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Article

# Oscillation Resynchronization in a Photosensitive Reaction-Diffusion System

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**Abstract:** Oscillation synchronization through diffusion-based communication of active materials can lead to emergence of diverse patterns and collective behaviors. A detailed general description of the formation process of synchronization or resynchronization dynamics is a challenging task. We employ a photosensitive Belousov-Zhabotinsky reaction-diffusion model (within a gel media) to investigate the recovery process of oscillation synchronization between a pair of gel patches. The recovery time for oscillation resynchronization can be modulated by patch-distance, species of signaling molecules, intensity and duration of illumination. Analysis reveals that the “switch effect” of the gel-distance and the “promotion effect” from illumination on the oscillation resynchronization originate from the competition between processes of photo-promotion of oscillation, diffusion of signaling molecules ( $\text{HBrO}_2$  and  $\text{Br}^-$ ) and disproportionation of  $\text{HBrO}_2$ . These results will benefit studies on bio-inspired active materials and soft motors.

**Keywords:** active materials; resynchronization; oscillatory media; photosensitive Belousov-Zhabotinsky reaction; reaction-diffusion system

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## 1. Introduction

Active matter with communicating elements is an integrated system in which its elements can consume energy to perform mechanical work or to moves, including living organisms and active artificial systems. Communicating in some way and achieving synchrony between these elements to generate collective behaviors is a key issue for the active matter [1–4]. In living systems, elements communicate with each other through the diffusion of signal molecules [5], electronic signals [6], and stress signals [7,8] at various levels including sub-cellular, cellular, tissues, individual, and colony levels. This communication allows for the achievement of synchrony or asynchrony states and subsequently leads to the generation of self-replicating, self-healing, self-organizing and self-driving processes [2,4–7]. For examples, embryogenesis [9], the organization of myosin motor and actin filaments in the muscle elements [10], neural networks organized into memory media [11], organ development [12], weak synchronization of collective oscillation in bacterial colony [13], synchronization of rhythmic cilia [14,15], synchronization of metabolic of yeast cells [16], shallow gradients sensing of cell colony [17], synchronization of firefly fluorescence [18] and Mexican waves in stadium [19]. The elements of active matter interact with each other through various type of communication to produce emergent collective behaviors.

The emergent mechanism and systematic control of this process are important scientific issues [20]. The research findings in this field have been utilized for designing artificial systems, including functional active materials and soft robots. For examples, Huygens' synchrony of coupled liquid crystalline oscillators [21], particle robots [22], bio-inspired Central pattern generator [23], Interactive Materials [24], synchronized pattern in active materials [25].

In the previous report, researchers explored how the synchrony state of the system changes with environment and system parameters. They discovered the mechanism that governs the final synchrony state and transitions between different synchrony states based on these parameters. Additionally, they proposed design criteria for various functions based on these laws. However, one challenge that has yet to be elucidated in this scientific field is understanding the general mechanism behind the evolution process of synchronous states, rather than solely studying stable synchronous

states. From a research operability perspective, this problem can be expressed as finding a general mechanism for the system recovering from a damaged synchrony state. E.g., How can the dynamics of resynchronization in the reaction-diffusion system (RDS) of a disarranged living organism [5] be described in general?

The synchronization between different sub-RDS through molecular diffusion-based communication is ubiquitous in nature, also serves as a universal model system for bioinspired synchronization [5–7,23–25]. In this work, a widely studied photosensitive active polymer gel that hosts the tris(bipyridine)ruthenium [Ru(bipy)]-catalyzed Belousov-Zhabotinsky reaction (BZR) is used to study the resynchronization behavior. It is a reaction-diffusion-force coupling system, which can transform chemical energy into mechanical work autonomously [26] and can be controlled by illumination. Balazs and coworkers simulated and analyzed chemical-mechanical co-oscillatory behavior within an anisotropic BZ gel medium via gLSM [27–29], stress-modulated synchronized oscillation [30], geometrical parameter modulated collective oscillation of multiple gels [31], synchronized waves modulated by the asymmetric size of media [32], mechanical-chemical effect on the synchronized oscillation [33] and materials with BZ gel that compute [34]. The BZ gel system is also one of the important research systems for bionic directed motion [35–41] and collective behavior [28,42,43], both of which are closely related to oscillation synchronization.

