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Article

Distributed Sequential Detection for Cooperative Spectrum Sensing in Cognitive Internet of Things

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Abstract: Considering the spectrum shortage problem of IoT devices, we introduce a collaborative spectrum sensing (CSS) framework in this paper to identify available spectrum resources, so that IoT devices can access it and meanwhile avoid causing harmful interference to the normal communication of the primary user (PU). However, in the process of the PU's signal detection in IoT devices, the issue about the stopping time and decision cost arises. To this end, we propose a distributed cognitive IoT model, which includes two IoT devices independently using sequential decision rules to detect the PU. On this basis, we define the stopping time and cost function for IoT devices, and formulate an average cost optimization problem in CSS. To solve this problem, we further regard the optimal stopping time problem as a finite horizon problem, and solve the threshold of the optimal decision rule by dynamic programming. At last, numerical simulation results demonstrate the correctness of our proposal in terms of the global false alarm and miss detection probability, and it always achieves minimal average cost under various cost of each observation taken and thresholds.

Keywords: internet of thing; cooperative spectrum sensing; sequential detection rule; stopping time; cost function

1. Introduction

As wireless communication technology rapidly develops, spectrum resources cannot meet the growing number of internet of thing (IoT) devices and their applications. However, the frequency spectrum by primary users (PUs) still lies in insufficient state in the time or space domain. To address this concern, cognitive radio (CR) is regarded as a prospective technology to identify available spectrum resources and allow IoT devices to opportunistically access it [1,2], without causing harmful interference to PUs [3]. But spectrum sensing behaviors of the single IoT device is susceptible to inherent factors of wireless propagations. Consequently, cooperative spectrum sensing (CSS) paradigm is formulated to exploit spatial diversity and then improve the sensing accuracy of the PU signal through the observations of spatially positioning IoT devices. However, IoT architectures differ from traditional network architectures, which imply a high degree of reconfigurability, adaptability, mobility, and heterogeneity, and present some insurmountable challenges to spectrum sensing. Traditional spectrum sensing techniques must be carefully redesigned for use in complex and scalable IoT systems [4].

In the past, there are some researchers to investigate spectrum sensing for IoT systems. An energy-efficient reliable decision transmission in Zhu et al. to was proposed to decrease packet error and packet loss in industrial IoT [5]. At a low signal-to-noise ratio (SNR) environment, to minimize the energy consumption and sensing time, Ansere et al. proposed a dynamic spectrum sensing

algorithm [6]. Wan et al. proposed an energy-efficient CSS scheme to reduce the negative impact of spatial correlation [7]. Since the previous energy detector is usually limited by the noise-uncertain, Miah et al. also proposed an energy efficient CSS in based CR-enabled IoTs network under the interference constraint [8]. Considering that battery-limited IoT devices are densely interconnected, Dao et al. optimized the sensing efficiency to leverage a lightweight but effective adaptive medium learning method [9]. Long et al. developed a harvesting-sensing-transmission tradeoff problem based cognitive IoT to take the diversity of energy harvesting efficiency, spectrum sensing performance and quality-of-service (QoS) of data transmission into consideration [10]. In order to enhance spectrum utilization in a 5G-based IoT, Abbas et al. proposed a hybrid mode of underlay and interweave enabled scheme [11]. Gharib et al. proposed a heterogeneous multi-band multi-user CSS scheme to realize secondary users' scheduling to sense a subset of channel in heterogeneous distributed CR networks [12]. Ejaz et al. presented multiband CSS and resource allocation framework in a CR-enabled IoT 5G network to minimize the energy consumption under the performance requirement [13]. To maximize the effective throughput, Zhang et al. jointly optimized the sensing time and packet error rate in cognitive IoT [14]. Miah et al. presented a CSS technique in a noise-uncertain environment to comprise the use of the Kullback-Leibler divergence in CR-based IoT [15]. To encourage the spectrum sharing among unlicensed IoT devices, Lu et al. integrated the incentive mechanism into orthogonal frequency division multiplexing (OFDM)-based cognitive IoT network with multiple unlicensed IoT devices in the context of incomplete information [16]. In the CSS of high real-time scene of IoTs, Gao et al. considered an improved CSS scheme to decrease the latency and increase low throughput, where each cognitive node performs truncated sequential probability ratio test (SPRT) over each observation vector [17]. Wu et al. achieved CSS between micro-sensing slots in cognitive unmanned aerial vehicle networks and approximated the error probability and the stopping time [18].

Most of these efforts are focused on CR-enabled IoT, considering issues such as the achievable throughput, energy efficiency, frequency efficiency, or joint optimization with spectrum resource allocation algorithm. These issues are also common in traditional CR networks. However, they did not take into account the cost issues in cognitive IoT, such as the sensing/stopping time cost, the cost of incorrect decisions, especially when considering CSS among multiple IoT devices. Because only by achieving low-cost detection of the PU while ensuring spectrum sensing performance) can efficient spectrum sensing and resource allocation be achieved. Therefore, this article considers the optimal decision rule in cognitive IoT from the perspective of cost. To this end, a distributed cognitive IoT model is first established, including a pair of IoT devices for CSS and sequential detection, on the basis of which the stopping time and decision cost are defined, and the joint optimization problem between them is proposed. The optimal stopping time and threshold are analyzed by dynamic programming to obtain the optimal decision rule.

The remainder of this article is organized as follows. The local spectrum sensing model and sequential detection for CSS in a cognitive IoT are presented in Section 2. The optimal stopping time and decision rule based on distributed sequential detection is proposed and analyzed in Section 3. Comprehensive simulation result analyses and discussions are discussed in Section 4, and Section 5 draws a conclusion about this article.

2. Materials and Methods

2.1. Spectrum Sensing Model

In a cognitive IoT without a centralized fusion center (FC), there is a PU and a pair of IoT devices participating in CSS, as shown in Figure 1. To protect the PU's normal operation from detrimental interference, each of IoT devices S_1 and S_2 individually exploits spectrum sensing technology to sense the PU at the sensing slot, and then derives a final local decision about the PU's presence through a predetermined combination rule through observations of the PU activity information at each multiple micro-sensing slot. According to the global decisions of IoT devices, a distributed CSS algorithm is adopted to derive a global decision after the sensing slot to decide whether to allow IoT

devices to access the channel. At last, a pair of IoT devices are allowed to utilize the free spectrum band via a predetermined spectrum resources algorithm during the transmitting slot if the PU is declared as absence.

