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Posted Date: 8 May 2023

doi: [10.20944/preprints202305.0456.v1](https://doi.org/10.20944/preprints202305.0456.v1)

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Article

Hybrid Off-Grid Energy Systems Optimal Sizing with Integrated Hydrogen Storage Based on Deterministic Balance Approach

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Abstract: Integrating numerous renewable resources has been extensively researched and studied to create a dependable energy system. This study investigated the best techno-economical hybrid energy system configuration while using hydrogen energy to keep the system's energy balanced. Additionally, this study aims to determine the best hybrid system configuration for the location under investigation. A novel technique of DBM (Deterministic Balanced Method) was introduced to determine the total annual energy output for the project's lifetime. This approach is used to contrast the outcomes of other HOMER software tools. Then, using HOMER, it is possible to confirm the sizing optimization results for the suggested method by comparing the power ratings and yearly energy output. A detailed comparison between our proposed method and HOMER Pro has been conducted for validation and verification. Our method has been rigorously tested in various hybrid off-grid energy systems, ensuring its applicability and reliability across different scenarios and configurations. The results of our study indicate a high degree of similarity between the proposed approach and HOMER pro for computing annual energy power for the studied energy systems. Specifically, our analysis revealed that the difference between the approaches was within a range of 5%, indicating a high level of consistency and reliability in our method. These findings suggest that our approach can be confidently applied to determine the appropriate size of hybrid energy systems accurately. Overall, our study provides valuable insights into the development of effective sizing methodologies for hybrid energy systems. After considering the amount of solar radiation and wind speed gathered by global weather data platforms like NASA and METEONORM, this paper has also included a real case study of the Cairo International Airport's hybrid renewable energy production systems. To guarantee the viability of this study, the system design was founded on an actual load that was researched and simulated. A cluster of distributed networks was finally proposed to use the excess energy and enable energy conversion processes to be used in industry and transportation applications.

Keywords: energy systems; hybrid; off-grid; solar PV; wind turbines; hydrogen system; sizing optimization; deterministic approach

1. Introduction

Hybrid off-grid systems are always challenging to design and optimize their operation for the project lifetime. The use of hydrogen as an energy storage carrier has made the sizing problem of

energy systems become more complicated and need global optimal solutions for best technoeconomical solution. Additionally, adverse nature of the wind-PV system can compensate the intermittency nature of each of system and therefore improve the overall reliability of the hybrid system. Hybrid energy systems are increasingly being used to provide sustainable and reliable power in off-grid and remote areas. These systems typically consist of a combination of renewable energy sources, such as solar and wind, and energy storage systems, such as batteries or hydrogen storage. While batteries have been widely used in hybrid energy systems, there is a growing interest in using hydrogen storage as a potential alternative due to its high energy density and the ability to produce hydrogen using renewable energy sources. A research conducted in (Gelma et al., 2011) described the design information of solar PV and wind turbine hybrid power generation systems to provide electricity to a model community of 100 households and health clinic and elementary school. The optimal simulation results in this study showed that PV/wind turbine/diesel generator/battery and converter is the best-configured system for their application with a renewable fraction of 84%. There are many research papers that had introduced different system configurations and comparative analysis for deciding the most economical feasible one. One of those researches was (Ghenai et al., 2015) which presented a case study in the desert region of United Arab of Emirates. It introduces a technical-economic analysis based on integrated modeling, simulation, and optimization approach to design an off-grid hybrid solar PV/Fuel Cell power system. This system is designed to meet the energy demand of 4500 kWh/day of the residential community (150 houses). The total power production from the distributed hybrid energy system was 52% from the solar PV, and 48% from the fuel cell with a 40.2 % renewable fraction which is a low value for renewable energy penetration of this system. Consequently, one of the main concerns of the paper research is how to achieve a renewable fraction of 100% in the simulated configurations of various hybrid off-grid systems. These given numbers of renewable fraction used to give a rough estimate for the previous research works that focused on the renewable resources' penetration (increasing the renewable fraction percentage) and select the best configuration for the application targets.

Another approach for choosing the best size and location for off-grid hybrid systems was presented by (Cai et al., 2020). To discover the ideal capacity and location for continually meeting the load while reducing levelized cost of energy and overall life cycle cost, they considered economic, technical, social, and environmental factors. The hybrid algorithm based on geographic information system, simulated annealing, and enhanced harmony search is evaluated with real data for a genuine case study in South Khorasan, Iran, and the findings show that it provides more accurate results than those from previous heuristic approaches. As comparison to a standalone diesel system, the hybrid system saves 8948 L of diesel generator fuel and reduces pollutant emissions by 59.6% according to the IHS SA-GIS methodology (Cai et al., 2020). (Alberizzi et al., 2020) present a methodology based on Mixed Integer Linear Programming (MILP) and an algorithm implemented through Matlab software to determine the ideal size of a hybrid solar-wind system with battery storage to replace a diesel-fueled internal combustion engine (ICE) for a mountain lodge in South Tyrol, Italy.

(Mahmoudi et al., 2023) evaluates different combinations of photovoltaic panels and wind turbines with a backup system using a reliability-based analysis. The goal is to compare the sizing of three hybrid energy systems, namely PV/DG, Wind/DG, and PV/Wind/DG, under three scenarios: reducing carbon dioxide emissions, reducing total annual costs, and reducing both simultaneously. The proposed method uses the gravitational search algorithm and compares results with the simulated annealing method. The study examines 45 cases and includes economic and environmental analysis, as well as an examination of the damage caused by carbon dioxide emissions to human health. The results indicate that the optimal system is PV/Wind/DG, which reduces pollution by 27.2% and saves up to 4.76% of costs compared to a PV/DG system. By imposing carbon taxes on hybrid system designs, it is possible to prevent about 9% of CO₂ emissions and reduce damage to human health by 8.9%.

(Özçelep et al., 2023) analyzed the electrical energy required for the heating system with a heat pump from a solar photovoltaic-hydrogen system and found that the 24 m² solar panel area and 0.08 m³ of hydrogen stored in 16 hydrogen cylinders is adequate for meeting energy demand. Using a

solar-hydrogen-heat pump system reduces carbon emissions by 86.5 tons per 1000 m² floor area greenhouse.

(Azad and Shateri, 2023) developed an approach to optimize power planning for an entirely renewable hybrid system that includes wind turbines, PV systems, bio-waste units, thermal energy storage, electric vehicle parking lots, and smart charging strategies. They have used a modified multi-objective function to minimize TANPC and LCOE and a modified cost model to increase modeling accuracy. Their results show that including bio-waste units can increase system efficiency and reduce greenhouse gas emissions, while implementing adaptive smart charging for electric vehicles can decrease LCOE and TANPC by load leveling and reducing the required storage capacity. They also considered uncertainties in renewable resources, loads, and electric vehicles' parameters to improve modeling accuracy. However, considering uncertainty leads to more resources and storage devices, which increases the system cost. They have used a modified combination of GWO and SCA to optimize the system, and their results show that their algorithm obtains the optimal solution with higher convergence speed and lower standard deviation compared to SEAs. Furthermore, this paper reviews the recent advancements in these methodologies, focusing on research published in the last few years in Table 1 and we classified their solution complexity by color bar and its popularity by sector area in Figure 1. Also, we used an evaluation metric named "common usage" that shows the most abundant combination of hybrid energy systems and their rank as shown in Figure 2.

