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Article

Unveiling the Diagenetic and Mineralogical Impact on the Carbonate Formation of the Indus Basin, Pakistan: Implications for Reservoir Characterization and Quality Assessment

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Abstract: The Chiltan Formation is a potential hydrocarbon-producing reservoir in the Indus Basin, Pakistan. However, its diagenetic alterations and heterogeneous behavior lead to significant challenges in accurately characterizing the reservoir and production performance. This manuscript aims to utilize Chiltan Limestone core samples to conduct a detailed analysis of the diagenetic impacts on reservoir quality. The formation evaluation was carried out through thin section analysis, SEM-EDS and FTIR investigation, as well as plug porosity and permeability measurements under different stress conditions. In results, Petrography revealed three microfacies with distinct diagenetic features and micro-nano fossil assemblages, including intraclasts, pelloids, bioclasts, and stylolites. Diagenesis has a significant impact on petrophysical properties, leading to increased reservoir heterogeneity. The specified depositional environment exposed the alteration of the Chiltan formation during distinct diagenetic phases in marine, meteoric, and burial settings. Pore morphology and mineralogy reveals complex micro-pore structure with various carbonate mineral phases and cement types in the formation samples. The average porosity and permeability of the core samples were found to be 3.4% and 0.449 mD respectively, indicating poor reservoir quality. Stress sensitivity was determined using Klinkenberg corrected permeability, which indicated a reduction in measured and absolute permeability due to increasing confining stress, further reducing the pore throat structure of the formation. In conclusion, the Chiltan formation possesses intricate reservoir heterogeneity and varied micro-pore structure caused by diagenesis and depositional settings. The formation is classified as a low-quality reservoir due to its non-uniform pore geometry, which exhibits low petrophysical properties resulting from overburden stress. The results of this study provide solid foundation in reservoir characterization and quality assessment which has implications for exploring and exploitation of indigenous resources.

Keywords: carbonate formation; mineralogy; diagenesis; petrophysical properties; stress sensitivity; reservoir quality

1. Introduction

The Middle Jurassic carbonates are extensively distributed worldwide and contain significant commercial hydrocarbon resources. It is estimated that approximately 60% of the global oil reserves and 40% of its gas reserves are held in carbonate deposits, with the Middle East holding 70% of oil and 90% of gas reserves in carbonate formations [1,2]. Similarly, Pakistan has considerable potential in carbonate deposits in the Indus Basin and Baluchistan Basin [3]. However, carbonates are challenging in petroleum exploration and production due to their complex reservoir heterogeneity,

diagenesis, and post-depositional environment factors [4,5]. Understanding these factors is crucial for assessing the reservoir potential. The reservoir quality of carbonates is influenced by initial depositional features and subsequent diagenetic modifications [6,7]. The depositional environment influencing formation characteristics, and diagenesis affecting reservoir quality through post-depositional processes [8,9]. Numerous physio-chemical and biological changes during rock development alter micro-pore structure, leading to complex reservoir heterogeneity [10,11]. The fundamental factors influencing carbonate reservoir quality include mineralogy, rock textures, and depositional settings, all of which outline the diagenetic alterations that occur. The main diagenetic processes that affecting carbonate reservoir quality encompasses include dolomitization, micritization, dissolution, compaction, cementation, and fracturing [12–14]. These processes alter reservoir characteristics in response to periodic facies variations in marine carbonates due to changes in depositional environment [15]. Therefore, a comprehensive understanding of these diagenetic and depositional factors is essential for effectively characterizing and developing carbonate reservoirs for hydrocarbon exploration and production.

Variations in petrophysical, pore-morphological, and mineralogical parameters within carbonate reservoirs are heavily influenced by a combination of factors, including the depositional environment, diagenetic processes, overburden stress, and tectonic activities. These factors collectively transform carbonate rocks into highly heterogeneous and challenging materials for their analysis, measurement, and interpretation [16,17]. Among these factors, overburden stress plays a particularly significant role in shaping pore morphology, pore geometry and over all petrophysical properties of the reservoir. In carbonate formations, the impact of pore sensitivity becomes even more pronounced when compared to clastic sand stones. This heightened sensitivity is due to their complex lithofacies and diagenetic processes, which tend to affect reservoir quality and recovery efficiency [18,19]. Stress sensitivity is often overlooked during reservoir characterization leading to severe complexities in interpretation, estimation, modeling and development. Measurements made under stress sensitivity are essential for accurately and effectively estimating reservoir parameters [20].

The Chiltan limestone is recognized as a prolific hydrocarbon producing formation within the Indus Basin, ranging from late Triassic to Pleistocene ages and forming a marine carbonate sequence in the Mughal Kot area [21,22]. Since its initial discovery in 1959, the Chiltan formation has served as a gas producing reservoir for various exploration and production companies. The formation comprises a wide range of carbonate units, varying from thin to thick-bedded, and includes irregular coarse grained, bioclastic and intraclastic limestones, that all indicative of deposition in shallow to marginal marine environments. The presence of age-diagnostic species of macro-nano fossils in this succession contribute significantly to severe diagenetic impacts on its reservoir potential [23,24]. The complexity of the reservoir is associated with its variable lithological composition, mineral content, pore space, conductivity, facies, and textures. These factors collectively pose challenges in recovery and increase exploration risks [25]. In the existing literature, there have been limited studies on the outcrop of the Chiltan Limestone, primarily focused on sedimentological and paleontological analyses. These studies aim to understand the diagenetic processes and depositional conditions of the formation, which can affects its reservoir quality [1]. However, these outcrop-based investigations provide insufficient information for effective reservoir quality management. Therefore, a comprehensive reservoir characterization and analysis are necessary to understand the diagenetic impacts on reservoir quality and improve recovery efficiency.

In this study, the Chiltan carbonate core samples have been utilized for the first time to conduct an integrated reservoir characterization. The primary objective of this research is to examine the impacts of diagenesis, depositional environment and overburden stress on reservoir quality using various methods like thin section petrography, mineralogy assessment, plug porosity, and gas permeability measurements under various overburden stress conditions. The study serves to address the key issues and challenges related to carbonate reservoir measurement and interpretation resulting from diagenesis. Ultimately, this research could lead to lower the risks associate with reservoir management and contribute to improve the productivity of indigenous resources.

1.1. Geological Settings of Study Area

The Lower Indus Basin is divided into central and southern basins by the Sukkur Rift Zone. The research region is situated in the eastern portion of Jacobabad-Khairpur High in an NNE-SSW orientation. Geographically, the area is primarily comprised of rocks from the Mesozoic age succession, with thick Jurassic sequences with a few outcrops of Triassic occurrences [26]. Despite the presence of shallow marine Eocene rocks; this region also exposes some of the oldest rocks, including those from the Triassic age (Wulgai formation) and Paleocene age (Dunghan Limestone). The Dunghan Limestone is deposited on the eastern side of the Jacobabad Khairpur High. Above the Cretaceous series, directly overlying the Middle Jurassic Chiltan formation, which showing well-known unconformity at the K-T boundary formed during collovian time throughout the Indus Basin [27,28]. Beyond the Cretaceous, the Paleocene Ranikot formation existed, and the sequence continued up to modern alluvium. According to data correlations and assumed thickness, the earlier Cretaceous and Middle Jurassic Chiltan formation are also present. The effects of collisional tectonics are limited to northern parts of Pakistan, with the Central Indus Basin largely unaffected. The surrounding regions underwent rifting during the Mesozoic succession, resulting in the formation of the Khairpur-Jacobabad High as depicted in Figure 1. Interestingly, the carbonate platform environment remained stable despite tectonic activity, that effectively producing subaqueous islands [29]. Chiltan Limestone is regarded as shelf carbonate sequence of Middle Jurassic age, characterized by thick layers of oolitic beds, including reefal development in the upper section. The Early Cretaceous interval includes pelagic Parh Limestone, Mughal Kot Formation and Pab sandstone followed by the Sembar shale, as well as Lower and Upper Goru sands in the lower part. The Eocene rocks overly the Paleocene sequence, while Oligocene Nari Formation sediments were deposited on top of the Eocene sequence. Additionally, the Siwaliks spread over the Indo-Pakistan Plate with unconformable contact [30,31]. The Chiltan Limestone and sands of Goru formations represent potential hydrocarbon resources in the region, with reservoirs ranging from shallow to deeper levels of Jurassic and Cretaceous age [31]. The intraformational and overlying shales act as seals, with anticline traps in the existing stratigraphic play. According to borehole data from exploration and production (E&P) companies, the stratigraphic column of the Southern Indus Basin spans from Triassic to modern alluvium as depicted in Figure 2.

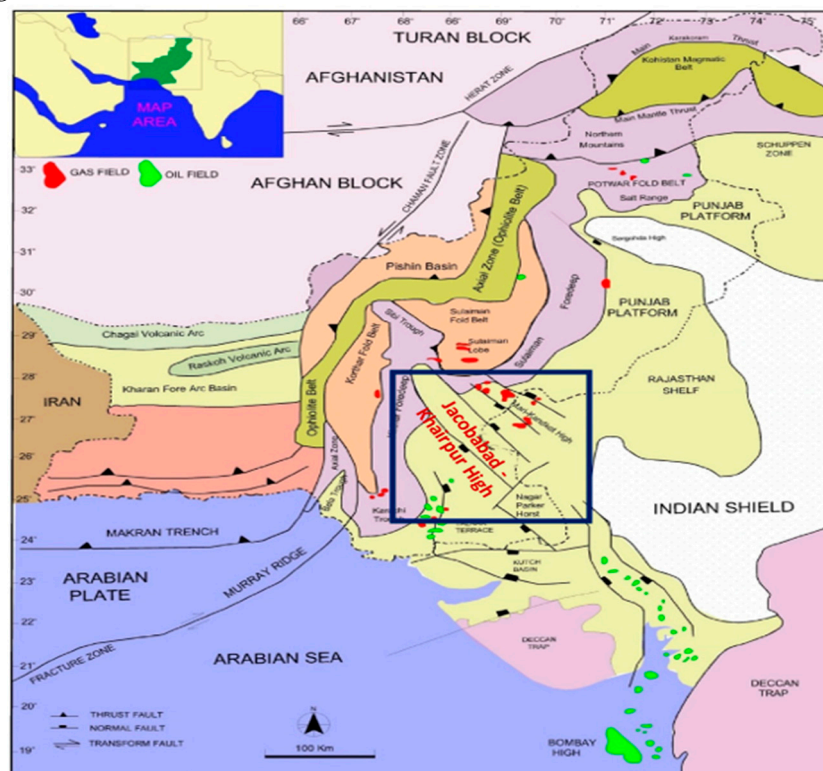


Figure 1. Tectonic history of adjoining regions of the study area.

