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## Article

# A Multi-Layer Neural Network Model “SR-KS” of Human Activity Recognition for the Problem of Similar Human Activity

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**Abstract:** Sensor-based human activity recognition is now well developed, but there are still many challenges, such as insufficient accuracy in recognising similar activities. In response to this question, We mainly collected data related to three-axis acceleration as well as gyroscope, based on these data we developed a model capable of classifying activities similar to human behavior and evaluated the effectiveness and generalization capabilities of this model. The data underwent initial preprocessing, including standardization and normalization. Additionally, recognizing the inherent similarities between human activity behaviors, we introduced a multi-layer classifier model. The first layer is a random forest model based on stepwise regression, which may encounter reduced accuracy for similar activities. The second layer employs a Support Vector Machine (SVM) model based on Kernel Fisher Discriminant Analysis (KFDA). KFDA is used to reduce the dimensionality of data points with potential confusion, followed by SVM for classification. The model was experimentally evaluated and applied to four benchmark datasets: UCI DSA, UCI HAR, WISDM, and IM-WSHA. The experimental results demonstrate that our approach achieved recognition accuracies of 99.71%, 98.71%, 99.12%, and 97.6% on these datasets than the best model respectively 0.75%, 0.34%, 0.11% and 6.15%, indicating excellent recognition performance. Furthermore, to assess the model's generalization ability, we performed K-fold cross-validation on the random forest model and utilized ROC curves for the SVM classifier. The results indicate that our multi-layer classifier model exhibits robust generalization capabilities.

**Keywords:** body-worn sensors; multi layer classifier; random forest; kernel fisher discriminant analysis; SVM; stepwise regression

## 1. Introduction and Related Work

Human Activity Recognition (HAR) involves identifying various human behaviors through a series of observations of individuals and their surrounding environment [39]. HAR has been generally applied in many fields, such as Security and Surveillance[40], sports and fitness[41], industry and manufacturing[42], autonomous driving[44], and the references therein.

A novel IoT-perceptive human activity recognition (HAR) approach using multihead convolutional attention in [1]. Hand-crafted and deep convolutional neural network features fusion and selection strategy in [2]. In [3], authors consider smart homes environments using Lstm networks. In [4], using A federated learning system with enhanced feature extraction to Human Activity Recognition and using Bi-LSTM network for multimodal continuous human activity

recognition and fall detection [5]. In the field of industry and manufacturing, Utilizing time factor analysis in conjunction with human action recognition for worker operating time [6] and applying deep learning to human activity recognition [7] etc., they rely heavily on HAR technology which improves the accuracy of targeting criminals [8]. In the field of autonomous driving [9], the recognition of human activities will help to develop a suitable autonomous driving system.

Human activity recognition (HAR) methods can be broadly categorized into two main directions: 1) vision-based HAR and 2) wearable sensor-based HAR. It is well-known that vision-based HAR is generally considered more advanced compared to wearable sensor-based HAR [10]. but, vision-based HAR also faces several challenges. For one thing, there are privacy concerns related to the potential leakage of video data, and image processing demands significant computational power and substantial storage resources. For another, factors such as the observer's position and angle, the subject's physique, attire, background color, and light intensity can all impact the accuracy of vision-based HAR [11]. In contrast, inertial sensor technology is typically cost-effective and offers greater robustness and portability in various environmental conditions [12]. Currently, sensor-based recognition technology has gained widespread attention due to its superior confidentiality and relatively lower computational requirements. Therefore, in [13], the authors discussed the role of sensor placement in the design of HAR systems to optimize their availability. Leveraging these advantages, wearable sensor-based HAR has garnered increasing interest in recent years.

In recent years, wearable sensor-based HAR has gained widespread attention. The earliest research on sensor-based recognition of human behavior can be traced back to the 1990s, with studies by researchers such as F. Foerster [21] and O. X. Schlmilch [22]. Nowadays, wearable sensor research has yielded many high-accuracy models. For example, Bao and his team achieved an overall accuracy of 84% through effective data collection and decision tree classification [23]. The Centinela system developed by D. Lara and colleagues achieved an overall accuracy of 95.7% [24]. However, at the same time, a problem has been identified where single classification models can lead to significant confusion when distinguishing similar activities (such as ascending stairs and descending stairs). In the study by JANSIR et al. [14], they employed chaotic mapping to compress raw tri-axial accelerometer data and extracted 38 time-domain and frequency-domain features, including mean, standard deviation, root mean square, dominant frequency coefficient, spectral energy, and others. They achieved a recognition accuracy of 83.22% in human activity recognition. However, the results showed significant confusion between activities such as running, ascending stairs and descending stairs. In the research by VANRELLS et al. [15], they extracted a 91-dimensional feature vector from single-axis accelerometer data, including cepstral coefficients, time-domain features, and periodicity features. They achieved a recognition accuracy of 91.21% in a classification task involving ten different human activities. However, the results also indicated substantial confusion between activities such as cycling on an exercise bike in horizontal, cycling on an exercise bike in vertical positions, ascending stairs and descending stairs. The reasons for the confusion between similar activities can be summarized in two aspects. Firstly, within the same individual, different activities may share similar activity cycles or amplitudes, leading to activity recognition confusion and a decrease in overall accuracy.

Kernel Fisher Discriminant Analysis (KFDA) is a powerful extension of Fisher Discriminant Analysis (FDA) [45] that has proven to be highly effective in various pattern recognition and classification tasks. While traditional FDA is primarily designed for linearly separable data, KFDA extends its capabilities by allowing the analysis of nonlinearly separable data through the use of kernel functions. It serves as a robust nonlinear classifier suitable for tackling pattern recognition, classification, and regression analysis tasks [46]. The KFDA method is capable of reflecting the nonlinear relationships between the input and output variables of the dataset, and shows good generalisation performance in many practical problems.

We have noticed the success of Shaoqun Dong and colleagues [43] in addressing similar Lithofacies identification problems, and we also intend to employ kernel Fisher discriminant analysis to preprocess similar issues before proceeding with data classification. Nowadays, there are

numerous applications of kernel Fisher discriminant analysis in the field of machine learning as well. For instance, Liu et al. [47] have used this technique to enhance tasks like face recognition.

To address the issue of confusion between similar activities in single-model human activity recognition and enhance the overall recognition accuracy of multi-class activities, we drew inspiration from the success of Shaoqun Dong [43] and others in solving similar Lithofacies identification problems. We decided to leverage KFDA to preprocess the similar activity data before performing classification. In this paper, we propose a multi-layer neural network model based on Kernel Fisher Discriminant Analysis. This approach comprises preprocessing steps, followed by initial classification using Random Forest. Subsequently, KFDA is applied to process the data. Finally, SVM are employed for detailed classification of ambiguous actions. The end result is a robust neural network classification model that effectively addresses the challenge of distinguishing similar activities.

Therefore, the main contributions of this paper can be summed up as follows:

- 1) We propose a model design aimed at addressing the issue of confusion between similar activities.
- 2) To tackle the problem of similar activity feature similarity, we introduce an SVM neural network classification approach based on Kernel Fisher Discriminant Analysis, which effectively classifies similar activities.
- 3) Additionally, we conducted classification experiments on four common benchmark datasets and performed detailed analyses on these datasets. We compared our model with mainstream classification models. Experimental results demonstrate that our model exhibits excellent classification performance.

The remaining sections of this paper are organized as follows. Section II provides a brief introduction to the work carried out in this paper, along with details about the dataset used. Section III conducts a basic data analysis and employs appropriate data preprocessing techniques. Section IV introduces our proposed human motion approach based on a multi-layer classifier. Section V presents the experimental setup, provides results for our proposed method on multiple datasets, and offers an analysis and discussion of these results. Finally, in Section VI, we summarize the insights gathered from these experiments and outline future directions.

## 2. Word

In the field of HAR research, various datasets have been previously published. Notable among them is the UCI (University of California, Irvine) HAR dataset, recognized for its widespread utilization in numerous studies and comparisons [48]. Additionally, the WISDM (Wireless Sensor Data Mining) dataset [17] is also prominently featured. Furthermore, datasets such as UCI DSA [16] and IM-WSHA [18], which are both accessible through UCI, have been employed. In addition to these, there exist several other datasets that are not individually detailed within this article. Subsequent sections will provide a comparative analysis of the strengths and weaknesses of these three primary datasets, as presented in Table 1.

To highlight these differences, a qualitative comparison between these three datasets is presented in Table 1.

While the data collected from UCI DSA may appear simpler in comparison to WISDM and UCI ADL, UCI HAR captures a wide range of 19 different human activities. Unlike other datasets, it better represents complex human activities and serves as a more comprehensive showcase for our model in this paper. We conducted experiments using the four aforementioned databases, but in the following sections, we focus our narrative on UCI DSA.

**Table 1.** Comparison between datasets: UCI DSA, UCI HAR, WISDM and UCI ADL.

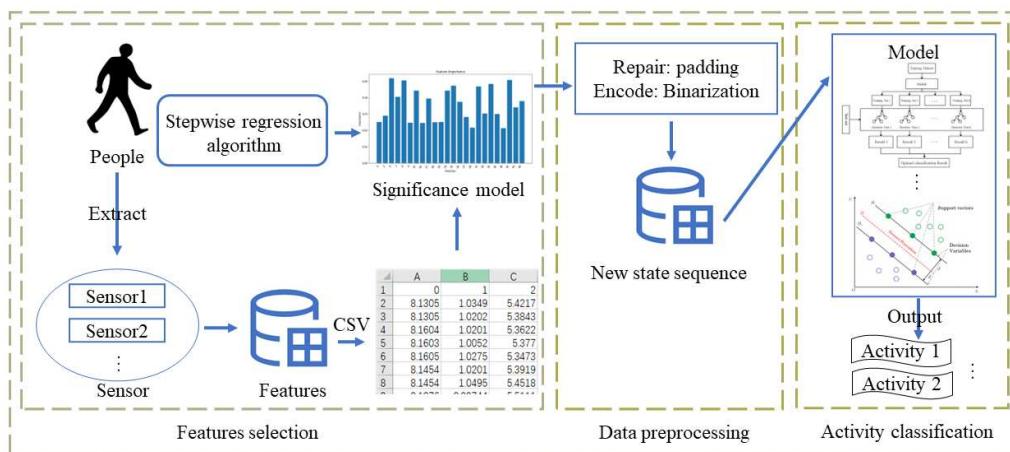
	UCI DSA	UCI HAR	WISDM	IM-WSHA
Type of activity studied	Short-time	Short-time	Short-time	Short-time
Different volunteers	Yes	Yes	Yes	Yes
Volunteers Number	4	30	36	10
Fixed sensor frequency	Yes	Yes	Yes	Yes
Instances	9120	10299	1098207	125955
Sensors	Acc. and gyro.	Acc. and gyro.	Acc	Acc. and gyro.
Sensor data collection	Comprehensively	Comprehensively	Selectively	Selectively
Sensor type	Phone	Phone	Phone	IMU
Sensor number	3	3	1	3
Activities type	19	6	6	11

The UCI DSA data in this paper were obtained from measurements of human activity by miniature inertial sensors and magnetometers in different parts of the body. Sensor data were collected from a total of 8 subjects performing 19 different activities. The total signal duration for each subject for each activity was 5 minutes. The sensor unit was calibrated to acquire data at a 25 Hz sampling frequency. The 5-minute signal was divided into 5-second segments, resulting in 480 (=60 × 8) signal segments for each activity.

A total of eight volunteers participated, resulting in a collection of 9120 instances. This dataset elaborately describes the data captured from various sensors, measuring activities performed by different subjects within the same time intervals. We consolidated this textual dataset into a CSV file comprising two columns: subject ID and activity type.

After data pre-processing, based on the filtered features, our team designed a feasible algorithmic solution to classify 19 human behaviors. Due to the particularly large amount of data and the inherent similarity of human activities, direct classification of the 19 human behaviors using a single machine learning algorithm would easily result in confusion of similar behaviors and lead to degradation of classification accuracy.

