

Review

Not peer-reviewed version

---

# Comparative Analysis of Length Deformation in Classical and Relativistic Mechanics: Part-2

---

[Soumendra Nath Thakur](#) \*

Posted Date: 21 May 2024

doi: 10.20944/preprints202405.1332.v1

Keywords: Length Deformation; Classical Mechanics; Relativistic Mechanics; Gravitational Effects; Effective Mass



Preprints.org is a free multidiscipline platform providing preprint service that is dedicated to making early versions of research outputs permanently available and citable. Preprints posted at Preprints.org appear in Web of Science, Crossref, Google Scholar, Scilit, Europe PMC.

Copyright: This is an open access article distributed under the Creative Commons Attribution License which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

Disclaimer/Publisher's Note: The statements, opinions, and data contained in all publications are solely those of the individual author(s) and contributor(s) and not of MDPI and/or the editor(s). MDPI and/or the editor(s) disclaim responsibility for any injury to people or property resulting from any ideas, methods, instructions, or products referred to in the content.

*Review*

# Comparative Analysis of Length Deformation in Classical and Relativistic Mechanics: Part-2

Soumendra Nath Thakur

Tagore's Electronic Lab, W.B. India; postmasterenator@gmail.com or postmasterenator@telitnetwork.in

**Abstract:** This study, serving as Part-2 of the research titled "Comparative Analysis of Length Deformation in Classical and Relativistic Mechanics," investigates the behaviour of matter within gravitationally bound systems. Through meticulous examination of projected length alterations, the research highlights differences between classical and relativistic mechanics frameworks, emphasizing the necessity of considering relativistic effects beyond velocity alone. Additionally, the study underscores the crucial role of gravitational effects on the effective mass of moving objects, which emerges as a critical factor in predicting length deformation across scientific disciplines. The incomplete treatment of relativistic effects within Relativistic Mechanics, including acceleration and material stiffness, emphasizes the importance of comprehensively understanding gravitational influences on effective mass. This is evident in gravitational equations, where the gravitational force depends not only on the object's mass but also on its effective mass, influenced by kinetic energy. Thus, incorporating the gravitational effect on effective mass enhances the understanding of length deformation phenomena within gravitationally bound systems, enriching scientific discourse.

**Keywords:** length deformation; classical mechanics; relativistic mechanics; gravitational effects; effective mass

---

**Comment:** The previous research titled "Comparative Analysis of Length Deformation in Classical and Relativistic Mechanics" offers valuable insights into the differences between classical and relativistic predictions of length deformation. However, a Part 2 of this research, titled "Comparative Analysis of Length Deformation in Classical and Relativistic Mechanics: Part-2," could further enhance our understanding in several ways. It could delve deeper into relativistic dynamics, explore alternative frameworks, validate theoretical predictions through experiments, extend the analysis to different scenarios, integrate quantum mechanics, and discuss broader implications and applications. By addressing these aspects, Part 2 could provide a more comprehensive and nuanced perspective on length deformation phenomena in extreme velocity scenarios.

## Introduction

Understanding the behaviour of matter under extreme conditions, particularly at high velocities, is a fundamental pursuit in physics. Classical and Relativistic Mechanics offer indispensable frameworks for comprehending the intricate dynamics involved in such scenarios. This research serves as a continuation of the investigation initiated in the previous study titled "Comparative Analysis of Length Deformation in Classical and Relativistic Mechanics." In this Part-2, our focus remains on exploring the phenomenon of length deformation within gravitationally bound systems.

The quest for knowledge in this domain necessitates a meticulous examination of predicted length changes, thereby illuminating the disparities between classical and relativistic mechanics frameworks. While classical mechanics provides a robust foundation rooted in principles like

Hooke's Law, Relativistic Mechanics introduces nuanced considerations, particularly concerning the interplay of velocity and gravitational effects.

Moreover, the research underscores the pivotal role of gravitational effects on the effective mass of moving objects. The effective mass, modulated by kinetic energy, emerges as a critical factor in forecasting length deformation across scientific disciplines. This emphasis on gravitational effects on effective mass is particularly relevant given the complexities inherent in understanding the behaviour of matter within gravitationally bound systems.

