

Review

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Review

Fundamental Mechanisms Underlying the Effectiveness of Nanoparticle Additives to Lubricants: 25 Examples Linking Nano- to Macroscale Friction

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Abstract: Studies of the fundamental origins of friction have undergone a rapid acceleration in recent years by providing valuable information on the nanoscale mechanisms responsible for the friction at the macroscopic level. Significant efforts have been directed into developing composite nanofluids and nanoparticle additives to unlock new tribological properties unattainable by traditional lubricants. The studies are now further evolving by developing methods to achieve active control of the nano- and/or mesoscale friction by application of magnetic and electric fields external to the contact. These methods constitute an area of rapidly growing interest, and they also are illuminating how the performance of conventional lubricants could be enhanced through synergistic addition of nanoparticles (NPs). This mini-review highlights 25 publications that collectively reveal significant progress, as well as important outstanding challenges, to a fundamental understanding of how the addition of NPs impacts the lubricant performance. The first two sections focus on the use of Quartz Crystal Microbalance (QCM), a technique that spans atomic to macroscale length and time scales. Subsequent sections expand to complimentary methods comparing results at the macro and atomic scale for similar materials. These studies highlight the pivotal role of the nanoparticle charge and surface treatment, while also indicating that rolling of nanoparticles is ineffective and/or detrimental.

Keywords: nanoparticle; lubrication; QCM; nanotribology; tribotronics; friction modifiers; nanolubricants

1. Introduction

Close to thirty years ago, in an early nanotribology experiment, Israelachvili and coworkers employed a surface forces apparatus (SFA) to measure the viscosity of toluene between atomically uniform mica surfaces as C₆₀ was added to the toluene [1]. Remarkably, they observed “full slip” conditions when C₆₀ was present that were not present for toluene alone. The authors suggested that macroscopic friction might also be profoundly impacted by addition of C₆₀ to lubricants. They cited rolling action of the small, 0.7 nm wide soccer-ball shaped molecules as a possible mechanism, or possibly changes to the slip conditions within one or two molecular layers from the surface.

Although C₆₀ did not subsequently become established as a commercial lubricant additive, the opportunities to reduce macroscale friction by using nanoparticle (NP) additives have sparked an intense interest among researchers and industry [2–4]. Most of the literature reports published to this date find that NP additives reduce friction, but their effectiveness as friction modifiers varies widely. For example, nanodiamonds of ca. 5 nm in diameter when added to oil reduce the macroscale friction coefficients by as much as 75% [5], while aqueous suspensions of nanodiamonds with certain surface treatments substantially increase friction in stainless steel contacts [6]. Clearly, the understanding of such opposite effects amongst very similar NP additives requires fundamental studies of the

underlying mechanisms (e.g., rolling, smoothing, film formation and electro-viscous effects, etc.) that give rise to nanoscale and macroscale tribological attributes (Figure 1).

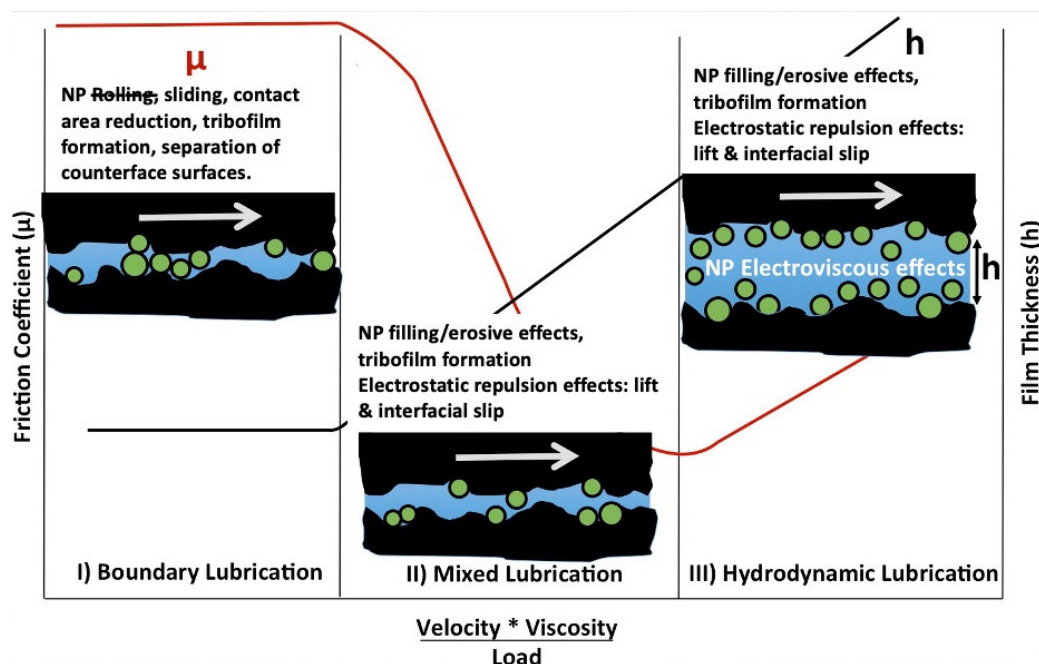


Figure 1. Stribeck curve including NP additives to the lubricant, depicting how the friction coefficient μ and film thickness h transition from solid contact to hydrodynamic lubrication. (Adapted from Curtis et al. [6]) and licensed with permission from Creative Commons 4.0 (<http://creativecommons.org/licenses/by/4.0>). A variety of mechanisms have been suggested for the impact of NP on friction in the various regimes. The studies presented in this mini review highlight the pivotal role of the nanoparticle charge and surface treatment, while also indicating that rolling of nanoparticles is ineffective and/or detrimental.

This mini review highlights 25 selected research reports [7–31], 24 of which were published in the decades following the pioneering work of Israelachvili and coworkers describing “full slip” conditions achieved by C_{60} additives. Collectively, they reveal significant progress, as well as important outstanding challenges, towards the fundamental understanding of how addition of NPs impacts the lubricant performance. The first two sections focus on how Quartz Crystal Microbalance (QCM) nanotribological response to solid contacts can be linked to macroscale friction coefficients and how QCM nanotribological response upon immersion into a liquid can be linked to macroscale lubricity in the mixed and hydrodynamic regimes. The sections that follow highlight the ineffective, and possibly detrimental, effect of nanoparticle rolling, an “astonishing” impact of surface treatments/surface charge, and how the friction can be tuned by varying electric charge and/or external electric potential. Given the very limited number of highlights presented here, a selection of in-depth and extensive topical review articles is also included in the references for more in-depth reading and background material [32–49].

2. Quartz Crystal Microbalance Response to Spherical Contacts Directly Links Nano- and Macroscale Friction

A QCM is comprised of a thin wafer of single crystal piezoelectric quartz, which is cut in way to oscillate in transverse shear motion when an alternating voltage is applied to metal electrodes deposited onto its two planar surfaces. Fundamental resonant frequencies are typically in the 5-10 MHz range, with very low internal dissipation. Initially developed in the 1920’s as a tuning-fork shaped time standard, or “quartz clock” [50], its use was extended to deposition rate monitors in the 1950’s [51] and to atomic-scale friction measurements in the 1980’s [52].

When employed for nanotribology applications, QCM is capable of directly linking nanoscale and macroscale properties because the typical peak electrode velocities of up to several m/s and the shear rates about 10^6 s^{-1} are comparable to those of macroscale systems. The method has been broadly applied to a wide range of soft materials' system [34,35] and is sensitive to both mass deposition on its surface electrode and viscoelastic coupling of fluids it may be in a contact with [39]. It was also used in geometries consisting of bare and lubricated tribological contacts with external objects such as spheres spanning a few mm to cm in diameter. Changes in the QCM frequency and dissipation in response to the external contacts yield information on the contact stiffness and/or friction coefficients [39,40]. Exceptionally high quality factors $Q \sim 10^6$ of QCM allow for precise measurements of shifts in frequency Δf and changes in ΔQ , which are inversely proportional to the half band width $\Delta \Gamma$ (Figure 2c). To enable a cross-comparison of QCM studies, highlights selected for this section employ QCMs oscillating in the fundamental mode at or near 5 MHz, with gold or steel electrodes (Figure 2). Further reading on modeling of contacts at the atomic scale, including QCM response, may be found in Refs. [32–35].

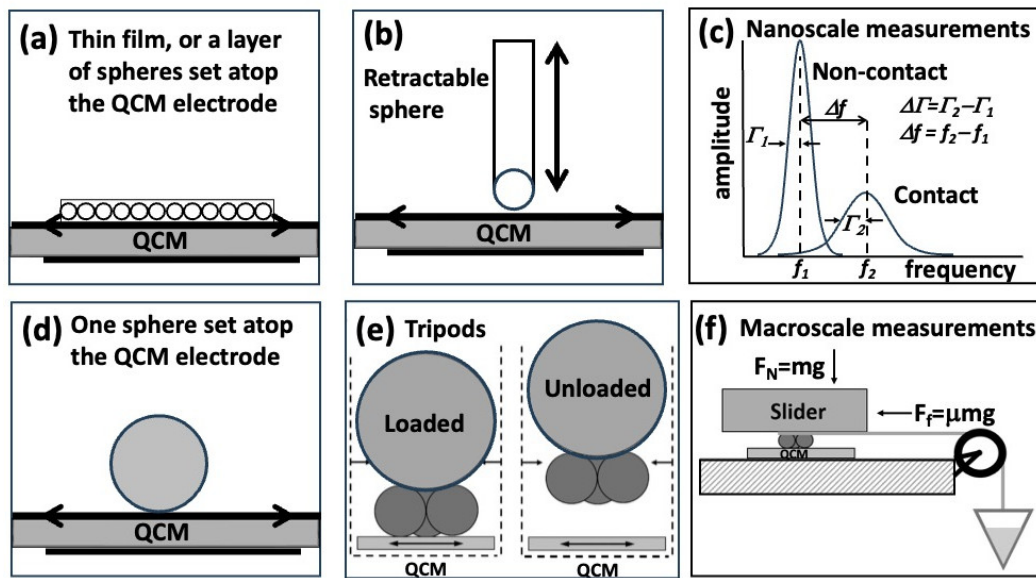


Figure 2. Geometries of tribological contacts highlighted in this section.

2.1. A Sensitive New Method for the Determination of Adhesive Bonding between a Particle and a Substrate [7]

In this 1985 publication, Dybwad reported frequency shift measurements associated with placement of one gold microsphere atop a gold electrode of a QCM oscillating in transverse shear motion and inferred the associated particle-substrate adhesive bond strengths for particles of various sizes [7]. For spheres with diameters ranging from 5 to 50 mm positive QCM frequency shifts in the range of 0.1 to 1.5 ppm were recorded.

For rigidly attached films deposited onto a QCM electrode (Figure 2a) the negative frequency shift is described by equations derived by Sauerbrey in the 1950s [51]:

$$\frac{m_f}{A} = \rho_f d_f = - \frac{\Delta f \sqrt{\rho_q \mu_q}}{2f_0^2}; \Delta f = - \frac{2f_0^2 \rho_2}{\sqrt{\rho_q \mu_q}}, \quad (1)$$

In Eq.(1), ρ_f and d_f are the film density and thickness respectively, $\rho_q = 2.648 \text{ g/cm}^3$ and $\mu_q = 2.947 \times 10^{11} \text{ gm cm}^{-1} \text{ s}^{-2}$ are the density and shear modulus of quartz, f_0 is the fundamental oscillation frequency before the film was deposited, and $\rho_2 = m_i/A$ is the mass per unit area of the film. For $f_0 = 5 \text{ MHz}$, Eq. (1) simplifies to

$$\Delta f = -2.263 \times 10^{-6} (f_0^2 \rho_2) = -5.66 \times 10^7 \rho_2, \quad (2)$$

where Δf has units of Hz and ρ_2 is g/cm^2 .