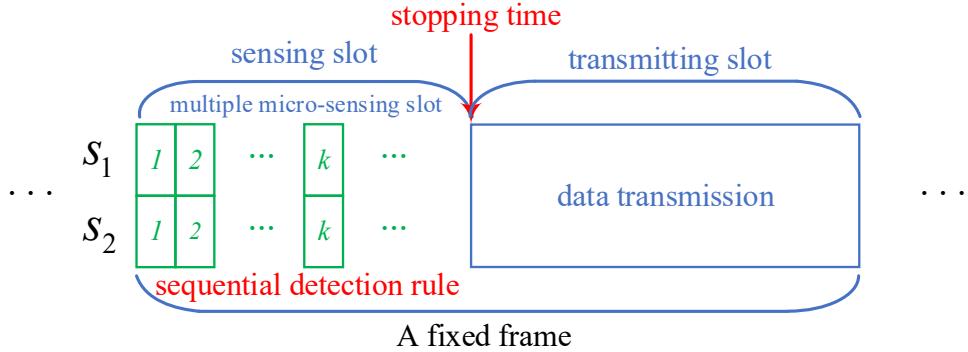


Figure 1. The periodic spectrum sensing frame structure of a cognitive IoT.

The energy detection is usually utilised as a local sensing technology because it is easy to implemented and compatible to the PU network. In an energy detector, suppose that the hypothesis \mathcal{H}_0 and \mathcal{H}_1 represent the PU's absence and presence, respectively, then the attenuated received PU signal at the k -th micro-sensing slot of a IoT device is expressed as [19]

$$y_k(m) = \begin{cases} n_k(m), & \mathcal{H}_0 \\ h_k s_k(m) + n_k(m), & \mathcal{H}_1 \end{cases} \quad (1)$$

where m is the PU signal sampling, $n_k(m)$ is the circularly symmetric complex Gaussian (CSCG) noise, $s_k(m)$ is the complex-valued phase shift keying (PSK) signal at the PU, $n_k(m)$ and $s_k(m)$ are independent each other, h_k is the channel gain. Then, the test static E_k of energy detector is expressed by

$$E_k = \frac{1}{M} \sum_{m=1}^M |y_k(m)|^2, \quad (2)$$

where M is the sampling number of the received PU signal.

Following (2), we evaluate the local performance via a pre-determined detection threshold λ_k . Under the hypothesis \mathcal{H}_0 , the probability density function (PDF) $p_0(l)$ of the test static E_k follows Chi-square distribution, the local false alarm probability is obtained by

$$P_{f,k} = P(r_k = 1 | \mathcal{H}_0) = P(E_k > \lambda_k | \mathcal{H}_0) = \int_{\lambda_k}^{\infty} p_0(l) dl, \quad (3)$$

where r_k is the sensing sample.

Suppose M is large enough, PDF of E_k is approximated as a Gaussian distribution where the mean $\mu_0 = \sigma_n^2$, the variance $\sigma_0^2 = [\mathbf{E}|n_k(m)|^4 - \sigma_n^4]/M$. Because $n_k(m)$ is CSCG, $\mathbf{E}|n_k(m)|^4 = 2\sigma_n^4$, thus $\sigma_0^2 = \sigma_n^4/M$. The sampling frequency is f_s , the duration time for the k -th micro-sensing slot is τ_k , for simplicity of denotation, $M = \tau_k f_s$. Therefore, the local false alarm probability is given by

$$P_{f,k} = Q\left(\left(\frac{\lambda_k}{\sigma_n^2} - 1\right) \sqrt{\tau_k f_s}\right), \quad (4)$$

where

$$Q(l) = \frac{1}{\sqrt{2\pi}} \int_{\lambda_k}^{\infty} \exp\left(-\frac{t^2}{2}\right) dt. \quad (5)$$

Under the hypothesis \mathcal{H}_1 , PDF of E_k is denoted by $p_1(l)$, the local detection probability can be expressed by

$$P_{d,k} = P(r_k = 1 | \mathcal{H}_1) = P(E_k > \lambda_k | \mathcal{H}_1) = \int_{\lambda_k}^{\infty} p_1(l) dl. \quad (6)$$

Since PDF of E_k is also regarded as a Gaussian distribution where the mean $\mu_1 = (1 + \lambda_k)\sigma_n^2$, the variance $\sigma_1^2 = [E|h_k s_k(m)|^4 + E|n_k(m)|^4 - (h_k^2 s_k^2(m) - \sigma_n^2)^2]/M = [(1 + \gamma_k)\sigma_n^4]/M$, where γ_k is the received SNR at the k -th micro-sensing slot, the local detection probability can be given by

$$P_{d,k} = Q\left(\left(\frac{\lambda_k}{\sigma_n^2} - \gamma_k - 1\right)\sqrt{\frac{\tau_k f_s}{1+2\gamma_k}}\right). \quad (7)$$

2.2. Sequential Detection

Building on the above spectrum sensing model in a cognitive IoT, we further present a sequential detection framework for CSS and make the following assumptions and descriptions. The IoT device S_i receives a sequence of observations $\{Z_k^i\}$, and $\{Z_k^i\}$ is i.i.d. and are independent of one another at a hypothesis, $i = 1, 2$. Under hypothesis \mathcal{H}_j , the observations from the i -th IoT device follows a marginal probability density function $q_j^{(i)}$. In addition, the probability of hypotheses \mathcal{H}_0 and \mathcal{H}_1 are $1 - \rho$ and ρ , respectively, a probability space is assumed to be $(\Omega, \mathcal{F}) = (\mathbb{R}^\infty \times \mathbb{R}^\infty, \mathcal{B}^\infty \times \mathcal{B}^\infty)$ equipped with the probability measure $P = \rho P_1 + (1 - \rho)P_0$, where $P_1 = P_1^{(1)}P_1^{(2)}$ and $P_0 = P_0^{(1)}P_0^{(2)}$, $P_j^{(1)}$ and $P_j^{(2)}$ denote the restrictions of P_j to the corresponding filtrations $\{\mathcal{F}_k^{(i)}\}$ with $\mathcal{F}_k^{(i)} = \sigma\{Z_1^{(i)}, \dots, Z_k^{(i)}\}$. Each IoT devices S_i devises a sequential decision rule [20], $T^{(i)}$ is the time of stopping sampling, and $\theta^{(i)}$ takes the value 0 or 1 to declare whether one of two hypotheses is accepted.

