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Posted Date: 27 December 2023

doi: 10.20944/preprints202312.2109.v1

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Article

Theoretical Study on the Structures and Stabilities of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1 - 4$) Clusters: Sequential Doping of Zn_3O_3 Cluster with Cu Atoms

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Abstract: Density functional theory (DFT) and coupled cluster theory (CCSD(T)) calculations are performed to investigate the geometric, electronic structures and chemical bonding of a series of Cu-doped zinc oxide clusters, $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$). The structural evolution of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) clusters are elaborated in our work. The planar seven-membered ring of CuZn_3O_3 cluster plays an important role in the structural evolution, that is, the Cu atom, Cu dimer (Cu_2) and Cu trimer (Cu_3) anchor on the CuZn_3O_3 cluster. The aggregate behavior of Cu atoms on Zn_3O_3 may offer insight into the study of Cu/ZnO-based catalysts. Additionally, it is found that the $\text{Cu}_n\text{Zn}_3\text{O}_3$ clusters become more stable as the Cu content (n) increases. Bader charge analysis points out that as the Cu atoms doping, the reducibility of Cu aggregation (Cu_{n-1}) on the CuZn_3O_3 cluster increases. Combined with the d-band centers and the surface electrostatic potential (ESP), the reactivity and the possible reaction sites of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) clusters are also illustrated.

Keywords: copper-doped zinc oxide clusters; density functional theory; structural evolution; reactivity

1. Introduction

Cu-based catalysts have played an important role in industry, such as electrocatalytic reduction of CO_2 , methanol steam reforming and water gas shift reaction.[1-4] But at the same time, Cu-based catalysts have still suffered some restrictions, such as thermal instabilities and low selectivity.[1,2] Cu-based catalysts are prone to sintering when the temperature rises above 300 °C.[2] Cu/ZnO catalysts is one of the commonly used Cu-based catalysts, in which Cu usually acts as the main active component, and ZnO plays the dual role of promoter and support.[5] Specifically, Cu^{2+} ions would be reduced to the active Cu^0/Cu^+ species, and the addition of ZnO would increase the copper dispersion and reducibility which are related to the enhanced catalytic activity.[3,6] Meanwhile, the sizes and geometries of the metal nano-particles and the species formed at the Cu-ZnO interface also affect the catalytic properties of Cu/ZnO catalysts. To develop the Cu-based catalysts with superior performance, the precise structures and the structure-activity relationship of catalytic active sites and the interaction of the main active component with the additives including the supports are the fundamental issues that needs to be solved.[7] In this regard, clusters which may serve as the models at the atomic level and the highly active catalytic materials have attracted great research interest.

Recently, well-supported single/dual-atom and cluster catalysts have become the research hotspots.[8-12] Among these, copper oxide clusters have been considered as the catalytic active sites of copper-exchanged zeolites in the methane oxidation to methanol.[12] Herein, copper oxide clusters with the different stoichiometries and sizes were embedded in the channel of zeolites, the geometries, stabilities of these clusters and their underlying correlations with the catalytic activities were elaborated. Additionally, a fully-exposed Cu_7 cluster anchored to the loop-like [6]cycloparaphenylene was found to be highly active and selective in the CO electro-reduction.[11] As for ZnO clusters, it is accepted that $(\text{ZnO})_n$ ($n < 8$) clusters favored the Zn-O alternating ring

structures. As the size (n) of $(\text{ZnO})_n$ clusters increased to 8, a ring-to-cage transition occurred.[13-15] In these stoichiometric $(\text{ZnO})_n$ ($n = 1-13$) clusters, $(\text{ZnO})_3$, $(\text{ZnO})_9$ and $(\text{ZnO})_{12}$ were found to possess relatively higher stability.[15] Moreover, the Zn_3O_3 six-membered ring can be found in the larger $(\text{ZnO})_n$ ($n > 8$) clusters and the hexagonal wurtzite structures of ZnO crystals.[14,16,17] Thus, the relatively stable Zn_3O_3 cluster may be used as a molecular model for the wurtzite ZnO surface.

We have constantly strived to explore the novel chemical bonding and the cluster models to gain further insights into the active sites of complicated catalyst surfaces and the reaction mechanisms of catalytic processes.[18-21] In this work, we make an effort to reveal the evolution rule of the geometric, electronic structures and chemical bonding in the Cu-doped $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) clusters. Bader charge analysis, d-band center theory and surface electrostatic potential (ESP) are used to analyze the reactivity and reaction sites of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) clusters. This work may enlighten the aggregation tendency of small Cu clusters on ZnO surface and the structures at the Cu-ZnO interface.