To simplify, we simulate the oscillation synchronization process between inert BZ gel samples immersed in the BZ reaction solution (a pair of circular gel samples), where illumination induces the destruction of an initially synchronized state. Where the “inert” refers to a nondeformable BZ gel with a highly crosslinked polymer [44]. The catalyst for the BZ reaction exists only inside the gel patch, therefore BZR occurs only inside the gel. The communication between patches can be achieved through the diffusion of the intermediate products of BZR [45]. In this work, we characterize the recovery process of oscillation synchronization by measuring time it takes for two gel blocks to resynchronize (recovery time). We explore the effect of the light intensity, the spacing of the gel patches and other factors on the recovery time. Finally, we propose a mechanism of the resynchronization between the gel patches.

## 2. Results and discussion

### 2.1. Model and schematic of the system

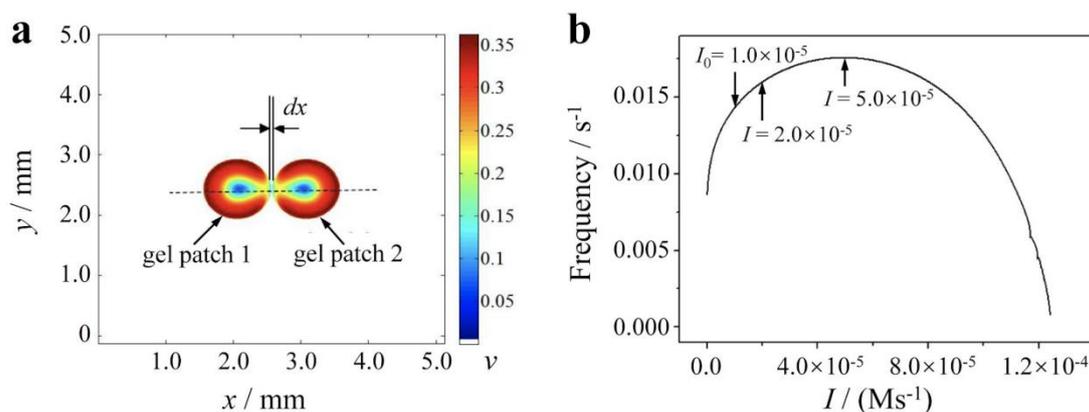
In this work, we employ a modified version of Amimiya’s photosensitive BZ reaction model (in its four-variable form [46]) to investigate a reaction-diffusion system, specifically the synchronized oscillation reaction between gel patches in a two-dimensional thin-solution condition. Note that oscillation denotes periodic changes of concentration versus time. For a solution system that is sufficiently thin, the hydrodynamic effect can be disregarded, implying that it can be described by a reaction-diffusion equation. Notably, this four-variable model enables us to explore the roles of the intermediate products  $\text{HBrO}_2$ ,  $\text{Br}^-$ , and  $\text{BrMA}$  in the process of communication and synchronization between gel patches. It also helps us to determine which substance plays a significant role in the communication process and acts as a signaling molecule. The differential expression reads

$$\begin{aligned}\partial x/\partial t &= (x - x^2 + y(q - x) + IP_2) / \varepsilon_1 + D_x \nabla^2 x \\ \partial v/\partial t &= (-qy + 2xy + 0.5x^2 - vz - rv - IP_1) / \varepsilon_2 + D_v \nabla^2 v \\ \partial y/\partial t &= (-qy - xy + vz + IP_1) / \varepsilon_3 + D_y \nabla^2 y \\ \partial z/\partial t &= x - z - nvz + I(0.5P_1 + P_2)\end{aligned}\tag{1}$$

Where  $x$ ,  $v$ ,  $y$  and  $z$  denote dimensionless concentration of  $\text{HBrO}_2$ ,  $\text{BrMA}$ ,  $\text{Br}^-$  and  $\text{Ru}^{3+}$ , respectively.  $x=X/X_0$ ,  $v=V/V_0$ ,  $y=Y/Y_0$ ,  $z=Z/Z_0$ ,  $X$ ,  $V$ ,  $Y$ ,  $Z$ ,  $H$  and  $X_0$ ,  $V_0$ ,  $Y_0$ ,  $Z_0$ ,  $H_0$  are dimensional concentration and initial concentration of  $\text{HBrO}_2$ ,  $\text{BrMA}$ ,  $\text{Br}^-$ ,  $\text{Ru}^{3+}$ ,  $\text{H}^+$  respectively.  $A_0$  and  $B_0$  are dimensional concentration of  $\text{BrO}_3^-$  and  $\text{MA}$ .  $q$ ,  $\varepsilon_1$ ,  $\varepsilon_2$ ,  $\varepsilon_3$ ,  $n$ ,  $P_1$  and  $P_2$  are parameters of the Amimiya model.  $q=1 \times 10^{-4}$ ,  $\varepsilon_1=3.1 \times 10^{-3}$ ,  $\varepsilon_2=1.8 \times 10^{-5}$ ,  $\varepsilon_3=3.5 \times 10^{-4}$ ,  $n=12.23$ ,  $P_1=0.124$ ,  $P_2=0.77$ .  $I$  is dimensionless