3. Distributed Sequential Detection

According to the above model, we delve into the distributed sequential detection for a cognitive IoT in this section, including the optimal stopping time and the optimal sequential detection.

3.1. Problem Formulation

To study the cost problem of a distributed sequential detection, we define a cost function $\Delta(\theta^{(1)}, \theta^{(2)}; \mathcal{H})$ indicates the cost of error decision in any one or both of the decisions made by a pair of IoT devices. To be specific, $\Delta(0, \theta^{(2)}; \mathcal{H}_1) \geq \Delta(1, \theta^{(2)}; \mathcal{H}_1)$, $\Delta(1, \theta^{(2)}; \mathcal{H}_0) \geq \Delta(1, \theta^{(2)}; \mathcal{H}_1)$, $\Delta(1, \theta^{(2)}; \mathcal{H}_0) \geq \Delta(0, \theta^{(2)}; \mathcal{H}_0)$, and $\Delta(0, \theta^{(2)}; \mathcal{H}_1) \geq \Delta(0, \theta^{(2)}; \mathcal{H}_0)$. Similarly, the inequalities apply to $\theta^{(1)}$. From these inequalities, each additional sample of an IoT device also incurs a cost of c . Combining the time of stopping sampling and the cost function, there is a following decision problem, such as,

$$\inf_{\{(T^{(i)}, \theta^{(i)})\}} E\{cT^{(1)} + cT^{(2)} + \Delta(\theta^{(1)}, \theta^{(2)}; \mathcal{H})\}. \quad (8)$$

3.2. Preliminary Analysis

Since a positive cost c correlates with each additional time step taken by IoT devices in (8), the person-by-person optimization (PBPO) approach is applied to distributed sequential detection to address the problem of (8) [21]. Fixing $(T^{(2)}, \theta^{(2)})$, a stochastic optimization problem is described as

$$J(\rho) = \inf_{\{(T^{(1)}, \delta^{(1)})\}} E\{cT^{(1)} + cT^{(2)} + \Delta(\theta^{(1)}, \theta^{(2)}; \mathcal{H})\}. \quad (9)$$

In (9), there is a special case, i.e., $\Delta(\theta^{(1)}, \theta^{(2)}; \mathcal{H}) = \Delta(\theta^{(1)}, \mathcal{H}) + \Delta(\theta^{(2)}, \mathcal{H})$, which is a classical sequential detection problem. Additionally, the cost function may be coupled between the two IoT devices.

Before solving (9), a sufficient statistic is preset as

$$\rho_k^{(1)} = P(\mathcal{H} = \mathcal{H}_1 | \mathcal{F}_k^{(2)}), \quad (10)$$

and the recursion result from Bayes' formula can be expressed as

$$\rho_{k+1}^{(1)} = \frac{\rho_k^{(1)} q_1^{(1)}(x)}{\rho_k^{(1)} q_1^{(1)}(x) + (1 - \rho_k^{(1)}) q_0^{(1)}(x)} P(\mathcal{H} = \mathcal{H}_1 | \mathcal{F}_k^{(2)}), \quad (11)$$

with $\rho_0^{(1)} = \rho$. Obviously, $\{\rho_k^{(1)}\}$ forms a Markov process about the filtration $\{\mathcal{F}_k^{(1)}\}$.

Considering the finite horizon problem, IoT device S_1 discontinues sampling and derives a decision not later than time τ . Let J_k^τ denote the minimal expected cost at the k -th micro-sensing slot, a dynamic programming equation

(1) When $\{T^{(1)} = \tau\}$, we have

$$J_{T^{(1)}}^\tau(\rho_{T^{(1)}}^{(1)}) = \inf \left\{ \mathbf{E} \left\{ \Delta(0, \theta^{(2)}; \mathcal{H}) \middle| \mathcal{F}_{T^{(1)}}^{(1)} \right\}, \mathbf{E} \left\{ \Delta(1, \theta^{(2)}; \mathcal{H}) \middle| \mathcal{F}_{T^{(1)}}^{(1)} \right\} \right\}. \quad (12)$$

(2) When $\{T^{(1)} = k\}$, $k = 1, \dots, \tau - 1$, we have

$$J_{T^{(1)}}^\tau(\rho_{T^{(1)}}^{(1)}) = \inf \left\{ \mathbf{E} \left\{ \Delta(0, \theta^{(2)}; \mathcal{H}) \middle| \mathcal{F}_{T^{(1)}}^{(1)} \right\}, \mathbf{E} \left\{ \Delta(1, \theta^{(2)}; \mathcal{H}) \middle| \mathcal{F}_{T^{(1)}}^{(1)} \right\}, c + \Delta_k^\tau(\rho_k^{(1)}) \right\}, \quad (13)$$

where $\Delta_k^\tau(\rho_k^{(1)}) = \mathbf{E} \{ J_{k+1}^\tau(\rho_{k+1}^{(1)}) | \mathcal{F}_k^{(1)} \}$.