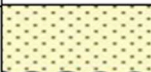





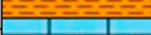


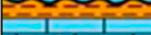

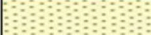
Era	Age	Group	Formation	Lithology	Reservoir Potential		
					Source	Seal	Reservoir
Cenozoic	Recent / Pliocene	Alluvium / Siwalik	Siwalik				
	Oligocene	Kirthar	Pir Koh MB.				*
			Sirki MB.			*	
			Habib Rahi MB.				*
	Eocene	Laki	Ghazij MB.			*	
			Sui Main Limestone				*
	Paleocene	RaniKot	Dhungan Limestone			*	
			Rani Kot/				
			Parh MB.				
	Cretaceous	Upper & Lower	Goru sandstone Intervals		*	*	*
Mesozoic			Sambar shell		*	*	
Mesozoic	Jurassic	Middle	Chiltan Limestone				*

Figure 2. Stratigraphic column of the study area showing petroleum play of different formations.

2. Materials and Methods

2.1. Materials and Preparation of core samples

The long cylindrical reservoir cores from the Middle Jurassic Chiltan Limestone formation were collected from subsurface core database Petcorelab, Hydrocarbon Development Institute of Pakistan, (HDIP) Islamabad, Pakistan. The selected core samples were prepared-through various core slabbing and core plugging procedures to create core plugs of the desired size. After labelling and tagging the samples, several core preparation techniques were employed for a comprehensive laboratory-scale investigation. The cylindrical core plugs, measuring 4.5cm in length and 2.5cm in diameter were prepared. A Standard procedure was followed to create 0.028mm polished, blue dyed stained thin sections and 3x3x2 mm cubical sample chips with carbon coatings for SEM-EDS analysis.

2.2. Characterization methods

The core samples of Chiltan carbonate formation were characterized through various techniques. The experimental workflow chart, with each specific procedure illustrated in Figure 3. This figure provides a visual representation of the entire experimental process of all undertaken procedures.

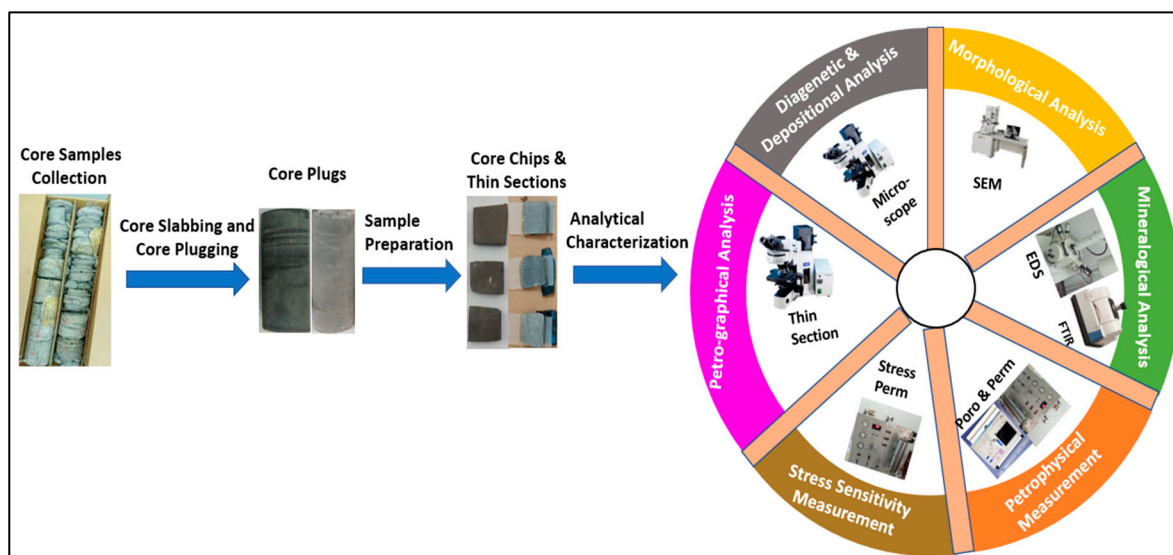


Figure 3. Schematic workflow of the Chiltan carbonate formation.

2.3. Petrographic and SEM analysis

The prepared thin sections were examined using a Polarized BX-51 microscope. To capture typical microphotographs of the obtained microfacies, a digital sight DS-U3 Nikon camera was attached to the microscope. Dunham's classification system was employed for petrographic analysis of the thin sections. Mineralogy, microstructure, and diagenetic interactions of the samples were examined through scanning electron microscopy (SEM) using a JEOL- JSM-6590LV, with a field emission Japan Compact SEM imaging interface software connected to a QUANTAX system for Energy Dispersive X-ray microanalysis (EDS analysis).

2.4. FTIR analysis

Fourier Transformed Infrared spectroscopy (FTIR) was conducted to confirm the carbonate mineralogy and identify any changes in mineral composition. The analysis was performed using a portable infrared spectrometer, ALPHA, by Bruker, Optik GmbH in Ettlingen, Germany.

2.5. Petrophysical measurements

Porosity measurements of selected core plugs were determined using the Coretest helium expansion PHI-220 porosity. Additionally, gas permeability and stress sensitivity assessments were carried out using the GP-12-2631 Temco permeameter under both ambient and various net stress conditions, with calculations based on Darcy equation [32].

$$k_g = 2\mu_g Q_b \frac{L}{A} (p_1^2 - p_2^2) \quad (1)$$

In this context, the core length is symbolized by L , cross-sectional area is denoted by A , μ_g represents gas viscosity, P_1 stands for the pressure across the core length (upstream pressure), and P_2 represents downstream pressure. The flow rate Q_b is directly related to gas permeability k_g .

2.6. Determination of klinkenberg permeability and stress sensitivity.

Steady-state gas permeability tests were conducted on 06 core samples at varying mean pore pressures to analyze the influence of gas slippage in heterogeneous carbonates. Nitrogen gas was injected into the core samples at different inlet pressures of 0.35, 0.52, 0.66, 0.82 and 1.02 atm, respectively, to determine gas permeability using **Equation (1)** of Darcy law, while keeping the pressure drop constant at 0.25atm. The Klinkenberg permeability expressed by following equation. [33].

$$k_g = k_{\infty} \left[1 + \frac{b}{P_{av}} \right] \quad (2)$$

Here, b represents the Klinkenberg constant, also known as gas slippage factor and k_{∞} denotes the Klinkenberg or absolute permeability. The gas slippage factor, b was determined using following equation [34].

$$b = \frac{(4C\lambda P_{av})}{rslip} \quad (3)$$

Where C is a constant of the order of 1, dependent on pore throat geometry and λ represents free path length of gas molecules and calculated using given below equation [35].

$$\lambda = \frac{\mu}{P_{av}} \sqrt{RT\pi/2M} \quad (4)$$

Here, R is the gas constant, M is the molar mass of gas, and T refers to absolute temperature. The influence of the Klinkenberg constant on pore throat structure was determined by the absolute permeability k_{∞} and expressed by following equation [36].

$$k_{\infty} = ak_g + b \quad (5)$$

In the pore throat relation between Klinkenberg permeability k_{∞} and measured permeability k_g , a represents the slope, and b represents the intercept. Stress sensitivity was also conducted to assess the impact of stress on carbonate rock permeability and pore throat structure at various stress conditions. The net stress is described by below given equation. [18].

$$\sigma' = \sigma_c - n_k p_p \quad (6)$$

Where n_k represents the stress coefficient, which is assumed as 1 for effective stress calculation without significant error. The coefficient value is typically greater than 1 for conventional rocks and less than 1 for rocks rich in clay content [37]. To analyze the combined effect of net confining stress and slippage factor at different pore pressures on slippage parameters, a model Equation was employed as follows.

$$k_{\infty} = K_a [1 + b/Pm] (\sigma_c - n_k p_p)^{-\gamma} \quad (7)$$

Where γ denotes the stress exponent, and k_{∞} is corrected or absolute Klinkenberg permeability.

3. Results and Discussion

The primary objective of this research was to undertake a thorough and integrated analysis of the Chiltan carbonate reservoir, aiming to explore the influence of diagenesis, depositional settings, and overburden stress on its potential reservoir quality. The characterization of reservoir involved thin section petrography, SEM, EDS, plug porosity and gas permeability, as well as stress sensitivity, all aimed at gaining a comprehensive understanding of reservoir heterogeneity and its impact on reservoir performance. The results of each analysis are detailed subsequently as follows.

3.1. Microfacies Analysis and Petrographic Description

Based on thin section petrographic investigations, three distinct microfacies were identified and categorized as follows: intraclastic packestone (MF1), bioclastic pellioidal packestone (MF2), and bioclastic ooidal grainstone (MF3), all indicative of shoal and lagoon environment.

MF1 is characterized by dark gray limestone displaying an intraclastic packestone texture. It consists of fine grained to medium size particles embedded with calcite, micrite cement and various bioclasts such as intraclasts, peloids, ooids, and pellets. Several diagenetic features, including induced calcite fractures, and tectonic fractures were observed in these microfacies. MF2 exhibits a light-pale gray bioclastic pellioidal packestone composed of fine to medium sized particles surrounded by variety of micro-nano fossils, including pellioids, bioclasts, algae, and gastropods. Common diagenetic shifts associated with a shoal environment include cementation, micritization and neomorphism, which were observed in these microfacies. MF3 is characterized by mild gray bioclastic grainstone containing euhedral to anhedral Ferron dolomite crystals. It features an accumulation of various micro-nano fossils, such as bioclasts, milioids, bivalves, echinoderms, and branchiopods.

Digenetic features observed in these microfacies include intense micritization, cementation and induced calcite fractures.

In petrography, the analysis revealed that the samples predominantly consist of limestone composition with some dolomite crystals as seen in Figure 4. Thin section analysis further unveiled that the examined core samples exhibit three distinct microfacies characterized by packestone and grainstone textures, ranging in color from dark grey to light brownish. These microfacies contain various bioclasts and intraclasts with diverse allochems. Visual estimates indicate that calcite, micrite, spar cement matrix and ferruginous clay content make up approximately 60-65% of microfacies in both packestones. In contrast, around 30-35% of the relative average allochems consists of intraclasts, bioclasts (bivalves and gastropods), and pallets in MF1, as shown in Figure 4(a & b). MF2, on the other hand, is predominantly composed of pelioids, bioclasts, algae, gastropods, and echinoderms, each with distinct ratios observed in Figure 4(c & d). The analysis also revealed vuggy, or solution and fracture porosity was ranging from to 2-5%, as depicted in Figure 4(a & d). Additionally, the unusual presence of siliciclastic quartz, appearing as rounded fine grained particles randomly arranged, as noted in Figure 4(a & d). In MF3 grainstone microfacies, visual estimates suggest that approximately 25-30% is comprised of cement with some ferron dolomite crystals, while 60-65% consist of allochems as observed in microphotographs. Various undifferentiated bioclasts, miliolid, foraminifers, echinoids, peloids, intraclasts, and ooids were identified in the analysis, as displayed in Figure 4(e & f). Additionally, minute traces of silici-clastic quartz were also observed in all three microfacies, as shown in Figure 4. The petrographic details of observed microfacies are provided in Table 1.