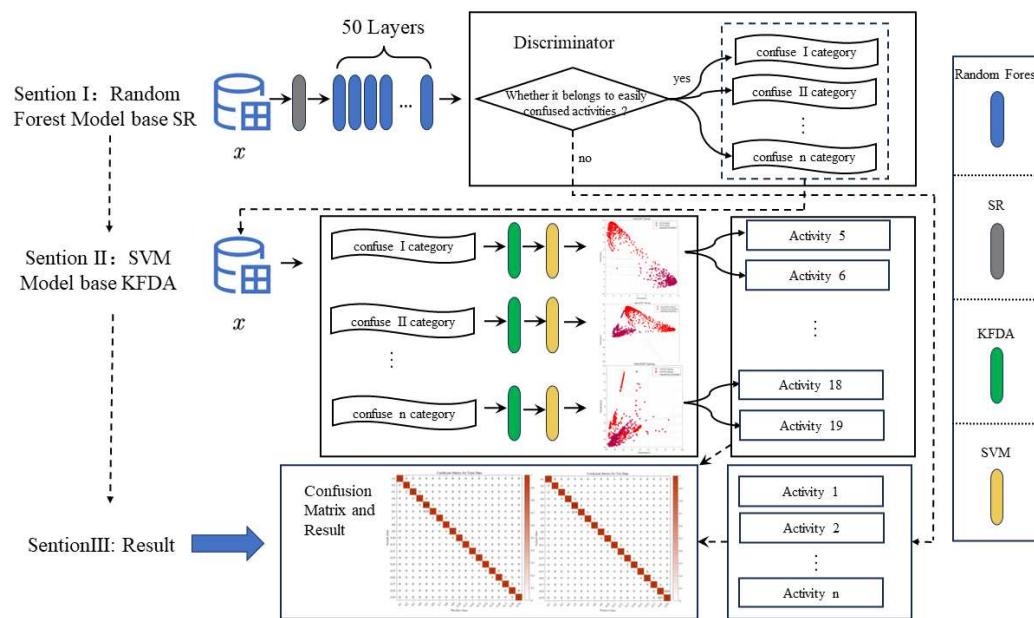
To provide a clearer presentation of our solution, our team utilizes Figure 2.1 and employs a flowchart to illustrate the framework of our approach.

**Figure 1.** Overview of the system workflow.

After data preprocessing and based on the selected features, our team devised a viable algorithmic solution. Initially, all activity data underwent a first-level classification using Random Forest. Subsequently, kernel Fisher discriminant analysis was applied to reduce dimensionality for activities prone to confusion, followed by further fine-grained classification using Support Vector

Machines (SVM). This iterative process continued until no more instances of confounding activities were encountered.

In order to provide a more detailed overview of our efforts in addressing similar activities and how we distinguish other actions within confusing scenarios, we have created the following diagram to illustrate our Model:



**Figure 2.** Model Workflow Diagram.

### 3. Method and data preprocessing

#### 3.1. Intuitive Data Processing

In this section, the preprocessing work, to avoid unnecessary complexity in the article, is illustrated using the UCI DSA dataset as an example. We downloaded the dataset from the official UCI website [16] and found it to be somewhat disorganized. To streamline the dataset, we consolidated the original files into a CSV file. Additionally, to simplify the lengthy labels under the "Behavior" column in the dataset, as discrete information such as IDs and names are not needed for the actual experiments, we adopted an abbreviated format. This processing aligns with the original dataset, for instance, replacing "sitting" with "A1." For detailed information, please refer to Table 2.

**Table 2.** Table of Specific Actions and Corresponding Codes in the Text.

Behavior	Codes	Behavior	Codes
sitting	A1	walking on a treadmill with a speed of 4 km/h (15 deg inclined positions)	A11
standing	A2	running on a treadmill with a speed of 8 km/h	A12
lying on back	A3	exercising on a stepper	A13
lying on right side	A4	exercising on a cross trainer	A14
ascending stairs	A5	cycling on an exercise bike in horizontal	A15
descending stairs	A6	cycling on an exercise bike in vertical positions	A16
standing in an elevator still	A7	rowing	A17

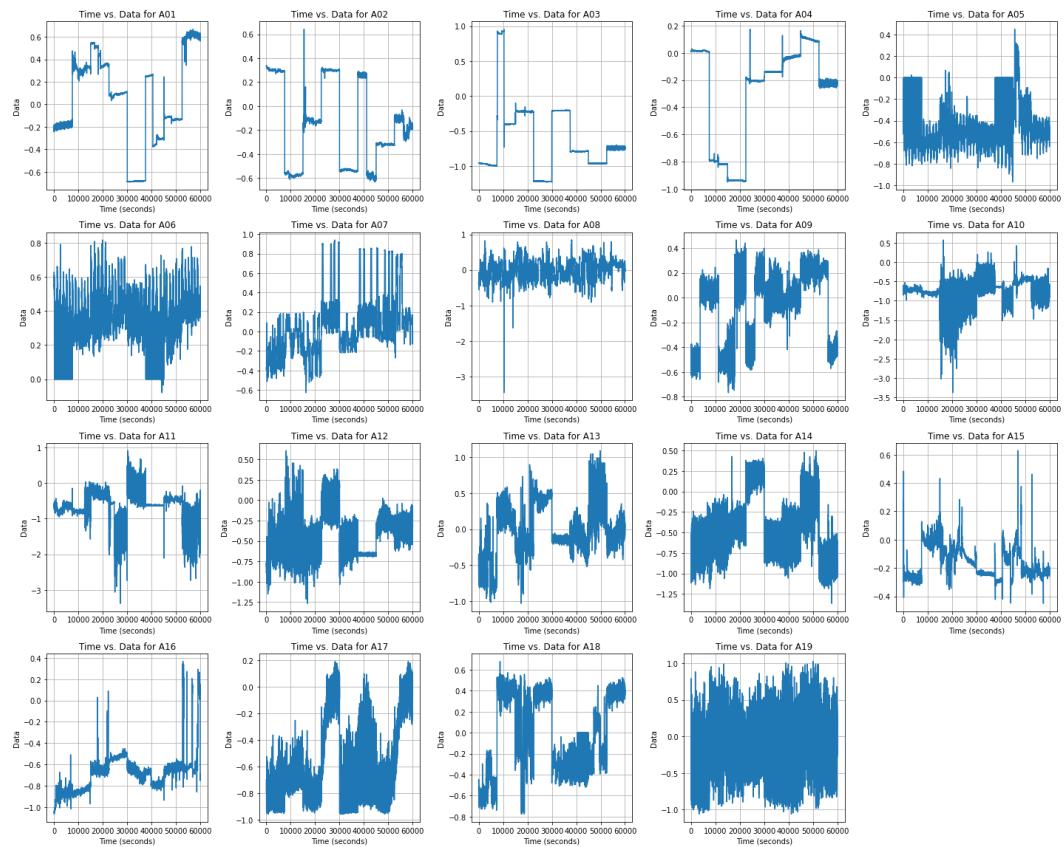
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moving around in an elevator	A8	jumping	A18
walking in a parking lot	A9	playing basketball	A19
walking on a treadmill with a speed of 4 km/h (in flat)	A10		

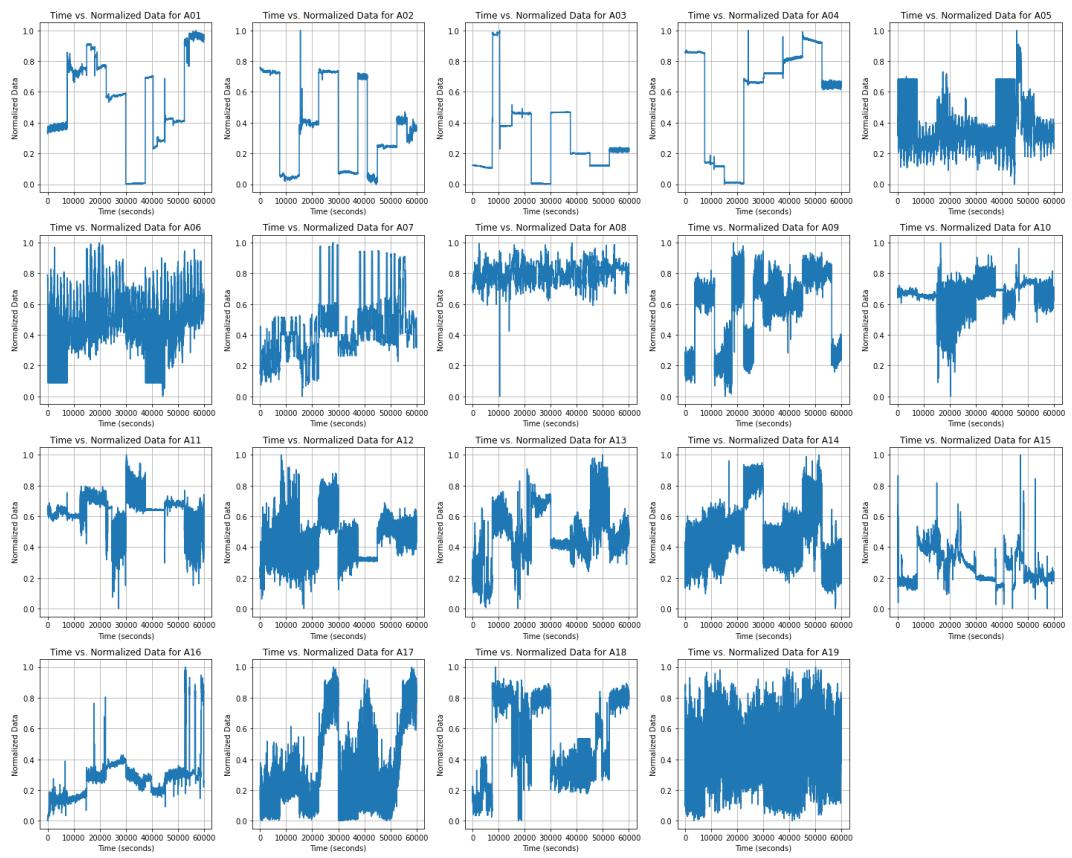
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### 3.2. Standardisation and normalisation

we examined the data samples by randomly selecting a metric and presenting it alongside 19 different activities. As shown below, we preprocessed the data through standardization and normalization methods. In Figure 3(a), the original data for this metric, comprising 60,000 sample points across various activities, is displayed. After our preprocessing, as depicted in Figure 3(b), it is evident that all data now falls within the range of 0 to 1, while preserving the fundamental characteristics of the data.



(a) Original data



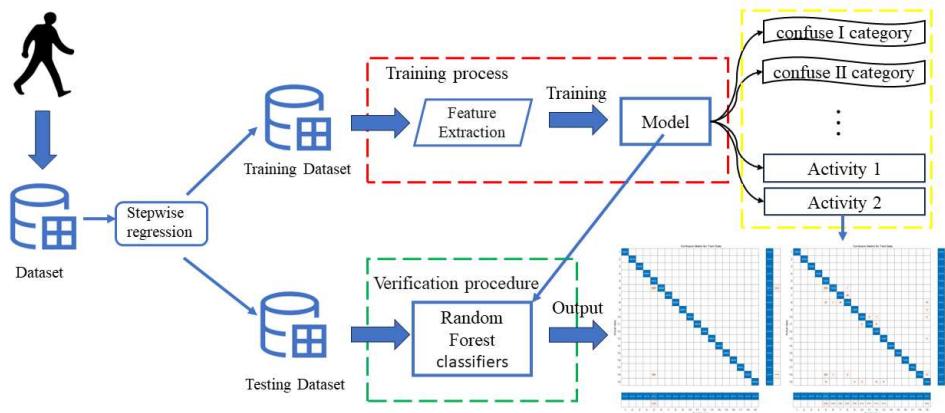
(b) The data after preprocessing

Figure 3. Pre- and post-data pre-processed to correspond to 19 human activities.

#### 4.1. Random Forest initial classification model base on stepwise regression

Firstly, the SR-Random Forest model is proposed by combining the stepwise regression analysis with the Random Forest model. Then, the KFDA-SVM Model is proposed by combining the kernel Fisher discriminant analysis with SVM. In this section, firstly, the stepwise regression algorithm and the Random Forest Model are introduced and the SR-Random Forest Model is proposed, and furthermore, the kernel Fisher discriminant analysis model and SVM model and gives their combined model.

In order to obtain a higher initial classification accuracy for subsequent improvement in the second classification stage. In [58], it is mentioned that the use of feature selection algorithms will be able to effectively improve the efficiency of machine learning, so we first extract the relevant metrics using stepwise regression to calculate the importance of the input metrics. Random forest is an ensemble classifier that uses multiple decision trees to train samples and make predictions. In this section, the SR -RF model is shown in Figure 4.



