

Article

Mechanism of Low Frequency Oscillation When EMUs Passing Neutral Zone and Suppression Method

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Abstract: This article addresses the problem of contact voltage increase caused by the low frequency oscillation of the train-grid system in the phase-separation process of the EMU. The article establishes the EMU-contact line-traction substation model, reveals the mechanism of low-frequency oscillation, and obtains the relationship between the separation phase angle of the pantograph with line and low-frequency oscillations. Methods to suppress the over-voltage during the low-frequency oscillation are proposed. The study shows that when the power phase angle of the pantograph-line separation is within the range of 60° – 90° and 240° – 270° , the voltage amplitude in the neutral zone is larger, the maximum amplitude can reach 52.2kV, and low-frequency oscillation will occur in the neutral zone. When low frequency oscillation occurs, the contact line voltage in the neutral zone is mainly 1/3 power frequency (16.7Hz). After installing an RC suppression device in the neutral zone, when the EMU enters the neutral zone, the absolute value of the voltage peak drops to below 20 kV. Compared with the situation where the suppression device is not connected, the absolute value of the voltage peak is reduced by nearly 60%. The study provides a basis for the design of the neutral zone of the contact line and the selection of the high-voltage equipment of the EMU.

Keywords: inrush current; high-speed train; over voltage; traction power supply system; vehicle

1. Introduction

When the EMU is in the neutral zone, during the switching process of the electric circuit, there is electromagnetic energy in the equipment such as voltage transformer inductance and the ground capacitance of the vehicle line. This energy is converted between the inductance element and the equivalent capacitance to form the low frequency oscillation. The oversaturation of ferromagnetism components, the increase of terminal voltage and the abnormal increase of the line voltage in the neutral zone pose a serious threat to the safety of EMUs and contact line electrical neutral zone equipment.

To solve the problem of low-frequency oscillation and overvoltage suppression in the power supply system, industry experts and scholars have carried out extensive and in-depth modeling study and characteristic analysis, and proposed methods for low-frequency oscillation suppression. As for the mechanism of low-frequency oscillation, Ruifeng Zhang and others have studied the power-side oscillation combined with the system impedance characteristics [26–30]. They proposed a method to adjust the power supply control strategy to reduce the low-frequency oscillation amplitude and oscillation time. For the problem of low-frequency oscillation caused by line-side faults, Lingling Fan et al. obtained the influence of line capacitance parameters on the ferromagnetic resonance in the system, and calculated the transient process. The influence of the selection of inductance, capacitance and resistance parameters on the ferromagnetic resonance phenomenon is

analyzed [31-35]. For the problem of low-frequency oscillation suppression, Haitao Hu and others combined the matching relationship between the impedance of the power supply line of the traction power supply system and the impedance of the locomotive, and proposed a strategy to reduce the oscillation by adding active filtering on the power control side. The method focused on the analysis of the input impedance characteristics of electric locomotives. The stability direction of the system is determined according to the coupling relationship between the input impedance and the impedance of the power supply line [36-40]. For the operating system, combining the characteristics of system impedance and low - frequency oscillation characteristics, a parallel RC device is proposed to reduce the oscillation process [41-45]. The above research provides a reference for the analysis of the low-frequency oscillation process of the EMU passing through the neutral zone and the formulation of suppression strategies in the traction power supply system.

However, the distance of the neutral zone in the contact line is short (200m), the EMU will experience disconnecting the traction motor load, entering the neutral zone and the intersection of the feeding section, and separating the pantograph from the line. This process is complicated, at the same time, the neutral zone has a short distance, the distributed capacitance and the circuit resistance is small, the oscillation process is complicated, as shown in Figure 1.

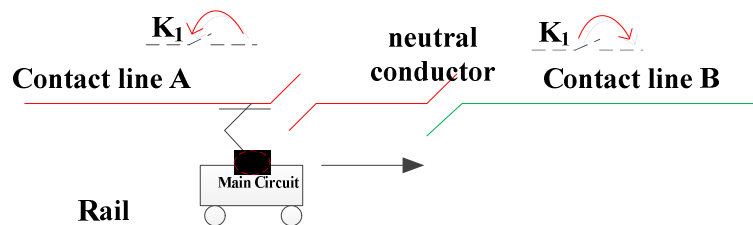


Figure 1. Transient process of EMU passing phase division zone.

If there is a low-frequency oscillation in the vehicle line system when EMU passing the neutral zone, the magnetic field of the excitation circuit of the voltage transformer and other equipment will increase, the terminal voltage will rise, and the high-voltage coil insulation of the equipment will be damaged. Using the existing research conclusions will have greater limitation. In response to this problem, this article combines the operating conditions of the existing lines to test the line voltage characteristics and the oscillation process of the EMU during the neutral zone process, establishes the EMU-contact line-traction substation model, reveals the low-frequency oscillation mechanism. The study obtains the relationship between the separation phase angle of the pantograph and the low-frequency oscillation, the low-frequency oscillation overvoltage suppression methods are proposed. The research provides a basis for the design of the contact line neutral zone and the selection of high-voltage equipment for the EMU.

2. Low-Frequency Oscillation and Overvoltage Characteristics of the Contact Line

2.1 Test method and test process

For on-line low-frequency oscillations, field tests are carried out. The test system consists of a voltage divider, a current sensor, and data acquisition. The data acquisition system uses a 20 kHz sampling frequency and can analyze 100th harmonics. The recording method is continuous interval recording, that is, store once in every 1000ms, and store 100ms data each time, so that the transient process can be recorded. The specific parameters of the test system design are shown in Table I.

Table I Main Test Equipment			
Serial number	Name	Model	Test standard, accuracy
1	Data acquisition	HS4	0.1%(12 bit)
5	Voltage probe	— —	100V/2V, 1%
6	Current Sensor	PQ5(U.S. Fluke)	0~5A,40~2kHz, 2%

During the test, the voltage and current signals are respectively obtained on the secondary terminals of the on-board voltage transformer and the current transformer. When the train is running on the line, the voltage waveform obtained is shown in Figure 2. The line voltage when passing through the neutral zone (i.e. the position A shown in Figure 1) is shown in Figure 2. At this position, there is an instantaneous drop in line voltage, but a higher amplitude overvoltage appears at the position2.

