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Brief Report

Parameterization of Quantum Interactions

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Abstract: *Background:* Previous papers have developed a statistical mechanics of neocortical interactions (SMNI) fit to short-term memory and EEG data (Ingber, 2018). Adaptive Simulated Annealing (ASA) was used for all fits to data. A numerical path-integral for quantum systems, qPATHINT, was used. *Objective:* The quantum path-integral for Calcium ions was used to derive a closed-form analytic solution at arbitrary time. The quantum effects is parameterized here, whereas the previous 2018 paper applied a nominal ratio of 1/2 to these effects. *Method:* Methods of mathematical-physics for optimization and for path integrals in classical and quantum spaces are used. The quantum path-integral is used to derive a closed-form analytic solution at arbitrary time, and is used to calculate interactions with classical-physics SMNI interactions among scales. *Results:* The mathematical-physics and computer parts of the study are successful, in that three cases with Subjects (blind to this author) after 1,000,000 visits to the cost function gave: Subject-07 = 0.04, Subject-08 = 0.55, and Subject-09 = 1.00. All other 9 Subjects gave 0.

Keywords: path integral; quantum systems; multiscale modeling; supercomputer

1. Introduction

This project calculates quantum Ca^{2+} using EEG for data. Only specific calcium ions Ca^{2+} are considered, those arising from regenerative calcium waves generated at tripartite neuron-astrocyte-neuron synapses.

This project is speculative, but it is testable, e.g., by fitting EEG.

SMNI has been developed since 1981. This evolving model including ionic scales have been published since 2012. Quantum physics calculations also support these extended SMNI models.

2. Statistical Mechanics of Neocortical Interactions (SMNI)

SMNI has been developed since 1981, scaling aggregate synaptic interactions to neuronal firings, up to minicolumnar-macrocolumnar columns of neurons to mesocolumnar dynamics, up to columns of neuronal firings, up to regional macroscopic sites (Ingber, 1981; Ingber, 1982; Ingber, 1983; Ingber, 1984; Ingber, 1985; Ingber, 1994).

SMNI has calculated agreement/fits with experimental data from various aspects of neocortical interactions, e.g., properties of short-term memory (STM) (Ingber, 2012a), including its capacity (auditory 7 ± 2 and visual 4 ± 2) (Ericsson & Chase, 1982; Zhang & Simon, 1985), duration, stability, primacy versus recency rule, Hick's law (Hick, 1952; Jensen, 1987; Ingber, 1999), and interactions within macrocolumns calculating mental rotation of images (Ingber, 1982; Ingber, 1983; Ingber, 1984; Ingber, 1985; Ingber, 1994). SMNI has scaled mesocolumns across neocortical regions to fit EEG data (Ingber, 1997b; Ingber, 1997a; Ingber, 2012a).

Recent work in SMNI includes explicitly showing how neural-networks can be improved by adding SMNI nonlinearities (Ingber, 2022).

2.1. Synaptic Interactions

The short-time conditional probability distribution of firing of a given neuron firing given just-previous firings of other neurons is calculated from chemical and electrical intra-neuronal interactions (Ingber, 1982; Ingber, 1983). With previous interactions with k neurons within τ_j of 5–10 msec, the conditional probability that neuron j fires ($\sigma_j = +1$) or does not fire ($\sigma_j = -1$) is

$$p_{\sigma_j} = \Gamma \cdot \Psi = \frac{\exp(-\sigma_j \cdot F_j)}{\exp(F_j) + \exp(-F_j)}$$

$$F_j = \frac{V_j - \sum_k a_{jk}^* \cdot v_{jk}}{(\pi \cdot \sum_{k'} a_{jk'}^* \cdot (v_{jk'} + \phi_{jk'}))^{1/2}}$$

$$a_{jk} = \frac{1}{2} A_{|jk|} (\sigma_k + 1) + B_{jk}$$

V_j is the depolarization threshold in the somatic-axonal region. v_{jk} is the induced synaptic polarization of E or I type at the axon, and ϕ_{jk} is its variance. The efficacy a_{jk} is a sum of A_{jk} from the connectivity between neurons, activated if the impinging k -neuron fires, and B_{jk} from spontaneous background noise.

2.2. Neuronal Interactions

Aggregation up to the mesoscopic scale from the microscopic synaptic scale uses mesoscopic probability P

$$P = \prod_G P^G [M^G(r; t + \tau) | M^G(r'; t)] = \sum_{\sigma_j} \delta \left(\sum_{j \in E} \sigma_j - M^E(r; t + \tau) \right) \cdot \delta \left(\sum_{j \in I} \sigma_j - M^I(r; t + \tau) \right) \cdot \prod_j^n p_{\sigma}$$

M represents a mesoscopic scale of columns of N neurons, with subsets E and I , represented by p_{q_i} . The “delta”-functions δ -constraint represents an aggregate of many neurons in a column. G is used to represent excitatory (E) and inhibitory (I) contributions. G designates contributions from both E and I .