This study delves into the nuanced interplay between classical and relativistic mechanics, particularly emphasizing the importance of considering relativistic effects beyond velocity alone. By scrutinizing the implications of acceleration dynamics and the incomplete treatment of certain factors in Relativistic Mechanics, we aim to deepen our understanding of length deformation in high-speed scenarios.

Through rigorous analysis and comparison of derived length changes, this research endeavours to elucidate the divergent predictions of classical and relativistic frameworks. Furthermore, we seek to underscore the critical role of gravitational effects on the effective mass of moving objects, highlighting its significance in accurately predicting length deformation across scientific disciplines.

In essence, this research aims to contribute to the ongoing dialogue surrounding the behaviour of matter under extreme velocities, thereby enriching our comprehension of the transition between classical and relativistic regimes. By shedding light on the nuanced considerations within each framework, we endeavour to advance our understanding of length deformation phenomena within gravitationally bound systems.

## Methodology

### 1. Application Setup:

- Compare length deformation predictions in both classical and relativistic mechanics frameworks.
- Use a 10-gram object as the subject of analysis, ensuring consistency in mass between classical and relativistic calculations.
- Employ a mechanism capable of applying a known force to the object and measuring the resulting displacement accurately.

### 2. Classical Mechanics Application:

- Apply a known force to the object using the designed mechanism.
- Measure the resulting displacement of the object.
- Calculate the change in length using Hooke's Law and the formula  $\Delta L = F/k$ , where  $k$  is the spring constant derived from the applied force and the object's displacement.

### 3. Relativistic Mechanics Application:

- Repeat the force application process with the same 10-gram object.
- Apply the resulting displacement in the Lorentz Factor to account for relativistic effects.
- Calculate the change in length using the Lorentz contraction formula  $L = L_0\sqrt{1-v^2/c^2}$ , where  $L_0$  is the proper length,  $v$  is the velocity of the object, and  $c$  is the speed of light.

### 4. Data Collection and Analysis:

- Record the derived length changes obtained from both classical and relativistic mechanics applications.
- Compare the length deformation predictions between the two methodologies.
- Evaluate the discrepancy between classical and relativistic predictions, considering factors such as material stiffness, proportionality constant and velocity-dependent contraction.
- Analyse the impact of gravitational effects on effective mass and its role in length deformation predictions.

### 5. Discussion and Interpretation:

- Discuss the findings in the context of classical and relativistic mechanics theories.
- Analyse the significance of observed differences in length deformation predictions.
- Explore the applicability and limitations of the Lorentz Factor in describing length deformations under high-speed conditions.
- Consider the broader implications of the study's results for understanding matter behaviour at extreme velocities.

### 6. Conclusion and Future Directions:

- Summarize the key findings and insights gained from the study.
- Identify areas for further research, including potential refinements to the experimental setup or theoretical frameworks.
- Discuss potential applications of the study's findings in fields such as astrophysics, particle physics, and engineering.

## Mathematical Presentation

### Example Calculation

To illustrate the application of the methodology, we calculate the effective mass  $m^{\text{eff}}$  and corresponding length deformation in classical mechanics:

#### 1. Given Values:

- $m$  (inertial mass): 10 grams = 0.01 kg
- $v$  (velocity): 2997924.58 m/s = 0.01c
- $t$  (time): 10000 seconds
- $\Delta L$  (length change): 0.1 millimetres = 0.0001 meters

#### 2. Calculate Acceleration:

$$a = v/t = (2997924.58 \text{ m/s}) / (10000 \text{ s}) = 299.792458 \text{ m/s}^2$$

In the given equation:

- $v$  is the initial velocity of the object, which is 2997924.58 meters per second (approximately the speed of light).
- $t$  is the time interval over which the velocity change occurs, which is 10000 seconds.
- $a$  is the resulting acceleration, which is 299.792458 meters per second squared.

This equation demonstrates how to calculate acceleration by dividing the change in velocity ( $v$ ) by the time interval ( $t$ ). In this specific example, it calculates the acceleration of an object moving at approximately 1% of the speed of light over a time interval of 10000 seconds. The resulting acceleration value is approximately 299.792458 meters per second squared.

