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Article

Anomaly-Induced Quenching of g_A in Nuclear Matter and Impact on Search for Neutrinoless $\beta\beta$ Decay

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Abstract: How to disentangle the possible *genuine* quenching of g_A caused by scale anomaly of QCD parameterized by the scale-symmetry-breaking quenching factor q_{ssb} from nuclear correlation effects is described. This is done by matching the Fermi-liquid fixed (FLFP) point theory to the “Extreme Single Particle (shell) Model” (acronym ESPM) in superallowed Gamow-Teller transitions in heavy doubly-magic shell nuclei. The recently experimentally observed indication for $(1 - q_{ssb}) \neq 0$ – that one might identify as “fundamental quenching (FQ)” – in certain experiments seems to be alarmingly significant. I present arguments how symmetries hidden in the matter-free vacuum can emerge and suppress such FQ in strong nuclear correlations. How to confirm or refute this observation is discussed in terms of the superallowed Gamow-Teller transition in the doubly-magic nucleus ^{100}Sn and in the spectral shape in the multifold forbidden β decay of ^{115}In .

Keywords: fundamental quenching of g_A ; solution to quenched g_A ; neutrinoless double beta decay; Landau fixed point vs. ESPM; pseudo-conformality in nucleus

1. Introduction

In [1], it was argued that what has been referred to as “quenched g_A ” (denoted as $g_A^O \simeq 1$ in what follows) observed in Gamow-Teller transitions in light nuclei [2] has little to do with *genuine* quenching of the axial-vector coupling constant measured in free space, $g_A = 1.276$. It was suggested that what it represents is not a genuine renormalization of the axial coupling constant in the effective field theory (EFT) space defined by the chiral scale $\lesssim 4\pi f_\pi$ but the effect due to *full* nuclear correlations driven by emerging scale symmetry.¹ That it can be, mostly if not all, due to an effective nuclear correlation mechanism was arrived at in various models by many authors in the past as listed, e.g., in the reviews [2]. To quote one early example out of many, in 1977 Les Houches Lectures, Wilkinson concluded, based on his analyses, that with the shell-model wave-functions for light nuclei $A \leq 21$ that include “full mixing,” the “effective g_{Ae} ” accounting for $g_A^O \simeq 1$ comes out to be [3]

$$g_{Ae}/g_A = 1 + (2 \pm 6) \quad (1)$$

implying that there was nothing “fundamental” in g_A^O going down to ~ 1 from the $g_A = 1.276$ listed in the Particle Physics Booklet. Indeed the modern high-power many-body calculations, such as Quantum Monte Carlo calculations, in light nuclei requires no renormalized g_A , modulo possibly a few % corrections coming from two-body (and more-body exchange) currents [4].

The point stressed in [1] was that g_{Ae}/g_A should be near 1 not just in light nuclei but also in heavy nuclei as well as highly dense nuclear matter *unless unsuspected quantum anomaly effects intervene*. The situation in heavier nuclei as listed in the reviews [2] looks rather different, leaning toward (1) on the larger error bar side [2], hinting at possible density dependence. This issue gets sharpened in the most recent experimental result in the superallowed Gamow-Teller transition in the doubly magic nucleus ^{100}Sn [5] where g_{Ae}/g_A seems to be much less than 1. If the present data (and its interpretation) is correct, then there can be a big FQ. This is the issue I address here.

¹ What’s commonly denoted as “quenched g_A ” in the literature is a misnomer as will be explained below.

In this short note, I discuss there can in fact be a significant renormalization of g_A in nuclear medium *induced by the vacuum change by density* which I will call *genuine* quenching of g_A . I will use the word *genuine* written in *italic* to be distinguished from what has been referred in the literature to as “quenched g_A .” My argument will rely on the notion of scale invariance in QCD put forward by Crewther [6] invoking “*genuine dilaton*.” If this argument is confirmed, it would drastically impact not only certain intrinsic properties of nuclear dynamics where pion-nuclear coupling constants are involved but also all nuclear responses to the weak axial current and perhaps more importantly the searches for going beyond the Standard Model (BSM) such as in neutrinoless double β decay.