**Figure 4.** Presentation of the Random Forest Model base on Stepwise regression algorithm Workflow.

#### 4.1.1. Stepwise regression algorithm

Stepwise regression analysis algorithms can be traced back to the 19th century statistician and mathematician Francis Galton, however, the formal development and promotion of stepwise regression can be traced back to the 20th century statisticians and mathematicians, especially R. A. Fisher. In this paper, we use stepwise regression analysis to analyse the 45 indicators in the UCI DSA ( $g_1, g_2, \dots, g_{45}$ ) rows of stepwise regressions. analyses, and we also chose a variable  $y$  as the response variable. It is assumed that the indicators satisfy equation (1):

$$y = \alpha_0 + \alpha_1 g_1 + \alpha_2 g_2 + \dots + \varepsilon, \quad (1)$$

Assuming that there is a linear relationship between  $g_1$  and  $g_2$ ,  $g_2 = ag_1 + b + v$ , and substituting it into equation (1), we get

$$y = \alpha_0 + b\alpha_2 + (\alpha_1 + a\alpha_2)g_1 + \dots + \varepsilon + \alpha_2 v, \quad (2)$$

Suppose that Eq:

$$y = \beta_0 + \beta_1 g_1 + \dots + \mu. \quad (3)$$

The estimation of model (3) is

$$\hat{\beta}_0 = \hat{\alpha}_0 + b\hat{\alpha}_2,$$

$$\hat{\beta}_1 = \hat{\alpha}_1 + a\hat{\alpha}_2,$$

The sum of squared residuals for model (3) is

$$\begin{aligned} Q_3 &= \sum_{i=1}^n [y_i - (\hat{\beta}_0 + \hat{\beta}_1 x_{i1} + \dots)]^2 \\ &= \sum_{i=1}^n [y_i - (\hat{\alpha}_0 + b\hat{\alpha}_2 + (\hat{\alpha}_1 + a\hat{\alpha}_2)x_{it} + \dots)]^2, \end{aligned} \quad (4)$$

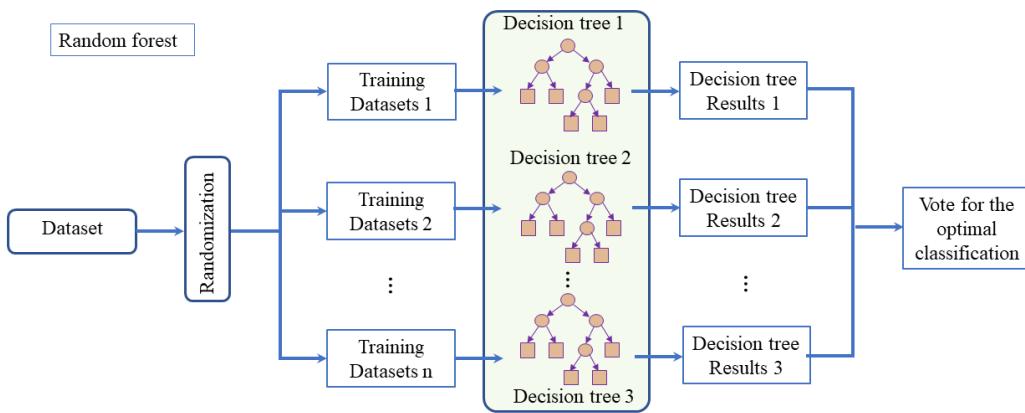
The sum of squared residuals for model (1) is

$$\begin{aligned} Q_1 &= \sum_{i=1}^n [y_i - (\hat{\beta}_0 + \hat{\beta}_1 x_{i1} + \hat{\beta}_2 x_{i2} + \dots)]^2 \\ &= \sum_{i=1}^n [y_i - (\hat{\beta}_0 + b\hat{\beta}_2 + (\hat{\beta}_1 + a\hat{\beta}_2)x_{i1} + v_i\hat{\beta}_2 + \dots)]^2. \end{aligned} \quad (5)$$

Comparing  $Q_1$  and  $Q_3$ ,  $Q_1 - Q_3 \approx 0$ , it is possible to eliminate  $g_1$ . The stepwise regression method can effectively reduce the number of features in the data, improving the fitting performance of the model.

#### 4.1.1. Stepwise regression algorithm

The main features that can classify human behavior have been extracted in the above steps. Considering the relationship between these data and the fact that the samples used for training are discrete and the amount of data is huge, the random forest algorithm is considered for network training, and its general algorithmic flow is shown in Figure 5. In order to initially identify multi-class activities, the random forest classification algorithm with excellent performance in supervised learning is chosen for the layer 1 classifier.



**Figure 5.** Random forest algorithm flow chart.

#### 4.1.2. Random forest base on Stepwise regression algorithm

Random Forest is a composite classification model composed of many decision tree classification models  $\{h(X, \Theta_k), k = 1, \dots\}$ , and the parameter set  $\{\Theta_k\}$  is a collection of independently and identically distributed random vectors. Under the given independent variables  $X$ , each decision tree classification model selects the optimal classification result through a majority vote. The basic idea is to first use bootstrap sampling to extract  $k$  samples from the original training set, with each sample having the same sample size as the original training set. Then,  $k$  decision tree models are built for the  $k$  samples, resulting in  $k$  different classification results. Finally, based on these  $k$  classification results, a majority vote is used to determine the final classification result for each record.

The final classification decision in a random forest is made by training through  $k$  rounds, obtaining a sequence of classification models  $\{h_1(X), h_2(X), \dots, h_k(X)\}$ , and using them to create a multi-classification model system. The ultimate classification result of this system is determined using a simple majority voting method:

$$H(x) = \arg \max_Y \sum_{i=1}^k I(h_i(x) = Y), \quad (6)$$

where,  $H(x)$  is a multi-classification model,  $h_i$  is an individual decision tree classification model, and  $Y$  represents the output variable.

The specific implementation of the above ideas, as illustrated in Algorithm 1, combines stepwise regression and random forest modeling to create a novel classification model. Its advantage lies in the ability to select features from the classification dataset effectively.

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**Algorithm 1:** Random Forest Model base on Stepwise regression algorithm

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**Input:** Let  $\mathcal{D} = (x_1, y_1), \dots, (x_N, y_N)$  denote the training data, with  $x_i = (x_1, \dots, x_k)$  number of trees  $M > 0$ .

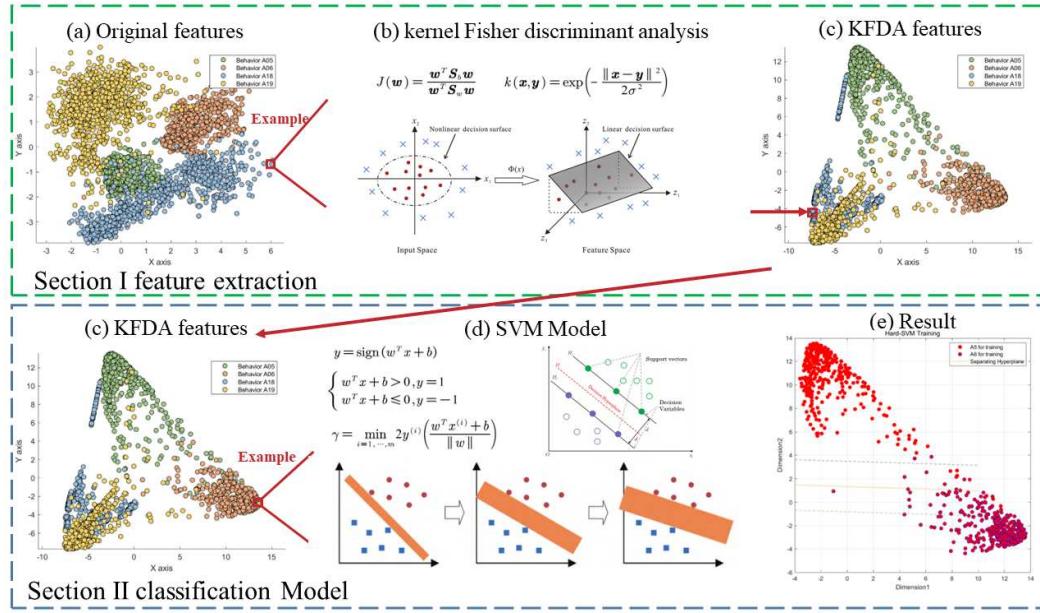
**Output:** Prediction of the random forest at  $x_i$  and random forest Model.

- 1: Construct  $M$  decision trees.
- 2 : **For**  $a = 1, \dots, k$  **do**
- 3 : Step-by-step substitution calculations for each indicator, replacing the old model with the new model if the new model is better.
- 4 : **End**
- 5 : Output  $m$  metrics and replace them with metrics from the  $\mathcal{D}$  dataset.
- 6: Randomly divide  $\mathcal{D}$  into train data  $\mathcal{R}$  and test data  $\mathcal{L}$  in a certain ratio.
- 7: Setting the objective function  $wx^T + b = 0$ , using train data  $\mathcal{R}$  and test data  $\mathcal{L}$ .
- 8 : **For**  $i = 1, \dots, M$  **do**
- 9 : Find Suitable  $w$  and  $b$ , meet:
- 10 :   **For**  $j = 1, \dots, J$  **do**
- 11 :     **if**  $y_j = +1$  **then**
- 12 :        $wx_j + b \geq +1$
- 13 :     **else if**  $y_j = -1$  **then**
- 14 :        $wx_j + b \leq -1$
- 15 :     **End**
- 16 :   **End**
- 17: Adjustment to Test set  $\mathcal{L}$ .
- 18: Getting the optimal  $w, b$ .
- 19 : **For**  $k = 1, \dots, M$  **do**
- 20 :   Train the  $k$ th tree based on the test set and the training set.get  $h_i(x)$ .
- 21 : **End**
- 22 : Classification of new samples is based on grown decision trees, utilizing a majority vote mechanism to determine the final classification result.
- 23 :  $f(x_i) = \text{majority vote } \{h_i(x)\} \quad (i = 1, 2, \dots, k)$ .

---

#### 4.2. Second layer SVM classification Base kernel Fisher discriminant analysis

To address the issue of similarity between two easily confused types of actions, we employed two key steps. First, we utilized KFDA for feature dimensionality reduction, effectively separating similar activities. This step aims to increase the distance between different actions in the data space, thereby facilitating subsequent SVM classification. Let's delve into the principles and workflow of these two steps in more detail. Firstly, we will introduce KFDA, and then we will provide a deeper explanation of SVM. This process's workflow is analogous to the one depicted in Figure 6.



**Figure 6.** SVM model workflow based on kernel Fisher discriminant analysis.

#### 4.2.1. Principle of kernel Fisher discriminant analysis

KFDA is a pattern recognition and classification method based on kernel techniques and is an extension of Fisher Discriminant Analysis. KFDA is designed to handle nonlinearly separable data by mapping the data to a high-dimensional feature space, thereby improving classification performance. We describe KFDA in conjunction with [43] Kernel Fisher Discriminant Analysis (KFDA) was first proposed by Schölkopf et al. in 1997 [52] and can be expressed as the maximisation equation (7):

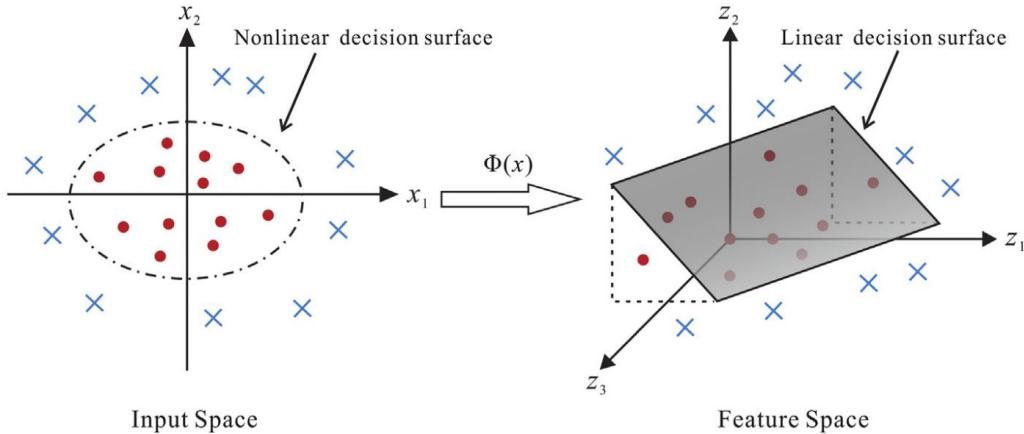
$$J(\mathbf{w}) = \frac{\mathbf{w}^T \mathbf{S}_b \mathbf{w}}{\mathbf{w}^T \mathbf{S}_w \mathbf{w}}, \quad (1)$$

wherein,  $\mathbf{S}_w$  represents the within-class scatter matrix,  $\mathbf{S}_b$  is the between-class scatter matrix, and  $\mathbf{w}$  denotes the projection vector.

