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## Article

# Characterization of Indium Tin Oxide (ITO) Thin Films Towards Terahertz (THz) Functional Device Applications

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**Abstract:** In this study, we explored the manipulation of optical properties in the terahertz (THz) frequency band of radio-frequency (RF) sputtered indium-tin-oxide (ITO) thin-films on highly resistive silicon substrate by rapid thermal annealing (RTA). The optical constants of as-deposited and RTA-processed ITO films annealed at 400°C, 600°C and 800°C are determined in the frequency range of 0.2 to 1.0 THz. The transmittance can be changed from ~27% for as-deposited to ~10% and ~39% for ITO films heat-treated at different annealing temperatures,  $T_a$ 's. Such variations of optical properties in the far infrared for the samples under study are correlated with their mobility and carrier concentration, which are extracted from Drude-Smith modeling of THz conductivity with plasma frequency, scattering time and the  $c$ -parameters as fitting parameters. Resistivities of the films are in the range of  $10^{-3}$  to  $10^{-4}$   $\Omega$ -cm, confirming that annealed ITO films can potentially be used as transparent conducting electrodes for photonic devices operating at THz frequencies. The highest mobility,  $\mu = 47$   $\text{cm}^2/\text{V}\cdot\text{s}$ , with carrier concentration,  $N_c = 1.31 \times 10^{21}$   $\text{cm}^{-3}$ , was observed for ITO films annealed at  $T_a = 600^\circ\text{C}$ . The scattering times of the samples were in the range of 8 – 21 fs, with  $c$ -values of -0.63 to -0.87, indicating strong back scattering of the carriers, mainly by grain boundaries in the polycrystalline film. To better understand the nature of these films, we have also characterized the surface morphology, microscopic structural properties and chemical composition of as-deposited and RTA-processed ITO thin-films. For comparison, we have summarized the optical properties of ITO films sputtered on fused silica substrates, as-deposited and RTA-annealed, in the visible transparency window of 400-800nm. The optical bandgaps of the ITO thin films were evaluated with a Tauc plot from the absorption spectra.

**Keywords:** Terahertz (THz); THz time-domain spectroscopy; Drude-Smith model; Sputtering; Rapid thermal annealing (RTA); Indium tin oxide (ITO); Transparent Conducting Oxide; Refractive indices; Conductivity; Optoelectronics (OE)

## 1. Introduction

Transparent conducting oxides (TCOs) [1–3] that exhibit good electrical conductivity and transparency in the desired wavelength range, are currently widely used for information display and energy-related products, e.g., solar cells, solid state lighting, multi-functional windows as well as sensors and thin film transistors. Among the TCOs, indium tin oxide or ITO, is perhaps the most commonly employed in commercial products and extensively studied. ITO is an n-type, degenerate wide band semiconductor that typically composed of indium oxide ( $\text{In}_2\text{O}_3$ ) with maneuverable valence states and oxygen vacancy defects in tin oxide ( $\text{SnO}_2$ ) [4–7]. It is highly transparent (up to 90%) in the visible window (400-700 nm), while its resistivity ( $< 200$   $\mu\Omega$  cm) is sufficiently low to serve as a conductive layer for biasing photonic devices [8–13].

To date, ITO thin films have been successfully deposited on various substrates using diverse growth technologies [3,14–19]. Among various deposition methods, magnetron sputtering is broadly used because of its ability to deposit large-area coatings rapidly with superior reproducibility while maintaining high uniformity at low processing temperature [20,21]. High-quality ITO thin films can be routinely fabricated by controlling sputtering parameters such as the working pressure, RF power,

oxygen partial pressure, and substrate temperature [22]. For example, Li *et al* [23] and Huang *et al* [24], studied ion behavior as the function of sputtering power for enhancing the properties of ITO thin films. Zhang *et al.* [25] showed that when the thickness was less than 130 nm, ITO films with a nominal  $\text{In}_2\text{O}_3/\text{SnO}_2$  ratio of 95/5 (wt.%) exhibited higher electrical conductivity compared to those with a commercially available target with an  $\text{In}_2\text{O}_3/\text{SnO}_2$  ratio of 90/10 (wt.%). Similar findings have also been reported by many groups [12,26]. In addition, numerous works have focused on improving the conductivity of ITO films and achieving preferential orientation in the [111] direction of ITO films by optimizing the substrate temperature during sputtering [27,28]. It is worth noting that, depending on the plasma mode used, either direct current (DC) or radio frequency (RF), the crystalline structure and morphology of fabricated ITO thin films change significantly due to differences in optimal deposition conditions such as RF power density, uncontrollable partial pressure in chamber, etc. [29]. The characteristics of ITO films are also significantly influenced by the chamber's base pressure, a key controllable parameter. For instance, Yang *et al.* [30] revealed that decreasing the base pressure led to increase in the carrier concentration, a decrease in resistivity, and an improvement in the figure of merit of ITO films. Meantime, Meng *et al.* [31] reported that increasing the base pressure altered the preferred orientation of the ITO thin film and significantly increased its roughness while maintaining the same deposition rate. Numerous groups have also studied the impact of varying partial pressure of the gas ambient in the chamber to attain the desired ITO properties on ITO films for different applications [32–36]. For example, Donercark *et al.* [37] recently demonstrated improvement on the overall efficiency of a solar cell by simply changing the oxygen partial pressure during the deposition of ITO films.

Post-deposition heat treatment or annealing is known to be an effective method to improve crystallinity and modify physical properties of ITO films [38–40]. Recent efforts have focused on tailoring the annealing parameters for specific applications. For instance, Shubitidze *et al.* [41] reported enhanced optical nonlinearity in ITO thin films with anisotropic crystallographic texturing, which further boosted the nonlinear refractive index modulation in ITO thin film when it is coupled to a silicon dioxide/silicon nitride ( $\text{SiO}_2/\text{SiN}$ ) multilayer structures. Kim *et al.* [42] employed microwave post-treatment to improve the optical and electrical properties of ITO thin film for solar cell applications.

Rapid thermal annealing (RTA) processes have been widely used to improve optical and electrical properties of as-deposited ITO thin films [43,44]. Furnace annealing [45] was widely used in earlier works. The treatment cycle including pre-heating time for furnace annealing is comparatively lengthy. It is also relatively difficult to control the temperature of the furnace precisely. There is also the problem of oxygen adsorption taking place. The other alternative being laser annealing [46], which is best used for local modification of materials. There is a wealth of previous works on RTA treatment of ITO thin films, opening avenues for various potential devices. For instance, Kim *et al.*, [47] reported a high-quality RTA-treated ITO films at an annealing temperature,  $T_a$  of 400°C and above, with a resistivity ( $\rho$ ) as low as  $3.3 \times 10^{-4} \Omega\text{-cm}$  and transmittance as high as 90% throughout the visible range (400 - 800 nm). In another work [48], a highly conductive RTA- processed ITO thin films ( $\rho = 7.4 \times 10^{-5} \Omega\text{-cm}$ ) was reported. While most RTA work on ITO were performed at relatively low temperatures ( $T_a \leq 300^\circ\text{C}$ ), Song *et al.* [49] did show that the ITO thin film annealed at the moderately high temperature of 600°C by RTA show improved electrical and optical properties.

RTA processing of the ITO thin film in a multilayer structure is also of current interests. For example, RTA-treated indium gallium zinc oxide (IGZO)/ITO multilayer TFTs, when compared to solely RTA-processed IGZO channels, exhibited a negative shift in threshold voltage, along with enhancements in on-to-off current ratio, subthreshold swing, and mobility. These improvements were facilitated by the elimination of donor-like defect states achieved through curing during the RTA process on the ITO electrode layer [50]. In another study by Maniyara *et al.* [51], an improvement in the insertion optical loss of the liquid crystal (LC) cell fabricated with RTA-treated ITO exhibit excellent near-infrared transparency beyond 1  $\mu\text{m}$ . Interestingly, RTA-treated heterojunctions composed of ITO/Silicon offered high photo-response by forming a rectifying junction at the interface of ITO and Silicon [52].

