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## Article

# Absence of Weak Localization Effects in Strontium Ferromolybdate

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**Abstract:** Sr<sub>2</sub>FeMoO<sub>6-δ</sub> (SFMO) double perovskite is a promising candidate for room-temperature spintronic applications since it possesses a half-metallic character (with theoretically 100% spin polarization), a high Curie temperature of about 415 K, and a low-field magnetoresistance (LFMR). However, due to different synthesis conditions of ceramics as well as thin films, different mechanisms of electrical conductivity and magnetoresistance prevail. In this work, we consider the weak localization effect in SFMO occurring in disordered metallic or semiconducting systems at very low temperatures due to quantum interference of back-scattered electrons. We calculate the quantum corrections to conductivity and the contribution of electron scattering to the resistivity of SFMO. We attribute the temperature dependence of SFMO ceramics resistivity in the absence of a magnetic field to the fluctuation induced tunneling model. Also, we attribute the decreasing resistivity in the temperature range from 409 K up to 590 K to adiabatic small polaron hopping and not to localization effects. Both fluctuation induced tunneling and adiabatic small polaron hopping do not favor quantum interference. Additionally, we demonstrate that the resistivity upturn behavior of SFMO cannot be explained by weak localization. Consequently, to the best of our knowledge, there is still no convincing evidence for the presence of weak localization in SFMO.

**Keywords:** strontium ferromolybdate; electrical conductivity; weak localization

## 1. Introduction

In a disordered electronic system, the electron motion is diffusive due to scattering at non-uniformities. Weak localization is a physical effect which occurs in disordered electronic systems at very low temperatures. The effect manifests itself as a correction  $D_s$  to the conductivity (or correspondingly the resistivity) of a metal or semiconductor arising in the case that the mean free path  $l$  is in the order of the wavelength  $\lambda_F = 2\pi/k_F$  of the carrier wavefunctions, i.e.  $kl \sim 1$ , with  $k_F$  denoting the Fermi wave vector. The weak localization correction comes from quantum interference of back-scattered electrons. Labeling all the trajectories by the time  $t$  it takes for a classical particle to go around a loop, the classical probability  $dP$  that the diffusing particle returns into the phase volume  $dV$  at a given time  $t$  is given by [1] (p. 153)

$$dP = \frac{dV}{(4\pi Dt)^{d/2}} \quad (1)$$

where  $P$  is the probability for a quantum mechanical particle to return to the starting point (the wave function of both time-reversed paths will constructively interfere with each other),  $D = v_F^2 t / d$  is the diffusion constant,  $t$  is the elastic scattering time and  $d$  is the dimension. The relevant phase volume can be estimated as  $v_F dt (\delta\rho\delta\varphi)^{d-1}$  [2,3], where  $v_F = (2E_F/m_e)^{1/2}$  is the Fermi velocity,  $E_F$  the Fermi energy,  $m_e$  the electron mass,  $\delta\rho$  and  $\delta\varphi$  characterize the transverse distance between the electron trajectories 1 and 2 at the intersection point and  $\delta\varphi$  is the intersection angle between the both trajectories. For the interference between paths 1 and 2 to be effective, the uncertainty relation should hold

$$p_F \delta \rho \delta \phi = \hbar k_F \delta \rho \delta \phi = h \quad (2)$$

where  $p_F = m_e v_F$  is the Fermi momentum and  $h$  the Planck constant. This leads to a relative change in conductivity of two and three dimensional systems yielding [1] (p. 183):

$$\begin{aligned} \frac{\delta \sigma_{2D}}{\sigma_0} &= -\frac{2}{\pi k_F l_e} \ln \frac{l_\phi}{l_e}, \\ \frac{\Delta \sigma_{3D}}{\sigma_0} &= -\frac{3}{2(k_F l_e)^2} \end{aligned} \quad (3)$$

where  $\sigma_0$  is the residual low temperature conductivity taken as the Drude conductivity, i.e.  $\sigma_D = e^2 n_e t_e / m_e$ , determined by relaxation time  $t$  of the dominating charge scattering mechanism, the electron charge  $e$ , the electron density  $n_e$ , the elastic scattering time  $\tau_e$  and the electron mass  $m_e$ . In eq. (3), the negative sign is due to the fact that the returning trajectory should arrive at the intersection point with the momentum almost opposite to the initial one. This means that interference lowers the conductivity. Note that for small sizes  $b$  the volume  $(Dt)^{d/2}$  should be replaced by  $(Dt)^{d/2} b^{3-d}$  since the charge carrier has a chance to diffuse repeatedly from one wall to the other and the probability of finding it at any point across films or wires limited in size will be the same [4]. However, we are considering macroscopic sizes rather than sizes of the order of atomic distances. The lower cutoff  $\tau_e$  is justified with the fact that within a time  $\tau_e$  no elastic scattering occurs, and therefore there will be no closed trajectories. The upper limit is given by [5]:

$$\tau_\phi^{-1} \sim \left( \frac{T}{D^{d/2} N_0 a^{3-d}} \right)^{2/(4-d)}, \quad (4)$$

where  $D = (v_F^2 t_e / d)$  is the diffusion constant,  $N_0$  is the one-spin density of states,  $d$  the characteristic sample dimension. The phase coherence time  $t_\phi$  defines the phase coherence length  $l_\phi = (Dt_\phi)^{1/2}$ . This yields conductivity corrections for two and three dimensional systems amounting in terms of quantum conductance  $e^2/h$  to [1] (p. 282):

$$\begin{aligned} \Delta \sigma_{2D} &= -\frac{2e^2}{\pi h} \ln \frac{l_\phi}{l_e} = -\frac{e^2}{\pi h} \ln \left( \frac{l_\phi}{l_e} \right)^2, \\ \Delta \sigma_{3D} &= -\frac{e^2}{\pi h} \left( \frac{1}{l_e} - \frac{1}{l_\phi} \right), \end{aligned} \quad (5)$$

with  $l_e$  the mean free path of the electron.

Temperature modifies the phase coherence length  $l_\phi$  and, therefore, modifies the weak localization correction. The temperature dependence of  $l_\phi$  can be described as [6,7]

$$\frac{1}{l_\phi^2(T)} = \frac{1}{l_\phi^2(0)} + A_{ee} T^{p_1} + A_{ep} T^{p_2}, \quad (6)$$

where  $l_\phi(0)$  is the zero-temperature phase coherence length and  $A_{ee} T^{p_1}$  and  $A_{ep} T^{p_2}$  represent the contributions from two different dephasing mechanisms, e.g. electron-electron (ee) and electron-phonon (ep) interactions, respectively. Note that the temperature exponents  $p_1$  and  $p_2$  changes fundamentally with the system dimensionality [8]. If electron-electron interaction is the dominant dephasing mechanism (also denoted as Nyquist dephasing mechanism), this gives rise to  $\tau_{ee} \propto T^{-p}$  with values of  $p$  equal to 0.66, and 1 for  $d = 1$  and  $d = 2$ , respectively [1] (chapter 13.6.4), [5]. For  $d = 3$  eq. (4) yields  $p = 2$  while the result in [1] (p. 509) is  $p = 1.5$ . The electron-phonon interaction decoherence mechanism would provide a temperature dependence of the dephasing time  $t_\phi \propto T^{-3}$  [9]. Typically, one finds  $\tau_\phi \approx \tau_{ep} \propto T^{-p}$  with the exponent of temperature  $p \approx 2-4$ .

In metals and semiconductors at low temperatures, quasielastic (small energy transfer) electron-electron scattering is the dominant dephasing process. Assuming only one dephasing process and accounting that  $l_\phi(0)$  is in the order of 50 nm to several micrometers, that is, usually  $l_\phi(0) \gg l_\phi(T)$  [6,7,10–12], a simplified approximation formula is given by [11]:

$$\frac{1}{l_\phi^2(T)} \approx A' T^{p_1}, \quad (7)$$

with  $p_1 = 1$  for quasielastic electron-electron scattering in agreement with experimental results in Bi<sub>2</sub>Te<sub>3</sub> thin films [13], 50 nm-thick Cd<sub>3</sub>As<sub>2</sub> films [11], Bi<sub>2</sub>Te<sub>3</sub> single crystals [7], Mo<sub>x</sub>W<sub>1-x</sub>Te<sub>2+d</sub> ultrathin films [14]. As a result, we obtain for quasi-elastic electron-electron scattering:

$$l_\phi^2 = l_\phi^2(T_0) \cdot \frac{T_0}{T}, \quad (8)$$

Consequently, eq. (5) transforms to

$$\begin{aligned} \Delta\sigma_{2D,WL} &= -\frac{e^2}{\pi h} \ln\left(\frac{l_\phi^2(T_0)}{l_e^2} \cdot \frac{T_0}{T}\right) = \frac{e^2}{\pi h} \ln\left(\frac{l_e^2}{l_\phi^2(T_0)} \cdot \frac{T}{T_0}\right) = \\ &= \frac{e^2}{\pi h} \left[ \ln\left(\frac{l_e^2}{l_\phi^2(T_0)}\right) + \ln\left(\frac{T}{T_0}\right) \right], \quad (9) \\ \delta\sigma_{3D,WL} &= -\frac{e^2}{\pi} \left( \frac{1}{l_e} - \frac{1}{l_\phi} \right) = -\frac{e^2}{\pi \cdot l_e} + \frac{e^2}{\pi \cdot l_\phi(T_0)} \left( \frac{T}{T_0} \right)^{1/2} \end{aligned}$$