To interpret the positive Δf results, Dybwad employed a coupled oscillator model consisting of a gold particle with mass m attached to a QCM with a spring with stiffness k . Coupling the particle to the QCM changes its resonant frequency in accordance with:

$$f^2 = \frac{1}{8\pi^2} \left(\frac{K}{M} + \frac{k}{M} + \frac{k}{m} \right) \pm \frac{1}{8\pi^2} \left[\left(\frac{K}{M} + \frac{k}{M} + \frac{k}{m} \right)^2 - 4 \frac{K}{M} \frac{k}{m} \right]^{1/2}, \quad (3)$$

where M and K are the effective mass and stiffness of the QCM, and the unloaded resonant frequency $f_0 = (2\pi)^{-1} \sqrt{K/M}$. The expression in Eq. (3) has a positive branch for values of k less than $k = Km/M$. To first order, the frequency at $k = Km/M$ is described by $f/f_0 = 1 \pm \sqrt{m/M}$ for $m \ll M$. For large values of $k = K$, Eq (3) reduces to the Sauerbrey result, Eq.(1):

$$f = \frac{1}{2\pi} \sqrt{\frac{K}{M+m}} \Delta f = -\frac{2f_0^2 \rho_2}{\sqrt{\rho_q \mu_q}} \quad (4)$$

For weak contact stiffness Eq. (3) reduces to

$$f = \frac{1}{2\pi} \sqrt{\frac{K+k}{M}} \Delta f = +\frac{kf_0}{2K}. \quad (5)$$

By employing Eq.(5) Dybwad inferred values of k of the order of 10^7 dyn/cm for the particles by estimating the effective mass of the QCM as a half of the mass in the region of the active oscillations as only the surfaces oscillate at the full amplitude.

For a QCM electrode with 5 MHz fundamental resonant frequency, the electrode thickness t is 0.0334 cm and a typical active electrode radius (i.e., the section between the two electrodes) is 0.32 cm. The effective mass M of the active oscillation region $\sim (\rho_q \pi r^2 t)/2$ yields $M = 0.0142$ g; $K = 1.4 \times 10^{13}$ dyn/cm; $A = 0.32$ cm², where $K = (2\pi f)^2 M$, and $m = 1.263$ mg for the 50 nm sphere having the bulk density of gold, 19.3 g/cm³.

If the mass of the microsphere is spread uniformly over the electrode, then $\rho_2 = 3.95$ mg/cm² corresponding to a 2 nm thick film, and $\Delta f = -223$ Hz using Eq.(1). For a comparison, the frequency shift decreases to $\Delta f = -16.0$ Hz for a non-slipping monolayer of close-packed C₆₀ molecules (mass per molecule 1.19559×10^{-21} g; area per particle 0.4244 nm²; $\rho_2 = 0.282$ mg/cm²) and to $\Delta f = -59.8$ Hz for a close-packed layer of 5 nm nanodiamonds ($\rho_3 = 3.5$ g/cm³; mass per particle 2.29×10^{-19} g; area per particle 21.65 nm², $\rho_2 = 1.058$ mg/cm²). Merging all these particles into a single sphere without any voids would yield a 90 nm diameter particle.

Dybwad observed +1.5 ppm frequency shift upon placement of the 50 nm gold particle on the electrode. From Eq. (5) the corresponding +7.5 Hz shift for a 5 MHz QCM yields $k = 42 \times 10^6$ dyn/cm, which is well below the transition value of $k = Km/M$. Dybwad noted that this value was of the order of a few hundred atomic bonds or a few thousand Van der Waals bonds and did not distinguish between viscoelastic resistance to shear and frictions energy dissipation associated with sliding.

2.2. High Frequency Tribological Investigations on Quartz Resonator Surfaces [8]

Laschitsch and Johannsmann reported in 1999 a study of QCM response to a macroscopic tribological contact by bringing a 3.5 mm diameter brass sphere in and out of a contact with a gold electrode (Figure 2b)[8]. They also studied several other sphere-electrode materials' combinations. Given the macroscopic size of the sphere, the QCM was treated as being in an oscillatory contact with a hard wall and a local elasticity at the contact. Employing the coupled oscillator approach and measuring Δf , these authors found the response to be well described by an increased stiffness of the QCM–sphere system, which for the full contact was reflective of the area of contact and the elasticity of the sphere.

In the range of distances where a contact was just being formed, Laschitsch and Johannsmann detected an additional contribution to the dissipation that was highly dependent on the specific materials in the contact. The authors attributed this to frictional processes associated with the transverse shear oscillatory motion of the contact. To test this hypothesis, they performed measurements on materials combinations that were known to exhibit high (gold on brass) and low (fluoropolymer on fluoropolymer) friction at the macroscale.

Using the loss factor $\Delta I/\Delta f$ as a metric for friction levels, they successfully linked larger values of $\Delta I/\Delta f$ to systems known to exhibit higher macroscale friction coefficients. The work therefore provided a direct means to connect QCM frequency and dissipation response to the macroscale friction coefficients. The loss factor metric as a gauge of macroscale lubricity will be further discussed in the highlights presented herein. See also Refs. [53,54] for closely related studies.

2.3. *An Integrated Force Probe and Quartz Crystal Microbalance for High-Speed Microtribology [9]*

Nearly 20 years after the Laschitsch and Johannsmann study, Borovsky and coworkers employed a similar geometry (Figure 2b) with a 50 mm Al_2O_3 sphere at the tip of a precision-controlled nanoindenter to form a microscopic contact with a gold QCM electrode coated with octadecanethiol (C18) [9]. Their report includes an excellent overview of the various QCM-tip studies inspired by the original Dybwad paper and the evolution of the technique for tribological studies up to 2017.

The QCM apparatus constructed by Borovsky et al. had the capability to measure frictional forces and contact areas over a wide range of applied loads, while maintaining microscopic contacts reaching high sliding speeds near 1 m/s. Nanoscale and microscale comparison studies of friction coefficients for identical materials contacts were reported for 50 μm diameter spheres pressed into the surface with ~ 1 mN loads and 2 μm contact diameters. Contact stiffness values consistent with the prior literature data were also reported. Energy dissipation and lateral contact stiffness were monitored by the QCM, allowing for direct determination of the friction force, friction coefficients, and contact areas. The authors found that the full slip threshold force was by about a factor of two larger than the kinetic friction and identified important transition points between the static and kinetic friction.

The work of Borovsky and coworkers provided detailed insights into measurements of the friction coefficients and contact areas in well-defined micro-contacts. Friction coefficients were calculated for the contacts in the full slip regime achieved at ~ 0.2 m/s velocity in QCM measurements and compared to measurements performed at 25 $\mu\text{m/s}$ velocity for the same contacts in a microtribometer setup. The authors found an agreement between the two systems with velocities spanning over a significant range. They also found the friction forces F_t to increase sublinearly with the load F_N in a close correspondence with the contact area while the shear strengths were relatively insensitive to pressure.

The relation that defines the friction coefficient as the ratio of the friction force to the normal force, $F_t = \mu F_N$, is based on multiasperity contact between the macroscale objects. The area of multiscale contact grows in proportion to the applied force, giving rise to a proportionality with the friction force. For this precision microscopic study, the measurements were performed in a regime of full sliding and a single contact.

2.4. *Partial Slip in Mesoscale Contacts: Dependence on Contact Size [10]*

In a series of publications from 2013 to 2015 Johannsmann and coworkers employed tripod geometry to further establish a link between the QCM nanoscale response to macroscale friction coefficients [10,15]. Their apparatus (Figure 2e) was based on 3 spherical contacts rigidly attached to a support platform upon which further weights can be added. It has several advantages over single sphere geometry (Figure 2d) as it prevents rolling of the spheres and allows for placing the contacts away from the center, where the amplitude of the vibration can more reliably be determined. The authors employed glass spheres from 50 to 275 μm in diameter on polymer surfaces and developed a formalism showing how QCM frequency and dissipation respond to the value of the coefficient of friction of the materials in contact. Focusing on the partial slip regime, they demonstrated that the QCM response had distinct characteristics in the static, partial slip, and full slip regimes. In particular, the authors made use of a Cattaneo-Mindlin (CM) slip model to relate contact stiffness to measurements of the QCM response for a contact with a friction coefficient μ .

The CM model is an approximation that allows for a simplified analysis framework for two curved surfaces that are pressed with a normal load F_N into contact and then sheared tangentially.

Such bodies commonly remain stuck to each other in one part of the contact while slipping in other regions. The authors' approximation treats the contact as a rigid indenter pressed into a flat elastic surface and assumes that the sliding friction in the slip region is governed by a "Coulomb" friction law, $F_f = \mu_k F_N$. For a small amplitude reciprocal motion, the partial slip regime in this model commences at the contact's edge in a form of a thin annulus. The annulus progressively grows as the amplitude of vibration increases. The system transitions to the full gross slippage for a sufficiently large applied tangential force. One central result of this study is depicted in Figure 3, showing the QCM response for a non-slipping contact exhibiting viscoelasticity, a partial slip, and the full slip conditions. Characteristic slopes of Δf and $\Delta \Gamma$ versus the amplitude of oscillations allow for the CM regime to be readily determined. The friction coefficient can then be inferred from the following equations:

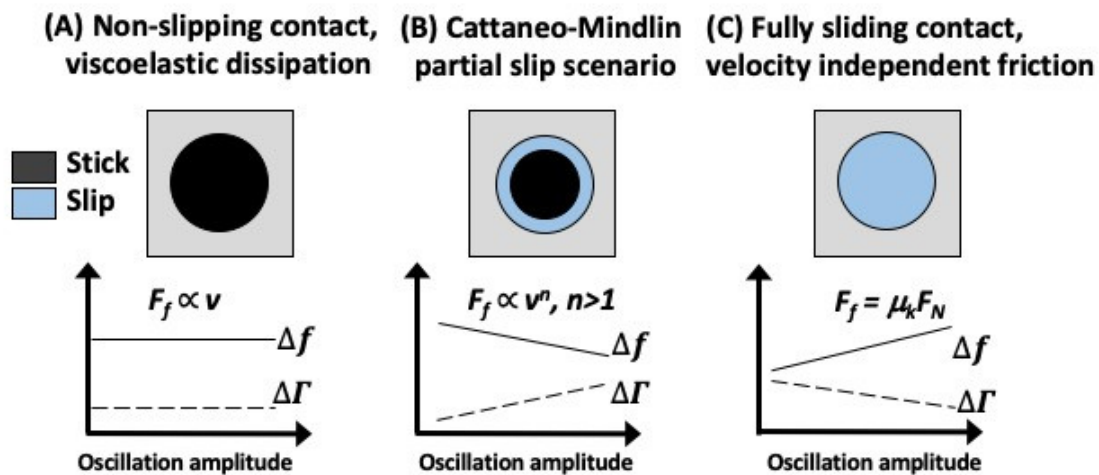


Figure 3. Schematic of the Δf and $\Delta \Gamma$ response of a QCM in three distinct idealized continuum contact conditions. (From Seed et al. [55], and licensed with permission from Creative Commons 4.0. <http://creativecommons.org/licenses/by/4.0>.) (A) a non-slipping viscoelastic contact, (B) a partially slipping contact with the slipping regions governed by a Coulomb friction, and (C) a fully slipping contact governed by a Coulomb friction.

$$\Delta f(u_o) = h - bu_o \quad \Delta \Gamma(u_o) = \frac{4}{3\pi} bu_o \quad (6)$$

$$h = \frac{n_p \kappa}{2n\pi^2 A_{eff} Z_q} \quad b = \frac{n_p \kappa^2}{6n\pi^2 A_{eff} Z_q F_N \mu} \quad (7)$$

where n_p is the number of contacts, μ is the coefficient of friction, and u_o is the amplitude of oscillation at the center of the QCM.

Vlachová et al. later employed the Hanke methodology by varying the amplitude of oscillation while monitoring Δf and $\Delta \Gamma$ [56]. The analysis yielded reasonable values for the friction coefficient μ , but the authors did not compare values obtained from QCM to the results of macroscale measurements for the same set of contacts. See also Ref. [57].

2.5. Correlation of High Frequency QCM Sphere-Plate Stiffness Measurements with Macroscopic Friction Contacts in Thin Film and Bulk Stainless-Steel Materials [11]

In 2020, Seed et al. performed a direct comparison of the QCM response to macroscale friction measurements involving a macroscale ball on disk tribometer as well as the classic "da Vinci" measurement of μ (Figure 2f) [11]. QCM response measurements were carried out in a tripod geometry (Figure 2e) for 2 mm stainless steel sphere ball bearings on stainless steel QCM electrodes. The values inferred from the two different microscale analysis methods (Example 1.4) were compared with the results of QCM measurements. Because the QCM electrodes are fragile and incompatible with some of the direct macroscale tribometers, a series of intermediate measurements were also performed to allow for all the data to be linked and compared. Overall, the results validated the

assumptions collectively employed in the analysis method reported by Vlachová' et al. [56] and yielded friction coefficient values that also compared favorably with the macroscale measurements.