There are relatively few studies on the optoelectronic properties and applications of ITO films in the far-infrared or THz ( $1\text{ THz} = 1 \times 10^{12}\text{ Hz}$ ) frequency band. Hamberg and Granqvist [53] reported that e-beam-evaporated heavily-doped ITO exhibits nearly flat reflectance of  $\sim 90\%$  from  $10 - 50\text{ }\mu\text{m}$  ( $30 - 6\text{ THz}$ ) for nearly-normal-incident p-polarized light. Appropriate dielectric functions for the far infrared were proposed. Uprety et al. [54] have reported complex dielectric function from *ex situ* spectroscopic ellipsometry data collected over  $0.4$  to  $4.1\text{ meV}$  ( $\sim 0.1$  to  $\sim 1\text{ THz}$ ). Using THz time-domain spectroscopy (THz-TDS), we have investigated the THz optical constants of DC-sputtered ITO films, ITO nanorods and nanowhiskers deposited by glancing angle electron-beam evaporation (GLAD) up to  $4\text{ THz}$  [55–59]. Wang et al. [60] reported terahertz conductivity of highly doped pulse-laser-deposited ZnO and ITO from  $0.5$  to  $18\text{ THz}$ , with data on ITO essentially in agreement with those reported in our works. Branched ITO nanowire network was also investigated by LaForge et al. [61], who showed that the conductivity of the ITO nanostructures can be controlled by the deposition flux rate. On the application side, Bauer et al. [62] showed that ITO-coated glass can be used as dichroic mirrors for far-infrared radiation, Jewell et al. [64] constructed a tunable Fabry-Perot etalon by sandwiching liquid crystal between ITO-coated glasses. Tsubouchi and Kumada [65] built an etalon with ITO as an out coupler to convert a single THz pulse into a pulse train with comb-like spectrum. While ITO film typically exhibits relatively high reflectivity in the THz band, transmittance of ITO nanostructures can be as high as  $90\%$  with low resistivity in the THz band. Our group successfully employed ITO nanostructures as transparent conductive electrodes in liquid-crystal-based THz shifters [66,67]. Alternatively, a wire-grid style, i.e., interdigital ITO electrodes can enhance the transmittance of ITO electrodes from  $40\%$  to  $> 85\%$ , more than adequate for device applications such as spatial light modulators [68,69]. A metamaterial-based THz “perfect absorber” was fabricated, using ITO to replace the conventional back plane [70]. The absorption bandwidth was  $3.20\text{ THz}$ , from  $2.30$  to  $5.50\text{ THz}$ , where the absorption is greater than  $50\%$ . In a related work, Liu et al. [71] demonstrated resonance enhancement of terahertz metamaterials by liquid crystals/indium tin oxide interfaces. Operating at somewhat lower frequencies, Bai et al. [72] proposed a microwave metamaterial absorber composed of conductive ITO thin films and transparent polymethyl methacrylate (PMMA) substrate layers. Moreover, we have demonstrated the enhancement of optically excited THz wave emission from a thick layer of ITO thin film coated on semi-insulating gallium arsenide (SI-GaAs) substrate at THz frequencies [73]. Meanwhile, Lu et al. [74] proposed and demonstrated the full-scope of functionality of the ultrathin ITO thin film as an innovative platform for generating broadband THz waves. Surprisingly, there are few works investigating annealing as a means to tune ITO optical and electrical properties for THz applications, except for Shi et al. [70], who studied furnace-annealed ITO films. A preliminary study on improvement in THz transmittance of RTA-treated ITO thin films were conducted by the authors, as reported in a conference paper [75].

In this paper, we report THz optical constants of as-deposited and RTA-processed ITO thin films at annealing temperatures of  $400^\circ\text{C}$ ,  $600^\circ\text{C}$  and  $800^\circ\text{C}$  using transmission-type THz time-domain spectroscopy (THz-TDS). The Drude-Smith model is used to fit experimental THz data and extract electrical parameters such as dc conductivity, carrier concentration and mobility of the samples. The structure, composition and morphology of as-deposited and annealed ITO films were characterized to understand their observed THz optical properties. Furthermore, we have determined the optical constants of these ITO thin films in the visible (VIS)-near infrared (NIR) light range, determining their optical bandgaps as well. This paper shows that post-annealing is an effective method for tuning THz optical properties of ITO and lay the foundation for next-generation THz photonic devices employing ITO as transparent conductive material in the far infrared. Our data also sheds light on visible optical properties of ITO thin films annealed at relatively high temperatures, an area with limited existing research.

## 2. Materials and Methods

We selected highly-resistive (HR), two-side polished silicon (intrinsic, thickness  $\sim 350 \pm 25\text{ }\mu\text{m}$ , resistivity  $> 10,000\text{ }\Omega\text{-cm}$ ) as substrates to study THz optical properties of the ITO thin films. Fused silica sheets (thickness  $\sim 800 \pm 25\text{ }\mu\text{m}$ ) were employed as substrates to study optical properties of the



ITO thin films in the so-called visible transparency window (400-800 nm). Prior to deposition, the substrates were subjected to a rigorous cleaning procedure involving sequential immersion in acetone, isopropyl alcohol and de-ionized water in an ultrasonic cleaner, followed by baking and cooling.

The deposition of ITO thin films was carried out using a radio frequency magnetron sputtering machine (RF Sputter, ULVAC RFS-200S). A 4-inch diameter ITO target with composition of indium oxide/tin oxide ( $\text{In}_2\text{O}_3/\text{SnO}_2$ ) of 90/10 wt. % was employed for this study. The pre-deposition vacuum pressure was  $5.2 \times 10^{-6}$  torr. During deposition, argon (flow rate  $\sim 50$  SCCM) was introduced into the deposition chamber that was maintained at the vacuum pressure of  $5 \times 10^{-5}$  Torr. The RF power of 60 W was kept constant during pre-deposition (for 6 minutes) and deposition (for 20 minutes). The substrate holder was not intentionally heated. Yet, we note that the temperature of the deposition chamber varied from 20°C to 45°C presumably due to RF heating and bombardment of sputtering molecules during the deposition process. The chamber was vented only after it returned to room temperature.

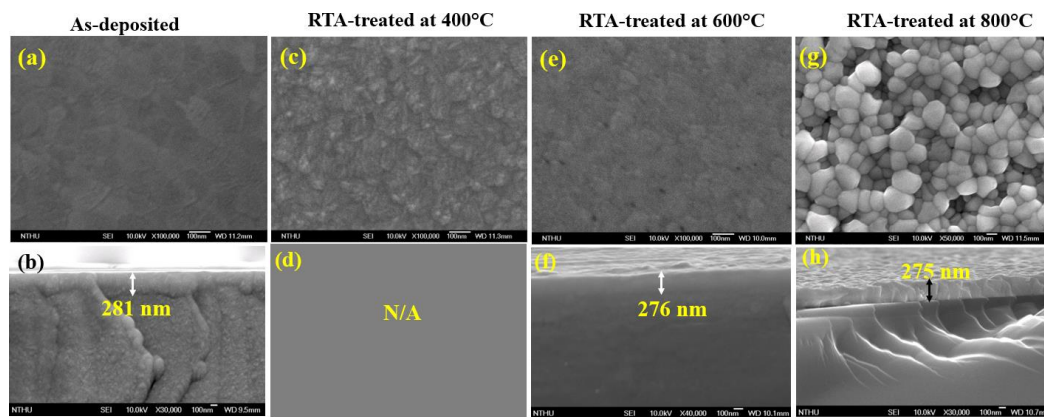
Subsequently, rapid thermal annealing (Premtex RTP-S61-M) were performed on the films at 400°C, 600°C and 800°C for 90 seconds in a nitrogen ambient (flow rate  $\sim 33$  SCCM). The as-deposited and RTA-treated samples were analyzed by a homemade photoconductive-antenna-based THz-TDS system [76,77]. Additionally, their structural and morphological properties were investigated by using atomic force microscopy (AFM, SEIKO SPA-300HV) and field emission scanning electron microscope (FESEM, JSM-7000F, Japan Electron Optics Laboratory Co., Ltd.). The composition of as-deposited and RTA treated ITO thin films was evaluated using energy-dispersive X-ray spectroscopy (EDS). Furthermore, transmittance and reflection spectra of the ITO thin films were obtained using an (UV-VIS-NIR) spectrometer (Hitachi U-4100), with operating wavelength range of (200-2000nm).

### 3. Results and Discussion

This section is organized as follows. First, Subsection 3.1 summarizes the structure, surface morphology and composition of samples under study. Next, we show the THz-TDS data and extract the THz optical constants and the transmission and reflective characteristics of the samples in the THz band. Both the Drude and the Drude-Smith model is used to analyze THz conductivity of as-deposited and annealed ITO films in Subsection 3.2. The latter was found to provide a better fit of the data. Finally, we report the UV-VIS-NIR optical properties of as-deposited and annealed ITO films that were deposited on fused silica, in the Subsection 3.3.

#### 3.1. Structure, Surface Morphology and Composition

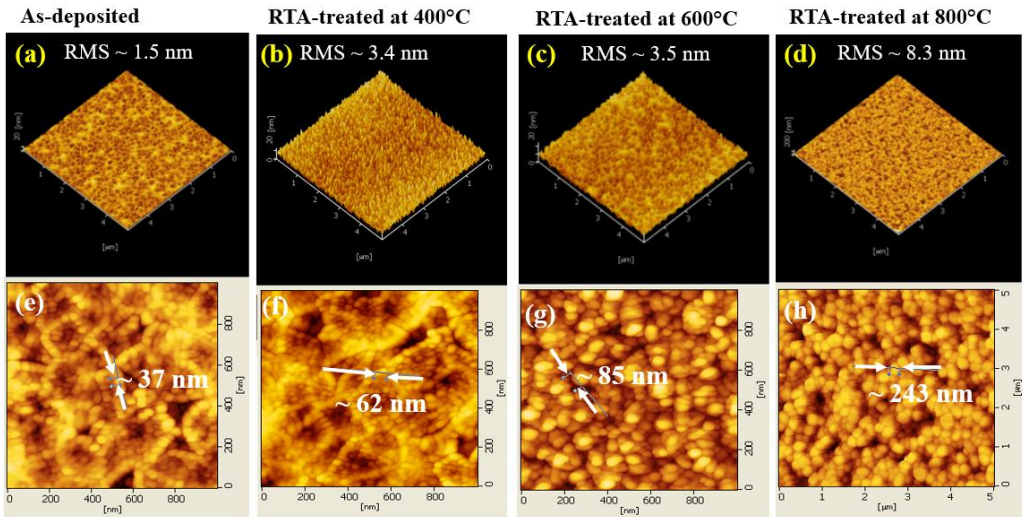
In Figure 1a, we present the SEM image of the top view of the as-deposited ITO thin film, revealing a smooth surface morphology. Previously, Franz et al. [78] showed that their  $\sim 300$  nm-thick RF-sputtered ITO films exhibited similar topology to ours, with no apparent grain growth. By enlarging the film thickness to  $\sim 30,000$  nm, these workers found the film composed of the typical columnar structure with a mean diameter of 140nm. Working backwards by modeling the columns as tapers with the acute point on the substrate, the diameter of the grains at the surface of  $\sim 300$  nm-thick ITO film was estimated to be between 10-25 nm, as confirmed by independent focused ion beam studies. Using a deposition system and parameters like we employed, Yüzüak & Coşkun [79] reported topology of as-deposited ITO films that resembles that of ours (Figure 1a). Their X-ray diffraction studies show that the as-deposited film is amorphous. Therefore, we hypothesized that our as-deposited ITO film is either amorphous or consists of nanocrystals with dimensions of this order.



