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Article

# On the Determination of Elastic Properties of Single-Walled Nitride Nanotubes Using Numerical Simulation

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**Abstract:** In the recent years, tubular nanostructures have been related with immense advances in various fields of science and technology. Considerable research efforts have been centered on the theoretical prediction and manufacturing of non-carbon nanotubes (NTs), which meet modern requirements for the developing of novel devices and systems. In this context, diatomic inorganic nanotubes formed by atoms of elements from the 13th group of the periodic table (B, Al, Ga, In, Tl) and nitrogen (N), have received much research attention. In the present work, the elastic properties of single-walled boron nitride, aluminium nitride, gallium nitride, indium nitride and thallium nitride nanotubes were numerically evaluated using the nanoscale continuum modelling approach (also called molecular structural mechanics). The elastic properties (rigidities, surface Young's and shear moduli, and Poisson's ratio) of nitride nanotubes are discussed with respect to the bond length of the corresponding diatomic hexagonal lattice. The results obtained contribute to a better understanding of the mechanical response of nitride compound-based nanotubes, covering a broad range from the well-studied boron nitride NTs to the hypothetical thallium nitride NTs.

**Keywords:** 13th group element; nitride nanotubes; rigidity; elastic moduli; modelling; numerical simulation

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## 1. Introduction

Compounds of elements of the 13th group of the periodic table, such as boron (B), aluminum (Al), gallium (Ga), indium (In) and thallium (Tl), with nitrogen (N), representative of the 15th group, are emerging materials attractive for electronic engineering and light industry. The ability of 13th group-nitrides to form a hexagonal graphene-like lattice [1] allows to expand the area of their upcoming applications and bring to light new perspectives in miniaturization and design of functional devices [2–4]. Hexagonal boron nitride (h-BN) is a high strength electric insulator, comparable to graphene, excellent thermal and chemical stability, and transparency for visible light [5–7]. Such characteristics make h-BN suitable for diverse applications as a dielectric in graphene electronics, components for photovoltaic devices, sensors and bio-detectors. Hexagonal aluminium nitride (h-AlN), gallium nitride (h-GaN) and indium nitride (h-InN), which also exhibit good thermal and chemical stability, are wide gap semiconductors and are able of emitting light in colours green, blue and UV bands [8]. As a result, these hexagonal metal nitrides (AlN, GaN and InN) are in the focus of research attention due to their promising applications in electronics and optoelectronics as solid-state light-emitting devices (LED) and high-speed field-effect transistors (FETs) [1,4,9].

Hexagonal thallium nitride (h-TIN), has a small or even negative band gap [10], pointing out to its semi-metallic nature. This makes h-TIN an appropriate candidate for infrared optical devices [3,11].

One-dimensional (1D) tubular nanostructures, i.e. nanotubes (NTs), made up from hexagonal BN, AlN, GaN, InN and TiN monolayers, are expected to have enhanced properties when compared with their bulk counterparts, envisioning new perspectives in the development of nanoscale electronic and light devices, but not limited to them. For example, boron nitride nanotube has the potential to be used in the smallest co-axial cable, a possibility that was unlocked when carbon nanotube was grown inside it [12]. The high surface to volume ratio of NTs allows suggesting their forthcoming applications for gas absorption and as chemical sensors. The possibility of tuning electronic, thermoelectric, optical and chemical properties of two-dimensional (2D) 13th group-nitride nanostructures through the introducing deformation [1,4,13–17], points to a promising use of their 1D allotropes in the field of strain engineering. In view of abovementioned perspectives, viable applications of boron nitride NTs as biosensors [18], aluminium nitride NTs as gas adsorbents [19] and for drug delivery [20], as well as suitability of gallium nitride NTs for nanoelectromechanical systems (NEMS) [21] were considered.

Most nanotubes based on the 13th group-nitride compounds were by now predicted and synthesized. After the theoretical prediction of the boron nitride nanotube (BNNT) in 1994 [22] and its synthetization in 1995 by Chowdhury and Adhikari [23], who used arc discharge for this end, BN nanotubes with a honeycomb atomic arrangement were successfully manufactured using chemical vapour deposition (CVD) [24,25], ball-milling [26], laser ablation [27] and thermal plasma jet [28]. Unlike BNNTs, progress in synthesizing of AlN, GaN and InN nanotubes is to some extent limited. In 2003, Zhang and Zhang [29] performed a theoretical study on the stability of the geometrical structure of aluminium nitride nanotubes (AlNNTs) and perspectives for their synthesis. It was concluded that the Al and N atoms form a hexagonal graphene-like arrangement, carrying out  $sp^2$  hybridization [29]. Wu et al. [30] synthesized AlNNTs by nitriding reaction, in the same year. The proposed growth method made it possible to obtain faceted AlNNTs with a length of a few micrometers and a hexagonal cross section. Balasubramanian et al. [31] grew AlNNTs by gas-phase condensation using solid–vapour equilibrium. The atomic structure of the resulting AlNNTs consisted of hexagonal rings of Al and N atoms, which adopt  $sp^2$  hybridization. Yin et al. [32] produced C-AlN-C coaxial composite NTs in mass quantity, by resorting to a chemical substitution reaction in a controllable two-step process with the use of multi-walled carbon nanotubes (MWCNTs) as template. The AlNNTs obtained were straight, several micrometers long and had a faceted single-crystalline structure. Stan et al. [33] synthesized faceted AlNNTs with a triangular cross-section through an epitaxial casting process that consisted of the depositing of aluminium nitride onto GaN nanowires, which were subsequently removed by annealing in a hydrogen atmosphere, so that the AlN tubes remained hollow. Finally, one-micrometer-long AlNNTs with hexagonal wurtzite structure were synthesized by Fan et al. [34], who used a thermal process to bend and roll-up the AlN monolayer for this purpose. With regard to gallium nitride nanotubes (GaNNTs), their structural stability and prospects of synthesis were first theoretically investigated in 1999 by Lee et al. [35], basing on density functional theory (DFT) calculations. Then, in 2003 Goldberger et al. [36] prepared single-crystalline GaNNTs with hexagonal cross-section, using an epitaxial casting method and ZnO nanowires as templates. Yin et al. [37] synthesized amorphous GaNNTs of a few micrometers in length by an In-assisted thermal evaporation process. Hu et al. [38] accomplished mass-quantity growth of straight crystalline GaNNTs with lengths up to 80  $\mu\text{m}$ , using a two-stage process based on controllable conversion of amorphous gallium oxide NTs. Hung et al. [39] synthesized uniform arrays of free-standing hexagonal GaNNTs on a GaN template by inductively coupled plasma etching. Liu et al. [40] manufactured single-crystalline hexagonal wurtzite-type GaNNTs based on controllable chemical thermal evaporation process. Jung et al. [41] fabricated long crystalline GaNNTs aided by the metal organic chemical vapour deposition (MOCVD) technique. Concerning indium nitride nanotubes (InNNTs), for the first time in 2004, Yin et al. [42] synthesized straight, high purity, crystalline InNNTs of several-micrometers length in mass quantity by controlled carbonitridation reaction in a vapour-solid (VS) route, using MWCNTs as carbon source to carry out chemical reaction.

Soon after, Sardar et al. [43] produced almost defect-free single-crystalline InNNTs by employing the low-temperature chemical reaction of indium acetate with hexamethyldisilazane (HMDS). At about the same time, the theoretical prediction of the InNNTs with stable honeycomb graphene-like structure was accomplished by Qian et al. [44], who used DFT calculations to this end.

Among the 13th group – nitrides, TiN is the least studied and nanostructures based on this compound have not been synthesized, possibly due to the high toxicity of thallium [2]. Despite the existence of several theoretical works dedicated to the structural stability of 2D TiN nanostructures with planar honeycomb atomic arrangement [45–47] and evaluation of their electronic [3,4] and mechanical [1,47] properties, thallium nitride nanotubes (TiNNTs) have not yet been predicted. The structural similarity of h-TiN with other representatives of the 13th group-nitrides suggests that TiNNTs will possibly be modelled and synthesized in the future. The inclusion of these hypothetical nanotubes in the current study envisages expanding the range of the potential applications of 13th group-nitride NTs and meets the requirements for the search of new materials for innovative nanodevices.

The mechanical stability of nanotubes and the knowledge on their mechanical behaviour are crucial for current and forthcoming applications involving NTs, as well as for the design of materials and instrument. It is worth noting that strain engineering is efficient to customize the functional properties of nanomaterials. From this point of view, the evaluation of the mechanical properties of the 13th group-nitride NTs gains the outmost importance.

The study of the mechanical behaviour of non-carbon nanotubes (N-CNTs), whose representatives are those based on nitride compounds, has been performed mostly theoretically, aided by analytical and numerical procedures, since experimental techniques for nanomaterials characterization are expensive and highly resource-consuming. As reported by Antunes et al. [48], the mechanical behaviour of N-CNTs can be characterized using three categories of theoretical methods, viz.: the atomistic approach, embracing ab initio and molecular dynamics (MD); the continuum mechanics (CM) approach; and the nanoscale continuum modelling (NCM) or molecular structural mechanics (MSM) approach. Amongst 13th group-nitride nanotubes, BNNTs have received the most research attention to date [48,49].

Referring to the atomistic approach, Kochaev [50] evaluated the surface Young's modulus (product of Young's modulus and nanotube wall thickness) and Poisson's ratio of BNNTs, AlNNTs and GaNNTs, making use of ab initio simulation. Hao et al. [51] studied size-dependent mechanical behaviour of the AlNNTs and evaluated their Young's modulus employing ab initio DFT calculations coupled with linear combination of atomic orbitals (LCAO). Fabris et al. [52] used the same method to calculate the Young's modulus of GaNNTs. Current studies, involving MD, rely on analytical or empirical potential functions to describe the interactions between atoms in the hexagonal diatomic lattice. The second-generation reactive empirical bond order (REBO) potential was used by Kumar et al. [53] in their MD simulation study to evaluate the Young's and shear moduli, and Poisson's ratio of BNNTs, AlNNTs and GaNNTs. Jeng et al. [54] adopted MD simulation with Tersoff many-body potential to assess the mechanical properties of GaNNTs under tension, including their Young's modulus. Xiong and Tian [55] studied the torsional properties of BNNTs, making use of MD simulation with Tersoff potential and calculated BNNTs the shear modulus. Tao et al. [56] used MD with Tersoff–Brenner (TB) potential to calculate the Young's modulus of BNNTs. The Stillinger-Weber (S-W) potential was employed to describe the interactions between Ga and N atoms by Xu et al. [57] in their MD simulation study for evaluating the Young's modulus of single-crystalline GaNNTs. Santosh et al. [58] with the aim of calculating the BNNTs Young's and shear moduli, implemented the force - constant approach for describing the B - N interactions under MD simulation. Le [59], based on MD simulations coupled with dimensional analysis, derived analytical expressions for the Young's modulus of the BNNTs.

With regard to the CM approach, where the nanotube is modelled as a continuum structure, Oh [60] employed a continuum lattice (CL) analytical thermodynamic method, in combination with the TB potential to calculate the Young's modulus and Poisson's ratio of BNNTs.