Seed et al. later employed the Example 1.4 analysis to infer macroscale friction coefficients μ for QCMs in both dry and lubricated contacts, with a focus on whether a continuum model is applicable to a complex liquid-nanoparticle-solid interface (Figure 4) [56]. While the QCM results for dry and water lubricated contacts compared favorably with the macroscale friction coefficients, the model failed to adequately describe the contacts lubricated with NP suspensions. The failure, however, was not primarily attributed to the continuum nature of the model but to either lack of a CM slip regime when NPs were present at the interface and/or the fact that the amplitude of the QCM vibration was close in size to the individual NP contacting regions, in violation of one key assumption of the model.

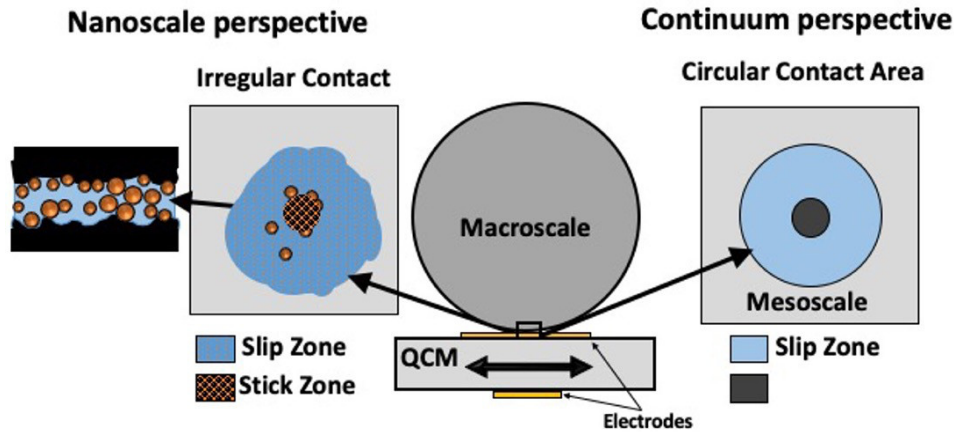


Figure 4. Schematic comparing nanoscale to macroscale perspectives for modeling of a sphere in tribological contact with a QCM electrode. (From Seed et al. [55], and licensed with permission from Creative Commons 4.0. <http://creativecommons.org/licenses/by/4.0/>).

3. Interfacial Slippage Impacts Lubrication in the Mixed and Hydrodynamic Regimes

The examples selected for this section highlight the impact of nanoscale levels of interfacial slippage on macroscale lubricity (Figure 5). Widom and Krim derived expressions in the 1980s for a QCM response to a slipping film layer, where $(V-V_q)$ is the velocity of film adjacent to the surface governed by a viscous friction law $F_f/A = -\eta_2(V-V_q)$: [52]

$$\Delta f = -\frac{2f_0^2 \rho_2}{\sqrt{\rho_q \mu_q}} \frac{1}{(1 + (2\pi f_0)^2 \tau^2)} = \frac{\Delta f_{non-slipping}}{1 + (2\pi f_0)^2 \tau^2}; \quad (8a)$$

$$\Delta \Gamma = \frac{2f_0^2 \rho_2}{\sqrt{\rho_q \mu_q}} \frac{2\pi f_0 \tau}{(1 + (2\pi f_0)^2 \tau^2)} = -2\pi f_0 \tau \frac{\Delta f_{non-slipping}}{1 + (2\pi f_0)^2 \tau^2}, \quad \frac{\Delta \Gamma}{\Delta f} = -2\pi f_0 \tau, \quad (8b, c)$$

where $\tau = \rho_2/\eta_2$ is a "slip time" associated with the interfacial friction coefficient η_2 [52]. Eqs. (8) imply that the magnitude of Δf for a slipping film layer is less than that of a rigidly attached film, Eq. (1). When immersed in liquid, the QCM response is also sensitive to the interfacial slippage (Figure 5c), and the response can be linked to the macroscale lubricity in mixed and hydrodynamic regimes. Further reading on the topic of interfacial slip, solid-liquid, slip and nanosuspensions may be found in Refs. [36–40].

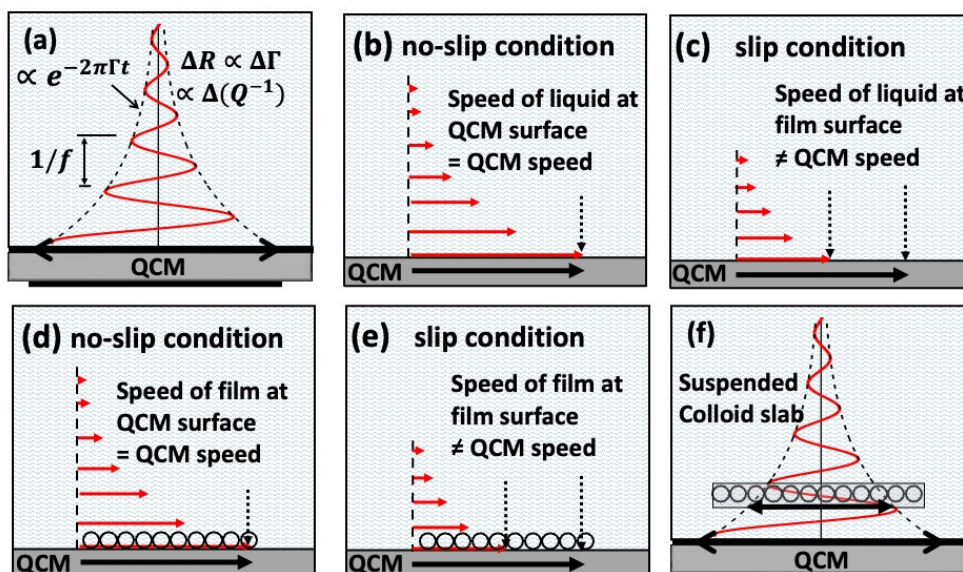


Figure 5. QCM response and interfacial slip geometries considered in this section that are particularly relevant to the hydrodynamic regime of lubrication.

3.1. Slippage at Adsorbate–Electrolyte Interface. Response of Electrochemical Quartz Crystal Microbalance to Adsorption [12]

Daikhin et al. employed a QCM immersed in water or butanol to study adsorption of pyridine as an additive and reported the results in this 2000 publication [12]. In non-slip conditions (Figure 6d) the total response of the QCM is:

$$\Delta\Gamma = \frac{f_0 \sqrt{\pi \rho_l \eta_l f_0}}{\sqrt{\rho_q \mu_q}}; \Delta f = -\frac{f_0 \sqrt{\pi \rho_l \eta_l f_0}}{\sqrt{\rho_q \mu_q}} - \frac{2f_0^2 \rho_2}{\sqrt{\rho_q \mu_q}}, \quad (9)$$

where the second term in Δf corresponds to the rigidly attached film as described by Eq.(1) and the remaining term is accounting for the contribution of the bulk fluid with viscosity η_l and density ρ_l . In practice, the QCM is first immersed in a bulk fluid and then, after a period of stabilization, the response is monitored as an additive is introduced to the bulk. Under these conditions, an uptake of pyridine is expected to result in a formation of a rigid film and, therefore, described by Eq.(1). However, the authors found that the experimentally observed shifts could not be explained in terms of a mass change in the adsorbed layer rigidly coupled to the oscillating surface. The mass-loading term in Eq. (9) could not be trivially replaced by Eq. (8) to incorporate the boundary slippage, since the slippage of a film in contact with the bulk also impacts the bulk contribution term significantly. Daikhin et al. therefore developed a model where the rigidly attached adsorbate molecules were replacing solvent molecules and a slip was allowed at the solvent interface. This “electrolyte” model incorporated both a rigid film and a bulk phase, but also allowed for the slip to occur only at the upper boundary of the film with the fluid phase.

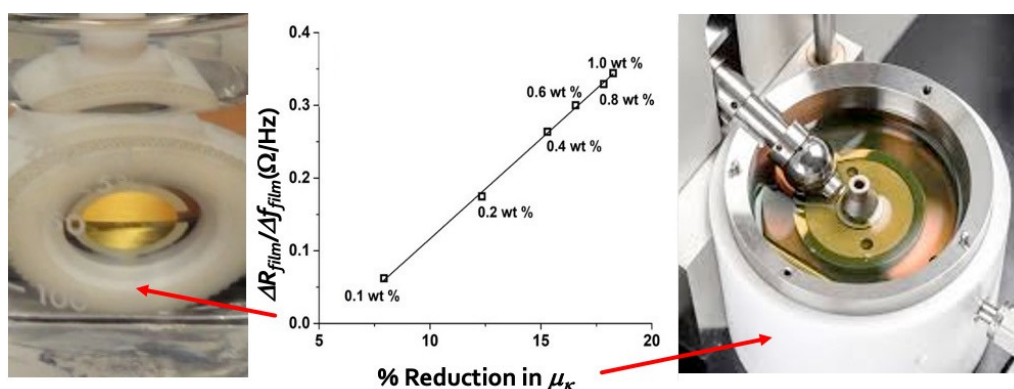


Figure 6. QCM loss factor measurements versus reduction in macroscale friction coefficients measured in a macroscopic setup for iron oxide particles added to water over a range of 0.1 to 1 wt %. The quantity $\Delta R_{film}/\Delta f_{film} \propto \Delta \Gamma_{film}/\Delta f_{film}$. Images depict QCM and macroscopic setup geometries for gold contacts. Measurements reported by Pardue et al. [14] were performed with alumina contacts. Image credit: J. Krim

Boundary slip was incorporated by inserting the velocity of a monolayer adjacent to the boundary governed by a friction law $F_f/A = -\eta_2(V - V_q)$ in place of the no-slip condition $V = V_q$:

$$\rho_2 \frac{d}{dt} V_f(t) = -\eta_2[V(t) - V_q(t)]. \quad (10)$$

The QCM response was then obtained by solving the system of equations of motion. After some rearrangement of terms, the results can be expressed as:

$$\Delta \Gamma = \frac{f_0 \sqrt{\pi \rho_l \eta_l f_0}}{\sqrt{\rho_q \mu_q}} \cdot \left[\frac{1 + 2a}{(1 + a)^2 + a^2} \right] \Delta f = -\frac{f_0 \sqrt{\pi \rho_l \eta_l f_0}}{\sqrt{\rho_q \mu_q}} \cdot \left[\frac{1}{(1 + a)^2 + a^2} \right] - \frac{2f_0^2 \rho_2}{\sqrt{\rho_q \mu_q}}, \quad (11)$$

where a is the ratio of the slip length λ_s to the penetration depth δ of the oscillations in a liquid. For fluids with uniform density the parameter a is related to η_2 as $\lambda_s = \eta/\eta_2$. Other parameters commonly employed in the literature to represent the boundary slip of a liquid are the slip parameter $s = 1/\eta_2$, which has units of $\text{cm}^2\text{s/g}$, and the parameter $\chi = 1/\tau$, which has units of s^{-1} . For a no-slip boundary condition at the film-fluid boundary, $a=0$ and the response reduces to the sum of the separate non-slipping film and bulk contributions, Eq. 9.

Eq. (11) describes a QCM response upon immersion into a liquid and allows one to infer adsorption levels and slip lengths from the experimental data. For pyridine added to water, typical values of surface uptake were about $5 \times 10^{10} \text{ mol/cm}^2$ with slip lengths of about 0.8 nm. Slip lengths were larger for water than butanol, approaching 2 nm for the highest concentrations of the adsorbate molecules. See also Refs. [39,58] for further details. Ref. [39] is a book chapter with a comprehensive discussion and an explanation of QCM in liquid with slipping interfaces, while Ref. [58] details examples of slip length calculations and mass uptake for nanoparticle suspensions employing the results of Daikin et al. and related methodologies.

3.2. A Low Friction Bearing Based on Liquid Slip at the Wall [13]

In this 2007 publication, Spikes and colleagues explored macroscale implications of bearing lubrication when the surfaces in a macroscopic tribological contact were configured so that the lubricating liquid exhibited a slip on one of the contacting surfaces and a no-slip boundary condition on the counterface [13]. They noted that the nanoscale slip had been firmly established in the decade prior to their work and that there was no intrinsic reason why a fluid is forbidden to slip at an interface. Non-wetting fluids, i.e., those in a contact with lyophobic surfaces, are expected to exhibit some degree of slippage while surfaces wetted by the lubricant should exhibit non-slip conditions. This publication described a bearing design and demonstrated that a conventional wetted surface draws a lubricant fluid into the contact to achieve hydrodynamic lubrication conditions. The counterface is prepared with a treatment that inhibits wetting by the lubricant, in turn giving rise to interfacial slippage at one of the contacts.