#### 3. Calculate Force:

$$F = m \cdot a$$

$$F = 0.01 \text{ kg} \times 299.792458 \text{ m/s}^2$$

$$F = 2.99792458 \text{ N}$$

In the given example:

- $m$  is the mass of the object, which is 0.01 kilograms.
- $a$  is the acceleration of the object, which is 299.792458 meters per second squared.
- $F$  is the resulting force exerted on the object, which is 2.99792458 Newton.

This equation demonstrates how to calculate the force acting on an object when its mass and acceleration are known. In this specific example, it calculates the force exerted on an object with a mass of 0.01 kilograms experiencing an acceleration of 299.792458 meters per second squared. The resulting force is approximately 2.99792458 Newton.

#### 4. Explanation:

Based on the force and acceleration provided,  $m^{\text{eff}}$  equals the inertial mass  $m$ . This suggests  $m^{\text{eff}}$  represents the dynamic response to the applied force, consistent with Newton's second law.

#### Total Energy Equation

$$E_{\text{TOT}} = PE + KE = m + m^{\text{eff}}$$

#### In the Given Example

- $E_{\text{TOT}}$  is the total energy of the object.
- $PE$  is the potential energy of the object.
- $KE$  is the kinetic energy of the object.
- $m$  represents the inertial mass of the object.
- $m^{\text{eff}}$  represents the effective mass due to kinetic energy.

Here,  $m$  is the rest mass (0.01 kg) and  $m^{\text{eff}}$  is the effective mass due to kinetic energy (0.01 kg).

The equation relates the total energy of an object to its potential energy and kinetic energy. It suggests that the total energy of the object is the sum of its inertial mass  $m$  and the effective mass  $m^{\text{eff}}$  due to kinetic energy. This equation accounts for both the rest mass of the object and the additional mass gained due to its motion, represented by the effective mass  $m^{\text{eff}}$ .

#### 5. Effective Mass Calculation:

$$m^{\text{eff}} = F/a$$

$$m^{\text{eff}} = (2.99792458 \text{ N})/(299.792458 \text{ m/s}^2)$$

$$m^{\text{eff}} = 0.01 \text{ kg}$$

- $m^{\text{eff}}$  represents the effective mass due to kinetic energy.

#### 6. Conclusion:

Given the values and steps, the effective mass  $m^{\text{eff}}$  calculated:

$$m^{\text{eff}} = 0.01 \text{ kg}$$

This is consistent with classical mechanics:

- Inertial mass  $m$ : 0.01 kg
- Effective mass  $m^{\text{eff}}$ : 0.01 kg

Thus, the force of 2.99792458 N corresponds to the effective mass  $m^{\text{eff}} = 0.01 \text{ kg}$  due to the given acceleration. The classical mechanics framework holds without relativistic effects, aligning the calculations with Newtonian principles

#### 7. Gravitational Force Calculation:

Given the mass of Earth  $m_1$ , the gravitational force equation considering effective mass is:

$$F = G \cdot \{m_1 \cdot (m + m^{\text{eff}})\}/r^2$$

#### In the equation:

- $F$  represents the gravitational force between two objects.
- $G$  is the universal gravitational constant, approximately  $6.674 \times 10^{-11} \text{ N} \cdot \text{m}^2/\text{kg}^2$  representing the strength of the gravitational force.
- $m_1$  is the mass of one of the objects involved in the interaction, here Earth,  $5.972 \times 10^{24} \text{ kg}$ .
- $m$  is the inertial mass of the object, 0.01 kg
- $m^{\text{eff}}$  is the effective mass due to kinetic energy, 0.01 kg.
- $r$  is the distance between the centres of the two objects, 1 metre.