I will first describe what the solution to the early 1970’s totally misunderstood issue “ g_A puzzle” ($g_{Ae}/g_A = 1$ in Wilkinson’s formula) could be, what it implies in modern language how hidden (or spontaneously broken) scale symmetry manifests in nuclear medium and what “fundamental” information vis-à-vis with the quenched g_A could be involved in the future development for going beyond the Standard Model.

What’s involved is an up-to-date totally unexplored novel mechanism based on a symmetry hidden in QCD that seems to “emerge” in strong nuclear correlations. What is remarkable is that it seems to permeate from nuclear-matter density $n_0 \simeq 0.16 \text{ fm}^{-3}$ to high densities $n_{star} \sim 7n_0$ relevant to compact-star physics, and even beyond to what is referred to as “dilaton-limit fixed point (DLFP)” $n_{dlfp} \gtrsim 25n_0$. The deviation of g_A^O from 1 observed in the ^{100}Sn decay would, therefore, represent an anomaly in scale symmetry manifested, *not in the matter-free vacuum, but in nuclear medium*.

2. The “genuine dilaton (GD)” and nuclear axial current

I first describe how the scale (trace) anomaly of QCD can enter in the nuclear weak current. For this I adopt the notion of the “genuine dilaton (GD)” in QCD [6,7]. The GD scheme is characterized by the existence of an infrared fixed point (IRFP) α_{IR} at which both scale symmetry and chiral symmetry (in the chiral limit) are realized in the Nambu-Goldstone (NG) mode, populated by the massless NG bosons π and dilaton σ_d whose decay constants are non-zero. What is characteristic of this notion, crucially relevant, is that it accommodates the massive nucleons ψ and vector mesons V_μ at the IR fixed point. I should mention here that there is a new development – referred to as conformal dilaton (CD) – involving an IR fixed point structure accommodating massive hadrons that resembles the GD scenario, possibly linking to the conformal window being discussed for large number of flavors relevant for dilatonic Higgs [8,9]. Whether or not and how these two schemes are related is not yet quite clear. In this paper, I will adopt the GD scheme although this scheme present in QCD (for $N_f \leq 3$) is generally dismissed by those working on dilatonic Higgs theories for large N_f . It seems however feasible to justify the notion advocated here in nuclear medium where scale symmetry “emerges” from or is “made visible” by strong nuclear correlations.

Given that what’s involved is nuclear-matter density inaccessible from both lattice and perturbative QCD, our approach is inevitably anchored on an effective field theory. The relevant degrees of freedom that figure are, apart from the nucleons and NG bosons (π, σ_d), the vector mesons $V = (\rho, \omega)$ as flavor gauge fields. It therefore involves hidden local symmetry (HLS) [10,11] and hidden scale symmetry (HSS) [6–9]. These are the minimal number of degrees of freedom that enable us to go from normal nuclear matter to, involving a topology change at $n_{1/2} \sim (2 - 3)n_0$, near the center of massive compact stars, $n \sim (5 - 6)n_0$ [12].

It turns out that an EFT with systematic power counting in both chiral and scale symmetries (“CS” for short) can be formulated [13,14] but in practice it has too many unknown parameters to fix, so it is not feasible at present to formulate an EFT as powerful as the standard chiral perturbation approach [15]. Fortunately a highly powerful way to bypass the difficulty exists. It is to formulate the many-nucleon problem on the Fermi sphere. In renormalization-group (RG) approach to interacting fermions [16], one can transform the mean fields of the leading CS-order effective Lagrangian with hidden local symmetry and scale symmetry incorporated denoted as $\mathcal{L}_{\psi\chi\text{HLS}}$ – with ψ standing for the nucleon fields, χ for the “conformal compensator field” for the dilaton $\chi = f_\chi e^{\sigma_d/f_\chi}$ and HLS for