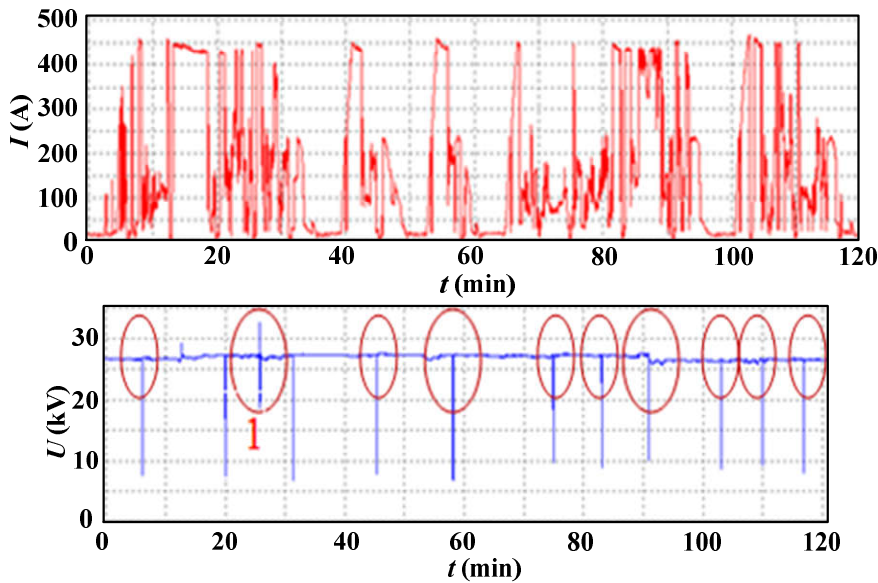


Figure 2. Train operating current and voltage (RMS value).

2.2 Wave characteristics and laws

When the train passes through the electrical neutral zone, the voltage waveform should be as shown in Figure 3 because the electrical separation belongs to the no-power zone.

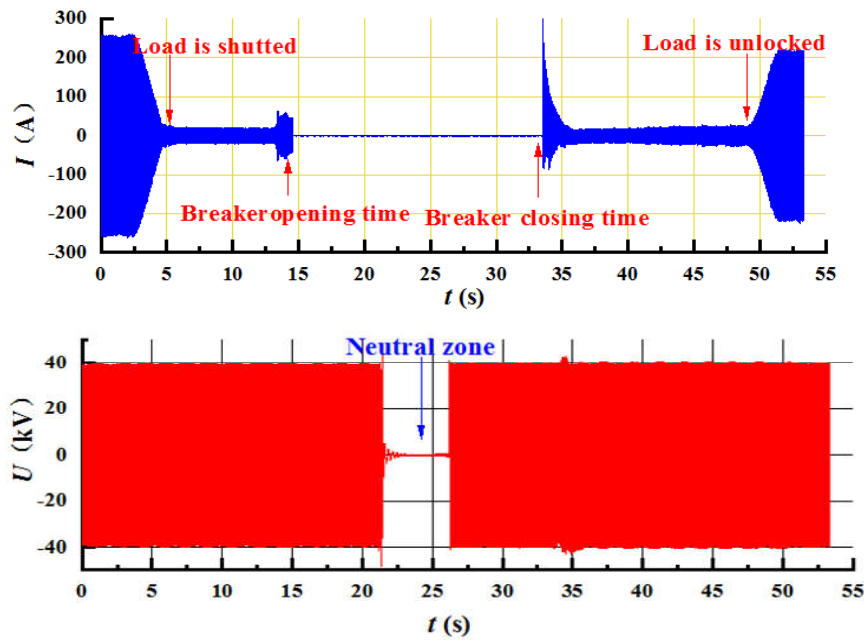


Figure 3. Train overcurrent split-phase voltage waveform.

When the train is separated from the feeding section at stage A, a brief pantograph arcing will appear. In the neutral zone, although the voltage is affected by the induced voltage of the feeding section and the voltage should be below 5kV and 50Hz power frequency normally.

When the EMU produces low-frequency oscillations in the neutral zone, the voltage transformer on the secondary side of the EMU voltage transformer will increase abnormally. If the EMU enters the neutral zone at position 34, besides the line over voltage due to the separation of the pantograph and the grid, the grid voltage waveform in the neutral zone will also have obvious low-frequency oscillation characteristics. When the amplitude of the oscillation voltage is obvious, it can reach 52.0kV. The neutral zone of the contact line mainly occurs low-frequency oscillation of 1/3 power frequency (16.7Hz).