The above problem can be equated to finding the generalised eigenvectors of the eigenvalue problem:

$$\mathbf{S}_b \mathbf{v}_i = \lambda_i \mathbf{S}_w \mathbf{v}_i. \quad (8)$$

where the eigenvalues  $\lambda_i$  represent the discriminative power of each projection vector. Once we obtain the projected vector  $\mathbf{v}$ , it can be used for classification instead of the original vectors with a linear classifier.



**Figure 7.** Transformation process illustration of a KFD model. A nonlinear mapping function  $\phi(x)$  converts a nonlinear problem in the original (low dimensional) input space to a linear problem in a (higher dimensional) feature space (from [43]).

The limitations of the LDA method are primarily due to its inherent linearity, especially for nonlinear problems [56]. In contrast, the KFDA method, an improved version of LDA that uses a kernel trick, overcomes these shortcomings. KFDA is better suited for the analysis of high-dimensional data and complex systems. It is easy to implement and is characterised by its adaptability and generalisation.

The core concept of KFDA is to map the original input data by a nonlinear mapping function  $\phi$  into a high-dimensional feature space  $F$ , typically a nonlinear space (see Figure 4.4). Through this transformation, non-linear relationships within the input data are indirectly transformed into linear relationships. LDA is then applied to extract the most significant discriminating features in this feature space. To overcome the computational challenges of calculating  $\phi$  directly, Adding kernel parameters to express functional relationships for nonlinear mappings.

The goal of KFDA is to find a set of projection vectors that maximises the inter-class distance while minimising the intra-class distance within the feature space. This is achieved by maximising the following kernel Fisher criterion:

$$J(\boldsymbol{\alpha}) = \frac{\boldsymbol{\alpha}^T \mathbf{K}_b \boldsymbol{\alpha}}{\boldsymbol{\alpha}^T \mathbf{K}_w \boldsymbol{\alpha}}, \quad (2)$$

where  $\boldsymbol{\alpha}$  represents the projection vector,  $\mathbf{K}_b$  represents the kernel between-class scatter matrix and  $\mathbf{K}_w$  is the kernel within-class scatter matrix in the feature space.

The described in Equation (9) can be reformulated as solving the generalized feature equation, thus reducing redundancy:

$$\mathbf{K}_b \boldsymbol{\alpha} = \lambda \mathbf{K}_w \boldsymbol{\alpha}, \quad (3)$$

where  $\lambda$  is the nonzero eigenvalue of projection vector  $\boldsymbol{\alpha}$ . Let  $\boldsymbol{\alpha}_{opt} = (\alpha_1, \dots, \alpha_M)$  be the optimal projection vector, It is also the maximum eigenvalue from Equation (4).  $\lambda_1, \dots, \lambda_M$  are the eigenvalue of  $\alpha_1, \dots, \alpha_M$  respectively, and  $\lambda_1 \geq \dots \geq \lambda_M$ . The number of vectors  $m$  is by the cumulative contribution rate  $\sum_{i=1}^m \lambda_i / \sum_{i=1}^M \lambda_i \geq 90\%$ .

If  $\boldsymbol{\alpha}_{opt}$  knows, the nonlinear decision function  $f(x)$  of KFDA as:

$$f(x) = \sum_{i=1}^n \alpha_i k(\mathbf{x}_i, \mathbf{x}), \quad (4)$$

where  $\alpha_i$  is the coefficient vector by the  $i$  kernel,  $\mathbf{x}_i$  is the  $i$  one in all the input samples, and  $k$  is the kernel function.

#### 4.2.2. Kernel parameter optimization

Among these kernel functions, the Gaussian kernel stands out due to its strong generalization capability and the fact that it requires fewer parameters to be set. This makes it particularly effective at capturing nonlinear relationships. Therefore, In [43], the Gaussian kernel function was chosen as the kernel function and is expressed as shown in Equation (12):

$$k(\mathbf{x}, \mathbf{y}) = \exp\left(-\frac{\|\mathbf{x} - \mathbf{y}\|^2}{2\sigma^2}\right), \quad (5)$$

where  $\sigma$  is the width parameter of Gaussian kernel.

The kernel parameter  $\sigma$  is very important and plays a crucial role in the KFDA-SVM model appearing in this paper, which can adjust the position and distribution of the data in the feature space, and largely affects the classification efficiency and the generalisation ability of the later SVM classification model, therefore, choosing the correct The kernel parameter  $\sigma$  Value is a very important step.

#### 4.2.2. SVM Model base on kernel Fisher discriminant analysis

In order to further subdivide the confusion action into a specific action, this paper introduces SVM vector machine as a sub-classification model to divide the confusion action. The principle of SVM classifier is to take the hyperplane to maximize the feature distance between different categories so as to achieve the classification effect. As shown in the figure, the wider the width of the classification interval (i.e., maximizing), the lower the impact caused by the local interference in the training set. Therefore, it can be considered that the last classification method has the best generalization performance and generality. The model of SVM can be formulated as:

$$y = \text{sign}(w^T x + b), \quad (6)$$

where,  $x$  is the feature vector,  $w$  is the weight vector,  $y$  is the marker vector, and  $\text{sign}(y)$  is the sign function.

When  $y = 1$ , the sample is positive; when  $y = -1$ , the sample is negative, i.e.

$$\begin{cases} w^T x + b > 0, y = 1, \\ w^T x + b \leq 0, y = -1. \end{cases} \quad (7)$$

As shown in Figure 8, SVM usually finds the optimal classification hyperplane by maximizing the classification interval. Assuming that the input of the training set is the set of  $x(i)$  vectors and the output is the set of  $y(i)$  vectors, the classification interval is twice the minimum distance from the full set of samples to the hyperplane, i.e., where  $m$  is the number of samples

$$\gamma = \min_{i=1, \dots, m} 2y^{(i)} \left( \frac{w^T x^{(i)} + b}{\|w\|} \right). \quad (8)$$

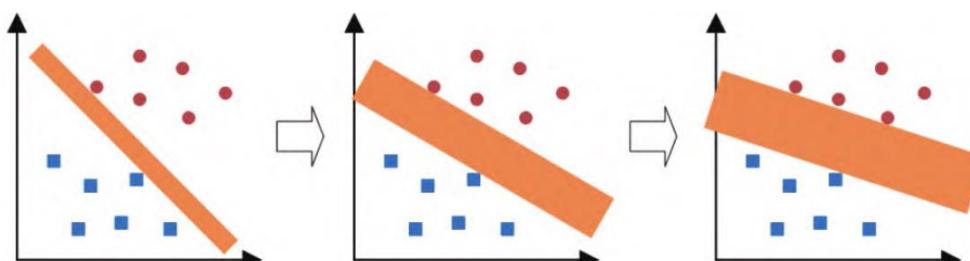
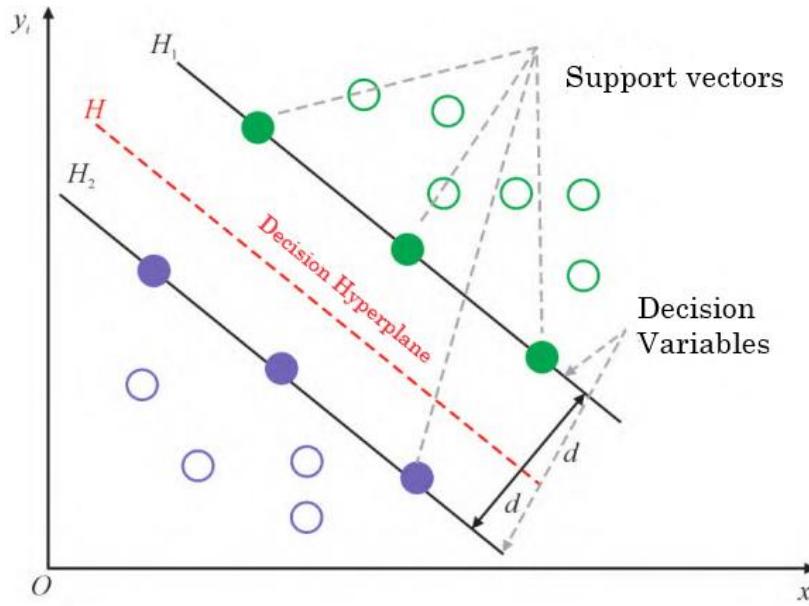


Figure 8. Vector machine classification flow chart.

Mathematically, all sample points that meet the requirements of equation (15) (i.e., sample points with the smallest Euclidean distance to the classification hyperplane) will be defined as support vectors, then the set of samples must satisfy the following two cases: if the samples are positive, then  $w^T x^{(i)} + b = 1$ . If the samples are negative, then  $w^T x^{(i)} + b = -1$ , as shown in Figure 9.



**Figure 9.** Vector machine classification schematic.

Therefore, the characteristic samples in the sample set should satisfy when the discriminant equation is multiplied by the corresponding coefficients.

$$y^{(i)} (w^T x^{(i)} + b) \geq 1. \quad (9)$$

## 5. Experimental

### 5.1. Experimental setting

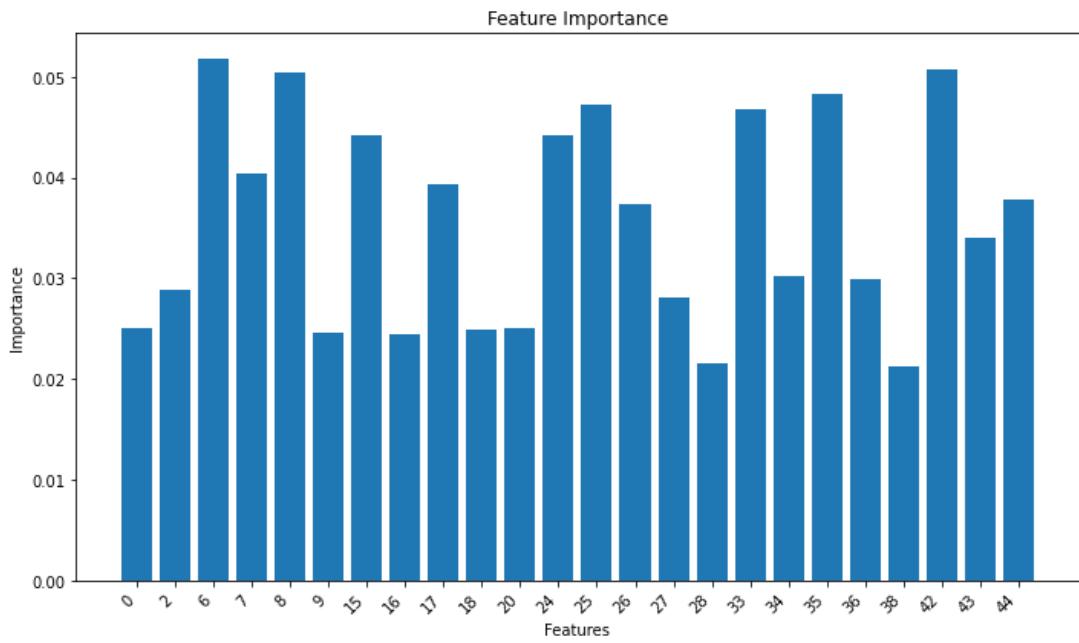
The experiments were conducted on the same computer with the following specifications: an AMD Ryzen 7 4800H processor with Radeon Graphics, operating at 2.90 GHz, 16GB of RAM, and an NVIDIA GeForce GTX 1660 Ti graphics card. The operating system used was Windows 10. We utilized both Matlab and Python tools for conducting the experiments and performed validations on four different datasets, namely UCI DSA, UCI HAR, WISDM, and UCI ADL. We also conducted a relevant evaluation of our approach. To maintain the conciseness of the paper, the following experiments are illustrated using the UCI DSA dataset as an example.

### 5.2. Extraction of important features

By employing the Stepwise regression algorithm to analyze the 45 features in the dataset, we can assess the varying importance of each feature. We select those features with an importance score exceeding 0.02 to be used as crucial features for the subsequent multi-layer classifier based on Generalized Discriminant Analysis. For features with lower importance, we filter them out to mitigate potential interference with our classification accuracy.

The histograms plotted for the weights of the significant characteristics are as follows:

Firstly, using the random forest model in Matlab, a plot illustrating the relationship between the number of decisions as the independent variable and the error as the dependent variable was generated, as depicted in Figure 10. Specific results can be found in Table 3.