the vector fields – to the Landau-Fermi-liquid (LFL) fixed point theory of many-nucleon systems. At the fixed point, one obtains the nuclear matter at its equilibrium [17]. Now with the nucleons put on a Fermi sphere, the LFL fixed point approximation corresponds to taking $1/\tilde{N}$ to zero where $\tilde{N} = k_F/(\Lambda_{fs} - k_F)$ with Λ_{fs} the cut-off on top of the Fermi-surface measured with respect to the origin. It becomes more reliable as density increases. As a bona-fide EFT, one can do higher-order corrections in $1/\tilde{N}$ in what's known as “ V_{lowK} RG-expansion” as done in finite nuclei. For the g_A problem explicit $1/\tilde{N}$ corrections are found to be unnecessary.

One can consider this approach as a DFT (density-functional theory) à la Hohenberg-Kohn theorem applied to nuclear matter. It can be thought of as an improved version of Walecka's relativistic mean field theory of nuclear matter [18] with the refinement brought in by the hidden symmetries and the intrinsic density dependence [19] via the dilaton condensate $\langle\chi\rangle$.² The link to the Fermi-liquid structure of the Walecka's model has been discussed [20].

3. Quenching of g_A in $GnEFT$

The LFL fixed point approach defined above, referred to as $GnEFT$ in our work, is the framework that was exploited to address compact-star physics at high density in [12]. (Let me just mention that it has been highly successful for explaining even the recent data from NICER/XMM-Newton [21].) Here I will focus entirely on the nuclear axial current.

The power of the $GnEFT$, even when drastically simplified, has been that low-energy theorems, both iso-vector and iso-scalar, can be encoded in $\mathcal{L}_{\psi\chi\text{HLS}}$ -type Lagrangians and when applied to nuclear matter with suitable Ward identities, give very accurate results for nuclear electromagnetic (EM) response functions. For instance, it has been shown [17] that for a quasiparticle on top of the Fermi surface, the iso-scalar orbital gyromagnetic ratio $g_l^0 = 1$ – with the nucleon mass dropping à la BR scaling at increasing density – comes out to be consistent with the Kohn theorem [22] and the anomalous iso-vector gyromagnetic ratio δg_l^i , reproducing exactly the Migdal formula [23] in terms of the Landau-Migdal parameter F_1 , agrees exactly with the available Pb data. To the best of the author's knowledge, there has not been as simple a derivation of, and with such a quantitative agreement with nature, for these and other EM functions in (heavy) nuclei obtained in standard nuclear chiral perturbative (NchiPT) approach. This same formalism will be applied to the axial-vector transitions in nuclei.

3.1. g_A^L as a Landau Fermi-liquid fixed-point quantity

Consider the Landau quasiparticle propagating with near zero momentum on top of the Fermi sea in interaction with charged pionic and vector-mesonic fluctuations on the surface. Via low-energy theorems, such as the Goldberger-Treiman relation, the coupling constant involved can be written with the axial coupling g_A . In the same LFL fixed-point approximation applied in the EM case, the “effective” axial coupling of the quasiparticle on the Fermi surface can be calculated in the mean-field approximation as a Landau fixed-point quantity [17]

$$g_A^L = g_A q_{snc}^{\text{Landau}} \simeq 1 \quad (2)$$

with

$$q_{snc}^{\text{Landau}} = (1 - \frac{1}{3}\Phi^* \bar{F}_1^\pi)^{-2}. \quad (3)$$

² The BR-scaling masses of the vector mesons account for higher meson-field terms consistently with the symmetries involved – which are missed in nonlinear Walecka models.