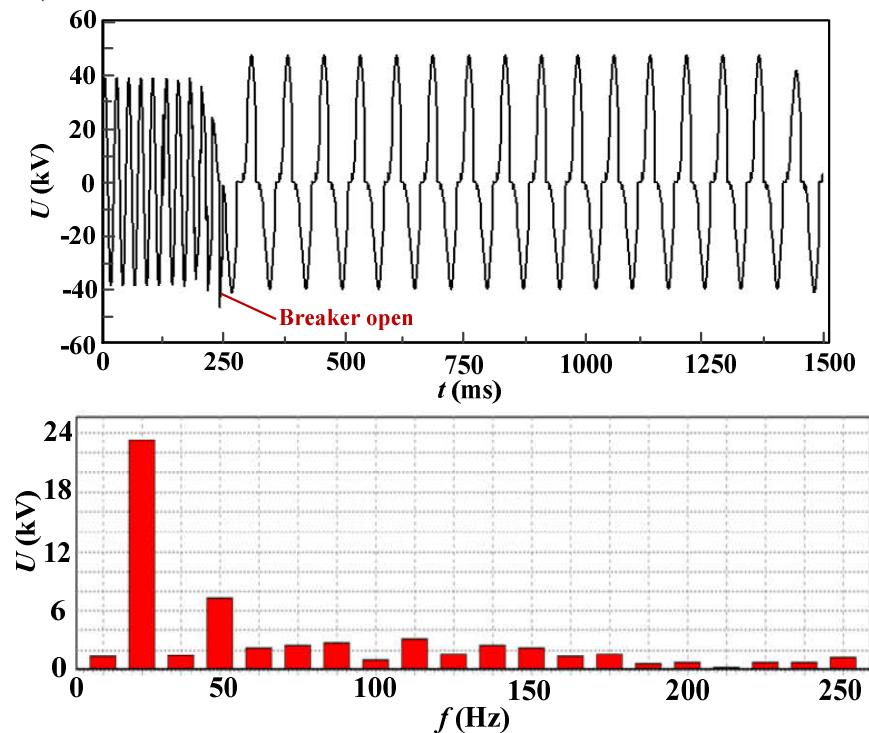


Figure 4. Harmonic frequency analysis of voltage in neutral zone.

Through the analysis of the harmonic proportion, the amplitude of the generated 1/3 power frequency harmonic is about 3 times of the induced voltage in the neutral zone, and the overvoltage after the voltage superposition will affect the safety of the EMU.

Table II. Harmonic frequency analysis data of grid voltage waveform in neutral zone

Frequency (Hz)	Percentage (%)	Frequency (Hz)	Percentage (%)
0	6.04	133.33	13.36
16.67	100	150	6.86
33.33	6.29	166.67	10.89
50	31.34	183.33	9.81
66.67	9.53	200	6.12
83.33	10.73	216.67	6.88
100	12.07	233.33	2.81
116.67	4.60	250	3.17

3. Vehicle-Line-Institute Model and Oscillation Characteristics

3.1 Research on the model of train passing through the neutral zone

In the tested Beijing-Zhangjiakou railway line, the AT power supply mode is adopted, and an autotransformer is installed every 10-15km. One terminal is connected to the contact line, the other terminal is connected to the positive feeder, and the neutral point is directly connected to the rail. As shown in Figure 5, the AT power supply mode is equipped with a protection wire (PW), which is directly connected in parallel with the rail (R); a connector of protective wire (CPW) is added to connect the rail and the midpoint of the autotransformer with the protection wire. In order to reduce the impedance of the traction power system, increase the voltage at the end of the feeding section, and reduce the power loss, the downstream contact lines, positive feeders, and steel rails of the double-track traction line are connected in parallel at each AT.

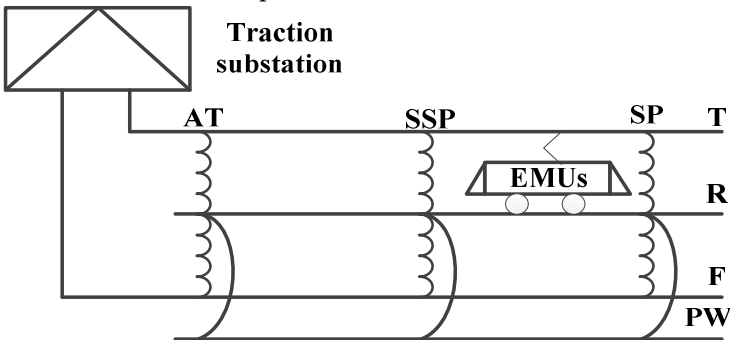


Figure 5. Structure of double-wire full parallel AT traction net.

Table IV. Equivalent circuit distributed capacitance calculation results

c	T1	R1	P1	F1	T2	R2	P2	F2
T1	13.12	-0.83	-1.74	-2.04	-2.00	-0.41	-0.36	-0.56
R1	-0.83	20.12	-0.63	-0.23	-0.41	-0.44	-0.12	-0.09
P1	-1.74	-0.63	8.42	-1.12	-0.36	-0.12	-0.08	-0.11
F1	-2.04	-0.23	-1.12	8.28	-0.56	-0.09	-0.11	-0.26
T2	-2.00	-0.41	-0.36	-0.56	13.12	-0.83	-1.74	-2.04
R2	-0.41	-0.44	-0.12	-0.09	-0.83	20.12	-0.63	-0.23
P2	-0.36	-0.12	-0.08	-0.11	-1.74	-0.63	8.42	-1.12
F2	-0.56	-0.09	-0.11	-0.26	-2.04	-0.23	-1.12	8.28

The electrical parameters of the voltage transformer are shown in Table V.

Table V. Voltage transformer inductance parameters

Serial Number	JDZXW5-25J	JDZXW5A - 25J	JDZXW7-25D
EMU Type	CRH3X	CRH5X	CR400XF
Primary DC Resistance 20°C	43160Ω	46488Ω	43160Ω
Primary inductance	11000H-12000H	11000-12000H	11000H-12000H

In the entire EMU, only the pantograph and the roof voltage transformer are connected to the contact line and the articulated electrical split. This main circuit can be equivalent to a high-level circuit composed of resistance, inductance and capacitance. The equivalent circuit is shown in Figure 6.

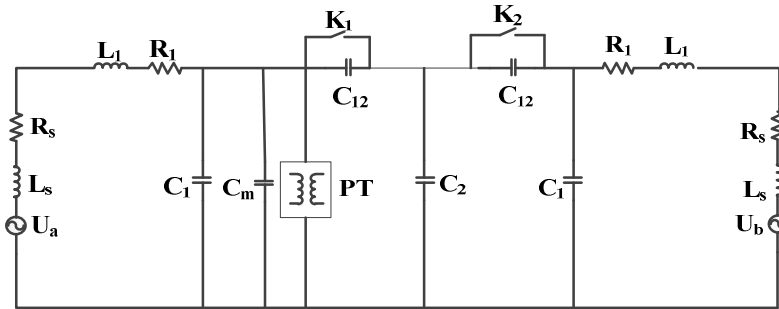


Figure 6. Equivalent circuit diagram of overphase division of EMU.