Since J_0^τ is the minimal expected cost of the finite horizon problem, (12) and (13) provide the dependence of the minimal expected cost on the sufficient statistic $\rho_k^{(1)}$. It can be clearly seen from the right-hand side of unfolding (12), according to $\mathbf{E} \left\{ \Delta(0, \theta^{(2)}; \mathcal{H}) \middle| \mathcal{F}_{T^{(1)}}^{(1)} \right\} = \sum_{d=0}^1 \sum_{j=0}^1 P_j(\theta^{(2)} = d) \Delta(0, d; \mathcal{H}_j) \times P(\mathcal{H} = \mathcal{H}_j | \mathcal{F}_{T^{(1)}}^{(1)})$, $\mathbf{E} \left\{ \Delta(1, \theta^{(2)}; \mathcal{H}) \middle| \mathcal{F}_{T^{(1)}}^{(1)} \right\} = \sum_{d=0}^1 \sum_{j=0}^1 P_j(\theta^{(2)} = d) \Delta(1, d; \mathcal{H}_j) \times P(\mathcal{H} = \mathcal{H}_j | \mathcal{F}_{T^{(1)}}^{(1)})$, and using (8). The same holds true for (13), then we have $\mathbf{E} \{ J_{k+1}^\tau(\rho_{k+1}^{(1)}) | \mathcal{F}_k^{(1)} \} = \int J_{k+1}^\tau(\rho_{k+1}^{(1)}) [\rho_k^{(1)} q_1^{(1)}(x) + (1 - \rho_k^{(1)}) q_0^{(1)}(x)] dx$.

In addition, we define a function with respect to $\rho_k^{(1)}$ as $f(\rho_k^{(1)}) = \min \left\{ \mathbf{E} \left\{ \Delta(0, \theta^{(2)}; \mathcal{H}) \middle| \mathcal{F}_{T^{(1)}}^{(1)} \right\}, \mathbf{E} \left\{ \Delta(1, \theta^{(2)}; \mathcal{H}) \middle| \mathcal{F}_{T^{(1)}}^{(1)} \right\} \right\}$, for all $k = 0, \dots, \tau$, there are inequalities about $f(0)$ and $f(1)$ which follow their respective definitions, i.e.,

$$f(0) < c + \Delta_k^\tau(0), \quad (14)$$

and

$$f(1) < c + \Delta_k^\tau(0). \quad (15)$$

Moreover, the monotonicity results of $J_k^\tau(\rho)$ can be given by

$$J_k^\tau(\rho) \leq J_{k+1}^\tau(\rho), 0 \leq \rho \leq 1, \quad (16)$$

and

$$J_k^\tau(\rho) \leq \Delta_{k+1}^\tau(\rho), 0 \leq \rho \leq 1, \quad (17)$$

since each of the left-hand quantities is a hypo-mundum, on a larger set of stopping times than the corresponding right-hand quantity.

3.3. Optimal Stopping Time

To solve problem (9), we consider the limit $\tau \rightarrow \infty$, the pointwise limit of J_k^τ exists and is independent of k . More specifically, we have

$$J(\rho) = \lim_{\tau \rightarrow \infty} J_k^\tau(\rho) = \lim_{\tau \rightarrow \infty} J_k^\tau(\rho), 0 \leq \rho \leq 1. \quad (18)$$

Theorem 1. The minimal expected cost on $J(\rho)$ satisfies the Bellman equation

$$J(\rho) = \min \left\{ \mathbf{E} \{ \Delta(0, \theta^{(2)}; \mathcal{H}) \}, \mathbf{E} \{ \Delta(1, \theta^{(2)}; \mathcal{H}) \}, c + \Delta_J(\rho) \right\}, 0 \leq \rho \leq 1, \quad (19)$$

where $\Delta_J(\rho) = \mathbf{E} \{ J(\rho_1) \}, 0 \leq \rho \leq 1$.

The optimal stopping time is

$$T_{opt} = \inf \{k \mid \rho_k^{(1)} \notin (\xi_L^{(1)}, \xi_U^{(1)})\}, \quad (20)$$

where a pair of thresholds $(\xi_L^{(1)}, \xi_U^{(1)})$ are described as

$$\xi_L^{(1)} = \sup \left\{ 0 \leq \rho \leq \frac{1}{2} \mid c + \Delta_J(\rho) = E\{\Delta(0, \theta^{(2)}; \mathcal{H})\} \right\}, \quad (21)$$

and

$$\xi_U^{(1)} = \inf \left\{ 1/2 \leq \rho \leq 1 \mid c + \Delta_J(\rho) = E\{\Delta(1, \theta^{(2)}; \mathcal{H})\} \right\}, \quad (22)$$

Proof of Theorem 1. Taking the limit of (13) and using (18), (19) follows. The concavity of J derives from the limit of concave functions. Inequalities like (14) and (15) also hold. Utilizing these inequalities, the concavity of Δ_J , and $J(\rho)$, the optimal stopping time is the threshold type, as shown in (20), where the threshold is determined by \square

$$c + \Delta_J(\xi_L^{(1)}) = E\{\Delta(0, \theta^{(2)}; \mathcal{H})\}|_{\{\rho=\rho_L^{(1)}\}}, \quad (23)$$

and

$$c + \Delta_J(\xi_U^{(1)}) = E\{\Delta(1, \theta^{(2)}; \mathcal{H})\}|_{\{\rho=\rho_U^{(1)}\}}. \quad (24)$$

This establishes the proposition.

3.4. Optimal Decision Rule

Similar to an argument used in the proof of Proposition 7.4 [20], the uniqueness of the limit value function for (9) follows. Moreover, since the optimal thresholds $\xi_L^{(1)}$ and $\xi_U^{(1)}$ are coupled from (14) and (15), two simultaneous dynamic programming equations should be solved.

Given a value of $\Delta(T^{(2)}, \theta^{(2)})$, the optimal local decision rule of the IoT device S_1 is derived, vice versa. That is to say, when two IoT devices achieve their respective optimal decisions for each other's optimal decision rule. As a result, the global optimal decision rules can be iteratively implemented by continuously fixing the threshold of one IoT device and optimizing the threshold of the other by Theorem 1.