Table 1. Petrographic illustration of visual estimates for observed microfacies of the Chiltan formation.

Microfacies	Carbonate Grains			Cement		Estimated	Dominant Pore Type	Diagenetic Features	Depositional Environment
Lithology	Bio-clasts %	Intraclasts/ Echinoderm %	Peloids/ Ooids %	Calcite %	Micrite %	Visual Porosity (Thin Section)			
Intra-clastic Ooidal packestone	05%	20%	10%	35%	25%	Bad porosity up-to 5%	Primary porosity is limited. Secondary porosity is developed because of Stylolization	Intra-Formational Clasts, Calcite veins, Neomorphism stylolization	Shoal
Bioclastic grainstone	25%	25%	15%	20%	13%	Bad porosity up-to 2-3%	Primary porosity is limited. Secondary porosity developed due to grain dissolution	Calcite vein, Cementation, Dissolution, Dolomitization	Lagoon
Pelliodal Packestone	15%	05%	15%	40%	20%	Bad porosity up-to 2-5%	Primary porosity is limited. Secondary porosity developed due to grain dissolution	Calcite vein, Cementation, Dissolution, Dolomitization	Lagoon

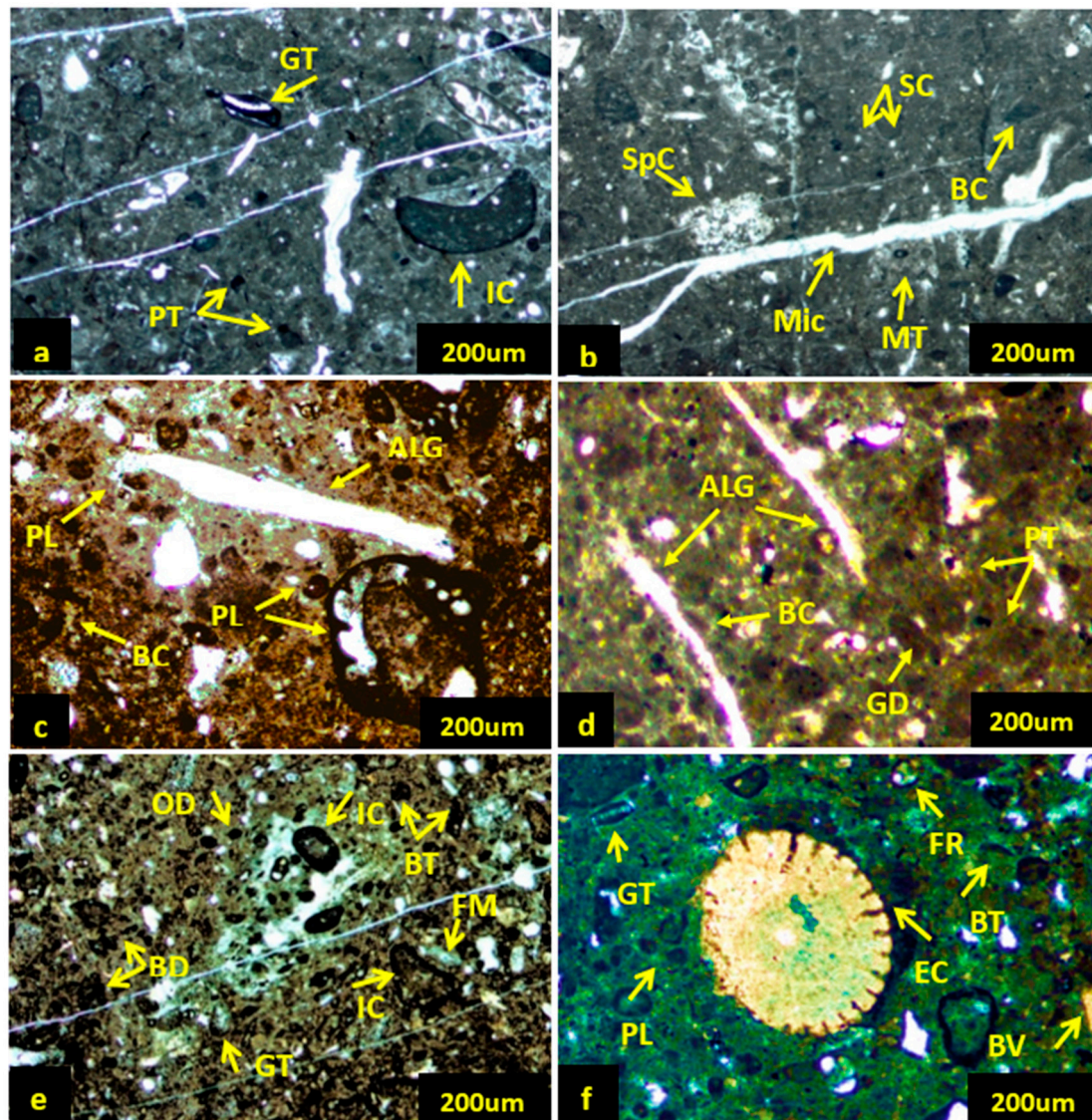


Figure 4. Thin section microphotographs of the Chiltan formation displaying identified microfacies MF1 (a-b), MF2 (c-d) and MF3 (e-f). pellets (PT), intraclasts (IT), gastropods (GT), bioclasts (BT), bivalves (BV), silicic clasts (SC), pellets (PL), echinoderms (EC), ooids (OD), foraminifera (FR), matrix (MT), Stylolite disintegration (SD), vuggy porosity (VP), cement filled evaporate (FM), spar cement (SpC), fracture porosity (FP), micrite cement (Mlc), branchiopods (BD), neo-morphed Algae (ALG).

The petrography and microfacies analysis of thin sections have illuminated the key diagenetic features and microstructure present in the examined microfacies. The microfacies were categorized using Dunham classification to identify grain size, cement type and matrices. Semi-quantitative data regarding carbonate constituents in the percentages were calculated using visual estimation charts developed by Baccelle and Bosellini [38]. The examination highly revealed bio-mineralized by-products indicative of shallow marine environment, including fossils fragments, carbonate sediments and surrounding cement muds. The predominance of micrite cement suggests a relatively quiet depositional environment, while the bivalves and gastropods points to limited water conditions observed in both microfacies [39,40]. The presence of bioclasts such as bivalve shells and other skeletal fragments indicates a moderately saline shallow marine environment. Intraclasts, bioclasts, cement, and ooids on the other hand, are indicative of high-tide conditions near seashore [41]. Allochems were found to be micritized in the observed microfacies, with some partially micritized rims particularly in case of bivalves. This suggests the reworking of low grains in high-energy environments.

3.2. Diagenesis and Identified Features

Diagenesis begins early during the interaction of sediment with water, although many diagenetic processes occur after deposition. Diagenesis exerts a significant impact on petrophysical properties, leading to an increase in reservoir heterogeneity. This complexity results in a reduction in porosity, permeability and micropore structure, which eventually affecting the reservoir quality [32,42]. Through petrography and SEM analyses, considerable diagenetic development was observed, characterized by stronger grain contacts and alteration of primary sedimentary features. These features include well-sorted fine-grained sediments and diversified clay minerals, which typically form tight reservoirs with low porosity and low permeability [42,43]. This research identified several diagenetic processes that modify the configuration of carbonate rocks over time, including micritization, cementation, compaction, dissolution, and dolomitizations. Different diagenetic processes with identified features through bio-stratigraphy analysis are discussed as under:

3.2.1. Micritization

Micritization was observed as an early diagenetic event that adversely affects the reservoir quality by altering the intrinsic characteristics of skeletal grains and microbial activity. Microscopic degradation of bioclasts was found to be highly significant in the examined samples, potentially creating a depositional micrite matrix, as depicted in Figure 5a. SEM imaging further confirmed that micrite underwent recrystallization, leading to the formation of microcrystalline calcite, as shown in Figure 5b. The micritization of allochems primarily occurs in shallow waters due to activity of algae boring (endolithic) organisms, which ultimately leads to the generation of peloids [39,44].

3.2.2. Dissolution

Dissolution or leaching of metastable bioclasts, because of circulation of the meteoric fluids, was frequently observed in petrography and SEM analysis, as shown in Figure 5(c & d). During dissolution, the micrite matrix disintegrates first, primarily during early marine and meteoric diagenesis due to methane exhalation resulting from algal decomposition [45]. This type of dissolution is common in packstone microfacies found in lagoons environment. Later stages of dissolution involve disintegration of dolomite grains, stylolitization, cementation and enlargement of fracture as observed in Figure 5(c & d). This dissolution follows the early diagenetic phase of burial diagenesis. Carbonate cement precipitates in the pores of allochems under strong shoal conditions. The retention of organic matter is limited by the constant refilling of pore spaces by oceanic water. Thus, disintegration of cement during early diagenesis cannot be attributed to the decomposing of organic materials. [39].

3.2.3. Cementation

Calcite cementation was frequently observed in the analysis, along with a small amount of ferroan-dolomite cement, blocky cement, isopach fibrous and drusy mosaic cement, as shown in Figure 5. The pore-filling calcite cement was found between the fossils, creating granular and drusy mosaic cement, as identified in Figure 5(e & g). Dolomite cement crystals were also found with defined shapes, ranging from euhedral to anhedral in packstone-grainstone microfacies. Isopachous fibrous cement is an initial stage cement that precipitated around the bioclasts and intraclasts, gradually encasing the fossils over time, as identified in Figure 5(e & g). This cement type formed in a marine diagenetic environment with high content of calcium carbonate and low clastic influx [7,46]. Blocky cement was frequently found in grainstone microfacies and precipitated in three distinct phases; intergranular, intraskeletal molds and fractures, as observed in Figure 5(e & f). The paragenetic sequence of cementation involves precipitation between allochems, grains dissolution and fractures through fossils, indicating its recent development.

3.2.4. Compaction

Two types of compactions have been observed in the examined samples. Mechanical compaction, caused by microscopic fractures in deep burial diagenesis is evident, with fractures slashing through allochems and calcite filling in open fractures, as observed in Figure 5(f & g). Physical compaction resulted from grain contacts, breaking, and deformation induced by sediment overburden. The presence of stylolites and matrix supported rocks serves as indicators of chemical compaction, as shown in Figure 5(a & f). Mechanical compaction may result from overburden stress, while chemical changes are sensitive to factors such as temperature, pressure and water volume in pore spaces [47].