The authors cited a previous theoretical work based on a half-wetted bearing principle (i.e., only one of the contacts is wetted by the lubricant) indicating that the friction could be significantly reduced in the lubricated sliding contacts [59,60], and then reported their experimental validation of the theoretical concept, which makes possible hydrodynamic lubrication of very low load contacts. They constructed a low load bearing and explored the influence of the surface roughness and the wetting properties of the surfaces on friction over a wide range of sliding speeds to construct Stribeck curves for various conditions (Figure 1). For the materials studied (hexadecane films in the contact between a rotating Pyrex cylinder and a stationary, sapphire flat), the authors concluded that the liquid slip can be used to considerably reduce friction under the full film hydrodynamic conditions. Based on the friction *versus* speed curves and numerical modeling of the contact, the authors

identified the range of the test conditions resulting in a thick-film hydrodynamic lubrication. They considered three possible origins of the observed tribological behavior and concluded that the most likely explanation was a slippage of the hexadecane along the smooth lyophobic coated sapphire surface. The latter exhibited friction coefficients of ~ 0.001 at 1 m/s and 0.2 N. This value compares favorably with the friction coefficient of ~ 0.003 and the slip lengths of ca. 4 mm observed for smooth incoated surface of lyophobic sapphire with the non-wetting contact angle measuring 109° .

3.3. A tribological Study of Aqueous Suspension of $\gamma\text{-Fe}_2\text{O}_3$ Nanoparticles [14]

In this 2018 report by Pardue et al. compared and contrasted nano- *versus* macroscale tribological properties of aqueous suspensions of maghemite ($\gamma\text{-Fe}_2\text{O}_3$) nanoparticles in a contact with alumina surfaces for various nanoparticle concentrations [14]. A QCM with an alumina electrode was employed for the nanoscale measurements while an alumina ball on alumina disk geometry was employed for the macroscale friction coefficients' experiments. The nanoparticle concentrations were increased stepwise and changes in friction and drag forces were monitored using both the QCM and a macroscale tribometer.

Several potential QCM "bulk" and "surface" "performance factors" were selected from functions of Δf and ΔR_m upon addition of nanoparticles to water surrounding the QCM, where R_m is the motional resistance and $R_m = \Delta\Gamma / (8K_0^2 C_0^2 f)$, C_0 is the static capacitance between the electrodes and $K_0^2 = 7.74 \times 10^{-3}$ is the electromechanical coupling factor for the AT-cut quartz crystal. A number of candidate functions were assessed, and the factor $\Delta R_{\text{film}} / \Delta f_{\text{film}}$ was observed to exhibit a linear correlation with reductions in the macroscale friction coefficient. The authors attributed this to interfacial effects and changes in the glide plane location upon introduction of nanoparticles – the two factors that would impact both nanoscale and macroscale friction (Figure 6). Notably the macroscale measurements were performed in a mixed lubrication regime, indicating the impact of slippage on the friction coefficient is not confined to the hydrodynamic lubrication regime.

Surface excess quantities were defined as differences between the experimentally measured shifts $\Delta\Gamma_{\text{exp}}$ and Δf_{exp} and the changes $\Delta\Gamma_{\text{ns}}$ and Δf_{ns} attributable to an increased viscosity η_{ns} and density ρ_{ns} of the bulk suspension when nanoparticles were added:

$$\Delta\Gamma_{\text{ns}} = -\Delta f_{\text{ns}} \Delta f_{\text{ns}} = \frac{f_0 \sqrt{\pi f_0}}{\sqrt{\rho_q \mu_q}} (\sqrt{\rho_l \eta_l} - \sqrt{\rho_{\text{ns}} \eta_{\text{ns}}}) \quad (12)$$

Both the average density and viscosity of the bulk fluid increase upon addition of NPs. Eq. (12) therefore indicates negative frequency shifts and positive band width shifts upon addition of NPs. The authors observed the "film" loss factor to scale linearly with reductions in macroscale friction coefficient, with correlation 0.999, defined as:

$$\frac{\Delta\Gamma_{\text{film}}}{\Delta f_{\text{film}}} = \frac{\Delta\Gamma_{\text{exp}} - \Delta\Gamma_{\text{ns}}}{\Delta f_{\text{exp}} - \Delta f_{\text{ns}}} \quad (13)$$

The factor in Eq.(13) was notably observed to be positive, since both the numerator and the denominator were observed to be positive: an addition of nanoparticles to the liquid surrounding the QCM caused a *decrease* in the half band width, which was attributed to slippage.

Atomic force microscopy was also utilized to both qualitatively and quantitatively determine surface roughness before and after the particle uptake. It was observed that the particles were easily removed from the surface without significantly altering surface morphology.

3.4. Nanotribological Performance Factors for Aqueous Suspensions of Oxide Nanoparticles and Their Relation to Macroscale Lubricity [15]

In 2019, Krim, Smirnov and coworkers extended the initial studies reported by Pardue et al. to a wide range of materials system combinations and reported the QCM performance factors along with selected comparisons to macroscale friction coefficients [15]. Aqueous suspensions of four ceramic nanoparticles, TiO_2 , SiO_2 , Al_2O_3 , and maghemite ($\gamma\text{-Fe}_2\text{O}_3$) and ten substrate materials (Au, Al, Cr, Cu, Mo, Ni, Pt, SiO_2 , Al_2O_3 , and stainless steel SS304) were studied. The variations in QCM response from one nanoparticle composition to another were observed to be far greater than from changes in the substrate material, indicating that the properties of nanoparticles are playing a larger

role in determining the frictional drag force levels than the substrates. The results were categorized according to the direction of the frequency and motional resistance changes and candidate statistical performance factors for the datasets were generated. Shift in frequency upon introduction of nanoparticles were observed to be zero, negative, or positive, depending on the degree of decoupling of the bulk fluid attributed to the interfacial slippage.

The performance factors were employed to identify associations between the QCM atomic scale results and the macroscale friction coefficient measurements. Macroscale measurements of friction coefficients for selected systems documented that a reduction or an increase in motional resistance to shear, as measured by the QCM, is linked to a decrease or increase, respectively, in the macroscale friction coefficients. The performance factors identified in the study of a single materials combination reported in 3.3 therefore were shown to be applicable to a broader set of statistically diverse samples. The authors concluded that sophisticated treatments are required to analyze the full implication of the results, given the wide-ranging values. The range of applicability for sliding speeds also remained an outstanding question for future studies.

3.5. Load impedance of Immersed Layers on the Quartz Crystal Microbalance: A Comparison with Colloidal Suspensions of Spheres [16]

In this 2020 publication, Melendez et al. considered a slab suspended at a distance d above an oscillating QCM electrode immersed in a bulk liquid (Figure 5f) [16]. Transverse shear waves propagating into the liquid with a heavy damping were characterized by a penetration depth d in the absence of the slab (Figure 2a). The slab was treated as both a continuous plate with thickness a and a density ρ' , and also as an array of spheres with diameter a . The location and dimensions of the slab were found to impact the degree to which it oscillates in a transverse shear motion, and the degree to which it changed the acoustic load on the QCM in a slab-free liquid. No-slip boundary conditions were applied to the solid-liquid boundaries at the QCM and the slab surfaces, and an expression was derived for the extra impedance due to the presence of the slab. Employing this no-slip geometry, the authors demonstrated that positive frequency shifts associated with decoupling of the bulk fluid occur in some regimes.

When an oscillating electrode of the QCM is exposed to a mass loading and/or a surrounding fluid, the acoustic impedance $Z = \mathcal{R} - i\mathcal{X}$ results in shifts to Δf and $\Delta \Gamma$ as:

$$\Delta \Gamma = \frac{\mathcal{R}f_0}{\pi\sqrt{\rho_q\mu_q}}; \Delta f = -\frac{f_0\mathcal{X}}{\pi\sqrt{\rho_q\mu_q}} \quad (14)$$

The authors derived an expression for an additional impedance arising from the presence of the slab in terms of dimensionless parameters ρ'/ρ , a/δ and d/δ .

$$\frac{Z_L}{Z_{ref}} = \frac{e^{-2(1-i)d/\delta}}{\left(\frac{1+i}{2}\right)\frac{\rho'a}{\rho\delta}(e^{-2(1-i)d/\delta} - 1) - 1} \quad (15)$$

where $Z_{ref} = -i2\pi f_0\rho_2$, is the impedance of a rigidly attached layer (the Sauerbrey Eq. (1)), and ρ_2 is the mass per unit area of the slab or the mass per unit area of the array of spheres with radius R . The analytical solutions derived in this example indicated positive frequency shifts upon introduction of suspended colloids for certain regimes, which the authors referred to a “negative acoustic mass” because mass-loading according to Eq.[1] results in a negative shift (Figure 7).

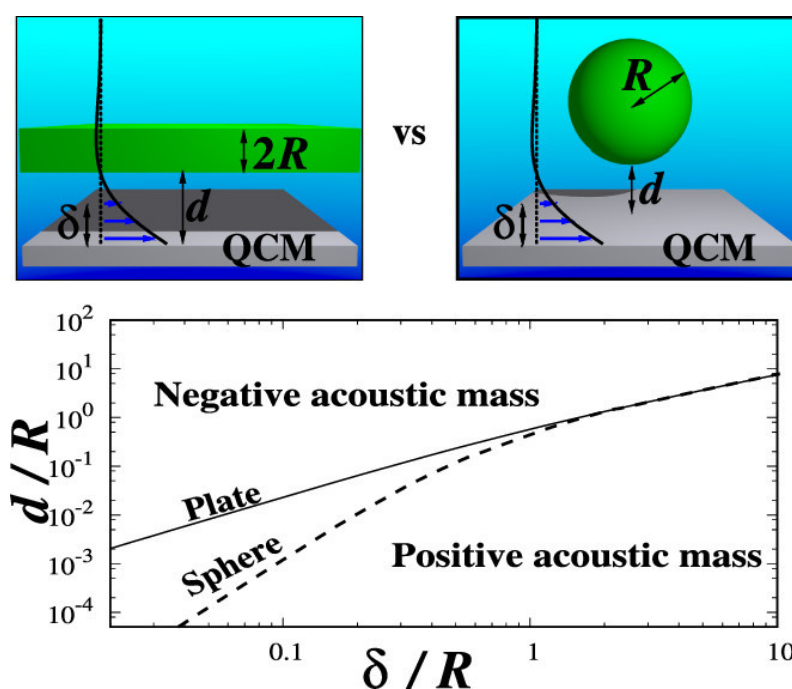


Figure 7. Regimes of positive (“negative acoustic mass”) and negative (“positive acoustic mass”) frequency shift for plate and sphere geometries in terms of the unitless quantities d/R and δ/R . The results demonstrate that mass loading does not always result in a negative frequency shift for NPs added to liquids. (From Melendez et al. [16]) and licensed with permission from Creative Commons 4.0 (<http://creativecommons.org/licenses/by/4.0>).

The authors noted that the Dybwad double oscillator contact methodology of the Section 2.1 has been used extensively in studies of colloids, and recommended the hydrodynamic approach of their work as a preferable methodology. The authors also compared the one-dimensional immersed plate theory with three-dimensional simulations of rigid and flexible submicron-sized suspended spheres, as well as with experimental results for adsorbed micron-sized colloids in the “negative acoustic mass” where frequency shifts are negative. One of the important conclusions of this work was a call for a revision of the existing theories, which are currently based entirely on adhesion forces and elastic contact stiffness, to include hydrodynamics. See also Ref. [61] where QCM response to an immersion in a flowing, rather than static, liquid was explored.

4. Nanoparticle Rolling has Little Influence and When Present May Increase Friction

Close to thirty years have passed since the pioneering work of Campbell et al. who utilized a surface forces apparatus to study intermolecular interactions and nanotribology of adsorbed C_{60} monolayers on mica surfaces immersed in toluene [1]. The results have raised a speculation that observed molecular “ball-bearing”-like attributes might give rise to macroscale lubricity, since C_{60} molecules are near-perfect spheres and when contacting crystalline solids, the molecules could rotate rapidly while remaining in their lattice positions (Figure 8). Campbell et al. noted that such lubricity was not observed for C_{60} alone, including control molecular scale experiments performed in air using 50 nm C_{60} films deposited on mica [1]. However, these authors discovered that the deposition of one or two weakly bound monolayers atop mica surfaces resulted in the full-slip (zero interfacial friction, within the detection limit of the apparatus) boundary conditions when immersed in a C_{60} additives suspension. The observed tribological behavior was dramatically different from that of conventional fluids. The authors concluded that C_{60} could hold a great promise as a macroscale lubricant additive and suggested the interfacial slippage might be linked to a rapid rotation of the molecules that somehow produced an effective boundary of near zero drag on the adjacent liquid.