In the NCM/MSM approach, the bonds between two atoms in the diatomic lattice are modelled as elastic elements (e.g., beams or springs), thus basing on the connection between NTs molecular structure and solid mechanics. In two their works Sakharova et al. [49,61] used the beam element to represent interatomic bonding within the framework of the NCM/MSM approach to evaluate Young's and shear moduli, and the Poisson's ratio of BNNTs [49] and InNNTs [61]. The latter, to our knowledge, is the only study devoted to the elastic properties of InNNTs. Employing the NCM/MSM approach combined with Euler beam model, Yan et al. [62] calculated the Young's and shear moduli of BNNTs resorting to longitudinal and torsional free-vibrations of nanotubes. Genoese et al. [63] evaluated the surface Young's and shear moduli of BNNTs, based on a link between the "stick-and-spring" (NCM/MSM) and the Donnell thin shell continuum models (CM). Jiang and Guo [64] also used the "stick-and-spring" model to derive analytical solutions for the surface Young's modulus and Poisson's ratio of BNNTs, AlNNTs and GaNNTs. With the exception of BNNTs, studies for mechanical characterization of NTs based on other nitrides of the 13th group –are limited (AlNNTs, GaNNTs), infrequent (InNNTs) or absent (TINNTs). Lack of systematized investigation of the mechanical response of the nanotubes formed by nitride compounds is also noticeable.

The objective of this work is to perform a systematic comparative study on the evaluation of the elastic properties (surface Young's and shear moduli, and Poisson's ratio) of single-walled nanotubes made of boron nitride, aluminium nitride, gallium nitride, indium nitride and thallium nitride (SWBNNTs, SWAlNNTs, SWGaNNNTs, SWInNNTs and SWTINNTs) in a wide range of chiral indices and diameters greater than 1.25 nm. To this end, a three-dimensional finite element (FE) model was built within the scope of the NCM/MSM approach to assess three rigidities (tensile, bending and torsional) and then calculate the surface Young's and shear moduli and Poisson's ratio of the 13th group – nitride nanotubes. In view of the lack of information on the value of nanotube wall thickness for nitride NTs, except in the case of SWBNNTs, the surface elastic moduli (the product of the respective elastic modulus by the NT wall thickness) were chosen for this analysis. The present work aims to improve the understanding of the mechanical response of the nitride nanotubes, which group materials with insulator, semiconductor and semi-metallic properties.

## 2. Materials and Methods

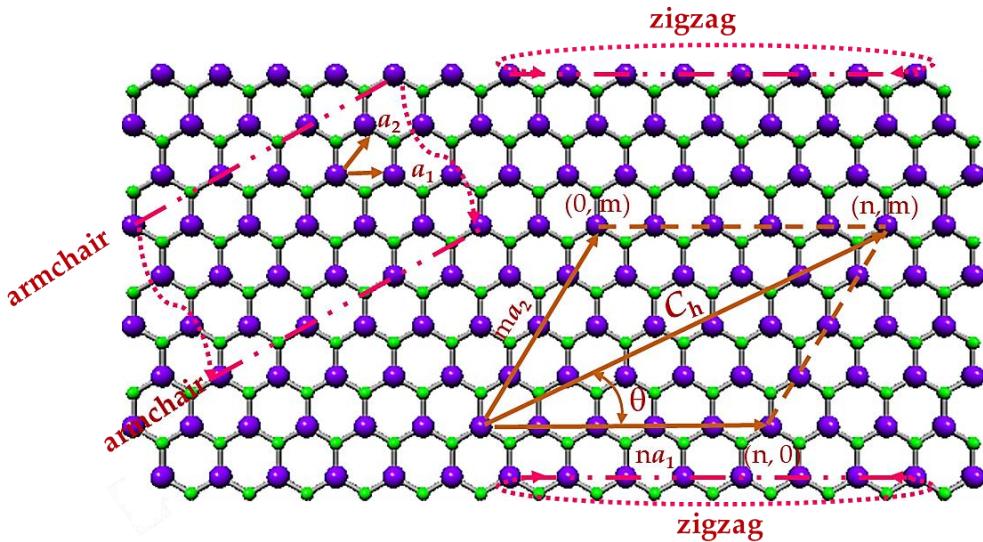
### 2.1. Atomic Structure of 13th Group Element - Nitride Nanotubes

Boron nitride, aluminium nitride, gallium nitride, indium nitride and thallium nitride sheets have a hexagonal lattice, where the atom that is part of the 13th group of the periodic table (now designated A13), such as boron (B), aluminium (Al), gallium (Ga), indium (In) or thallium (Tl) form with nitrogen (N) a honeycomb structure with planar geometry [1,65], as shown in Figure 1 for the case of the GaN nanosheet. The honeycomb atomic arrangement is defined by the chiral vector,  $\mathbf{C}_h$ , and the chiral angle,  $\theta$ , expressed as follows, respectively:

$$\mathbf{C}_h = n\mathbf{a}_1 + m\mathbf{a}_2, \quad (1)$$

$$\theta = \sin^{-1} \frac{\sqrt{3}}{2} \frac{m}{\sqrt{n^2 + nm + m^2}}, \quad (2)$$

where  $n$  and  $m$  are the chiral indices, both having integers values;  $\mathbf{a}_1$  and  $\mathbf{a}_2$  are the unit vectors of the diatomic hexagonal lattice. The length of the unit vector  $\mathbf{a}$  is calculated by  $a = \sqrt{3}a_{A13-N}$ , where  $a_{A13-N}$  is the equilibrium bond length. As can be seen in Table 1, where the bond lengths of nitride NTs available in the literature are presented, there is no conformity about the  $a_{A13-N}$  values.



**Figure 1.** GaN hexagonal nanosheet with designations of the chiral indices,  $n$  and  $m$ , chiral vector,  $C_h$ , chiral angle,  $\theta$ , and the schematic to roll up armchair and zigzag NTs geometries. Ga atoms are depicted in purple; N atoms in green.

**Table 1.** Bond length values of 13th group element - nitride nanostructures available in the literature.

|                         | BN          | AlN         | GaN         | InN        | TIN        |
|-------------------------|-------------|-------------|-------------|------------|------------|
| $a_{\text{A13-N}}$ , nm | 0.1446 [53] | 0.177 [50]  | 0.175 [72]  |            |            |
|                         | 0.1447 [66] | 0.179 [65]  | 0.184 [50]  |            |            |
|                         | 0.145 [65]  | 0.1805 [1]  | 0.185 [65]  | 0.203 [44] | 0.2154 [1] |
|                         | 0.147 [50]  | 0.185 [69]  | 0.1852 [1]  | 0.206 [65] | 0.224 [46] |
|                         | 0.151 [67]  | 0.1856 [53] | 0.186 [69]  | 0.2074 [1] | 0.230 [4]  |
|                         | 0.153 [68]  | 0.193 [70]  | 0.1863 [53] |            |            |
|                         |             | 0.195 [71]  | 0.194 [70]  |            |            |

Single-walled nitride NTs are cylinders, which are formed by rolling up the respective A13-N nanosheet with a honeycomb atomic arrangement, varying the chiral angle,  $\theta$ , in the range  $0^\circ \leq \theta \leq 30^\circ$ . The diameter of resulting nanotube,  $D_n$ , is given by:

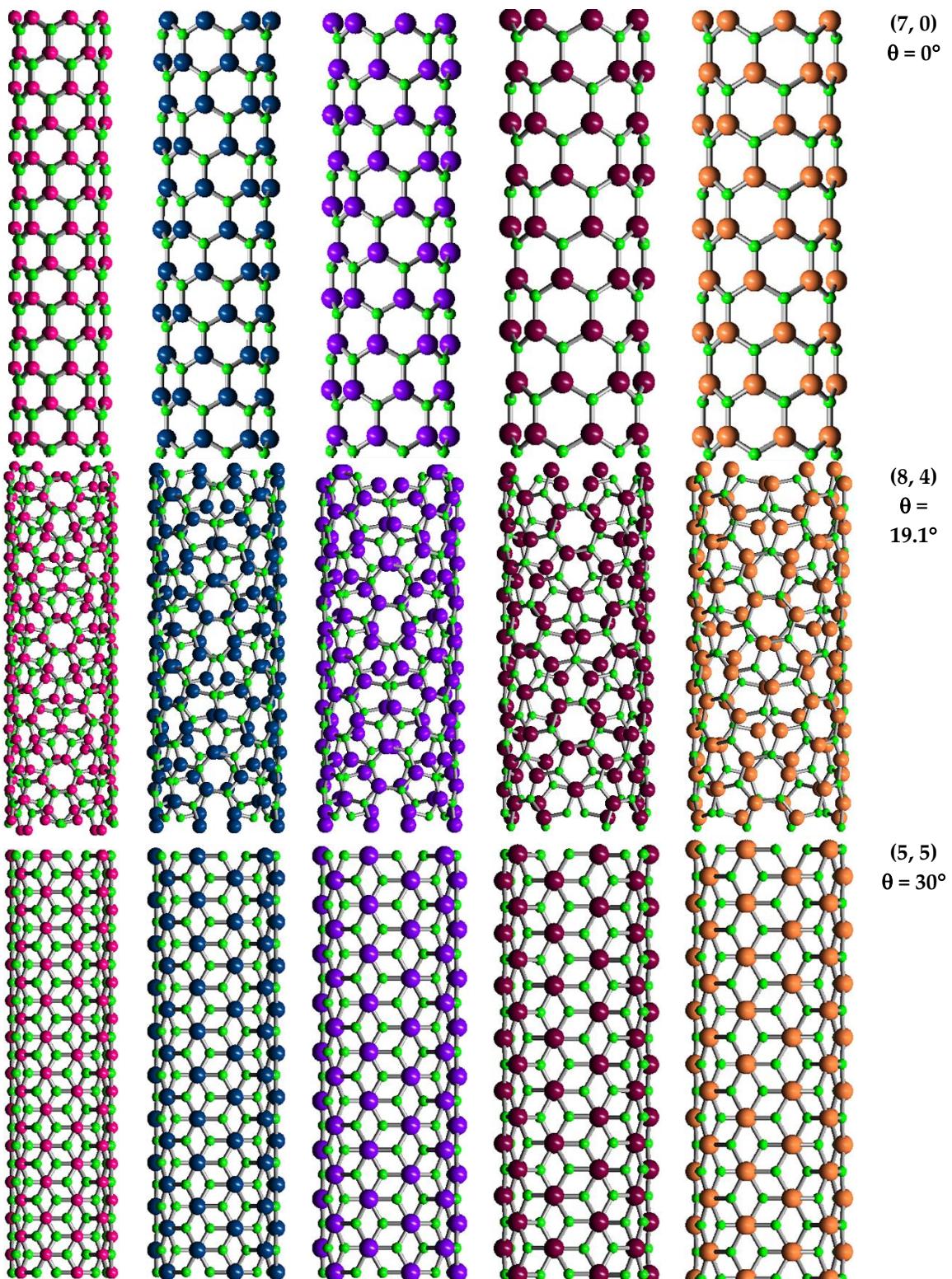
$$D_n = \frac{a_{\text{A13-N}} \sqrt{3(n^2 + nm + m^2)}}{\pi}, \quad (3)$$

where  $n$  and  $m$  are the chiral indices and  $a_{\text{A13-N}}$  is the equilibrium bond length of the diatomic nanostructure based on the nitride compounds under study.