2. Methods

The initial geometries of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) clusters were constructed using the structural searches of the ABCluster program [22,23] in combination with the artificial constructions. These initial geometries were optimized using the B3LYP functional [24-26] in the Gaussian 09 program.[27] The Stuttgart small-core relativistic effective core potential (RECP) was used for the Cu and Zn atoms, whose corresponding basis sets are Cu: [6s,6p,4d,3f,2g], Zn: [6s,6p,4d,3f,2g].[28-31] As for O atoms, the aug-cc-pVTZ basis set was adopted.[32,33] In the structural optimizations, the vibrational frequencies were calculated to ensure that the optimized structures were free of imaginary frequencies. In order to verify the reliability of the above computational methods (denoted as B3LYP/BS), we compared the bond lengths, binding energies, vibrational frequencies and dipole moments of ZnO and CuO molecules from the available experiments with our calculations. As shown in Table S1, our calculations are in agreement with those data from experiments. The low-lying isomers within 0.50 eV at the B3LYP/BS level were then subjected to more accurate coupled cluster CCSD(T) single-point-energy calculations using the Molpro 2010 software.[34] Multiwfn program [35,36] was employed to analyze the Bader charge, surface electrostatic potential (ESP) and d-band centers of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 0-4$) clusters.

3. Results

It is accepted that Zn_3O_3 cluster is a planar six-membered-ring structure with D_{3h} symmetry (Figure 1a),[13] in which Zn and O atoms are alternately bonded ($d_{\text{Zn-O}} = 1.817 \text{ \AA}$). The distances between two Zn atoms are 2.654 \AA .

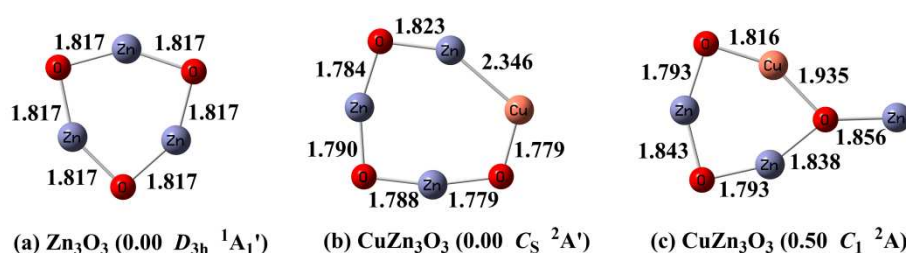


Figure 1. Optimized structures ($\Delta E \leq 0.50 \text{ eV}$) for Zn_3O_3 and CuZn_3O_3 . The bond lengths are in angstroms and the relative energies (ΔE) in eV are in the parentheses.

3.1. Optimized Structures of CuZn_3O_3

CuZn_3O_3 clusters are constructed by adding a Cu atom to the most stable Zn_3O_3 cluster. The most stable structure of CuZn_3O_3 is shown in Figure 1b, which is consistent with the previous theoretical study.[15] It can be regarded as inserting a Cu atom into the Zn-O bond of Zn_3O_3 cluster, leading to the planar seven-membered-ring structure. The second low-lying isomer (Figure 1c) lies 0.50 eV higher in energy, for which the six-membered Zn_3O_3 ring is broken. Other CuZn_3O_3 isomers are higher in energy by at least 0.50 eV. They are collected in the Supporting Information (Figure S1).

3.2. Optimized Structures of $\text{Cu}_2\text{Zn}_3\text{O}_3$

To search for the ground state of $\text{Cu}_2\text{Zn}_3\text{O}_3$ cluster, a Cu atom was added to the most stable CuZn_3O_3 cluster. The optimized $\text{Cu}_2\text{Zn}_3\text{O}_3$ clusters with the relative energy below 0.50 eV are shown in Figure 2. The ground state of $\text{Cu}_2\text{Zn}_3\text{O}_3$ cluster (Figure 2a) can be viewed as inserting a Cu atom into the Zn-Cu bond of CuZn_3O_3 cluster, resulting in a planar eight-membered-ring structure. It is consistent with the earlier finding of $\text{Cu}_2\text{Zn}_3\text{O}_3$ cluster.[15] The Cu-Cu bond length is 2.366 Å, slightly longer than Cu-Zn bond length (2.343 Å). It is in agreement with the covalent radius of the Cu and Zn atoms ($d_{\text{Cu}} = 1.52$ Å, $d_{\text{Zn}} = 1.45$ Å)[37] and suggests the metal-metal bonding of the inserting Cu atom with the neighboring Cu and Zn atoms. The second low-lying isomer (Figure 2b) which can be viewed as adding a bridged Cu to the CuZn_3O_3 ground state is 0.39 eV less stable than the ground state. Other isomers are found to be much higher in energy ($\Delta E > 0.50$ eV) which are given in the Supporting Information (Figure S2).

