twin Development partition. The Verification spots, marked with a red diamond, define the points of control at which the embedded verification mechanism triggers. The Validation spots, marked with a black diamond, define the points of control at which the embedded validation mechanism triggers. The inter-phases exchange objects represent resources that accompany the horizontal transfer of control between MBSE main phases. These resources serve as a foundation for feeding the Mapping to DT activity zone and guiding DT Development activity zone.



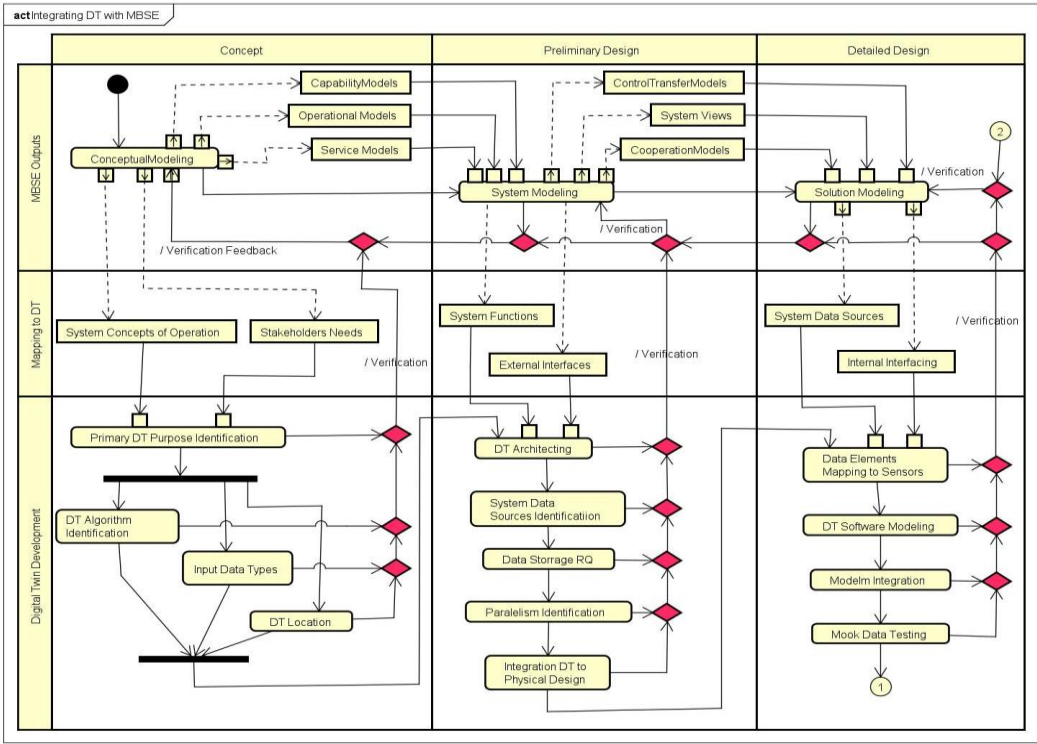


Figure 24. Integrated DT with MBSE with Verification Feedback Spots (Modified from [11]).