Three main symmetry groups of NTs are defined based on the value of  $\theta$ , such as: zigzag ( $n, 0$ ) NTs with  $\theta = 0^\circ$  ( $m = 0$ ); chiral ( $n, m$ ) NTs with  $0^\circ < \theta < 30^\circ$  ( $n \neq m \neq 0$ ); armchair ( $n, n$ ) NTs with  $\theta = 30^\circ$  ( $n = m$ ). The two configurations, limiting the range of  $\theta$ , viz. zigzag ( $n, 0$ ) and armchair ( $n, n$ ) (see, Figure 1) are called non-chiral nanotubes.

Non-chiral (zigzag and armchair) and chiral SWBNNTs, SWAINNTs, SWGaNNTs, SWInNNTs and SWTINNTs, with the same chiral indices ( $n, m$ ) for each symmetry group, are represented schematically in Figure 2.

SWBNNTs    SWAINNTs    SWGaNNTs    SWInNNTs    SWTINNTs



**Figure 2.** Configurations of (7, 0) zigzag, (8, 4) chiral and (5, 5) armchair of SWBNNTs, SWAlNNNTs, SWGaNNTs, SWInNNTs and SWTlNNNTs, obtained using the software Nanotube Modeler©. N atoms are depicted in green, B atoms are in bright pink, Al atoms are in blue, Ga atoms are in purple, In atoms are in dark red and Tl atoms are in pale orange.

## 2.2. Geometrical Characteristics and Finite Element Modeling of the Elastic Behaviour of SWBNNTs, SWAlNNNTs, SWGaNNTs, SWInNNTs and SWTlNNNTs

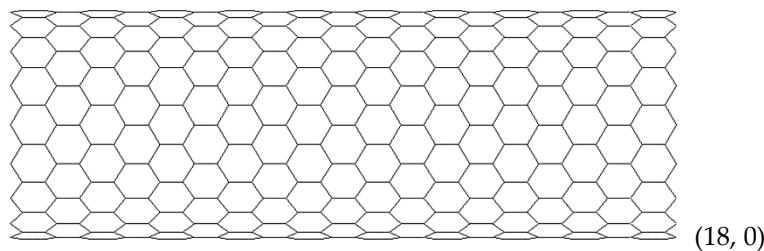
The geometric characteristics of SWBNNTs, SWAINNTs, SWGaNNTs, SWInNNTs and SWTINNTs of three main configurations, armchair ( $\theta = 30^\circ$ ), zigzag ( $\theta = 0^\circ$ ) and chiral ( $\theta = 19.1^\circ$  family, which is consistent with the biggest number of NTs), used in the finite element analysis (FEA), are shown in Table 2. The chiral indices of the NTs were chosen to obtain structures with comparable diameters. To guarantee the mechanical response of the NTs regardless of the nanotube length, the length of the NTs was chosen nearly 30 times bigger than the diameter of the NTs [49].

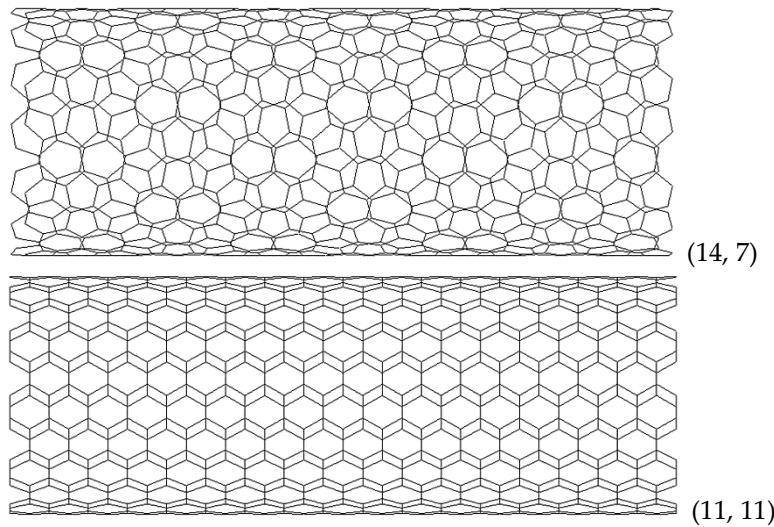
**Table 2.** Chiral indices ( $n, m$ ) and diameters,  $D_n$ , of the SWBNNTs, SWAINNTs, SWGaNNTs, SWInNNTs and SWTINNTs.

| NT type                          | SWBNNTs<br>(n, m) | $D_n$ ,<br>nm* | SWAINNTs<br>(n, m) | $D_n$ , nm*<br>(n, m) | SWGaNNTs<br>(n, m) | $D_n$ , nm*<br>(n, m) | SWInNNTs<br>(n, m) | $D_n$ , nm*<br>(n, m) | SWTINNTs<br>(n, m) |
|----------------------------------|-------------------|----------------|--------------------|-----------------------|--------------------|-----------------------|--------------------|-----------------------|--------------------|
| zigzag,<br>$\theta = 0^\circ$    | (16, 0)           | 1.297          | (13, 0)            | 1.312                 | (13, 0)            | 1.398                 | (12, 0)            | 1.363                 | (11, 0)            |
|                                  | (26, 0)           | 2.107          | (20, 0)            | 2.018                 | (19, 0)            | 2.043                 | (18, 0)            | 2.044                 | (17, 0)            |
|                                  | (38, 0)           | 3.080          | (29, 0)            | 2.926                 | (27, 0)            | 2.903                 | (26, 0)            | 2.953                 | (25, 0)            |
|                                  | (43, 0)           | 3.485          | (34, 0)            | 3.430                 | (32, 0)            | 3.440                 | (30, 0)            | 3.407                 | (29, 0)            |
|                                  | (47, 0)           | 3.809          | (38, 0)            | 3.834                 | (36, 0)            | 3.870                 | (34, 0)            | 3.862                 | (32, 0)            |
| chiral,<br>$\theta = 19.1^\circ$ | (14, 7)           | 1.501          | (10, 5)            | 1.335                 | (10, 5)            | 1.422                 | (10, 5)            | 1.502                 | (10, 5)            |
|                                  | (20, 10)          | 2.144          | (16, 8)            | 2.136                 | (14, 7)            | 1.991                 | (14, 7)            | 2.103                 | (14, 7)            |
|                                  | (26, 13)          | 2.788          | (22, 11)           | 2.936                 | (20, 10)           | 2.844                 | (20, 10)           | 3.005                 | (18, 9)            |
|                                  | (28, 14)          | 3.002          | (26, 13)           | 3.470                 | (24, 12)           | 3.413                 | (24, 12)           | 3.606                 | (22, 11)           |
|                                  | (32, 16)          | 3.431          | (30, 15)           | 4.004                 | (28, 14)           | 3.982                 | (26, 13)           | 3.906                 | (26, 13)           |
| armchair,<br>$\theta = 30^\circ$ | (10, 10)          | 1.404          | (8, 8)             | 1.398                 | (7, 7)             | 1.303                 | (7, 7)             | 1.377                 | (7, 7)             |
|                                  | (15, 15)          | 2.106          | (12, 12)           | 2.097                 | (11, 11)           | 2.048                 | (11, 11)           | 2.164                 | (10, 10)           |
|                                  | (20, 20)          | 2.807          | (17, 17)           | 2.971                 | (16, 16)           | 2.979                 | (15, 15)           | 2.951                 | (14, 14)           |
|                                  | (25, 25)          | 3.509          | (20, 20)           | 3.495                 | (19, 19)           | 3.538                 | (18, 18)           | 3.541                 | (17, 17)           |
|                                  | (27, 27)          | 3.790          | (22, 22)           | 3.845                 | (21, 21)           | 3.910                 | (20, 20)           | 3.934                 | (19, 19)           |

\* The diameters,  $D_n$ , of SWBNNTs, SWAINNTs and SWGaNNTs are calculated adopting the bond lengths  $a_{B-N} = 0.147$  nm,  $a_{Al-N} = 0.183$  nm and  $a_{Ga-N} = 0.195$  nm, respectively as defined by Nanotube Modeler© software; for the SWInNNTs and SWTINNTs, the bond lengths  $a_{In-N} = 0.206$  nm [65] and  $a_{Ti-N} = 0.2154$  nm [1] were respectively assumed.

The FE meshes of SWBNNTs, SWAINNTs, SWGaNNTs, SWInNNTs and SWTINNTs used in FEA were built using the Nanotube Modeler© software. The program database files, acquired from this software, were converted to the format compatible with the ABAQUS® code. The in-house application *InterfaceNanotubes.NM* [49] was used for this purpose. FE meshes for zigzag, chiral and armchair InNNTs are exemplified in Figure 3.





**Figure 3.** FE meshes of zigzag (18, 0), chiral (14, 7) and armchair (11, 11) InN nanotubes.

The interatomic bonds, A13 – N, of the hexagonal NTs lattice were modelled as equivalent beam elements within the framework of the NCM/MSM approach, which makes use of the connection between the nanotube molecular structure and the equivalent continuum structure. The latter is composed of beam elements and characterised by its tensile,  $E_b A_b$ , bending,  $E_b I_b$ , and torsional,  $G_b J_b$ , rigidities, which are related to the bond stretching,  $k_r$ , bond bending,  $k_\theta$ , and torsional resistance,  $k_\tau$ , force field constants, representing the respective molecular structure, through the following expressions [73]:

$$E_b A_b = l k_r, \quad E_b I_b = l k_\theta, \quad G_b J_b = l k_\tau, \quad (4)$$

where,  $A_b = \pi d^2/4$  is the cross-section area,  $I_b = \pi d^4/64$  is the moment of inertia, and  $J_b = \pi d^4/32$  is the polar moment of inertia of a circular cross-section beam with diameter  $d$ , being  $l$  the beam length, equal to the bond length,  $a_{A13-N}$ .