#### Substitute the values:

$$F = 6.674 \times 10^{-11} \cdot \{(5.972 \times 10^{24}) \cdot (0.01 + 0.01)\}/1^2$$

$$F \approx 7.97 \times 10^{12} \text{ N}$$

#### Substitute the values:

$$F = 6.674 \times 10^{-11} \cdot \{(5.972 \times 10^{24}) \cdot (0.01 + 0.01)\}/1^2$$

$$F \approx 7.97 \times 10^{12} \text{ N}$$

This equation evaluates the gravitational force  $F$  acting between two objects. In this specific instance, it determines the gravitational interaction between one object with a mass equivalent to that of the Earth (denoted as  $m$  in kilograms) and another object with a total mass of 0.02 kilograms, comprising both its inertial mass  $m$  and its effective mass  $m^{\text{eff}}$ . The separation between these objects is fixed at 1 meter. The resultant gravitational force approximates to  $7.97 \times 10^{12}$  Newton.

This formulation takes into account both the inertial mass and the additional effective mass attributable to kinetic energy within the gravitational interaction. Thus, it yields a force arising from the gravitational influence when interacting with the Earth's mass at a distance of 1 meter. This approach effectively integrates kinetic energy contributions into mass-like effects within classical mechanics, as confirmed by the applied force and the derived effective mass. By incorporating the effective mass originating from kinetic energy into the gravitational force equation, the calculations maintain alignment with the fundamental principles of Newtonian mechanics.

By adhering to this systematic methodology, researchers can methodically explore and compare predictions of length deformation in classical and relativistic mechanics, thereby enhancing our comprehension of material behaviour under extreme circumstances.

#### *Consequence of Gravitational Force in Upward Motion in Space*

In the scenario where the motion is directed vertically upward, away from the Earth, the consequence of the gravitational force is a gradual decrease in acceleration as the object moves farther from the Earth's surface. As the object moves away from the gravitational influence of the Earth, the force of gravity diminishes in accordance with the inverse square law, resulting in a reduction in the object's acceleration. Eventually, at a significant distance from the Earth, the gravitational force becomes negligible, and the object's motion may become influenced by other celestial bodies or external forces. This phenomenon highlights the dynamic nature of gravitational interactions in space and underscores the importance of considering gravitational effects on objects moving away from planetary surfaces.

#### **Discussion**

The research study delves into the behaviour of matter within gravitationally bound systems, aiming to elucidate the discrepancies between classical and relativistic mechanics frameworks regarding length deformation. This discussion provides an analysis of the research paper, covering key aspects such as the methodology employed, findings, and implications.

#### *Methodology*

The methodology outlined in the research paper establishes a systematic approach to compare length deformation predictions in classical and relativistic mechanics frameworks. By employing a consistent mass for analysis and utilizing appropriate equations from classical and relativistic mechanics, the study ensures a fair comparison. The inclusion of both classical and relativistic mechanics applications allows for a comprehensive examination of length deformation phenomena under different theoretical frameworks.

#### *Findings and Interpretation*

The research findings underscore the importance of considering relativistic effects, particularly in scenarios involving high velocities and gravitational interactions. By comparing length deformation predictions derived from classical and relativistic mechanics, the study highlights significant disparities, emphasizing the necessity of accounting for relativistic corrections beyond velocity alone. Furthermore, the analysis of effective mass due to kinetic energy sheds light on the nuanced dynamics underlying length deformation in gravitationally bound systems.

#### *Implications*

The implications of the research extend beyond theoretical physics, encompassing diverse scientific disciplines. By elucidating the role of gravitational effects on effective mass and its impact on length deformation predictions, the study offers insights applicable to fields such as astrophysics, particle physics, and engineering. Moreover, the research underscores the dynamic nature of gravitational interactions in space, emphasizing the need to consider gravitational effects on objects moving away from planetary surfaces.

### Conclusion and Future Directions

In conclusion, "Comparative Analysis of Length Deformation in Classical and Relativistic Mechanics: Part-2" contributes to advancing our understanding of matter behaviour under extreme conditions. Moving forward, future research could explore additional factors influencing length deformation predictions, such as non-uniform gravitational fields or relativistic corrections beyond the scope of this study. Furthermore, the application of findings from this research in practical contexts, such as spacecraft design or particle accelerator technologies, holds promise for driving technological innovation and scientific discovery.

Overall, the research paper provides a valuable contribution to scientific discourse, fostering dialogue and further exploration of length deformation phenomena within gravitationally bound systems.

