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Article

Hydration Heat and Hydration Kinetics of Cement Paste Compound with Molybdenum Tailings Powder

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Abstract: Molybdenum tailings powder (MTs) is an industrial waste that contains more than 85% contents of SiO₂, Al₂O₃, CaO, and Fe₂O₃. Therefore, MTs has the potential pozzolanic activity and can be used as a mineral admixture in cementitious materials. In order to understand the influence of MTs as an admixture on the cement hydration process, the hydration heat and hydration kinetics of the composite cementitious materials (CCMs) were investigated by an isothermal calorimeter and the Krstulovic-Dabic model. Furthermore, the influences of fly ash (FA), slag (SL) and MTs on hydration heat at the same content were compared and analyzed. Results show that proper amount of MTs can promote the hydration of CCMs. When the content of MTs is not more than 15%, the second exothermic peak of CCMs appears earlier and the peak heat release increases. However, when the content of MTs exceeds 15%, the second exothermic peak of CCMs is delayed and the peak heat release decreases. The cumulative heat release of CCMs gradually decreases with an increasing content of MTs. When the replacement of MTs, FA, and SL is 15% respectively, the addition of MTs enhances the second exothermic peak of CCMs compared to FA and SL. The final heat release of MTs is higher than that of FA, but lower than that of SL. The hydration process of CCMs undergoes three stages: nucleation and crystal growth (NG), interactions at phase boundaries (I), and diffusion (D). The incorporation of MTs shortens the NG stage and I stage.

Keywords: molybdenum tailings powder; hydration heat; hydration kinetics; kinetic parameters

1. Introduction

With the rapid development of the Chinese economy, there is also a growing demand for mineral resources, which has resulted in the large-scale exploitation of various minerals, including molybdenum minerals. However, the ore grade of molybdenum deposits is low [1,2]. After separating the valuable metals from the ore, the majority (95% of the total) is discharged as molybdenum tailings [3,4]. The accumulation of molybdenum tailings not only occupies large amounts of land, but also pollutes the surrounding environment [5,6]. Therefore, the utilization of molybdenum tailings as a resource is of great significance in reducing environmental pollution and achieving a low-carbon economy. Molybdenum tailings powder (MTs) used as an admixture in cementitious materials can not only effectively reduce cement consumption and carbon emission, but also contribute to the sustainable development of resources and the environment [2–4,7].

Mineral admixtures are an important component of modern concrete. Studies have shown [8–14] that tailings containing SiO₂, Al₂O₃, CaO, and Fe₂O₃ can be used as concrete admixtures after being made into fine powders. Han et al. [8] and Cheng et al. [9,10] confirmed the feasibility of using activated iron tailings powder as an admixture in concrete preparation. Geng [11] and Qiu et al. [14] reported that activated lead-zinc tailings powder can be used as an admixture in concrete preparation. Xu et al. [12] and Huang et al. [13] found that it is feasible to use the activated copper tailings powder as a concrete admixture. Molybdenum tailings have a chemical composition similar to that of iron, lead-zinc, and copper tailings, and can be used as an admixture in concrete. However, different types of tailings fine powders have different performances as concrete admixtures due to

differences in beneficiation process and ore composition. It has also been shown [15–17] that the incorporation of copper, iron, or bauxite tailings powders reduces the hydration rate and accumulated heat release of the cement paste, and then there were some differences in the hydration process of cement by different tailings powders. Meanwhile, studies have shown [18–22] that molybdenum tailings can be used as fine aggregate to replace natural sand or as admixture to replace cement in preparing mortar or concrete. At present, research on the influence of molybdenum tailings as fine aggregate or admixture on the performance of mortar or concrete mainly focuses on macro-performance and micro-performance. Furthermore, the influence of MTs as an admixture on the early hydration process of composite cementitious materials (CCMs) is of great significance to the later performance of CCMs. Therefore, further study the influence of MTs on the hydration hardening mechanism and kinetics of CCMs, it is of great significance to study the properties of molybdenum tailings powder-cement cementitious materials and fully understand the influence of MTs on the early hydration process of cement. This will enhance the utilization rate of molybdenum tailings resources.

Presently, there are more methods available to investigate the hydration process and kinetics of CCMs [23–27], with the Krstulovic-Dabic model being the most commonly used. Krstulovic et al. [27] proposed a hydration kinetic model that can calculate the rate curve of the hydration reaction and the kinetic parameters. This model is based on the hydration heat and can be used to determine the hydration process and kinetic parameters of the CCMs. Yan et al. [28,29] discovered that the Krstulovic-Dabic model can better characterize the hydration process of the CCMs when the fly ash (FA) content is not more than 65% and the slag (SL) content does not exceed 70%. Cheng et al. [16] found that the Krstulovic-Dabic model can also simulate the hydration kinetics of cement-iron tailings powder composite cementitious materials. Therefore, the Krstulovic-Dabic model could be used to characterize the hydration process of CCMs with MTs.

In this paper, the MTs comes from Yichun Luming Mining Co., Ltd, China. The hydration heat of CCMs was measured by an isothermal calorimeter to investigate the influence of MTs on the hydration heat of cement. Based on the Krstulovic-Dabic model, the hydration process and kinetic parameters of the CCMs were calculated and analyzed. The influence of MTs, FA, and SL on the hydration heat and hydration kinetics of cement were compared and analyzed under the same dosage. Additionally, the influence of MTs on the early hydration process of cement was discussed. The purpose of this paper is to explore the influence of MTs as mineral admixture on cement hydration process. This research aims to provide a theoretical and experimental basis for the efficient utilization of molybdenum tailings as a valuable resource.

2. Hydration Kinetic Model

The hydration process of CCMs is generally divided into five stages: initial interaction period (I), induction period (II), reaction acceleration period (III), deceleration period (IV), and slow interaction period (V) [30,31]. While in early hydration, its heat release normally accounts for only about 5% of the total heat release, which is negligible compared to the whole hydration process. Therefore, the influence of the first exothermic peak is generally ignored in the study of hydration kinetics, and the simulation discussion begins at the end of the induction stage [32–34].