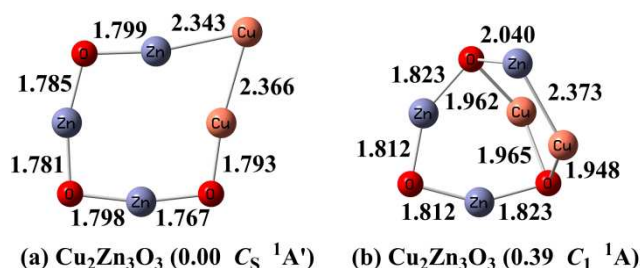


Figure 2. Optimized structures ($\Delta E < 0.50$ eV) for $\text{Cu}_2\text{Zn}_3\text{O}_3$. The bond lengths are in angstroms and the relative energies (ΔE) in eV are in the parentheses.

3.3. Optimized Structures of $\text{Cu}_3\text{Zn}_3\text{O}_3$

As the number of doped Cu atoms increases, more low-lying isomers appear for the $\text{Cu}_3\text{Zn}_3\text{O}_3$ clusters (Figure 3). The most stable $\text{Cu}_3\text{Zn}_3\text{O}_3$ cluster (Figure 3a) can be seen as adding a copper dimer (Cu_2) between two bridged oxygen atoms of the CuZn_3O_3 ground state. At this point, the 3-fold coordinated bridged oxygen atom ($\mu_3\text{-O}$) begins to appear in the ground states of $\text{Cu}_n\text{Zn}_3\text{O}_3$ clusters. The Cu-Cu bond length of Cu dimer (Cu_2) is 2.388 Å in $\text{Cu}_3\text{Zn}_3\text{O}_3$ cluster which is much longer than that (2.232 Å) of isolated Cu_2 molecule ($D_{\infty h}$ $^1\Sigma_g^+$) at the same calculation level. It is inferred that there are relatively strong interactions of the Cu_2 moiety with the remaining fragment of $\text{Cu}_3\text{Zn}_3\text{O}_3$. As shown in Figure 3, there are several isomers that have energies close to the ground state. To further distinguish the stability of these low-lying isomers, the single-point CCSD(T) calculations were performed using their B3LYP equilibrium geometries. The single-point CCSD(T) calculations still support the structure contained the Cu_2 (Figure 3a) to be the most stable $\text{Cu}_3\text{Zn}_3\text{O}_3$ cluster (Table S2). Other higher-energy isomers ($\Delta E > 0.50$ eV) are shown in the Supporting Information (Figure S3).