In Figure 6, U_a and U_b are traction power supplies; R_s and L_s are the resistance and inductance of the traction transformer converted according to the Thevenin circuit equivalent; R_1 and L_1 are the equivalent resistance and reactance of the contact line feeding section; C_1 is the feeding section ground capacitance; C_2 is the neutral zone-to-ground capacitance; C_{12} is the coupling capacitance between the neutral zone and the power supply zone; PT is the roof voltage transformer; C_m is the EMU pantograph-to-ground capacitance; K_1 and K_2 are equivalent switch. The initial state is the off state, which is used to simulate the circuit conversion process of the over-phase division of the EMU.

When the EMU enters the neutral zone, the equivalent switch K_2 remains open, and the equivalent switch K_1 quickly changes from the open state to the closed state. The neutral zone voltage in this transient process can be determined by the differential equation. Since the core inductances L_m

and R_m of the roof voltage transformer are relatively large, and C_1 and C_m are relatively small compared to C_2 , the neutral zone and the power supply zone coupling capacitor C_{12} are short-circuited after the switch K_1 is closed, so in the differential equation expression, the influence of the parameters L_m , R_m , C_1 , C_m , and C_{12} can be ignored. If $L=L_s+L_1$, $R=R_s+R_1$, $C=C_2$ according to the equivalent circuit of the EMU after the equivalent switching action, the loop equation can be listed:

$$u_L + u_C + u_R = u_s \quad (1)$$

Among them u_s is the power supply voltage, the inductor voltage $u_L=Ldi/dt$, the resistance voltage $u_R=R \cdot i$, and the loop current $i=Cdu_C/dt$. Substituting them into equation (1), the differential equation can be obtained:

$$LC \frac{d^2 u_C}{dt^2} + RC \frac{du_C}{dt} + u_C = u_s \quad (2)$$

Since the impedance of the contact line in the neutral zone is very small, the voltage drop of the contact line impedance in the neutral zone can be ignored. Then the voltage u_C at both ends of the neutral zone-to-ground capacitance C_2 in the equation (2) is the voltage of the neutral zone on the joint-type electrical split.

Equation (2) is a second-order linear non-homogeneous differential equation with constant coefficients, and its full response can be decomposed into zero input response and zero state response.

The induced voltage of the neutral zone-to-ground capacitance C_2 on the electric neutral zone, after the switch K_1 is closed, the capacitance C_2 discharges to the R-L circuit. The differential equation is:

$$LC \frac{d^2 u_C}{dt^2} + RC \frac{du_C}{dt} + u_C = 0 \quad (3)$$

The zero input expression of the effective circuit is:

$$\begin{aligned} u_C &= -\frac{p_2 U_0}{p_1 - p_2} e^{p_1 t} + \frac{p_1 U_0}{p_1 - p_2} e^{p_2 t} \\ &= \frac{U_0}{p_1 - p_2} (p_1 e^{p_2 t} - p_2 e^{p_1 t}) \end{aligned} \quad (4)$$

Due to the different circuit parameters, the characteristic root may have three different situations. The neutral zone-to-ground voltage in these three situations will be discussed:

1) When $\alpha=\omega_0$, that is $R > 2\sqrt{L/C}$, p_1 and p_2 are two unequal negative real numbers.

$$u_C = \frac{U_0}{p_1 - p_2} (p_1 e^{p_2 t} - p_2 e^{p_1 t}) \quad (5)$$

This situation is called aperiodic discharge or non-oscillating discharge process.

2) When $\alpha=\omega_0$, that is $R < 2(L/C)^{0.5}$, p_1 and p_2 are equal, then the equivalent circuit has only one frequency, and the neutral voltage to ground is:

$$u_C = U_0 (1 + \alpha t) e^{-\alpha t} \quad (6)$$

It can be seen from equation (6) that there is no oscillating change, and it has a non-oscillating nature, but this is the dividing line between an oscillating circuit and a non-oscillating circuit, so the situation when $R < 2(L/C)^{0.5}$ is called a critical non-oscillating process.

3) When $\alpha < \omega_0$, that is $R < 2(L/C)^{0.5}$, p_1 and p_2 are a pair of conjugate complex roots, and the neutral voltage to ground is:

$$u_C = \frac{U_0 \omega_0}{\omega_d} e^{-\alpha t} \sin(\omega_d t + \beta) \quad (7)$$

This is an oscillating discharge situation. During the whole process, the waveform will periodically change direction, and the energy storage element will also periodically exchange energy.

When $u_s = U_m \sin(\omega t + \Phi)$ in formula (2), where ω is the angular frequency of the power supply and Φ is the initial phase angle of the power supply voltage. At this time equation (2) becomes:

$$LC \frac{d^2 u_c}{dt^2} + RC \frac{du_c}{dt} + u_c = U_m \sin(\omega t + \phi) \quad (8)$$

1) If it is a non-oscillating circuit, the neutral voltage to ground can be expressed as:

$$u_c = \frac{U_m}{Z} X_C \sin\left(\omega t + \phi - \varphi - \frac{\pi}{2}\right) + A_1 e^{p_1 t} + A_2 e^{p_2 t} \quad (9)$$

Substituting formula (5) into the formula, the expression of U_c and i is:

$$u_c = \frac{U_m}{Z} X_C \left[\sin\left(\omega t + \phi - \varphi - \frac{\pi}{2}\right) + \frac{\cos(\phi - \varphi)}{p_1 - p_2} (p_1 e^{p_2 t} - p_2 e^{p_1 t}) + \frac{\sin(\phi - \varphi)}{p_2 - p_1} (p_1 e^{p_1 t} - p_2 e^{p_2 t}) \right] \quad (10)$$

2) If the circuit is in a critical state, in the same initial state, the same as above can be obtained:

$$u_c = \frac{U_m}{Z} X_C \left\{ \sin\left(\omega t + \phi - \varphi - \frac{\pi}{2}\right) + e^{-\alpha t} [(1 + \alpha) \cos(\phi - \varphi) + t \omega \sin(\phi - \varphi)] \right\} \quad (11)$$