3.2.5. Neomorphism

Several neomorphic processes were observed during the analysis, including the replacement and recrystallization of bioclasts and the microscopic matrix. Neomorphism became progressively evident because of partial to total recrystallization of skeletal components. Calcite with high magnesium content accumulates in fossil bioclasts under meteoric to burial conditions and replaces the bioclasts with a crystalline form in a systematic manner, as observed in Figure 5(c, g, h).

3.2.6. Dolomitization

Dolomite crystals were observed in the garinstone microfacies of the Chiltan formation. These dolomite crystals were found to be fine to medium grained and displayed subhedral to rhombohedral shapes, indicating their sequential evolution under ambient fluid chemistry, as seen in Figure 5(e & f). The dolomite crystals in this form are composed of ferroan material, as revealed by SEM and EDS analysis. Additionally, some ankerite crystals were found within the dolomite rhombs, suggesting that when magnesium is replaced by iron, dolomite first becomes ferroan dolomite and then ankerite, as shown in Figure 5e. Mg ions are released from clays associate with carbonates to form ferroan dolomite during early-stage burial diagenesis, and over time Fe ions gradually replace the Mg ions, as indicated by the EDS patterns.

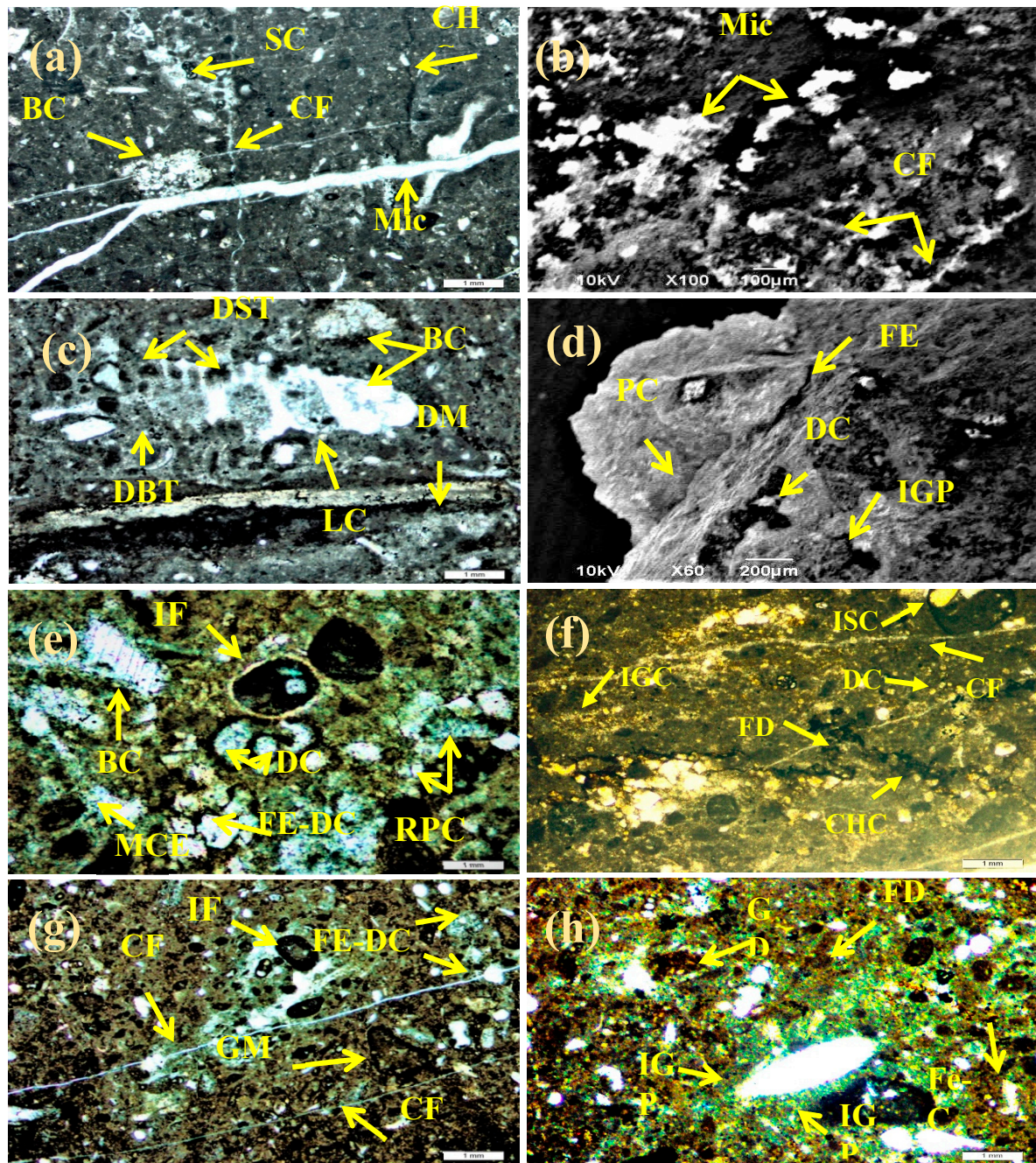


Figure 5. Showing thin section microphotographs (a, c, and e-h) and SEM microphotographs (b and d) of the Chiltan carbonate formation indicating different diagenetic features. Cement micritization (MIC), Dissolution of stylolite (DST), Dissolution of bioclasts (DBT), Dissolution of micrite cement (DM), Intragranular pores (IGP), Drusy cement (DC), Fracture enlargement (FE), Isopach fibrous cement (IF), Angular mosaic cement (GM), Dolomite crystals (DC), Blocky cement (BC), Spar cement (SC), Calcite filled fractures (CF), Physical compaction (PC), Low magnesium calcite (LC), Replacement and recrystallization (RPC), Grain Dissolution (GD), fracture dissolution (FD), ferron dolomite crystals (FE-DC), micrite envelop (MCE), clay minerals (GM).

3.3. Depositional Environment and Diagenetic history reconstruction

The depositional environment of the Chiltan formation is classified on various identified facies and their depositional settings. The Chiltan Formation is interpreted to have been deposited approximately 17 million years ago (Ma). The numerical ages are distributed, and the relative sea level interpreted the second order rise cycle over the long term, characterized by composite

transgressive tract systems. In the short term, it exhibits two episodes of third-order cycles of rising and falling sea level, while the Haq curve comprises three episodes [48]. The absence of a single event in the Chiltan formation may be due to the local tectonic activity. The Chiltan formation exhibits a complex diagenetic history, marked by several diagenetic settings and events that have taken place and altered the primary sedimentary structures. This diagenetic history suggests the presence of both high-energy tidal shoal and low energy wave lagoons inner shelf settings. The presence of ooids and peloids is indicative of wave-disturbed, shallow water, and high energy conditions. Sand shoals/barrier and grainstone facies separate the open marine from the restricted-marine environment, with several effects of early marine to meteoric diagenesis [49]. Conversely, the presence of dolomite crystals, neomorphism and dissolution of biotic components suggests burial settings below storm wave base depositional phase, as shown in Figure 6.

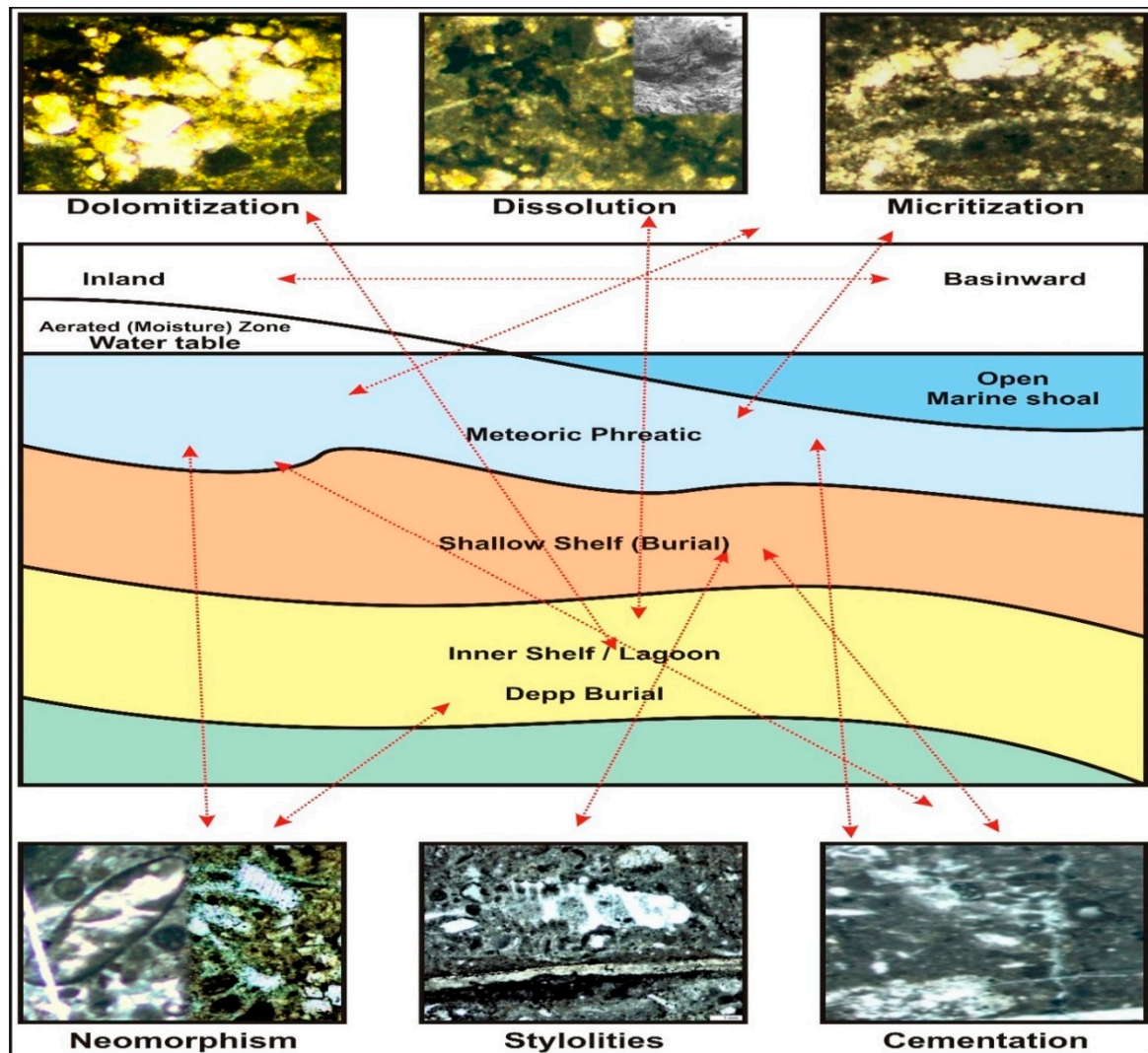


Figure 6. Schematic Depositional phases and diagenetic environments proposed for the Chiltan Limestone.