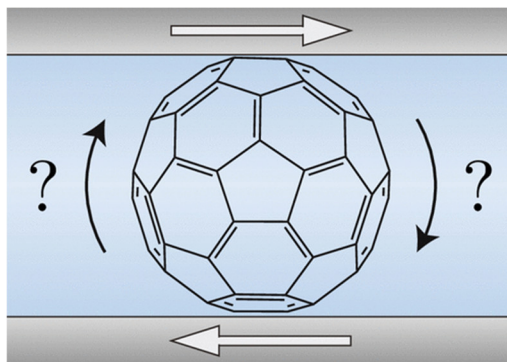


Figure 8. Schematic of a C_{60} molecule in a sliding contact with two surfaces. Reprinted with permission from [18]. Copyright 2018 American Chemical Society. Speculation that rotation of the soccer-ball shaped molecule may reduce friction levels triggered an interest in spherical additives (molecular and NP) for decades.

While the notion of molecular ball-bearings may be intuitive as a nanoscale mechanism for friction reduction for both C_{60} and NP additives, the current consensus is that the profound changes in the interfacial slippage and friction are not attributable to molecular rotation. When present, the rotation may actually increase friction, as highlighted by the examples in this section. Further reading on the topic of carbon materials as lubricant additives may be found in Refs. [41,42].

4.1. C_{60} molecular Bearings and the Phenomenon of Nanomapping [17]

In 2001 and 2006, Coffey and coworkers reported a set of nanotribological measurements of C_{60} employing atomic force microscope (AFM) and quartz crystal microbalance (QCM) techniques. AFM failed to detect C_{60} at the toluene/mica interface by yielding friction levels that were unchanged by the presence of C_{60} additives. The authors suggested that C_{60} was easily displaced from the interface by the slow-moving AFM probe tip and, therefore, no effects of the C_{60} additive on the interfacial friction were observed such experiments. In contrast, QCM measurements of interfacial friction and slippage for toluene/Ag(111) interface were highly sensitive to the presence of interfacial C_{60} . **The friction however doubled** when C_{60} was deposited as a film onto the Ag(111) surface in advance of the tribological experiments.

To explore and isolate the role of molecular rotation on friction, Coffey and Krim measured sliding friction on fixed and rotating C_{60} layers by preparing substrates upon which the C_{60} molecules rotated at a high rate (10^9 - 10^{10} Hz), a slow rate (< 1 Hz), or did not rotate at all (Figure 9). Sliding friction for methanol on various substrates was measured at room temperature, and for krypton layers at 77 K. At the latter temperature all rotations are known to cease. To the best of our knowledge this was the first experimental report to directly link friction to a documented molecular rotation state. *The observed friction was, however, higher when the C_{60} was rotating, in defiance of the ball-bearing analogy.* See also Ref. [62].

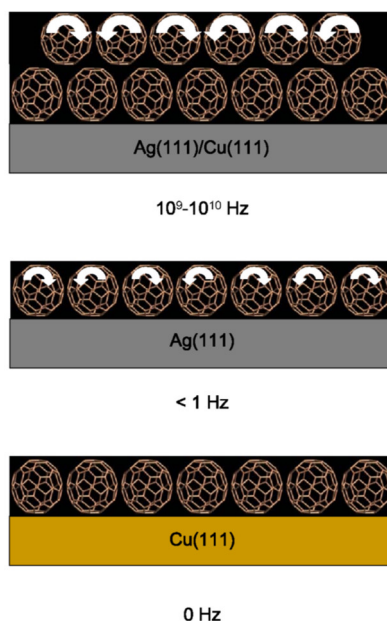


Figure 9. Schematic of the QCM experiment reported in Ref. [17]. On Ag(111) or Cu(111), C_{60} molecules in the 2nd layer rotate rapidly in random independent directions. On Ag(111), the molecules in the 1st layer ratchet slowly between the preferred orientations, while on Cu(111), they do not rotate at all. The interfacial slippage is observed to be higher for the non-rotating case of Cu(111). Reprinted with permission from [17].

4.2. Are Buckminsterfullerenes Molecular Ball Bearings [18]?

The topic of rotation by C_{60} molecules was revisited in 2019 by Lhermerout *et al.*, twenty years after the original Campbell publication. The authors employed a surface force balance method to study C_{60} additives to tetralin and reported the first quantitative friction force measurements of C_{60} dispersed in between surfaces in the boundary regime of lubrication. As such, the study was complementary to the hydrodynamic regime measurements reported by Campbell *et al.* in a system with geometry more directly comparable than the one employed by Coffey *et al.* [17,62].

Lhermerout *et al.* noted that C_{60} molecules freely rotate at room temperature not only when dissolved in a liquid but also in a solid state and examined whether the molecules could prevent contact in the boundary regime while simultaneously dissipating shear stress through fast rotation. High-resolution shear and normal force measurements between mica sheets separated by 0.1 wt% C_{60} solutions were performed in a single asperity contact geometry and with sub-nanometer resolution in film thickness. The authors observed that C_{60} forms a solid-like amorphous boundary film sustaining a high normal load that suggests that the system undergoes a glass transition when confined. Overall, the C_{60} films were deemed to be excellent boundary lubricants and, up to moderate applied loads, exhibited low friction coefficients. The fact that the molecules were readily trapped in contacts was attributed to them being close to an aggregation while in solution, with the solvent squeezed out when the contact was made.

The authors discussed rotation extensively throughout the publication, and suggested that, among other possibilities, a lubrication mechanism involving the molecules rotating while in a glass phase cannot be ruled out because of the available space for such rotations. *It was concluded that although rotation may be important, a comparative study of fixed (via chemical grafting) and rotating molecules would be required to clarify the role of rotation.* While this study found C_{60} to be a beneficial lubricant additive for systems in the boundary regime, no specific evidence that molecular rotation impacted the friction levels was obtained.

4.3. Friction Properties of Carbon Nanoparticles (Nanodiamond and Nanoscroll) Confined between diamond Like Carbon and α -SiO₂ Surfaces [19]

In this study, Zhao et al. compared tribological properties of carbon nanoparticles including nanodiamonds (NDs) and nanoscrolls (NSs) formed by wrapping graphene sheets around nanodiamonds. The authors performed nonequilibrium molecular dynamic simulation of sliding diamond-like carbon over the nanoparticles supported by amorphous silica slabs (Figure 10). The friction coefficient for sliding of nanoscrolls was observed to be 72% lower than that of the nanodiamonds and found to be in a regime of superlubricity ($\mu \leq 0.01$) consistent with the experimental observations.

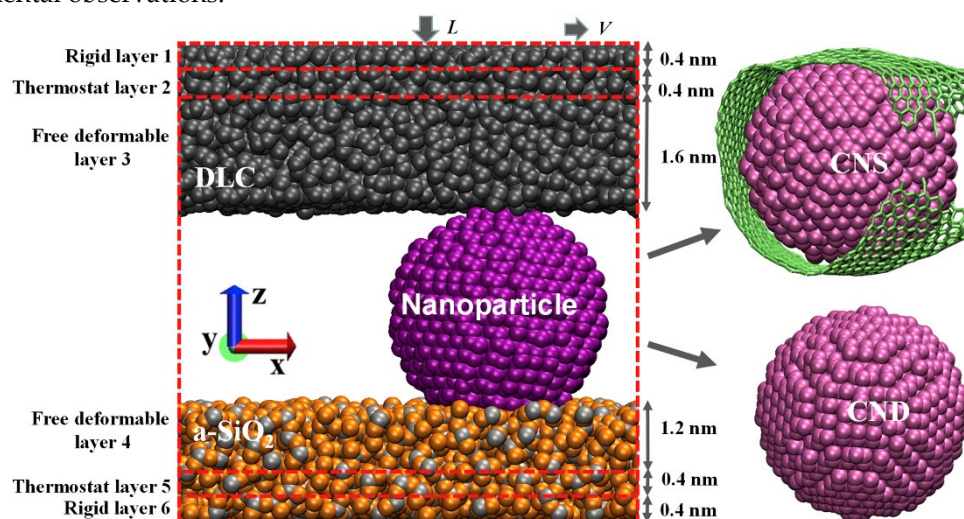


Figure 10. Illustration of the carbon nanodiamonds (NDs) and nanoscrolls (NSs) formed by wrapping graphene sheets around nanodiamonds whose tribological properties were studied by Zhao *et al.*. Reduced friction levels for the nanoscrolls were attributed to the lack of rolling motion in combination with a lower contact area. Reprinted with permission from Zhao *et al.*, Ref. [19].

The lower friction for the nanoscroll-diamondlike carbon combination was attributed to a lower contact area as well as a lack of rolling motion, both attributed to the presence of the graphene patch surrounding the nanodiamond. *The authors concluded that in contrast to the rolling motion of ball bearings at the macroscale, the repression of rolling motion of nanoparticles at the nanoscale reduces the system friction dissipation.* They conclude that nanoscrolls should be more effective as a solid lubricant *versus* nanodiamonds. Although the study was not performed in suspension, we note that the results should be applicable to the boundary regime of lubrication, in cases where solvents are squeezed out of the contact.

4.4. Addition of Solid Oxide Particles for Friction Reduction [20]

Van Sang et al. performed numerical simulations consisting of a combined SPH/DEM method to explore lubrication mechanisms of 20 types of micron-sized oxide particles added to water or diesel-based fluids in iron contacts. The rough on flat iron contacts and spherical iron oxide particles were respectively modeled by elastic particle lattice coarse-graining and discrete element methods. The interactions between the iron-oxide surfaces with the various oxide particles, as well as the particle-particle interactions included both Hertz repulsive contacts and attractive van der Waals forces for non-contacting separation distances. Friction was determined by assessing the kinetic energy dissipated into the environment via Stokes damping forces. The authors found that the stability and shear properties of films formed on the iron surfaces dominated friction reduction levels, and that denser and/or heavier oxide particles resulted in better lubricity. Friction was also reduced for an increasing number of particles in the tribofilm and the sliding speed. Although the nature of the surrounding fluid and temperature strongly influenced the overall friction levels, the relative ranking of lubricity amongst the various oxides studied was observed to be almost independent of

the base fluid. *Van der Waals forces were meanwhile found to have very little effect on lubricity and rolling of the particles had almost no effect whatsoever.*

The friction coefficient for bare contact was 0.32, and all the particles, including iron oxides, reduced the friction coefficient. The rank ordering of lubricity for the oxides in this study was Bi_2O_3 , CeO_2 , SnO_2 , WO_3 , Co_3O_4 , CuO , CoO , FeO , ZnO , Cr_2O_3 , ZrO_2 , Fe_2O_3 , Fe_3O_4 , Y_2O_3 , Al_2O_3 , TiO_2 , MgO , V_2O_5 , BeO , SiO_2 , with Bi_2O_3 providing the largest reduction ($m = 0.04$) and SiO_2 the least reduction ($m = 0.22$).

4.5. Functionalized Carbon Nanostructures as Lubricant Additives – A Review [21]

In this comprehensive review of carbon nanostructures as lubricant additives, Nyholm et al. described the state of the field as of 2023 and identified the most promising future research areas. Additive dimensionality, structural integrity, and the nature of chemical interactions were identified as particularly important properties governing the tribological behavior. The theoretical basis for fundamental lubrication mechanisms revealed that much was yet to be understood. Nonetheless, the authors concluded that two-dimensional graphene-based nanostructures and carbon quantum dots are the likely most promising candidates for a new generation of lubricant additives due to their excellent properties as carrier materials and the well-established chemistry of carbon (Figure 11). These attributes were identified as particularly important for customization of additives through surface functionalization to achieve wide-ranging and beneficial surface properties. The authors also commented that the surface functionalization of nanomaterials, a key component of the samples presented in the first highlight of the next section, has the potential to impact both the dispersibility and the inherent lubrication mechanisms of the nanostructure, enabling development of multifunctional additives.