3) If it is an oscillating circuit, at this time p_1 and p_2 are a pair of conjugate complex numbers, $p_1 = -\alpha + j\omega_d$, $p_2 = -\alpha - j\omega_d$, which can be obtained under the same initial state:

$$u_c = \frac{U_m}{Z} X_C \left\{ \sin\left(\omega t + \phi - \varphi - \frac{\pi}{2}\right) + \frac{e^{-\alpha t}}{\omega_d} [\omega_0 \sin(\omega_d t + \beta) \cos(\phi - \varphi) + t \omega \sin \omega_d \sin(\phi - \varphi)] \right\} \quad (12)$$

When the EMU enters the neutral zone and low-frequency oscillation occurs, the equivalent circuit is obviously oscillating. According to the principle of circuit superposition, add equations (7) and (6) with equations (12) and (11) respectively, and then we can get the mathematical expression of electric current when the EMU enters the electrical neutral zone.

$$u_c(t) = \frac{U_m}{Z} X_C \sin\left(\omega t + \phi - \varphi - \frac{\pi}{2}\right) + \frac{U_m e^{-\alpha t}}{Z \omega_d C} \sin \omega_d t \sin(\phi - \varphi) + \left[\frac{U_0 \omega_0}{\omega_d} + \frac{U_m X_C}{Z \sin \beta} \cos(\phi - \varphi) \right] e^{-\alpha t} \sin(\omega_d t + \beta) \quad (13)$$

Combining equation (13) at the moment when the EMU enters the articulated electrical neutral zone, the magnitude of the neutral zone's ground voltage is related to the phase angle of the contact line power supply of the traction substation. The neutral zone structure affects the ground capacitance parameter C , it will also determine the voltage oscillation process in the neutral zone. Since the time when the pantograph enters the neutral zone is random, the instantaneous phase angle of the system power supply voltage is different each time the EMU enters the neutral zone. Therefore, when the EMU enters the electrical neutral zone at different times, different electromagnetic transient processes will be generated, resulting in different excitation levels for the roof voltage transformer. The oscillation angular frequency of the circuit ω_0 is higher than the oscillation frequency of the free component ω_d . The oscillation frequency of the free component ω_d decays exponentially. The speed of the decay depends on the attenuation coefficient $\alpha = R/2L$. Obviously, the larger the value α , the faster the amplitude decays, and the shorter time it takes to decay to zero. Taking into account the contact line impedance

$$Z = 0.05 + j0.145lg\frac{D}{d}$$

(14)

The resistance part is 0.05Ω/km, and the resistance value is about 0.01Ω when the length of the neutral zone is 200m.

Comparing the inductance and resistance parameters of the oscillating system, it can be seen that $\alpha=0.001/10000$, the damping in the oscillation process is extremely small, and there is almost no attenuation process.

3.2 Oscillation process and overvoltage characteristics

According to the power supply line percenters and the operation status of the train, a source, power supply line and train system model was established, shown in figure 7. By changing the on-off state of the time-controlled breaker and the position of the PT in the model, the pantograph-net contact state of the over-phase division of the EMU is simulated. The control breaker is in the open state, and switch quickly to the closed state when entering, and the time control switch controls the closing time and then opens.

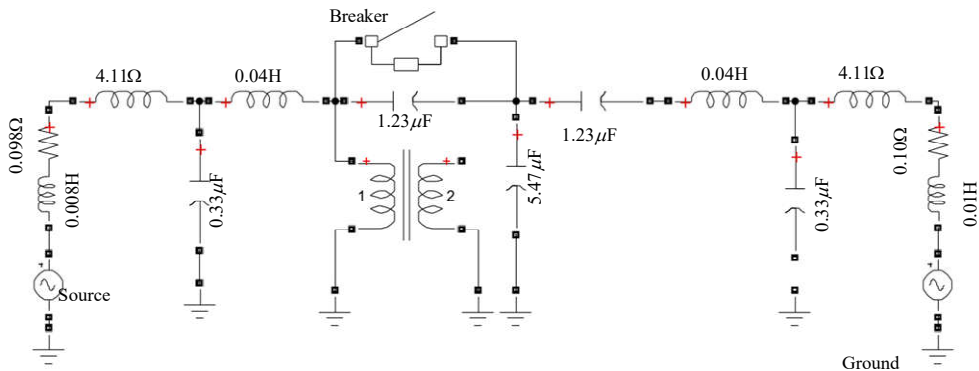


Figure 7 A source, power supply line and train system simulation model

In order to explore the influence of the power phase angle on the occurrence of low-frequency oscillation at the moment of separation of the pantograph and the line, the fixed time-controlled switch is adopted to control the closing and opening time. The power phase angle is changed, the occurrence of low-frequency oscillation in the neutral zone is observed, and the power phase angle range is recorded. The maximum voltage amplitude in the neutral zone is corresponding to different phase angles. Under different phase angle conditions, the maximum amplitude of the voltage of the EMU through the neutral zone is shown in Table VI.

Table VI. Maximum voltage in neutral zone of electrical split					
Phase angle(°)	Voltage (kV)	Phase angle (°)	Voltage (kV)	Phase angle (°)	Voltage (kV)
0	46.70	120	51.78	240	69.75
10	52.25	130	48.37	250	68.85
20	56.15	140	45.10	260	67.61
30	58.80	150	40.53	270	64.44
40	60.64	160	41.80	280	62.25
50	62.30	170	45.39	290	61.29
60	66.22	180	50.11	300	57.81
70	66.12	190	55.04	310	53.40
80	64.11	200	59.57	320	48.50
90	64.98	210	62.00	330	44.55

100	59.25	220	65.17	340	43.84
110	57.01	230	67.84	350	42.74

When the phase angle of the power supply is at 60°~90° and 240°~270°, it has a large amplitude. The phenomenon of low frequency oscillation in the neutral zone is most obvious in these phase angle ranges under the simulation conditions. Under the condition of the same power phase angle, the typical waveform of the low-frequency oscillation of the EMU through the electrical neutral zone is shown in Figure 8.