Finally, there are following process at the optimal decision rule of the IoT devices S_i , $i = 1, 2$, such as, (1) if $\rho_k^{(i)} \leq \xi_L^{(i)}$, the decision rule accepts \mathcal{H}_0 ; (2) if $\rho_k^{(i)} \geq \xi_U^{(i)}$, the decision rule accepts accept \mathcal{H}_1 ; (3) if $\xi_L^{(i)} \leq \rho_k^{(i)} \leq \xi_U^{(i)}$, the decision rule continues sampling, where a pair of thresholds $(\xi_L^{(i)}, \xi_U^{(i)})$ at the per-IoT device are obtained by

$$\xi_L^{(i)} = \frac{\bar{P}_m^{(i)}}{1 - \bar{P}_f^{(i)}}, \quad (25)$$

and

$$\xi_U^{(i)} = \frac{1 - \bar{P}_m^{(i)}}{\bar{P}_f^{(i)}}, \quad (26)$$

where $\bar{P}_m^{(i)}$ and $\bar{P}_f^{(i)}$ are the tolerable miss detection probability and the tolerable false alarm probability, respectively.

A similar method can be utilised for the quickest detection problem. In such a problem, each of the IoT devices S_j sequentially receives observations $\{Z_k^{(j)}\}$, then there exists a change point t following a geometric distribution with a mass at 0, and correspondingly there is a known marginal density $q_0^{(j)}$ for $k = 1, \dots, t-1$ and $q_1^{(j)}$ for $k = t, \dots$. Given the change point, IoT device observations are assumed to be conditionally independent and it is valid within IoT devices and across IoT devices. Now, in order to quickly detect the change point and control the false alarm probability, each IoT device needs to optimally select stopping times $T^{(i)}$ (each measurable with

respect to their own filtrations $\mathcal{F}^{(i)}$) with aim of minimizing $E\{\Delta(T^{(1)}, T^{(2)}; t)\}$, where $\Delta(T^{(1)}, T^{(2)}; t) = \mathbf{1}_{\{T^{(1)} < t\}} \mathbf{1}_{\{T^{(2)} < t\}} + c_1(T^{(1)} - t) \mathbf{1}_{\{T^{(1)} \geq t\}} + c_2(T^{(2)} - t) \mathbf{1}_{\{T^{(2)} \geq t\}}$. Therefore, the optimal solution can be given by

$$T^{(1)} = \inf\{k \mid P(t \leq k \mid \mathcal{F}_k^{(1)}) \geq \xi_1^*\}, \quad (27)$$

and

$$T^{(2)} = \inf\{k \mid P(t \leq k \mid \mathcal{F}_k^{(2)}) \geq \xi_2^*\}, \quad (28)$$

where a pair of optimal thresholds ξ_1^* and ξ_2^* are coupled via a system of two dynamic programming equations. The term $\mathbf{1}_{\{T^{(1)} < t\}} \mathbf{1}_{\{T^{(2)} < t\}}$ appears in the cost function that couples the solution.

4. Simulation results

In this section, simulation results are introduced to corroborate the correctness and effectiveness of our proposal with respect to the global performance and the average cost from a IoT device. To this end, in 10^6 spectrum sensing frames, unless otherwise specified, some parameter settings are considered as follows: the number of micro-sensing slots is 20, the probability ρ of the hypothesis \mathcal{H}_1 is 0.5, the local detection probability and the local false alarm probability are set to be 0.6 and 0.4, respectively. Both of the tolerable false alarm probability and the tolerable false alarm probability varies from 0.01 to 0.3 within an interval of 0.01.

Figure 2 illustrates the relationship of the global false alarm probability Q_f and the tolerable false alarm probability \bar{P}_f under various tolerable miss detection probabilities. First of all, it can be seen that as the tolerable false alarm probability becomes more relaxed, the global false alarm probability shows a stepwise increase, and the larger the tolerable false alarm probability, the larger the gradient of the step. This is because for a fixed probability, an increase in the tolerable false alarm probability leads to a decrease in the upper threshold ξ_U , and the sequential detection rule is easier to accept \mathcal{H}_1 , which in turn results in an increase in the global false alarm probability. Meanwhile, it is worth noting that on the steps before the global false alarm probability jumps, although the tolerable false alarm probability continues to increase, the global false alarm probability remains unchanged. At this point, an increase in the initial stopping time does not bring about a change in the global false alarm probability, that is, an increase in observation does not bring about a change in the global false alarm probability, and the initial stopping time is the optimal stopping time.

Moreover, the impact of the tolerable miss detection probability on the global false alarm probability can be neglectable at the beginning. That is to say, the thresholds (ξ_L, ξ_U) of the sequential detection rule is still not satisfied. But as the tolerable false alarm probability increases, the impact of the tolerable miss detection probability is becoming more and more obvious. To be specific, the larger the tolerable miss detection probability, the faster the global false alarm probability jumps. Apparently, the large the tolerable miss detection probability, the larger the upper threshold ξ_U , resulting in a more acceptable \mathcal{H}_1 .

Under various tolerable miss detection probabilities, the relationship of the global miss detection probability Q_m and the tolerable false alarm probability \bar{P}_f is shown in Figure 3. In contrast to Figure 2, the tolerable false alarm probability has a greater effect on the global miss detection probability than the global false alarm probability and the effect is positive. In details, when the tolerable false alarm probability increases from 0.01 to 0.3, correspondingly, the global miss detection probability basically goes down from 0.95 to 0.22. Since the lower threshold ξ_L increases as the tolerable false alarm probability increases according to (25), the sequential detection rule is prone to accept \mathcal{H}_0 , resulting in a decrease of the global miss detection probability. Furthermore, in such an environment, the global miss detection probability of a large tolerable miss detection probability decreases first because it increases the lower threshold ξ_L , i.e., $\bar{P}_m = 0.2$.