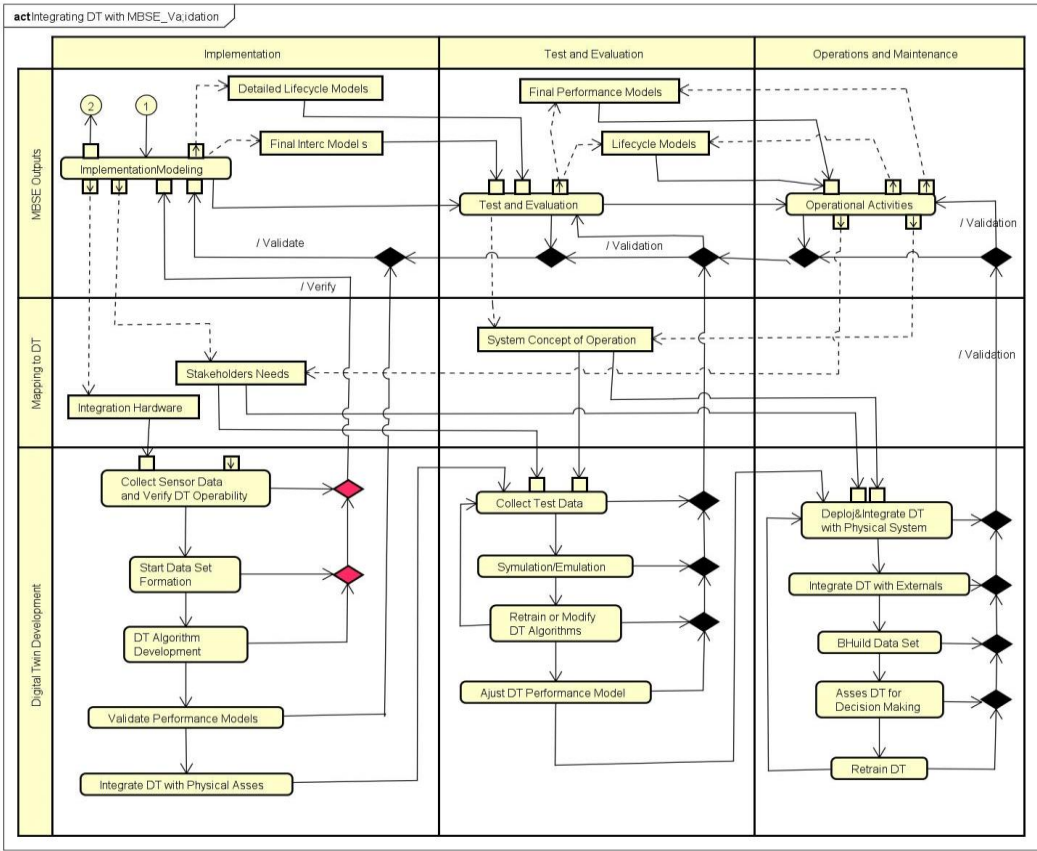


Figure 25. DT with MBSE with Verification and Validation Feedback Spots (Modified from [11]).

3.4. Quintuple Helix Conceptual Framework Mediation

We have nominated the extendibility as a mandatory capability of the specified conceptual framework. Due to the inherent complexity of individual conception framework configuration instances, hiding the resulting complexity is a must. The universal conceptual model of the mediation mechanism enables the complexity hiding while connecting the Actual System (AS) and the related DT Element instances (Figure 26).