The Krstulovic-Dabic model shows the relationship between the hydration degree (α) and the hydration time (t), and the kinetic model is divided into the following three stages [27,35]:

Nucleation and Crystal Growth, NG

$$\left[-\ln(1-\alpha)\right]^{1/n} = K_1(t-t_0) = K'_1(t-t_0) \quad (1)$$

Interactions at phase boundaries, I

$$\left[1-(1-\alpha)^{1/3}\right]^1 = K_2 t^{-1}(t-t_0) = K'_2(t-t_0) \quad (2)$$

Diffusion, D

$$\left[1-(1-\alpha)^{1/3}\right]^2 = K_3 t^{-2}(t-t_0) = K'_3(t-t_0) \quad (3)$$

Differentiating Equations (1) ~ (3) yields Equations (4) ~ (6).

NG

$$d\alpha / dt = F_1(\alpha) = K_1' n (1-\alpha) [-\ln(1-\alpha)]^{(n-1)/n} \quad (4)$$

I

$$d\alpha / dt = F_2(\alpha) = K_2' \cdot 3(1-\alpha)^{2/3} \quad (5)$$

D

$$d\alpha / dt = F_3(\alpha) = K_3' \cdot 3(1-\alpha)^{2/3} / [2 - 2(1-\alpha)^{1/3}] \quad (6)$$

Where α is the hydration degree; n is the reaction order; K_i and K_i' ($i = 1, 2, 3$) are the reaction rate constants of three hydration processes; t is the hydration time; t_0 is the end time of the induction period, which is the point at which the hydration exothermic rate starts to increase uniformly [36]; r is the reaction particle radius; $d\alpha/dt$ is the hydration rate.

Based on the hydration heat test measured by isothermal calorimetry, the hydration heat release rate and cumulative heat release of CCMs were obtained. The formulas (7) ~ (8) were used to transform the hydration heat data into the required in the hydration kinetics model. The hydration kinetic formula (Equation (9)) proposed by Knudsen [37] was used to calculate the Q_{\max} . The formula is as follows.

$$\alpha(t) = Q(t) / Q_{\max} \quad (7)$$

$$d\alpha / dt = dQ / dt \cdot 1 / Q_{\max} \quad (8)$$

$$1 / Q(t) = 1 / Q_{\max} + t_{50} / [Q_{\max} (t - t_0)] \quad (9)$$

Where $Q(t)$ is the heat released by time t ; Q_{\max} is the total heat release at the end of hydration; and t_{50} is the hydration time required for the heat release to reach 50% of Q_{\max} .

3. Experimental

3.1. Raw Materials

P.I 42.5 Portland cement (PC) satisfied Chinese GB 175 was supplied by China Fushun Aocell Technology Co., Ltd. Molybdenum tailings powder (MTs) from Yichun Luming Mining Co., Ltd, China. The low calcium class F fly ash (FA) and S95 grade fine slag (SL) were employed, produced by Xiangtan Power Plant and Xiangtan Steel Plant (Hunan Province, China), respectively. Distilled water was used. The photos of raw materials are shown in Figure 1, their chemical compositions and physical properties are shown in Table 1. Table 2 lists the main technical indexes of MTs. The particle size distribution of raw materials is shown in Figure 2. The XRD pattern of MTs is shown in Figure 3a. The main mineralogical compositions of MTs are quartz, feldspar, mica and chlorite. The SEM pattern of MTs is shown in Figure 3b, the MTs particles with irregular shapes and rough surfaces.

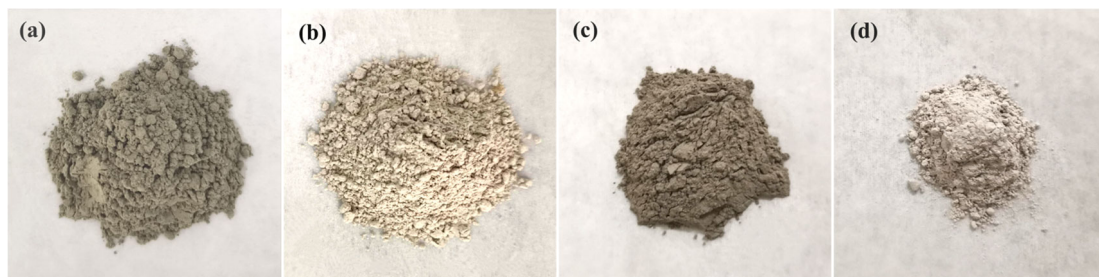


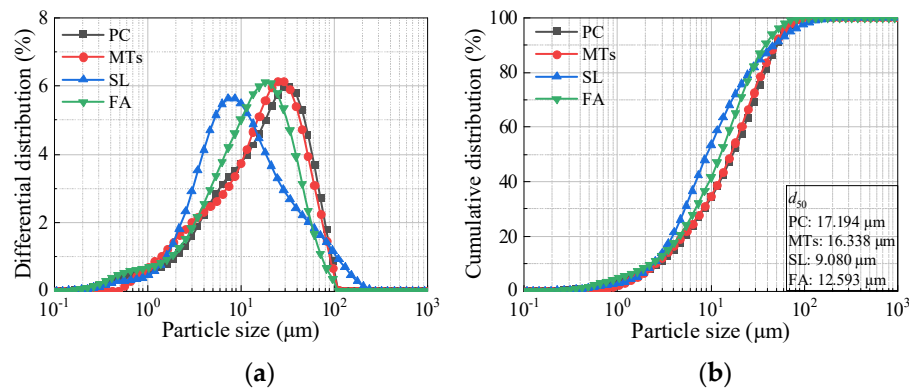
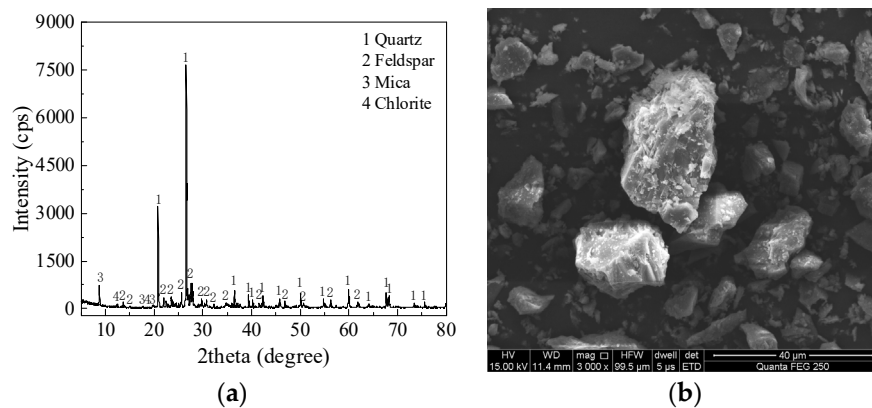
Figure 1. Raw materials. (a) PC, (b) MTs, (c) FA, (d) SL