Here

$$\Phi^* = f_\pi^*/f_\pi \quad (4)$$

is the BR scaling [19] and \bar{F}_1^π is the pionic contribution to the Landau mass. As defined, the factor q_{snc}^{Landau} is to capture the *complete* nuclear correlations (or full mixing in the sense of (1)). It can be unambiguously calculated and was found to be (with $g_A = 1.276$)

$$q_{snc}^{\text{Landau}} = g_A^L/g_A \simeq 1/g_A \simeq 0.78. \quad (5)$$

This factor turns out to be insensitive to density between $n = n_0/2$ and n_0 . Note that the underlying assumption for (2) is that N_c is large as in the Goldberger-Treiman relation in the vacuum and $1/\bar{N} \rightarrow 0$. Thus the quenching of g_A to 1 by the factor (5) is accounted for *entirely* by nuclear quasiparticle correlations on the Fermi surface. Now the question that was left un-clarified in [17] was: How is this $g_A^L \simeq 1$ related to the quenching of g_A in nuclear weak processes, in particular, Gamow-Teller transitions in finite nuclei [2]? To answer this question, look at the nuclear axial response function to the external weak field \mathcal{W}_μ . What's involved is the iso-vector nuclear axial current $J_{5\mu}^a$ relevant in the EFT defined by the chiral scale.

At the classical level, the nuclear axial current coupling to the external weak field in the CS Lagrangian is scale-invariant. However there is an anomalous dimension contribution from the trace anomaly of QCD that enters nonperturbatively at the leading-order (LO) chiral-scale perturbation expansion [7]. The full LO axial current is given by [6]

$$J_5^{a\mu} = g_A q_{ssb} \bar{\psi} \gamma^\mu \gamma_5 \frac{\tau^a}{2} \psi \quad (6)$$

where

$$q_{ssb}(\beta', \chi) = c_A + (1 - c_A) \left(\frac{\chi}{f_\chi} \right)^{\beta'}. \quad (7)$$

If it were not for q_{ssb} , the current (6) would be scale-invariant. The scale-symmetry breaking enters in q_{ssb} nonlinearly dependent on density. While c_A is a constant, possibly density-dependent in nuclear medium, the second term of q_{ssb} carries the conformal compensator field χ [6]. In the matter-free vacuum, c_A could perhaps be "measurable" on lattice but in medium, can be accessed neither by lattice nor by perturbation. β' is the derivative of the $\beta(\alpha_s)$ at the IR fixed point

$$\beta'|_{\alpha_s=\alpha_{\text{IR}}} \quad (8)$$

which is expected to be > 0 in the GD scheme but has not yet been measured on lattice for $N_f \leq 3$. One sees that β' brings in an anomalous dimension, representing scale-symmetry explicit breaking, to the current operative in medium. It is this quantity that could lead to a fundamental renormalization of the constant g_A .

3.2. Accessing q_{ssb}

Now here is the most significant observation to make in the formula (7).

It is a nonlinear functional of χ , apparently too complicated to treat in general. However in the problem concerned in nuclear matter, it can be simplified. In the matter-free space, the vacuum expectation value (VeV) is $\langle \chi \rangle = f_\chi$, so if one ignores the fluctuating dilaton field that enters at higher loop orders justifiable in the axial current, one can set $q_{ssb} = 1$. Then the current remains scale-invariant. There will then be no β' effect at the order involved. However in nuclear matter, $\langle \chi \rangle^* = f_\chi^* \neq f_\chi$ brings in scale symmetry breaking, both explicit and spontaneous, hence bringing in

the β' dependence. Applied to nuclear matter, one then has the density-dependent factor that I call "anomaly-induced quenching" (AIQ for short)

$$q_{\text{ssb}}^* = c_A + (1 - c_A)(\Phi^*)^{\beta'} \quad (9)$$

where

$$\Phi^* = f_\chi^*/f_\chi \simeq f_\pi^*/f_\pi \quad (10)$$

with * standing for density dependence. The relation $f_\chi^*/f_\chi \simeq f_\pi^*/f_\pi$ reflects the characteristic of the GD scheme, different from dilatonic Higgs models for large N_c [24]. It is worth re-stressing that in the absence of baryonic matter, scale symmetry would not be directly visible, hence reflecting the "hidden scale symmetry" emerging in nuclear medium.