Table 1. Recent optimization research on HRES-H₂ systems.

Hybrid system	Method	Discussion	Authors/year
PV-WTG - battery - H ₂ storage	Mixed-integer-linear programming	The cogeneration model was created to regulate the energy repository system's two-way energy flow. The model can significantly reduce the cost of producing hydrogen overall, especially when the load profile is high.	(Zhang et al., 2020)
WTG - PV- geothermal - H ₂ storage - battery	Bi-level mixed-integer	A model addressing the leveled cost of hydrogen was introduced in order to lower the cost of hydrogen generation. To address problems with system performance and dependability, the model includes a variety of continuous and discrete factors.	(Pan et al., 2020)
Wind- PV – battery- H ₂ storage	Particle swarm optimization	The -constraint method minimizes the COE while constraining loss of power supply probability and non-renewable usage. Simulation and optimization use particle swarm optimization and HOMER software	(Mokhtara et al., 2021)

PV battery- H ₂ storage	- Iterative method	Based on empirical data on electric power load, solar irradiation, and ambient temperature, the modeling process of the solar hydrogen energy system was examined using MATLAB. The cost of electricity was leveled by \$0.195/kWh due to energy distribution, which is a financial consideration.	(Hassan, 2020)
PV battery- H ₂ storage	- Particle swarm optimization, genetic algorithm	Systems operating in P-PMS mode outperformed R-PMS in terms of cost, renewable integration, and environmental impact. The efficiency of the chosen algorithms was found to be a significant determinant of P-PMS, though. P-PMS might greatly lessen how FC and ELZ instantaneous responses affect the size and operation of the energy system.	(Brka et al., 2016)
WTG - PV - H ₂ storage -battery	Multi-objective- genetic algorithm	Using multi-objective optimization, a trigeneration system that produces ammonia, hydrogen, and electricity was examined. The measured range of the exergy efficiency was 10.9% to 38.2%, depending on the size of the meteorological data.	(Siddiqui and Dincer, 2021)
WTG- PV – battery- H ₂ storage	Flower pollination algorithm	Renewable energy generation and hydrogen energy storage have an inverse relationship to the system's dependability restrictions. In some Iranian places, it was found that PV panels were more cost-effective than wind turbines. Moreover, wind turbines may be used as a reserve energy source to fulfill peak load requirements.	(Hadidian Moghaddam et al., 2019)
WTG- PV – battery- H ₂ storage	Improved salp swarm optimization algorithm (ISSOA)	Dimensions of Hydrogen Tank and Battery storage In comparison to PV/WT with a battery storage system, H ₂ was shown to have a larger Cost of energy generation, while the latter exhibits superior system dependability. In terms of designing a hybrid system, ISSOA performed better than SSOA and PSO.	(Vahid et al., 2020)

WTG- PV – H ₂ storage	Hybrid wolf sine cosine algorithm	grey	When LSCS and LIP were taken into account, PV/WTG/FC was shown to be the best configuration to meet the load requirement. H ₂ was essential in reducing RE fluctuation, which helped the system achieve the highest level of dependability. The fuel cell's efficiency was shown to be inversely related to stored H ₂ and LSCS, while directly related	(Jahannoosh et al., 2021)
WTG- PV – H ₂ storage	HOMER		The purpose of the study was to verify the effect of various storage technologies on HES. Minimum NPC and COE were supplied by the VRX battery system. The system made up of FC and H ₂ showed the fewest changes. By employing the load tracking control, it was discovered that the minimal SOC considering net cost fluctuated more than when using the load cycle control.	(Arévalo et al., 2020)

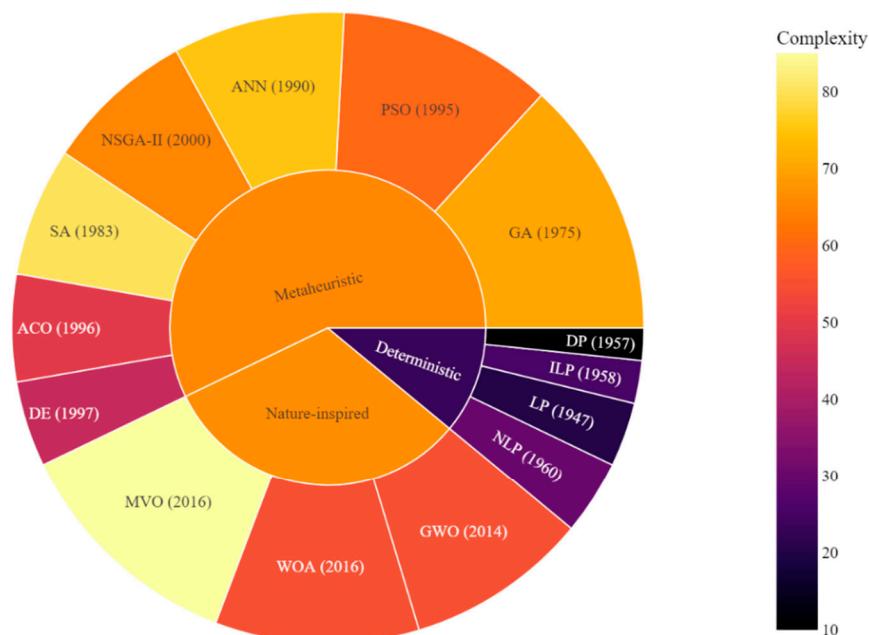


Figure 1. Methods used for solving the sizing optimization of energy systems. Source: Self painted by the author