Equations (4) allow computing the input parameters for the numerical simulation making use of the  $k_r$ ,  $k_\theta$ , and  $k_\tau$  force field constants. Unlike BNNTs, for which several values of the bond stretching,  $k_r$ , and bond bending,  $k_\theta$ , force constants are available in the literature [49], for the other 13th group elements - nitride NTs, these data are scarce or nonexistent. For this reason, in the present study, the  $k_r$  and  $k_\theta$  force field constants were calculated resorting to the method that uses analytical molecular mechanics (MM) expressions for the surface Young's modulus,  $E_s$ , and the Poisson's ratio,  $v$ . The values of  $E_s$  and  $v$ , in turn, originate from DFT calculations or can be obtained experimentally. Thus, the bond stretching and bond bending force constants are derived by solving the following system of equations [74]:

$$\begin{cases} E_s = \frac{4\sqrt{3}k_r k_\theta}{k_r \frac{a_{A13-N}^2}{2} + 9k_\theta} \\ v = \frac{k_r a_{A13-N}^2 - 6k_\theta}{k_r a_{A13-N}^2 + 18k_\theta}. \end{cases} \quad (5)$$

As a result, the  $k_r$  and  $k_\theta$  force field constants are assessed as follows:

$$k_r = \frac{3E_s}{\sqrt{3}(1-v)}, \quad (6)$$

$$k_\theta = \frac{E_s a_{A13-N}^2}{2\sqrt{3}(1+3v)}. \quad (7)$$

The parameters  $a_{A13-N}$ ,  $E_s$  and  $\nu$ , necessary for calculating the bond stretching,  $k_r$ , and bond bending,  $k_\theta$ , force constants (Equations (6) and (7)) together with calculated  $k_r$  and  $k_\theta$  values are presented in Table 3.

With regard to the torsion resistance force constant,  $k_\tau$ , the value calculated by Ansari et al. [75], based on the relationship of the  $k_\tau$  constant with the bending rigidity of the BN nanosheet, was adopted for SWBNNTs. For the remaining nitride NTs under study, the  $k_\tau$  was acquired using DREIDING force field [76], where the torsional behaviour is defined only by the hybridization of the diatomic nanostructure atoms. The values used for  $k_\tau$  are shown in Table 3.

**Table 3.** Bond length, surface Young's modulus and Poisson's ratio, and  $k_r$ ,  $k_\theta$  and  $k_\tau$  force field constants for BN, AlN, GaN, InN and TiN nanotubes.

| Compound | $a_{A13-N}$ , nm<br>[65] | $E_s$ , nN/nm<br>[65] | $\nu$ [65] | $k_r$ , nN/nm | $k_\theta$ , nN·nm/rad <sup>2</sup> | $k_\tau$ , nN·nm/rad <sup>2</sup> |
|----------|--------------------------|-----------------------|------------|---------------|-------------------------------------|-----------------------------------|
| BN       | 0.145                    | 267                   | 0.21       | 585           | 0.994                               | 2.470                             |
| AlN      | 0.179                    | 116                   | 0.46       | 372           | 0.451                               |                                   |
| GaN      | 0.185                    | 110                   | 0.48       | 366           | 0.445                               |                                   |
| InN      | 0.206                    | 67                    | 0.59       | 283           | 0.296                               | 0.625                             |
| TiN      | 0.2154*                  | 34.5*                 | 0.689*     | 192           | 0.151                               |                                   |

\* Values from Ye and Peng [1].

Finally, based on Equations (4) and the values of  $k_r$ ,  $k_\theta$ , and  $k_\tau$  from Table 3, and taking into account the equality of the bond and beam lengths,  $a_{A13-N} = l$ , it is possible to calculate of the input values for the numerical simulation (geometrical and elastic properties of the beams) according to Table 4, together with their respective formulation.

**Table 4.** Geometrical and elastic properties of beams as input parameters in FE simulations.

| Compound | diameter<br>'<br>d, nm | Formula<br>tion                    | Young's<br>modulus,<br>$E_b$ , GPa | Formula<br>tion | Shear<br>modulus,<br>$G_b$ , GPa | Formula<br>tion   | Poisson's<br>ratio, $\nu_b$ |
|----------|------------------------|------------------------------------|------------------------------------|-----------------|----------------------------------|-------------------|-----------------------------|
| BN       | 0.1648                 |                                    | 3977                               |                 | 4941                             |                   | 0.21 [65]                   |
| AlN      | 0.1392                 |                                    | 4374                               | $E_b =$         | 3032                             | $G_b =$           | 0.46 [65]                   |
| GaN      | 0.1395                 | $d = 4\sqrt{\frac{k_\theta}{k_r}}$ | 4437                               | $k_r^2 l$       | 3113                             | $k_r^2 k_\tau l$  | 0.48 [65]                   |
| InN      | 0.1294                 |                                    | 4432                               | $4\pi k_\theta$ | 4674                             | $8\pi k_\theta^2$ | 0.59 [65]                   |
| TiN      | 0.1120                 |                                    | 4200                               |                 | 8712                             |                   | 0.689 [1]                   |

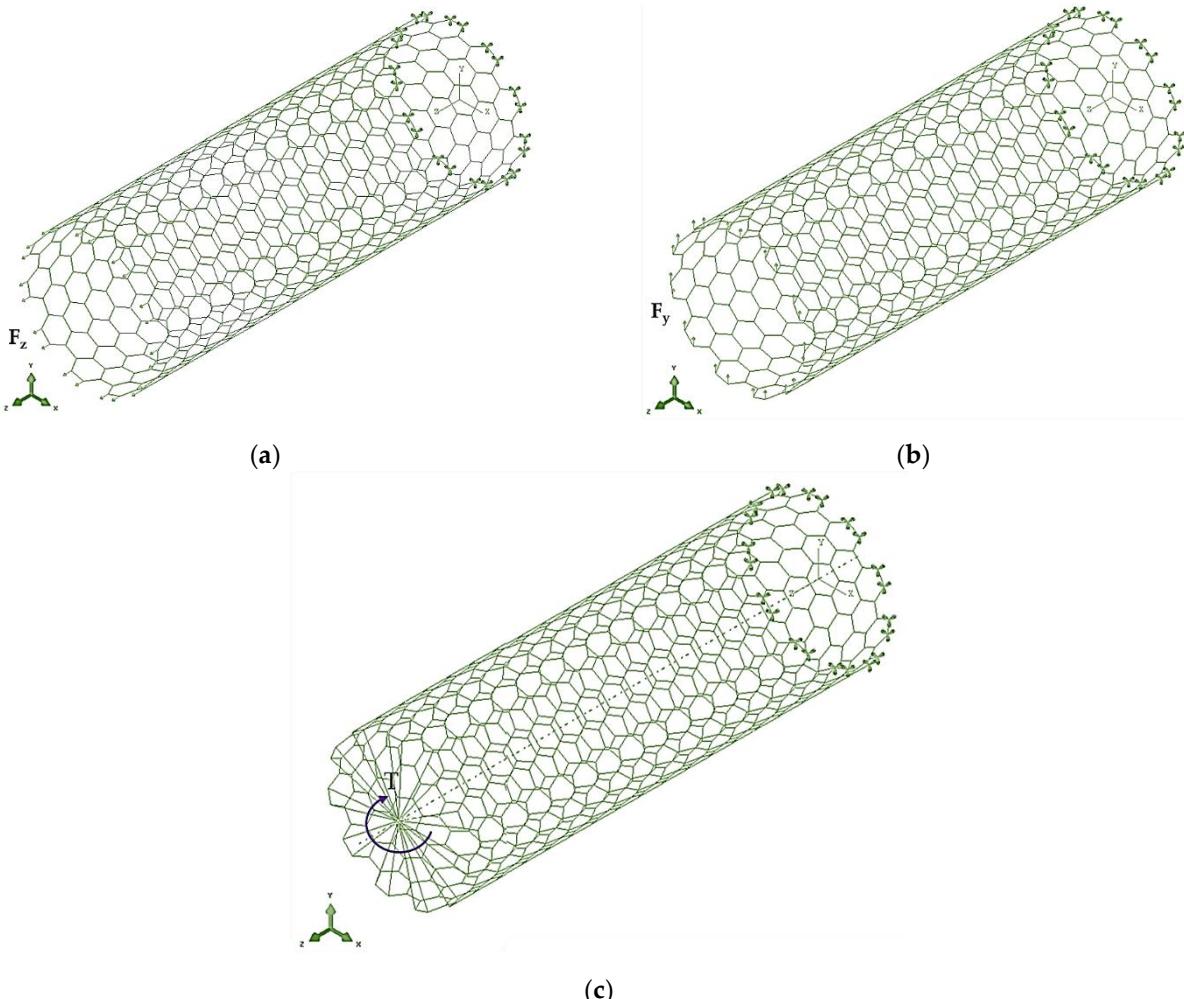
### 2.3. Elastic Properties of SWBNNTs, SWAlNNTs, SWGaNNTs, SWInNNTs and SWTiNNTs

Firstly, the tensile, EA, bending, EI, and torsional, GJ, rigidities of the 13th group – nitride nanotubes were obtained from the results of the FE analysis, carrying out tensile, bending, and torsion tests using the ABAQUS® FE code (see Figure 4). To perform each abovementioned test, the axial tensile force,  $F_z$ , the transverse force,  $F_y$ , and the torsional moment,  $T$ , were applied to one end of the NT. The boundary conditions applied at the opposed NT end, restricted all degrees of freedom of the nodes involved. In the torsion test, an additional boundary condition was imposed, which consists in preventing the edge nodes from moving in the radial direction, as shown in Figure 4c. Consequently, the tensile, bending and torsion tests made it possible to acquire the axial displacement,  $u_z$ , the transverse displacement,  $u_y$ , and the twist angle,  $\phi$ , directly from the FEA. These results are used to calculate the tensile, EA, bending, EI, and torsional, GJ, rigidities of the nitride NTs with the length  $L_n$  as follows:

$$EA = \frac{F_z L_n}{u_z}, \quad (8)$$

$$EI = \frac{F_y L_n^3}{3u_y}, \quad (9)$$

$$GJ = \frac{TL_n}{\varphi}. \quad (10)$$



**Figure 4.** Boundary and loading conditions applied in tests of: (a) tension, (b) bending and (c) torsion, of armchair SWInNNTs.

The tensile, EA, and bending, EI, rigidities from Equations (8) and (9), respectively, are required to assess the Young's modulus, E, of the nitride NTs as follows [77]:

$$E = \frac{EA}{\pi t_n \sqrt{8 \left( \frac{EI}{EA} \right) - t_n^2}}, \quad (11)$$

where  $t_n$  is the nanotube wall thickness. The knowledge of the valid value of  $t_n$  is not available for most of the 13th group element – nitride NTs, except for BNNTs.