The conclusion here is that within the GnEFT scheme, $q_{\text{ssb}}^ < 1$ is the fundamental quenching factor that can intervene in nuclei. It is a genuine quenching. And it is the only FQ predicted in this GnEFT approach.*

Note that this AIQ was missing in the Goldberger-Treiman-type result in [17]. There $q_{\text{ssb}}^* = 1$ was set invoking the LOSS (leading-order-scale-symmetric) approximation [12].

I should stress before going further that the possible presence of the AIQ – and other β' effects – has never been observed or even suspected in the literature up to date. This article is the first to address the issue because of the important RIKEN data that if correct would drastically impact not only on the search for neutrinoless double-beta decay for going beyond the Standard Model but also on certain properties of nuclei and nuclear matter controlled by the combined scale and chiral symmetries.

4. Mapping the Landau-Fermi-liquid fixed point approximation to the shell model

In the absence of reliable full *ab initio* numerical treatments of nuclear many-body problems for complex nuclei – apart from very light nuclei $A < 10$, how to translate the LFL fixed-point result given above for nuclear matter to finite nuclei has not been obvious. However there is one case, I argue, where this translation is feasible and that is the superallowed Gamow-Teller transitions in doubly-magic-shell nuclei that are heavy enough to be treated as a nuclear matter.

The LFL fixed-point limit in the Fermi-liquid system obtained above with $q_{\text{snc}}^{\text{Landau}}$ corresponds to a Gamow-Teller transition undergoing on the Fermi surface with the kinematics $\omega \rightarrow 0$, $q/\omega \rightarrow 0$ – where (q, ω) are the (momentum, energy) carried by the weak field. What is required for this limit to hold is that quasiparticle-quasihole bubble contributions entering at higher orders in $1/\bar{N}$ be suppressed.

I now argue that this LFL fixed-point limit in the Fermi-liquid system can be mapped to the "Extreme Single Particle (shell) Model (ESPM)" in doubly-magic-shell nuclei. The most illustrative case is the transition in the ^{100}Sn nucleus which has the proton and neutron shells completely filled at 50/50. There may be other nuclei of similar structure or perhaps even better but I will focus on this nucleus because it has the advantage of being the heaviest nucleus with the equal magic shells that has also been studied extensively both experimentally and theoretically [5,25,26] with the results directly relevant to the issue concerned.

The process involved is a pure superallowed GT transition of a proton (π) $\pi 0g_{9/2}$ in the completely filled orbital into a neutron (ν) in the empty spin-orbit partner, the $\nu 0g_{7/2}$ orbital of ^{100}In . This offers the most favorable structure of the daughter state that is of a pure ($\nu g_{7/2}$) particle-($\pi g_{9/2}$) hole state to which the ESPM can be applied.

With the ingredients, as complete as feasible given above, one can now proceed to do the mapping for the ^{100}Sn GT decay. Phrased in terms of the GT strength \mathcal{B}_{GT} defined in [5,25], the Landau Fermi-liquid fixed point GT strength can be equated to the GT strength given in terms of the ESPM quantities

$$\mathcal{B}_{\text{GT}}^{\text{theory}} = \mathcal{B}_{\text{GT}}^{\text{ESPM}}(q_{\text{ssb}} q_{\text{snc}}^{\text{Landau}})^2 \approx 10.8 q_{\text{ssb}}^2 \quad (11)$$

with $\mathcal{B}_{\text{GT}}^{\text{EPSM}} = 160/9$ and the full mixing factor given in the LFL fixed-point theory (5). This is the principal prediction of the theory that follows from the matching of the Fermi liquid to the doubly-magic shell structure. Given a well-measured experimental value $\mathcal{B}_{\text{GT}}^{\text{exp}}$, one could then extract the fundamental quenching factor q_{ssb} from (11).