illumination intensity. Dimensionless diffusion coefficients  $D_x$ ,  $D_y$ , and  $D_z$  are set at 1.0 (serving as the default value), which corresponds to a diffusion coefficient value of  $1.5 \times 10^{-5}$  cm<sup>2</sup>/s for the substance in solution ( $D_{\text{real}}$ ). The absence of a diffusion process for the catalyst substance ( $z$  variable) is attributed to its binding with the gel chains. The unit time  $T_0 = 1/(k_5 B_0)$ , the unit length  $L_0 = (D_{\text{real}} T_0)^{0.5}$ . The time step is set at  $1.0 \times 10^{-4}$ . The governing partial differential equations were numerically integrated using an explicit fourth-order Runge-Kutta method and utilizing nine-point central-difference approximations for 2D Laplacian operators. Our simulation of the 2D system employs  $1024 \times 1024$  grid points, and zero-flux boundary conditions were used at all ends.

As shown in Figure 1a, two circular gels are positioned and fixed in the center of the rectangular area with a distance  $dx$ . The remaining area (excluding the gels) contains the catalyst-free BZ solution. A pair of samples consists of gel patch 1 and 2, which are placed on the left and right sides of the space, respectively. The default concentration of reactants enables autonomous oscillation reactions to occur in the gel. The diffusion of intermediate products (HBrO<sub>2</sub>, Br<sup>-</sup>, and BrMA) continues throughout all regions of the system. Note that BZ reactions take place in the gel patches; while only the disproportionation of HBrO<sub>2</sub> occurs in the solution part. The reactants bromate, acidity, and malonate of BZR are uniformly distributed throughout the space and are assumed to satisfy the Pool approximation, which ensures that their concentrations remain constant.