Table 1. Chemical compositions and physical properties of raw materials

Materials	Chemical composition (%)									LOI ¹ (%)	SSA ² (m ² /kg)
	SiO ₂	Al ₂ O ₃	Fe ₂ O ₃	CaO	MgO	SO ₃	K ₂ O	Na ₂ O	MgO		
PC	20.84	4.68	3.56	63.43	3.29	2.30	—	0.55	—	1.48	358
MTs	67.75	13.84	2.71	2.75	1.14	2.24	5.45	1.77	1.14	2.01	367
FA	52.70	25.80	9.70	3.70	1.20	0.20	1.16	0.79	0.88	4.20	434
SL	31.96	14.33	0.49	36.42	6.65	2.50	0.56	0.43	6.65	—	483

¹ Loss on ignition, ² Specific surface area.**Table 2.** Main technical indexes of MTs

Materials	Standard consistency (%)	f-Cao	Setting time (min)		Activity index (%)		Water demand ratio (%)
			Initial	Final	7 d	28 d	
MTs	32.5	Eligible	386	540	75	69	109

**Figure 2.** (a) Differential distribution and (b) Cumulative distribution of raw materials**Figure 3.** (a) XRD pattern and (b) SEM pattern of MTs

3.2. Mixture Proportions and Testing Methods

The mixture proportions of the CCMs pastes are summarized in Table 3. The MTs substitution rates were 0%, 5%, 15%, 25%, and 35%, the FA and SL replacement rates were both 15%, and the water-to-binder (w/b) ratio of 0.4 was used in this study. An eight-channel TAM Air isothermal calorimeter (as shown in Figure 4) was used to determine the exothermic characteristics of CCMs pastes. In the preparation of pastes, each CCMs sample was 50 g, and it had the same mixing period (dry stirring for 60 s, slow and fast stirring for 60 s after adding water). The test temperature is set at 20 °C, and the test time is 120 h.

Table 3. Mixture proportions.

Sample	Mass fraction (%)					w/b
	PC	MTs	FA	SL	Water	
PC	100	0	—	—	40	0.4
MT _{S5}	95	5	—	—	40	0.4
MT _{S15}	85	15	—	—	40	0.4
MT _{S25}	75	25	—	—	40	0.4
MT _{S35}	65	35	—	—	40	0.4
FA ₁₅	85	—	15	—	40	0.4
SL ₁₅	85	—	—	15	40	0.4

4. Results and Discussion

4.1. Effect of Hydration Heat

4.1.1. MTs Content

The hydration heat of CCMs with different MTs content is shown in Figure 4. As presented in Figure 4a, the end time of the induction period of CCMs delays and the rate of heat release decreases with MTs increasing. When the content of MTs is not more than 15%, the second exothermic peak of the CCMs is advanced and its peak heat release enhanced. When the content of MTs exceeds 15%, the second exothermic peak of CCMs is delayed and its peak heat release decreases. And the addition of MTs influences the peak pattern of the second exothermic peak of CCMs. The PC undergoes a relatively gentle exothermic phase before reaching the second peak of exothermic reaction. However, as the MTs increases, the gentle section before the peak of the second exothermic peak of CCMs gradually shortens until it disappears. Furthermore, the pozzolanic activity of MTs is activated in the later stage of hydration, and its pozzolanic effect results in higher heat release rate for MT_{S5}, MT_{S15}, MT_{S25}, and MT_{S35} compared to PC.

As shown in Figure 4b, the cumulative heat release of CCMs gradually decreases with increasing MTs content. When the hydration time is not more than 20 hours, there are minimal differences in the cumulative heat release curves of MT_{S5}, MT_{S15}, and PC. However, the difference between the cumulative heat release curves of MT_{S5} and MT_{S15} and that of PC gradually increases as the hydration time extends.

The incorporation of MTs influences the heat release rate and cumulative heat release of CCMs due to its crystallization nucleation and pozzolanic effect. The crystallization nucleation and pozzolanic effect of MTs occur in the hydration acceleration period and the hydration stable period of CCMs, respectively [28,29,38–40]. Meanwhile, the incorporation of MTs reduces the proportion of cement clinker in CCMs and influences the effective water-to-cement (w/c) ratio of CCMs. Therefore, when the content of MTs is small, the effective w/c ratio of CCMs increases. Moreover, cement particles wrap around MTs particles, and the surface of MTs acts as a crystallization nucleation site. This provides more nucleation points, increases the formation rate of hydration products such as C-S-H gel, and enhances the rate of hydration heat release. However, when the MTs content is higher, the proportion of cement clinker in CCMs significantly decreases, and the promotion effect of crystallization nucleation of MTs is not significant. Therefore, the hydration heat release rate is reduced. Furthermore, in the later stage of hydration, the formation of Ca(OH)₂ increases the pH value, which stimulates the pozzolanic activity of MTs. This promotes the secondary hydration reaction of CCMs, resulting in the generation of hydration products such as C-S-H gel and a slight increase in the rate of hydration heat release.