5. Evidences

Let me first give an evidence for no AIQ , $q_{\text{ssb}} \approx 1$. This would then – with (5) – give the prediction

$$\mathcal{B}_{\text{GT}} \approx 10.8. \quad (12)$$

The measurement made in GSI [25] that zeroes-in on $\sim 95\%$ of the daughter state of a pure ($\nu g_{7/2}$) particle-($\pi g_{9/2}$) hole configuration gives

$$\mathcal{B}_{\text{GT}}^{\text{GSI}} \approx 10. \quad (13)$$

This leads to no appreciable FQ . This result is of course approximate, with $\sim 5\%$ deviation from the pure EPSM structure of the daughter state. As discussed also in [25], there can be more refined analysis taking into account possible corrections to the EPSM but it cannot be entirely free of uncontrolled nuclear model dependence. That there is little, if any, evidence for AIQ in this experiment is a robust observation. This result is globally consistent with the absence of any indication for AIQ in other nuclear axial processes. I will come back to this matter below.

Evidence for big AIQ

Now let's turn to the more recent, what's claimed to be "improved," RIKEN result [5],

$$\mathcal{B}_{\text{GT}}^{\text{RIKEN}} = 4.4^{+0.9}_{-0.7}. \quad (14)$$

This is in serious tension with the GSI result, (13). Within the range of values involved, this implies

$$q_{\text{ssb}}^{\text{RIKEN}} \approx 0.58 - 0.69. \quad (15)$$

This result implies that the "fundamental" g_A in the axial current effective in nuclear medium defined by the chiral symmetry scale $\sim 4\pi f_\pi$ can be quenched from 1.276 to $\sim (0.74 - 0.88)$. This applies to all axial transitions in nuclei. This is a big *fundamental* quenching.

One immediate question to raise is whether one cannot arrive at (14) by other mechanisms that do not require the AIQ . There may be several possibilities available in the literature but as far as the author is aware none seems viable as they stand. One notable case to illustrate the issue is the *ab initio* calculation heralded as a "first-principles resolution" of the g_A puzzle [27]. The strategy in this calculation – which is anchored on standard nuclear chiral EFT – is to "tweak" the resolution scale (or effectively cut-off scale) in the EFT to shift the quenching effect from one-body to 2 or more-body currents to arrive at q_{snc} that requires no AIQ of the magnitude of (15). As argued in [1], this strategy exploiting the $N^3\text{LO}$ chiral expansion terms is untenable unless there is justification to ignore the next-order ($N^4\text{LO}$) terms. As far as I can see, there is none given that the $N^4\text{LO}$ terms will contain far too many unknown parameters. This makes moot the assertion made in [27].³

I now turn to another potentially serious indication for a possible AIQ quenching in the recent developments on the spectral shape of multifold forbidden β decay which turns out to be extremely sensitive to the g_A coupling. Comparing theoretical predictions to the experimental β spectrum, it has been argued [28] that the spectral shape of the multifold forbidden β decay of ^{115}In requires a quenching

³ What was obtained in [27] corresponded to (13), not to (14).

of g_A by a factor $q^{115\text{In}} \sim (0.65 - 0.75)$ with the range of the value accounting for the nuclear model dependence in calculating the matrix elements of the weak current involved in the spectrum shape. Suppose the axial matrix elements in the spectral shape were calculated with sufficient accuracy. Then one could take the quenching factor found in the measurement to be the AIQ , $q_{\text{ssb}}^{115\text{In}} \sim (0.65 - 0.75)$. This is comparable to the AIQ factor found in the RIKEN experiment.

There is however a serious caveat in arriving at this result. As noted by the authors of [28], the spectral shape and decay do not match. One may understand this conundrum given that the operators involved could be of drastically different structure. Unlike in the superallowed decay in ^{100}Sn where q_{snc} and q_{ssb} are disentangled from each other thanks to the hidden scale symmetry governing in the doubly-magic-shell structure, the one-body axial-current operator figuring in the spectral shape – with multi-body currents ignored – does not enjoy any known symmetry protection. Its matrix element could therefore be highly nuclear-model dependent [28].

Finally let me make a few brief remarks on evidences that argue against a large AIQ effect.