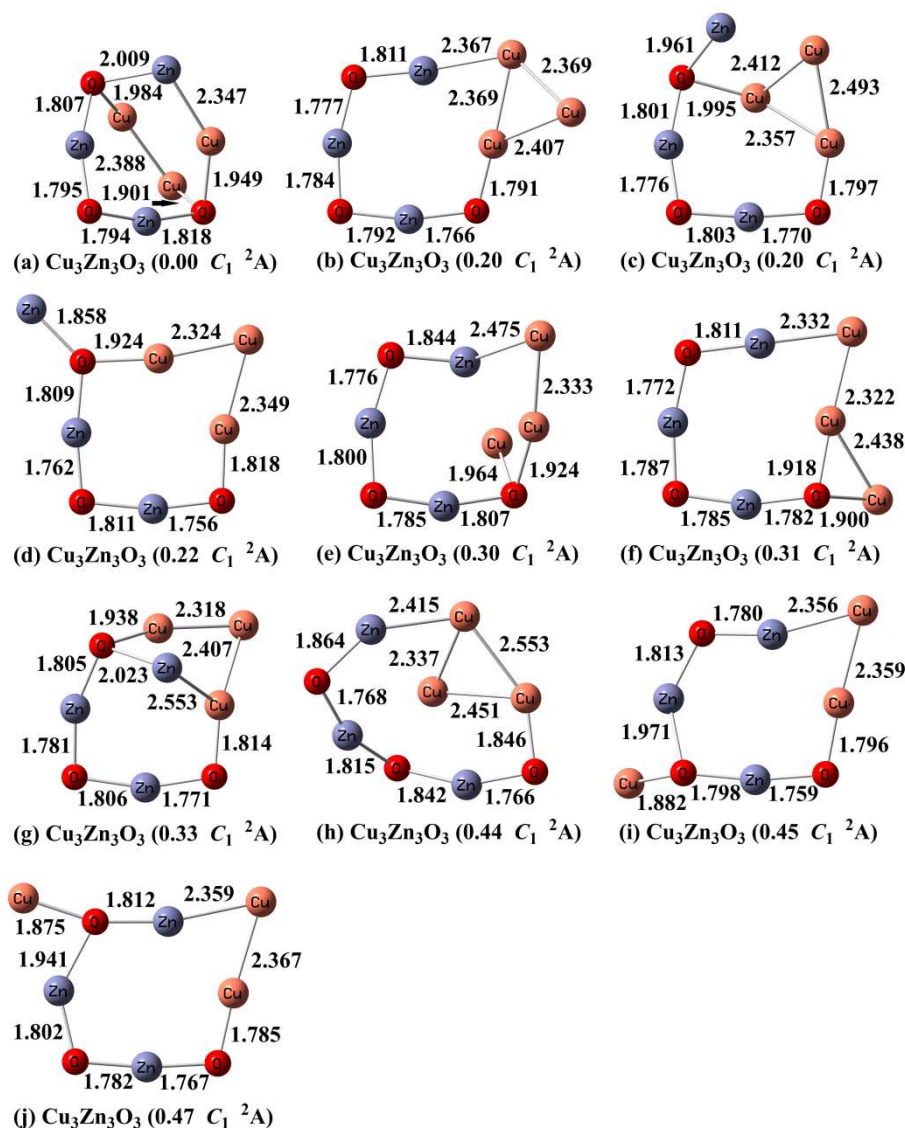


Figure 3. Optimized structures ($\Delta E < 0.50$ eV) for $\text{Cu}_3\text{Zn}_3\text{O}_3$. The bond lengths are in angstroms and the relative energies (ΔE) in eV are in the parentheses.

3.4. Optimized Structures of $\text{Cu}_4\text{Zn}_3\text{O}_3$

In our calculations, the most stable $\text{Cu}_4\text{Zn}_3\text{O}_3$ cluster is shown in Figure 4a. It can be viewed as adding a copper trimer (Cu_3) between two bridged oxygen atoms of the CuZn_3O_3 ground state. Meanwhile, several low-lying isomers within 0.50 eV were found (Figure 4). Among them, there is an isomer (Figure 4b) which contains the Cu_4 moiety and is only 0.10 eV higher in energy. The relative energies of these isomers were further refined by the CCSD(T) single-point calculations (Table S2). The CCSD(T) results support the structure shown in Figure 4a to be the most stable one, and the isomer shown in Figure 4b is 0.28 eV less stable. Other higher-energy isomers ($\Delta E > 0.50$ eV) are displayed in the Supporting Information (Figure S4).

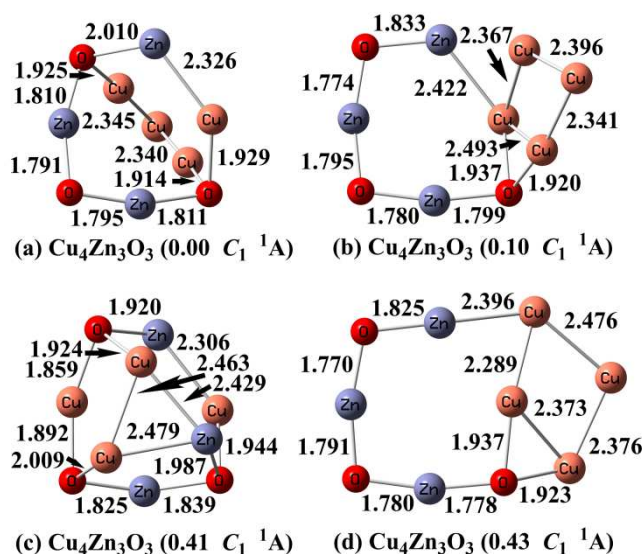


Figure 4. Optimized structures ($\Delta E < 0.50$ eV) for $\text{Cu}_n\text{Zn}_3\text{O}_3$. The bond lengths are in angstroms and the relative energies (ΔE) in eV are in the parentheses.

4. Discussion

4.1. Structural Evolution in $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) Clusters and Their Stability

It has been reported that the supported Cu_2 and Cu_3 clusters are the multi-atom cluster catalysts in specific reactions, and appropriate supports could improve their stability and dispersibility.[38,39] Zinc oxides as one of the most common promoter and support for Cu-based catalysts, the Zn_3O_3 six-membered ring is common in the larger $(\text{ZnO})_n$ ($n > 8$) clusters and the wurtzite ZnO . [14,16,17] Studying the structural evolution of the $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) clusters via sequential doping of Zn_3O_3 cluster with Cu atoms may help us gain insight into the aggregation behavior of small Cu clusters on ZnO surface.