Finally, the total conductivity consisting of 2D at high magnetic fields and 3D contributions is written as:

$$\sigma(T) = \sigma_0 + A \cdot \ln\left(\frac{T}{T_0}\right) + B \cdot \left(\frac{T}{T_0}\right)^{1/2}, \quad (10)$$

with

$$\sigma_0 = \sigma_D - \frac{e^2}{\pi h b} \cdot \ln\left(\frac{l_\phi^2(T_0)}{l_e^2}\right) - \frac{e^2}{\pi h \cdot l_e}, \quad (11)$$

and the coefficients:

$$A = \frac{e^2}{\pi h b}, \quad B = \frac{e^2}{\pi h \cdot l_\phi(T_0)}, \quad (12)$$

where  $b$  is the effective thickness of the 2D layer introduced to convert a 2D conductivity to a 3D one. A minimum of conductivity appears only when the second right-side term in Equation (10) changes sign, i.e.:

$$B = -\frac{2A}{(T_{\max}/T_0)^{1/2}} \Big|_{T_0=T_{\max}} = -2A, \quad (13)$$

With regard to Equation (10), quantum correction to residual conductivity may be written as [15]:

$$\Delta\sigma(T) = A \ln T + B T^{1/2}, \quad (14)$$

Assuming that Mathiessen's rule holds, and representing resistivity as a sum of elastic and inelastic contributions where the latter increase with increasing temperature due to a power law (e.g. a term  $CT^n$ ), the resistivity data can be fitted to [16,17]:

$$\rho(T) = \frac{1}{\sigma_0 + A' \ln T + B' T^{1/2}} + C_n T^n, \quad (15)$$

with  $n$  equal to 3/2, 2, 3, depending on the dominant scattering mechanism [18].

Separate conductivity quantum correction terms in the form  $A' \ln T$  and  $B' T^{1/2}$  were introduced for  $\text{La}_{0.7}\text{Ca}_{0.3}\text{MnO}_3$  by Kumar et al [19]. Here, the first term  $A' \ln T$  was attributed also to the Kondo effect [20]. In order to account for higher order scattering mechanisms and to extend the analytical description to higher temperatures, an additional term  $CT^n$  was included. The electron-electron interaction term  $B' T^{1/2}$  was applied also to  $\text{La}_{0.7-x}\text{Y}_x\text{Sr}_{0.3}\text{MnO}_3$  ( $0 \leq x \leq 0.2$ ) ceramics of 1 mm thickness [21], to  $\text{La}_{0.7}\text{A}_{0.3}\text{MnO}_3$  ( $\text{A}=\text{Ca}, \text{Sr}, \text{Ba}$ ) ceramics [22], to  $\text{La}_{0.6}\text{Re}_{0.1}\text{Ca}_{0.3}\text{MnO}_3$  ( $\text{Re} = \text{Pr}, \text{Sm}, \text{Gd}, \text{Dy}$ ) ceramics of 1 mm thickness all three prepared by conventional solid state reaction [23], to  $\text{SrRuO}_3$  thin films with a thickness of 6 to 8 nm deposited by pulsed laser deposition onto (100) $\text{SrTiO}_3$  substrates [16], to ultrathin  $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$  films (3.5 to 40 nm), deposited by molecular beam epitaxy [17], and to metallic  $\text{SrRuO}_3$  and  $\text{LaNiO}_3$  thin films deposited by pulsed laser deposition with a thickness of 6 and 240 nm, respectively [24].

In the  $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$  ultrathin film case, a crossover from  $T^{1/2}$  to a  $\ln T$  behavior in the low-temperature resistivity dependence with decreasing thicknesses was related to a change in the dimensionality of the system, going from 3D for samples thicker than 20 nm to 2D in the limit of ultrathin samples. The origin of this effect is that in the case of a film thickness larger than the Landau orbit length  $L_H = (\hbar/2eB)^{1/2}$  the system behaves essentially as 3D while in the opposite electron confinement results in a 2D behavior of the system. In the 3D case of metallic and ferromagnetic  $\text{SrRuO}_3$  and of metallic and paramagnetic  $\text{LaNiO}_3$  epitaxial thin films the term  $B' T^{1/2}$  was splitted into two terms where in the 3D case first term  $b_1 T^{p/2}$  accounts for the weak localization and the  $b_2 T^{1/2}$  term stands for the renormalized electron-electron interaction quantum corrections [25]. In the 2D case, both these quantum corrections to conductivity have a similar temperature dependence. Here, only a  $\ln T$  term remains. The quantum correction of conductivity in metallic  $\text{LaNi}_{1-x}\text{Co}_x\text{O}_3$  ( $0 \leq x \leq 0.75$ ) below 2 K follows a power law  $BT^m$  where away from the metal-insulator transition ( $x \leq 0.4$ )  $m$  takes a value of  $m = 0.3 \dots 0.4$ . Such power-law conductivities are seen at the metallic side of the metal-insulator transition also for other  $\text{ABO}_3$  oxides [26].

In this work, we attribute the temperature dependence of the SFMO ceramic resistivity in the absence of a magnetic field to the fluctuation induced tunneling model and the decrease of resistivity in the temperature range from 409 K up to 590 K not to localization effects but to adiabatic small polaron hopping. Both fluctuation induced tunneling and adiabatic small polaron hopping do not favor quantum interference. Also, we demonstrate that the resistivity upturn behavior of SFMO cannot be explained by the weak localization effect.