**Figure 1.** The SEM images of as-deposited ITO thin film with (a) top-view (b) cross-sectional view, ITO thin film with RTA-treated at 400°C with (c) top-view (d) cross-sectional view (N/A), ITO thin film with RTA-treated at 600°C with (e) top-view (f) cross-sectional view, and RTA-treated at 800°C with (g) top and (h) cross-sectional view.

Figures 1c and 1e illustrate the surface morphology of the ITO thin films processed by RTA at 400°C and 600°C, respectively. The two are quite similar and yet clearly distinguishable from that of the as-deposited film. Notably, a remarkable change in surface morphology of the ITO thin film treated with RTA at 800°C occurred, as depicted in Figure 1g, where prominent but non-uniform particles are evident. From image analysis of the SEM pictures (ImageJ, University of Wisconsin-Madison, USA), we estimate that the average areas of grains are 80 nm<sup>2</sup>, 175 nm<sup>2</sup> and 694 nm<sup>2</sup> for those annealed at 400°C, 600°C and 800°C, respectively. The corresponding lateral grain sizes are 5 nm, 7.5 nm and 15.8 nm. The results indicate a significant increase in grain sizes of the ITO thin films as the RTA temperature increases from 400 to 800°C, a phenomenon also observed in the work of Maniyara et al [51], who studied RTA of ITO films at annealing temperatures from 350 to 850°C. Our values are in general agreement with the crystallite sizes determined using XRD analysis by Chauhan et al. [80] (400°C: 12 nm) and Stroescu et al. [81] (600°C: 11 nm), yet are slightly smaller than those reported by Song et al. [49] (400°C: ~ 21 nm; 600°C: ~ 24 nm). The film thickness of our as-deposited ITO film is 275±6 nm, according to the cross-sectional SEM picture of the film. This is shown in Figure 1b. The thickness of the ITO thin films RTA-treated at 600°C and 800°C are 273±3 nm and 273±2 nm, respectively. The corresponding cross-sectional SEM images are shown in Figures 1f and 1h. These are almost the same but just slightly thinner than that of the as-deposited one. This reduction in thickness after annealing may be attributed to the minimization of defects or an increase in density of surface area to volume ratio [82,83]. The cross-sectional SEM view the post-annealed ITO thin film treated with RTA at 400°C is not available (specified by N/A in Figure 1d). Judging from the observed trend, its thickness should be close to that of the other annealed films in this study. While we did not perform X-Ray Diffraction (XRD) measurements, it is highly plausible that our samples, as-deposited one is amorphous while annealed ones are polycrystalline. Using XRD analysis, Song et al. [49], Chauhan et al. [80], and Stroescu et al. [81] reported that ITO thin films crystallized when subjected to RTA for 60 seconds in a nitrogen environment at 600°C, 600°C, and 400°C, respectively. It is worth noting that fully crystalline ITO thin films with a thickness of 300 nm are achievable with RTA treatment at relatively low temperatures of 300°C for 15 minutes in an argon environment [84]. This suggests that lower annealing temperatures necessitate increased annealing times to achieve the crystallite ITO films.

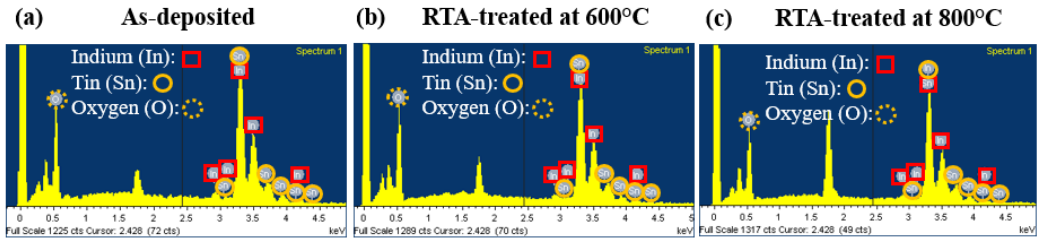
AFM was employed to determine the surface roughness and particle size of the ITO thin films. Figure 2a-d display the 3-D top view of the samples under study by AFM. The root mean square (RMS) roughness of the as-deposited ITO film is 1.5 nm, whereas RTA-treated ITO films at 400°C, 600°C, and 800°C are 3.4, 3.5 nm, and 8.3 nm, respectively. The increasing surface roughness with increasing annealing temperature is consistent with those reported in the literature, e.g., Song et al [49]. Note that the RMS roughness for RTA-treated ITO thin films at 400°C and 600°C are nearly the same. This is also in agreement with work of Song et al. [49].



**Figure 2.** The AFM surface topography images of (a) as–deposited, (b) RTA-treated at 400°C (c) RTA-treated at 800°C and (d) RTA-treated at 800°C ITO thin film. The surface with scaling of particle size of (e) as–deposited (f) RTA-treated at 400°C, (g) RTA-treated at 600°C and (h) RTA-treated at 800°C ITO thin film.

We also studied the surface topology of the films using AFM, as shown in Figure 2e-h. The calculated particle sizes (or diameters) of the as-deposited, RTA-treated at 400°C, RTA-treated at 600°C, and RTA-treated at 800°C ITO thin films are 37 nm, 62 nm, 85 nm, and 243 nm, respectively. The trend of particle size increasing in AFM images with annealing temperature has also been observed by other groups [84]. We note that the AFM topological study revealed particle areas (3020 nm<sup>2</sup> at 400°C, 5676 nm<sup>2</sup> at 600°C, and 46395 nm<sup>2</sup> at 800°C much higher than those obtained with SEM. This discrepancy is likely due to the particles detected by AFM comprising multiple crystallites or grains as measured with SEM (Figure 1). Other authors have also reported that sputtered ITO films exhibit a domain-subgrain structure where all subgrains in a domain (up to 500 nm diameter) have the same crystallographic orientation [85,86]. Another reason is the resolution difference between AFM and SEM. For instance, Brintlinger et al. [87] found that the image diameter of nanotubes measured by AFM was 50–100 nm, significantly larger than the actual diameter of 1–5 nm measured by SEM.

Energy-dispersive X-ray spectroscopy (EDS) was utilized on the top surface for the elemental analysis of the samples of interest. Figure 3a-c show the EDS spectra, confirming the presence of all related elements, i.e., indium (In), tin (Sn), and oxygen (O). Furthermore, the weight and atomic percentages of all elements recorded by EDS for these samples are displayed in Table 1. The EDS spectroscopic study on RTA-treated ITO thin film at 400°C is not available.



**Figure 3.** Element analysis of (a) as-deposited (b) RTA-treated at 600°C and (c) RTA-treated at 800°C ITO thin film. .

**Table 1.** Element weight and atomic percentage analysis of as-deposited (denoted by As-), RTA-treated at 600°C (denoted by 600°C) and RTA-treated at 800°C (denoted by 800°C) ITO thin film.