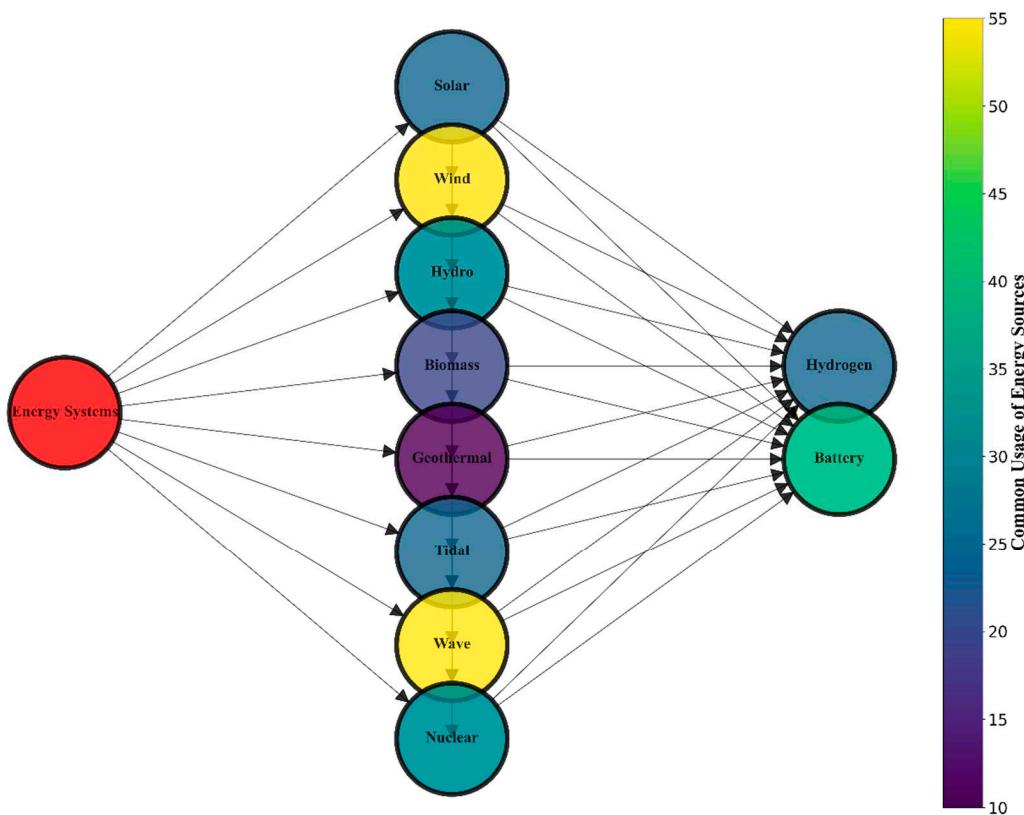


Figure 2. Common usage metric for energy resources and storages.

Sizing hybrid energy systems with hydrogen storage presents a unique set of challenges. Unlike batteries, hydrogen storage systems are more complex and require careful consideration of factors such as the size and type of the storage tank, the electrolyzer and fuel cell efficiency, and the overall system balance. Moreover, the intermittent nature of renewable energy sources such as wind and solar can further complicate the sizing of hybrid systems with hydrogen storage. A critical aspect of designing these systems is determining the optimal sizing of each component, which has prompted the development of various sizing methodologies. Starting from iterative methods are characterized by their trial-and-error approach to determining the optimal sizing of hybrid off-grid systems. Although intuitive and straightforward, these methods can be computationally intensive and may not guarantee the global optimum.

Optimization-based methods, including linear programming (LP), mixed-integer linear programming (MILP), and multi-objective optimization, employ mathematical algorithms to optimize the sizing of hybrid off-grid systems by minimizing cost, maximizing efficiency, or addressing multiple objectives simultaneously (Ben Seddik et al., 2022). These methods are effective in finding the global optimum but often require extensive computation and may be limited by the complexity of the mathematical models (Adedoja et al., 2023).

Simulation-based methods, such as Monte Carlo simulations, artificial neural networks (ANN), and machine learning algorithms, use statistical models to simulate the performance of hybrid off-grid systems under varying conditions and determine the optimal sizing accordingly (Al-Othman et al., 2022). These methods are advantageous in accounting for uncertainties and variability in input data, such as weather and load profiles, but may require significant computational resources and training data.

Based on the limitations discussed above, several research gaps can be identified:

- Development of more efficient algorithms: There is a need to develop more efficient algorithms that can reduce the computational burden of iterative and optimization-based methods while still ensuring the global optimum solution.

- Adaptive sizing methodologies: As hybrid off-grid energy systems evolve over time due to factors such as changing load demands and component degradation, there is a need for adaptive sizing methodologies that can account for these changes and optimize system performance throughout its lifecycle.
- Scalability and applicability: As the demand for hybrid off-grid energy systems grows, there is a need to develop sizing methodologies that can be applied to various scales, from small residential systems to large-scale microgrids. Research should focus on developing scalable algorithms and techniques that can handle the increasing complexity and size of these systems.
- Incorporation of new technologies and energy sources: The rapid development of renewable energy technologies and energy storage solutions, such as advanced battery systems and hydrogen storage, necessitates the integration of these new technologies into existing sizing methodologies. Future research should explore how these emerging technologies can be effectively incorporated into the sizing process to enhance the performance of hybrid off-grid energy systems.
- Standardization and benchmarking: There is a lack of standardization and benchmarking in the field of sizing methodologies for hybrid off-grid energy systems. Developing standardized benchmarks and performance metrics can facilitate the comparison and evaluation of different sizing approaches, driving further improvements and innovation in the field.

By addressing these research gaps, the field of sizing methodologies for hybrid off-grid energy systems can continue to advance, leading to more efficient, reliable, and cost-effective systems. The development of novel algorithms, improved modeling techniques, and the incorporation of deterministic approaches will not only enhance the performance of these methodologies but also contribute to the broader adoption of sustainable energy solutions in remote and off-grid areas. Deterministic methods for sizing hybrid off-grid energy systems rely on fixed input parameters and deterministic mathematical models to determine the optimal sizing of system components. These methods have several advantages:

- Simplicity: Deterministic methods often involve simpler mathematical models and algorithms compared to stochastic or simulation-based approaches, making them easier to implement, understand, and interpret.
- Computational efficiency: Due to their simplicity, deterministic methods generally require less computational resources and time compared to other approaches, such as stochastic or simulation-based methods.
- Reproducibility: Deterministic methods, by their nature, provide consistent results for the same input data, ensuring reproducibility and comparability across different applications and scenarios.
- Ease of integration: Deterministic methods can be more easily integrated into other optimization or decision-making frameworks, such as linear programming, mixed-integer linear programming, and multi-objective optimization algorithms.
- Lower uncertainty: By relying on fixed input parameters, deterministic methods eliminate the uncertainty associated with variable input data, such as weather conditions and load profiles, leading to more predictable and consistent results.

From this literature analysis, we come up with a conclusion that the proposed system in this work must follow certain techno-economical outlines that is mandatory to design an energy hub for electricity and fuel production. This system is considered to achieve a 100% renewable fraction with different system configurations as shown in figure below:

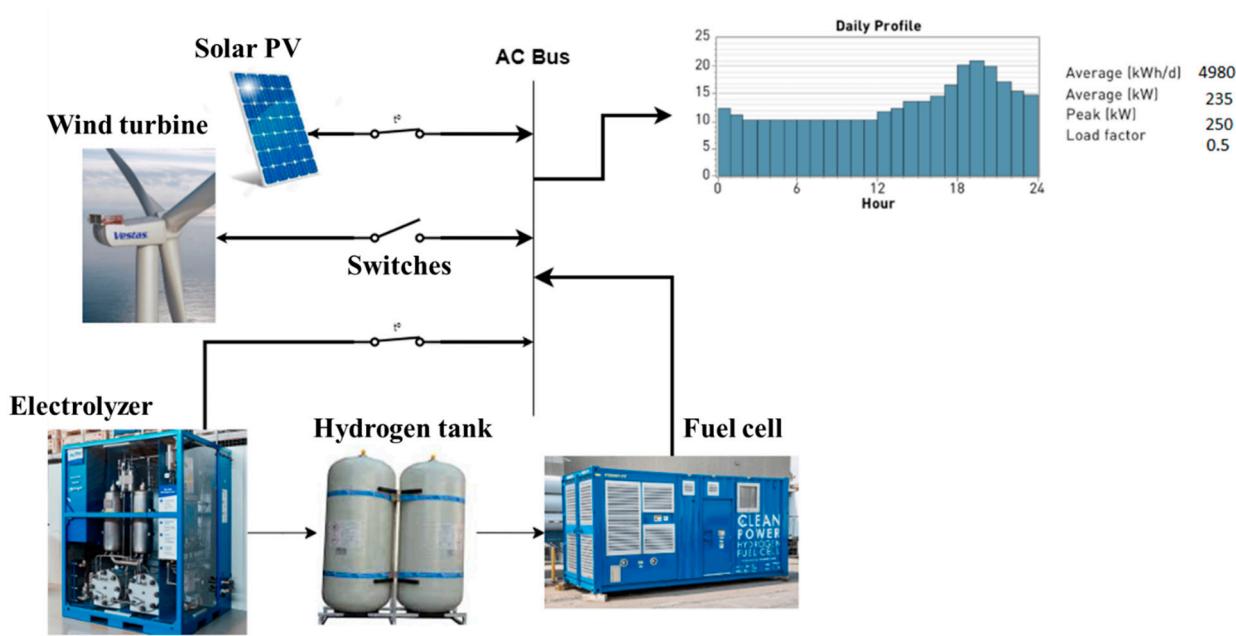


Figure 3. Conceptual model for energy system based on hydrogen storage.

The primary objective of this endeavor is to develop a comprehensive model of an off-grid system composed of photovoltaic generators, wind turbines, fuel cells, electrolyzers, and hydrogen storage tanks. The meteorological data of Cairo International Airport as one of the data input files for the system model and the RTS load model as the current load profile for the design were both emphasized. Using the Deterministic Balance Method (DBM) for calculating the annual energy production for the system and then reflecting it on the load demand to ensure a balanced mode of generation, the system's sizing methodology is utilized to determine the system's design limitations. This method was then used to achieve the optimal dimensions of each system component. The hourly electricity and hydrogen balance must be satisfied by either converting excess electricity into hydrogen or storing hydrogen into electricity. The hourly simulation is performed for an entire year to size the system components so that there is no electricity curtailment. Another objective of the design of this energy system was to consider the optimal utilization of excess energy in relevant industrial and transportation domains. This strategy has paved the way for distributed energy networks to be designed and regulated for sharing available energy based on demand analysis and forecasting.

The main contributions of this work can be summarized as follows:

- A novel method named Deterministic Energy Balance Method (DBM) is proposed to find the optimal sizing of hybrid renewable energy sources (RESs). This method is based on energy balance computation for system's yearly profiles to avoid using any heuristic algorithms that are based on trial and error to find the global optima for system parameters and cost function.
- Cost analysis model is computed for all studied systems for one-year simulation based on DBM method to come up with a techno-economical solution for fair comparison with commercial software.
- 100% renewable energy system is introduced within different system setups and they are optimally sized using the DBM to achieve high reliability of energy supply. Additionally, seasonal variations' impact on energy generation is utilized to manage the hydrogen production process for supplying the surplus energy in times of lack of generation.
- Verification and validation of the proposed method are achieved by using HOMER to judge the Levelized cost of energy for different system configurations and justify the power ratings of installed components for different setups.

2. Modeling of the Hybrid Energy System

2.1. Solar Photovoltaic

The main objective functions were used to get the output power of the PV modules taking into consideration the efficiency of the modules and other derating factors. The first equation used in PV modeling is an output power function of Irradiance (Elshimy et al., 2015)

$$P_{pv} = Y_{pv} f_{pv} \left(\frac{G_T(t)}{G_{T,STC}} \right) \quad (1)$$

Other factors that had been encountered during the literature view. Temperature and wind speed had significantly affected the model to get more accurate results that are feasible for execution. Consequently, another objective function for calculating the output power was then evolved providing a relation between the irradiance and temperature to deliver the actual output power shown in equation (Skoplaki et al., 2009)

$$p = \eta T_{ref} A G_T [1 - 0.0045(T_c - 298.15)] \quad (2)$$

After studying the behavior of temperature and irradiance throughout the meteorological model, the effect of this behavior was linked to the changes in each of the two parameters and the overall efficiency of the PV system (Skoplaki et al., 2009). This relation was supported by the following equation:

$$\eta = \eta_{Tref} [1 - B_{ref} (T_{c,i} - T_{ref})] \quad (3)$$

2.2. Wind Turbine Generators (WTGs)

1. The Wind Turbine Generator (WTG) hourly power output, at the studied location, depends on the hourly wind speed as shown in Figure 4. It can be expressed by following equations (Khiareddine et al., 2018):

$$P_{wind}(V_V) = \begin{cases} P_r(A + BV_V + CV_V^2), & V_D \leq V_V \leq V_N \\ P_r, & V_N \leq V_V \leq V_R \\ 0 & Elsewhere \end{cases} \quad (4)$$

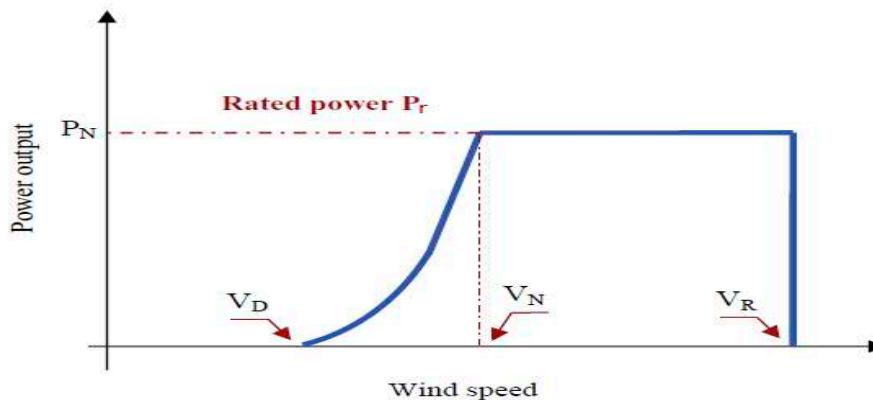


Figure 4. Power output curve of wind (Khiareddine et al., 2018).

2.3. Hydrogen System

Fuel cell can be defined as an electrochemical device that produces electrical power directly from a fuel like hydrogen, natural gas, diesel and propane. Its operation is similar to that of a conventional battery except in some parts that will be discussed in detail later in this paper and will affect the modeling of the hybrid off-grid system. Accordingly, their development has been much related to development of electrochemistry more than the power engineering and it is already studied as a distinct branch of physical chemistry (Larminie et al., 2003).