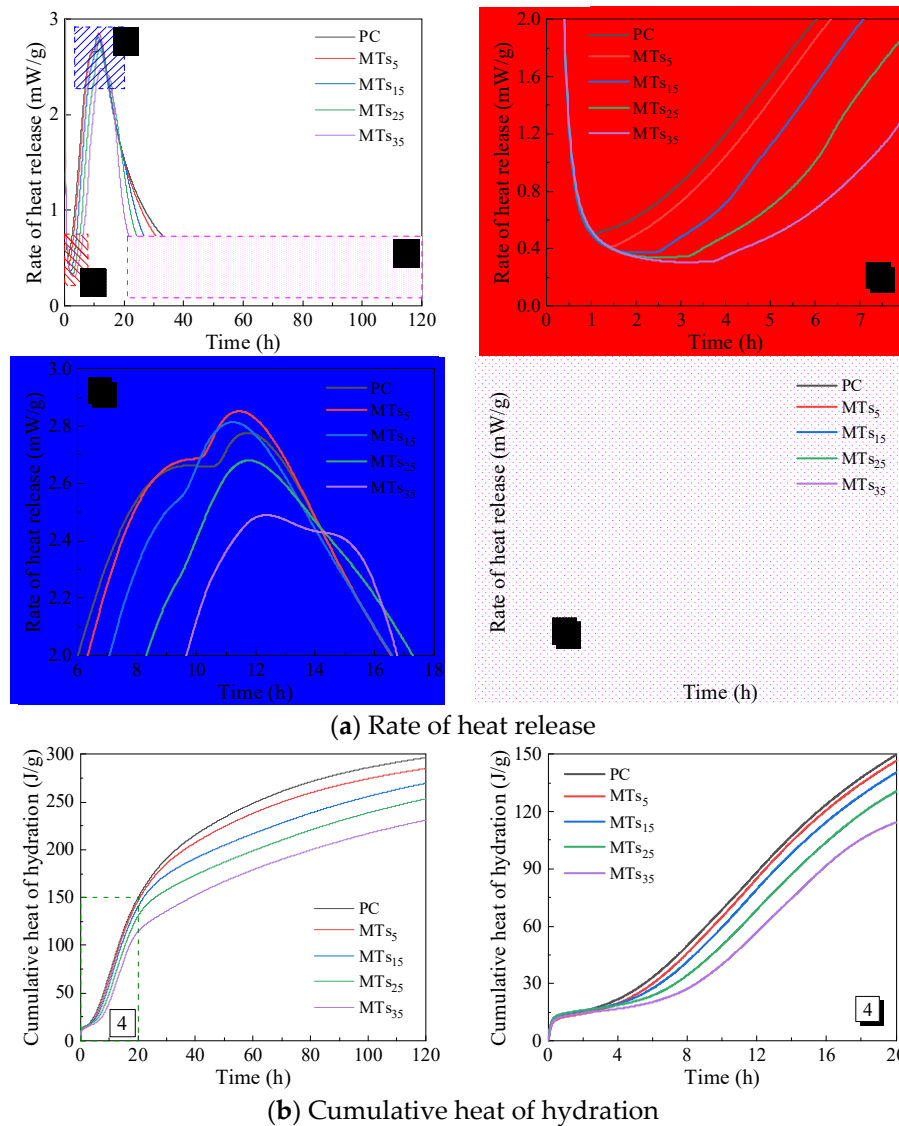


Figure 4. Influence of MTs content on hydration heat release of the CCMs. (1~4 is enlargements of corresponding parts)

Table 4 presents the influence of MTs content on the acceleration period of CCMs. The incorporation of MTs delays the end time of induction period t_0 of CCMs. Furthermore, as the amount of MTs increased, t_0 was progressively delayed. When the content of MTs increased from 0% to 35%, t_0 was delayed from 1.07 h to 3.72 h. Compared with PC, MTs₅ and MTs₁₅ reach the second exothermic peak with shorter time t_1 and higher exothermic peak V , while MTs₂₅ and MTs₃₅ reach the second exothermic peak with later time t_1 and lower exothermic peak V . However, the incorporation of MTs shortens the time from the end of the induction period to the second exothermic peak (the acceleration period ($t_1 - t_0$) is shortened).

The incorporation of MTs reduces the proportion of cement clinker and the concentration of Ca^{2+} in CCMs, therefore, prolonging the nucleation time of $\text{Ca}(\text{OH})_2$ and delaying the end time of the induction period [28]. When the MTs content is small, the dilution effect of MTs and the surface of MTs act as crystallization nucleation sites in CCMs, thus promoting the hydration of CCMs and increasing their hydration heat release rate. When the MTs content is larger, the proportion of cement clinker in CCMs is significantly reduced, and MTs has a lower promote effect on cement hydration, which reduces the hydration heat release rate of CCMs.

Table 4. Influence of MTs content on the acceleration period of CCMs

Sample	t_0 (h)	t_1 (h)	(t_1-t_0) (h)	$V(mW/g)$
PC	1.07	11.72	10.65	2.776 3
MTs ₅	1.45	11.45	10.00	2.851 8
MTs ₁₅	2.50	11.22	8.72	2.813 6
MTs ₂₅	3.15	11.77	8.62	2.680 1
MTs ₃₅	3.72	12.31	8.59	2.489 5

Note: t_0 is the end time of the induction period, t_1 is the time to reach the second exothermic peak, t_1-t_0 is the acceleration period time, and V is the peak value of the second exothermic peak.

Table 5 indicates the relative percentage of hydration heat of CCMs. The relative percentage of hydration heat is the ratio of the hydration heat of CCMs with the mixture to the hydration heat of the reference sample [15]. It can be seen from Table 5 that the incorporation of MTs reduces the relative percentage of hydration heat of CCMs. With the extension of hydration time, the relative percentage of hydration heat of CCMs gradually stabilized, which is greater than the mass fraction of cement in CCMs. MTs has a certain potential activity. However, in the early stage of hydration, the filler effect and nucleation role of MTs are mainly played [38,41–43]. In the later stage of hydration, the pozzolanic activity of MTs is stimulated, resulting in a pozzolanic exothermic effect, so that the percentage of hydration heat is greater than the mass fraction of cement in CCMs.