To calculate the shear modulus, G, the torsional rigidity, GJ, obtained by Equation (10), is needed, in addition to the EA and EI rigidities. The evaluation of the Poisson's ratio,  $\nu$ , is based on the bending, EI, and torsional, GJ, rigidities, and  $\nu$  is independent of the value of  $t_n$ . The following expressions are used for assessment of G and  $\nu$  [78]:

$$G = \frac{GJ}{2\pi t_n \left( \frac{EI}{EA} \right) \sqrt{8 \left( \frac{EI}{EA} \right) - t_n^2}}, \quad (12)$$

$$v = \frac{E}{2G} - 1 = \frac{EI}{GJ} - 1. \quad (13)$$

Assuming the uncertainty of the values of the NT wall thickness, the surface Young's ( $E_s = Et_n$ ) and shear ( $G_s = Gt_n$ ) moduli, were calculated in the present study. In fact, the  $E_s$  and  $G_s$  elastic moduli are more reliable to describe the mechanical response of the nitride NTs, since they do not depend on the wall thickness. Considering that  $t_n^2 \ll 8 \left( \frac{EI}{EA} \right)$  and that the term  $t_n^2$  in Equations (11) and (12) can be neglected, the surface Young's,  $E_s$ , and shear,  $G_s$ , moduli are determined, respectively, as follows:

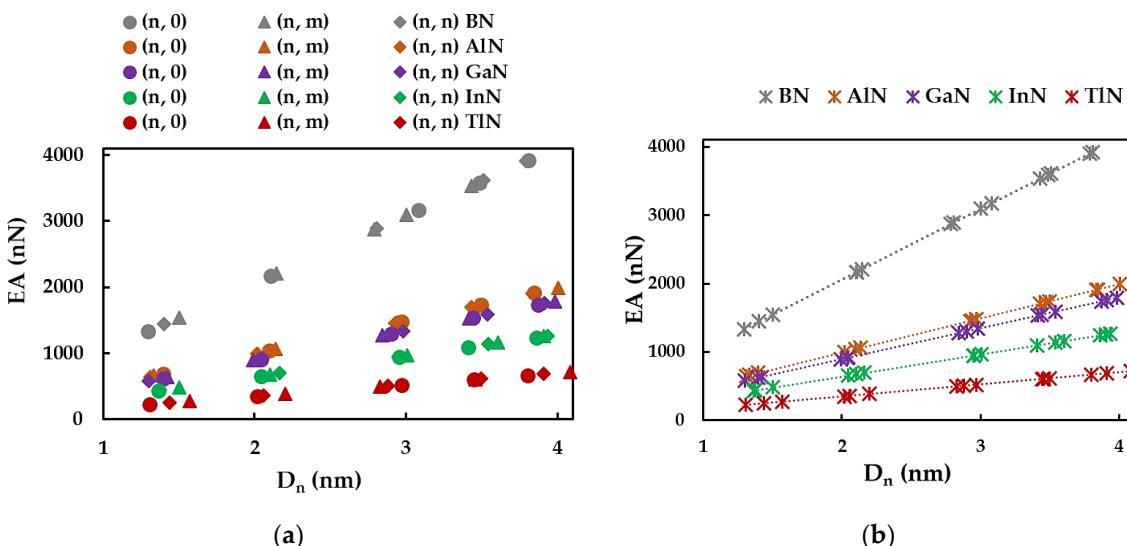
$$E_s = Et_n = \frac{EA}{\pi \sqrt{8 \left( \frac{EI}{EA} \right)}}, \quad (14)$$

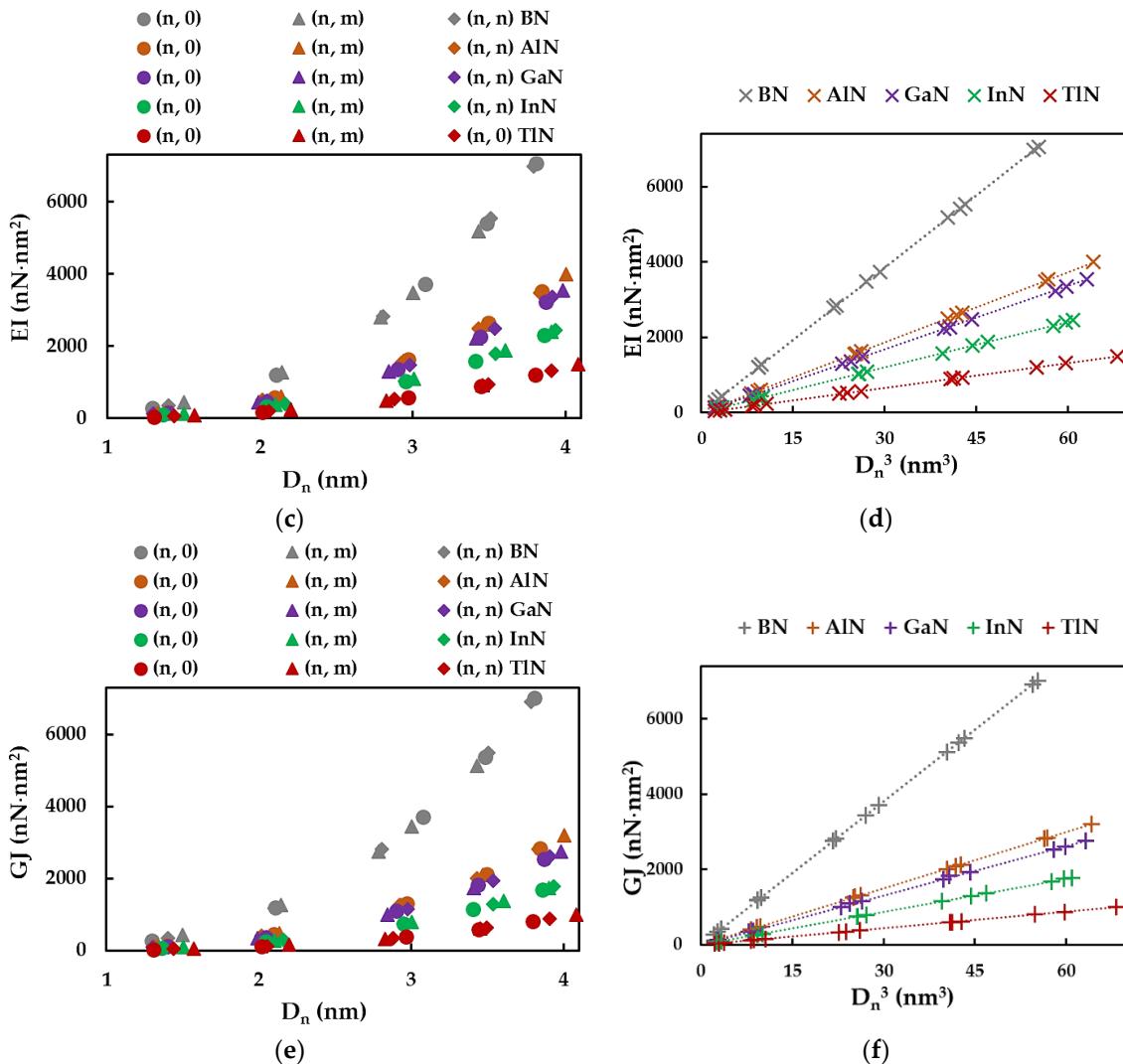
$$G_s = Gt_n = \frac{GJ}{2\pi \left( \frac{EI}{EA} \right) \sqrt{8 \left( \frac{EI}{EA} \right)}}. \quad (15)$$

### 3. Results and Discussion: Elastic Properties of SWBNNTs, SWAlNNTs, SWGaNNTs, SWInNNTs and SWTINNTs

#### 3.1. Rigidities

The tensile, EA, bending, EI, and torsional, GJ, rigidities of the SWBNNTs, SWAlNNTs, SWGaNNTs, SWInNNTs and SWTINNTs, calculated by Equations (8) – (10) from the FEA results, are plotted as a function of the nanotube diameter,  $D_n$ , in Figure 5a,c,e. For each of the rigidities EA, EI and GJ, the same trend is observed with the increase of the nanotube diameter, regardless of the NTs symmetry group (zigzag, chiral or armchair) and the nanotube compound. It is worth noting that the EA, EI and GJ rigidities decrease from the values obtained for SWBNNTs to those for SWTINNTs. As previously established for the phosphide [79] and carbide [80,81] nanotubes, in the case of the 13th group element – nitride NTs, the tensile rigidity, EA, can be represented by a linear function of  $D_n$  (Figures 5a,b), while the bending, EI, and torsional, GJ, rigidities can be represented by a linear function of  $D_n^3$  (Figure 5c,e and Figure 5d,f).





**Figure 5.** Evolutions of: (a,b) Tensile, EA, (b) Bending, EI, and (c) Torsional, GJ, rigidities as a function of the NT diameter,  $D_n$ , and (d) Bending, EI, and (f) Torsional, GJ, rigidities as a function of  $D_n^3$ , for the SWBNNTs, SWAlNNTs, SWGaNNTs, SWInNNTs and SWTiNNTs in Table 2.

Similar to what was found in the authors' previous work for the phosphide [79] and carbide [80,81] nanotubes, the slope of the straight lines in Figures 5b,d,f can be determined as follows:

$$EA = \alpha_{A13-N} D_n, \quad (16)$$

$$EI = \beta_{A13-N} D_n^3, \quad (17)$$

$$GJ = \gamma_{A13-N} D_n^3. \quad (18)$$

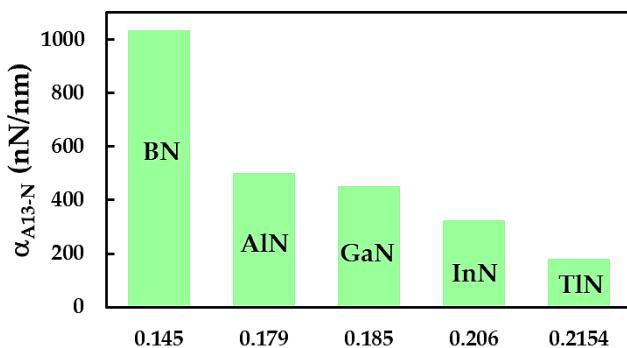
In these equations,  $\alpha_{A13-N}$ ,  $\beta_{A13-N}$  and  $\gamma_{A13-N}$  are fitting parameters and  $D_n$  is the diameter of the nitride NTs. The values of these parameters, determined as slope of the dash lines in the graphs of Figures 5b,d,f, together with the mean differences between the values of EA, EI and GJ evaluated by the analytical expressions (16)–(18) and those derived from FEA (Equations (8)–(10)), are shown in Table 5. It can be seen in this table that the mean difference does not exceed 0.58%. Therefore, Equations (16)–(18) result in accurate values the three rigidities of SWBNNTs, SWAlNNTs, SWGaNNTs, SWInNNTs and SWTiNNTs, and can be used to evaluate the EA, EI and GJ rigidities without resource of numerical simulation.

**Table 5.** Fitting parameters  $\alpha_{A13-N}$ ,  $\beta_{A13-N}$  and  $\gamma_{A13-N}$  for SWBNNTs, SWAINNTs, SWGaNNTs, SWInNNTs and SWTINNTs and mean difference between the EA, EI and GJ rigidities calculated with the aid of these parameters (Equations (16) – (18)) and the corresponding rigidities acquired from FEA.