The second element in the hydrogen system is the electrolyzer, which is an electrochemical device that makes an electrolysis for the water molecules to produce hydrogen and oxygen. This

process is powered by the excess electrically in the system. In other words, electrolyzer is used to convert the unused electrical energy into stored chemical energy inside hydrogen and then recall it back in the time of operation. The mathematical formula of the produced hydrogen from the electrolyzer can be expressed as follows (Fathy et al., 2016).

Energy required to produce one kilogram of hydrogen

$$= \eta_{Elz} X \frac{H_2 \text{ Heating Value}}{H_2 \text{ density}} \quad (5)$$

2.4. Load Profile System

In this study, it is assumed that the DC and AC wiring losses are small enough to be neglected, due to the small geographic scatter of the study system. The Reliability Test System (RTS) load profile is used in this study (IEE Standards et al., 1979) as shown in Figure 5 and the peak load is set to 250 kW. The load profile is then determined per hour for the 8760 hours of a year and illustrated in the appendix.

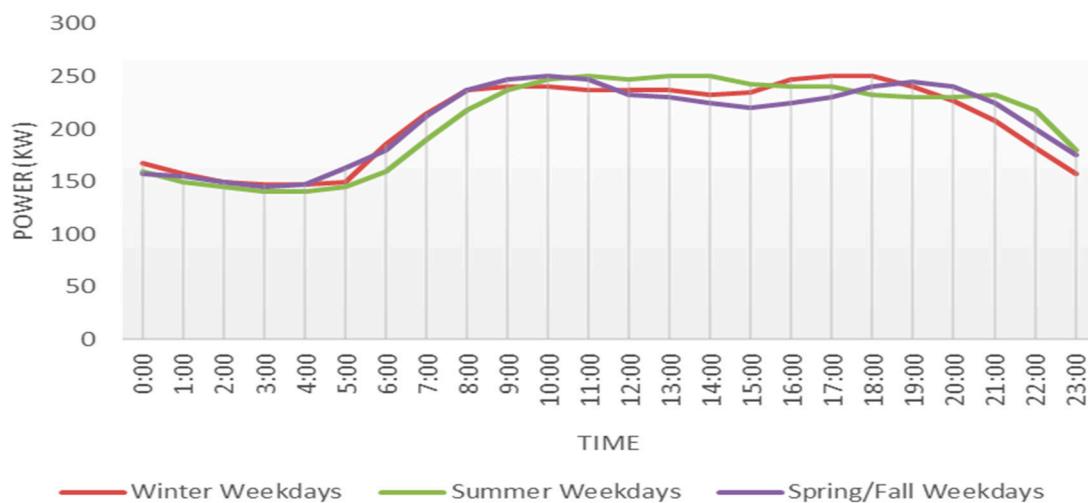


Figure 5. Load profile system based on RTS system.

2.5. Economic Investigation for the Studied System

The economic study is what determines the feasibility of the hybrid renewable system. It reflects the whole image for the policy maker and decision makers to invest and work on these types of projects. The levelized cost of energy (LCOE), capital cost and cash flow study are what encourages the investor to direct the fund and grants to establish hybrid renewable system for remote areas. To start with, some definitions must be firstly explained to enable the researchers and engineers to apply optimizations techniques which satisfies the load demand with the minimum cost of energy. **Levelized Cost of Energy** is the annualized cost of producing electricity by the total electric load served for the entire life lime of the project. **Net present cost** is the present value of all the costs of installing and operating the system over the project lifetime. This analysis is performed using the cash flow table where it shows the operation & maintenance costs, salvage costs, replacement costs and fuel cost (if exists). Another factor which is added to the table to be multiplied by the costs discussed is the Discount factor. **Discount factor** is a direct reflection of the time value of money after a certain period. Additionally, there is a significant difference between the discount factor and the inflation rate. A factor named the real discount factor appears which compensates the effect of inflation analysis and represent the costs in year-zero dollars (HOMER et al., 2022)

Annualized cost is the cost that, if the investor pays every year would resemble the same net present cost at the end of the project when using the yearly cash flow sequence shown

Capital Recovery Factor (CRF) is a factor that converts the total net present cost into a total annualized cost. It depends on the inflation rate of the country and the lifetime of the project.

After defining the previous definitions, the cost objective function was elaborated where well-known optimization techniques could be applied in minimizing the function and obtaining the optimum configuration resulting in the least total annualized cost.

To optimally design the hybrid generation system, the optimization problem, defined by Equation (9) as in (HOMER et al., 2022), must be solved using any of the mentioned optimization techniques in the paper.

$$C_{cpt} = [N_{pv} X C_{PV} + N_{Tank} X C_{Tank} + C_{FC/ELZ} + N_{conv} X C_{conv}] \quad (6)$$

Where C_{PV} is unit cost of PV panel, N_{tank} is the number of storage tanks, C_{Tank} is unit cost of hydrogen storage tank and $N_{Conv/Invis}$ is the number of converter/inverter systems.

$$C_{Mtn} = \frac{(i + 1)^n - 1}{i(1 + i)^n} (N_{PV} X C_{PV,Mtn} + C_{FC,Mtn} + C_{Elz,Mtn}) \quad (7)$$

Where $C_{PV,Mtn}$, $C_{FC,Mtn}$ and $C_{Elz,Mtn}$ are the annual maintenance costs of PV, fuel cell and electrolyzer systems, respectively.

To minimize the total cost function,

$$C_T = C_{cpt} + C_{Mtn} \quad (8)$$

The economic model of the studied system was studied for the lifetime of the system using the following equations [33]

$$O\&M\ costs(\$/year) = AEP * O\&M\ costs \quad (9)$$

$$AR = AEP * ESP \quad ANI = AR - O\&M\ costs(\$/year) \quad (10)$$

$$NPV = \sum_{k=1}^{n=20} \frac{ANI}{(1+R)} - CI \quad (11)$$

$$PVM = \sum_{k=1}^{n=20} \frac{NPV}{(1+R)} - CI \quad (12)$$

$$PV^* = FV \frac{1}{(1 + R)^P} \quad (13)$$

$$AC = \frac{-PVC * R}{(1 - (1 + R)^{-P})} \quad (14)$$

$$PVC = PVDC + PVM + CI \quad (15)$$

$$LCOE = \frac{LAC}{AEP} \quad (16)$$

3. Methodology: Deterministic Balance Method (DBM)

The deterministic Balance Method (DBM) application required determining PV output power, fuel cell size and efficiency, and hydrogen tank efficiency models. The accuracy of the PV model is crucial since it will be used to guide the overall layout of the system. To use the DBM, it is necessary to balance the energy needed to offset the time of zero PV output hour (usually at night) with the energy produced net by the PV (during sun hours after being absorbed through the load). Hydrogen tanks will store this surplus energy until needed; at this point, Fuel Cells will convert it to meet the day's energy needs. Power generated by PV and required by the load through Fuel Cells was determined using the area under graphs, as illustrated in Figure 6, which are computed using the Trapezium Rule. A discrete optimization was performed to find out how many PV modules would be ideal for striking this equilibrium.