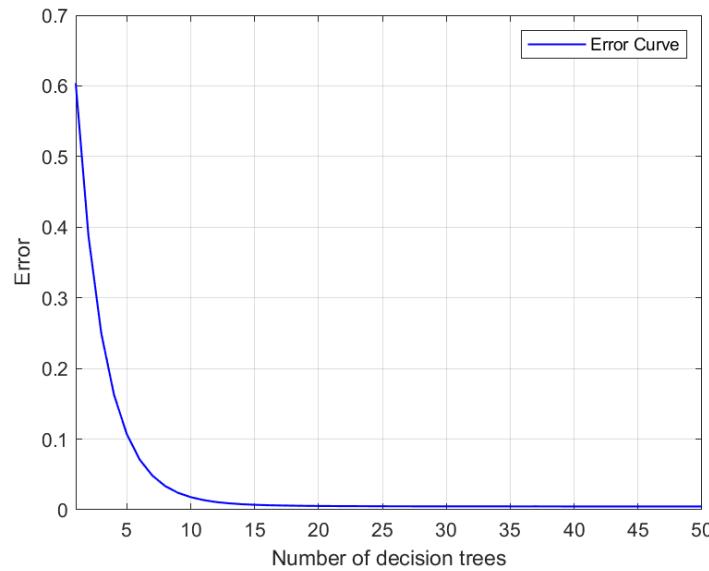
**Figure 10.** Weights of important features chart.

**Table 3.** Number of decisions and error rate.

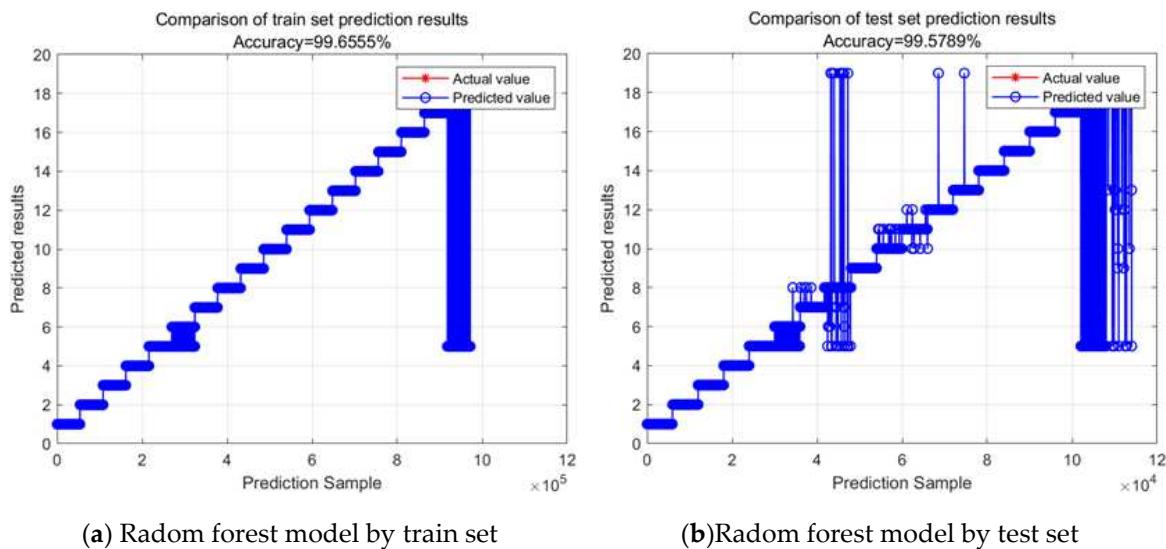
Number of decisions tree	Error rate
1	63.1%
5	10.5%
10	2.8%
20	1.2%
35	0.8%
50	0.3%

### 5.3. Extraction of random forest base on stepwise regression algorithm

From the above Figure 12, it can be observed that, in this dataset, based on an analysis of computer performance, model accuracy, and the reliability of the model, the number of decision trees was determined to be 50. To better assess the classification performance of the Random Forest model, we established a test dataset. Using MATLAB, we conducted experiments where we uniformly partitioned the overall data into different ratios based on various human activities and different volunteers. The results for different ratios and their impact on the accuracy of both the training and test sets are presented in Table 4.



**Figure 11.** Plot of the number of decisions versus error in the random forest model.

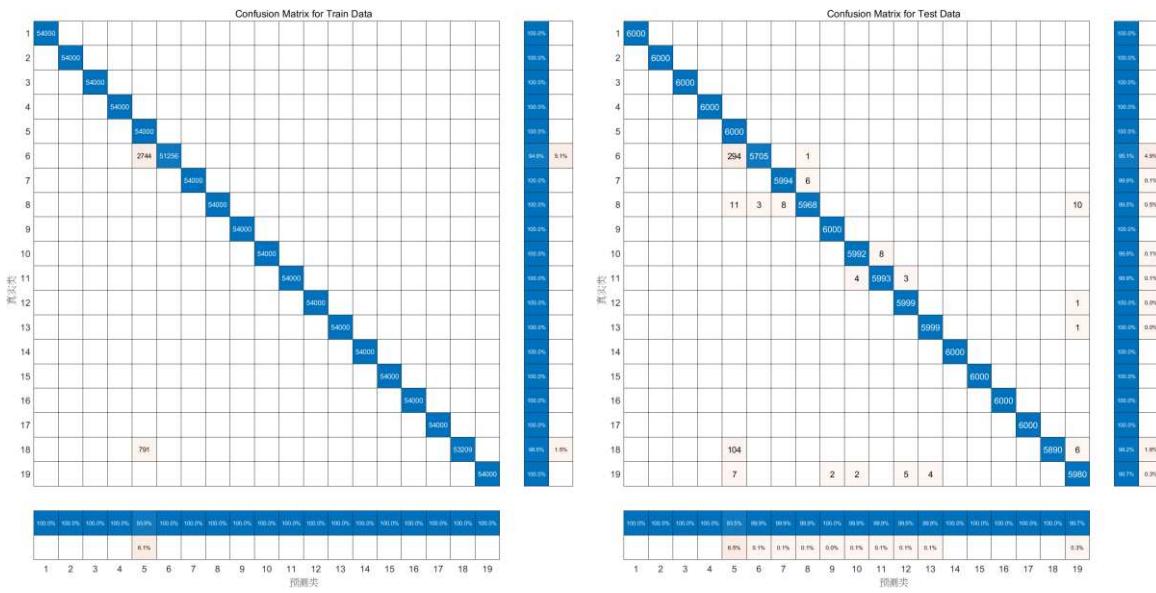


**Figure 12.** Random forest model recognition results comparison chart.

To better analyze the above random forest identification results, a confusion matrix plot of the above two results was made using MATLAB as follows.

**Table 4.** This is a table. Tables should be placed in the main text near to the first time they are cited.

Ratio (training:testing)	UCI DSA	
	Training data	Testing data
9:1	99.6555%	99.5789%
8:2	99.6043%	99.5689%
7:3	99.66%	99.5269%
6:4	99.6756%	99.5445%
5:5	99.6656%	99.5040%
4:6	99.6706%	99.3753%



(a) Confusion matrix of Radom forest model by train set

(b) Confusion matrix of Radom forest model by test set

Figure 13. Confusion matrix of test set and training set random forest training.

We also performed Random Forest classification on data from the other three databases separately, following a similar experimental setup. The experimental results obtained are presented in Table 5.

Table 5. Random forest Result table between datasets: UCI DSA, UCI HAR, WISDM and UCI ADL.

Ratio (training: testing)	UCI DSA		WISDM		IM-WSHA	
	Training data	Testing data	Training data	Testing data	Training data	Testing data
9:1	99.6555%	99.5789%	99.9415%	99.1819%	99.9973%	97.5342%
8:2	99.6043%	99.5689%	99.9543%	98.6841%	99.9982%	96.9773%
7:3	99.66%	99.5269%	99.6646%	98.5631%	99.9977%	96.8102%
6:4	99.6756%	99.5445%	99.6326%	98.4698%	99.9973%	96.4045%
5:5	99.6656%	99.5040%	99.6061%	98.3741%	99.9984%	95.9813%
4:6	99.6706%	99.3753%	99.5841%	98.2694%	99.996%	95.3001%

Observing the four charts above and drawing upon real-world judgment, this study suggests that the primary reason for the inconsistency between action recognition results and actual results is the similarity in features among these actions, making them easily confusable during the algorithmic recognition process. For instance, actions such as walking up and down stairs, walking or standing in an elevator, exhibit such similarities. Apart from these mentioned actions, the predictive accuracy for all other actions approaches 100%. This indicates that these actions can be recognized and classified as genuine actions at this layer of the classification model.

The remaining unrecognized actions fall into two main categories. For instance, the model classifies A6, A18, and A19 as A5 and confuses A7 and A8 with each other. To facilitate subsequent fine-grained classification models, these similar actions are divided into two main categories, as illustrated in the Table 6.

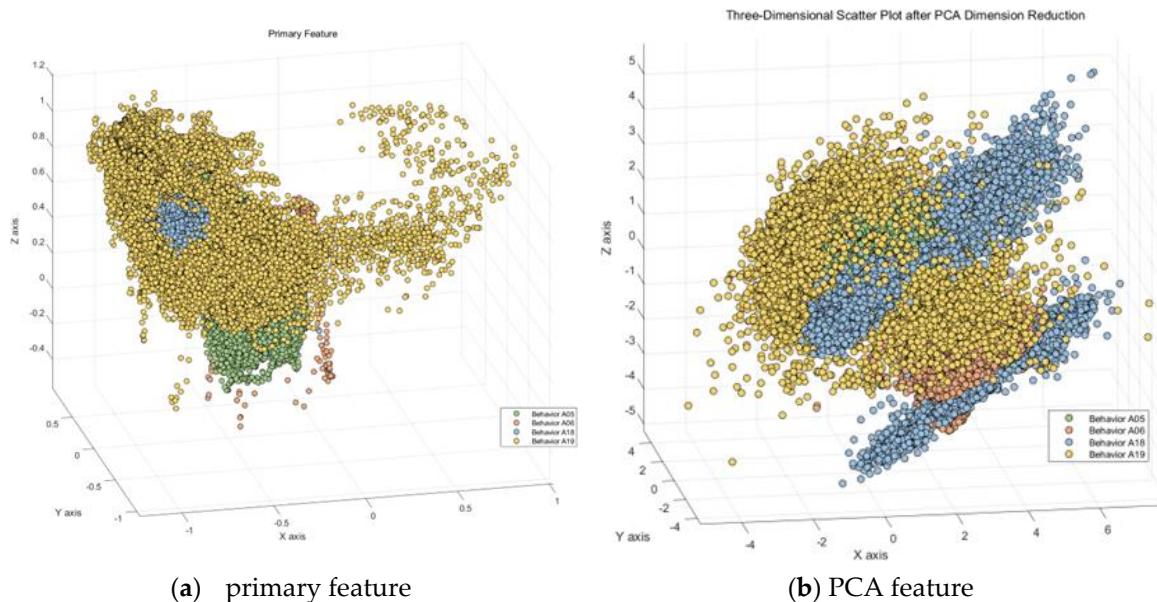
**Table 6.** Confusion action classification table.

Confusion category	Easily confused actions
Confusion I category	A5,A6,A18,A19
Confusion II category	A7,A8

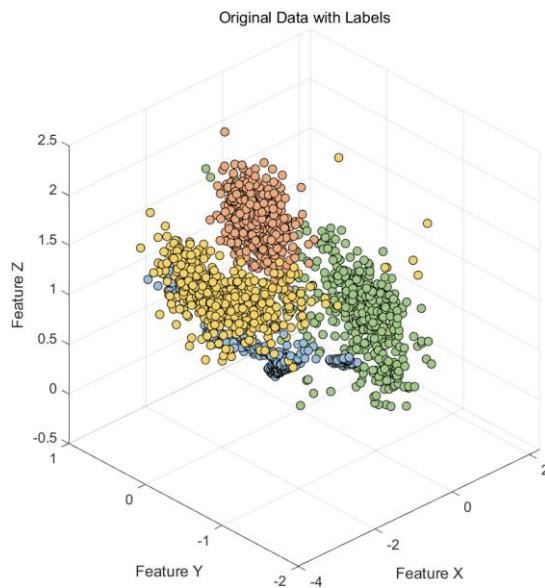
### 5.3. Extraction of SVM Model base on kernel fisher discriminant analysis

Taking the four Behaviors classes (A5, A6, A18, A19) as an example of Confusion Type I, we first extracted three of the most important features from the dataset and created a scatter plot as shown on the left side of Figure 14. It can be observed that these four Behaviors classes have a relatively short spatial distribution in these three original features, indicating a small inter-class distance and a large intra-class distance. This is not conducive to the activity recognition by the classifier.