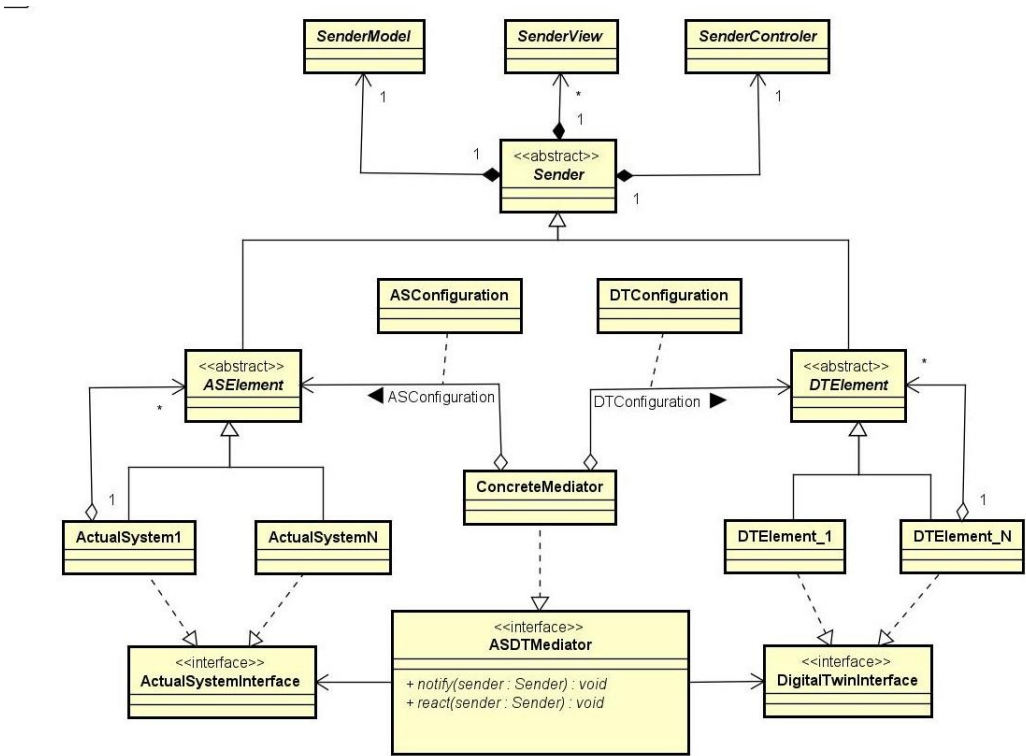


Figure 26. The Conceptual Framework Bridge Mediator.

The proposed conceptual framework establishes multilayered and multidimensional architecture with bridging mechanisms that support virtually unlimited extendibility. It creatively combines different challenging features and builds the foundation for further research that will need deeper diving into each of the presented dimensions. With the embedded mechanisms, its architecture converges to a collaborative hyper-framework, the interoperable configuration of different frameworks (a framework-of-frameworks-(FoF)).

All of the elaborated concept models relate to the essential group of requirements and justify the proposed approach. The rest of the specified requirements are an open challenge for further critical analysis and creative development activities.

#### 4. Discussion

Establishing a sustainable and trustworthy comparative analysis of independently developed creative solutions is a demanding and usually "rotten" problem. We consider the problem rotten if it may be correctly solved, if and only if it has been previously incorrectly solved at least once. Selecting relevant research topics is probably the most demanding step toward the valuable discussion. With current scientific and technical production, the composition of search criteria, and the rationality of article namespace and keywords, it is possible to waste energy and time with relatively low benefits.

The other obvious obstacle was a different sense of a word framework found in particular research instances explicitly mentioning framework as a keyword. The inflation of frameworks tends to convert them into buzzwords and ruins the importance of framework-based architecting. Through the introductory and materials and methods sections, we have selected a group of references and formed the union of addressed features. We ended up with 25 extracted features and used them for



F06	○	●	○	○	○	○	○	○	○	○	○	○	○	●	○	○
F07	○	○	○	○	○	○	○	○	○	○	●	○	○	○	○	○
F08	●	●	○	○	○	○	○	●	○	○	○	○	○	●	○	○
F09	○	○	○	○	○	○	●	○	○	○	○	●	●	●	○	●
F10	○	○	○	○	○	○	○	○	○	●	○	○	○	○	○	●
F11	○	○	○	○	○	○	●	●	●	●	○	○	○	○	●	○
F12	○	○	●	○	●	●	○	○	○	○	○	○	○	○	●	○
F13	○	○	●	○	○	○	○	○	●	○	○	○	○	○	○	●
F14	○	○	●	○	●	○	○	○	●	○	○	○	○	○	●	●
F15	○	○	○	○	●	○	○	○	○	○	○	○	○	○	○	●
F16	○	○	●	○	●	○	○	○	○	○	○	○	○	○	○	●
F17	○	○	○	○	○	○	○	○	○	○	○	○	○	○	○	●
F18	○	○	○	○	○	○	○	○	○	○	○	○	○	○	○	●
F19	○	○	○	○	○	○	○	○	○	○	○	○	○	○	○	●
F20	●	●	○	○	○	○	○	○	○	○	○	○	○	○	○	●
F21	○	○	○	○	○	○	○	○	●	○	○	○	○	○	○	●
F22	○	○	○	○	○	○	○	○	○	●	○	○	○	○	●	●
F23	○	○	○	○	○	○	○	○	○	○	○	○	○	○	●	●
F24	○	○	○	○	○	○	○	○	○	○	○	○	○	○	○	●
F25	○	○	○	○	○	○	○	○	○	○	○	○	○	○	○	●
25	2	3	4	1	5	5	5	5	5	5	3	3	3	7	4	19

Figure 27 visualizes the absolute possible envelope (the Absolute rate), the individual coverage (Reference Covers), and the individual Gap of the compared frameworks.