## 2. Methods

First we estimate the coefficient  $A'$  in Equation (15). Taking  $l_f < 0.46$  nm at room temperature [27] and  $b = 20$  nm [17], the ratio of the coefficients  $A'/B'$  will be in the order of  $10^{-2}$ . Since for arguments larger than one the natural logarithm function will be smaller than the root function, the logarithmic term can be neglected. A further indication of small  $A'$  coefficients arises from the depth of the conductance minimum, i.e. the difference  $r(0) - r(T_{min})$ , which changes with increasing magnetic flux [19]. Values of above 35 mW·cm in the absence of a magnetic field down to 2.4 mW·cm at 7 T [28] yield coefficients  $A' = 10^{-2} \cdot (r(0) - r(T_{min}))$  [20,29]. In  $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$  ultrathin films (3.5 to 40 nm), deposited by molecular beam epitaxy [17], the agreement of fits of conductivity data to equation (15) with only the  $A' \ln T$  term ( $B' = 0$ ) was much worse than in the case with only the  $B' T^{1/2}$  term ( $A' = 0$ ). Therefore, we neglect in the following the term  $A' \ln T$ . This corresponds to the common practice of describing similar materials like  $\text{La}_{0.7-x}\text{Y}_x\text{Sr}_{0.3}\text{MnO}_3$  ( $0 \leq x \leq 0.2$ ) ceramics of 1 mm thickness prepared by conventional solid state reaction [21],  $\text{La}_{0.7}\text{A}_{0.3}\text{MnO}_3$  ( $\text{A}=\text{Ca}, \text{Sr}, \text{Ba}$ ) ceramics prepared by

conventional solid state reaction [22], and SrRuO<sub>3</sub> thin films with a thickness of 6 to 8 nm deposited by pulsed laser deposition onto (100)SrTiO<sub>3</sub> substrates [16].

The coefficient  $B'$  is given by [15]:

$$B' = .0309 \frac{e^2}{\hbar} \cdot \sqrt{\frac{k}{\hbar D}} = \frac{2.72149 \cdot \Omega^{-1} \text{K}^{-1/2} \text{s}^{-1/2}}{\sqrt{D[\text{m}^2 / \text{s}]}}. \quad (16)$$

with  $\hbar = h/2\pi$  the Planck constant expressed in J s radian<sup>-1</sup>. For a mean free path  $l_e$  of 0.46 nm at room temperature [27] and a carrier relaxation time  $\tau$  of  $1.6 \times 10^{-14}$  s [30], the carrier diffusion constant will be  $1.32 \times 10^{-5} \text{ m}^2 \text{ s}^{-1}$  yielding a coefficient  $B' \approx 748 \text{ W}^{-1} \text{ m}^{-1} \text{ K}^{-1/2}$  in satisfactory agreement with values of  $B' \approx 360 \dots 500 \text{ W}^{-1} \text{ m}^{-1} \text{ K}^{-1/2}$  in  $(\text{Ni}_{0.5}\text{Zr}_{0.5})_{1-x}\text{Al}_x$  metallic glasses [31] and with a universal value of  $B' \approx 600 \text{ W}^{-1} \text{ m}^{-1} \text{ K}^{-1/2}$  of amorphous and disordered metals [32]

The coefficient  $C_n$  was calculated as follows: We start with Drude conductivity:

$$\rho_D = \frac{\hbar k_F}{n_e e^2 l_e}, \quad (17)$$

where  $n_e$  the electron density and  $e$  the electron charge. Taking  $n_e = 1.1 \times 10^{28} \text{ m}^{-3}$  [33] we obtain  $\hbar k_F = 4.8 \cdot 10^{-25} \text{ Jsm}^{-1}$  and

$$\rho_D = \frac{1.87 \cdot 10^{-15} \Omega \text{m}}{l_e[\text{m}]}, \quad (18)$$

We assume electron mean free paths  $l_e = 0.46 \text{ nm}$  and  $1.11 \text{ nm}$  at room temperature and 4 K, respectively, calculated from the ordinary Hall coefficient [27]. This yields  $r_D = 4.07 \text{ } \mu\text{Wm}$  at room temperature and  $r_D = 1.68 \text{ } \mu\text{Wm}$  at 4 K in satisfactory agreement with experimental data of single crystal SFMO in [34]. Now we assume that in a ferromagnetic state below room temperature magnetic scattering controls electrical transport in SFMO at low temperatures [27]. The mean free path of electron scattered by a spin wave with energy  $E_s$  travelling through the bcc I4/mmm lattice in thermal equilibrium at a temperature  $T$ , is given by [35]:

$$l_e = \frac{S^2 V^{1/3} \theta^{-7/2}}{\pi \zeta(3/2) (E_s / kT)} \approx 0.38 \cdot S^{9/2} a \cdot \left( \frac{J}{kT} \right)^{5/2}, \quad (19)$$