For CuZn_3O_3 , the Cu atom is inserted into the Zn-O bond of Zn_3O_3 cluster. For $\text{Cu}_2\text{Zn}_3\text{O}_3$, the Cu atom is inserted into the Zn-Cu bond of CuZn_3O_3 cluster. As for $\text{Cu}_3\text{Zn}_3\text{O}_3$ and $\text{Cu}_4\text{Zn}_3\text{O}_3$ clusters, the planar seven-membered ring of CuZn_3O_3 cluster starts to play an important role in the subsequent aggregation of Cu atoms (Figure 5), that is, the Cu dimer (Cu_2) and Cu trimer (Cu_3) are attached to the CuZn_3O_3 cluster by two bridged oxygen atom ($\mu_3\text{-O}$). Herein, we found that at the low Cu content ($n = 1,2$), Cu atoms prefer to insert into the Zn-O bond of Zn_3O_3 first, then aggregate to form the ZnCu_2 units. The six-membered ring of Zn_3O_3 gradually expanded to the eight-membered ring of $\text{Cu}_2\text{Zn}_3\text{O}_3$. When the Cu content further increases ($n = 3,4$), the extra Cu atoms aggregate with each other to form Cu_{n-1} units which is supported on CuZn_3O_3 cluster.

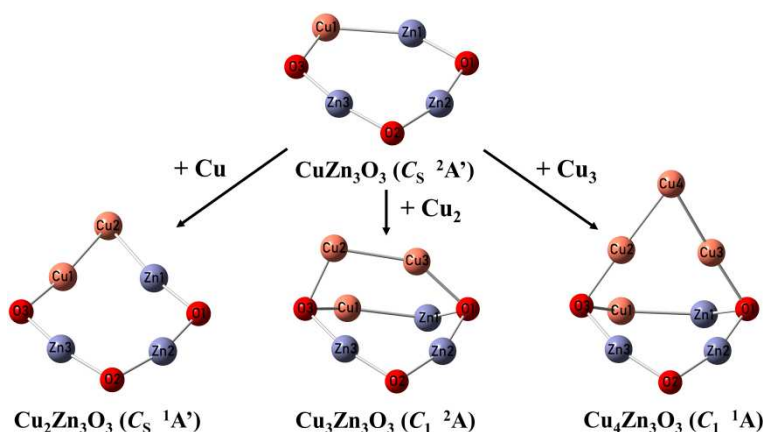


Figure 5. Structural evolution of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) clusters.

The relative stability of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) clusters is evaluated by the calculated atomization energy ($E_{b,1}$). The atomization energy ($E_{b,1}$) of $\text{Cu}_n\text{Zn}_3\text{O}_3$ clusters were calculated by the following formula:

$$E_{b,1} = nE(\text{Cu}) + 3E(\text{Zn}) + 3E(\text{O}) - E(\text{Cu}_n\text{Zn}_3\text{O}_3) \tag{2}$$

$E(\text{Cu}_n\text{Zn}_3\text{O}_3)$, $E(\text{Cu})$, $E(\text{Zn})$ and $E(\text{O})$ represents the energy of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ground state, Cu, Zn and O atom, respectively. As seen in Table 1, the $E_{b,1}$ increases gradually with the increase of Cu content. It suggests the $\text{Cu}_n\text{Zn}_3\text{O}_3$ clusters become more stable as the Cu atoms doping ($n = 0-4$).

Table 1. Atomization energy ($E_{b,1}$) of $\text{Cu}_n\text{Zn}_3\text{O}_3$ cluster. The energies are in eV.

Cluster	Zn_3O_3	CuZn_3O_3	$\text{Cu}_2\text{Zn}_3\text{O}_3$	$\text{Cu}_3\text{Zn}_3\text{O}_3$	$\text{Cu}_4\text{Zn}_3\text{O}_3$
$E_{b,1}$	22.07	24.03	26.68	28.28	31.27

4.2. Chemical Bonding of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) Clusters

It is known that zinc has the electronic configuration of $3d^{10}4s^2$. Usually, its 3d electrons do not participate in bonding with other elements. So in zinc oxides, it almost shows the exclusively +2 oxidation state. But copper as the neighbor element of zinc, it has the $3d^{10}4s^1$ configuration, its 3d electrons participate in the bonding. So the oxidation state of Cu is more abundant (+1, +2 and +3).[40] To better understand the charge transfer in the sequential doping of Zn_3O_3 cluster with Cu atoms, we calculated the Bader charges of the $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) clusters (Table 2). For Zn_3O_3 cluster, the Bader charge of Zn and O atom is +1.13 |e| and -1.13 |e|, respectively. Obviously, the oxidation state of Zn and O in Zn_3O_3 cluster is +2 and -2, respectively. Thus, the Bader charge of about ± 0.5 |e| is indicative of a single-electron transfer, and the Bader charge of about ± 1.0 |e| corresponds to two-electrons transfer.[41]