One of the open challenges for further research is the formation of a representative dataset with an extendible classification mechanism that would enable the application of machine-learning mechanisms and Large Language Models to gradually refine framework-related publications concerning model-based-engineering of complex cyber-physical and socio-technical systems and thereby enhance the fidelity and relevance of future comparisons.

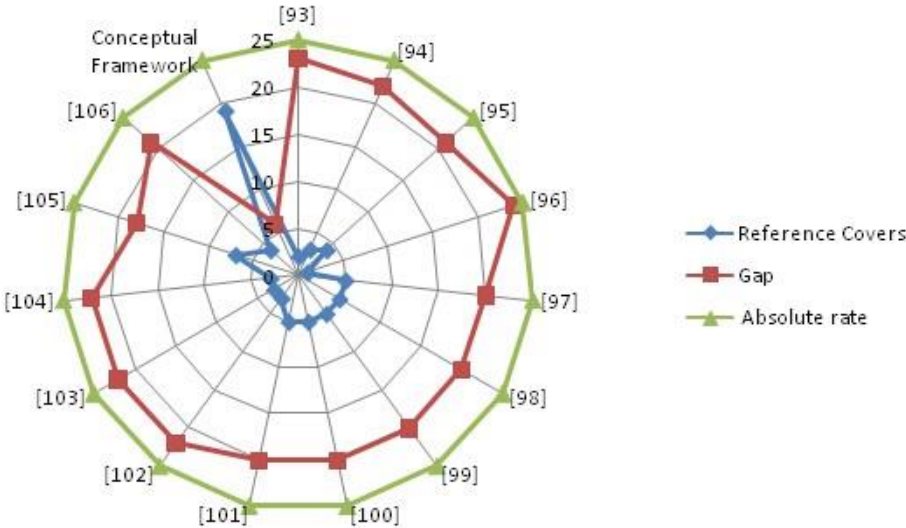


Figure 27. Absolute and relative feature coverage (Table 3).

The proposed conceptual framework is only one of the milestones that marks the future research directions. The conceptualization and abstraction levels demand further refinements to fully transform from the conceptual framework to the collection of related conceptual models, with enough details to support the transformation into extendible integrated development that enables the creation and tailoring of arbitrary framework instances in virtually unlimited number of configurations with embedded verification and validation and digital twinning support.



We find each formulated requirement (Table 1) as a challenging component and designate it as a domain framework. The proposed concepts trace the road to the framework-of-frameworks architecting.

## 5. Conclusions

A lack of frameworks integrating the DT Design, DT Verification, DT Validation, and DT Operation in currently published scientific and engineering research is the essential motivation factor for this article's launching. We argue that Verification and Validation are not isolated steps in the DT Design and Operation stages, similar to testing in software development. When integrated into design and operational activities, they form a mental discipline that ensures the lowest possible risk level for utilizing an engineered system.

With that in mind, we have defined five pillars of the proposed conceptual framework specification:

- the Digital Twin Consortium's Digital Twin Ecosystem Capabilities Periodic Table, containing a systematic collection of referent capabilities and the associated semantics;
- the generative potentials of the DNA helix model with the built-in combinatorial complexity replicating within two back-bones coupled by four-dimensional nucleotides;
- the unified conceptualization approach to reasoning about framework entities and stages that relays on applied MOF model to abstracting framework resources;
- *the standards and standardization support extendibility; and*
- Bridging of the abstract specification and the diverse repertoire of implementation platforms favoring the heterogeneity and harmonization of specification, development, modeling, implementation, and execution platforms involved.

The proposed framework combines the Quintuple Helix model with the Problem and Operational Domains of a Real (Actual) Twin, the Solution and Implementation Domains of a Virtual Twin, and the Execution Domain as the bridge that links them. Verification and Validation dimensions follow the Meta Object Facility abstraction layers (Instance, Model, Meta-model, and Meta-meta-model) mapping over five Helices. Embedding the complexity reduction mechanisms in the proposed framework builds a suite for extendible and verifiable digital twinning in simulation and real-time scenarios.

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