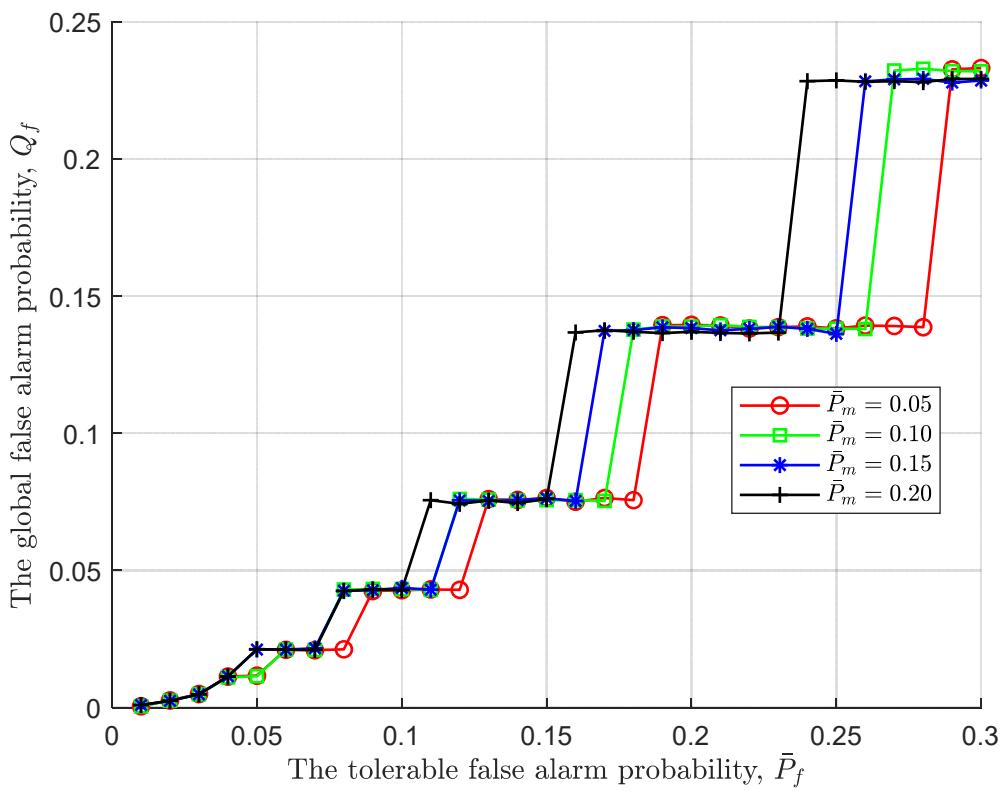


Figure 2. The global false alarm probability vs the tolerable false alarm probability.

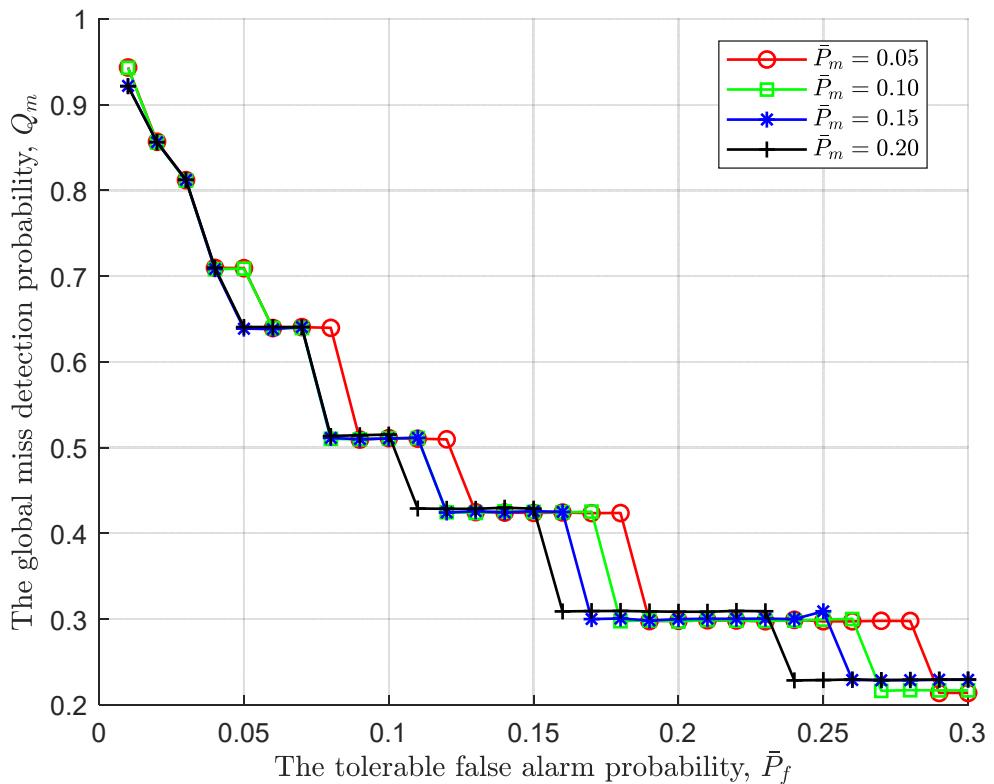


Figure 3. The global miss detection probability vs the tolerable false alarm probability.

In addition, similar to Figure 2, the steps before the global miss detection probability jumps, although the tolerable false alarm probability continues to increase, the global false alarm probability remains unchanged. At this point, an increase in the initial stopping time does not bring about a change in the global miss detection probability, that is, an increase in observation does not bring about a change in the global miss detection probability, and the initial stopping time is the optimal stopping time.

Next, we further take the impact of the tolerable miss detection probability on the global performance given a fixed tolerable false alarm probability into consideration. As displayed in Figure 4, regardless of the tolerable miss detection probability, it is obvious that a large tolerable false alarm probability leads to a low upper threshold ξ_U , therefore being prone to accept \mathcal{H}_1 . However, it also should be noted that as the tolerable miss detection probability increases, the global false alarm probability under different tolerable false alarm has jitter at different positions, such as jitter up at $\bar{P}_f = 0.05, 0.1, 0.2$ and jitter down when $\bar{P}_f = 0.2$. This is not surprise, and is a direct of that a pair of tolerable probabilities simultaneously change, and the decision condition is reached within a certain stopping time.