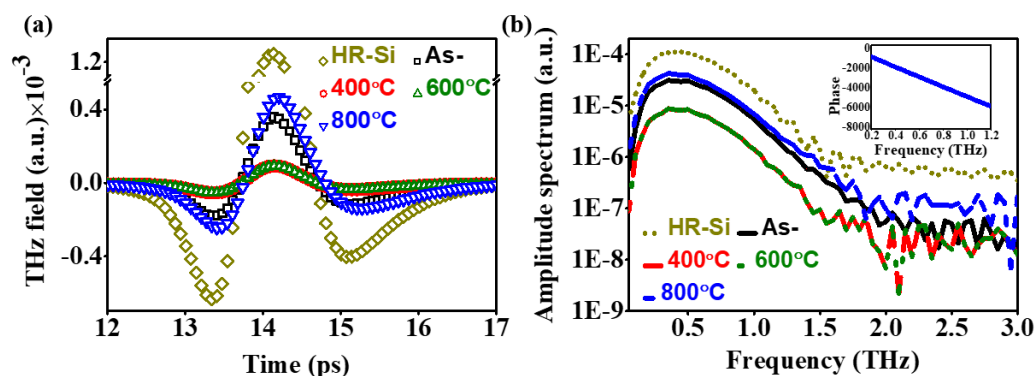
Sample	O K	In L	Sn L
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	Weight (%)	Atomic (%)	Weight (%)	Atomic (%)	Weight (%)	Atomic (%)
As-	22.78	68.01	67.44	28.05	9.77	3.93
600°C	22.98	68.23	69.48	28.75	7.54	3.02
800°C	24.71	70.27	66.90	26.51	8.38	3.21

We note a trend of increasing weight and atomic percentage of oxygen (O) from the ITO samples that were as-deposited (weight: 22.78%, atomic: 68.01%) to RTA-treated at 600°C (weight: 22.98%, atomic: 68.23%) to RTA-treated at 800°C (weight: 24.71%, atomic: 70.27%). This trend is suspected to be due to the increasing oxygen partial pressure in the environment, although we performed RTA in a Nitrogen ambient. Similar phenomena were reported in spinel-type nickel manganite oxide ( $\text{NiMn}_2\text{O}_4\delta$ ) polycrystalline samples treated at high temperatures of 800°C [88]. On the other hand, indium (In L) recorded higher values in both weight (69.48%) and atomic (28.75%) percentages in RTA-treated ITO samples at 600°C compared to the as-deposited ones (weight: 67.44%, atomic: 28.05%). In contrast, tin (Sn L) exhibited lower values in both weight (7.54%) and atomic (3.02%) percentages in RTA-treated ITO samples at 600°C compared to the as-deposited ITO thin film (weight: 9.77%, atomic: 3.93%). In related studies by Thirumoorthi et al. [89], and Seki et al. [90], the resistivity of the ITO film is lower, carrier concentration is higher and mobility also increased with increasing Sn L concentrations due to the valence difference between Sn L and In L ion ions. Thus, we expect ITO films RTA-treated at 600°C to be more conductive, as compared to the as-deposited and RTA-treated ITO thin film at 800°C. T As we shall see later, the trends for mobility and carrier concentration in annealed ITO films are more complex, even though the resistivity of RTA-processed at 600°C is indeed lower.

### 3.2. THz Optical and Electrical Properties

The THz optical properties of as-deposited and RTA-treated ITO thin films coated on HR silicon and the reference (bare HR silicon) were studied by using a home-made transmission-type THz-TDS system. The THz pulse waveforms transmitted through the reference and ITO/HR silicon samples are shown in Figure 4a. A small-time delay due to discernible phase shift as well as attenuation of the THz pulse traversing the samples under study can readily be seen. Next, a Fast Fourier Transform (FFT) algorithm was applied to convert the THz time-domain signal to its spectral amplitudes. These are displayed in Figure 4b. The data, i.e., time-delay or phase shift and attenuation imply significant interaction between the THz wave and materials investigated. The inset of Figure 4b shows an example of a nearly perfect phase linearity of transmitted THz wave through all the samples in the frequency range from 0.2 to 1.2 THz.



**Figure 4.** THz (a) temporal waveforms and (b) amplitude spectra transmitted through bare HR silicon, as-deposited, RTA-treated 400°C, RTA-treated 600°C and RTA-treated 800°C ITO thin films. Inset in (b) shows phase linearity of the THz signal transmitted through a ITO /HR-Si annealed at 800°C.

For extraction of the optical constants, we employ the same approach as in our previous works on various thin films and nanostructures [55–59,91,92]. We reiterate here for the benefits of readers: Consider the ITO layer (subscripted as 2) to be sandwiched between air (subscripted as 1) and a



substrate (subscripted as 3) with complex refractive indices  $n_2$ ,  $n_1$  and  $n_3$ , respectively. The THz wave is assumed to be incident on this thin layer with a thickness of  $d$  from the air toward the substrate. Considering multiple reflections [93], the transmitted THz electric field through the ITO-coated substrate can be written as

$$E_{sig}(\omega) = t_{31}E_0(\omega) \frac{t_{12}t_{23}e^{\frac{i n_2 \omega d}{c}}}{1 - r_{21}r_{23}e^{\frac{i 2n_2 \omega d}{c}}} e^{\frac{i n_3 \omega D}{c}} \quad (1)$$

where  $E_0$ ,  $t_{12}$ ,  $t_{23}$ ,  $t_{31}$ ,  $r_{21}$ , and  $r_{23}$  are the incident electric field, transmission, reflection coefficients between various interfaces;  $\omega$  is the angular frequency of the THz wave;  $c$  is the speed of the light in vacuum;  $D$  is the thickness of substrate. Similarly, a reference THz field defined as the THz field transmitted through the bare substrate can be written as

$$E_{ref}(\omega) = t_{13}t_{31}E_0(\omega)e^{\frac{i \omega d + n_3 \omega D}{c}} \quad (2)$$

The transfer function of the THz wave through the ITO layer then can be written as

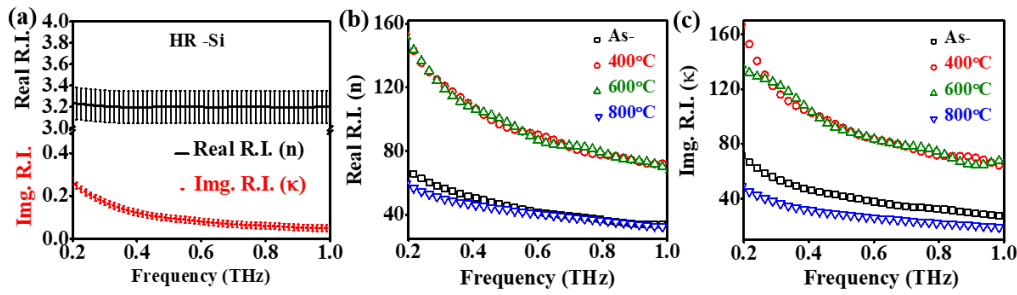
$$E_{theo}(\omega, n_2) = \frac{E_{sig}(\omega)}{E_{ref}(\omega)} = \frac{t_{12}t_{23}e^{\frac{i (n_2-1) \omega d}{c}}}{t_{13} \left( 1 - r_{21}r_{23}e^{\frac{i 2n_2 \omega d}{c}} \right)} \quad (3)$$

Experimentally,  $t_{exp}(\omega, n_2)$  is obtained from ratios of the frequency components of the Fourier transforms of the measured THz waveforms through the as-deposited and annealed ITO/HR-Si and the bare substrate. An error function  $Error(\omega, n_2)$  is defined as follows:

$$|t_{exp}(\omega, n_2) - t_{theo}(\omega, n_2)| = Error(\omega, n_2) \quad (4)$$

By minimizing the error function, the real and imaginary parts of the complex refractive index  $n_2$  of the thin film layer can be deduced.

Figure 5a shows the real ( $n$ ) and imaginary ( $\kappa$ ) part of refractive indices of the substrate (HR-Si) in the frequency range from 0.2 to 1 THz. The calculated values of  $n \sim 3.2 \pm 0.18$  is nearly constant across the THz frequency band. The value is comparable to that reported by Li et al [94] and slightly lower than those reported by Dai et al and others [95–97]. On the other hand, the calculated  $\kappa$  is slowly decreasing from 0.24 to 0.05 with the frequency increased from 0.2 to 1 THz. This trend closely resembles that reported by Li et al [94]. Figure 5b, c shows the real and imaginary parts of the complex refractive index,  $n$  and  $\kappa$  of as-deposited and RTA-treated ITO films at 400°C, 600° and 800°C as a function of frequency. In the frequency range of 0.2-1.0 THz, as-deposited ITO thin film exhibits a decreasing trend in  $n$  from  $\sim 65$  to  $\sim 33$ , while  $\kappa$  varies from  $\sim 66$  to  $\sim 27$ . Such decreasing trend and values of optical constants for as-deposited ITO thin film are very close to those of the DC-magnetron-sputtered and electron-beam-deposited ITO thin films reported previously by us [55–59] as well as pulsed-laser-deposited ITO thin film reported by Wang et al. [60]. This implies that the THz optical constants of ITO films deposited by various methods are very similar. Note that  $n \approx \kappa$  throughout this frequency band. This implies that the real part of the dielectric constant is very small, since  $\text{Re}[\epsilon] = n^2 - \kappa^2$ . The dielectric response of the material at THz frequencies is thus dominated by the imaginary part of the dielectric constant.



**Figure 5.** (a) The real (n) and imaginary (κ) part of refractive indices of the substrate (HR-Si) (added an error bar for thickness variation of  $\sim 350 \pm 15 \mu\text{m}$ ). (b) the n and (c) κ ITO films as a function of frequency. Black open square: as-deposited, red circles: RTA-treated at 400°C, green open triangles: RTA-treated at 600°C and blue open triangles: RTA-treated at 800°C.

The THz optical constants of RTA-treated ITO thin films also exhibit analogous decreasing trend with increasing frequency. Note, however, the n and κ of ITO films RTA-treated at 400°C and 600°C are similar in magnitudes and trend. For example, n for the former ( $T_a = 400^\circ\text{C}$ ) varies from  $\sim 143$  to  $\sim 72$  and the latter ( $T_a = 600^\circ\text{C}$ ) from  $\sim 143.4$  to  $\sim 68$ , respectively, over the frequency band of 0.2 – 1.0 THz. The extinction coefficients of ITO films RTA-treated at 400°C and 600°C, κ, varies from  $\sim 153$  to  $\sim 64$  for the former ( $T_a = 400^\circ\text{C}$ ), as compared to  $\sim 132$  to  $\sim 68$  for the latter ( $T_a = 600^\circ\text{C}$ ) in the same frequency band. These values, are much higher in values in comparison to those of the as-deposited ITO thin film. In contrast, the n values of RTA-treated at 800°C ITO thin film revert back to about the same values as those of the as-deposited sample, while its κ is somewhat lower, ranging from  $\sim 45$  to  $\sim 19$ . These trends can be understood by examining the electric characteristics of the films such as carrier concentration and mobility, which are extracted from the THz optical constants determined above.