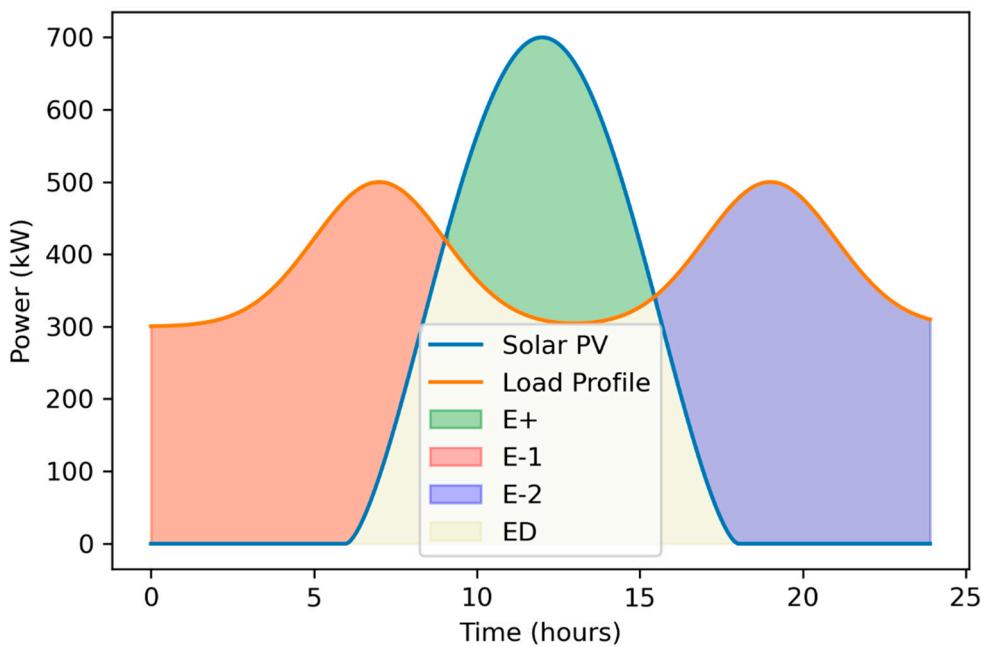


Figure 6. Area under curve for DBM.

In the first stage of the DBM design process, it was estimated that N solar PV modules would be sufficient to meet the required load and provide excess power at the end of the day. To begin computing energy Production values, this was founded on a random guess. This initial estimate was based on the energy balance equation discussed in the prior work [Selim et al., 2020] and was performed to estimate the surplus power supplied by PV to completely compensate the time of zero PV output power.

Using the data from NASA and METEONORM [34,35], the output PV power was calculated using equations (1,2) based on the irradiance profile of a specific day. Throughout the entirety of the model, the method of calculating energy production by obtaining the area under curves was the primary method employed. Numerous methods for calculating the area under curves, including the trapezium rule and the integration of curve functions in MATLAB. This model used the trapezium rule to calculate the area under curves in a 1 hour time step because it was challenging to obtain the function of each curve so that it could be integrated. In addition, the accuracy of the trapezium rule was deemed acceptable with minimal error ranges. As shown in Figure 6, Area under curve was calculated for the E^+ E^- and E^D

$$E^{-1} = \int (P_l - P_{pv}) dt, \text{ for } t_{s,1} < t < t_{e,1}, \text{ where } P_{pv} < P_l \quad (17)$$

$$E^{-2} = \int (P_l - P_{pv}) dt, \text{ for } t_{s,2} < t < t_{e,2}, \text{ where } P_{pv} < P_l \quad (18)$$

$$E^+ = \int (P_{pv} - P_l) dt, \text{ for } t_{s,+} < t < t_{e,+}, \text{ where } P_l < P_{pv} \quad (19)$$

$$E^D = \int P_l dt, \text{ for } 0 < t < t_e, \text{ where } P_l < P_{pv} \quad (20)$$

E^+ has to equal or greater than E^- to ensure the energy balanced operation

Our target is to find the optimal sizing of N_{PV} as follows:

$$N_{PV} = \frac{E^+ + E_D}{E_{1,PV}} \quad (21)$$

Figure 7 depicts the computation of the optimal number of solar PVs. For equation (21), we used to iteratively compute the number of solar photovoltaics (PVs) given the energy provided by each PV module (E_1). This calculation is based on the premise that these are the maximum values required by the load during nighttime hours to obtain the optimal surplus of PV power capable of covering the load (considering the fuel cell's and hydrogen tank's efficiencies). It was also observed that the

surplus energy the solar PV modules supplied must exceed the nighttime discharge power by a certain amount. This value primarily depends on the efficiency of the fuel cell, electrolyzer, and hydrogen tank. Consequently, system components with a higher efficiency yield a superior sizing optimization result. Equation (22) describes the effect of system component efficiencies on the surplus energy supplied and is a constraint for the optimization strategy.

$$E^- = E^+ \cdot \eta_{FC} \cdot \eta_{H2,Tank} \quad (22)$$

$E_{D,1}, E_{D,2}$ resemble the Energy the load consumes via PV modules during the first hours between sunset and sunrise. In previous calculations, these two values should have been taken into account. Nevertheless, it is essential to analyze them, as they will account for the losses that occur during the conversion process via hydrogen tanks and fuel cells. Numerous factors prohibit solar PV arrays from operating at maximum efficiency. In addition to voltage drop and dust accumulation, one of these factors is the operating temperature of the PV module, which can contribute considerably to the most significant proportion of power loss. The effect of temperature on output varies by module and can be calculated using the temperature coefficients supplied on the manufacturer's data sheets and the following relationships:

$$T_m = 20.4 + 1.2 \times T_a \quad (23)$$

$$T_x = 1 + \alpha(T_m - T_a) \quad (24)$$

In this model, it was assumed that AC losses are fixed at roughly 7% while array temperature losses range between 5% and 11% depending on the monthly temperature profile. We used the optimal N_{PV} to calculate the cost analysis indicated in section 2.5.