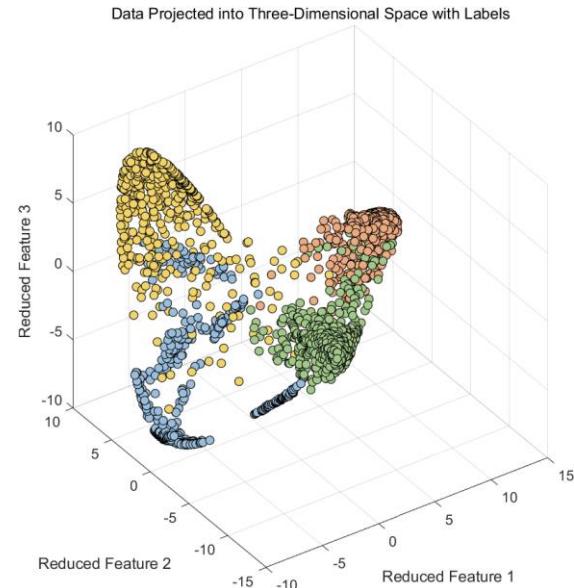
Subsequently, we applied Principal Component Analysis (PCA) for dimensionality reduction, as illustrated on the right side of Figure 14. It represents three randomly selected nonlinear discriminative features extracted from the original features of these four similar activities. In this study, we find that the mapping results of PCA are not particularly favorable, as the intra-class distance remains small.

**Figure 14.** primary feature and PCA feature.

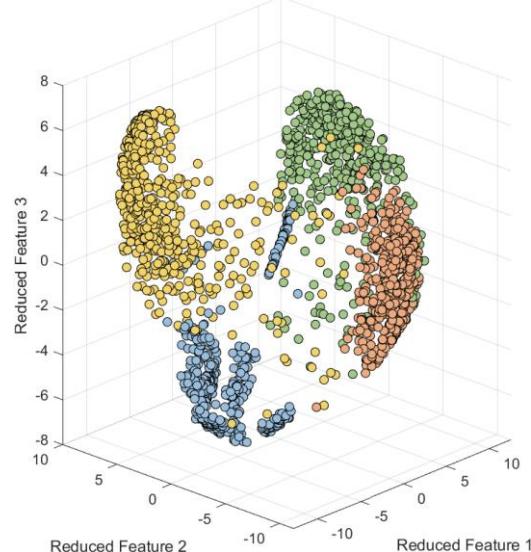
Therefore, in this study, we employed Kernel Fisher Discriminant Analysis for dimensionality reduction, focusing on the points that were previously confused in the upper layer of Random Forest. Kernel Fisher Discriminant Analysis has a parameter denoted as  $\sigma$ , which can vary. Typically, this parameter's range is set within  $[0, 10]$ . We experimented with different parameter settings and obtained various images, as shown in Figure 15.



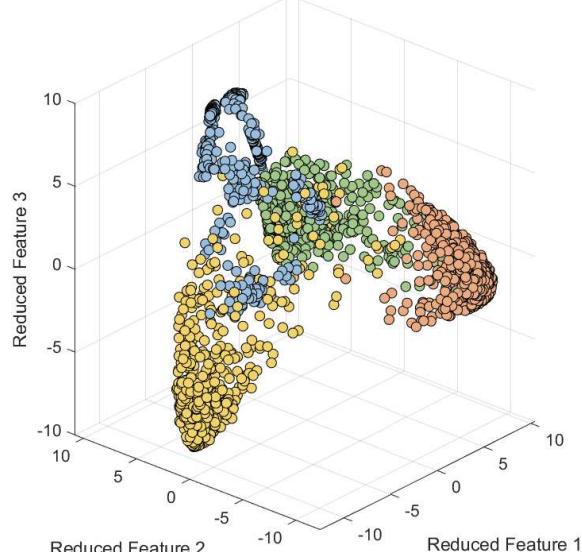
(a)  $\sigma = N/A$   
Data Projected into Three-Dimensional Space with Labels



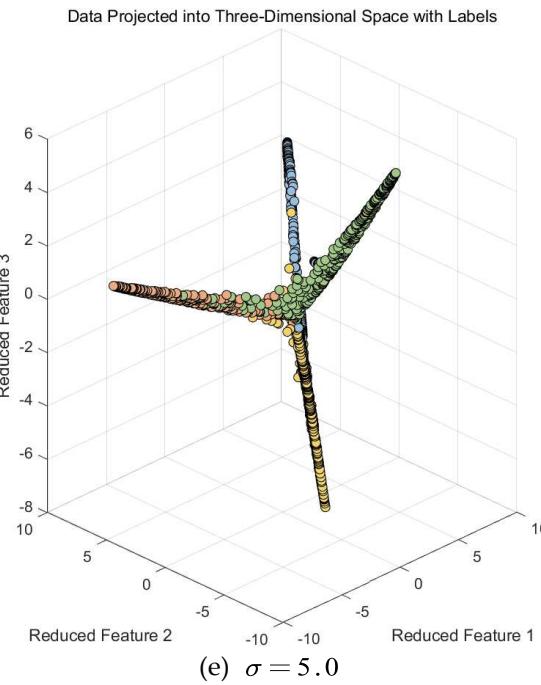
(b)  $\sigma = 1.55$   
Data Projected into Three-Dimensional Space with Labels



(c)  $\sigma = 0.5$



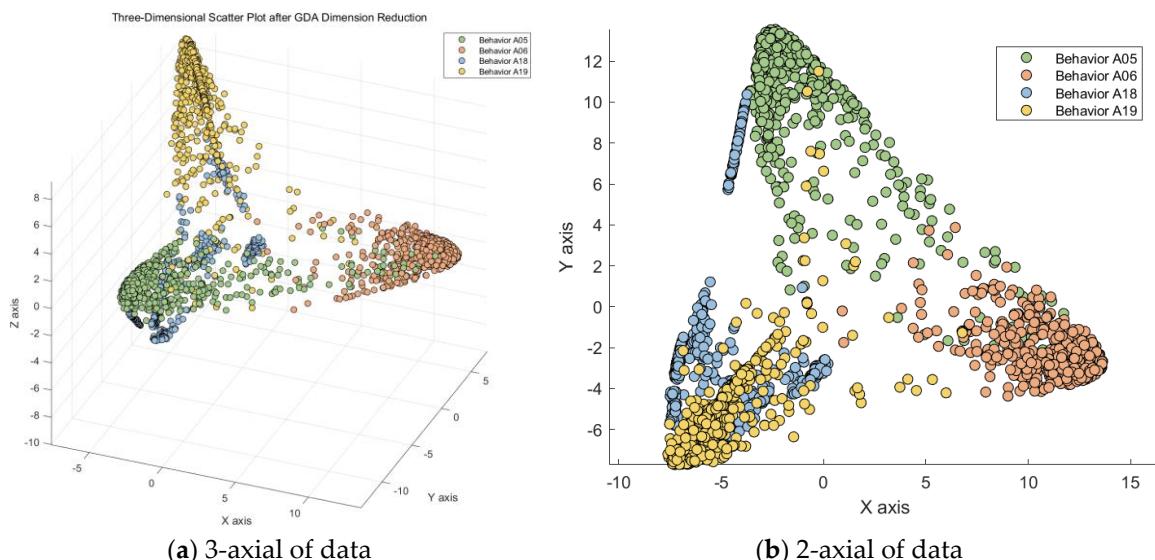
(d)  $\sigma = 1.0$



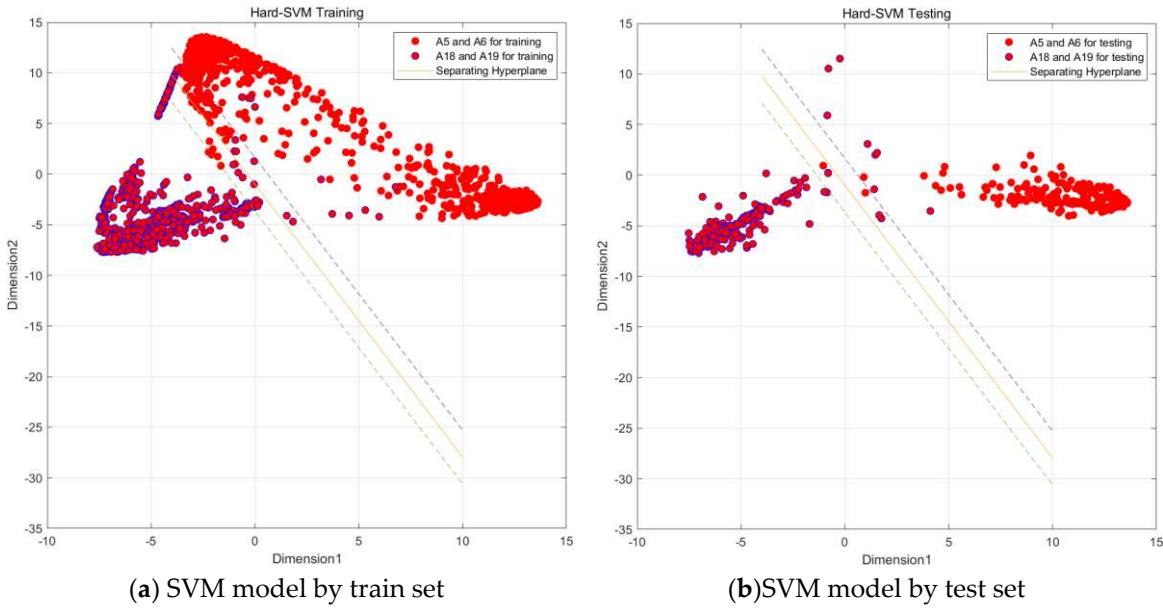
**Figure 15.** The Result of Kernel Fisher Discriminant Analysis with varying parameter .

Based on the above experimental results, we can see that in this scenario, upon observing the three-dimensional scatter plot, the data has been categorized into four classes. In order to obtain a clearer visual representation, we selected the two features that performed best in the three-dimensional space and generated a two-dimensional scatter plot, as shown in Figure 16.

In this paper, we use MATLAB to sub-classify the above model, and input the indicators that have been generalized discriminant analysis into SVM as the original data, taking the confusion I class as an example, because A5 and A6 are more closely connected, and A18 and A19 are also more closely connected, so we first subdivide the confusion I class into two large classes A5, A6, and A18, A19, and then a second subdivision, we can subdivide the confusion I class into the more A5, A6, A18, and A19 classes by a two-layer SVM vector machine. A5, A6, A18, and A19 which are the four classes of activities, As shown in the Figure 17.