The complex THz conductivity, or optical conductivity in the THz band,  $\sigma^*$  is related to the dielectric function,  $\varepsilon(\omega) = [n(\omega) + i\kappa(\omega)]^2$  through

$$\sigma^*(\omega) = (\sigma_r + i\sigma_i) = i\omega\varepsilon_0(\varepsilon_\infty - \varepsilon^*) \quad (5)$$

where  $\varepsilon_0$  is the free-space permittivity,  $\varepsilon_\infty \sim 4$  is the high-frequency dielectric constant of ITO [58,98,99], consisting of contributions from bound electrons. Therefore, we can determine THz conductivities of samples under study from their complex refractive indices, i.e.,

$$\sigma_r = \omega\varepsilon_0\varepsilon_i = 2nk\omega\varepsilon_0, \quad (6)$$

$$\sigma_i = \omega\varepsilon_0(\varepsilon_\infty - \varepsilon_r) = \omega\varepsilon_0(\varepsilon_\infty - n^2 + \kappa^2). \quad (7)$$

Conversely, the complex optical constants can also be written in terms of the complex conductivity.

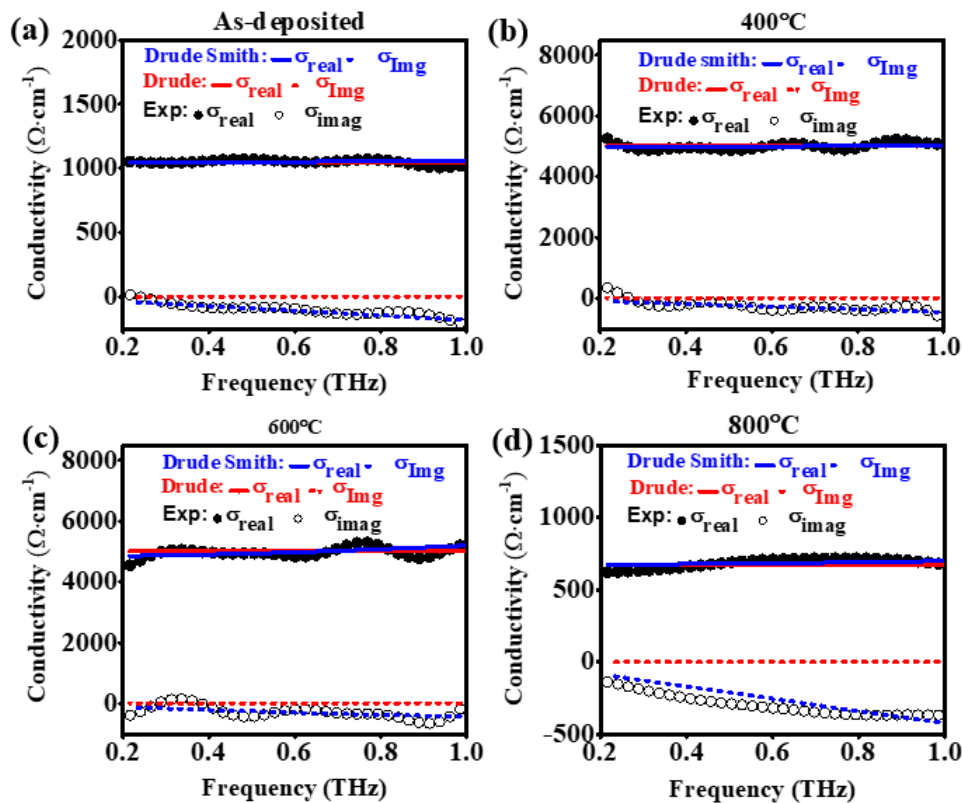
In degenerate semiconductors such as ITO, the Drude free-electron model has been most widely used to describe its electrical characteristics. That is,  $\sigma^*(\omega) = \varepsilon_0\omega_p^2\tau(1 - i\omega\tau)$  [100], where  $\omega_p = N_e e^2\tau/m^*$  and  $\tau$  are unscreened plasma frequency and scattering time of carriers in the material;  $N_e$ ,  $e$ , and  $m^* = 0.3 m_0$  [101] are free-electron concentration, electronic charge and effective mass of the electron, respectively, whereas  $m_0$  is the electron mass. The real part of the THz conductivity,  $\text{Re}\{\sigma\}$ , exhibits a maximum at zero (DC) frequency, and its value decreases with increasing frequency. For  $\text{Im}\{\sigma\}$  [55–59], it can only be positive and approaches a maximum as the frequency approaches that of the inverse of the scattering rate. We have found, however, that the THz conductivities of ITO films and nanostructures exhibit non-Drude-like behavior, e.g., depressed values of DC conductivity and negative values for  $\text{Im}\{\sigma\}$  [55–59]. Therefore, a more generalized conductivity model such as the Drude-Smith model [102], which considers the carrier localization effect, can be considered to describe THz conductivity of the ITO material. In this model,

$$\sigma^*(\omega) = \frac{N_c e^2 \tau / m^*}{1 - i\omega\tau} \left[ 1 + \frac{c}{1 - i\omega\tau} \right] \quad (8)$$

where  $c$  is a fitting parameter that depicts the persistence of velocity of free electrons in the material and can be associated with the degree of backscattering that a carrier suffers after a collision. The values of  $c$  is set to vary in the range from -1 to 0 and When  $c = 0$ , scattering of free electrons is isotropic and the Drude model is recovered. In the other limit, i.e.,  $c = -1$ , carriers undergo complete backscattering or localization. This simple empirical model works remarkably well for a variety of materials and nanostructures [55–59,103]. The mechanisms for carrier localization in ITO films can be either backscattering from grain boundaries [104] or by the impurity ions [105].

The unscreened plasma frequency and scattering time together with the  $c$ -parameter are judiciously varied to fit the dielectric constants, i.e., optical constants from the THz-TDS data of the samples under study. The electrical parameters such as carrier concentration, mobility, conductivity and resistivity using the well-known relations:  $\rho = 1/\sigma_{DC}$ ,  $\sigma_{DC} = \sigma(0) = (1+c)eN_c\mu = (1+c)\frac{N_c e^2 \tau}{m^*} = (1+c)\epsilon_0 \omega_p^2 \tau$  and  $\mu = (1+c)\frac{e\tau}{m^*}$ . For the Drude model,  $c = 0$  in the above.

As we can see in Figure 6, the Drude-Smith model fits the THz conductivity data better than the simple Drude model. All the fitting parameters as well as the electrical parameters deduced are summarized in Table 2, where we have listed instead the screened plasma frequency,  $\omega_p^* = \omega_p/(\epsilon_\infty)^{1/2}$ ,  $\epsilon_\infty \approx 4$  for ITO [106]. The values of  $\epsilon_\infty$  and  $m^*$  varied somewhat in the literature. Recent work showed that both are dependent on carrier concentration. Fujiwara and Kondo [107] showed that  $\epsilon_\infty$  reduces while  $m^*$  increases with increasing carrier concentration in the range of  $10^{19}$  to  $10^{21}$  cm<sup>-3</sup>. This is confirmed in a recent study by Blair et al. [108]. Here we assumed that both are constants, independent of carrier concentration. This can introduce ambiguity in the extracted electrical parameters.



**Figure 6.** (a) The real ( $\sigma_{\text{real}}$ ) and (b) imaginary ( $\sigma_{\text{img}}$ ) part of conductivities as the function of THz frequencies of various ITO films. Solid and open circles are experimentally extracted conductivities. The dashed curves are fitting lines using both models.

**Table 2.** The electrical parameters of as-deposited (specified as As-), RTA-treated at 400°C (specified as 400°C), RTA-treated at 600°C (specified as 600°C) and RTA-treated at 800°C (specified as 800°C) ITO thin films.