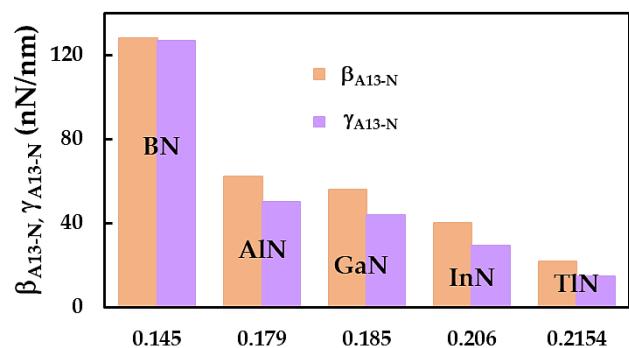
| Com-<br>poun-<br>d | Fitting parameters          |                            |                             | Mean difference, % |                        |                        |
|--------------------|-----------------------------|----------------------------|-----------------------------|--------------------|------------------------|------------------------|
|                    | $\alpha_{A13-N}$ ,<br>nN/nm | $\beta_{A13-N}$ ,<br>nN/nm | $\gamma_{A13-N}$ ,<br>nN/nm | EA, nN             | EI, nN·nm <sup>2</sup> | GJ, nN·nm <sup>2</sup> |
| BN                 | 1029.96 <sup>1</sup>        | 128.08 <sup>1</sup>        | 126.93 <sup>1</sup>         | 0.08               | 0.23                   | 0.08                   |
| AlN                | 497.38                      | 62.09                      | 49.94                       | 0.23               | 0.36                   | 0.31                   |
| GaN                | 448.92                      | 55.99                      | 43.78                       | 0.24               | 0.34                   | 0.58                   |
| InN                | 321.72 <sup>1</sup>         | 40.14 <sup>1</sup>         | 29.28 <sup>1</sup>          | 0.32               | 0.49                   | 0.31                   |
| TiN                | 175.71                      | 21.92                      | 14.60                       | 0.41               | 0.56                   | 0.54                   |

<sup>1</sup> Values of the fitting parameters for the BNNTs and InNNTs are similar to those obtained in the author's previous works [49,61].

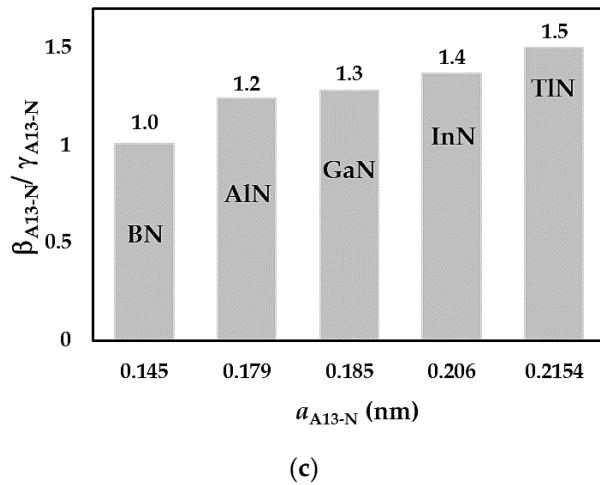
The fitting parameters  $\alpha_{A13-N}$ ,  $\beta_{A13-N}$  and  $\gamma_{A13-N}$  in Table 5 allow quantifying the tensile, EA, bending, EI, and torsional, GJ, rigidities, respectively, thereby describing the mechanical response of nanotubes under tension, bending and torsion. To this end, the values of  $\alpha_{A13-N}$ , and  $\beta_{A13-N}$  together with  $\gamma_{A13-N}$  are presented in Figure 6a,b, respectively, for the bond lengths,  $a_{A13-N}$ , corresponding to the SWBNNTs, SWAINNTs, SWGaNNTs, SWInNNTs and SWTINNTs. All three fitting parameters drop from SWBNNTs to SWAINNTs, then the  $\alpha_{A13-N}$ ,  $\beta_{A13-N}$  and  $\gamma_{A13-N}$  values decrease gradually, when moving to SWTINNTs, i.e. as the  $a_{A13-N}$  value increases (see Figure 6a,b). With regard to the relationship between bending, EI, and torsional, GJ, rigidities, which can be defined by the ratio between respective fitting parameters,  $\beta_{A13-N}$  and  $\gamma_{A13-N}$ , the ratio  $\beta_{A13-N}/\gamma_{A13-N} \approx 1$  for the SWBNNTs (see Figure 6c). It suggests that in this case, the EI and GJ rigidities are practically identical. For the remaining cases, the ratio of  $\beta_{A13-N}/\gamma_{A13-N}$  becomes nearly equal to 1.2 for the SWAINNTs, and continues increasing in increments of 0.1 up to  $\beta_{A13-N}/\gamma_{A13-N} \approx 1.5$  for the SWTINNTs. As seen in Figure 6c, increasing of the bond length,  $a_{A13-N}$ , leads to the decrease in torsional rigidity and, subsequently, to the more significant difference between the EI and GJ rigidities. It can be concluded that the SWInNNTs and SWTINNTs with longer bond lengths,  $a_{In-N} = 0.206$  nm and  $a_{Ti-N} = 0.215$  nm, respectively, have weaker torsional properties when compared with those of the other 13th group atom –nitrides NTs.



(a)



(b)



(c)

**Figure 6.** Fitting parameters as a function of the bond lengths,  $a_{A13-N}$ : (a)  $\alpha_{A13-N}$ ; (b)  $\beta_{A13-N}$  together with  $\gamma_{A13-N}$ , and (c)  $\beta_{A13-N}/\gamma_{A13-N}$  ratio for SWBNNTs, SWAlNNTs, SWGaNNTs, SWInNNTs and SWTiNNTs.

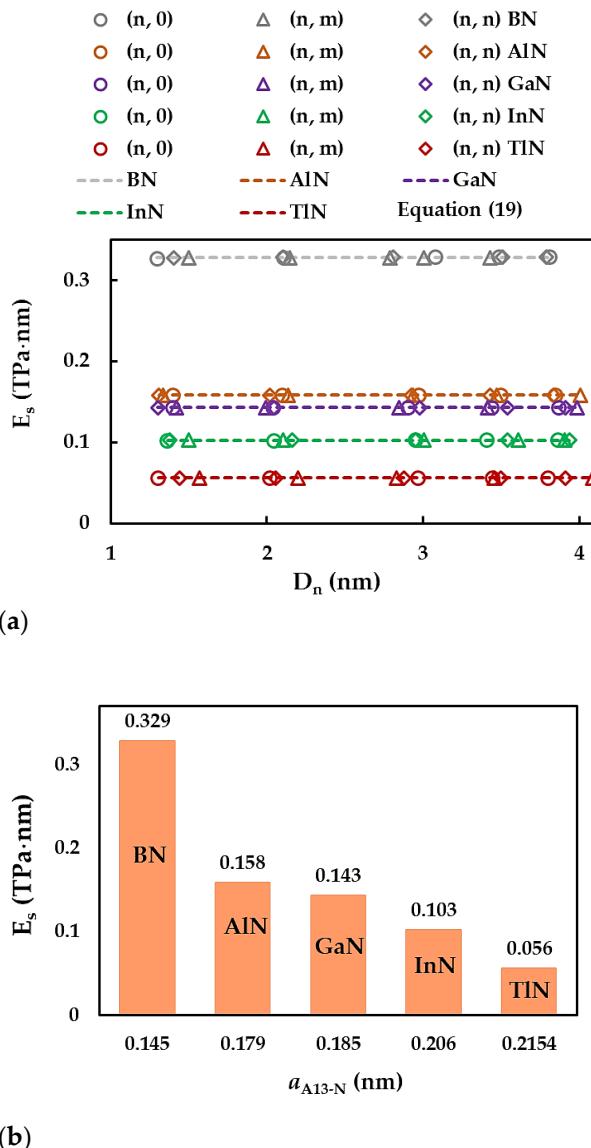
### 3.2. Surface Young's Modulus

The surface Young's modulus,  $E_S$ , of the SWBNNTs, SWAlNNTs, SWGaNNTs, SWInNNTs and SWTiNNTs was assessed by Equation (14), which makes use of the results of the numerical tensile and bending tests. In addition, it is possible to obtain an analytical expression for  $E_S$ , which does not depend on  $D_n$ . For this, the tensile, EA, and bending, EI, rigidities in Equation (14) are replaced by expressions (16) and (17), leading to the following equation:

$$E_S = \frac{\alpha_{A13-N}}{\pi \sqrt{8 \left( \frac{\beta_{A13-N}}{\alpha_{A13-N}} \right)}}. \quad (19)$$

where  $\alpha_{A13-N}$  and  $\beta_{A13-N}$  are fitting parameters from Table 5.

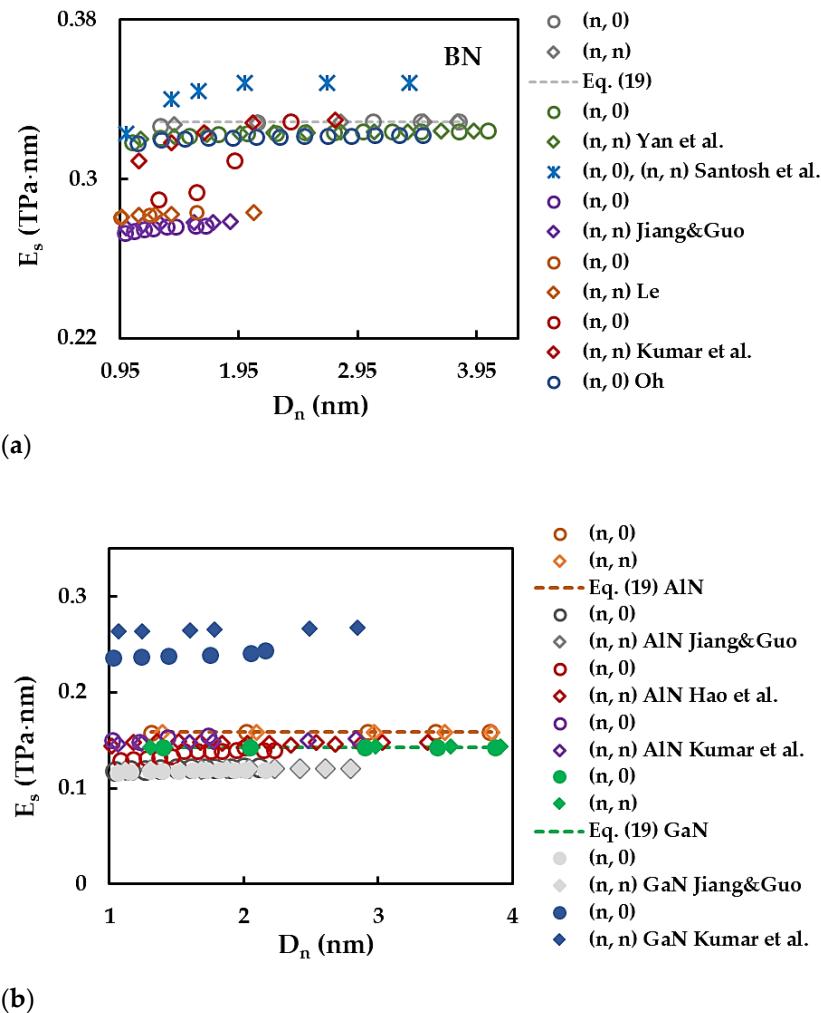
Figure 7a shows the evolutions of the surface Young's modulus,  $E_S$ , assessed by Equation (14) with the NT diameter,  $D_n$ , for all single-walled nitride nanotubes studied. The results of  $E_S$  calculated by Equation (19) are also plotted in Figure 7a, by dashed lines. For the 13th group – nitride NTs, regardless of the chiral angle (zigzag, chiral or armchair NTs) as well the compound (BN, AlN, GaN, InN or TiN), the surface Young's modulus is quasi-constant with increasing the NTs diameter, through the range of  $D_n$  considered in the current work. It can be concluded from Figure 7a that Equation (19) permits an accurate evaluation of the surface Young's modulus of nitride nanotubes. In fact, the mean differences between the values of  $E_S$  analytically evaluated by Equation (19) and those determined from the FEA with the aid of Equation (14) are 0.18%, 0.08%, 0.10%, 0.12% and 0.17% for the SWBNNTs, SWAlNNTs, SWGaNNTs, SWInNNTs and SWTiNNTs, respectively. As a result, the elastic properties of the nitride NTs can be accurately evaluated without resorting to numerical simulation. To examine the influence of the first element (B, Al, Ga, In, Ti) of nitride compound forming the nanotube on the  $E_S$  results, the values of the surface Young's modulus,  $E_S$ , assessed by Equation (19) are plotted in Figure 7b, considering the respective bond lengths,  $a_{A13-N}$ .