The path integral is derived in terms of mesoscopic Lagrangian L . The short-time distribution of firings in a minicolumn, given its just previous interactions with all other neurons in its macrocolumn is thereby defined.

2.3. Columnar Interactions

In the prepoint (Ito) representation the SMNI Lagrangian L is

$$L = \frac{\sum_{GG'} (2N)^{-1} (M^G - g^G) G_{GG'} (M^{G'} - g^{G'})}{2N\tau} - V'$$

$$g^G = -\tau^{-1} (M^G + N^G \cdot \tanh F^G)$$

$$g^{GG'} = (g_{GG'})^{-1} = \delta_G^{G'} \tau^{-1} N^G \sec h^2 F^G$$

$$g = \det (g_{GG'})$$

2.4. SMNI Parameters From Experiments

Values of parameters and their bounds are taken from experimental data, not fit to specific phenomena.

$N^G = \{N^E = 160, N^I = 60\}$ was set for visual neocortex, $\{N^E = 80, N^I = 30\}$ was set for all other neocortical regions, M^G and N^G in \tilde{F}^G are afferent macrocolumnar firings scaled to efferent minicolumnar firings by $N/N^* \approx 10^{-3}$. N^* is the number of neurons in a macrocolumn, about 10^5 . V' includes nearest-neighbor mesocolumnar interactions. τ is usually considered to be on the order of 5–10 ms. $V^G = 10$ mV, $v^G = 0.1$ mV, $\phi^G = 0.03^{1/2}$ mV.

Nearest-neighbor interactions among columns give dispersion relations consistent with speeds of mental visual rotation (Ingber, 1982; Ingber, 1983).

The wave equation cited by EEG theorists, permitting fits of SMNI to EEG data (Ingber, 1995), is derived using the variational principle applied to the SMNI Lagrangian. This creates an audit trail from synaptic parameters to the averaged regional Lagrangian.

Basic SMNI Model

Consistent with experimental evidence of shifts in background synaptic activity under conditions of selective attention (Mountcastle *et al*, 1981; Briggs *et al*, 2013), a Centering Mechanism (CM) on case BC, giving BC', where the numerator of F^G only has terms proportional to $M^{E'}$, $M^{I'}$ and $M^{\ddagger E'}$, i.e., zeroing other constant terms by resetting the background parameters B^G , still within experimental ranges. This brings in a maximum number of minima into the physical firing M^G -space, due to the minima of the new numerator in being in a parabolic trough defined by

$$A_E^E \cdot M^E - A_I^E \cdot M^I = 0$$

about which nonlinearities develop multiple minima identified with STM phenomena.

A Dynamic CM (DCM) model is used, resetting B^G every few epochs of τ . Such changes in background

synaptic activity on such time scales are seen during attentional tasks (Briggs *et al*, 2013).

2.5. Comparing EEG Testing Data with Training Data

EEG data was used from <http://physionet.nlm.nih.gov/pn4/erpbc1> (Goldberger *et al*, 2000; Citi *et al*, 2010), SMNI was again fit to highly synchronous waves (P300) during attentional tasks, for each of 12 subjects (Ingber, 2016b). The electric potential Φ is experimentally measured by EEG, but both are due to the same currents \mathbf{I} . \mathbf{A} is linearly proportional to Φ with a scaling factor included as a parameter in fits to data. Additional parameterization of background synaptic parameters, B^G and $B^{\ddagger E}$, modify previouswork.

2.5.1. Canonical Momentum $\Pi = \mathbf{p} + q\mathbf{A}$

In the Feynman (midpoint) representation of the path integral, the canonical momentum, Π , defines the dynamics of a moving particle with momentum \mathbf{p} in an electromagnetic field. In SI units,

$$\Pi = \mathbf{p} + q\mathbf{A}$$

where $q = -2e$ for Ca^{2+} , e is the magnitude of the charge of an electron = 1.6×10^{-19} C (Coulomb), and

\mathbf{A} is the electromagnetic vector potential. \mathbf{A} represents three components of a 4-vector.

2.5.2. Vector Potential of Wire

A columnar firing state is modeled as a wire/neuron with current \mathbf{I} measured in $\mathbf{A} = \text{Amperes} = \text{C/s}$,

$$A(t) = \frac{\mu}{4\pi} \int \frac{dr}{r}$$

along a length z observed from a perpendicular distance r from a line of thickness r_0 . If far-field retardation effects are neglected, this yields

$$A = \frac{\mu}{4\pi} \cdot \log\left(\frac{r}{r_0}\right)$$

where μ is the magnetic permeability in vacuum = $4\pi \cdot 10^{-7}$ H/m (Henry/meter).

\mathbf{A} includes minicolumnar lines of current from hundreds to thousands of macrocolumns, within a region not so large to include many convolutions, but still contributing to large synchronous bursts of EEG.