Parameters	As-	400°C	600°C	800°C
$\mu$ (cm <sup>2</sup> /V·s)	5.3	22	47	14
$\omega_p^*$ (rad·THz)	1784	1865	1294	839
$\tau$ (fs)	6	12	21	20
$c$	-0.83	-0.68	-0.63	-0.87
$N$ (cm <sup>-3</sup> )	$1.02 \times 10^{21}$	$1.31 \times 10^{21}$	$6.31 \times 10^{20}$	$2.65 \times 10^{19}$
$\sigma_{\text{DC}}$ ( $\Omega^{-1} \cdot \text{cm}^{-1}$ )	1019	4815	4792	628
$\rho$ ( $\Omega \cdot \text{cm}$ )	$9.8 \times 10^{-4}$	$2.0 \times 10^{-4}$	$2.0 \times 10^{-4}$	$15.9 \times 10^{-4}$

Previously, we have shown that THz-TDS analysis yield electrical parameters, e.g., the DC conductivity, that provide reasonable estimates to those obtained by Hall measurements [55]. Similar observations were made by Brown et al. [109], the deviation being attributed by the observation that ITO is non-Drude-like and surface roughness. Mergel and Qiao [85] observed that the "optical" conductivity and mobility in ITO films are generally higher than their corresponding electrical parameters. This discrepancy is due to pronounced microstructures with poorly conducting grain boundaries, which reduce DC conductivity but do not hinder the oscillatory motions of optically excited carriers. Upřety et al. [54] also stated that the inclusion of THz range data for spectroscopic ellipsometric measurement is necessary to achieve good agreement with conventional direct current approaches such as measurements done by Hall or 4-point probe instruments. Examining Table 2, we find that the resistivity of the ITO film first drops to  $2.0 \times 10^{-4} \Omega \cdot \text{cm}$  as the annealing temperature was raised to 400°C and 600°C, then becomes higher for  $T_a = 800^\circ\text{C}$ , reaching  $15.9 \times 10^{-4} \Omega \cdot \text{cm}$ , somewhat higher than that of the as-deposited film,  $9.8 \times 10^{-4} \Omega \cdot \text{cm}$ . Since the optical constants of ITO films are closely related to resistivity or conductivity, the dependence of  $n$  and  $\kappa$  on  $T_a$  shown in Figure 5 can now be qualitatively understood.

Rapid thermal annealing is expected to (i) substitute more  $\text{In}^{3+}$  by  $\text{Sn}^{4+}$ , (ii) create more oxygen vacancies, and (iii) enlarge the grain (Figs. 1 and 2) with reduced density of grain boundaries for creating more free and mobile charge carriers. As a result, the mobility and carrier concentration of the annealed films are expected to be higher. Previously, A. Valla et al. [110] identified the role of various scattering mechanisms that limit the mobility of ITO films for a range of carrier concentrations. If the carrier concentration ( $n$ ) in the film is less than  $2 \times 10^{19} \text{ cm}^{-3}$ , then the mobility is adversely affected by the grain boundaries scattering mechanism. Scattering by ionized/neutral impurities, on the other hand, can play a dominant role for reduction in the mobility value if the ITO film contains high carrier concentration ( $n > 2 \times 10^{20} \text{ cm}^{-3}$ ). This is indeed the case of annealed ITO films treated at  $T_a = 400$  and  $600^\circ\text{C}$ . Several other groups have reported similar finding. In their work on RTA-treated ITO films with  $T_a$  between  $500 - 950^\circ\text{C}$ , Parida et al. [111] observed a plateau region for resistivity of their samples at  $T_a = 500 - 600^\circ\text{C}$ . Upon further increasing of annealing temperature,  $\rho$  first drops but becomes higher for  $T_a \geq 850^\circ\text{C}$ . The authors argued that the structure of ITO annealed at relatively high temperatures are unstable, with  $\rho$ ,  $\mu$  and  $N_c$  co-related to each other due to the formation of oxygen interstitials and Sn-related defect centers. Studying the annealing temperature from  $100$  to  $550^\circ\text{C}$ , Yuan et al. [112] found that the resistivity of -annealed ITO film RTA in vacuum rapidly decreases until about  $450^\circ\text{C}$ , reaching a minimum of  $2.5 \times 10^{-4} \Omega \cdot \text{cm}$  at  $450^\circ\text{C}$ . Further increasing the annealing temperature, the resistivity rises to  $4.5 \times 10^{-4} \Omega \cdot \text{cm}$  at  $550^\circ\text{C}$ . Ahmed et al. [38] also observed that furnace annealing at  $550^\circ\text{C}$  input excess heat that adversely affects the film structure by creating voids between the grains. In a study to extend the NIR transmission window of ITO films by RTA at various temperatures starting from  $350^\circ\text{C}$  to  $850^\circ\text{C}$ , Maniyara et al. [51] also observed that the sheet

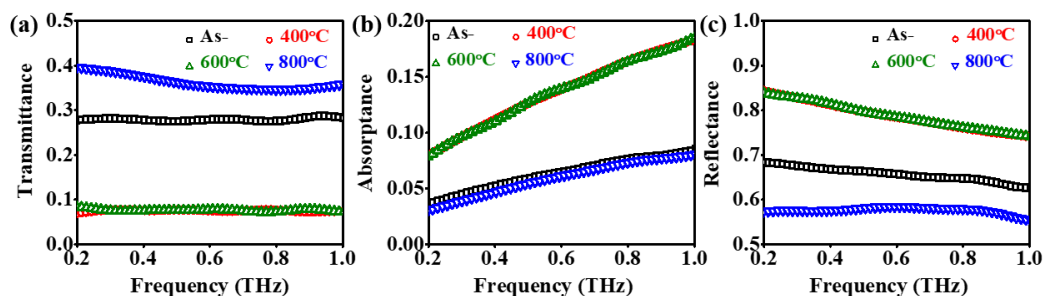


resistance of the film decreased with increasing annealing temperature up to 750 °C but increased abruptly above that point. Sun et al. [113] studied effects of ambient high-temperature annealing (700 -1000°C) on electrical properties of ITO films. Increased resistivity at elevated temperatures was thought to be due to adsorbed oxygen molecules occupying positions of oxygen vacancies. Consequently, carrier concentration sharply decreased. While we performed annealing in a nitrogen ambient. Residue oxygen desorbed from the RTA chamber cannot be ruled out. The findings of these groups are consistent with what we observed and are correlated with values of  $c$ -parameters of the samples shown in Table 2: -0.83 and -0.87 for as-deposited and heat-treated ITO films at 800°C, -0.68 and -0.67 for annealed ITO films at 400°C and 600°C. Such values of the  $c$ -parameter suggest the presence of strong scattering centers like grain boundaries and ionized impurities, i.e., oxygen vacancies and  $\text{Sn}^{+4}$  substitutions. Back scattering is stronger for as-deposited and RTA-processed ITO films at 800°C than annealed ITO films at 400°C and 600°C. As a result, the mobility for the former two is lower. Insights can also be gained by examination of some relevant length scales. The mean free path of carriers,  $L_{\text{free}}$ , can be estimated as [104]

$$L_{\text{free}} = v_{\text{thermal}} \cdot \tau = (3 \cdot k_B \cdot T \cdot \tau^2 / m^*)^{1/2}, \quad (9)$$

where  $k_B = 1.381 \times 10^{-23} \text{ J} \cdot \text{K}^{-1}$  is the Boltzmann constant,  $T = 300 \text{ K}$  is the temperature of the samples in Kelvin and  $v_{\text{thermal}}$  is the thermal velocity from classical equipartition of energy. Using the above values and the scattering times,  $\tau$ , in Table 2,  $L_{\text{free}}$  of samples under study are estimated to be 1.28 nm, 2.56 nm, 4.48 nm and 4.26 nm, respectively, for as-deposited and RTA-treated ITO films at 400°C, 600°C and 800°C, respectively. From SEM studies (see Figure 1), we show that the lateral grain sizes for annealed samples are 5 nm, 7.5 nm and 15.8 nm, respectively. Hence, the mean free path is comparable to the grain sizes in our samples. As a result, scattering of carriers by grain boundaries is expected to be significant. Further, the charged impurity (Tin) scattering centers in ITO will also enhance the localization of carriers [105,114]. The average distance between dopant ions is proportional to the inverse of the third root of doping concentration. Therefore, free electrons will run into the dopant ions easily if the doping concentration is high enough. The average distance between dopant ions can be estimated from  $(N_c)^{-1/3}$  or 9.95 nm, 9.26 nm, 11.84 nm and 38.93 nm for as-deposited and RTA-treated ITO films at 400°C, 600°C and 800°C, respectively. Consequently, free carriers are unlikely to run into such scattering centers in the length of one mean free path. Therefore, carrier scattering by impurity ions are expected to play a minor role in our samples.

The transmittance of samples under study was calculated using the ratio of measured frequency-domain THz field amplitudes through the ITO/HR silicon to that through the reference (bare HR silicon), see Figure 7a. The THz transmittance of as-deposited and RTA-treated ITO thin films are slow-varying in the band of 0.2 – 1.0 THz. The average transmittance of as-deposited and RTA-treated ITO films at 400°C, 600°C and 800°C are 27 %, 8 %, 8 % and 39 %, respectively. We note the average THz transmittance of as-deposited ITO thin film is somewhat lower than those thinner ( $\sim 100 \text{ nm}$ ) as-deposited ITO thin films ( $T \sim 40\%$ ) used in our earlier device works [68]. This is primarily attributed to the thickness dependent free carrier absorption of ITO thin films. The THz transmittance of ITO thin film treated with RTA at 400°C and 600°C are as low 8 %. This is consistent with higher extinction coefficients of RTA-annealed ITO films at either 400°C or 600°C shown in Figure 5b. Our results indicate that annealing temperature is a critical parameter affecting transmittance and reflectance of the ITO film in the THz band.