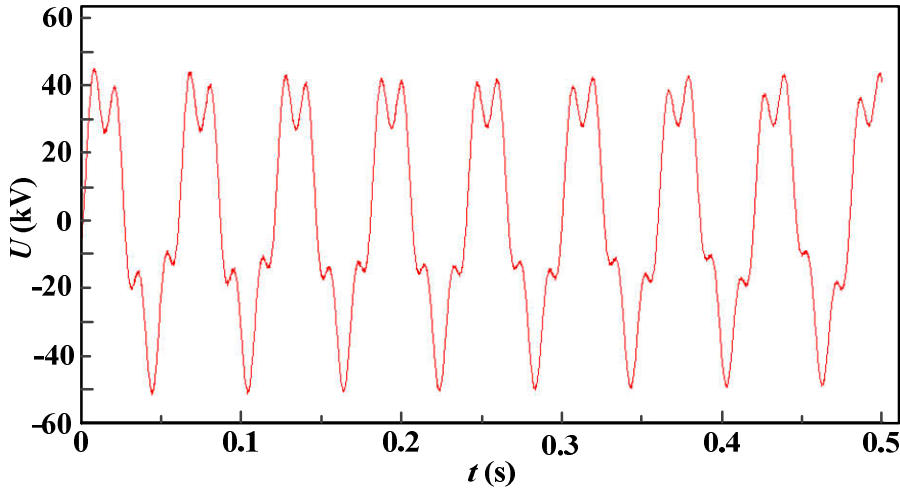


Figure 8. EMU enters the electric split-phase simulation model.

The frequency spectrum of the low-frequency oscillation line voltage in the neutral zone is analyzed, taking 50Hz as the fundamental frequency. When the low-frequency oscillation phenomenon occurs, the contact line voltage in the neutral zone is mainly 1/3 power frequency (16.7Hz) harmonics. Figure 9 shows the spectrum analysis graph of the simulation waveform of abnormal line voltage in the neutral zone area.

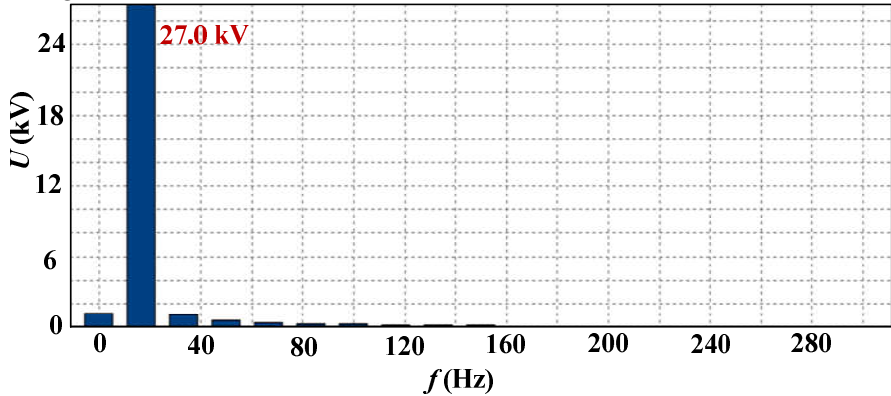


Figure 9. Frequency spectrum of low-frequency oscillation network voltage in phase-separated neutral zone.

In the simulation, the low-frequency oscillation voltage waveform is a periodic oscillation waveform, and there is no non-periodic oscillation phenomenon. The occurrence of abnormal grid voltage is mainly determined by the excitation factor ($p=\omega E$) and damping factor ($q=1/RC$) in the oscillation loop. When the excitation factor is a fixed value, increasing the capacitance or resistance value can reduce the damping factor, which may cause malfunction in the oscillation circuit. The method of increasing the coupling capacitance between the feeding section and the neutral zone is adopted to simulate the abnormal grid voltage phenomenon of the oscillation circuit, as shown in Figure 10.

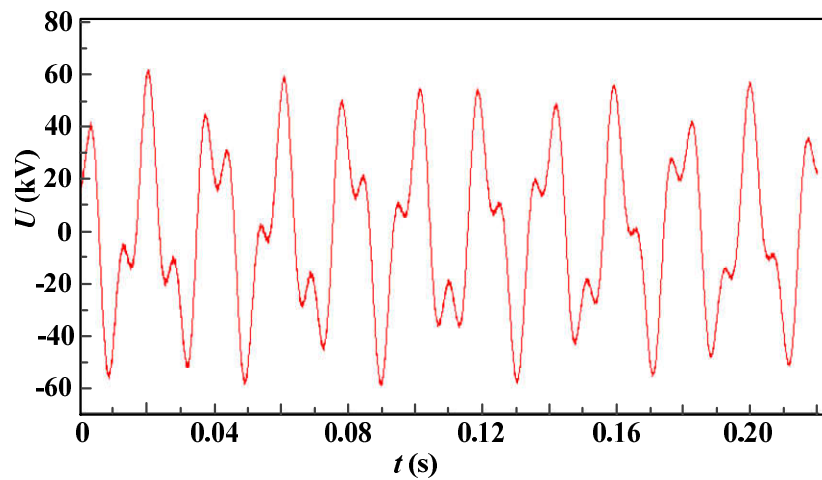


Figure 10. Abnormal network pressure phenomenon in the neutral zone.

The above simulation results show that:

1) The voltage in the neutral zone when the EMU entering the neutral zone is related to the phase angle at the moment when the pantograph separated with the line. If the phase angle when the pantograph separated with the line is between $60^\circ \sim 90^\circ$ and $240^\circ \sim 270^\circ$, the voltage in the neutral zone is large, the maximum amplitude can reach 69.75kV, and low-frequency oscillation will occur in the neutral zone of the electrical neutral zone. The analysis shows that the process of EMU entering the neutral zone has low-frequency oscillation characteristics in the circuit of capacitor voltage and inductance current. Because the phase angle at the time of the separation of the pantograph and the line has randomness, the oscillation process is also random. Therefore, it is verified that within a certain range of power phase angle, the neutral zone will produce a higher overvoltage. The over voltage will stimulate the roof voltage transformer to produce low-frequency oscillation, indicating that the occurrence of low-frequency oscillation is related to power source phase angle when the EMU enters the neutral zone.