After inserting a Cu atom into the Zn-O bond of Zn_3O_3 cluster, the Bader charge of the Zn atom (denoted as Zn-1 in Figure 5) next to the newly added Cu atom (denoted as Cu-1) drops to +0.64 |e|, the charge of the Cu-1 atom is +0.43 |e|. In other words, the ZnCu unit in CuZn_3O_3 transfers 1.07 |e| to the nearby oxygen atoms (denoted as O-1 and O-3) in total. It is inferred that Zn-1 and Cu-1 atoms each transfer an electron to the adjacent oxygen atoms (O-1 and O-3). It leads to the metal-oxygen single bond. Meanwhile, the remaining 4s electron of Zn-1 forms the metal bond with Cu-1 atom. Continuing adding a Cu atom to the CuZn_3O_3 cluster, the added Cu atom (denoted as Cu-2) inserts into the Zn-Cu bond of CuZn_3O_3 cluster. As given in Table 2, the Bader charge of Cu-2 is approximately zero (+0.02 |e|). It could be understood by the formation of metal bonds between the Cu-2 atom and the Zn-1 and Cu-1 atoms. Herein, ZnCu₂ unit in $\text{Cu}_2\text{Zn}_3\text{O}_3$ cluster transfers 1.14 |e| to the adjacent oxygen atoms (O-1 and O-3) in total. Compared with Zn_3O_3 cluster, the charges on the other atoms do not change much.

For $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 3,4$) clusters, they can be viewed as adding the Cu₂ (Cu-2 and Cu-3) and Cu₃ (Cu-2, Cu-3 and Cu-4) to the CuZn_3O_3 cluster linked by two 3-fold coordinated oxygen atoms (O-1 and O-3). Compared with the ZnCu diatom of CuZn_3O_3 cluster, the Bader charge of Zn-1 reduces from +0.64 |e| to +0.37 |e|, and the charge of Cu-1 also decreases from +0.43 |e| to roughly +0.3 |e|. It suggested less charge transfers from the ZnCu diatom of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 3,4$) to the O-1 and O-3 atoms. As compensation, the newly added Cu₂ and Cu₃ units in $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 3,4$) transfer charges of +0.51 |e| and +0.56 |e| to the O-1 and O-3 atoms. To analyze the interaction of Cu aggregation (Cu_{n-1}) with CuZn_3O_3 cluster, the binding energies ($E_{b,2}$) of the isolated Cu_{n-1} clusters with CuZn_3O_3 cluster were calculated by the following formula:

$$E_{b,2} = E(\text{Cu}_n\text{Zn}_3\text{O}_3) - E(\text{CuZn}_3\text{O}_3) - E(\text{Cu}_{n-1}) \tag{1}$$

$E(\text{Cu}_n\text{Zn}_3\text{O}_3)$, $E(\text{CuZn}_3\text{O}_3)$ and $E(\text{Cu}_{n-1})$ represents the ground-state energy of $\text{Cu}_n\text{Zn}_3\text{O}_3$, CuZn_3O_3 and Cu_{n-1} clusters, respectively. The $E_{b,2}$ of Cu_2 in $\text{Cu}_3\text{Zn}_3\text{O}_3$ cluster is calculated to be -1.60 eV, and that of Cu_3 in $\text{Cu}_4\text{Zn}_3\text{O}_3$ cluster is -3.21 eV. The more negative $E_{b,2}$ means the stronger interaction between Cu aggregation (Cu_{n-1}) and CuZn_3O_3 cluster, and higher stability of Cu_{n-1} on the CuZn_3O_3 seven-membered ring. Here, the more negative binding energies ($E_{b,2}$) coincides with the more transferred charge from Cu_{n-1} to CuZn_3O_3 . For Cu/ZnO catalysts, the addition of ZnO is conducive to increasing the dispersion and reducibility of the active copper component.[42] From the perspective of Bader charge, the Cu_{n-1} in $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 3,4$) is more reducible than the Cu_n in $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1,2$). The synergistic interaction between Cu and Zn in CuZn_3O_3 may enhance the reducibility of Cu species in $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 3,4$).

Table 2. Bader charges (|e|) analysis of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 0-4$).