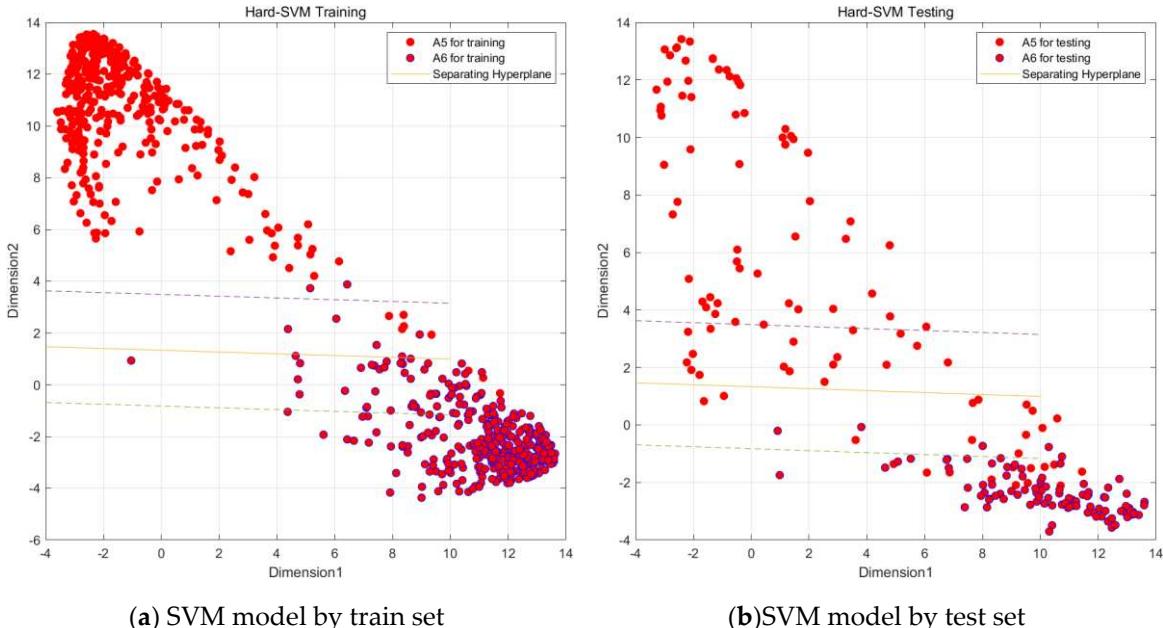


**Figure 16.** kernel Fisher discriminant analysis feature.

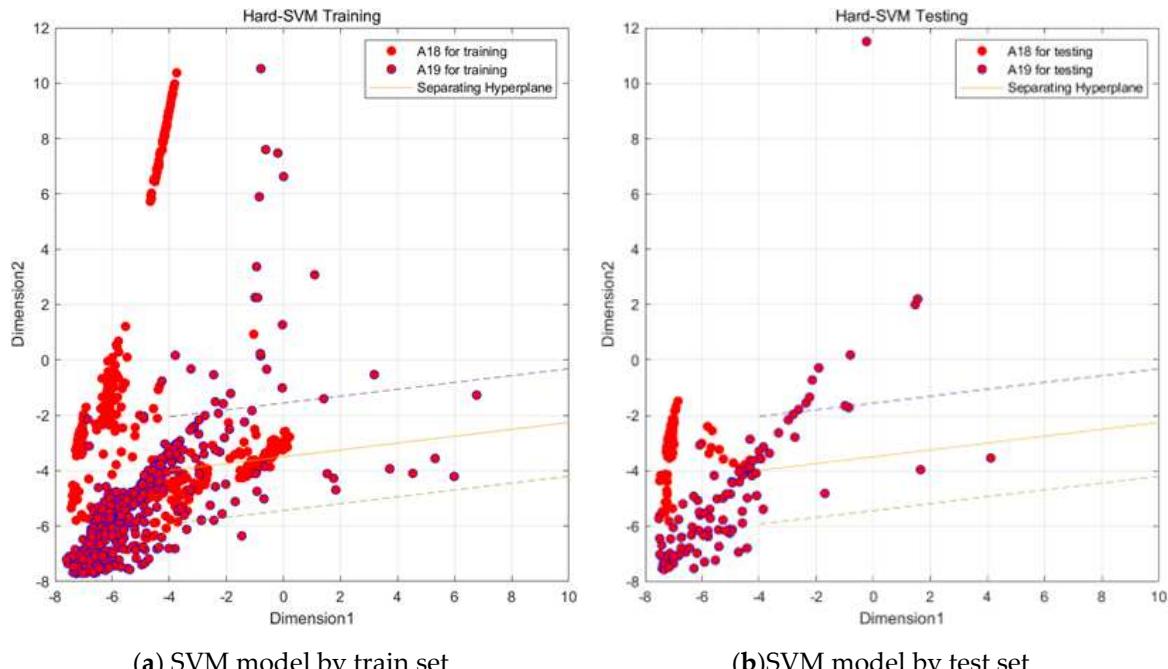


**Figure 17.** SVM preliminary segmentation obfuscation I class result graph.

Through the above steps, the data of the confusion I class has been classified into two major classes A1, A2 and A7, A8 by SVM vector machine, and in order to classify them more carefully, this paper then performs a fine classification of these two major classes into specific activity classes. As shown in the figure 6.8 and Figure 18 and Figure 19.



**Figure 18.** SVM preliminary segmentation obfuscation I class result graph.



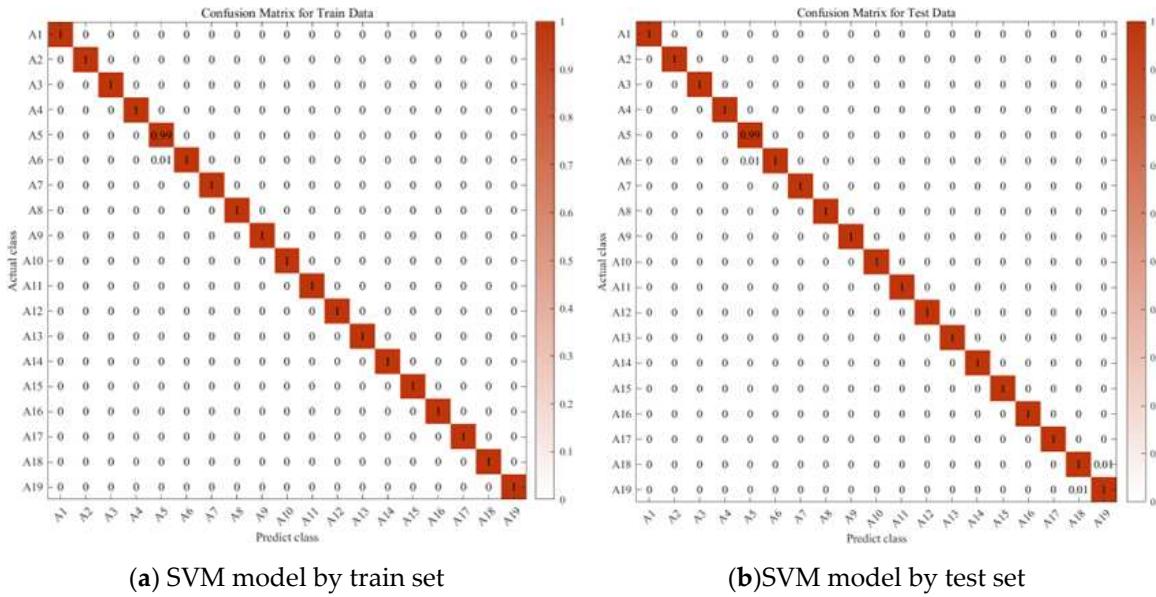
**Figure 19.** SVM preliminary segmentation obfuscation I class result graph.

Through the steps related to figure, we are able to classify all the data of the confusion I class into specific active classes by the above SVM vector machine meticulous classification, although the effect of SVM vector machine fine classification A18, A19 is not significant as shown in Figure 19, but it is much better than the initial random forest classification effect has been much better than the initial random forest. Similarly, we conducted various experiments as shown in Table 7.

**Table 7.** Random forest Result table between datasets: UCI DSA, UCI HAR, WISDM and UCI ADL.

Ratio (training: testing)	A5, A6 and A18, A19 Accuracy (%)		A5 and A6 Accuracy (%)		A18 and A19 Accuracy (%)	
	Training data	Testing data	Training data	Testing data	Training data	Testing data
9:1	99.90	99.75	95.11	90.98	78.10	66.77
8:2	98.96	98.41	95.12	90.56	81.00	78.75
7:3	96.56	95.83	95.28	91.04	75.33	74.70
6:4	95.75	95.06	95.33	91.25	68.25	69.30
5:5	94.90	95.35	94.80	90.65	73.20	64.80
4:6	93.91	94.62	90.56	85.34	77.16	70.65

In this paper, the same operation was also performed on the confusion II class, which was input to the second layer of the classification vector machine to obtain the recognition probabilities of the four similar actions, and the final recognition results of the four similar activities were obtained by weighted average with the recognition probabilities of the first layer classifier. The confusion matrix is shown in figure, and it can be seen that the original confusion-prone actions are improved a lot, and the overall correct rate is improved from 99.57% to 99.71%.



(a) SVM model by train set

(b) SVM model by test set

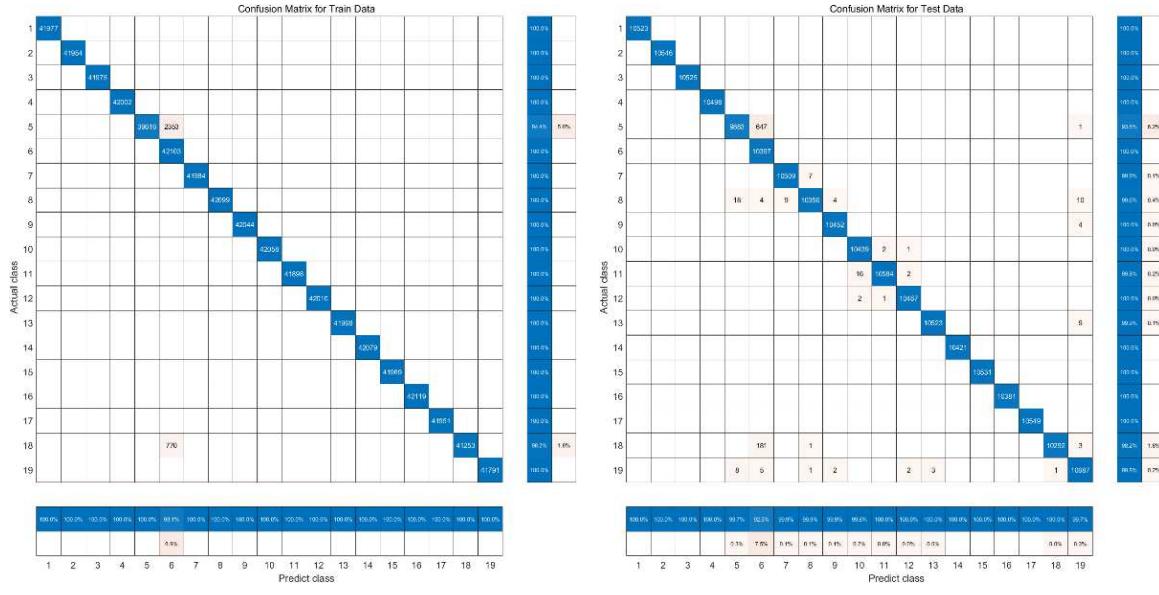
Figure 20. Confusion matrix diagram for two-level classifier.

We also compared our approach with those of others on three datasets: UCI HAR, WISDM, and IM-WSHA, as shown in Table 8.

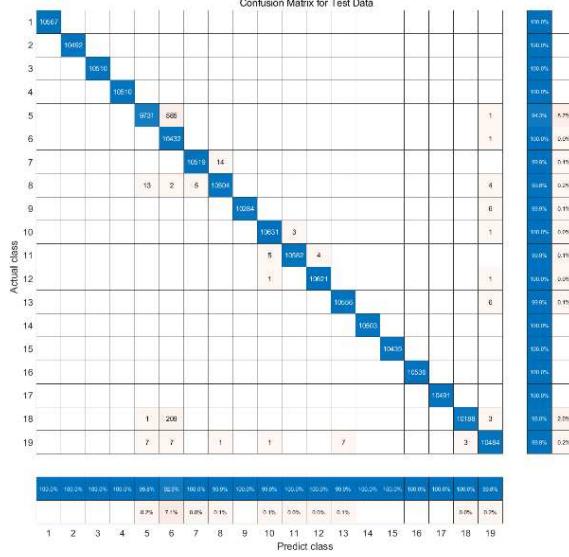
**Table 8.** Comparison of recognition accuracy of the proposed method with other state-of-the-art methods over UCI DSA, UCI HAR, WISDM and IM-WSHA datasets.

Method	UCI DSA	UCI HAR	WISDM	IM-WSHA
MS-DLD[25]				88.3%[25]
HPAR[26]		91.83%[26]		90.18%[26]
HDAR[27]				91.45%[27]
RPLB[28]				83.18%[28]
Kinematics features with kernel sliding perceptron[29]				81.47%[29]
Estimation algorithm[30]				80.49[30]
Accelerometer and Gyroscope Sensors[31]		96.33%[31]		
Deep CNN-LSTM[32]		93.11%[32]		
Deep CNN-GRU[33]		96.20%[33]	97.21%[33]	
EdgeHARNet[34]			94.036%[34]	
MarNASNet-b[35]		94.20%[35]	90.62%[35]	
DMEFAM[36]		96%[36]	97.9%[36]	
BLSTM[37]		98.37%[37]	99.01%[37]	
CAEL-HAR[38]		96.45%[38]	98.57%[38]	
2D CNN-LSTM[49]	92.95%[49]			
MVTS[50]	98.96%[50]			
<b>SR-KS</b>	<b>99.71%</b>	<b>98.71%</b>	<b>99.12%</b>	<b>97.6%</b>

Below, we validate the aforementioned model. First, we conducted experiments using K-fold cross-validation on the random forest. In this study, we set K=5 for validation. The experimental results are shown in Figure 21, demonstrating the strong generalization capability of our model.