2) According to spectrum analysis, when low-frequency oscillation occurs, the voltage of the contact line in the neutral zone is mainly 1/3 power frequency (16.7 Hz) harmonics. This is the same as the frequency characteristics of the measured case of low-frequency oscillation when EMU passes the neutral zone. This match verifies the accuracy of the simulation model.

3) The simulation waveform of the low-frequency oscillation voltage in the neutral zone of the EMU is a periodic oscillation waveform, and there is no non-periodic oscillation. If the length of the feeding section is appropriately increased or the coupling capacitance in the neutral zone is changed, the low-frequency oscillation line voltage in the neutral zone can be slightly suppressed.

3.3 Methods of Suppressing Oscillation Process

As shown in Figure 10, R_1 and L_1 are the equivalent impedance of the contact line power supply, C_1 is the equivalent capacitance of the traction power system, R_2 and C_2 represent the resistance and capacitance in the protection device, respectively. Figure 11(a) only considers the case of parallel resistance. Analysis of this second-order circuit shows that the increase in parallel resistance reduces the damping of the system, and the overvoltage value decreases. Figure 11(b) only considers the case of parallel capacitors. The same analysis of the second-order circuit shows that the parallel capacitors increase the damping of the system and reduce the overvoltage value. The following equation mainly analyzes the situation in Figure 11(c). After the switch S is closed, the differential equation about the capacitor voltage u_{c1} can be listed:

$$R_1 (i_1 + i_2) + L \frac{d(i_1 + i_2)}{dt} + u_{c_1}(t) = u_s(t) \quad (15)$$

$$R_2 i_2 + u_{C_2} = u_{C_1} \quad (16)$$

$$i_1 = C_1 \frac{du_{C_1}}{dt} \quad (17)$$

$$i_2 = C_2 \frac{du_{C_2}}{dt} \quad (18)$$

Using Laplace transform, we can obtain:

$$\Phi(s) = \frac{u_{C_1}(s)}{u_s(s)} = \frac{1 + R_2 C_2 s}{LR_2 C_1 C_2 s^3 + (LC_1 + LC_2 + R_1 R_2 C_1 C_2) s^2 + (R_1 C_1 + R_1 C_2 + R_2 C_2) s + 1} \quad (19)$$

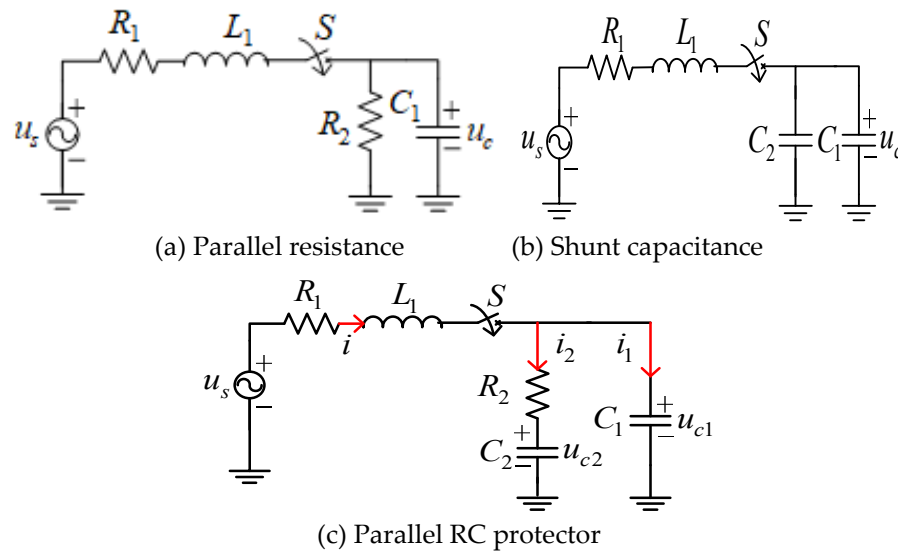


Figure 11. Simple equivalent circuit diagram.

MATLAB is used to analyze the unit step response of the transfer function, and the results are shown in Figure 12 to Figure 13.

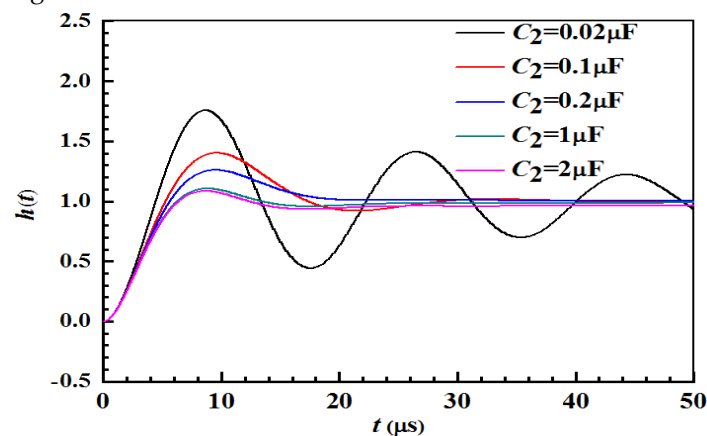


Figure 12. Step response under different capacitance values (keep the resistance R_2 at 200Ω unchanged)

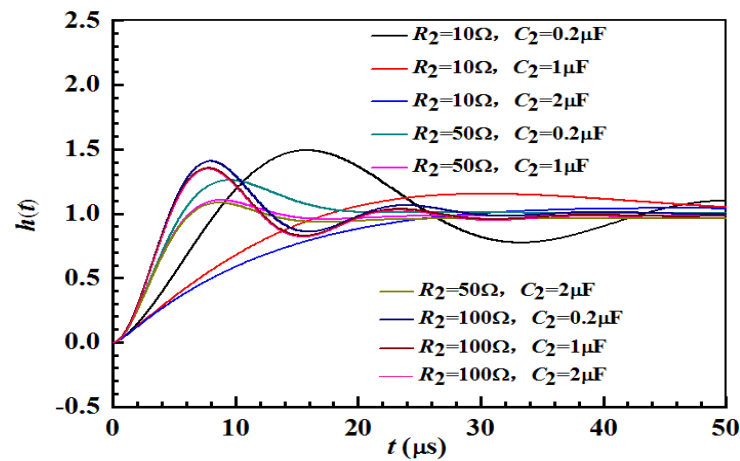


Figure 13. Step response under different resistance and capacitance.