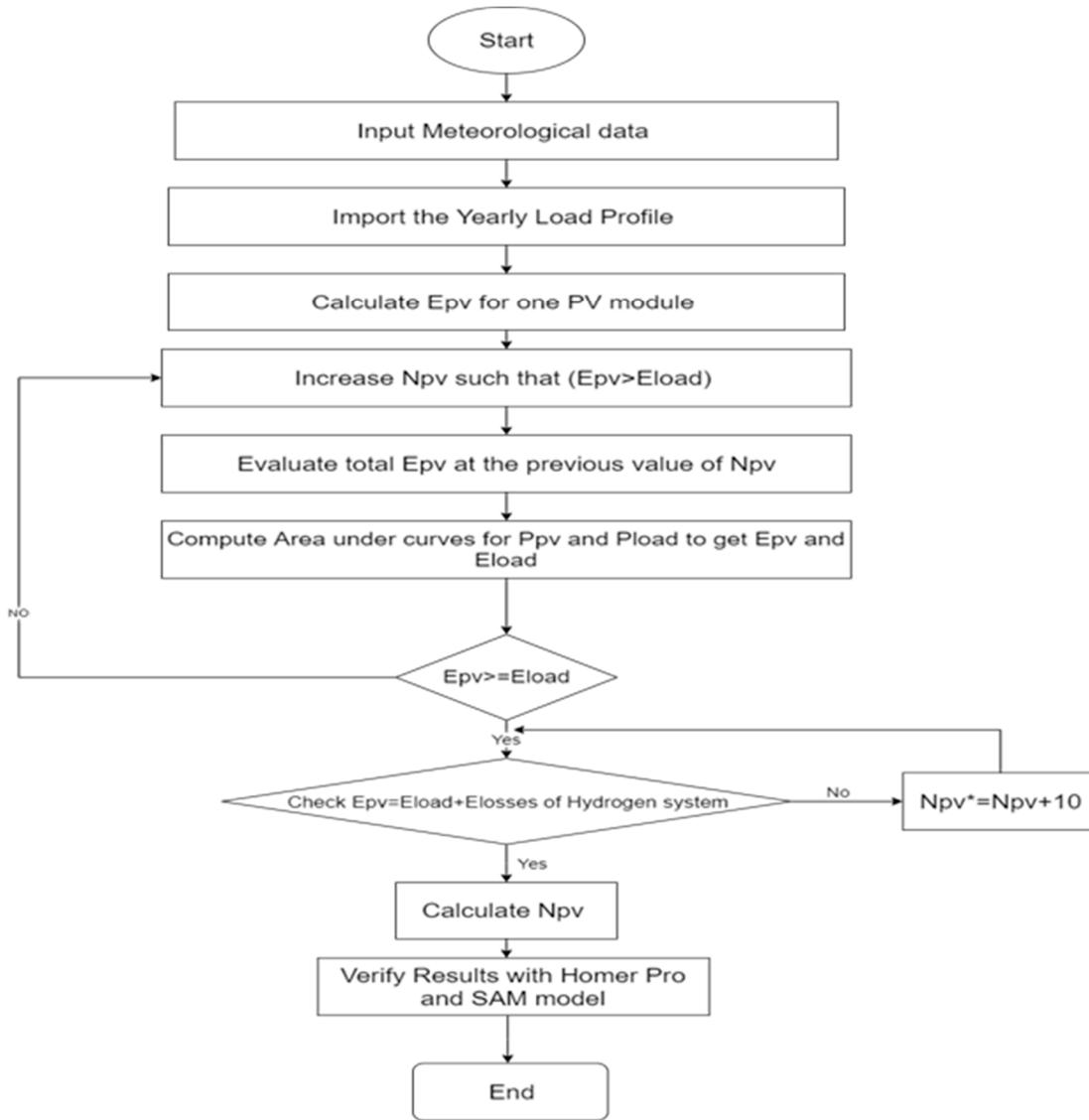


Figure 7. Flow chart of the DBM method.

4. Results and Discussion

4.1.a. Sizing Methodology of Hybrid PV/Hydrogen System: Case Study 1

In analyzing the annual system behavior for the examined location of Cairo International Airport, the production and energy consumption were investigated (same data as Selim et al., 2020). From October to March, hydrogen consumption exceeds production, and solar energy is the sole source of hydrogen production. During April through September, solar energy increases due to increased irradiance and moderate temperature ranges, causing hydrogen production to exceed consumption. The entire year's worth of excess solar electricity is stored in a hydrogen tank, yielding approximately 2,000 kg of hydrogen that will be exported to the grid upon application of the power management method during January and December, when there is no surplus power and end consumers consume all produced energy.

As shown in Figure 8, the net energy produced by PV modules is sufficient to cover the load demand for each month except for December which considered as the worst-case scenario. The PV contribution in that energy mix is found to be 50% or exceeding depending on the month of the year and this what proves the capability of the deterministic balance method for optimizing the generation and meeting the load requirement. In December, there was a lack of generation around 5% which are

supplied by the stored hydrogen from the excess of the previous months. Finally, energy profiles for solar PVs, fuel cell, electrolyzer and hydrogen production were deduced for 8760 hours as shown in Figures (9-a,b,c,d,e).

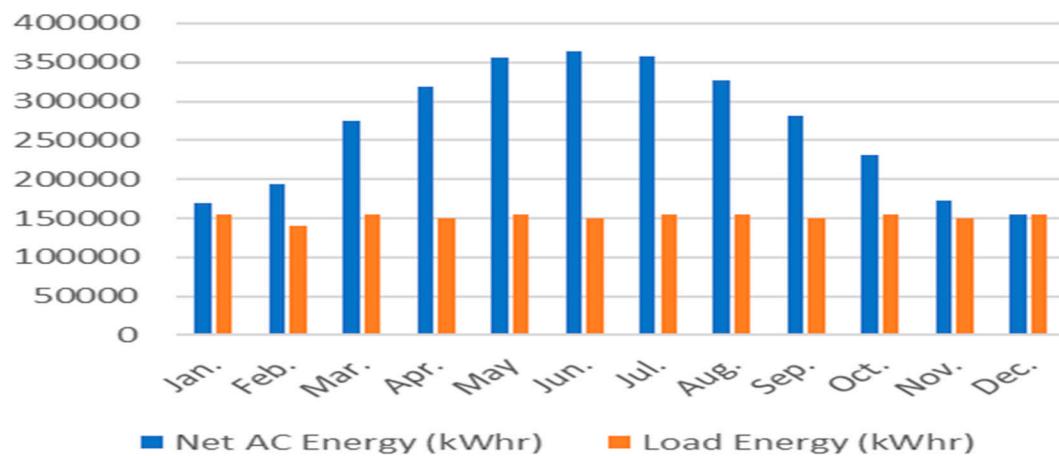


Figure 8. Net AC energy compared with load energy using DBM.