Cluster	Zn-1	Zn-2	Zn-3	O-1	O-2	O-3	Cu-1	Cu-2	Cu-3	Cu-4
Zn_3O_3	1.13	1.13	1.13	-1.13	-1.13	-1.13				
CuZn_3O_3	0.64	1.12	1.15	-1.15	-1.14	-1.06	0.43			
$\text{Cu}_2\text{Zn}_3\text{O}_3$	0.75	1.14	1.12	-1.15	-1.15	-1.10	0.37	0.02		
$\text{Cu}_3\text{Zn}_3\text{O}_3$	0.37	1.11	1.12	-1.16	-1.14	-1.09	0.28	0.25	0.26	
$\text{Cu}_4\text{Zn}_3\text{O}_3$	0.37	1.12	1.11	-1.17	-1.14	-1.11	0.26	0.31	0.31	-0.06

4.3. Reactivity of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) Clusters

The model of d-band center was developed by Nørskov and co-workers[43] and was used as an important descriptor to determine the reactivity of surfaces and clusters.[44-48] The partial density of states (PDOS) for the d-orbitals of metal atoms in $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 0-4$) clusters are depicted in Figure 6, and the d-band centers (ϵ_d) are denoted by the red solid line. For the open-shell systems, the spin up (α) and spin down (β) d-band centers (ϵ_d) were calculated separately (Table S3), and the spin down ones were always higher in energy. So we uniformly use the spin down d-band centers (ϵ_d) for the subsequent comparison. The energy level of highest occupied molecular orbital (HOMO- β) are marked by the blue dashed line. For comparison, all HOMO energy levels in Figure 6 are shifted to zero. As shown in Figure 6f, the ϵ_d move toward HOMO- β as the Cu content (n) increases. It suggests the interaction between nucleophilic molecules and the metal atoms become stronger as the Cu content (n) increases.[44,47] It also infers the reactivity of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 0-4$) clusters increase as the Cu content (n) increases.

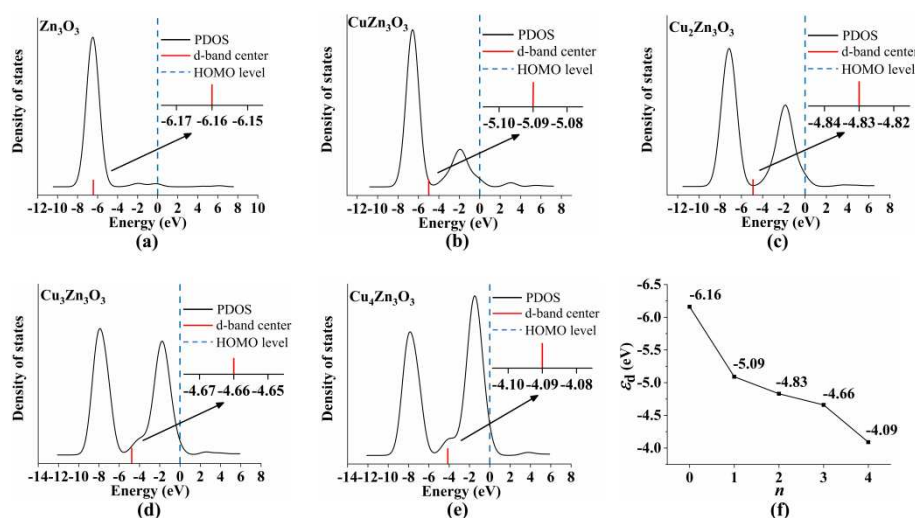


Figure 6. (a)-(e) The d-band density of states for the lowest-energy $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 0-4$) clusters. The inset is the enlarged drawing of the d-band center. (f) The d-band center (ϵ_d) as a function of Cu content (n) in $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 0-4$) clusters.

The electrostatic potential (ESP) provides a way of identifying the active sites.[44,49] The surface ESP for $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) clusters are shown in Figure 7. Obviously, the red-colored (positive ESP) regions are positioned at the metal atoms, and the ESP of $\text{Cu}_n\text{Zn}_3\text{O}_3$ clusters are less localized compared with the Zn_3O_3 clusters. Additionally, the cyan and yellow tiny spheres in Figure 7 point out the locations of the extreme points of the surface ESP, and the arrows indicate the extreme points with the maximum absolute values. The sites with the most positive values of molecular ESP are associated with the ideal adsorption positions for nucleophilic reagents, whereas the most negative ESP are related to that of electrophilic reagents. In this series of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) clusters, the most positive regions of ESP are always nearby the Zn-2 atom except for $\text{Cu}_2\text{Zn}_3\text{O}_3$. Except for $\text{Cu}_2\text{Zn}_3\text{O}_3$, the other $\text{Cu}_n\text{Zn}_3\text{O}_3$ clusters can be viewed as adding the Cu₂ and Cu₃ units to the CuZn_3O_3 cluster linked by two 3-fold coordinated oxygen atoms (O-1 and O-3). For $\text{Cu}_2\text{Zn}_3\text{O}_3$, the newly added Cu atom (Cu-2) expands the seven-membered ring of CuZn_3O_3 to the eight-membered ring. The most positive region of ESP of $\text{Cu}_2\text{Zn}_3\text{O}_3$ is nearby the newly added Cu-2 atom. In $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) clusters, the ESP of 3-fold coordinated oxygen atoms are more negative than that of 2-fold coordinated oxygen atoms. For CuZn_3O_3 and $\text{Cu}_2\text{Zn}_3\text{O}_3$, the most negative regions are located near the O-1 or O-3 atom. For $\text{Cu}_3\text{Zn}_3\text{O}_3$ and $\text{Cu}_4\text{Zn}_3\text{O}_3$, the most negative regions are located near the O-2 atoms. They infer the sensitivity of reactivity to the structures.