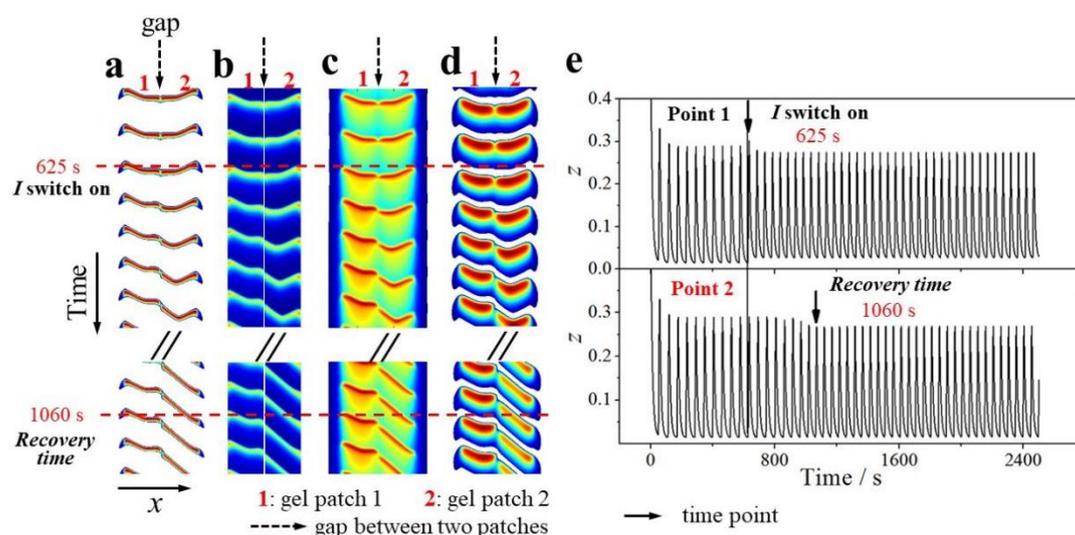


**Figure 1.** Schematic of simulated system and the illumination-modulated oscillation frequency. (a) for oscillation synchronization between the gel patches. The distance between two fixed gel patches is set at  $dx$ . Color denotes the value of  $z$  variable, with white indicating catalyst-free BZ solution. (b) Simulated nonmonotonic relationship between the oscillation frequency and the light intensity by using the modified four-variable Amimiya's model. Model concentrations:  $[\text{BrO}_3^-] = 0.1\text{M}$ ,  $[\text{H}^+] = 0.6\text{M}$ ,  $[\text{MA}] = 0.06\text{M}$ , which serve as default parameter values for our simulations.

The background light intensity ( $I_0$ ) illuminates both gel patch 1 and 2, serves as the default value for environmental illumination. Starting at a specific moment (uniformly 625s), a sustaining light intensity  $I$  is initiated and only illuminates to the gel patch 1. Photoreaction process in the BZR enables the system to produce various products, such as Br<sup>-</sup>, Ru<sup>3+</sup> and HBrO<sub>2</sub>. On the one hand, this process obeys a nonmonotonic relationship between oscillation frequency and light intensity (the F-I relationship) [46], that is, with increasing illumination, the oscillation frequency undergoes a fast rise and a slow drop, namely photo-promoting ( $I = 0.0 \sim 5.0 \times 10^{-5}$ ) and photo-inhibiting ( $I = 5.0 \times 10^{-5} \sim 1.28 \times 10^{-4}$ ) of oscillation frequency, respectively, as shown in Figure 1b. On the other hand, it modulates various types of diffusion-based communication through signal molecules. Here, the light intensity is a dimensionless parameter. In this paper, the destruction of oscillation synchrony is carried out based on the F-I relationship (the frequency of oscillation modulated by illumination intensity). Initially, the two gel patches have the same oscillation frequency under the background illumination ( $I_0 = 1.0 \times 10^{-5}$ ). When the light intensity is applied solely to the gel patch 1, it changes the oscillation frequency and generates a transient state of asynchronous oscillation between the gel pair. Then, the recovery process from oscillation synchrony can be observed and analyzed.

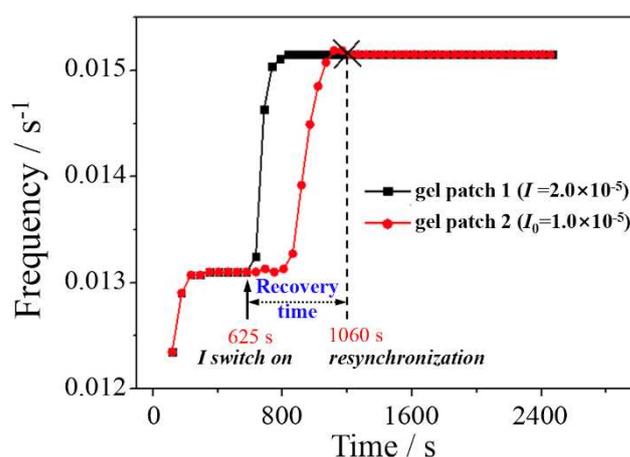
## 2.2. Recovery of synchrony oscillation between gel patches