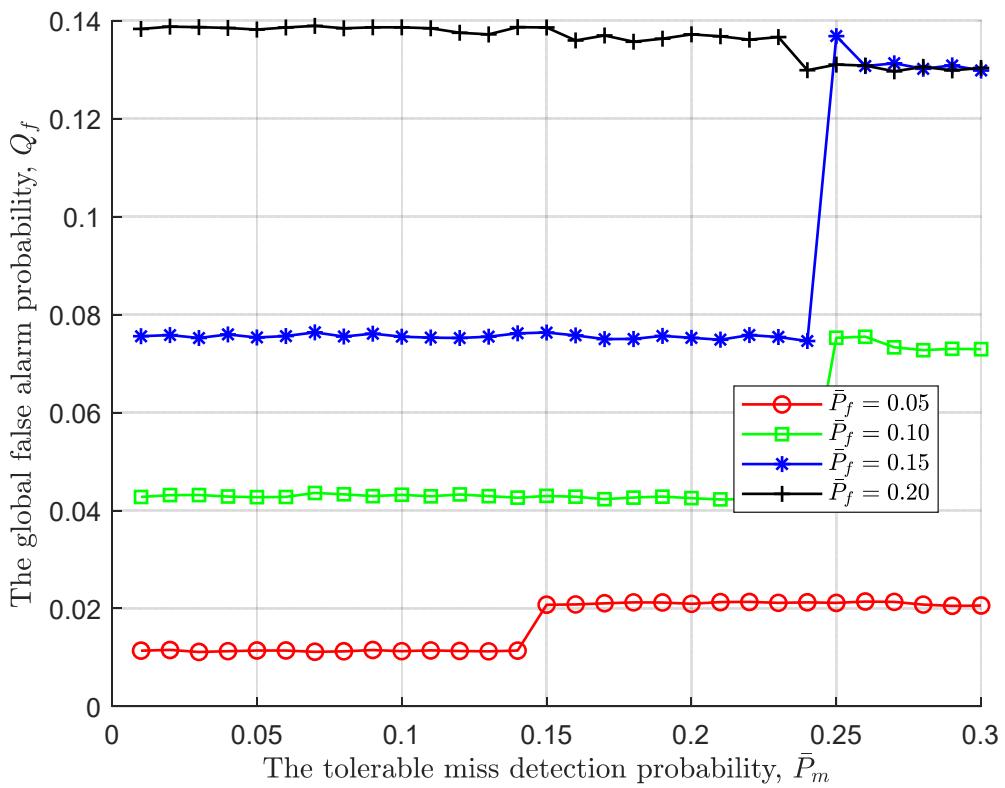


Figure 4. The global false alarm probability vs the tolerable miss detection probability.

Similar to the global miss detection probability of Figure 4, given the tolerable false alarm probability, the positive impact of the tolerable miss detection probability is illustrated in Figure 5. In particular, the trend of the global miss detection probability is exactly the opposite to that of the global false alarm probability and the change interval is larger. There is no doubt that, the tolerable miss detection probability makes the lower threshold ξ_L smaller so that \mathcal{H}_1 is easier to accept.

Following the joint impact of the tolerable performance metrics on the global performance, we further simulate the optimal cost of the tolerable performance under various costs of each observation taken, where the cost of each observation taken c is set to be 0.1 and 1. As shown in Figure 6, for a pair of fixed tolerable performance, the larger cost of each observation taken c , the larger the average cost. Moreover, as the tolerable false alarm probability increases, the average cost decreases. This is to say, an increasing tolerable false alarm probability makes the lower/upper threshold

larger/smaller, resulting in that the global decision is difficult to be made. Consequently, the stopping time increases. However, the increasing tolerable false alarm probability also makes the global miss detection probability decrease, as shown in Figure 3. As a result, the global miss detection probability dominates the average cost because the cost about the miss detection decreases.

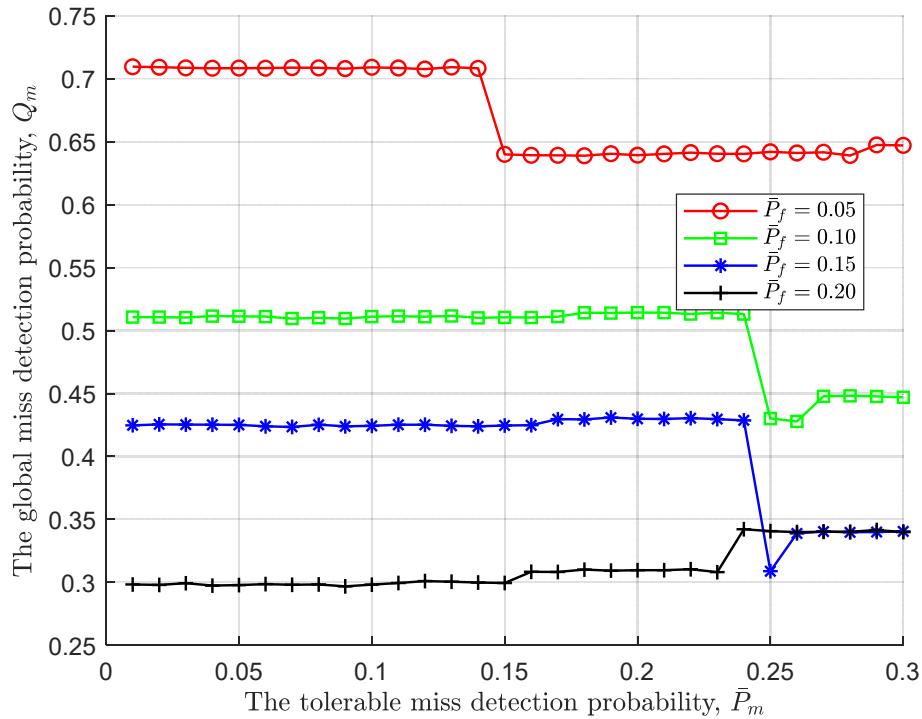


Figure 5. The global miss detection probability vs the tolerable miss detection probability.