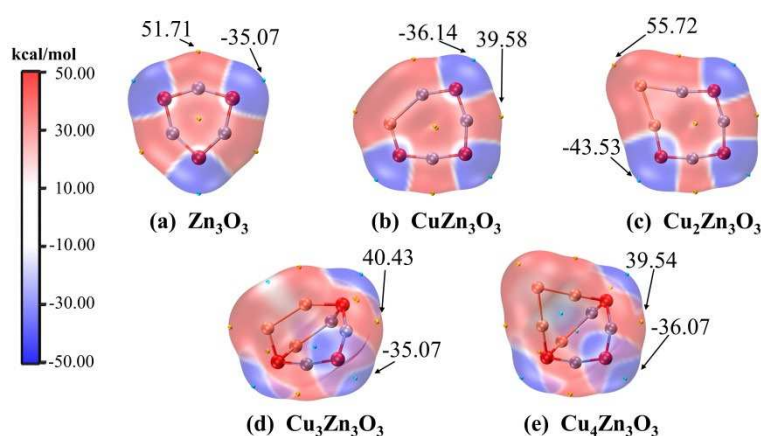


Figure 7. The electrostatic potential (ESP) map on the van der Waals surface for the lowest-energy $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 0-4$) clusters.

5. Conclusions

We report a systematic theoretical study of a series of copper-doped zinc oxide clusters: $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$). The geometric, electronic structures and chemical bonding of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) clusters are investigated by extensive density functional theory (DFT) and coupled cluster theory (CCSD(T)) calculations. The structural evolutions of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) clusters are found in our work. At the low Cu content ($n = 1,2$), Cu atoms prefer to insert into the Zn-O bond of Zn_3O_3 first, then aggregate to form the ZnCu_2 units. The six-membered ring of Zn_3O_3 gradually expands to the eight-membered ring of $\text{Cu}_2\text{Zn}_3\text{O}_3$. When the Cu content further increases ($n = 3,4$), the extra Cu atoms aggregate with each other to form Cu_{n-1} units on the CuZn_3O_3 cluster. Additionally, relative stability of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) clusters is evaluated. The $\text{Cu}_n\text{Zn}_3\text{O}_3$ clusters become more stable as the Cu atoms doping ($n = 1-4$). Bader charge analysis suggests that as the Cu content (n) increases, the reducibility of Cu aggregation (Cu_{n-1}) on the CuZn_3O_3 cluster increase. The studies on d-band centers of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 0-4$) clusters infer the reactivity also increase as the Cu content (n) increases. The information on the possible reaction site of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) clusters are predicted by the surface electrostatic potential (ESP) calculations.

Supplementary Materials: he following supporting information can be downloaded at the website of this paper posted on Preprints.org. Table S1: Calculated results at the B3LYP/BS level for the bond lengths, binding energies and other properties of ZnO and CuO along with the corresponding available experimental data. Table S2: Relative energies of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) clusters which were further refined by the CCSD(T) single-point

calculations. Table S3: The calculated d-band centers for the spin up (α), spin down (β) and both spin modes of $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 0-4$) clusters. Figures S1-S4: Alternative optimized structures for $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 1-4$) clusters at the B3LYP/BS level. Table S4: Cartesian coordinates for the optimized $\text{Cu}_n\text{Zn}_3\text{O}_3$ ($n = 0-4$) clusters.

Author Contributions: Investigation, Z.W.T.; visualization, H.Y.Z. and H.H.L.; writing—original draft preparation, Z.W.T. and H.Y.Z.; writing—review and editing, B.W. and W.J.C. All authors have read and agreed to the published version of the manuscript.

Funding: This work was supported by the National Natural Science Foundation of China (21301030 and 21603117).

Data Availability Statement: The data presented in this study are available from the corresponding authors upon reasonable request.

Acknowledgments: The authors gratefully acknowledge supports from the National Natural Science Foundation of China (21301030 and 21603117).

Conflicts of Interest: The authors declare no conflict of interest.

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