The order of diagenetic processes was established to identify the paragenetic relationships during the diagenetic study. These processes include micritization, cementation, dissolution, compaction, fracturing, and vein filling occurring in distinct diagenetic environments like marine, meteoric and burial as identified in Figure 7. The early marine diagenetic settings encompass micritization of allochems, matrix disintegration and precipitation of isopachous fibrous cement, as observed during this phase. Micritization was caused by micro-boring organisms that partially destroy the grains at sediment-water interface and forming a micrite envelope. Isopachous calcite cement is an early marine cementation process which primarily restricted to open sea environment,

leading to the early lithification of grains and the preservation of porosity [50,51]. Meteoric diagenesis follows early marine diagenesis and is characterized by the dissolution of granular and drusy mosaic cement, resulting in the formation of vugs and molds, as identified in Figure 7. Meteoric diagenesis precedes burial diagenesis, which is characterized by marine cementation and dissolution. consequently, the pore spaces associated to stylolites, dolomite, and fractures cannot be expand or bridged [52]. Following meteoric diagenesis, pore-filling cement and blocky cement were recognized as evidence of shallow burial settings, identified from micro-fractures, displaced grains, neomorphism and recrystallization. Deep burial diagenesis occurs at depths of hundreds of meters and involves various alterations like stylolitization, calcite vein filling, formation of coarse-grained dolomite crystals, compaction and neomorphism. The dolomites were formed by the release of Mg and Fe ions from clay during deep burial diagenesis, associated with stylolites [51,53].

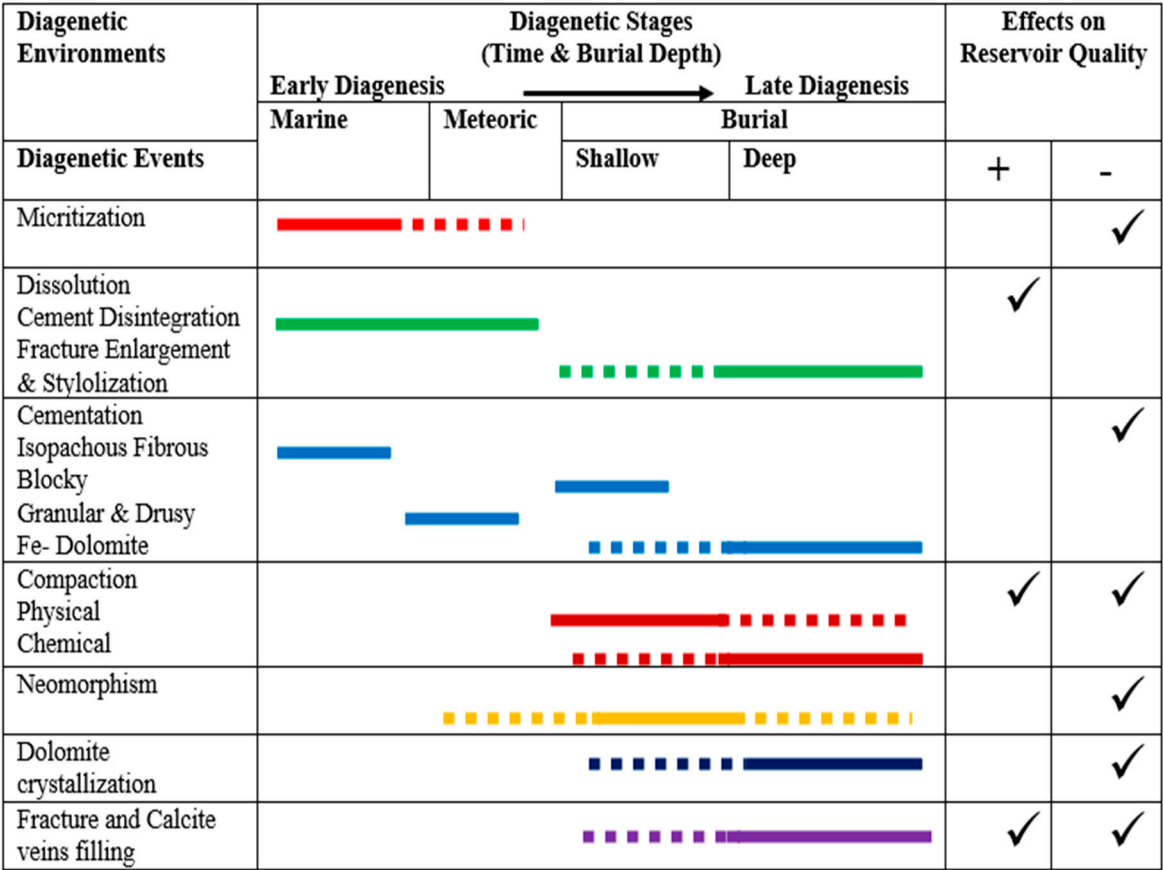


Figure 7. Sequential occurrences of diagenetic events and features with impacts on reservoir quality.

3.4. Mineralogical Analysis

The mineral constituents of Chiltan limestone were analyzed through SEM-EDS, FTIR and thin sections. The observed mineralogy of the examined samples contains calcite, dolomite, and an intermix of clay and cementing materials as dominant mineral components. Furthermore, the presence of aluminum (Al), silicon (Si), iron (Fe), Sodium (Na), clay and cementing material were also observed. These minerals form the grain structure of carbonate rocks and detected in SEM-EDS patterns, as shown in Figure 8(a & c). Calcium intermixed with magnesium (Mg) in the presence of Fe and formed saddle ferron dolomites. Meanwhile, the exposure of silicon (Si), aluminum (Al), sulfur (S), and sodium (Na) indicates the presence of clay minerals intermixed with silici-clastic influx, likely forming micrite, as shown in Figure 8(a & c). The detailed mineral composition obtained from EDS analysis, along with their weight percentages (%), is shown in Table 2. Mineral compositions were compared with spectral bands in analysis to identify any changes in the mineral structures of the examined samples. The minerals within the specimen can be identified by detected

absorption spectra. The FTIR investigation shows that low-Mg calcite predominates in both samples, despite a small high-Mg calcite phase being observed in analysis, as shown in Figure 9. The carbonate phases were determined based on the peak wavenumbers of absorption bands. Dolomite phase was identified with three absorption bands of spectrum peak wavenumbers in sample 2, while a huntite phase (Mg rich content) was also observed with several bands in the spectrum. Furthermore, the absorption spectra of several tested minerals like quartz, feldspar, and kaolinite were also identified as non-carbonate phases.

Table 2. Mineral composition of Chiltan limestone.

Element	Atomic No.	Mass Norm. %	Weight, %
Oxygen	8	50.90	71.46
Calcium	20	42.09	23.59
Iron	26	1.92	0.77
Aluminum	13	0.94	0.78
Silicon	14	2.86	2.29
Sulphur	16	0.43	0.30
Magnesium	12	0.57	0.53
Sodium	11	0.28	0.28

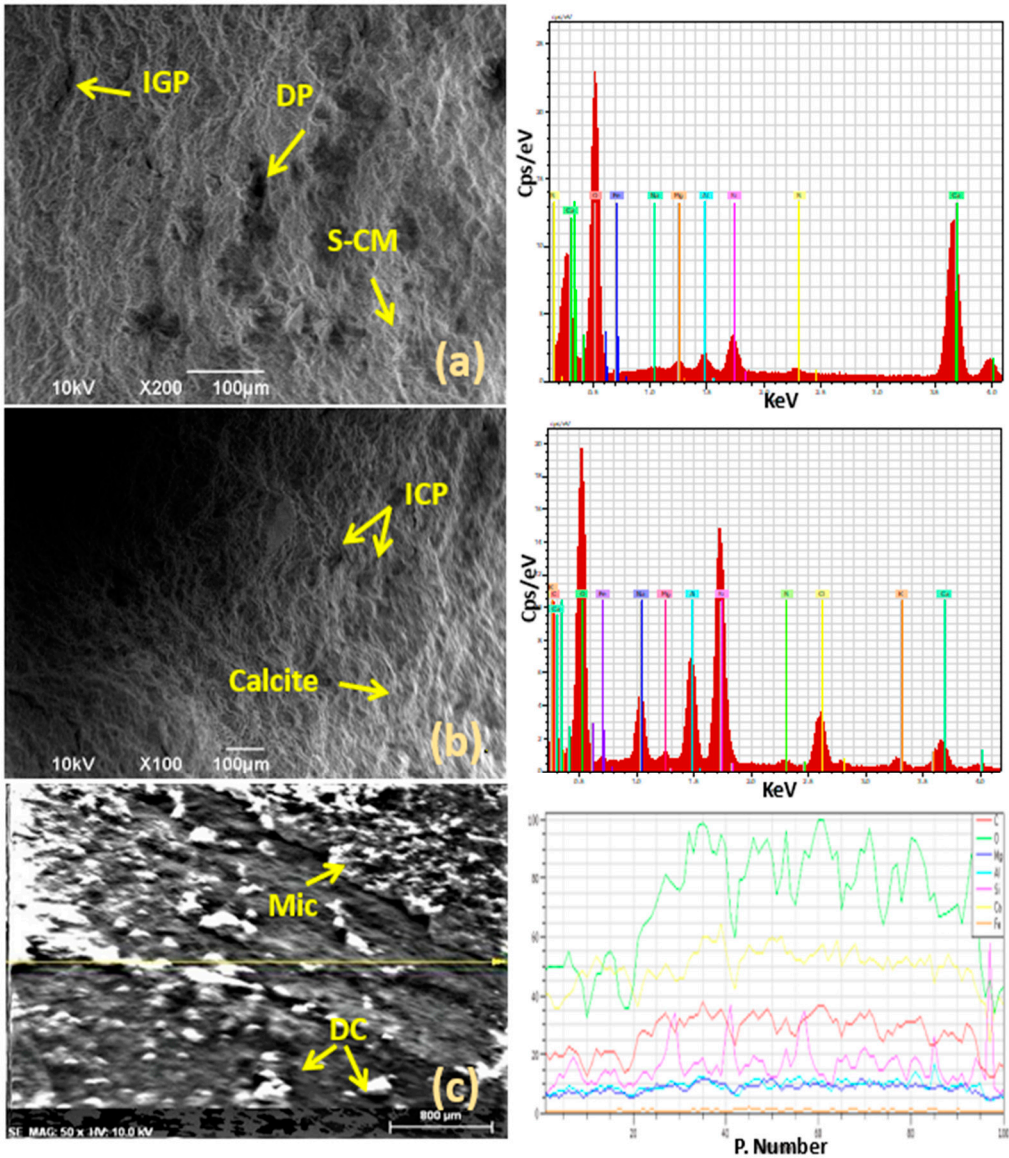


Figure 8. SEM microphotographs (a, b, and c) and EDS Patterns of studied Chiltan formation indicating various minerals and diagenetic features. Dissolution pores (DP), intragranular pores (IGP), silici-clastic minerals (S-CM), intracrystalline pores (ICP), micrite (Mic), dolomite crystals (DC).