According to the low frequency oscillation excitation characteristic test of the voltage transformer, the equivalent circuit of the neutral zone after installing RC protection device is shown in Figure 13. The transient process of the EMU passing the neutral zone is simulated with PSCAD/EMTDC software, and the simulation model is shown in Figure 14.

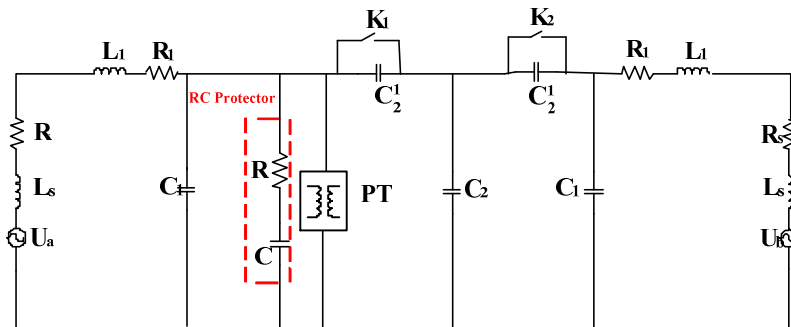


Figure 14. Equivalent circuit diagram of over-phase division of EMU.
(additional RC device in the neutral zone)

Under the same simulation conditions as the original low-frequency oscillation, an RC device was installed in the neutral zone, and the voltage waveform of the contact line in the neutral zone is shown in Figure 15.

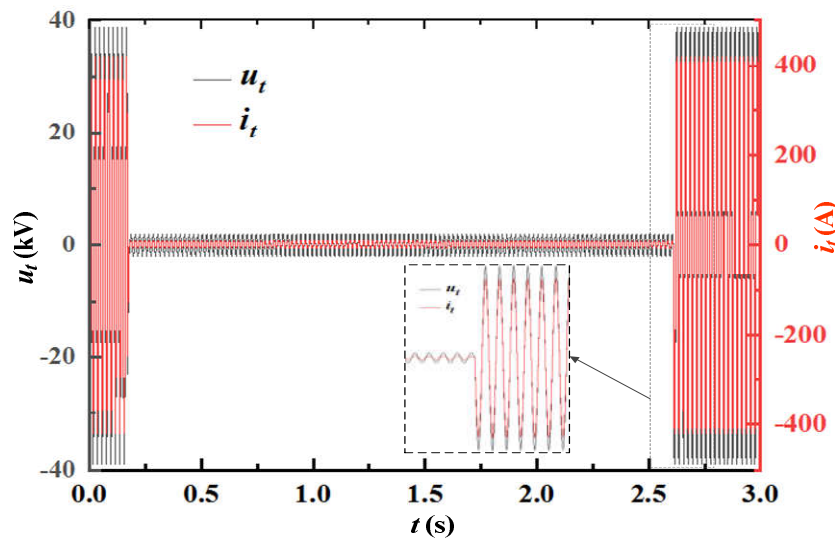


Figure 15. Voltage waveform of the neutral zone.

It can be seen from the simulation waveform that after the suppression device is installed, when the EMU enters the electrical neutral zone and the time-controlled switch in the simulation model is closed, the absolute value of the voltage peak drops to below 20 kV. Compared with the situation without the suppression device, the absolute value of the peak voltage has been reduced by nearly 30%, and the low frequency oscillation has been effectively suppressed. In the simulation, the equivalent circuit of the RC protection device connected in parallel to the roof voltage transformer or the neutral zone of the electric neutral zone is the same, and the suppression effect on the low frequency oscillation is also the same.

4. Conclusions

The article combines model calculation and field test analysis to study the mechanism of low-frequency oscillation when the EMU passes the neutral zone and proposes suppression methods. The detailed conclusions of the study are as follows:

- (1) Under normal operating conditions when the EMU enters the neutral zone, due to the opening and closing of the circuit breaker, the change of the equivalent circuit of the vehicle line leads to obvious operating overvoltage, while the neutral zone line voltage is very small. When there is an abnormal increase in the grid voltage in the neutral zone, the grid voltage waveform has obvious low frequency oscillation characteristics. When the amplitude of the oscillation voltage is obvious, it can reach 51.8kV, which is 1/3 power frequency low-frequency oscillation.
- (2) The voltage in the neutral zone of the EMU during the electrical separation is related to the power phase angle at the moment when the EMU enters the electrical neutral zone. When the phase angle of the power supply separation between the pantograph and the line is within the range of $60^{\circ}\sim 90^{\circ}$ and $240^{\circ}\sim 270^{\circ}$, the voltage amplitude in the neutral zone is relatively large, and the maximum amplitude can reach 69.75kV. Low-frequency oscillation will also occur in the neutral zone. When low-frequency oscillation occurs, the contact line voltage in the neutral zone is mainly 1/3 power frequency (16.7 Hz).
- (3) After installing the RC suppression device in the neutral zone, when the EMU enters the electrical neutral zone, the absolute value of the voltage peak drops to below 20 kV. Compared with the case where the suppression device is not connected, the absolute value of the voltage peak is reduced by nearly 60%. And the low-frequency oscillation phenomenon can be effectively suppressed.

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