**Figure 7.** Evolutions of surface Young's modulus,  $E_s$ , for SWBNNTs, SWAlNNTs, SWGaNNTs, SWInNNTs and SWTINNTs as a function of the: (a) NT diameter,  $D_n$ , and (b) bond lengths,  $a_{A13-N}$ .

The  $E_s$  value decreases by almost half when moving from SWBNNTs to SWAlNNTs, and  $E_s$  continues to decrease at a slower rate with increasing interatomic bond length,  $a_{A13-N}$ . The surface Young's modulus of SWTINNTs ( $a_{Ti-N} = 0.215$  nm) is about 6 times lower when compared to that obtained for the SWBNNTs ( $a_{B-N} = 0.145$  nm). This decreasing trend of surface Young's modulus with increasing bond length was also reported by Jiang and Guo [64], for nitride and phosphide NTs, and by Sakharova et al. [79], for phosphide NTs.

Figure 8 compares the surface Young's modulus,  $E_s$ , values obtained for SWBNNTs (Figure 8a), and SWAlNNTs and SWGaNNTs (Figure 8b) with those available in the literature. Comprehensive comparison of the Young's modulus results of SWBNNTs with literature was carried out in a previous work by the authors [49], and therefore only a few selected  $E_s$  values were currently chosen. The  $E_s$  results of Hao et al. [51], Kumar et al. [53], Santosh et al. [58], Oh [60], and Yan et al. [62], were calculated from the Young's modulus,  $E$ , using the equality  $E_s = Et_n$ , for the NT wall thickness  $t_n = 0.333$  nm [62], 0.340 nm [58], 0.330 nm [53,60] and 0.410 nm [51].



**Figure 8.** Comparison of the current evolutions of the surface Young's modulus,  $E_s$ , with those available in the literature, for: (a) SWBNNTs and (b) SWAlNNTs and SWGaNNTs, as a function of the NT diameter,  $D_n$ , [51,53,58–60,62,64].

A good agreement is observed when the current values of the SWBNNTs surface Young's modulus are compared with those reported by Yan et al. [62] for non-chiral (zigzag and armchair) NTs (difference  $\approx 1.30\%$ ), Oh [60] for zigzag NTs (difference  $\approx 2.00\%$ ), and Kumar et al. [53] for armchair NTs with  $D_n \gtrsim 1$  nm (difference  $\approx 0.36\%$ ) and zigzag NTs with  $D_n \gtrsim 1.95$  nm (difference  $\approx 0.14\%$ ), as seen in Figure 8a. The  $E_s$  values of the SWAlNNTs evaluated in the present study are about 4.6% and 6.9% lower than those obtained in the works by Kumar et al. [53] and Hao et al. [51], respectively (Figure 8b). With regard to SWGaNNTs, a scattering of the surface Young's modulus results is noticeable (see Figure 8b). Whatever the case, SWAlNNTs or SWGaNNTs, more Young's modulus results are needed to build a reliable benchmark to ascertain their elastic properties by theoretical methods.

### 3.3. Surface Shear Modulus and Poisson's Ratio

In this section, two elastic properties are discussed that require torsional rigidity in addition to tensile and bending rigidities or just bending rigidity for their calculation, i.e. surface shear modulus and Poisson's ratio, respectively.

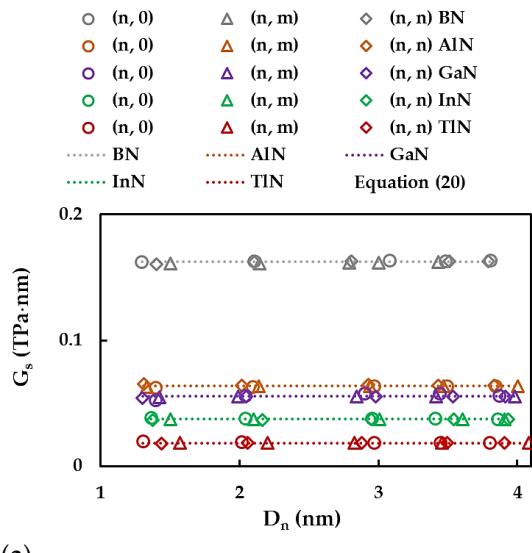
The surface shear modulus,  $G_s$ , of the SWBNNTs, SWAlNNTs, SWGaNNTs, SWInNNTs and SWTiNNTs was evaluated by Equation (15), which makes use of the results of the numerical tensile, bending and torsional tests. Also, by replacing in Equation (15) the tensile, EA, bending, EI, and

torsional, GJ, rigidities from expressions (16)–(18) and knowing the fitting parameters,  $\alpha_{A13-N}$ ,  $\beta_{A13-N}$  and  $\gamma_{A13-N}$ , from Table 5,  $G_s$  can be assessed analytically by the following expression:

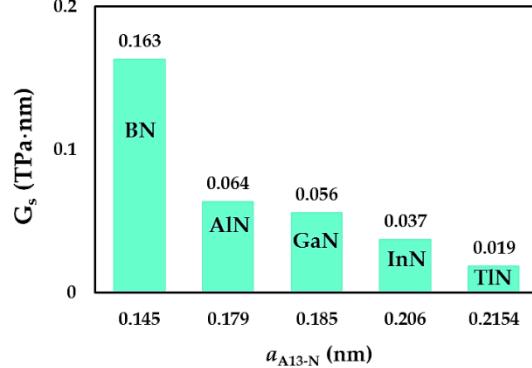
$$G_s = \frac{\gamma_{A13-N}}{\pi \sqrt{32 \left( \frac{\beta_{A13-N}}{\alpha_{A13-N}} \right)^3}}, \quad (20)$$

which allows calculating  $G_s$  without needing to know the NTs diameter,  $D_n$ .

The evolutions of the surface shear modulus,  $G_s$ , calculated by Equation (15) as a function of the NT diameter,  $D_n$ , together with the  $G_s$  values evaluated using Equation (20) are plotted in Figure 9a, for the cases of SWBNNTs, SWAINNTs, SWGaNNTs, SWInNNTs and SWTINNTs. For nitride nanotubes, whatever the NTs symmetry and the first element of nitride compound forming the NT, the surface shear modulus is quasi-constant with increasing of  $D_n$ . The mean differences between the  $G_s$  values calculated analytically by Equation (20) and those obtained from the FEA results with the help of Equation (15) are 0.13%, 0.17%, 0.59%, 0.19% and 0.26% (1.46%, 1.74%, 2.83%, 2.45% and 1.97% for NTs with  $D_n \lesssim 1.5$  nm), for the SWBNNTs, SWAINNTs, SWGaNNTs, SWInNNTs and SWTINNTs, respectively. It can be concluded that Equation (20) allows an accurate evaluation of the surface shear modulus of the 13th group atom – nitride nanotubes, across the entire range of the NT diameters considered in the present study, although the error obtained for NTs with  $D_n$  up to 1.5 nm is slightly higher. The  $G_s$  values calculated by Equation (20) are shown in Figure 9b as a function of the bond length,  $a_{A13-N}$ .



(a)

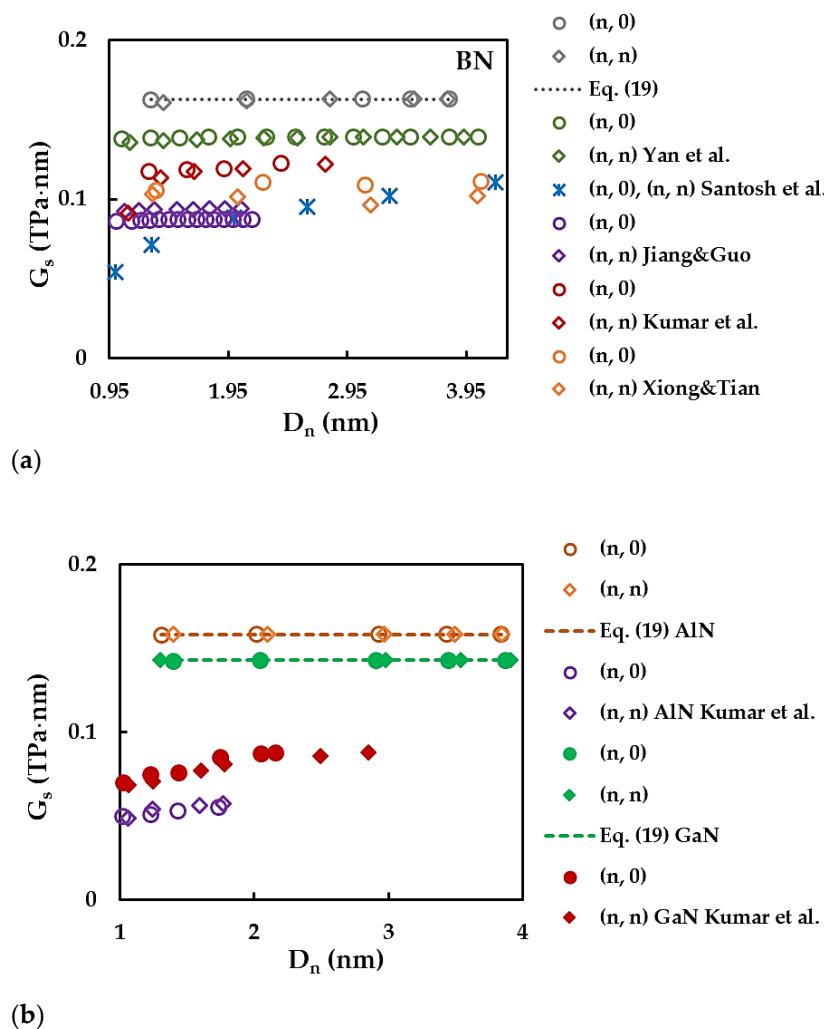


(b)

**Figure 9.** Evolutions of the surface shear modulus,  $G_s$ , for SWBNNTs, SWAlNNTs, SWGaNNTs, SWInNNTs and SWTInNNTs as a function of the: (a) NT diameter,  $D_n$ , and (b) bond length,  $a_{A13-N}$ .