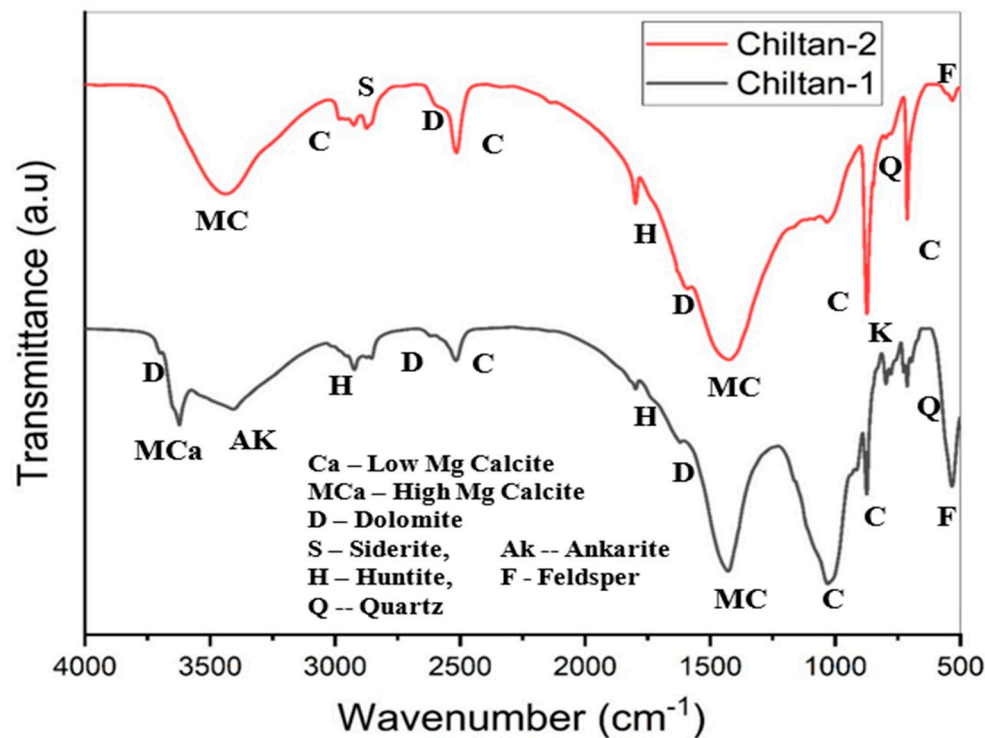


Figure 9. FTIR analysis of Chiltan carbonate formation.

According to the findings from FTIR analysis, Chiltan limestone exhibits a diverse range of carbonate phases. However, pure calcite (with low magnesium content, CaCO_3) is commonly found, characterized by peak wavenumbers at 850cm^{-1} , 1050cm^{-1} , 2500cm^{-1} and 3100cm^{-1} , as observed from Figure 9. An increase in magnesium content results in a shift of peak wavenumber positions from calcite to dolomite, while peak wavenumbers for huntite and magnesite are greater than those for dolomite [54]. Varying magnesium contents give rise to a range of high-Mg calcite [$\text{Ca}_{1-n}\text{Mg}_n(\text{CO}_3)$] bands observed in analysis. In high-Mg calcite matrices, Ca^{2+} ions are replaced by Mg^{2+} , leading to an increase in wavenumbers. This phenomenon has also been reported in binary and ternary carbonate solid solution systems [55–57]. Based on SEM, EDS, FTIR and thin section analyses, the most prevalent carbonate cements in Chiltan limestone include calcite, ferroan dolomites, micrite muds and some clay minerals, which can impact carbonate quality through mineral precipitation. Additionally, some terrigenous sediment, grain coatings, huntite minerals and kaolinite clay were also identified, which could influence the quality of carbonate reservoir.

3.5. Petrophysical Measurements

For petrophysical assessment, density, porosity, and permeability of core plugs from each microfacies were determined. The relatively average density of the core samples was 2.664 g/cc . The relationship between bulk density and porosity was calculated to identify the degree of reservoir homogeneity. The observed relationship was linear and inverse with a weak correlation, as shown in Figure 10a. This suggests that the rock samples had variable mineralogical structures, grain shape, packing, and fabric resulting in a non-uniform and heterogenous pore structure. The measured matrix porosity ranged from 0.52% to 6.4% with an average of 3.4% , while the permeability values ranged from 0.18 to 1.69 mD with an average of 0.449 mD . It was also observed from porosity determination that wackestone microfacies had somewhat larger plug porosity values compared to

the grainstone. Estimated visual porosity during microfacies analysis ranged from 2-4%, including intergranular, intracrystalline and dissolution porosities, which were distinguished by SEM analysis in Figure 8(a - c). The plotted permeability and porosity data did not show a strong correlation and demonstrated a linear relationship with a weak coefficient due to the varied pore size and pore throat network, as shown in Figure 10b. This complexity of the pore structure significantly impacts on fluid flow properties, which can be determined through rigorous porosity and permeability relationships. Few deviations in the cross-plotted data points were observed, indicating the presence of micro cracks, as confirmed by thin section and SEM analysis.

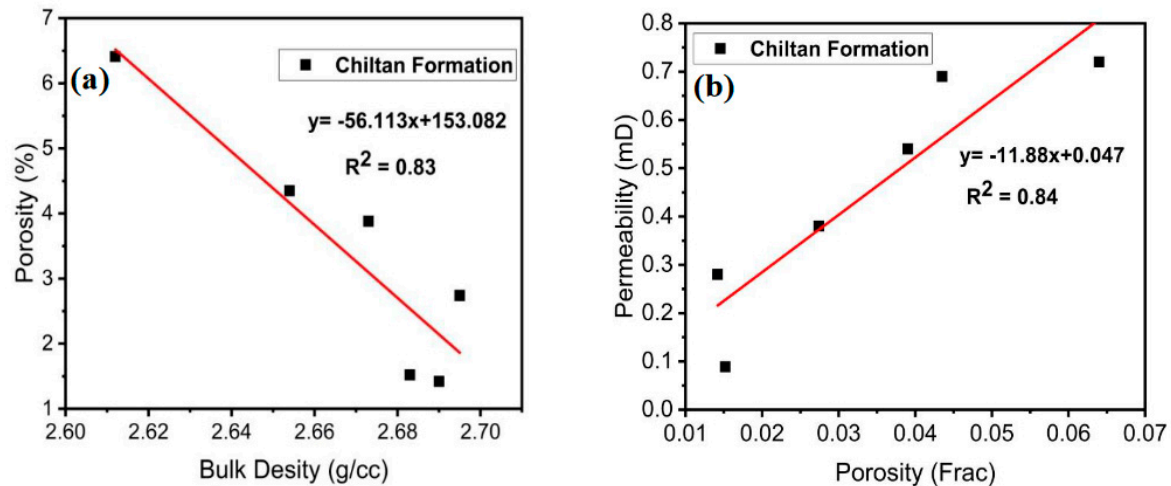


Figure 10. (a) Relationship between Porosity Vs Bulk Density, (b) relationship between Permeability Vs Porosity.

3.6. Klinkenberg Corrected Permeability and Gas Slippage Factor

Tight permeability rocks are sensitive to stress and pore pressure, which can lead to gas molecules slippage at low pore pressures, resulting in an increase in the measured permeability. This slippage effect occurs due to the difference between free path of the gas molecules and pore-throat sizes [58,59]. The account for the gas slippage effects in low permeability cores at low pore pressures, the measured permeability is often corrected using the Klinkenberg permeability method in current studies. Therefore, a practical method was established to calculate Klinkenberg permeability and the gas slippage factor in the low permeable Chiltan carbonate formation. Different empirical equations were utilized to determine the Klinkenberg corrected permeability based on the observed pore-throat geometries of the examined samples. Figure 11 illustrates the linear relationship between permeability coefficients (k_g) and the reciprocal of average pore pressure ($1/P_{av}$) under varying pore pressure conditions using Equation (1). The Klinkenberg permeability was determined by extrapolating the gas permeability line to zero. The obtained regression for the measured data was found to be satisfactory, with a coefficient of determination (R^2) equal to 0.994. The gas permeabilities measured at various mean pore pressures and identified Klinkenberg permeability values of 6 carbonate core samples are provided in Table 3.

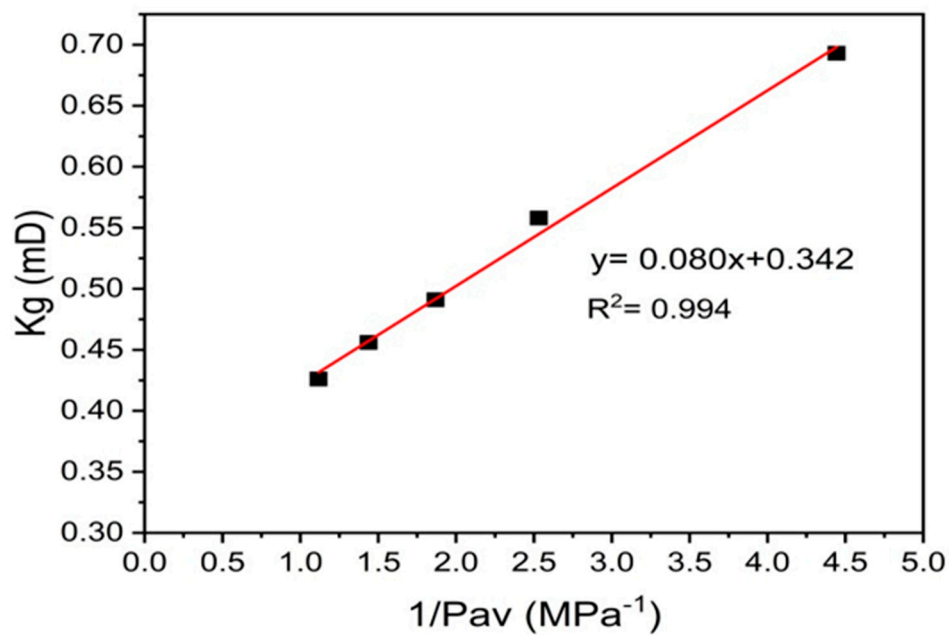


Figure 11. Measured gas permeability versus reciprocal mean pore pressure of sample # 03.

Table 3. Gas Permeability Data sheet and adjusted parameters at different mean pore pressures @ 500psi stress condition.