where  $S$  is the effective spin  $S_{\text{eff}} = (S_{\text{Fe}} S_{\text{Mo}})^{1/2} = (1/2 \cdot 5/2)^{1/2} = 1.118$ ,  $V$  the unit cell volume,  $q$  a dimensionless temperature,  $z$  the Rieman Zeta function,  $a$  the lattice constant, and  $J$  the exchange constant of the 180° Fe-O-Fe interaction amounting to -25 K [36,37]. Finally, we arrive at:

$$\rho_D = 2.413 \cdot 10^{-9} \cdot T^{5/2} \Omega \text{m}, \quad (20)$$

Compared to the experimental value of  $R_{2.5} = 1.4 \times 10^{-11} \text{ WmK}^{-5/2}$  in a relation  $r = r_0 + R_{2.5} T^{2.5}$  the calculated value of  $R_{2.5}$  is overestimated by almost two orders of magnitude in part due to the approximation of the Fermi surface as a sphere and the disregard of additional  $s$ - $d$  transitions in transition metals which reduce the mean free path [38]. Also, the value of  $R_{2.5}$  may be lowered by assuming a higher effective spin.

### 3. Results and discussion

Strontium ferromolybdate Sr<sub>2</sub>FeMo<sub>6</sub>-d (SFMO) is a half-metallic, ferrimagnetic compound with a saturation magnetization of 4  $\mu\text{B/f.u.}$  [28]. However, SFMO does not exhibit a general metallic conductivity mechanism. In the absence of a magnetic field, the temperature dependence of conductivity of SFMO ceramics [28] is well described by the fluctuation-induced tunneling (FIT) model [39], e.g., by the presence of conducting grains separated by nanosized energy barriers where large thermal voltage fluctuations occur when the capacitance of an intergrain junction is in the order of 0.1 fF. Here, tunneling occurs between large metallic grains via the intergrain junctions with a



width  $w$  and area  $A$ . The FIT model is specified by three parameters [39]: (i) The temperature  $T_1$  characterizing the electrostatic energy of a parabolic potential barrier,

$$kT_1 = \frac{A \cdot w \cdot \epsilon_0 E_0^2}{2}, \quad (21)$$

where  $k$  is the Boltzmann constant and the characteristic field  $E_0$  is determined by:

$$E_0 = \frac{4V_0}{e \cdot w}, \quad (22)$$

(ii) the temperature  $T_0$  representing  $T_1$  divided by the tunneling constant,

$$T_0 = T_1 \cdot \left( \frac{\pi \chi w}{2} \right)^{-1}, \quad (23)$$

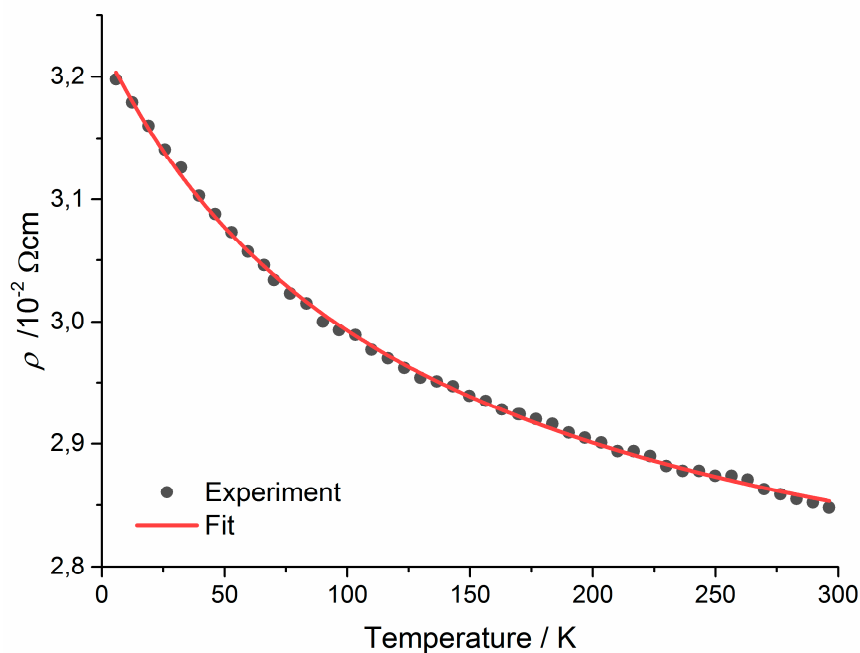
with the reciprocal localization length of the wave function

$$\chi = \sqrt{\frac{2m^*V_0}{\hbar^2}}, \quad (24)$$

where  $m^*$  is the effective electron mass, and (iii) the residual resistivity  $r_0$ . The resulting resistivity of this model is then given by [39]:

$$\rho(T) = \rho_0 \exp\left(\frac{T_1}{T_0 + T}\right), \quad (25)$$

In our case, the model parameters amount to  $T_0 = 141.1$  K,  $T_1 = 25.6$  K and  $s_0 = 1/r_0 = 37.16$  S/cm (cf. Figure 1). The FIT model was recently applied to intergrain tunneling in polycrystalline  $\text{Sr}_2\text{CrMoO}_6$  and  $\text{Sr}_2\text{FeMoO}_6$  ceramics [40], in half-metallic double-perovskite  $\text{Sr}_2\text{BB}'\text{O}_6$  ( $\text{BB}' = \text{FeMo}$ ,  $\text{FeRe}$ ,  $\text{CrMo}$ ,  $\text{CrW}$ ,  $\text{CrRe}$ ) ceramics [41] and in  $\text{Ba}_2\text{FeMoO}_6$  thin films [42].



**Figure 1.** Fitting of the conductivity data of SFMO ceramics at zero magnetic flux [28] to the fluctuation induced tunneling model [39]. Fitting parameters are:  $T_0 = 141.1$  K,  $T_1 = 25.6$  K and  $s_0 = 37.16$  S/cm.

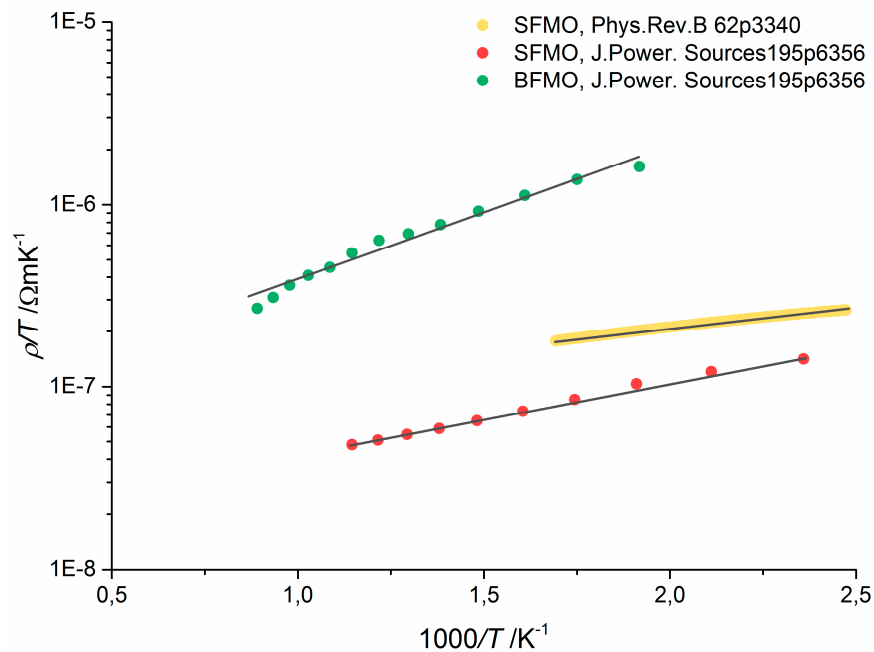
One feature attributed to weak localization in SFMO ceramics is the decrease of resistivity in the temperature range between 405 K and 590 K [43]. In the following this resistivity behavior should be considered more in detail. According to [43], the resistivity behavior of vacuum-annealed SFMO ceramics above room temperature is separated into three regions: (i) From 300 K up to the Curie temperature of about 405 K the electrical resistivity increases with temperature and shows metallic behavior, (ii) Above 405 K up to approximately 590 K the resistivity decreases with temperature, (iii) Finally, from 590 K up to 900 K the resistivity increases since the material becomes metallic again [43].

Another report on the electrical resistivity of SFMO indicates metallic behavior up to 420 K, a decrease of resistivity in the temperature range 420–820 K, and the reversion to metallic behavior between 820 and 1120 K [44]. A similar resistivity behavior with a resistivity maximum at about 450 K, far above the Curie temperature of ~330 K [45], was obtained for  $\text{Ba}_2\text{FeMoO}_{6-\delta}$  while  $\text{Ca}_2\text{FeMoO}_{6-\delta}$  shows solely metallic behavior in the whole temperature range 320–1120 K [44].

A more detailed consideration of the reported resistivity behavior of  $\text{Sr}_2\text{FeMoO}_{6-\delta}$  and  $\text{Ba}_2\text{FeMoO}_{6-\delta}$  above  $T_c$  [43,44], reveals a convincing fit to the adiabatic small polaron hopping model [46] (Figure 2). In the small polaron model, electrical conduction of perovskites at higher temperature, i.e., above a certain transition temperature, occurs by small polarons moving through the lattice by thermally activated jumps between neighboring sites. The transition temperature from small polaron motion in a conduction band to small polaron hopping was estimated to be in the order of  $\theta_D/2$  with  $\theta_D$  the Debye temperature which amounts to 338 K for SFMO [47]. The adiabatic small polaron hopping model yields a resistivity of [46]:

$$\rho = \rho_0 T \exp\left(\frac{E_a}{kT}\right), \quad (26)$$

where  $E_a$  is the thermal activation energy. The obtained  $E_a$  values are 0.045–0.08 eV for  $\text{Sr}_2\text{FeMoO}_{6-\delta}$  and about 0.13 eV for  $\text{Ba}_2\text{FeMoO}_{6-\delta}$  and are in the order of the values of other perovskites and double perovskites:  $\text{La}_{1-x}\text{Sr}_x\text{Co}_{1-y}\text{Fe}_y\text{O}_3$  [48],  $\text{Sr}_{1.6}\text{Sm}_{0.4}\text{MgMoO}_{6-\delta}$ ,  $\text{Sr}_{1.4}\text{Sm}_{0.6}\text{MgMoO}_{6-\delta}$ , and  $\text{Sr}_{1.2}\text{Sm}_{0.8}\text{MgMoO}_{6-\delta}$  [49], as well as  $\text{Sr}_2\text{Fe}_{1.5}\text{Mo}_{0.5}\text{O}_{6-\delta}$  and  $\text{Sr}_2\text{Fe}_{1.5}\text{Mo}_{0.5-x}\text{Nb}_x\text{O}_{6-\delta}$  [50].



**Figure 2.** Fitting of the conductivity data of  $\text{Sr}_2\text{FeMoO}_6$  ceramics between 405 K and 590 K [43] as well as of  $\text{Sr}_2\text{FeMoO}_6$  ceramics between 420 and 870 K and  $\text{Ba}_2\text{FeMoO}_6$  ceramics between 520 and 1120 K [44] to the adiabatic small polaron hopping model [46].



Weak localization effects were taken into account in order to explain the presence of minima in the  $\rho$ - $T$  curves of perovskite oxides exhibiting metallic conductivity [17,19,25,51,52]. It has been suggested [20,21] that the resistivity minimum and, consequently, the resistivity upturn at lower temperature arises from the competition of two contributions—one, usual, increasing and the other, decreasing with the increase of the temperature. In eq. (15), the corresponding terms are  $(B'\ln T)^{-1}$  and  $C_n T^n$ , respectively. The resistivity versus temperature plots of SFMO ceramics in a magnetic field [28] are very similar to the ones of  $\text{La}_{0.7}\text{Ca}_{0.3}\text{MnO}_3$  and  $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$  thin films [17,19]. Also here, a resistivity minimum appears in polycrystalline SFMO ceramics at low temperature [28] which was explained by weak localization [52]. In this case, a quantum correction terms  $A_W T^{p/2}$  [17,52] was added to the residual resistivity  $s_0$  and an electron interaction term  $A_p T^n$  to the resistivity. A similar approach was applied to perovskite ceramics ( $\text{LaNi}_x\text{Co}_{1-x}\text{O}_3$  and  $\text{Na}_x\text{Ta}_y\text{W}_{1-y}\text{O}_3$  [53],  $\text{La}_{0.5}\text{Pb}_{0.5}\text{MnO}_3$  and  $\text{La}_{0.5}\text{Pb}_{0.5}\text{MnO}_3$  ceramics containing 10 at.% Ag in a dispersed form [15].

To evaluate the origin of the low temperature resistivity minimum in SFMO, we fitted the experimental data [28] to eq. (15) assuming  $A' = 0$  (Figure 3, Table 1). The increase of the  $s_0(B)$  values correspond to a negative magnetoresistance obtained in ferrimagnetic SFMO ceramics which arises due to the suppression of spin disorder by the magnetic field [27,28,43]. The fitted  $s_0$  values describe a power law magnetic flux dependence of the magnetoresistance,  $-MR \propto B^m$ , with a power of  $m = 0.284$ . This value lies in-between the values of  $m = 0.5$  for metallic behavior and electron-electron interaction in the temperature range between the temperature of minimum resistivity and the Curie temperature and  $m = 0.1$  for semiconducting conductivity behavior, both at high magnetic fluxes [54]. The fitted  $B'$  values are three orders of magnitude lower than the ones calculated above. Consequently, the elastic scattering time should be reduced by six orders of magnitude. This is physically nonsense. Also, the  $C_n T^n$  term does not correspond to physically meaningful quantities. The values of the exponent  $n$  cannot be attributed to a certain electron scattering mechanism. On the other hand, electron scattering should sufficiently change in dependence on the magnetic flux. When assuming  $n = 2$  for electron-electron scattering, and taking the value  $C_n = 2.16 \times 10^{-11} \text{ WmK}^{-2}$  from [33], the fit becomes of much worse quality (Figure 4). Here, a satisfactory fit occurs only for  $B = 0$ . Assuming  $n = 2.5$  and taking the value  $C_n$  of eq. (20), the fit is even worse with a no satisfactory fit even for  $B = 0$ .