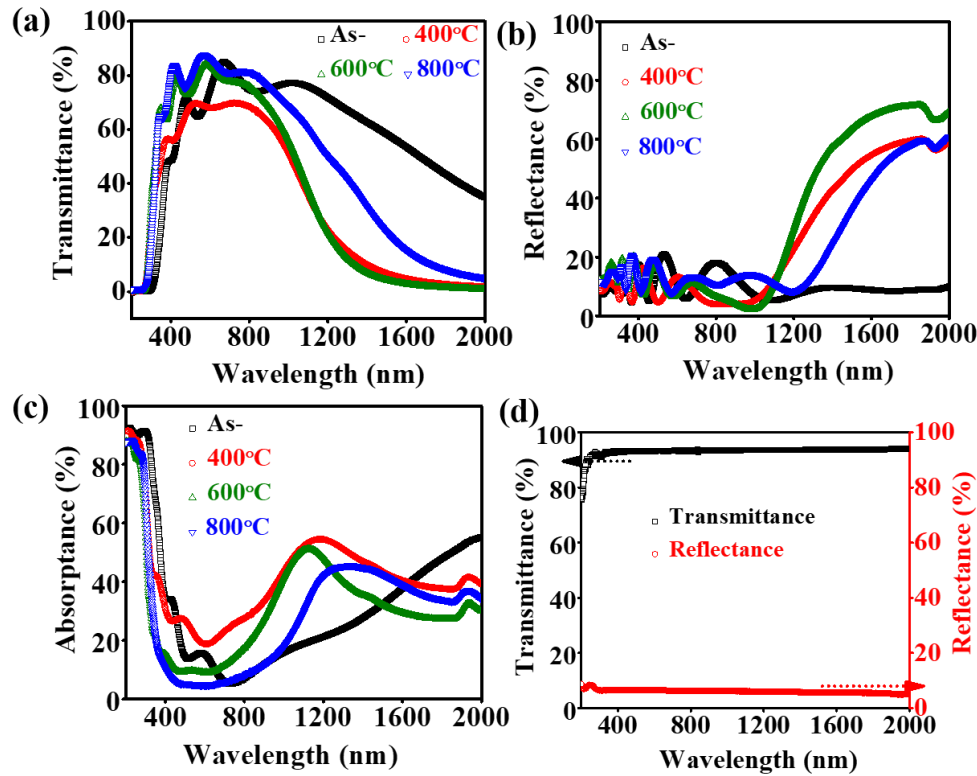


**Figure 7.** THz frequency dependent (a) transmittance (b) absorbance and (c) reflectance of as-deposited, RTA treated at 400°C, RTA treated at 600°C and RTA treated at 800°C ITO thin film.

In Figure 7b,c, the absorptance and reflectance of ITO thin films depend strongly on the annealing temperature in this frequency band. Here, the absorptance,  $A \approx \alpha d$ , where the absorption coefficient  $\alpha$  is related to the extinction coefficient  $\kappa$  by  $\alpha = 4\pi\kappa/\lambda$ . In turn, reflectance of the samples is given by  $R = 1 - T - A$ . We note that the decreasing trend of reflectance with frequency and dependence on conductivity or resistivity is consistent with the Hagen-Rubens relation [70,115],  $R(\omega) = 1 - 2\sqrt{2\epsilon_0\omega/\sigma}$ . Both absorptance and reflectance are found to be much higher for ITO films heat-treated by RTA at 400°C and 600°C than that of as-deposited ones. This suggests that RTA-treated ITO thin films at either 400°C or 600°C could potentially be useful as dichroic mirrors or absorbers for the THz band [70,116]. On the other hand, ITO thin films RTA-treated beyond 800°C could be an effective THz TCE material for THz photonic devices. We note the transmittance of ITO-coated device can be further enhanced by employing a grating-like, i.e., wire-grid structure, as we have demonstrated earlier [68].

### 3.3. Annealing Effects on UV-VIS-NIR Optical Properties of ITO Films

It is interesting to compare the optical properties of ITO films fabricated and processed for this work in the ultraviolet (UV), visible (VIS) and near infrared (NIR) band as a bearing on their optical properties in the far infrared (FIR) or THz frequency range. We have experimentally measured transmittance and reflectance of as-deposited and RTA-treated ITO thin films coated on fused silica as well as that of the substrate itself in the energy range of 0.6 eV – 6 eV, or the wavelength band of 200 – 2000 nm. These are shown in Figure 8. The average transmittance in the VIS-NIR region (400-800 nm) band for as-deposited ITO film was  $T_{av} \sim 72\%$ . After annealing at 400°C, 600°C, and 800°C,  $T_{av} \sim 68\%$ ,  $\sim 80\%$  and  $83\%$ , respectively. Considering the contribution by the substrate (see Figure 8d), all samples can be considered highly transparent. Higher transmittance of samples after heat treatment by annealing can be attributed to increasing sizes of crystallites after annealing as shown in the SEM data (see Figure 1). It is well-known that improved crystallinity leads to reduced scattering of incident light in the transparency window. Thus transmission of visible light through the film is higher. Transmittance drops off sharply in the NIR and UV band for all samples. The positions of the band gap or onset of absorption shifted to shorter wavelength for samples annealed at increasingly higher temperatures. This point will be addressed in more detail later on in this subsection.



**Figure 8.** (a) The transmittance (b) reflectance and (c) absorbance of as-deposited, RTA-treated at 400°C, RTA-treated at 600°C and RTA-treated at 800°C ITO thin film coated on fused silica as well T and R of fused silica (d) in UV-VIS-NIR region. .

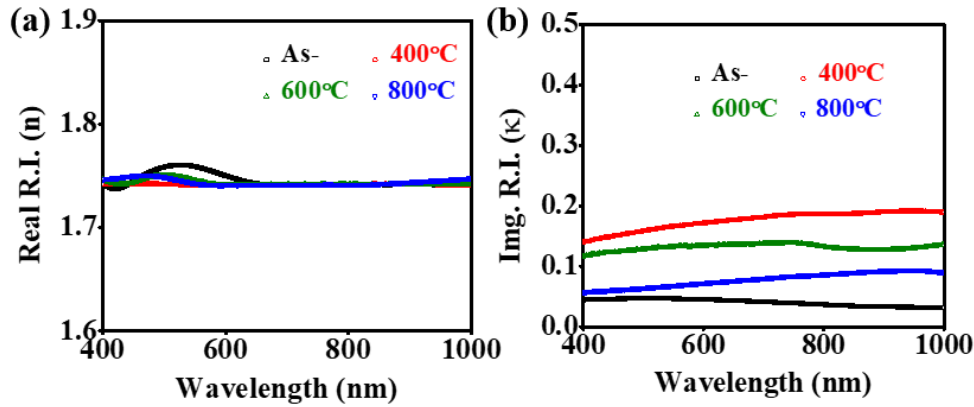
The average reflectance of as-deposited ITO thin film in the visible band (400-800 nm),  $R_{av} \sim 14\%$ . Whereas, the average reflectance of ITO thin film RTA-treated at 400°C, 600°C and 800°C are  $\sim 10\%$ ,  $\sim 12\%$  and  $\sim 13\%$ , respectively in this transparency window. In addition, the reflectance curves show small yet significant oscillations due to multiple reflections of light within the sample. This is also in reasonably good agreement with previous findings by others [117]. Further, annealed samples show higher reflectivity in the NIR region [118,119], approaching the plasma edge. The highest NIR reflectivity,  $\sim 70\%$  was attained by the ITO film annealed at 600°C. We tentatively attributed this to the high carrier concentration in this sample, see Table 2 for a tabulation of carrier concentration for all samples. Note, the reflectivity is slightly lower for the ITO thin film RTA-treated at 800°C. This correlates with lower carrier concentration found in this sample, which also exhibits the highest surface roughness of all samples [120]. The position of the plasma edge and steepness of reflectance curves in the NIR for the annealed samples is related to its post-annealing carrier concentration and mobility [85,121]. Comparing with Figure. 7, we note that the transmission properties of as-deposited and RTA-annealed ITO films in the visible transparency window and the THz band are somewhat different. This could be understood by realizing that ITO films are dielectric-like in the visible, metal-like in the far infrared.

We now focus on spectral regions of ITO films that are weakly absorbing and also shown prominent maximum ( $T_M$ ) and minimum ( $T_m$ ) transmission spectrum, i.e., the visible window of 400-800 nm (see figure 8a). Following Swanepoel [122], the refractive index of ITO the film in its weakly absorbing VIS-NIR (400 to 1000 nm) band can be written as  $n = [N + (N^2 - n_{sub}^2)^{1/2}]^{1/2}$ , where

$$N = 2n_{sub} \frac{T_M - T_m}{T_M T_m} + \frac{n_{sub}^2 + 1}{2}, \quad T_M \text{ and } T_m \text{ are envelopes of maxima and minima of the transmission}$$

curve, whereas  $n_{sub} = \frac{1 + (1 - T^2)^{1/2}}{T}$  is the refractive index of fused silica substrate and is determined using its transmission spectrum (T) to be  $\sim 1.43$ , and found to be fairly independent of wavelength.

The calculated refractive index  $n$  of as-deposited and RTA-treated ITO thin films in wavelength range from 400 to 1000 nm are shown in Figure 9a. Note that the refractive index of 1.74 in this band is almost wavelength-independent and approximately the same for all types of ITO thin films studied in this work. In the literature, the reported refractive indices for as deposited as well as annealed ITO thin films vary from 1.6 to 2 in this band [123].



**Figure 9.** (a) real ( $n$ ) and (b) imaginary ( $\kappa$ ) refractive indices of as-deposited, RTA-treated at 400°C, RTA-treated at 600°C and RTA-treated at 800°C ITO thin film. .