Table 5. Relative percentage of hydration heat of CCMs (%)

Sample	3 h	6 h	12 h	24 h	48 h	72 h	96 h	120 h
PC	100	100	100	100	100	100	100	100
MTs ₅	89	88	97	98	96	96	96	96
MTs ₁₅	94	82	90	93	88	87	89	91
MTs ₂₅	94	70	77	86	80	81	83	85
MTs ₃₅	83	61	64	74	71	73	76	78

4.1.2. Mineral Admixture Types

Figure 5 shows the influence of MTs, FA, and SL with the same replacement ratio of 15% on the hydration heat of CCMs. According to Figure 5a, the incorporation of MTs, FA, and SL all delays the end time of the induction period of the cementitious system, among which MTs has a significant influence on the end time of the induction period of CCMs, and the end time of the induction period of CCMs mixed with FA and SL is similar. The incorporation of MTs, FA, and SL all reduces the heat release rate at the end of the induction period of CCMs, and the reduction range is similar, which decreases from 0.5 mW/g to about 0.35 mW/g. And the incorporation of MTs, FA, and SL influences the peak value and peak pattern of the second exothermic peak of CCMs. The second exothermic peak of CCMs with MTs is advanced and its peak heat release increases, the second exothermic peak of CCMs with FA is delayed and its peak heat release decreases, and that of CCMs with SL is reduced. It shows that compared with FA and SL, the same replacement ratio of MTs resulted in faster hydration products in CCMs during the acceleration period [as shown in Figure 5a-2]. After 60 h of hydration of CCMs [as shown in Figure 5a-3], the hydration heat release rate of MTs₁₅ and SL₁₅ gradually exceeds that of PC and FA₁₅.

According to Figure 5b, when the hydration time is not more than 30 h, the cumulative heat release curves of the PC, MTs₁₅, FA₁₅, and SL₁₅ are similar. When the hydration time is 120 h, the order of cumulative heat release is PC>SL₁₅>FA₁₅>MTs₁₅.

From the hydration heat curve, it can be seen that MTs, FA, and SL play a similar role in CCMs. In the hydration acceleration period, they mainly play the role of crystallization nucleation. In the hydration stable period, the pozzolanic effect of them mainly occurs to promote the secondary hydration of CCMs. Studies have shown [38,44] that the specific surface area and surface properties of the admixture will influence the nucleation role, and the nucleation role of the SL in the hydration

acceleration period is stronger than that of FA. It can be seen from Table 1 that the specific surface areas and surface properties of MTs, FA, and SL are different, so their effects on the hydration heat release of cement are also different. Meantime, the difference of MTs, FA, and SL of the potential activity, resulted in different activities excited in the later stage of hydration. Therefore, the hydration heat release rate and cumulative heat release of CCMs are different with different intensities of the pozzolanic effect.

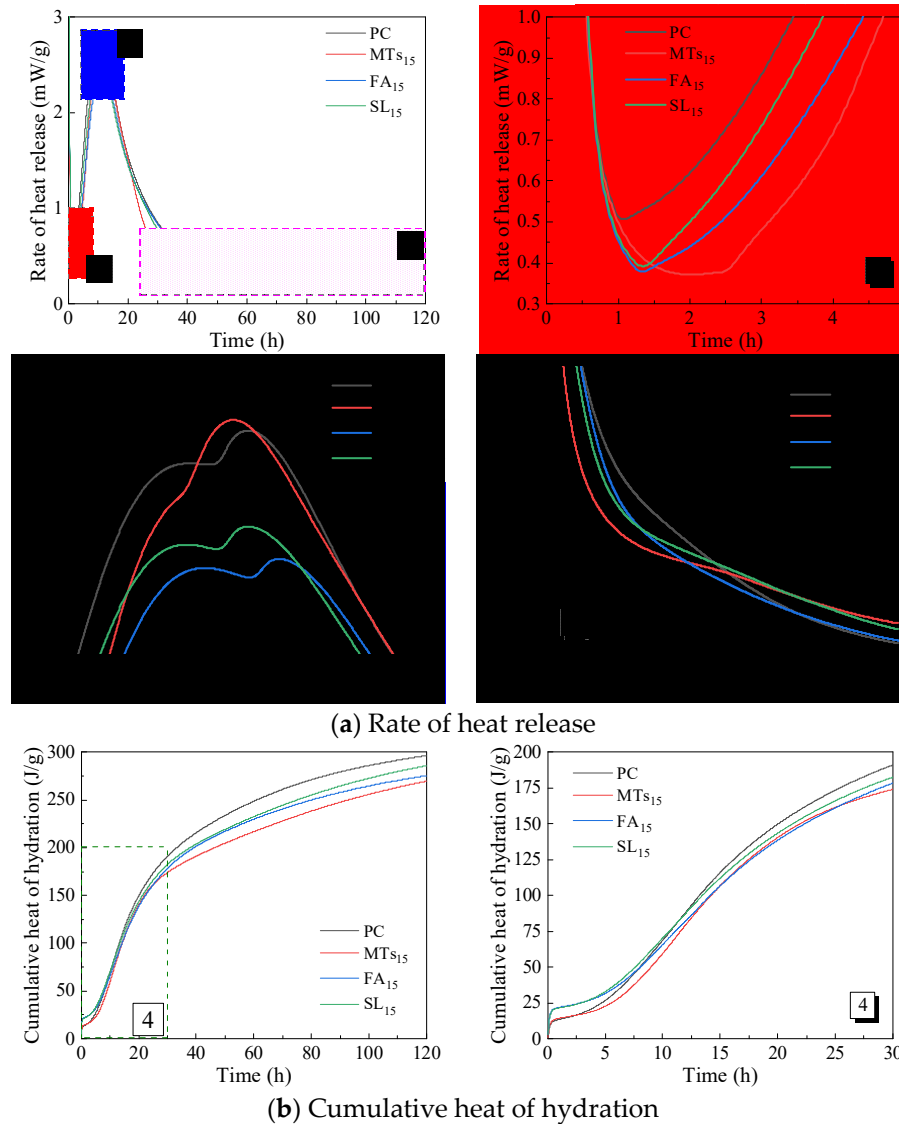


Figure 5. Influence of admixture types on hydration heat release of CCMs (1~4 is enlargements of corresponding parts)

The influence of admixture types on the acceleration period of CCMs is shown in Table 6. The incorporation of MTs, FA, and SL all delays the end time of the induction period of the cementitious system, and the incorporation of MTs has the greatest influence on the end time of the induction period of the system. The second exothermic peak of CCMs with MTs is advanced and its peak heat release increases; the second exothermic peak of CCMs with FA or SL is delayed and its peak heat release decreases. The incorporation of FA prolongs the acceleration period of CCMs, and the incorporation of MTs and SL shortens the acceleration period of CCMs. The acceleration period of MTs₁₅ is the shortest, indicating that the incorporation of MTs accelerates the hydration rate of CCMs and shortens the hydration time of CCMs.