Sample ID:	Parameters	Mean Pore Pressure					Klinkenberg Permeability (mD)
		0.225	0.395	0.535	0.695	0.895	
23-CHL-01	Gas Permeability (K_g), mD	0.693	0.558	0.491	0.45	0.426	0.343
	Slip radius (r_{slip}), μm	1.5	1.39	1.49	1.59	1.59	
	Gas slip factor (b_k), psi	14.01	26.52	33.49	40.78	52.56	
23-CHL-2A	Gas Permeability (K_g), mD	0.543	0.41	0.322	0.289	0.257	0.168
	Slip radius (r_{slip}), μm	0.68	0.6	0.7	0.69	0.72	
	Gas slip factor (b_k), psi	30.64	60.94	71.14	94.32	115.06	
23-CHL-03	Gas Permeability (K_g), mD	0.089	0.059	0.042	0.036	0.031	0.011
	Slip radius (r_{slip}), μm	0.21	0.2	0.22	0.21	0.21	
	Gas slip factor (b_k), psi	175.2	184.6	218.72	236.7	246.3	
23-CHL-4B	Gas Permeability (K_g), mD	0.712	0.502	0.408	0.341	0.273	0.153
	Slip radius (r_{slip}), μm	0.41	0.38	0.38	0.4	0.48	
	Gas slip factor (b_k), psi	50.15	96.5	129.36	160.94	170.36	
23-CHL-05	Gas Permeability (K_g), mD	0.381	0.251	0.173	0.149	0.112	0.027
	Slip radius (r_{slip}), μm	0.12	0.1	0.19	0.11	0.12	
	Gas slip factor (b_k), psi	179.18	185.7	190.3	204.5	210.4	
23-CHL-06	Gas Permeability (K_g), mD	0.283	0.186	0.132	0.112	0.095	0.032
	Slip radius (r_{slip}), μm	0.19	0.18	0.21	0.2	0.19	
	Gas slip factor (b_k), psi	107.67	243.6	242.54	251.2	263.1	

To calculate the gas slippage factor (b), a straight line was fitted to the permeability data obtained from Klinkenberg tests using Equation (2) & (3). The outcome that could be fitted to a straight line with a correlation coefficient of greater than 0.79 for 30 data points were considered for the study. It was observed that there was variation and scattering in the data regarding the relationship between gas permeability (k_g) and gas slip factor (b_k), as shown in Figure 12, and other relevant data are presented in Table 3. The variation in slippage parameters and permeability may be attributed to the heterogeneity in carbonate rocks and non-uniform pore sizes in the samples under study. Consequently, it is evident that permeability results cannot be reliably calculated using available empirical correlations, as carbonate rocks exhibit significant heterogeneity and a variety of pore geometries [18]. The slippage effect in a conventional reservoir core is negligible due to larger pore

radius, and gas slip factor becomes close to zero. In contrast, a tight reservoir core possesses a very small pore radius and has significant effect on gas flow [34,60].

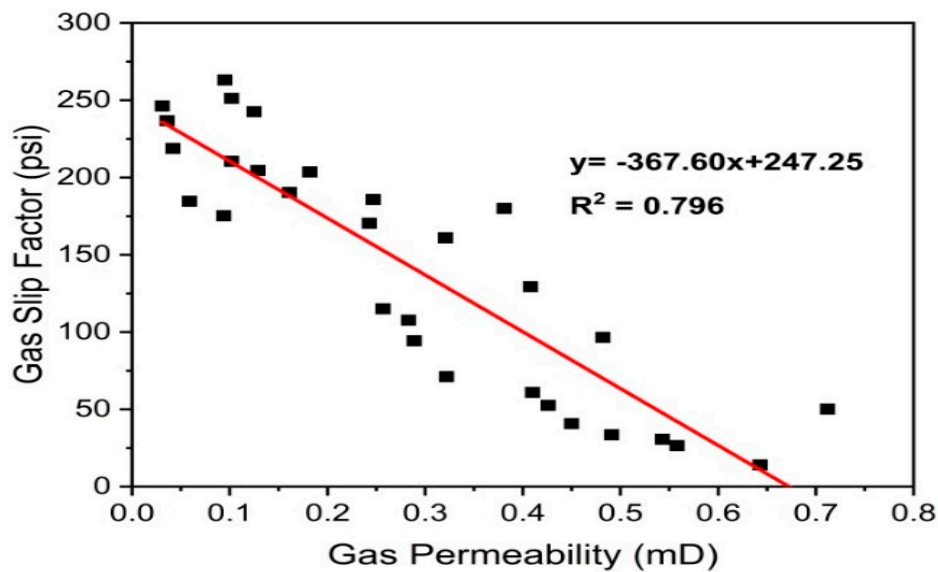


Figure 12. Relationship between gas slip factors versus measured gas permeability of studied carbonate samples.

Furthermore, it was observed that the gas slippage effect increases the permeability at reduced pore pressure. This indicates that gas molecules have longer free paths than the pore throat diameter, which depends on effective pore size (r_{slip}). Therefore, the pore-throat structure of core samples has a significant impact on the Klinkenberg constant, which describes the difference between the measured gas permeability (k_g) and Klinkenberg permeability (k_∞). The calculated values of effective pore size (r_{slip}) and gas slip factor (b_k) for Klinkenberg permeability of the studied samples at different mean pore pressures were determined using Equation. (2), (3), & (4) and provided Table 3. The linear relationship between k_∞ and k_g at various mean pore pressures was also observed using Equation (5) and illustrated in Figure 13. The corrected Klinkenberg permeability did not precisely match the average gas permeability at different mean pore pressures. This discrepancy can be attributed to the heterogeneity of carbonate rock and varying pore throat geometry of different lithofacies caused by diagenesis. Sample #03 is the only one that closely approximates the experimental results, with an average gas permeability of 0.21mD, which is somewhat close to corrected Klinkenberg permeability 0.11mD, as mentioned in Table 3. Carbonates possess secondary porosity and fracture permeability due to their heterogeneity. Therefore, laboratory measurements of reservoir properties, such as special core analysis (SCAL) are essential for understanding reservoir performance.

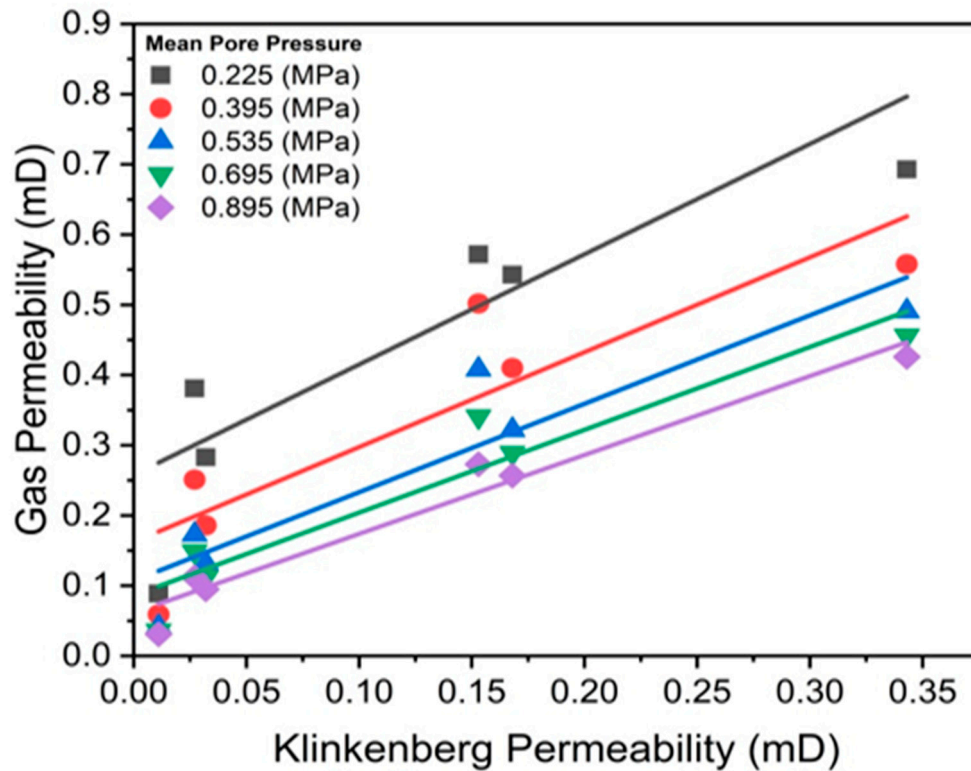


Figure 13. Relation between Corrected Klinkenberg Permeability versus measures gas permeability at different mean pore pressures.

3.7. Effect of Overburden Stress

Overburden stress can significantly reduce the permeability of low-permeable reservoirs, with a profound impact on pore morphology, geometry, and petrophysical properties. Carbonate reservoirs are particularly sensitive due to their complex lithofacies and diagenetic processes, which affects the reservoir quality and recovery [20]. According to experimental findings using Equation (6) & (7), gas permeability exhibits an inverse relationship and decreases with an increase in net stress, as illustrated in Figure 14. This suggests that an increase in net stress leads to a decrease in pore pressure, resulting in increased permeability due to the gas slippage effect. This effect allows gas to flow more easily through the pores. Furthermore, it was observed that an increase in net stress resulted in a decrease in absolute permeability, as shown in Figure 15.

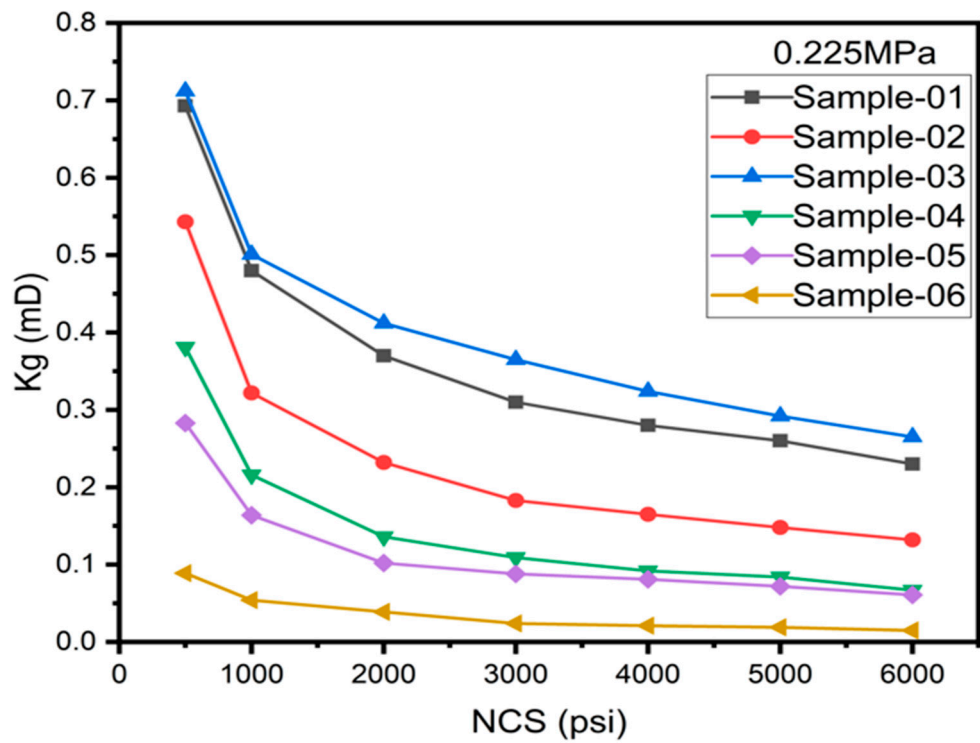


Figure 14. Permeability versus Net confining stress relation.