Firstly, we analysis the recovery process of oscillation synchrony between the gel patches just after applying light  $I$  ( $2.0 \times 10^{-5}$ ) only to the patch 1. As shown in Figure 1b, the illumination  $I = 2.0 \times 10^{-5}$  is located at the photo-promotion region of the  $F$ - $I$  relationship. As shown in Figure 2a–d, the simulated spatiotemporal plot of each intermediate products enables us to analyze the process of resynchronized oscillation intuitively. Each space-time plot consists of 3000 concentration data for (a)  $\text{HBrO}_2$ , (b)  $\text{Ru}^{3+}$ , (c)  $\text{Br}^-$ , and (d)  $\text{BrMA}$  scan along the center line crossing the pair gels (see dashed line in Figure 1a) at 3 s intervals. The left and right areas of each plot, representing patches 1 and 2, are separated by respective gaps. The gap in the middle of each plot represents the space between the gel pair, where variables  $x$ ,  $v$ , and  $y$  can diffuse and fill due to their nature of diffusion. Note that the gap shown in Figure 2 represents the shortest distance between the two circular gels, however, the average distance between them is greater. When the system is in an initial synchronized state (time < 625 s), the pair gel has the same oscillation phase and frequency due to identical details on both patches (in the time region above the dashed line in Figure 2a–d). When the gel patch 1 is illuminated at time = 625 s (indicated by the dashed line), sustained changes occur in the spatiotemporal pattern within the patches (asynchrony state) until 1060 s, when two patches oscillate with the same frequency, implying the resynchronized oscillation. Note that the oscillation frequency of patch 2 changes only due to the communication between the gel, without any other impact on it. Figure 2e shows the local value of the variable  $v$  at the center of both patches versus time, revealing noticeable variations in oscillation amplitude at time points (625 s and 1060 s), respectively. At around 1060 s, the oscillation period of gel patch 2 is the same as that in patch 1 but with a phase delay due to a photo-promotion effect ( $I = 2.0 \times 10^{-5}$ ) on oscillation frequency in the gel patch 1, resulting in wave propagation from patch 1 to patch 2. Note that intermediate  $\text{HBrO}_2$  will gradually decompose during diffusion, which limits its communication distance as a signaling molecule. In previous studies, it is regards as the main signaling molecule for diffusion-based communication between the BZ gels [28]. The effect of different signaling molecules on the synchrony-recovery will be discussed later in order to identify the dominate signaling molecule.



**Figure 2.** Spatiotemporal plots of a pair of the gel patches. Data are read from the location which is denoted by a dash line as shown in Figure 1 (recording from 500 s to 1500 s with 3000 data in total). A dash line in (a) to (d) indicates the start time of illumination ( $I = 2.0 \times 10^{-5}$ ) to irradiate the gel patch 1 only, besides both gels are irradiated by background illumination ( $I_0 = 1.0 \times 10^{-5}$ ). (e) Time series of  $v$ -variable oscillations at the center point of the two gel patches.

Real-time oscillation frequencies in the center of two patches are shown in Figure 3, respectively. The real-time frequency refers to the reciprocal of current period of these oscillations. Figure 3 demonstrates a clear increase in oscillation frequency when the gel patch 1 is illuminated with  $I=2.0\times 10^{-5}$ , which aligns accord with the  $F-I$  relationship (refer to Figure 1b). Compared to Figure 2, Figure 3 clearly illustrates the time points when illumination starts and the recovery of synchrony. Moreover, Figure 3 demonstrates that the oscillation frequency of the pair patches ultimately matches that of the illuminated one (the gel patch 1).

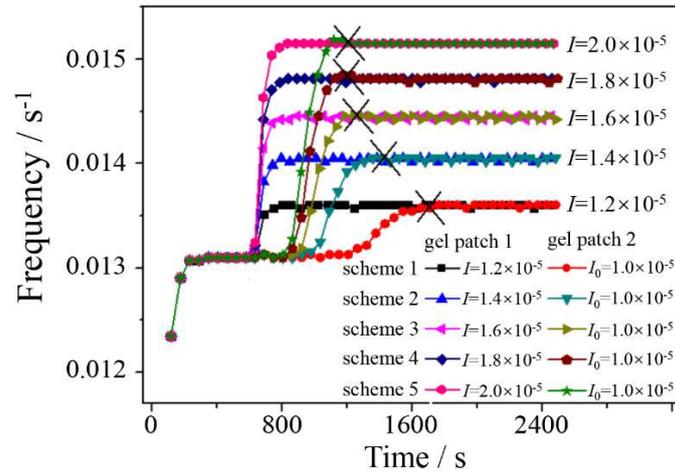


**Figure 3.** Time series of real-time oscillation frequency at the center of gel patches 1 and 2, respectively. Arrows indicate the moment when starts irradiating ( $I=2.0\times 10^{-5}$ ). The time point of synchronization recovery is denote by (×).

### 2.3. Recovery time of synchronization modulated by illumination

It is clear that the recovery time can server as a dynamic characteristic of the synchronization recovery. The effect of parameters on the resynchronization, specifically in terms of recovery time, is currently under investigation. The parameters include the light intensity of  $I$ , the distance between patches and the duration of illumination. Furthermore, studying diffusion-limited schemes help to identify signaling molecules. The mechanics of resynchronization can be discussed based on this.