Table 6. Influence of admixture types on the acceleration period of CCMs

Sample	t_0 (h)	t_1 (h)	(t_1-t_0) (h)	V (mW/g)
PC	1.07	11.72	10.65	2.776 3
MT _{S15}	2.50	11.22	8.72	2.813 6
FA ₁₅	1.33	12.77	11.44	2.328 5
SL ₁₅	1.33	11.73	10.40	2.441 9

Table 7 shows the relative percentage of hydration heat of CCMs with MTs, FA, and SL, respectively. The relative percentage of hydration heat of MT_{S15} is 94% and 82% at 3 h and 6 h, which is lower than 100%. The relative percentage of hydration heat of FA₁₅ is 139% and 109% at 3 h and 6 h, and the relative percentage of hydration heat of SL₁₅ is 139% and 115% at 3 h and 6 h, which are higher than 100%. With the extension of hydration time, the relative percentage of hydration heat of MT_{S15}, FA₁₅, and SL₁₅ gradually approaches 91%, 93%, and 96%, respectively, which are all greater than the mass fraction of cement in CCMs. It shows that the pozzolanic activity of MTs, FA and SL is activated in the stable hydration period, which leads to the relative percentage of hydration heat greater than the mass fraction of cement in CCMs.

Table 7. Relative percentage of hydration heat of CCMs (%)

Sample	3 h	6 h	12 h	24 h	48 h	72 h	96 h	120 h
PC	100	100	100	100	100	100	100	100
MT _{S15}	94	82	90	93	88	87	89	91
FA ₁₅	139	109	93	93	93	92	92	93
SL ₁₅	139	115	99	96	94	94	95	96

4.1.3. Total Heat Release

The hydration heat only measured the cumulative heat release of CCMs for 120 h. The total heat release Q_{\max} of CCMs was derived according to hydration heat data and the Knudsen formula [Equation (9)]. Herein, PC was used as an example to derive the total heat release Q_{\max} and the time t_{50} to reach 50% of Q_{\max} . The fitting curve in Figure 6 was linearly fitted according to the hydration heat data. The calculation process of other groups was similar to that of PC. The Knudsen formula, Q_{\max} and t_{50} are shown in Table 8. It can be seen from Table 8 that with the increase of MTs content, the Q_{\max} of CCMs gradually decreases, and the time t_{50} gradually prolongs, which is the same as the conclusion of the hydration heat test.

The Q_{\max} can reflect the hydration trend and degree of CCMs to a certain extent. The higher the Q_{\max} value, the higher the hydration degree of CCMs. According to Table 8, the Q_{\max} of SL₁₅ is the largest, followed by MT_{S15}, which is different from the 120 h cumulative heat release obtained by the hydration heat test. The activation effect of MTs may be stronger than that of FA in the later stage, thus leading to its accumulated heat release gradually exceeding that of FA. Compared with FA₁₅ and SL₁₅, the Q_{\max} of MT_{S15} is increased by 4.95% and -3.83%, respectively. This shows that the hydration degree of SL is higher, followed by MTs.

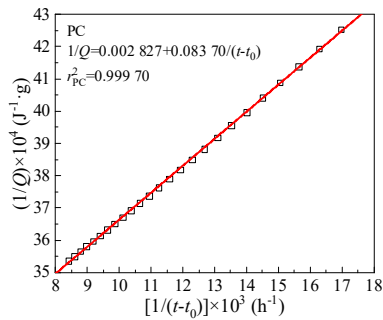


Figure 6. Determination of total heat release Q_{\max} from linear regression

Table 8. Knudsen formulas of CCMs

Sample	Knudsen formula	Q_{\max} (J/g)	t_{50} (h)
PC	$1/Q=0.002\ 827+0.083\ 70/(t-t_0)$	353.73	29.61
MT _{S5}	$1/Q=0.002\ 928+0.089\ 04/(t-t_0)$	341.53	30.41
MT _{S15}	$1/Q=0.002\ 948+0.119\ 85/(t-t_0)$	339.21	40.65
MT _{S25}	$1/Q=0.003\ 033+0.143\ 69/(t-t_0)$	329.71	47.38
MT _{S35}	$1/Q=0.003\ 270+0.165\ 03/(t-t_0)$	305.81	50.47
FA ₁₅	$1/Q=0.003\ 094+0.102\ 27/(t-t_0)$	323.21	33.05
SL ₁₅	$1/Q=0.002\ 835+0.114\ 00/(t-t_0)$	352.73	40.21

4.2. Hydration Kinetic Analysis

The Q_{\max} of CCMs has been calculated according to the Knudsen formula. And the hydration degree (α) and hydration rate (da/dt) required by the Krstulovic-Dabic model can be obtained according to formulas (7) and (8). Taking PC as an example, the kinetic parameters K_1' and n of stage NG can be derived by the formula (1) and linearly fitting the curve of $\ln[-\ln(1-\alpha)]$ vs. $\ln(t-t_0)$, as shown in Figure 7a. The K_2' of stage I and K_3' of stage D can also be derived using the formulas (2) and (3) for linear fitting, respectively, as shown in Figure 7b,c. Substituting the parameters n , K_1' , K_2' and K_3' into formulas (4) - (6), the hydration reaction rate curves of NG, I, and D can be obtained. The hydration reaction rate curves and hydration kinetic parameters of other groups were similar to those of PC.