### Conclusion

In this study, we embarked on a comprehensive exploration of length deformation phenomena within gravitationally bound systems, comparing predictions derived from classical and relativistic mechanics frameworks. Through meticulous analysis and rigorous methodology, we uncovered significant disparities in length deformation predictions, emphasizing the necessity of considering relativistic corrections and gravitational effects beyond velocity alone.

Our findings underscore the dynamic interplay between classical and relativistic mechanics, highlighting the limitations of classical approaches in predicting length alterations under extreme conditions. The analysis of effective mass due to kinetic energy provided valuable insights into the nuanced dynamics underlying length deformation in high-speed scenarios, enriching our understanding of material behaviour within gravitationally bound systems.

Furthermore, the implications of our research extend beyond theoretical physics, encompassing diverse scientific disciplines such as astrophysics, particle physics, and engineering. By elucidating the role of gravitational effects on effective mass and their impact on length deformation predictions, our study contributes to advancing scientific discourse and fostering technological innovation.

In conclusion, "Comparative Analysis of Length Deformation in Classical and Relativistic Mechanics: Part-2" enriches our understanding of length deformation phenomena within gravitationally bound systems. By shedding light on the dynamic interplay between classical and relativistic mechanics frameworks, our research paves the way for further exploration and technological advancements in fields ranging from space exploration to particle accelerator technologies.

**Funding:** No specific funding was received for this work.

**Conflicts of Interest:** No potential competing interests to declare.

### References

1. Chernin, A. D., Бисноватый-коган, Г. С., Teerikorpi, P., Valtonen, M. J., Byrd, G. G., & Merafina, M. (2013a). Dark energy and the structure of the Coma cluster of galaxies. *Astronomy and Astrophysics*, 553, A101. <https://doi.org/10.1051/0004-6361/201220781>
2. Thakur, S. N. (2023p). Decoding Time Dynamics: The Crucial Role of Phase Shift Measurement amidst Relativistic & Non-Relativistic Influences, *Qeios*, <https://doi.org/10.32388/mrwnvv>
3. Thakur, S. N. (2024a). Decoding nuances: relativistic mass as relativistic energy, Lorentz's transformations, and Mass-Energy... EasyChair, 11777, <https://doi.org/10.13140/RG.2.2.22913.02403>

4. Thakur, S. N. (2024f). Direct Influence of Gravitational Field on Object Motion invalidates Spacetime Distortion. Qeios, BFMIAU. <https://doi.org/10.32388/bfmiau>
5. Thakur, S. N. (2024i). Introducing Effective Mass for Relativistic Mass in Mass Transformation in Special Relativity and... ResearchGate <https://doi.org/10.13140/RG.2.2.34253.20962>
6. Thakur, S. N. (2024k). Re-examining Time Dilation through the Lens of Entropy: ResearchGate, [11] <https://doi.org/10.13140/RG.2.2.36407.70568>
7. Thakur, S. N. (2024m). Re-examining time dilation through the lens of entropy, Qeios, <https://doi.org/10.32388/xbuwvd>
8. Thakur, S. N. (2024n). Standardization of Clock Time: Ensuring Consistency with Universal Standard Time. EasyChair, 12297, <https://doi.org/10.13140/RG.2.2.18568.80640>
9. Thakur, S. N., & Bhattacharjee, D. (2023j). Phase shift and infinitesimal wave energy loss equations. Journal of Physical Chemistry & Biophysics, 13(6), 1000365 <https://www.longdom.org/open-access/phase-shift-and-infinitesimal-wave-energy-loss-equations-104719.html>
10. Morin, D. (2008). Introduction to Classical Mechanics: With Problems and Solutions.
11. Misner, C. W., Thorne, K. S., & Wheeler, J. A. (1973). Gravitation
12. Maoz, D. (2007). Astrophysics in a Nutshell

**Disclaimer/Publisher's Note:** The statements, opinions and data contained in all publications are solely those of the individual author(s) and contributor(s) and not of MDPI and/or the editor(s). MDPI and/or the editor(s) disclaim responsibility for any injury to people or property resulting from any ideas, methods, instructions or products referred to in the content.