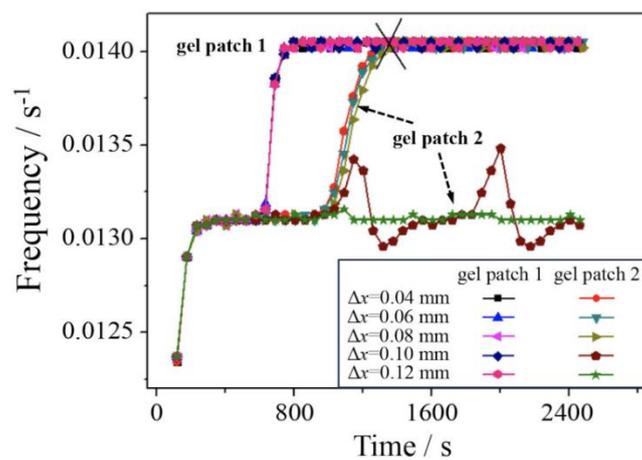
As shown in Figure 4, there are five scenarios with  $I$  set at  $1.2\times 10^{-5}$ ,  $1.4\times 10^{-5}$ ,  $1.6\times 10^{-5}$ ,  $1.8\times 10^{-5}$  and  $2.0\times 10^{-5}$ , respectively. The time series of frequency for each scenario eventually achieve a resynchronized state with different frequency, that is, high intensity of  $I$  for high frequency which dominated by photo-promotion effect as shown in Figure 1b. Keeping the start time of irradiating fixed at 625 s, the recovery time of oscillation synchronization between two gel patches decreasing from 1082 s, 732 s, 575, 520 s to 516 s, with increasing light intensity ( $I$ ) from  $1.2\times 10^{-5}$ ,  $1.4\times 10^{-5}$ ,  $1.6\times 10^{-5}$ ,  $1.8\times 10^{-5}$  to  $2.0\times 10^{-5}$ , respectively. Note that when  $I$  is greater than  $1.6\times 10^{-5}$ , the decreasing trend of the recovery time gradually slows down. Why is fasting recovery with illumination used for generating synchronization? According to the Amimiya's photosensitive BZR model [46], our work on the  $F-I$  relationship [46], and a general viewpoint of  $\text{HBrO}_2$  diffusion-based communication [28], at low light intensity, photoreaction generates  $\text{HBrO}_2$  which not only promotes oscillation frequency but also increases diffusion-based communication due to a high concentration of photo-generated  $\text{HBrO}_2$ , thereby shorting the recovery time. However, at high light intensity, the photo-generation effect on  $\text{HBrO}_2$  approaches saturation [45,46], where the photo effect on the recovery time changes little with light intensity.



**Figure 4.** Recovery of synchronization for scenarios of gel patches with different  $I$ . The start time for irradiating the gel patch 1 is the same for all scenarios, at time point 625 s as arrow indicated.  $I_0=1.0\times 10^{-5}$ . The moments of recovered synchronization are marked as (x) on curves, respectively.

#### 2.4. Recovery time of synchronization modulated by the patches-distant

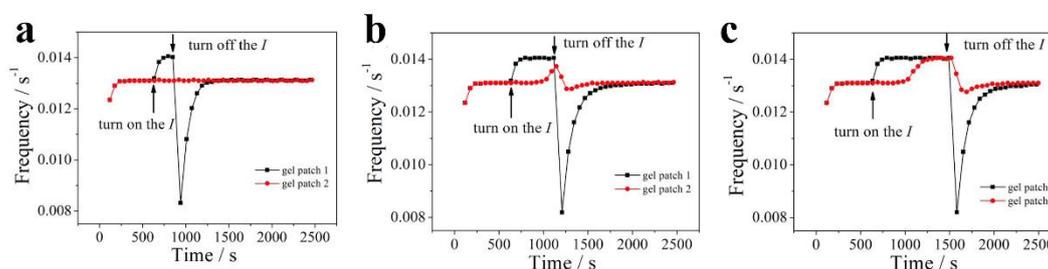
Another crucial factor that influences the communication process is the distance separating the communicated pair. As shown in Figure 5, here are five schemes with the distance  $dx$  set at 0.04 mm, 0.06 mm, 0.08 mm, 0.10 mm, and 0.12 mm, respectively. In the initial state, each scheme has the same oscillation frequency until the gel patch 1 is exposed to the irradiated light intensity ( $I = 1.4\times 10^{-5}$ ). It is evident from the Figure 5 (e.g., at the marking of gel patch 1) that the oscillation frequency of gel patch 1 increases rapidly in all the systems after application and then stabilizes. After the “light on” (time > 625 s), the oscillation frequency of gel patch 1 suddenly increases to 0.014 s<sup>-1</sup>, while the frequency of gel patch 2 undergoes changes based on the value of  $dx$ . Specifically, when  $dx \leq 0.08$  mm, resynchronization between the pair is successful with almost identical recovery time (732 s). However, when  $dx > 0.08$  mm, the gel pair experiences an asynchronous state. In particular, new frequency of the oscillation frequency occurs when  $dx = 0.10$  mm, which is represented as a period change of frequency versus time (see Figure 5). The results suggest that the synchronous state can only occur when the distance is small enough ( $dx \leq 0.08$  mm).