Electric \mathbf{E} and magnetic \mathbf{B} fields, derivatives of \mathbf{A} with respect to r , do not possess this logarithmic insensitivity to distance, and they do not linearly accumulate strength within and across macrocolumns.

Estimates of contributions from synchronous firings to P300 measured on the scalp are tens of thousands of macrocolumns spanning 100 to 100's of cm^2 . Electric fields generated from a minicolumn may fall by half within 5–10 mm, the range of several macrocolumns.

2.5.3. Reasonable Estimates

Classical physics calculates $q\mathbf{A}$ from macroscopic EEG to be on the order of 10^{-28} kg-m/s, while the momentum \mathbf{p} of a Ca^{2+} ion is on the order of 10^{-30} kg-m/s. This numerical comparison includes the influence of \mathbf{A} on \mathbf{p} at classical scales.

Direct calculations in both classical and quantum physics show ionic calcium momentum-wave effects neuron-astrocyte-neuron tripartite synapses modify background SMNI parameters and create feedback between ionic/quantum and macroscopic scales (Ingber, 2012a; Ingber, 2012b; Nunez *et al*, 2013; Ingber *et al*, 2014; Ingber, 2015; Ingber, 2016b; Ingber, 2017a).

2.6. PATHINT/qPATHINT Code

qPATHINT is an N-dimensional code which calculates the propagation of quantum variables in the presence of shocks. Applications have been made to SMNI and Statistical Mechanics of Financial Markets (SMFM) (Ingber, 2017a; Ingber, 2017b; Ingber, 2017c).

The PATHINT C code of 7500 lines of code using the GCC C-compiler was rewritten to use double complex variables instead of double variables, developed for arbitrary N dimensions, creating qPATHINT (Ingber, 2016a; Ingber, 2017a; Ingber, 2017b).

3. Results Including Quantum Scales

The wave function ψ_e describing the interaction of \mathbf{A} with \mathbf{p} of Ca^{2+} wave packets was derived in closed form from the Feynman representation of the path integral using path-integral techniques (Schulten, 1999), modified to include \mathbf{A} .

\mathbf{p} of the Ca^{2+} wave packet and $q\mathbf{A}$ of the EEG field make about equal contributions to Π (Ingber, 2015).

3.1. SMNI + Ca^{2+} wave-packet

Tripartite influences on synaptic B^G , is measured by the ratio of packet's $\langle \mathbf{p}(t) \rangle_{\psi^* \psi}$ to $\langle \mathbf{p}_0(t_0) \rangle_{\psi^* \psi}$, at the onset of each attentional task. Here $\langle \rangle_{\psi^* \psi}$ is taken over $\psi^* \psi_e$. \mathbf{A} changes slower than \mathbf{p} , and the static approximation of \mathbf{A} used to derive ψ_e and $\langle \mathbf{p} \rangle_{\psi^* \psi}$ is use within P300 EEG epochs, resetting $t = 0$ at the onset of each classical EEG measurement (1.953 ms apart), using the current \mathbf{A} .

3.2. Supercomputer Resources

1000 hours of supercomputer CPUs are required for an ASA fit of SMNI to the same EEG data used previously, i.e., from <http://physionet.nlm.nih.gov/pn4/erpbci> (Goldberger *et al*, 2000; Citi *et al*, 2010), using mostly the same codes used previously (Ingber, 2016b).

3.3. Results Using $\langle \mathbf{p} \rangle_{\psi^* \psi}$

$\langle \mathbf{p} \rangle_{\psi^* \psi}$ was used in classical-physics SMNI fits to EEG data using ASA. Runs using 1M or 100K generated states gave results not much different. The current calculations use one additional parameter across all EEG regions to weight the contribution to synaptic background B^G . \mathbf{A} is taken to be proportional to the currents measured by EEG, i.e., firings M^G . Otherwise, the “zero-fit-parameter” SMNI philosophy was enforced, wherein parameters are picked from experimentally determined values or within experimentally determined ranges (Ingber, 1984).

As with previous studies using this data, results sometimes give Testing cost functions less than the Training cost functions. This is due to differences in data, likely from differences in subjects' contexts, e.g., possibly due to subjects' STM strategies. Further tests of these multiple-scale models with more EEG data are required, and with the PATHINT-qPATHINT coupled algorithm described previously.

4. Results

The mathematical-physics and computer parts of the study are successful, in that three cases with Subjects (blind to this author) after 1,000,000 visits to the cost function gave: Subject-07 = 0.04, Subject-08 = 0.55, and Subject-09 = 1.00. All other 9 Subjects gave 0.

5. Conclusion

The SMNI model demonstrates can be very well fit to experimental data, e.g., EEG recordings under STM experimental paradigms. qPATHINT permits an inclusion of quantum scales in the multiple-scale SMNI model, by evolving Ca^{2+} wave-packets with momentum \mathbf{p} , including serial shocks, interacting with the magnetic vector potential \mathbf{A} derived from EEG data, marching forward in time with experimental EEG data.

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