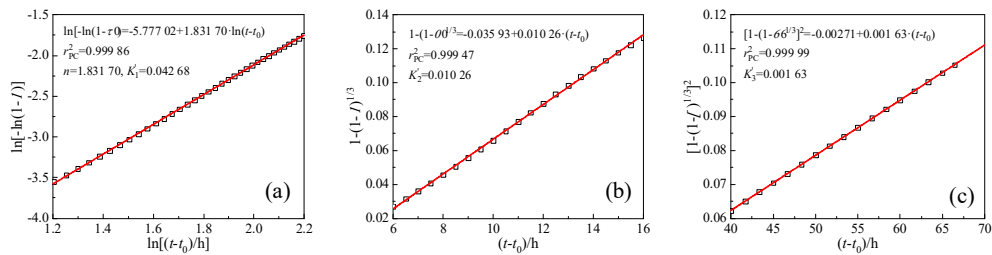


Figure 7. Determination of kinetic parameters n , K_1' , K_2' , K_3' via linear regression

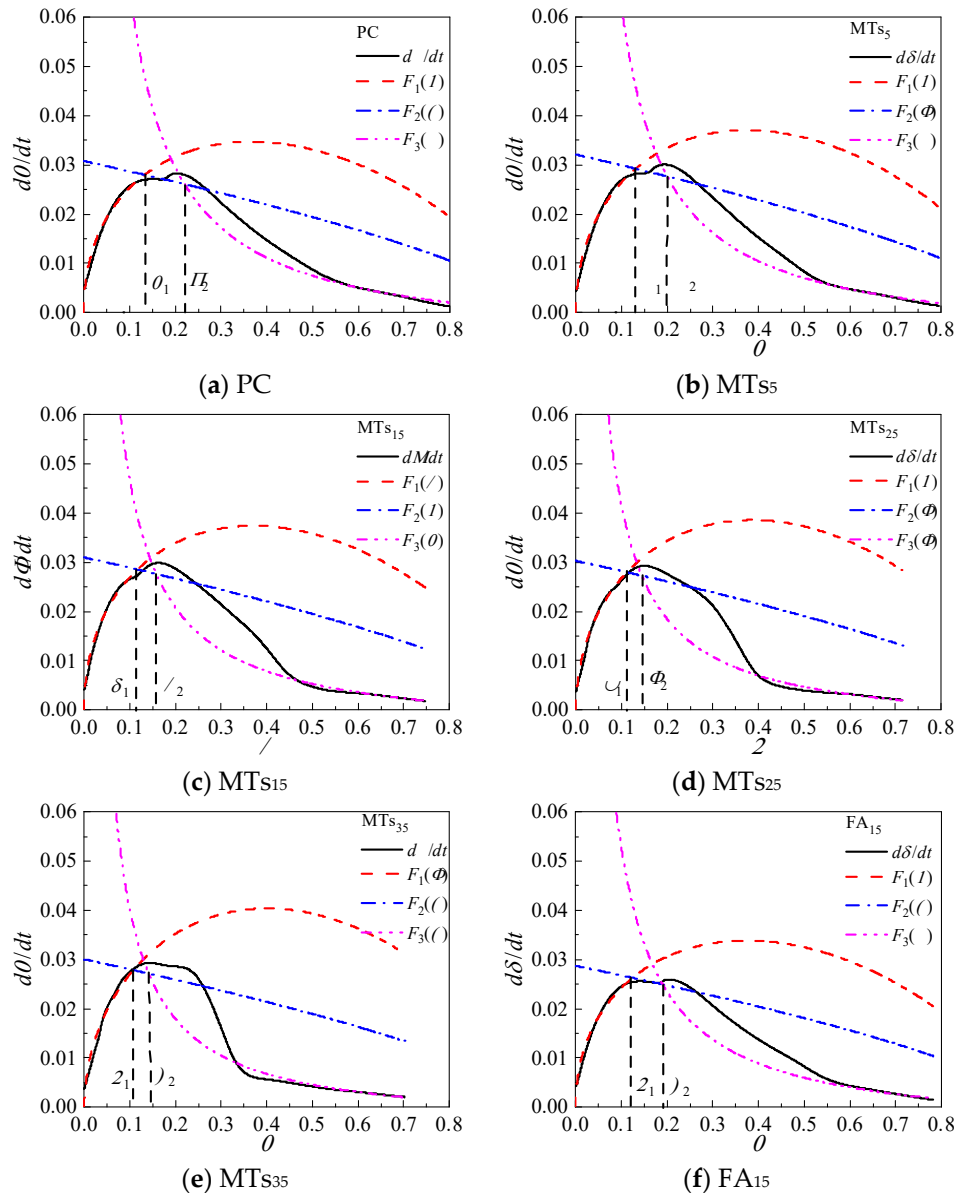
4.2.1. Hydration Process Simulation of CCMs

Based on the Krstulovic-Dabic model, the hydration process is divided into three stages: nucleation and crystal growth (NG), interactions at phase boundaries (I), and diffusion (D). These three stages may take place simultaneously, but the whole development of the hydration process depends on the slowest reaction stage [33,45]. In the early stage of hydration, the CCMs have more water and fewer hydration products, and the ion migration resistance and rate are smaller and faster, respectively, thus the hydration becomes controlled by NG. As the extension of hydration time, the hydration products in the CCMs increase and the structure becomes dense. Therefore, ion migration

resistance is increased and migration rate decreases, and the hydration process is controlled by the I stage and then by the D stage [17].

The relationship between hydration degree α and hydration reaction rate $d\alpha/dt$ of CCMs are shown in Figure 8. The curves of $F_1(\alpha)$ and $F_2(\alpha)$ intersect with $F_3(\alpha)$ at α_1 and α_2 , where α_1 is the transition point from NG process to I process and α_2 is the transition point from I process to D process. This shows that the incorporation of MTs, FA, and SL does not influence the hydration process of CCMs, and the hydration process all undergoes three stages: NG-I-D. The Krstulovic-Dabic model can better simulate the hydration processes NG, I, and D of CCMs, respectively.

According to Figure 8, when the MTs content is not more than 35%, the simulation effect of NG, I and late D stages of the hydration reaction with the hydration rate curve obtained from the hydration heat test is well. When the MTs content is 35%, the simulation effect of NG and late D stages are better, while the simulation effect of the I stage has a large deviation from the reaction rate measured by the experiment. This is because the degree of influence of MTs on the total hydration reaction of CCMs increases with the MTs content, and the deviation of the simulation gradually increases with the MTs content. When the content of MTs, FA, and SL is 15%, the Krstulovic-Dabic model has a better simulation effect on FA, SL, and MTs. However, the simulation effect of the pre-D stage deviates from the actual data due to the weak pozzolanic effect produced by admixture in the late hydration.