**Figure 5.** The recovery time of synchronization versus the distant between the two patches.  $I = 1.4\times 10^{-5}$ .

#### 2.5. Effect of illumination-duration on the recovery time

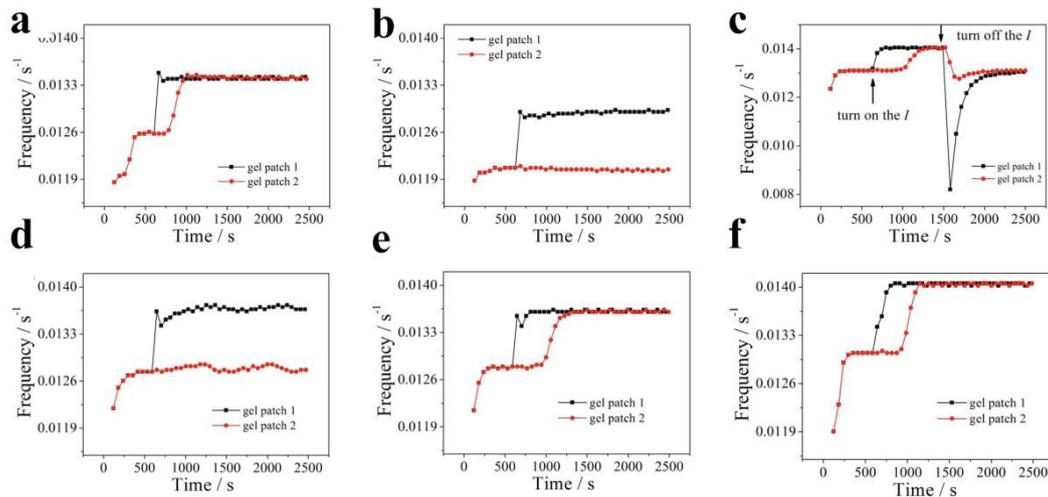
In the above schemes, there is only “switch on” option for the irradiation on the patch 1. As shown in Figure 6, the effect of  $I$ -duration on the resynchronization is discussed, with options for both “switch on” and “switch off” irradiation. The  $I$ -duration for three schemes is 250 s, 500 s, and 875 s, respectively. For the gel patch 1, all schemes shown a fast decrease of oscillation frequency. In the photosensitive BZR, the critical concentration of  $\text{Br}^-$  ( $[\text{Br}^-]_{\text{cr}}$ ) in photo-promotion state ( $I=1.4\times 10^{-5}$ ) is high than that in the low light intensity ( $I_0=1.4\times 10^{-5}$ ), thus, when the illumination changes from  $I$  to  $I_0$  (switch off), the reaction requires more time to reach  $[\text{Br}^-]_{\text{cr}}$ , resulting in a prolonged period of oscillation and a decrease in frequency [46]. For gel patch 2, there is no change in frequency 2 when the duration is short (Figure 6a). However, when the duration equals 500 s, a critical state of resynchronization occurs (see Figure 6b). When the  $I$ -duration is large enough, clear resynchronization takes place until “switch off”. This suggests that the diffusion-based communication of signaling molecules in response to light intensity can only be effective if the new state of patch 1 is maintained for a certain duration. In other words, the resynchronization requires sufficient time for the diffusion of signaling molecules through the gap while the patch 1 remains in its current state (illuminated by  $I$ ).



**Figure 6.** The relationship between the duration of  $I$  and the synchronization recovery.  $I = 1.4\times 10^{-5}$ . The start time of  $I$  for all scenarios are the same. The duration time of  $I$  respectively are: (a) 250s; (b) 500s; (c) 875s, respectively.