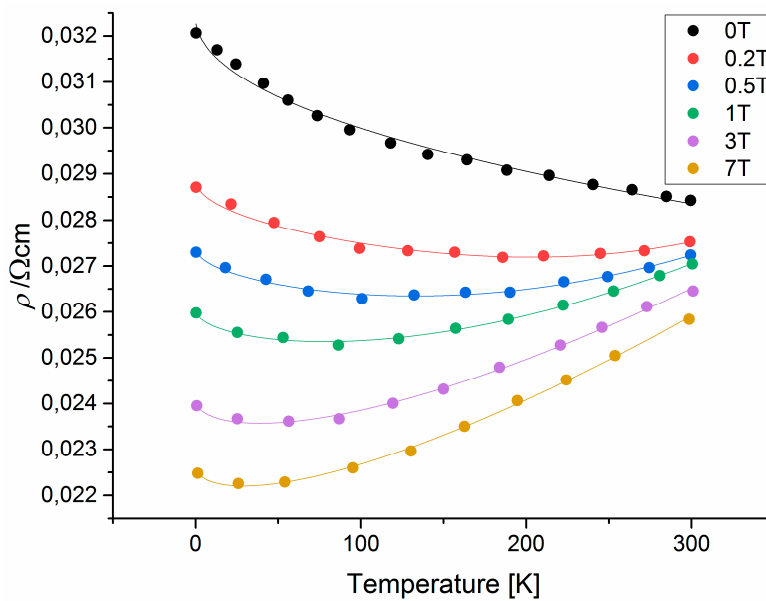
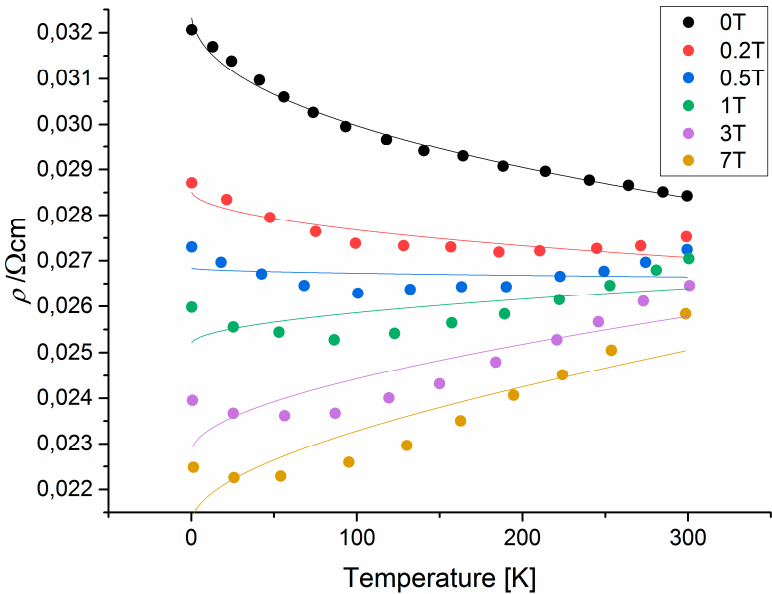


Figure 3. Fit of the conductivity data of  $\text{Sr}_2\text{FeMoO}_6$  [28] to eq. (15) assuming  $A' = 0$ .

**Table 1.** Fit of the parameters of eq. (15) assuming  $A'=0$  to experimental data in [28].

$B, T$	$s_0, \text{Sm}^{-1}$	$B', \text{Sm}^{-1}\text{K}^{-1/2}$	$C_n, \text{WmK}^{-n}$	$n$
0	3087	0.222	$-1.37 \times 10^{-5}$	0.61
0.2	3464	0.174	$6.09 \times 10^{-12}$	3.31
0.5	3649	0.161	$3.75 \times 10^{-9}$	2.29
1	3839	0.166	$1.15 \times 10^{-7}$	1.77
3	4150	0.235	$2.21 \times 10^{-6}$	1.34
7	4414	0.270	$3.73 \times 10^{-6}$	1.22



**Figure 4.** Fit of the conductivity data of  $\text{Sr}_2\text{FeMoO}_6$  [28] to eq. (15) assuming  $A' = 0$ ,  $C_n = 2.16 \times 10^{-11}$ ,  $n = 2$ .

Thus, the only possible conclusion is that the resistivity upturn at low temperatures in  $\text{Sr}_2\text{FeMoO}_6$  ceramics cannot be modeled by the weak localization correction due to quantum interference. Note that neither fluctuation induced tunneling nor adiabatic small polaron hopping provide favored conditions for quantum interference of back-scattered electrons.

4. Conclusions

We have related the temperature dependence of the SFMO resistivity in the absence of a magnetic field to the fluctuation induced tunneling model. The decrease in resistivity above the resistivity maximum around Curie temperature was attribute to adiabatic small polaron hopping instead to localization effects. Both fluctuation induced tunneling and adiabatic small polaron hopping do not favor quantum interference. This is evidenced by the observation that the resistivity upturn behavior of SFMO cannot be explained by weak localization. Consequently, to the best of our knowledge, there is still no convincing evidence for the presence of weak localization in SFMO.

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