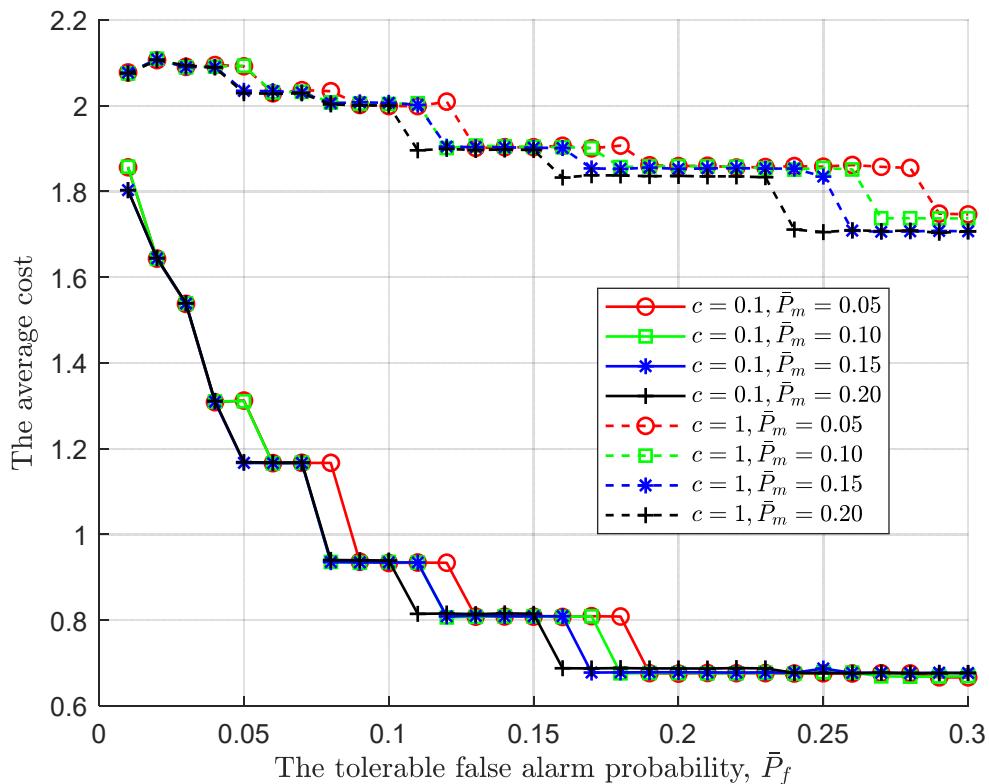


Figure 6. The average cost vs the tolerable false alarm probability under various costs of each observation taken.

As with Figure 6, the larger cost of each observation taken results in a larger average cost in Figure 7. Following the global miss detection probability in Figure 5, the average cost follows it. The simulation result also confirms once again that the global miss detection dominates the average cost. In summary, following PBPO methodology, the optimal sequential detection rule can be reached as the sensing environments to minimize the cost at a IoT device.

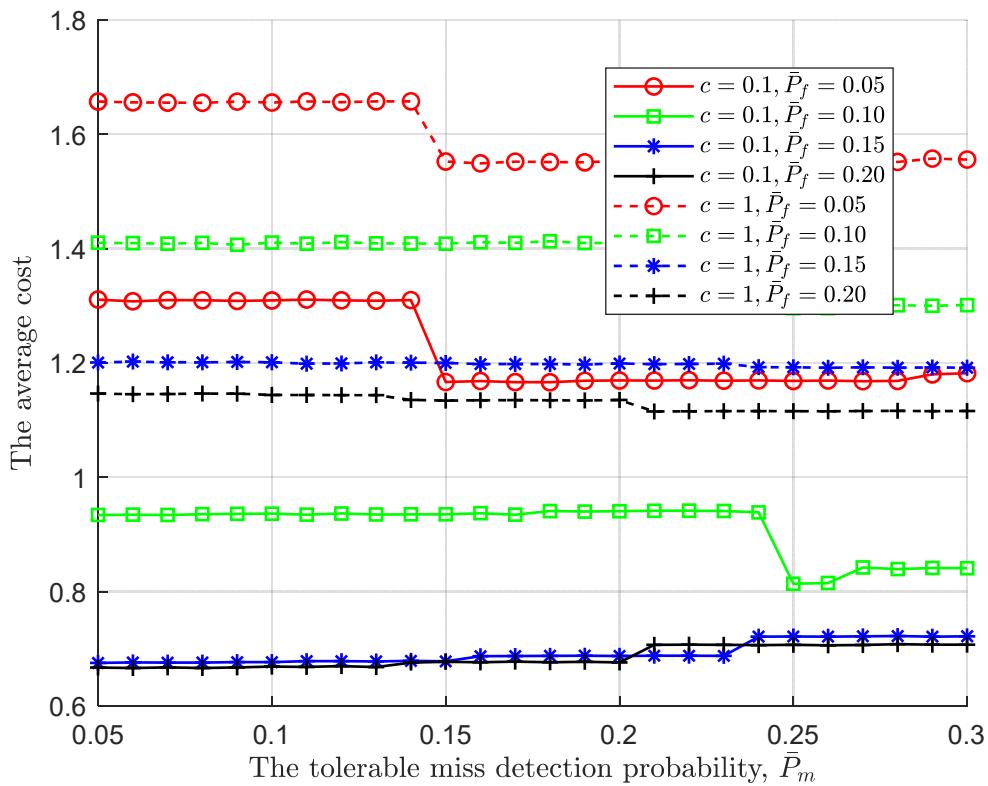


Figure 7. The average cost vs the tolerable miss detection probability under various costs of each observation taken.

5. Conclusions

In this article, we delved into the distributed sequential detection rule for CSS in a cognitive IoT. Consequently, we first establish a spectrum sensing model in the periodic spectrum sensing frame structure and propose a sequential detection framework. On basis of this, we further define the stopping time and cost function for a IoT device and propose an optimization problem about the average cost. Moreover, PBPO methodology is applied to solve such a finite horizon problem, thereby analysing the stopping time for the optimal sequential detection. Finally, a series of numerical simulation results show that correctness and effectiveness of our proposed sequential detection rule in terms of the stopping time and thresholds.

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