### 2.6. Signal molecules for the synchrony recovery

Another fundamental question remains unanswered: what is the effect of diffusive molecules ( $\text{HBrO}_2$ ,  $\text{BrMA}$  and  $\text{Br}^-$ ) of BZR on the resynchronization. Here, numerical simulations are conducted for ideal schemes with limited diffusion. These schemes involve variables  $x$ ,  $v$  and  $y$ , which correspond to  $\text{HBrO}_2$ ,  $\text{BrMA}$  and  $\text{Br}^-$  in the system with or without diffusion. Some conclusions can be drawn from these six schemes based on the data in Figure 7. Firstly, in all schemes, the resynchronization will fail where the diffusion of  $\text{HBrO}_2$  is totally prohibited, which indicate the diffusion of  $\text{HBrO}_2$  is the sufficient and necessary condition for the resynchronization. Secondly, by comparing Figure 6a,e, it is clear that the diffusion of  $y$  ( $\text{Br}^-$ ) prolongs the recovery time of resynchronization process, indicating an inhibition effect of  $\text{Br}^-$  on the recovery. Thirdly, by comparing Figure 6 (a) with (f), the diffusion of  $\text{BrMA}$  have a promotion effect on the basic oscillation frequency (without regard to illumination) but have little effect on the recovery time. In addition to  $\text{HBrO}_2$ , the prolonging effect of  $\text{Br}^-$  on the resynchronization is due to its inhibition of BZR autocatalysis. The promotion effect of  $\text{BrMA}$  diffusion on the basic oscillation frequency originates from a decrease in concentration of  $\text{BrMA}$  within the gel patch 1 induced by diffusion, which indirectly reduces the production of  $\text{Br}^-$ , as demonstrated in our previous work [46]. As shown in Figure 7, it is evident that the presence of  $\text{Br}^-$  inhibits the recovery process, indicating its role as a signaling molecule for communication in our system. As far as we know, this is the first time that a second signaling molecule has been identified in the synchronization of the BZR system.



**Figure 7.** Recovery of synchronization for various diffusion limited systems.  $I=1.4 \times 10^{-5}$ . Only variable (a)  $x$ , (b)  $v$ , or (c)  $y$  with diffusion ( $D=1.0$ ), respectively. Only variable (d)  $x$ , (e)  $v$ , or (f)  $y$  without diffusion ( $D=0.0$ ), respectively. Other variables are the same as the default setting.

### 3. Conclusions

Using a modified Amimiya's photosensitive BZR model for studying resynchronization oscillation between a pair gel patch, we found that recovery process of the synchronization can be modulated by distance between the pair, the intensity and the duration of illumination. The results revealed that photo-promotion effect of the  $F$ - $I$  relationship shorting the oscillation resynchronization with one patch-illuminated, while both the pair distance and the illumination-duration manifest as a "switch effect" on the oscillation resynchronization. Moreover, besides  $\text{HBrO}_2$ , we found the inhibitor of oscillation BZR ( $\text{Br}$ ) have an obvious delay effect on the resynchronization process, which indicate oth  $\text{HBrO}_2$  and  $\text{Br}$  are signaling molecules for such diffusion-based communication. To sum up, our results indicate that a "switch effect" of pair-distance which modulate by photo-promotion of the  $F$ - $I$  relationship of the photosensitive BZR on the oscillation resynchronization of the pair gel patches, which originate from the competition between photo-generation while diffusion of signaling molecules ( $\text{HBrO}_2$  and  $\text{Br}$ ) and disproportionation of  $\text{HBrO}_2$ .

Furthermore, new experimental efforts should be conducted under the guidance of these simulations. The size of gel with a circular shape may significantly impact the distance effect on resynchronization. Therefore, further research should be carried out using pairs of rectangle gels or other shaped samples. Another important issue is how the new frequency generation occurs during the transition from resynchronization to asynchronization via a state of periodic changes in oscillation frequency. Moreover, based on our results in the inert system, exploration into various types of directional locomotion and collective behavior of active gel with diffusion-based communication can proceed further.

**Author Contributions:** Conceptualization, L.R. and D.S.; methodology, L.R.; formal analysis, D.S.; investigation, Y.T.; data curation, Q. Z.; writing—original draft preparation, D.S.; writing—review and editing, L.R.; visualization, D.S.; project administration, L.R.; funding acquisition, L.R. All authors have read and agreed to the published version of the manuscript.

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