The thickness  $d$  of those ITO thin films can be determined using the envelopes of maxima and minima of the transmission curve in the visible spectra,  $d = \frac{\lambda_1 \lambda_2}{2(\lambda_1 n_2 - \lambda_2 n_1)}$ , where  $n_1$  and  $n_2$  are the

refractive indices at two adjacent maxima or minima,  $T_m$  or  $T_m$ , corresponding to wavelengths at  $\lambda_1$  and  $\lambda_2$ , respectively. The estimated thickness of as-deposited and RTA-treated ITO thin films at 400°C, 600°C and 800°C are ~ 470 nm, ~ 410 nm, ~ 483 nm and ~ 468 nm, respectively. Knowing the thickness of ITO thin films, the absorption coefficient  $\alpha$  of these samples are extracted using the relationship between transmittance ( $T$ ), reflectance ( $R$ ) and thickness  $d$ , given by

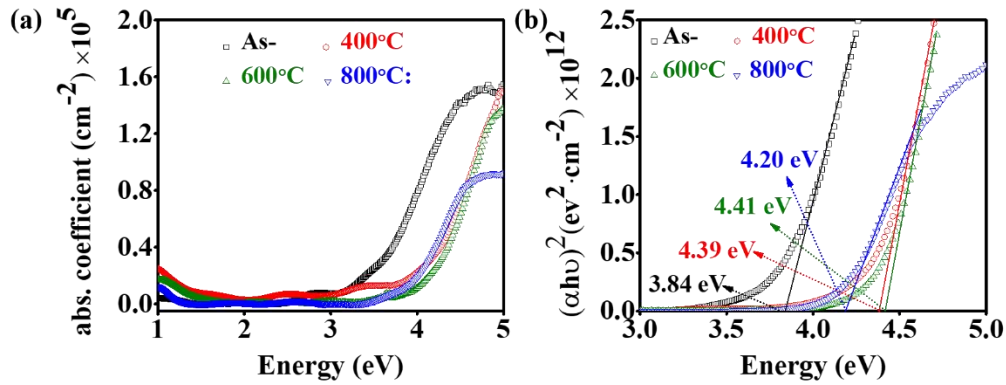
$$\alpha = \frac{1}{d} \ln \left[ \frac{(1-R)^2}{2T} + \sqrt{\frac{(1-R)^4}{4T^2} + R^2} \right].$$

Next, the imaginary part of refractive index  $\kappa$  as the function of

wavelength is evaluated using the relation,  $\kappa = \alpha \lambda / 4\pi$ . This is plotted in Figure 9b. We found that  $\kappa$  in the wavelength range of 400 to 1000 nm is small and slow varying and approximately 0.04, 0.18, 0.13 and 0.07 for as-deposited and RTA-treated ITO thin films at 400°C, 600°C and 800°C, respectively. Such estimated values are also in agreement with those reported in previous works [123].

Crystalline ITO has been shown to be a direct gap semiconductor [124]. From the absorption coefficient  $\alpha$  as plotted in Figure 10a, the optical bandgap  $E_g$  or the onset of absorption can be extracted using the extrapolation method proposed by Tauc:  $(\alpha h\nu)^2 = A (h\nu - E_g)$  [125]; where  $A$  is a constant and  $h = 6.626 \times 10^{-34}$  J.s is the Planck constant. These are shown for the samples under study in Figure 9b. The optical band gap  $E_g$  of as-deposited ITO thin film was found to be 3.84 eV, which broadened for RTA-treated ITO thin films at 400°C, 600°C and 800°C to 4.39 eV, 4.41 eV and 4.2 eV, respectively. The basic physics of this phenomenon is the carrier-concentration dependence of  $E_g$ , i.e., Burstein-Moss effect [126,127] and band gap shrinkage or renormalization due to electron-electron and electron-ionized impurity scattering [5,53,128]. Our values are in a good agreement with typical value reported previously. For example, Abd-Elnaïem et al. [129], extracted  $E_g$  for as-deposited and annealed ITO thin films with thickness of ~ 80 nm at 300°C to be ~ 3.2 eV and ~ 3.8 eV, respectively. Meanwhile,  $E_g$  for a 200 nm-thick ITO films heat-treated with RTA at 600°C was reported to be 4.04 eV by Song et al. [49]. We note the band gap of ITO thin films increases by 0.57 eV after RTA treatment at 600°C. This aligns with observation of Park et al. [130], who reported a 0.60 eV shift after furnace annealing at 400°C for their 150 nm-thick ITO films.





**Figure 10.** The (a) wave-length dependent refractive index and (b) optical bandgap of as-deposited, RTA-treated at 400°C, RTA-treated at 600°C and RTA-treated at 800°C ITO thin film.

#### 4. Conclusions

In this study, we explored the manipulation of optical properties of radio-frequency (RF) sputtered indium-tin-oxide (ITO) thin-films on highly resistive silicon substrate by rapid thermal annealing (RTA) in the terahertz (THz) frequency band. The optical constants of as-deposited and RTA-processed ITO films annealed at 400°C, 600°C and 800°C are determined by THz time-domain spectroscopy (THz-TDS). The THz optical constants of RTA-treated ITO thin films are shown to exhibit a decreasing trend with increasing frequency. In contrast, the  $n$  values of RTA-treated at 800°C ITO thin film revert back to about the same values as those of the as-deposited sample. These trends can be understood by examining the electric characteristics of the films such as carrier concentration and mobility. The real ( $n$ ) and imaginary ( $\kappa$ ) refractive indices of ITO films RTA-treated at 400°C and 600°C are similar in magnitudes. For example,  $n$  for the former ( $T_a = 400^\circ\text{C}$ ) varies from  $\sim 143$  to  $\sim 72$  and the latter ( $T_a = 600^\circ\text{C}$ ) from  $\sim 143.4$  to  $\sim 68$ , respectively, over the frequency band of 0.2 – 1.0 THz. The extinction coefficients of ITO films RTA-treated at 400°C and 600°C,  $\kappa$ , varies from  $\sim 153$  to  $\sim 64$  for the former ( $T_a = 400^\circ\text{C}$ ), as compared to  $\sim 132$  to  $\sim 68$  for the latter ( $T_a = 600^\circ\text{C}$ ) in the same frequency band. Their values, are much higher in values in comparison to those of the as-deposited ITO thin film, which exhibits a decreasing trend in  $n$  from  $\sim 65$  to  $\sim 33$ , while  $\kappa$  varies from  $\sim 66$  to  $\sim 27$ . In contrast, the  $n$  values of RTA-treated ITO films at 800°C ITO thin film revert back to about the same values as those of the as-deposited sample, while its  $\kappa$  is somewhat lower, ranging from  $\sim 45$  to  $\sim 19$ .

The transmittance can be changed from  $\sim 27\%$  for as-deposited to  $\sim 10\%$  and  $\sim 39\%$  for ITO films heat-treated at different annealing temperatures,  $T_a$ 's. RTA-treated ITO thin films at either 400°C or 600°C could potentially be useful as dichroic mirrors or absorbers for the THz band. On the other hand, ITO thin films RTA-treated beyond 800°C could be an effective material as transparent conducting electrodes (TCE) for THz EO devices. We note the transmittance of ITO-coated device can be further enhanced by employing a grating-like, i.e., wire-grid structure, as we have demonstrated earlier. Such variations of optical properties in the far infrared for the samples under study are correlated with their mobility and carrier concentration, which are extracted from Drude-Smith modeling of THz conductivity with plasma frequency, scattering time and the  $c$ -parameters as fitting parameters. Resistivities of the films are in the range of  $10^{-3}$  to  $10^{-4} \Omega\text{-cm}$ , confirming that annealed ITO films can potentially be used as transparent conducting electrodes for photonic devices operating at THz frequencies. The highest mobility,  $\mu = 47 \text{ cm}^2/\text{V}\cdot\text{s}$ , with carrier concentration,  $N_c = 1.31 \times 10^{21} \text{ cm}^{-3}$ , was observed for ITO films annealed at  $T_a = 600^\circ\text{C}$ . The scattering times of the samples were in the range of 8 – 21 fs, with  $c$ -values of -0.63 to -0.87, indicating strong back scattering of the carriers, mainly by grain boundaries in the polycrystalline film. To better understand the nature of these films, we have also characterized the surface morphology, microscopic structural properties and typical chemical composition of as-deposited and RTA-processed ITO thin-films. For comparison, we have summarized the optical properties of ITO films sputtered on fused silica substrates, as-deposited and RTA-annealed, focusing on the visible transparency window and the near infrared (400-1000 nm). the refractive index of 1.74 in this band is almost wavelength-independent and approximately the same

for all types of ITO thin film studied in this work. The extinction coefficient,  $\kappa$  in this band is small and slow varying and approximately 0.04, 0.18, 0.13 and 0.07 for as-deposited and RTA-treated ITO thin films at 400°C, 600°C and 800°C, respectively. The optical band gap  $E_g$ 's of as-deposited ITO thin film were found to be 3.84 eV, which broadened for RTA-treated ITO thin films at 400°C, 600°C and 800°C to 4.39 eV, 4.41 eV and 4.2 eV, respectively.

Overall, our study offers valuable insights into leveraging rapid thermal annealing to modify terahertz optical properties of ITO films, with potential applications spanning from coatings for waveguides to terahertz electro-optic switching devices and manipulation of terahertz electromagnetic waves.

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