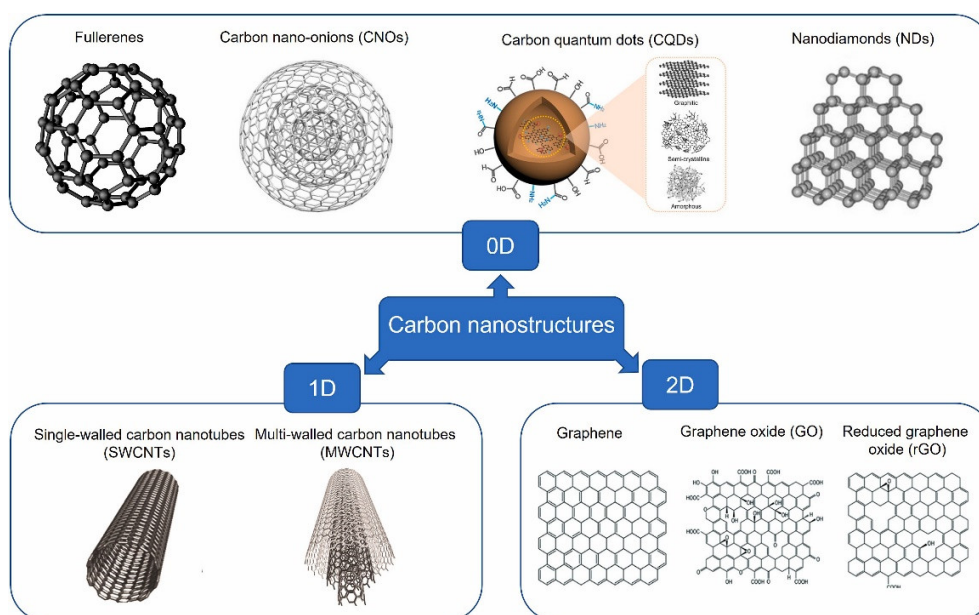


Figure 11. An overview of the carbon nanostructures considered in Ref. [21] and classified according to their dimensionality. 0D and 1D structures are potentially capable of rolling in tribological confinement, but no benefits of rolling were identified. From Nyholm et al. [21], and licensed with permission from Creative Commons 4.0. <http://creativecommons.org/licenses/by/4.0>.

Notably, after an exhaustive and in-depth discussion and review of carbon-based lubricant additives, the authors found no evidence to document rolling as a beneficial mechanism to reduce friction and commented on the difficulty of achieving the rolling motion for nanoscale structures, such as 1D carbon nanotubes (CNTs), in the first place. It was concluded that *“even though there is some theoretical support for the rolling ability of certain 0D carbon nanostructures, it is uncertain*

whether this contributes to reducing the interfacial friction between tribosurfaces to any significant extent" [21].

"After critically reviewing the fundamental research available at present date, the roller bearing ability of 1D CNTs is also deemed unlikely for several reasons....., even if all the aforementioned challenges (e.g., entanglement, need for commensurability, structural collapse, etc.) were minimized or eliminated in a way such that rolling motion of CNTs was more plausible, it is still unclear whether this would contribute to friction reduction in any significant way" [21].

5. Surface Charge on Nanoparticles and Contacting Surfaces and the Surface Groups that Give Rise to the Charge Have an "Astonishing" Impact on Friction

The prior example of the effects of carbon nanostructures on friction highlighted a review article that emphasized a major observation of surface functionalization of nanomaterials having a pivotal role in both particle dispersibility and the lubrication mechanisms. It is well documented that the surface charge, causing electrostatic repulsion between the nanoparticles, enables suspension stability [2,42,45,49]. The repulsive interactions also impact lubrication through changes to slip planes and/or counteracting externally applied normal forces. Some nanoparticle materials, but not all, become charged when added to lubricants (Figure 12) while other require additional surface treatments to render them charged and/or provide steric repulsion. The articles selected for this section highlight the major impact of the nanoparticle surface charge on lubricity.

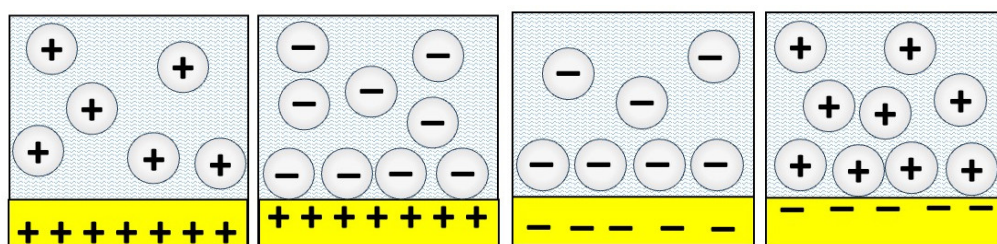


Figure 12. Substrates immersed in lubricants routinely acquire surface charge. Nanoparticle additives to lubricants also routinely become charged, either naturally or through surface functionalization to prevent agglomeration. The resulting electrical interactions, repositioning of particles, and size changes arising from the thickness of the surface functionalization layer collectively impact the system's tribological properties.

5.1. Tribological Properties of Nanodiamonds in Aqueous Suspensions: Effect of the Surfaces Charge [22]

Liu et al. monitored the frequency and dissipation of QCMs with gold electrodes immersed in aqueous suspensions of positive and negatively charged detonation nanodiamonds (NDs) [22]. Surface charge and nanoparticle end groups were varied by preparing them via either a reduction reaction for the case of the positive (hydroxylated) particles or alternatively an oxidation of a soot in ozone-enriched air for the case of the negative (carboxylated) particles. The size dependence of the negatively charged ND was studied for 5, 10, and 15 nm particles. Tribological contact with macroscale spheres was also studied for both -ND and +ND by placing stainless steel ball bearings atop the QCM electrode in a contact with the nanosuspension as depicted in Figure 2a.

NDs were found to have a profound effect on the tribological performance as assessed by both the nanoscale QCM studies and the macroscopic experiments of lubricated contacts with ball bearings. The tribological effects were also strongly influenced by the sign of the surface charge, with negatively (positively) charged particles exhibited weaker (stronger) adhesion. The QCM results consistently indicated that positively charged particles increased friction at the solid-liquid interface, while negatively charged particles of comparable size were observed to decrease the interfacial friction and increase the interfacial slippage. For macroscopic contacts with gold electrodes, -NDs appeared to be displaced from the contact, while +NDs were not. Zeta potential of as-prepared -NDs was varied from -35 to -45 mV depending on the size while 5 nm as prepared +NDs exhibited +33.4±2.1 mV potential. The smaller magnitude of the Zeta potential of +NDs was likely responsible

for lesser stability of the corresponding suspensions vs. those composed of -NDs. In a follow-up study, the same group compared QCM nanoscale nanotribological data with macroscale tribological attributes of alumina and stainless-steel surfaces measured using a commercial macroscale tribometer. Immersion of the contacts in -ND suspensions resulted in a decrease in the macroscopic friction coefficients to values in the range 0.05–0.1 for both stainless steel and alumina, while +ND suspensions caused an increase in friction for stainless steel contacts and little to no increase for the alumina contacts. Quartz crystal microbalance (QCM), atomic force microscopy (AFM), and scanning electron microscopy (SEM) measurements were employed to assess nanoparticle uptake, surface polishing, and resistance to solid–liquid interfacial shear motion. The QCM studies revealed abrupt changes to the surfaces of both alumina and stainless steel upon adding -NDs to lubricating water – the effects consistent with a strong attachment of NDs and/or chemical changes to the surfaces. The authors suggested that carboxylated -NDs in aqueous suspensions may be forming robust lubricious deposits on stainless and alumina surfaces that enabled gliding/slippage through the surrounding -NDs. In stark contrast, +ND suspensions not only failed to improve tribological performance but potentially abraded the existing protective boundary layers for the case of stainless-steel contacts. To conclude, the authors reported radically different tribological properties at both the nanoscale and macroscale for the two different surface treatments of the same nanoparticles. Such reports are increasingly common, as highlighted in the next example.

5.2. Astonishingly Distinct Lubricity Difference between the Ionic Liquid Modified Carbon Nanoparticles Grafted by Anion and Cation Moieties [23]

Wang et al. reported macroscale measurements of friction coefficients in a macroscale reciprocating tribometer for another carbon-based nanoparticle additive - carbonnanoparticles (CNPs) prepared by pyrolysis [23]. Like NDs the CNPs studied were formed from carbon but the latter demonstrated poor crystallinity based on the XRD analysis. The CNPs were further treated to yield oppositely charged end groups. The nanoparticles were employed as 0.7 wt% additives to polyethylene glycol (PEG200) – a synthetic oil with biodegradability - and the difference in lubricity between the two treatments was described by the authors as “astonishingly distinct” (Figure 13).

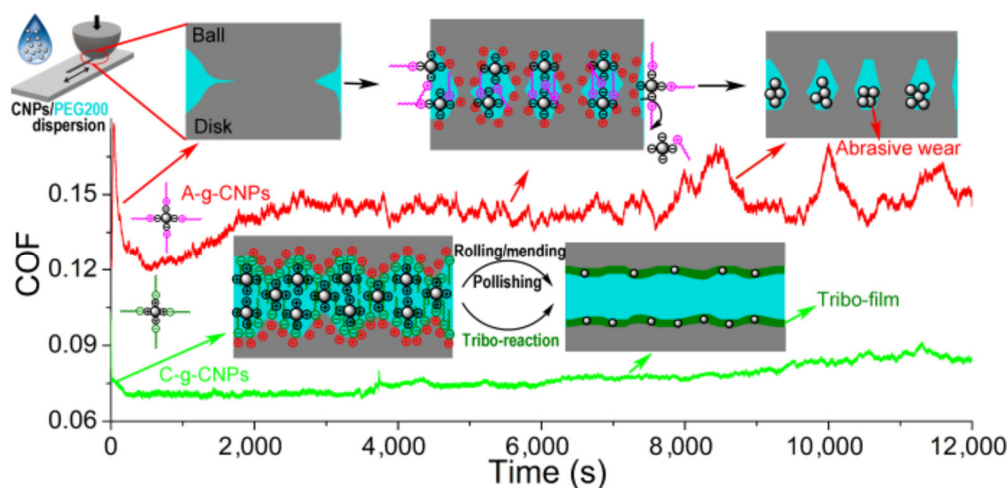


Figure 13. Coefficient of friction (COF) versus time for a 100 N load in a reciprocating tribometer and schematic plots of the lubrication mechanisms of positively charged carbon nanoparticles (C-g-CNPs) and negatively charged carbon nanoparticles as 0.7 wt% additives to PEG200. Reprinted from Wang et al. [23]) and licensed with permission from Creative Commons 4.0 (<http://creativecommons.org/licenses/by/4.0>).

Positive CNPs, designated as A-g-CNPs, were prepared by preferential electrostatic adsorption of negatively charged inner parts with repulsive peripheral cation end groups. These additives were found to have little effect and/or actually to impair the lubricity of PEG200. Abrasive wear was also

reported. Negatively charged peripheral anion end groups and positively charged inner parts of CNPs, designated as C-g-CNPs, meanwhile absorbed onto the frictional contacts, presumably by electrostatic interactions, to form organic–inorganic electric double layer structures, “tremendously boosting” the lubricity of PEG200.

A common theme in this and the previous Example is the role of electrostatics in determining impact of surface treatments on system lubricity. Four geometries were employed for the studies at varying length scales (QCM, ball-bearing on QCM, pin-on-disk, and reciprocating pin-on-flat), and a range of contacting materials were studied (*e.g.*, steel on gold, alumina on alumina, stainless on stainless, *etc.*). Abrasive wear was observed for positively charged +CNPs and +NDs, while an improved lubricity was reported for -CNPs and -NDs.

5.3. Interdependent Roles of Electrostatics and Surface Functionalization on the Adhesion Strengths of Nanodiamonds to Gold in Aqueous Environments Revealed by Molecular Dynamics Simulations [24]

It is apparent that both surface functionalization and surface charge play major roles in lubricity. An important fundamental problem is to decipher the individual contributions of each phenomenon, which can be explored through molecular-level simulations of NP systems in the presence and absence of induced image charges to assess the impact of electrostatics. Such simulations were reported for +ND and -ND in aqueous suspensions on gold surfaces by Su *et al.*, who found that adhesion strengths resulted from an interdependence of electrostatics and surface functionalization [24]. The simulations revealed a water layer containing Na^+ counterions between -NDs with the surface -COO^- functional groups, but no such layer for a +ND with -NH_3^+ functional groups. The closer proximity of the +ND to the gold surface and the lack of cancelation of electrostatic interactions due to counterions and the water layer resulted in an electrostatic adhesion force for +ND that was nearly three times greater than that of a -ND. The authors therefore demonstrated how both surface functionalization and electrostatics contribute to determining the adhesive binding strengths (Figure 14).

In a follow-up study, the same group modelled tribological contact between two gold surfaces lubricated by NDs in water to explore friction levels, rolling, and surface deformation [63]. Higher friction levels were notably observed when induced image charges in the gold contacts were present *versus* where w those were absent.