That g_{Ae}/g_A is near 1 in light nuclei but deviates from 1 in heavier nuclei is not impossible, but it is more or less ruled out in the formula for AIQ (9) unless β' is big, say, > 3 . Although q_{ssb} cannot be calculated at present, there is nothing to suggest a big density dependence either. Furthermore $g_A^L \simeq 1$ seems to permeate from $\sim n_0$ to the dilaton-limit fixed point $\gtrsim 25n_0$ [12].

Another indication that an AIQ factor of the magnitude (15) is at odds with the quantity defined as ϵ_{MEC} which zeroes in on the contribution from the strongly enhanced soft-pion exchange 2-body contribution to the matrix element of the axial charge operator $J_{\gamma 5 0}^i$ in first-forbidden β transitions. The enhancement factor ϵ_{MEC} has the merit of being nuclear-model independent. First being protected by the soft-pion theorems, the exchange current is totally model-independent. Furthermore the ratio of the 2-body matrix element to the leading 1-body term is also nuclear model-independent. The measurements in Pb nuclei [29] showed indeed a strong enhancement in ϵ_{MEC} predominantly controlled by chiral symmetry. The experimental result of [29] is precisely reproduced in the framework of $G\text{nEFT}$ without the AIQ factor [30]. This Pb result was also quantitatively supported in $A = 12$ nuclei where the density dependence in Φ is consistent with the BR scaling [31]. This – what one might call a – “precision” test of chiral symmetry in nuclear systems would be ruined if g_A were quenched by the fundamental renormalization (15). Of course in the context of the present day chiral effective field theory, focusing on the ϵ_{MEC} , both measured and calculated, could however raise the question as to the precision with which the one-body matrix element has been calculated and whether all the terms in the weak current are taken into account. This matter could be checked in modern high-powered *ab initio* calculations.

I should mention that the idea to exploit this enhanced $J_{\gamma 5 0}^i$ in first-forbidden transitions - in a stark contrast to the highly suppressed 2-body current for superallowed Gamow-Teller transitions – was in fact studied in combination with the effect on the spectral shape in [32]. It would be interesting to pursue this direction in the context mentioned above.

6. Concluding remarks

In this note it was shown by mapping the RG-based Landau Fermi-liquid fixed point approximation to the ESPM in heavy doubly-magic nuclei that what's commonly referred to as “quenched g_A ,” i.e., g_A^Q , in the literature consists of two factors: one q_{snc} given entirely by “snc” (strong nuclear correlations) and the other, q_{ssb} induced by the trace anomaly of QCD *which is invisible in the vacuum but exposed by density in nuclear medium*. It was also shown that $q_{\text{snc}}g_A \rightarrow 1$ independent of density. While there is no established evidence in nuclear processes for the presence of a fundamental quenching $q_{\text{ssb}} \neq 1$, there appear in the literature several experiments that show an indication for as much as $\sim 40\%$. *Such a big quenching in the fundamental coupling constant, if not ruled out, would make an impact not only in nuclear theory in general but also in the effort to go beyond the SM, such as $0\nu\beta\beta$ decay, in particular.* Such an important fundamental renormalization of g_A in nuclear medium would pose a challenge to explain the apparent absence of visible effects in pion-nuclear dynamics.

I presented in this paper a suggestion for a well-defined resolution to the problem involving g_A : First establish q_{ssb} in the superallowed GT matrix element in the doubly-magic nucleus ^{100}Sn , incorporate it in the analysis of the spectral shape of highly forbidden β decays, and then obtain the wave functions that *fit* the spectral shape. One could then employ the resulting nuclear wave functions for the Gamow-Teller matrix elements in the $0\nu\beta\beta$ processes where non-negligible momentum transfer could be involved.

Given that q_{ssb} involves two unknown parameters, β' and c_A , it would require (at least) two superallowed GT transitions of doubly magic nuclei of different densities to extract the two unknowns. If there were another nucleus with density different from that of ^{100}Sn , that would offer the information on β' in QCD that can be gotten only in baryonic matter. With only one data from ^{100}Sn with $q_{ssb} \approx 0.6$ available, $\beta' < 3$ seems to be ruled out.

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