Similar to what was established for the surface Young's modulus, the surface shear modulus,  $G_s$ , values decrease gradually with increasing the bond length, after an initial drop when moving from SWBNNTs to SWAlNNTs.

The  $G_s$  results available in the literature are scarce even for the case of SWBBNTs and show considerable discrepancy as seen in Figure 10a,b. Xiong and Tian [55], Kumar et al. [53], Santosh et al. [58] and Yan et al. [62] reported shear modulus,  $G$ , values. To enable a comparison, the respective surface shear modulus was calculated by using  $G_s = Gt_n$  for the NT wall thickness  $t_n = 0.330$  nm [53], 0.333 nm [62], 0.340 nm [58]. Xiong and Tian [55] did not report any  $t_n$  value, so in this case  $t_n = 0.34$  nm [49] was used.



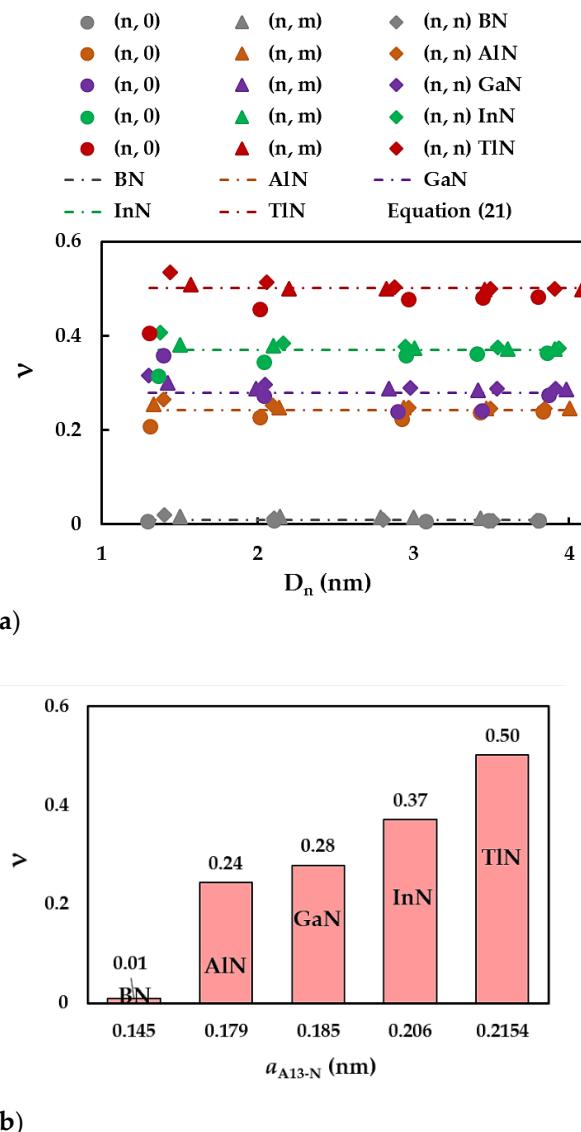
**Figure 10.** Comparison of the current evolutions of the surface shear modulus,  $G_s$ , with those available in the literature, for: (a) SWBNNTs and (b) SWAlNNTs and SWGaNNTs, as a function of the NT diameter,  $D_n$  [53,55,58,62,68].

The Poisson's ratio,  $\nu$ , of nitride nanotubes was assessed by Equation (13), using the EI and GJ rigidities, obtained from bending and torsional tests, respectively, and the  $\beta_{A13-N}$  and  $\gamma_{A13-N}$  fitting parameters in Table 5. This equation can be combined with expressions (17) and (18) for EI and GJ rigidities, to calculate  $\nu$ , as follows:

$$v = \frac{\beta_{\text{A13-N}}}{\gamma_{\text{A13-N}}} - 1, \quad (21)$$

whose expression is independent of the NT diameter.

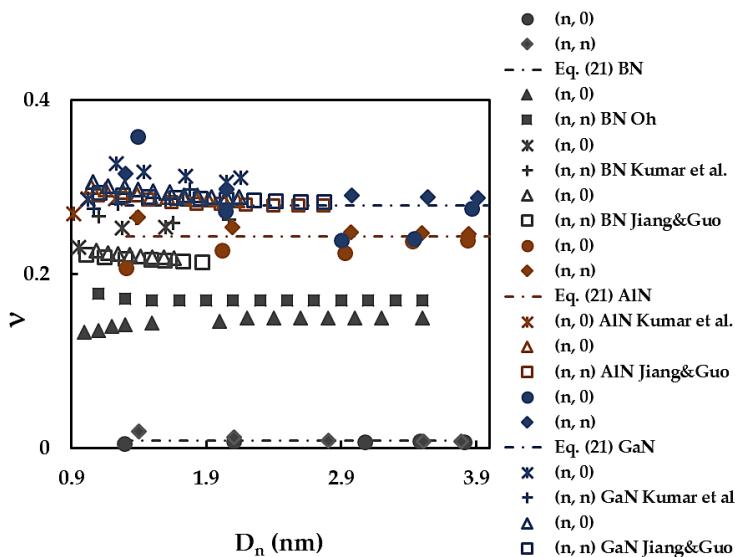
Figure 11a shows the evolution of the Poisson's ratio,  $v$ , calculated by Equation (13), with the NTs diameter,  $D_n$ , for the SWBNNTs, SWAlNNTs, SWGaNNTs, SWInNNTs and SWTINNTs in Table 3. The values of  $v$  calculated by Equation (21) are also presented in the Figure 11a. For zigzag, chiral and armchair nitride NTs with high value of  $D_n$ , the Poisson's ratio converges to the constant value calculated by Equation (21). The higher the value of the bond length,  $a_{\text{A13-N}}$ , the bigger the nanotube diameter,  $D_n^{\text{st}}$ , for which  $v$  becomes stable (see Figure 11a). The  $D_n^{\text{st}}$  values are approximately 1.4 nm, 2.0 nm, 2.1 nm, 3.0 nm and 3.4 nm for SWBNNTs, SWAlNNTs, SWGaNNTs, SWInNNTs and SWTINNTs, respectively. Similar qualitative results were reported for 13th group element - phosphide nanotubes [79]. For nitride NTs with diameter  $D_n < D_n^{\text{st}}$ , the Poisson's ratio increases for  $(n, 0)$  zigzag NTs, almost does not change for  $(n, m)$  chiral NTs and decreases for  $(n, n)$  armchair NTs.



**Figure 11.** Evolutions of the Poisson's ratio,  $v$ , for SWBNNTs, SWAlNNTs, SWGaNNTs, SWInNNTs and SWTINNTs as a function of the: (a) NT diameter,  $D_n$ , and (b) bond length,  $a_{\text{A13-N}}$ .

To understand the effect of first element (B, Al, Ga, In, Tl) of nitride NTs on the Poisson's ratio, the values of  $\nu$  assessed by Equation (21) are shown in Figure 11b as a function of the bond length,  $a_{A13-N}$ . The lowest value of  $\nu = 0.01$  was found for SWBNNTs. The Poisson's ratio grows up to 0.24 when moving from SWBNNTs to SWAINNTs, and then,  $\nu$  continues to increase with increasing bond length. The highest  $\nu$  value equal to 0.50 is observed for the SWTINNTs, which value is about 50 times greater than that of SWBNNTs. This difference can be explained by the relationship between bending, and torsional rigidities,  $EI/GJ$ , necessary to determine  $\nu$  by Equations (13) and (21). In fact, the  $\beta_{A13-N} / \gamma_{A13-N}$  ratio is approximately equal to 1 and 1.5, for the SWBNNTs and SWTINNTs, respectively. This means that bending,  $EI$ , and torsional,  $GJ$ , rigidities are almost the same for the boron nitride NTs and  $EI > GJ$  for the thallium nitride NTs, resulting in a substantial increase in the  $\nu$  value of SWTINNTs. The increase in Poisson's ratio with increasing bond length was reported in the works by Jiang and Guo [64], for nitride and phosphide NTs, and by Sakharova et al. [79], for phosphide NTs.

Figure 12 compares the current Poisson's ratio results with those available in the literature for the cases of SWBNNTs, SWAINNTs and SWGaNNTs. A good agreement, with a difference of  $\approx 2\%$ , is found when the value of  $\nu$  calculated by Equation (21) for SWGaNNTs is compared with that reported by Jiang and Guo [64] for the non-chiral GaN nanotubes. The Poisson's ratios evaluated by Kumar et al. [53] for  $(n, 0)$  and  $(n, n)$  GaNNTs are  $\approx 8\%$  lower and  $\approx 6\%$  higher, respectively, than the  $\nu$  values currently obtained. In other cases presented in Figure 12 there is considerable scattering of the  $\nu$  values.



**Figure 12.** Comparison of the current evolutions of the Poisson's ratio,  $\nu$ , for SWBNNTs, SWAINNTs and SWGaNNTs with those available in the literature, as a function of the NT diameter,  $D_n$  [53,60,64].

Jiang and Guo [64] reported for both armchair and zigzag SWBNNTs, SWAINNTs and SWGaNNTs the trends in the evolutions of the Poisson's ratio as a function of NTs diameter,  $D_n$ , for which  $\nu$  decreases with increasing  $D_n$ , and afterwards, the value of  $\nu$  converges to an almost constant value (see Figure 12). This trend is in line with the current one for the evolutions of  $\nu$  as a function of  $D_n$ , for armchair BN, AlN and GaN nanotubes, although, the decreasing rate found by Jiang and Guo [64] is slower.

#### 4. Conclusions

The elastic properties, including the three rigidities, tensile, bending and torsional, the surface Young's and shear moduli and the Poisson's ratio of SWBNNTs, SWAINNTs, SWGaNNTs, SWInNNTs and SWTINNTs, were evaluated in a numerical simulation study, based on the NCM/MSM approach. The main conclusions are specified below.

Analytical expressions, which allow evaluating the three rigidities as a function of the NTs diameter and the fitting parameters without resorting to numerical simulation, were obtained for the most complete set of the 13th group atom - nitride nanotubes.

Also, the knowledge of these fitting parameters permits accurate analytical assessment of the surface Young's and shear modulus of the SWBNNTs, SWAlNNTs, SWGaNNs, SWInNNTs and SWTINNTs with diameters,  $D_n$ , higher than 1.25 nm, and the Poisson's ratio, limiting to the nanotubes with diameters,  $D_n > D_n^{\text{st}}$ . The longer the bond length, the higher the value of  $D_n^{\text{st}}$ , for which the Poisson's ratio does not change with the increase in the NT diameter.

The tensile, bending and torsional rigidities, the surface Young's and shear moduli, and the Poisson's ratio of SWBNNTs, SWAlNNTs, SWGaNNs, SWInNNTs and SWTINNTs are sensitive to the interatomic bond length of the hexagonal lattice. The three rigidities, and the surface Young's and shear moduli decrease, while the Poisson's ratio increases, with increasing bond length.

The results presented constitute a considerable contribution to a benchmark about the determination of the elastic properties of nitride nanotubes by theoretical methods.

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