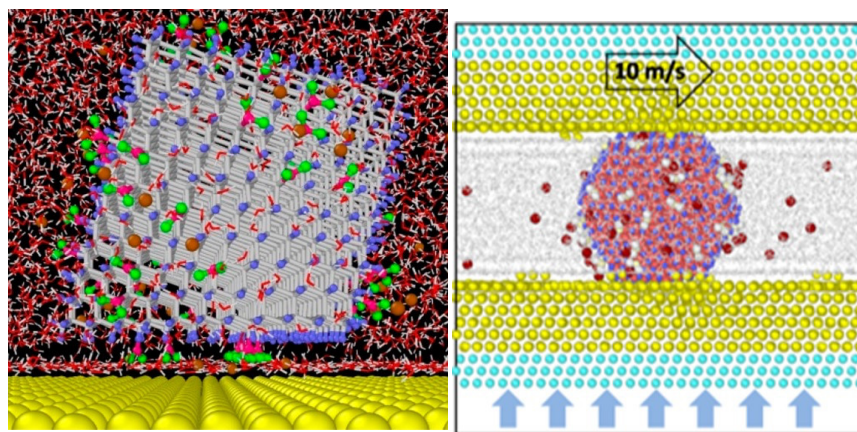


Figure 14. Left: Schematic of a functionalized nanodiamond atop a gold surface in an aqueous environment. Reproduced with permission from Ref. [24]. Copyright 2018 American Chemical Society. Right: Illustration of a nanodiamond in tribological contact with sliding gold surfaces. Higher friction levels were observed when induced image charged were included in the simulation. Reprinted from Su *et al.* [63]) and licensed with permission from Creative Commons 4. 0 (<http://creativecommons.org/licenses/by/4.0>).

Significant surface deformation was observed when -NDs were placed between gold surfaces under external loads that were sufficient to displace water from the contact. Rolling and relatively high friction levels were also observed under these conditions. This observation is consistent with

conclusions drawn from highlight 4.5: Friction levels are not necessarily reduced when the normal forces reach the levels to cause rolling of the trapped NPs. Both neutral and +NDs meanwhile exhibited sliding behavior with only minor deformations of the gold surfaces under similar load conditions, suggesting that the size of the surface functional group is a major factor in determining sliding *versus* rolling.

5.4. Potential-Controlled Boundary Lubrication Using MoS₂ Additives in Diethyl Succinate [25]

In this 2020 publications, Liu et al. demonstrated an active friction control by applying an external electric field to 900 nm MoS₂ nanoparticle additives in diethyl succinate base oil lubricating a ZrO₂ sphere in contact with a copper surface [25]. MoS₂ particles displayed a natural negative charge in base oil, but can be positively charged through modification with poly(diallyldimethyl-ammonium chloride). In contrast to the prior examples, both charge polarities reduced the friction coefficient, with significant reductions of up to 60-70% (*i.e.*, from 0.18 to ~0.06). The mechanism underlying friction control was investigated by observing the distributions of the particle additives and characterizing the tribofilms formed at different potentials. As expected, charged particles were attracted to the electrically opposite pole and the effect was reversed by applying the opposite potential. Interfacial slippage was presumed to occur near the interface where NPs were attracted. For locally high concentrations of MoS₂ particles, a MoS₂/MoO_x tribofilm with a thickness of 100–500 nm and a loose structure were formed on the lower friction pair resulting in a significant decrease in the shear force during the friction process.

5.5. Probing Self-Assembly and Nonlinear Friction Behavior of Confined Gold Nanoparticles [26]

In this nanotribological study the authors employed a surface forces apparatus to explore the assembly and associated surface forces for aqueous suspensions of 5 nm gold nanoparticles confined between pairs of mica (negatively charged) and (3-aminopropyl) triethoxysilane modified mica (APTES-mica, positively charged) surfaces. Notably, in this study it was the surface charge of the contacts that was reversed and not the surface charge of the NPs. The Au NPs were observed to be squeezed out of the confined gap between the two (negatively charged) mica surfaces during the loading process – an effect attributed to a repulsive electric double layer force. In contrast, multilayers of Au NPs were observed to remain between the two positively charged APTES-mica surfaces (Figure 15). The authors attributed this observation to an attractive double-layer force between the oppositely charged surfaces of Au NPs and the APTES-mica sheets. It was also noted that the interaction between Au NPs and APTES-mica is stronger than the interactions between Au NPs, which caused a rearrangement of the confined Au NPs under shear motion. The confined nanoparticles did not, however, enhance lubricity: the friction coefficients ($\mu > 0.7$) characterized by a nonlinear stick-slip friction were observed when sliding the two APTES-mica surfaces with thin (~20 nm) confined layers of Au NPs.

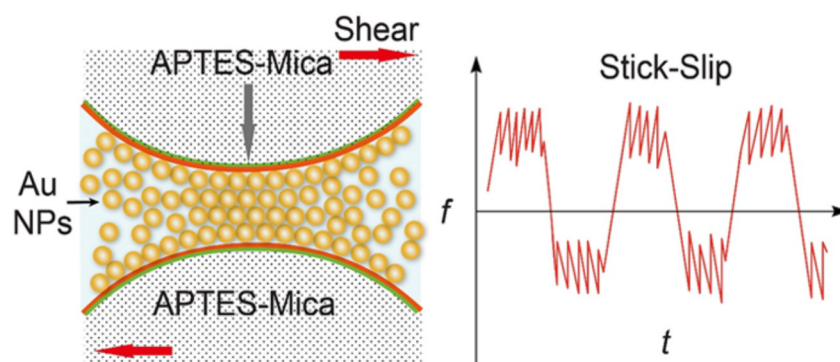


Figure 15. Schematics of surface forces apparatus (SFA) measurements of effects of Au NPs in water squeezed between positively charged mica surfaces. The NPs remain in contact for positively charged mica, resulting in an increased friction and stick-slip behavior. The particles are, however, squeezed

out of the contact when negatively charged mica surfaces are utilized. Reprinted with permission from [26]. Copyright 2019 American Chemical Society.

The results presented in this Example demonstrate the potentially important role of the hydrodynamic glide as a component of the friction-reducing mechanisms associated with the introduction of NP as additives: the oil was not reported to be squeezed out from the interface as in the highlight 5.4 All examples in this section moreover illuminatre the important role of the surface charge, which in turn implies that an external control of friction levels can be achieved by applying external electric fields, as demonstrated in the highlight 5.4. Tuning the friction by this mechanism is the topic of the next and the final section.

6. Tuning Friction through Charge and Potential Variations

Tribotronics involves the design of active control methods for nano and/or meso scale friction by typically employing magnetic and/or electric fields external to the contact. A number of approaches to electromagnetic tuning of friction have been reported in the literature [57]. The tribotronic methods are particularly amenable to charged lubricant additives and have a potential to achieve in situ control of friction levels without removing and replacing lubricant materials situated within the inaccessible confines of a contact. Applications include, but are not limited to triboelectric generators, electric vehicles, magnetic spintronics, geological drilling, automotive braking and efficiency, spacecraft systems, biological systems, and a rapid recharging of flow batteries. The impact of an external field on the tribological performance of lubricants with charged additives is, however, highly variable, as is the speed with which a lubricant responds to an imposition of an external field (Figure 16). The publications highlighted in this section demonstrate both a great potential, as well as great challenges that hold for the field of tribotronics.

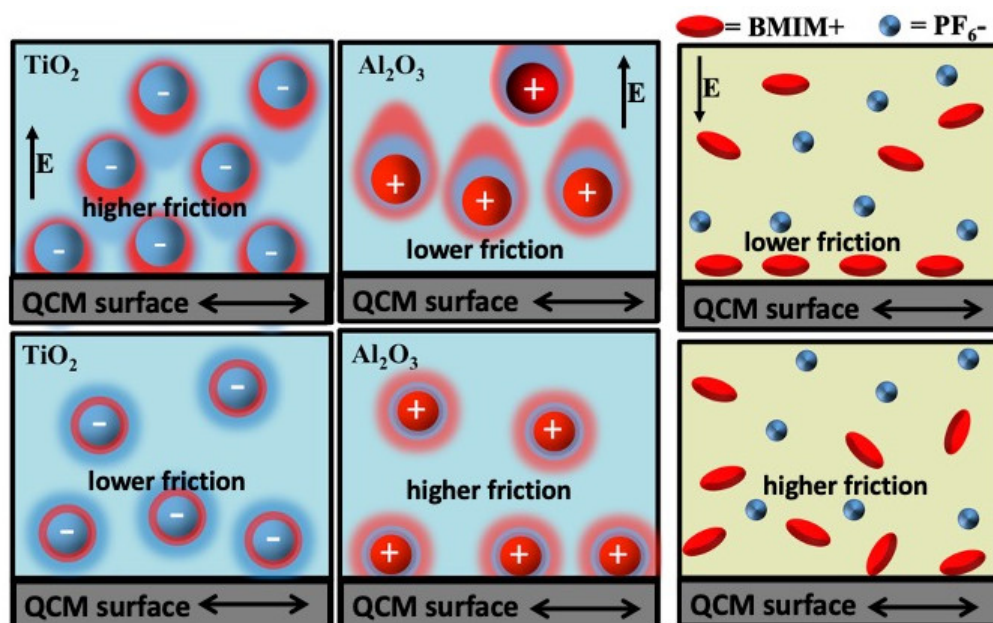


Figure 16. Schematics of the impact of an external electric field on charged lubricant additives. The fields reposition the additives and the impact on interfacial friction is system dependent. Adapted with permission from Ref. [27].

6.1. Study of Tribotronic Control in Ionic Liquids and Nanoparticle Suspensions [27]

When combined with an externally applied field, QCM can serve as a rapid screening tool for tribotronic applications, as reported in 2021 by Seed et al. [27]. This work followed up on an earlier work by Acharya et al. by reporting a comparative study of ionic liquids and NP additives [64].

The group employed an experimental setup consisting of a QCM serving as a tribology sensor and an electrode and a nearby counter electrode immersed in a liquid that contained electrically charged constituents. Electric potential applied between the two electrodes produced a well-defined field resulting in electrophoretic forces which repositioned the charged constituents in the surrounding liquid (Figure 17). The resulting changes in the interfacial friction were detected by QCM for both static and alternating (sinusoidal) fields. The latter provided data on the system response time to the external electric field.

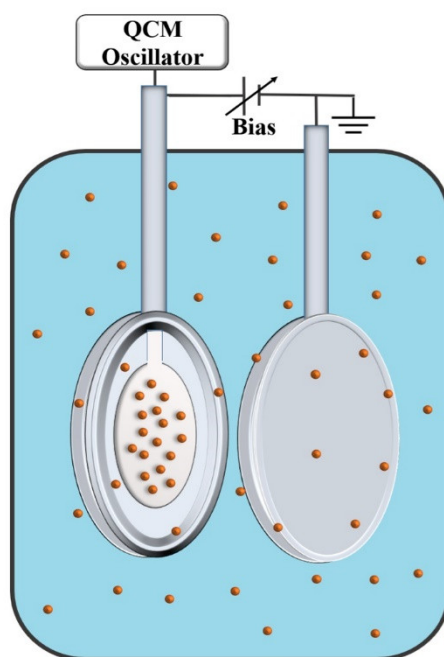


Figure 17. Schematics of a rapid screening geometry for tribotronic response of additives in external electric fields. A sensing QCM (left) is placed parallel and opposite to a counter electrode with an applied bias. In addition to rapid screening of materials, the setup distinguishes the individual tribological response of positively and negatively biased surfaces. Reprinted with permission from Ref. [27].

The authors employed aqueous suspensions of negatively charged TiO_2 nanoparticles, positively charged Al_2O_3 nanoparticles, and also aqueous solutions of positive and negatively charged constituents of the ionic liquid 1-butyl-3-methylimidazolium hexafluorophosphate, $\text{BMIM}^+\text{PF}_6^-$. Application of electric fields induced a variety of responses. Positively and negatively charged constituents were attracted or repelled from the surface, depending on the field direction, and the strength and duration of the field determined whether the electrodeposition would occur.

Characteristic response times from ca. 100 to 1000 s showed that the tribotronic tuning of the system studied was not instantaneous. Depending on the particulars of the system, a deposited layer could increase or decrease friction. The overall tribological impact was attributable to how the interfacial layer interacted with the charged constituents in the surrounding liquid and the resulting changes to the slip planes. See also Ref. [65].