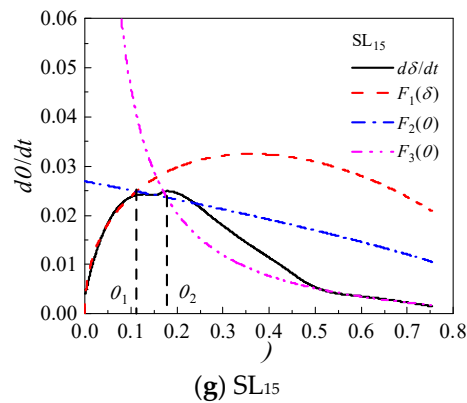


Figure 8. Hydration rate curves for CCMs

4.2.2. Hydration Kinetic Parameters of CCMs

The hydration kinetic parameters of CCMs are presented in Table 9. The reaction order n reflects the crystallization nucleation and crystal production of the hydration products of the CCMs [46]. The greater the n value, the greater the reaction resistance of CCMs [16,47]. The n of the CCMs gradually increases with increasing MTs content. This shows that the introduction of MTs has reached the reaction resistance in the crystallization process of hydration products in CCMs, and the influence of MTs content of 35% is the most obvious [27,29]. When the content of MTs, FA and SL is 15%, the order of n of the CCMs is $FA_{15} > MT_{S15} > SL_{15}$, indicating that MTs, FA, and SL have different influences on the nucleation effect, and the influence of FA is more than MTs and SL on the crystallization process of the hydration products of CCMs.

Table 9. Hydration kinetic parameters of CCMs

Sample	n	K_1'	K_2'	K_3'	α_1	α_2	$\alpha_2 - \alpha_1$
PC	1.831 70	0.042 68	0.010 26	0.001 63	0.133	0.220	0.087
MT _{S5}	1.881 52	0.044 87	0.010 69	0.001 53	0.130	0.199	0.069
MT _{S15}	1.860 04	0.045 61	0.010 32	0.001 15	0.116	0.158	0.042
MT _{S25}	1.949 23	0.045 73	0.010 09	0.001 02	0.111	0.144	0.033
MT _{S35}	2.047 24	0.046 34	0.010 01	0.000 99	0.107	0.141	0.034
FA ₁₅	1.878 14	0.041 04	0.009 57	0.001 30	0.124	0.190	0.066
SL ₁₅	1.810 73	0.040 21	0.008 97	0.001 13	0.111	0.177	0.066

The reaction rate constant K_1' of the NG process gradually increases with increasing MTs content. This is because the incorporation of MTs increases the effective w/c ratio of CCMs, and MTs can be used as a nucleation site to increase the hydration reaction rate. The reaction rate constant K_2' of the I process increases first and then decreases with the increase of MTs content. When the MTs content is small, the addition of MTs disperses the not-hydrated cement particles in the paste, causing the contact area between cement and water to increase, and the degree of hydration also increases, thereby improving the reaction rate. When the MTs content is high, the cement content decreases and the concentration of Ca^{2+} in CCMs decreases, which delays the time for $Ca(OH)_2$ crystals to reach saturation, resulting in the hydration reaction rate decreasing. The reaction rate constant K_3' of the D process gradually decreases with the increase of the MTs content. This is because the hydration products in the paste increase in the later stage of hydration. Furthermore, the filling effect of MTs fills the pores and the pozzolanic effect of MTs promotes the generation of hydration products, making the structure denser, resulting in greater ion migration resistance, and the hydration reaction rate reduces. When the content of MTs, FA and SL is 15%, the K_1' and K_2' parameters of MT_{S15} are greater than those of FA₁₅ and SL₁₅. This indicates that the reaction rate of crystallization nucleation and phase boundary reaction of hydration products of paste with MTs is higher than that of FA and SL, and the hydration heat release rate of the CCMs in the acceleration period is larger. The K_3' of

MTs₁₅ is smaller than that of FA and larger than that of SL, indicating that the reaction rate of MTs in the diffusion process is lower than that of FA but higher than that of SL.

The hydration degree α_1 gradually decreases with the increasing MTs content, indicating that MTs shortens the NG process of CCMs, and the higher the amount of MTs, the more obvious the shortening. This is because the incorporation of MTs accelerates the hydration rate and shortens the time for crystal nucleation and crystal growth, resulting in a shortened NG process. The α_2 - α_1 gradually decreases as the MTs content increases, indicating that the MTs shortens the I process of CCMs. When the content of MTs, FA and SL is 15%, the α_1 of MTs₁₅ is less than that of FA₁₅ and greater than that of SL₁₅. The difference of α_1 indicates that mineral admixtures have different influences on the NG process, and the influence effect of SL is greatest. The α_2 and α_2 - α_1 parameters of MTs₁₅ are smaller than those of FA₁₅ and SL₁₅, indicating that the incorporation of admixtures all shortens the I process, and the influence effect of MTs on the I process is greatest.

5. Conclusions

- (1) The incorporation of MTs prolongs the end time of the induction period (t_0 increases) and shortens the acceleration period of CCMs (t_1 - t_0 shortens). When the content of MTs is not more than 15%, the second exothermic peak of CCMs appears earlier and the peak heat release value increases. When the content of MTs exceeds 15%, the second exothermic peak of CCMs appears later and the peak heat release value decreases. The cumulative heat release of CCMs gradually decreases with increasing MTs content, but the relative percentage of hydration heat is greater than the mass fraction of cement in the paste.
- (2) When the content of MTs, FA, and SL is 15%, compared with FA and SL, the influence of MTs on the extension of the end time of the induction period of CCMs is most significant, and the second exothermic peak of CCMs with MTs is advanced and its peak heat release increases. When the hydration time is 120 h, the cumulative heat release of FA and SL is greater than that of MTs. Based on the final cumulative heat release calculated by the Knudsen formula, the final cumulative heat release of MTs exceeds that of FA. Compared with FA₁₅ and SL₁₅, the Q_{max} of MTs₁₅ is increased by 4.95% and -3.83%, respectively;
- (3) The hydration process of CCMs undergoes three stages: nucleation and crystal growth (NG) - interactions at phase boundaries (I) - diffusion (D), and the relationship curve between hydration degree and hydration reaction rate calculated based on the Krstulovic-Dabic model can better simulate the hydration reaction rate curve measured by hydration heat test. With the increase of MTs content, the reaction order n and K_1' of CCMs increase, K_2' increases first and then decreases, and K_3' , α_1 , and α_2 decrease. The incorporation of MTs shortens the NG and I process of CCMs.

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