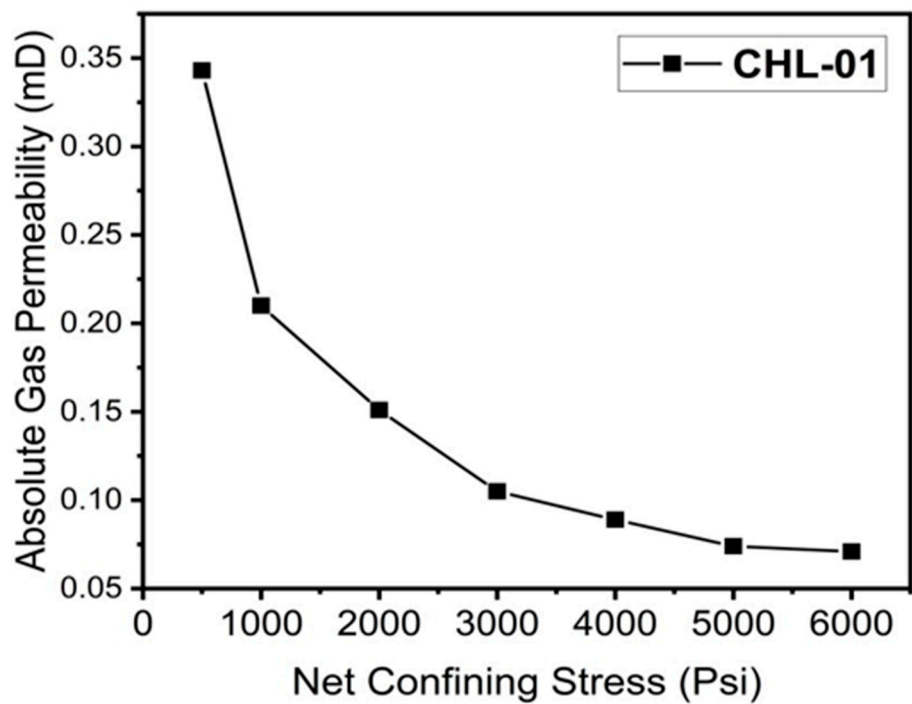


Figure 15. Relationship between Absolute gas permeability and Net confining stress.

This implies that at lower stress levels, an increase in net stress leads to a decrease in permeability due to gas slippage effect, which becomes less pronounced at high pore pressure. The increased flow due to slippage effect compensates for the reduction in slip-adjusted permeability, resulting in larger decrease in permeabilities at higher net stresses and low pore pressures. The higher

reduction in permeability at lower overburden stress was confirmed through micro-cracks, as identified in few samples by SEM and thin section analysis shown in Figure 4 and Figure 8. These micro-cracks at grain boundaries increase the permeability at lower confining stress. The variation in effective stress and pore pressures is the primary cause of changes in gas permeability. Therefore, it is essential to analyze the relationship between net stresses and gas slippage to evaluate their impact on reservoir pore radius [32]. However, the slippage radius values calculated at different confining stresses using model Equation (7) are illustrated in Figure 16. The observed slippage radius decreases with increasing net stress in steady-state and pulse-decay measurements. This indicates that the compaction of observed micro-cracks, as identified through SEM and thin section analysis, causes a lower reduction in permeability at net confining stress. It implies that permeability below 01mD is more sensitive to net overburden stress. The permeability drop in heterogeneous carbonates cannot be generalized for all types of low permeable reservoirs. Therefore, the permeability of the examined samples demonstrated a continuous decline under increased net confining stress, especially with very low initial absolute permeability.

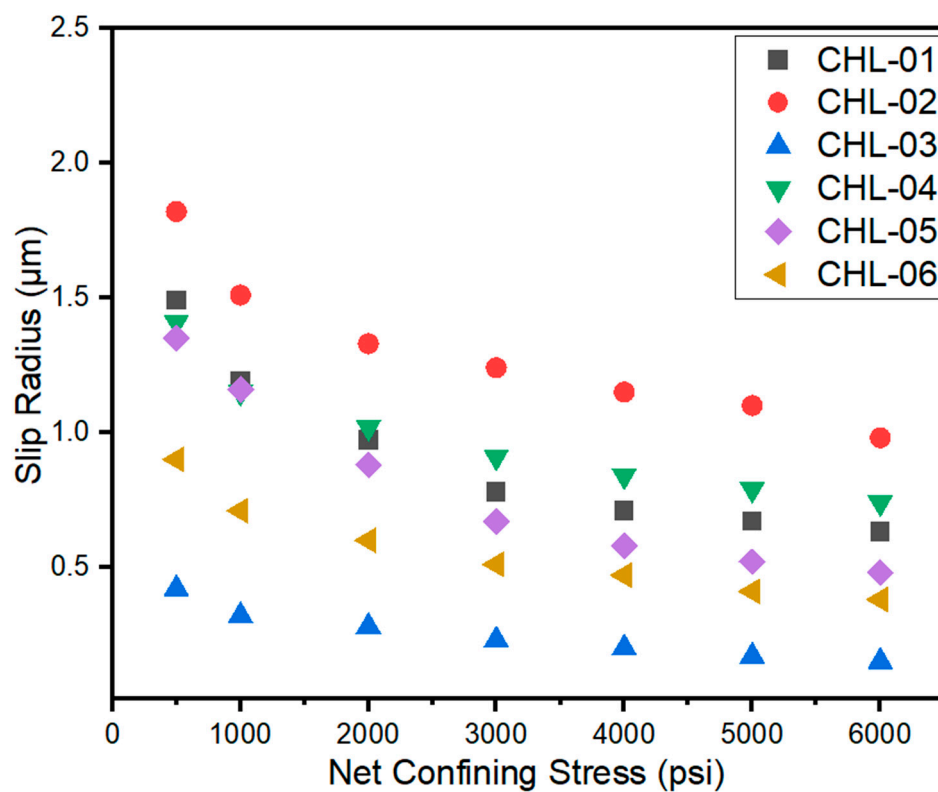


Figure 16. Slip radius as a function of net confining stress.

4. Reservoir quality Assessment

An integrated study has been conducted to assess the impacts of diagenesis and overburden stress on the reservoir quality of the Chiltan limestone reservoir. Several microfacies depositions with different diagenetic settings have primarily influenced the reservoir quality. Various diagenetic processes and depositional environments, such as marine, meteoric, and burial diagenesis have significantly impacted the reservoir potential, which provide the basis for static and dynamic reservoir conditions. These diagenetic events include dissolution, compaction and dolomitization, all of which affect the reservoir quality. Depositional environments reduce petrophysical properties due to early to late-stage cementation. Compaction resulting from overburden stress reduces rock porosity through burial activities, degrading the reservoir quality after cementation. Observed micro-fractures, stylolites accumulation and grains degradation may enhance the reservoir porosity at different stratigraphic stages, which is later overfilled by calcite cement during deep burial activities, as observed in analysis. Petrophysical and petrographic evidence indicates the reduction in inter-

granular porosity and even permeability. The observed dolomitization may reduce the reservoir quality, whereas dissolution may contribute to its improvement. Analyzed samples contained substantial marine organic compounds that precipitate with carbonate minerals and grains, as observed in SEM and thin section analysis, affecting reservoir quality. Furthermore, rock lithification processes, such as aging, mineral compositional changes, and mineral cementation have a significant impact on grain textural qualities. Different carbonate minerals have diverse effects on reservoir potential. The minerals' authigenesis and rock diagenesis control fluid flow movement in porous media [26,61]. Stress sensitivity indicates a reduction in gas permeability with increasing pore pressure, determining the gas slippage effects in the heterogeneous pore structure of the carbonate reservoir. This suggests a significant relationship between overburden pressure, porosity and permeability. The distribution of porosity and permeability in tight or vuggy carbonates closely relates to stress variations, as these properties depend on rock lithofacies and pore architecture. The examined samples had low primary porosity and permeability values, resulting in denser carbonate rocks. Overburden pressure and compaction cause the grain boundaries to come closer together, reducing their petrophysical properties and making them low-quality reservoirs.

5. Conclusions

The detailed petrographic, diagenetic and mineralogical study of Chiltan carbonate formation reveals the following conclusions:

- The identified microfacies primarily consists of shallow to deep marine carbonate deposits, ranging from packstone to grainstone, containing various micro and nano fossil assemblages. The particle size is predominantly fine-grained to medium, with euhedral to anhedral dolomite crystals, calcite cement, bioclasts in associated with micrite matrix, and clay minerals.
- Several diagenetic processes, including micritization, cementation and neomorphism, have had a detrimental impact on reservoir quality during different diagenetic phases, such as marine, meteoric and burial diagenesis. Conversely, dissolution, chemical compaction, and fracturing have enhanced secondary porosity and permeability, which, in turn, are subsequently reduced by induced calcite cementation and the intermixing of clay minerals.
- The obtained average porosity and permeability values of the Chiltan Formation were 3.4% and 0.449 mD respectively. The packstone facies exhibits fair reservoir potential, while the grainstone facies show poor quality, indicating the presence of a complex pore throat structure.
- SEM, EDS and FTIR analyses reveal that the formation predominantly contains calcite, dolomite, and huntite minerals, which have a strong affinity with grains and clay minerals, leading to precipitation and an increase in reservoir heterogeneity.
- Overburden stress sensitivity testing exposed a substantial drop in permeability with various gas slippage effects at lower pore pressures. This indicates that rock compaction due to net confining stress tends to decrease in primary porosity and permeability with an increase in burial depth, resulting in a poor-quality reservoir.
- These findings underscore the complex interplay of diagenetic processes, mineralogy, and overburden stress in determining reservoir quality. Incorporating these outcomes can improve the reservoir characterization accuracy and improve reservoir quality assessment, with the implication for exploration and exploitation of carbonate reservoirs. This will not only be particularly valuable in development of indigenous resources in the region and the country but also contribute to the advancement of the field on a global scale.

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