6.2. Electric Response of CuS Nanoparticle Lubricant Additives: The Effect of Crystalline and Amorphous Octadecylamine Surfactant Capping Layers [28]

This 2019 publication by Liu et al. reported on tuning the macroscale friction coefficients by applying an external potential – an effect attributed to a repositioning of nanoparticles added to an ester-base fluid [28]. The results highlighted the interdependent roles of electrostatics and surface functionalization on friction levels reported in the highlight 5.3, as well as the rich variety of the

responses attainable. Specifically, it was demonstrated that surface treatments resulting in crystalline structures enhanced the tribotronic response while the amorphous treatments essentially eliminated sensitivity to the external fields while still enhancing lubricity (Figure 18).

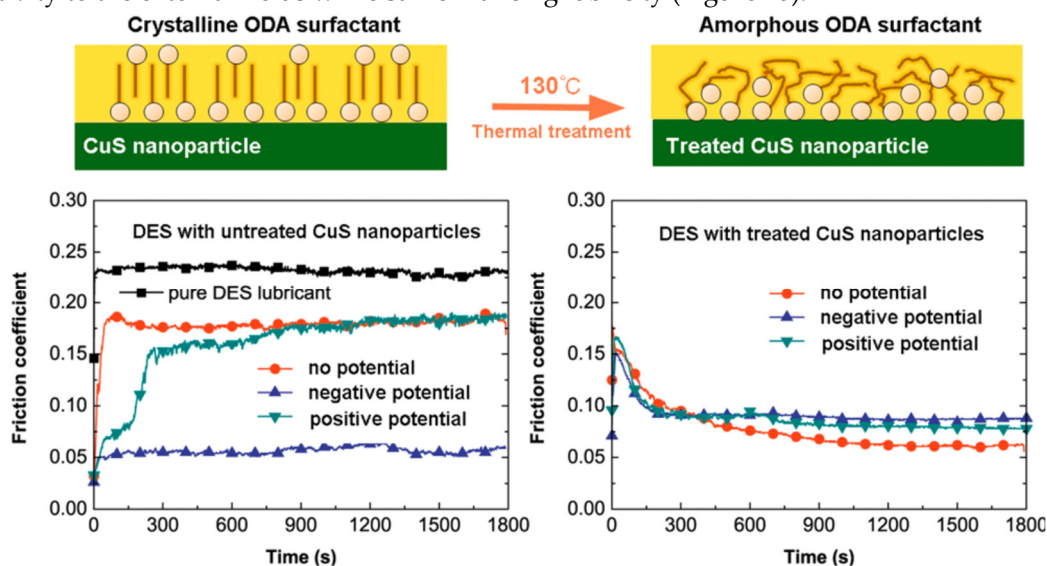


Figure 18. Impact of an electric bias on CuS nanoparticles capped with crystalline (untreated) and amorphous (treated) surfactant layers. The NPs with amorphous surface treatments do not respond to the presence of an external bias. Reprinted with permission from Ref. [28]. Copyright 2019 American Chemical Society.

The measurements were carried out using a macroscale reciprocating tribometer configured with a copper plate and a ZrO₂ ball and octadecylamine-coated CuS nanoparticles added to an ester-base stock lubricant. Such additives are of a great interest in electric vehicle applications because of the capability for maintaining electrical conductivity in critical system components. This publication was a follow up of an earlier study, where the same group observed that for copper plate potentials lower than -14 V the friction coefficient decreased from 0.18 to 0.05 after an induction period [66]. This reduction in friction coefficients was attributed to an excess of positively charged nanoparticles in the vicinity of the negatively charged plate. The induction periods were shorter for increasingly negative potentials. The latter observation is consistent with an increased rate of nanoparticles' migration with increasingly negative potentials.

CuS nanoparticles prepared with a crystalline surfactant were positively charged due to the presence of the amino headgroup in octadecylamine. The surface zeta potential was reported to be $+18.47 \pm 0.99$ mV higher than with the amorphous surfactant – an effect attributed to random chain conformations of the octadecylamine molecules. The observed friction coefficient decreased from 0.18 to 0.09 and 0.05, respectively, when the negative potential (for the copper lower pair) was applied. A thermal treatment was employed to destroy the local order in the layer of the surface ligands and the lack of response to the external field was attributed to amino groups being obscured by the disordered carbon chains. The authors concluded that this hindered the electron transfer and, thus, weakened the system response to external fields.

6.3. Tribotronic and Electrochemical Properties of Platinum–Nanofluid Interfaces Formed by Aqueous Suspensions of 5 and 40 nm TiO₂ Nanoparticles [29]

For nanoparticles to be effective as liquid lubricant additives, the nanoparticle suspension must remain stable. This consideration would tend to favor NPs with a higher magnitude of the Zeta potential and also smaller in size. However, the smaller NPs may respond differently depending on the material systems: Small particles, for example, may fill voids to render a surface smoother. Larger particles meanwhile provide better separation of contacting surfaces, lesser susceptibility to surface

roughness. The stronger repulsive forces required to keep larger NPs separated in liquids may also act to counteract normal forces in the contacting surfaces.

The particle size considerations pose a significant design challenge since NPs are generally present in a range of sizes, along with unintentional constituents such as wear particles. In this 2023 publication, Seed et al. employed QCM in combination with cyclic voltammetry to characterize nanotribological and electrochemical behavior of platinum–nanofluid interfaces formed by aqueous suspensions of negatively charged 5, 40, and 100 nm TiO₂ NPs, including the response to externally applied electric fields [29]. TiO₂ particles gain negative charge in suspension, and, therefore, did not require additional surface treatments. The particles of all three sizes reduced interfacial frictional drag forces when added to pure water in zero field conditions. Unfortunately, the 100 nm NPs failed to remain in suspension for longer than 10–20 min. The 5 and 40 nm NP were readily repositioned by an external electric field in a reversible manner, consistent with no permanent attachment of NPs to the QCM surface. For electric fields of sufficient amplitude and duration, the 40 nm TiO₂ NPs displayed an electrochemical signature consistent with a reversible electrophoretic deposition of the NPs that was accompanied by changes in the electrochemical attributes and an increased interfacial drag.

The smallest 5 nm NPs under the same field conditions resulted in progressive reductions in the interfacial drag forces associated with field-induced increases in concentration of NPs at the surface. The response time to external fields was not significantly different. Slip lengths, which are longer for lower interfacial friction, in zero field conditions were estimated to be 17 nm (22 nm) respectively for the 5 nm (40 nm) NPs. Attractive fields increased the slip lengths for the 5 nm NPs but decreased them for the 40 nm, exemplifying the great degree of sensitivity to NP size. The authors attributed this primarily to the greater charge held on the larger NPs.

Overall, the study suggested a method for active tribological control and optimization of device performance in applications where suspensions of charged nanoparticles are present and can be exposed to external fields, or alternatively a method for selecting the best NP size to optimize system performance based on the electrochemical properties of the materials of interest.

6.4. Friction and Adhesion Control between Adsorbed Layers of Polyelectrolyte Brush-Grafted Nanoparticles via pH-Triggered Bridging Interactions [30]

In this 2018 publication, Riley et al. employed multiple nanotribological methods to explore tuning of friction by changing pH of a base fluid doped with brush-grafted silica nanoparticles. The main innovation of this work was to employ pH-responsive brush grafted NPs with annealed polyelectrolyte brushes capable of undergoing controlled changes in surface area coverage through post-adsorption swelling or de-swelling into non-equilibrium layer conformations (Figure 19). The changes in the surface coverage can then switch the particle intercalation on and off. The resulting bridging attractions and an enhanced energy dissipation upon sliding provide for a mechanism to tune friction and adhesion.

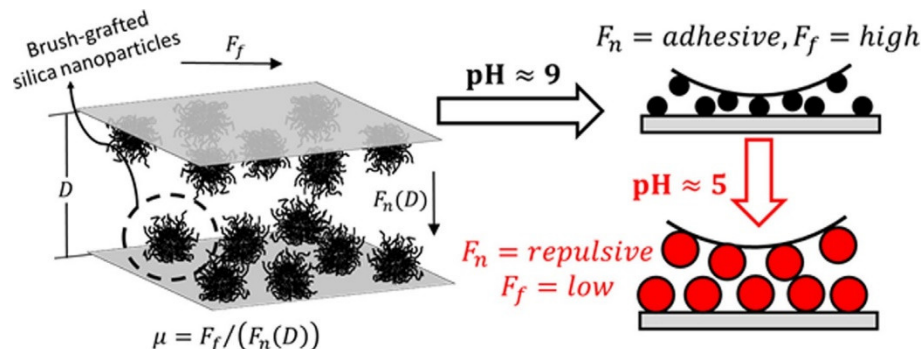


Figure 19. Schematics of tuning of friction and adhesion by changing pH of a base fluid containing brush-grafted silica nanoparticles. The NPs undergo controlled changes in surface area coverage through post-adsorption swelling or de-swelling into non-equilibrium layer conformations. Reprinted with permission from Ref. [30].

In this study colloidal probe atomic force microscopy was employed to measure normal and frictional forces between negatively charged silica surfaces with adsorbed pH-responsive cationic brush-grafted silica nanoparticles. Complimentary QCM and ellipsometry measurements were also performed in the swollen and de-swollen states, providing independent measures of mass density and thickness of the confined NPs.

The study confirmed that adsorbed brush-grafted NPs can be swollen or de-swollen by adjusting pH, thus, allowing for a direct control of the surface coverage and bridging interactions. Adhesive bridging contacts with a high friction ($m \approx 1.5$) were observed for the de-swollen/weakly charged state while non-adhesive contacts with low friction levels ($m \approx 0.1$) were observed for the swollen/highly charged repulsive condition. Overall, this work demonstrated an alternate means to tune friction. See also Ref. [68].

6.5. High Lubricity and Electrical Responsiveness of Solvent-Free Ionic SiO₂ Nanofluids [31]

Conventional NPs and surface functionalized NPs are in general solid-like when not dispersed in a base fluid. Colloidal stability of such particles can be improved by surface functionalization and then the properties of the surface ligands become essential when considering such particles as lubricant additives. "Solvent-free" ionic nanofluids (NFs) are liquid materials composed of NPs whose surface functionalization renders them to behave similarly to ionic liquids [69]. NFs in particular are characterized by Newtonian liquid behavior, macroscopic homogeneity, good thermal stability, and good tribological properties when used alone or as additives.

In this 2018 study, Gou et al. explored the impact of external fields on nanofluids consisting of functionalizing silica nanoparticles with a charged corona and ionically tethered with oligomeric chains as a canopy [31]. The study demonstrated that the as-synthesized nanofluids were both stable and fluid and showed excellent friction-reducing and anti-wear properties both as additives and as pure liquids. Similar to what has been observed for conventional ionic liquids, the authors found that a small fraction of nanofluids blended into a base fluid reduces friction and wear as effectively as the nanofluid alone.

Measurements were performed with a macroscale reciprocating tribometer using a steel ball on steel disk contact. NFs were studied both in pure forms and as additives to a polyethylene glycol base oil. For one specific shell structure, μ dropped from about 0.15 to 0.13 for an applied potential of both +3 V (disk as anode) and -3 V (disk at cathode). For the second specific shell structure, the friction coefficient dropped from about 0.12 to 0.11 only for -3 V (disk as cathode) and no change was observed when a positive potential was applied. Formation of a unique double electric layer consisting of both organic and inorganic materials during the friction was suggested as the underlying mechanism for the observations, which can be essential for yielding robust lubrication of the adsorption film. The authors also noted that a nanostructured tribofilm comprising of a significant fraction of silica and tribo-chemical products of the organic layers had formed and it was believed to be significant in improving the boundary lubrication performance.

The results reveal both the great promise of such novel lubricants, and the challenges associated with the sensitivities to external field conditions. The latter issue must be harnessed in order to optimize the lubricant performance.

7. Summary and Concluding Comments

In this mini review, we have highlighted 25 selected research reports that demonstrate the major progress and important challenges in the linkage of nanoscale contacts and nanoparticles on the macroscale tribological properties. In the years following Israelachvili and coworkers reporting "full slip" conditions achieved by C₆₀ additives, it had become evident that changes in the slip conditions at the interface are far more likely than rolling of the spherical additives to underlie their observations. Important outstanding challenges to the fundamental understanding of how addition of NPs can impact the lubricant performance include rapid screening of materials, and the role of surface charge, which allows for tuning friction by varying electric charge and/or external electric

potential. Response times to external fields also remain an outstanding challenge, as well as dispersion of nanomaterials, and high sensitivity of materials to additive particle size.

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