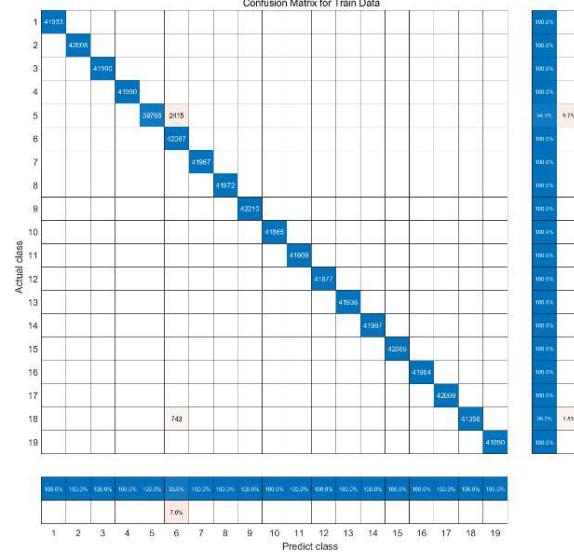


(a) First split training set confusion matrix

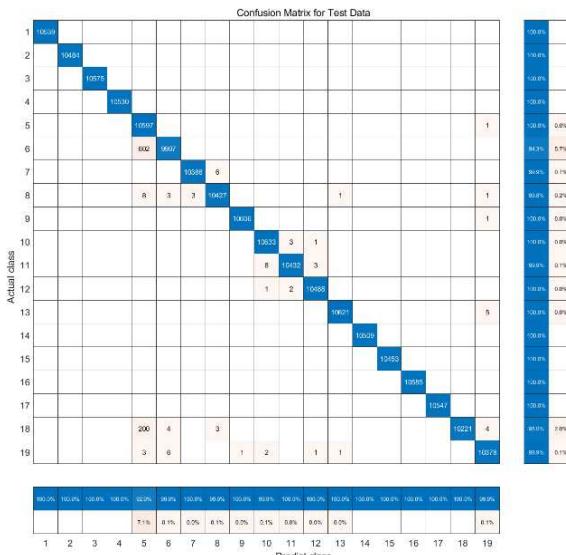


(c) Second split training set confusion matrix

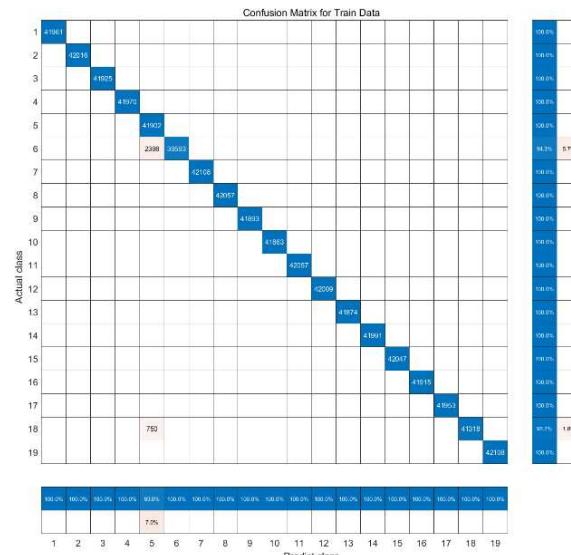
### (b) First split testing set confusion matrix



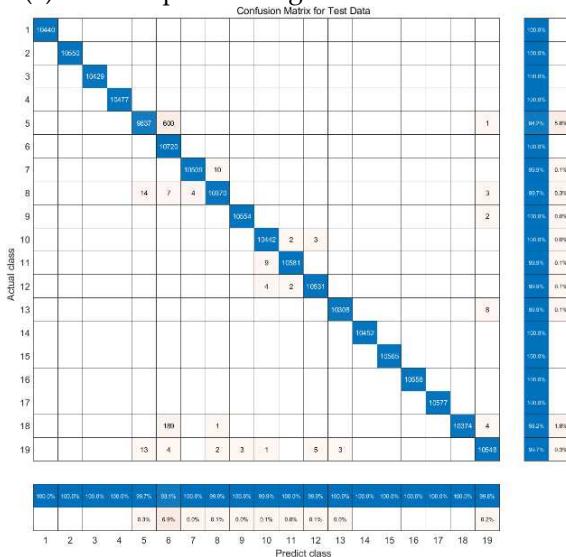
(d) Second split testing set confusion matrix



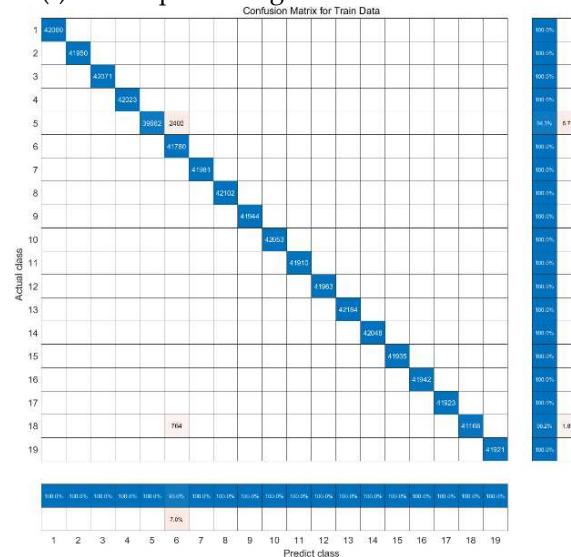
(e) Third split training set confusion matrix



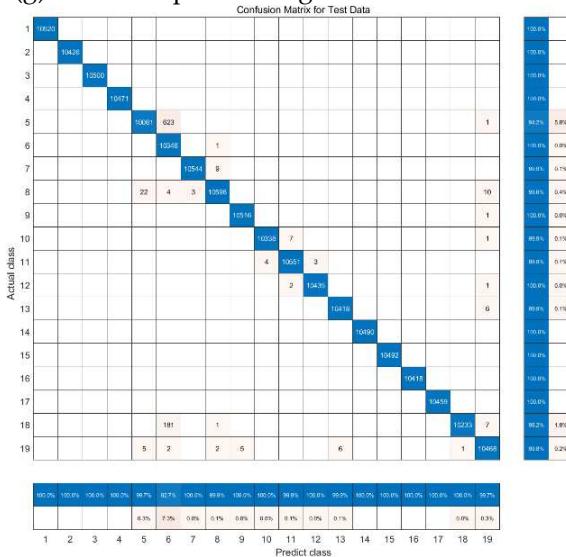
### (f) Third split testing set confusion matrix



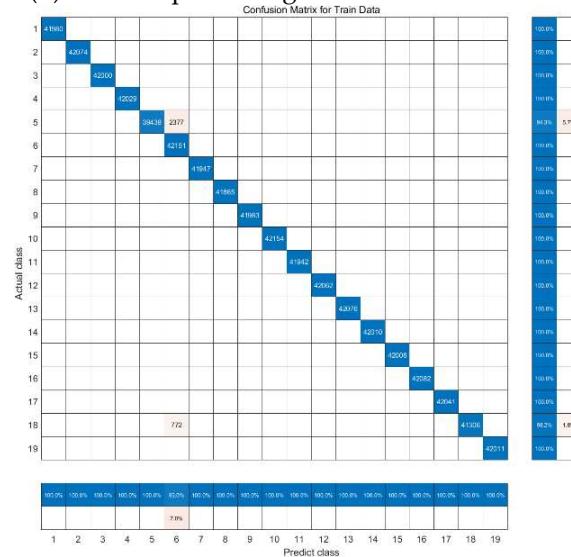
(g) Fourth split training set confusion matrix



#### (h) Fourth split testing set confusion matrix



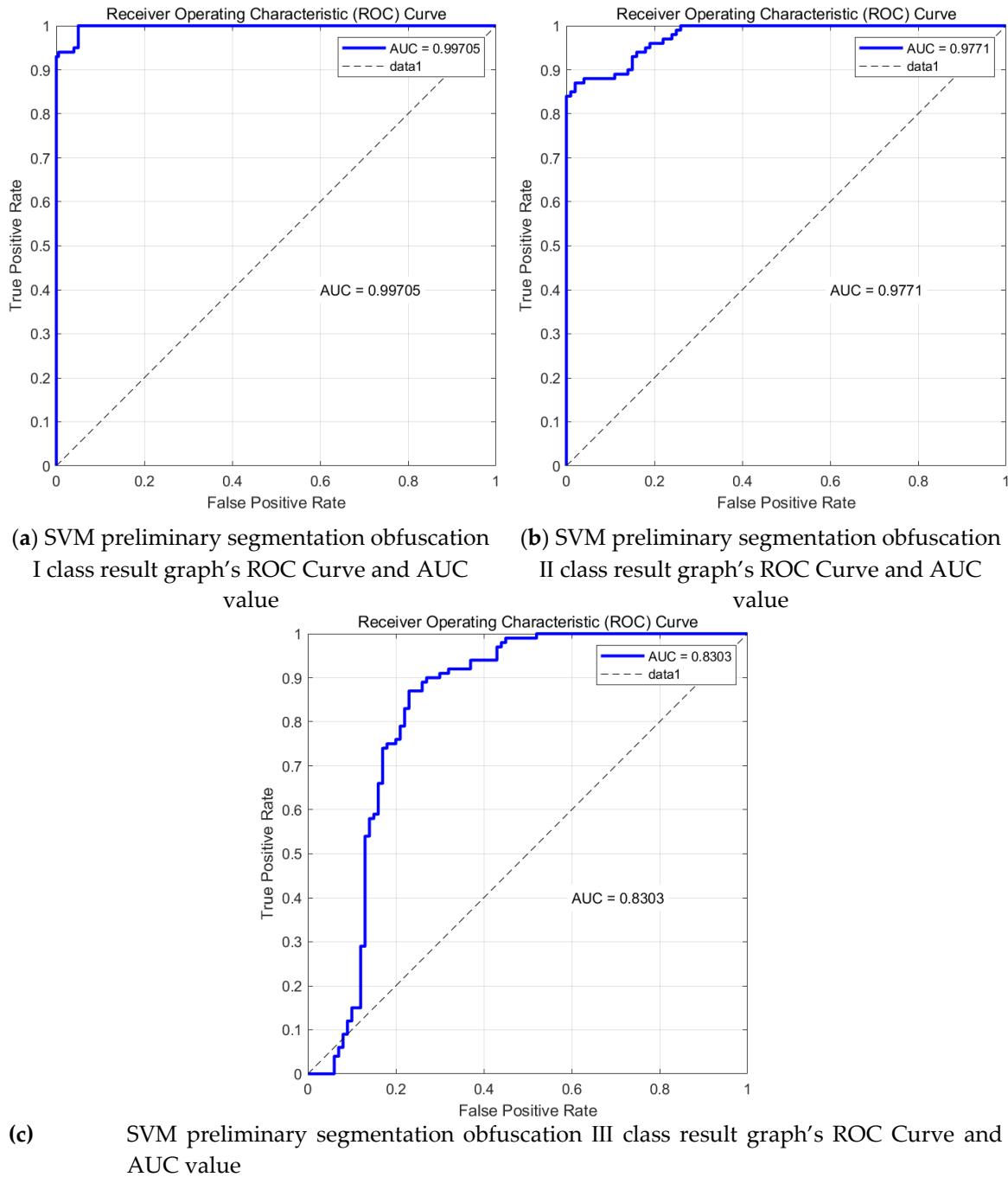
(i) Fifth split training set confusion matrix



### (j) Fifth split testing set confusion matrix

**Figure 21.** Let  $k$  be the cross-validation result for 5.

Immediately after that, the SVM model was validated using ROC curves as well as AUC values with the following results:



**Figure 22.** SVM Model ROC Curve and AUC value.

## 6. Conclusion

This study proposes an approach to the problem of identifying similar activities, in which a multilayer model called "SR-KS" is introduced, where all the features of the data are firstly filtered using Stepwise Regression Analysis, and a part of the features are selected for Random Forest Classification, which will improve the efficiency of classification effectively. Based on the above classification results, we screened out the data points that were confusing in terms of identification, and then used the SVM model based on Kernel Fisher Discriminant Analysis to identify them, which firstly utilised the Kernel Fisher Discriminant Analysis to separate the similar activities from data perspective, followed by using SVM model to classify the above data, and finally get a good

recognition result, we also used k cross validation as well as ROC curves to validate the above model respectively, and the result proved that our model has a good generalisation ability. Our method can identify similar human activities very well, but at the same time, we also found that the recognition effect of A18,A19 is not very good, we shall investigate a more suitable model and its simulation algorithm to obtain high accuracy for human activity in A18 or A19. Our future research work can be focused on the following two points:

- Extending the proposed technique to cope with classification tasks under more similar activity data, such as typing and handwriting. Extending the proposed technique to cope with generative tasks under more demanding driving conditions, such as datasets with few features and insufficient data sample;
- Starting from the data collection, designing and implementing a sound and specific sensor data collection scheme and collection algorithm design, for example, we consider the removal of noise in data collection as well as the collection of data conducive to the identification of human activity.

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