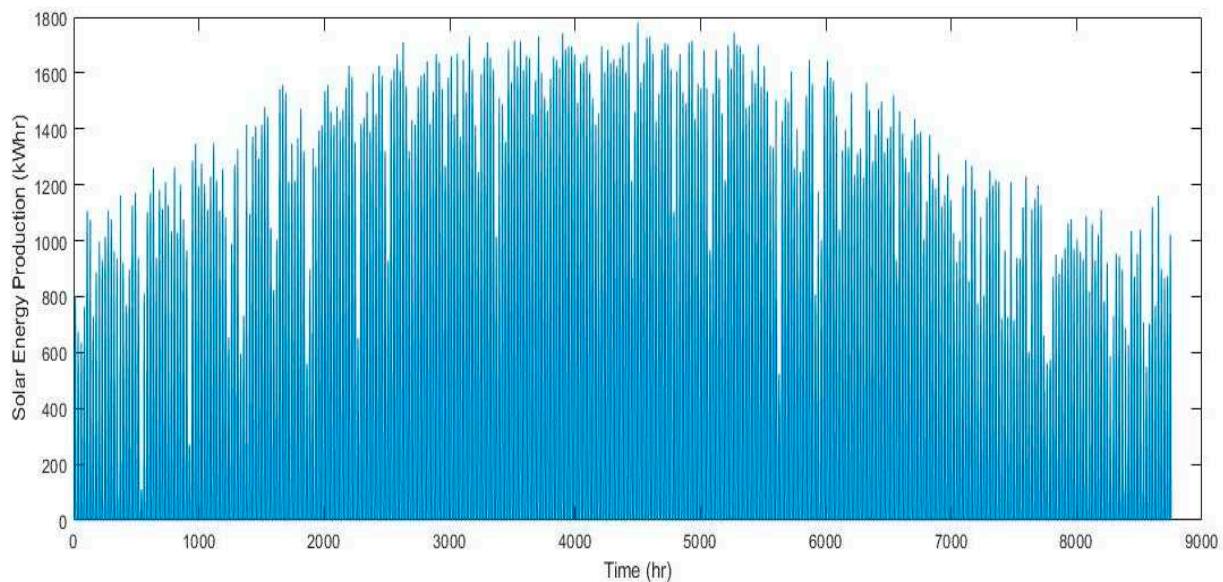


Figure 9. a. Solar PV Energy Available using DBM.

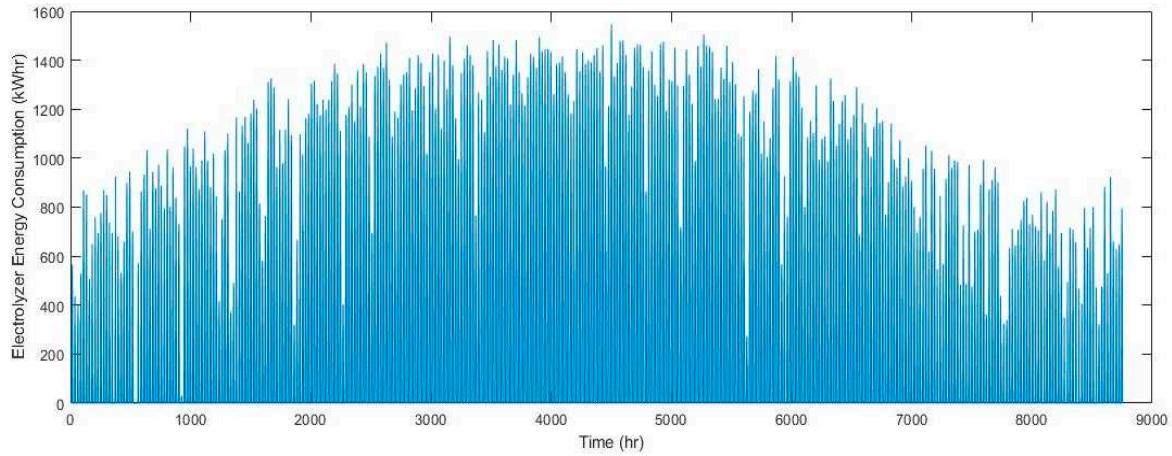


Figure 9. b. Electrolyzer Energy Available using DBM.

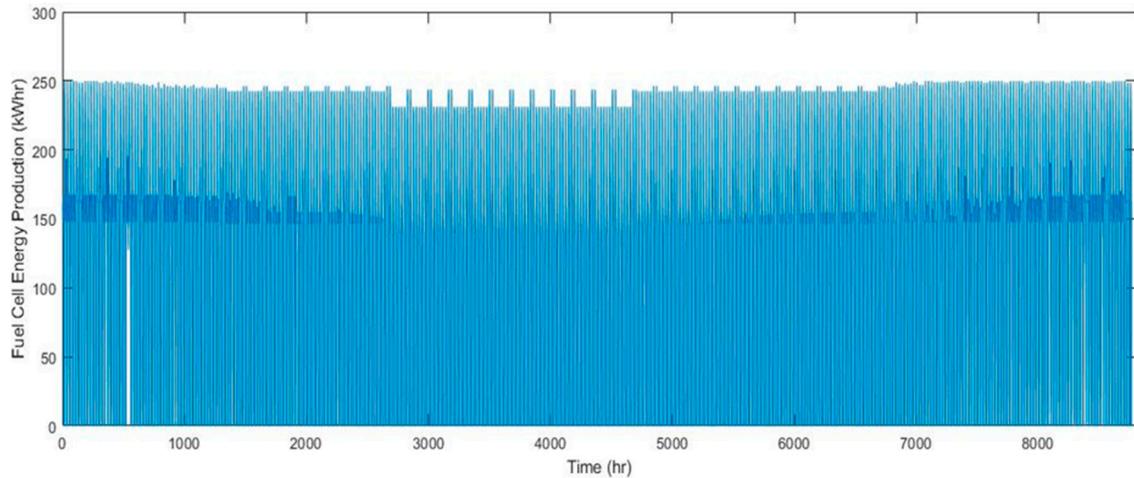


Figure 9. c. Fuel Cell Energy Production using DBM.

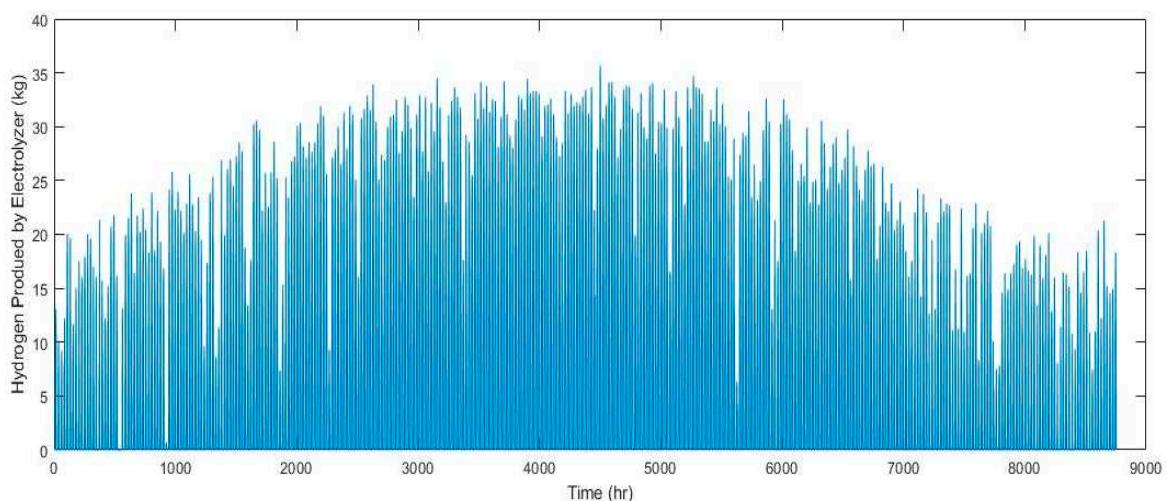


Figure 9. d. Electrolyzer Energy Production using DBM.

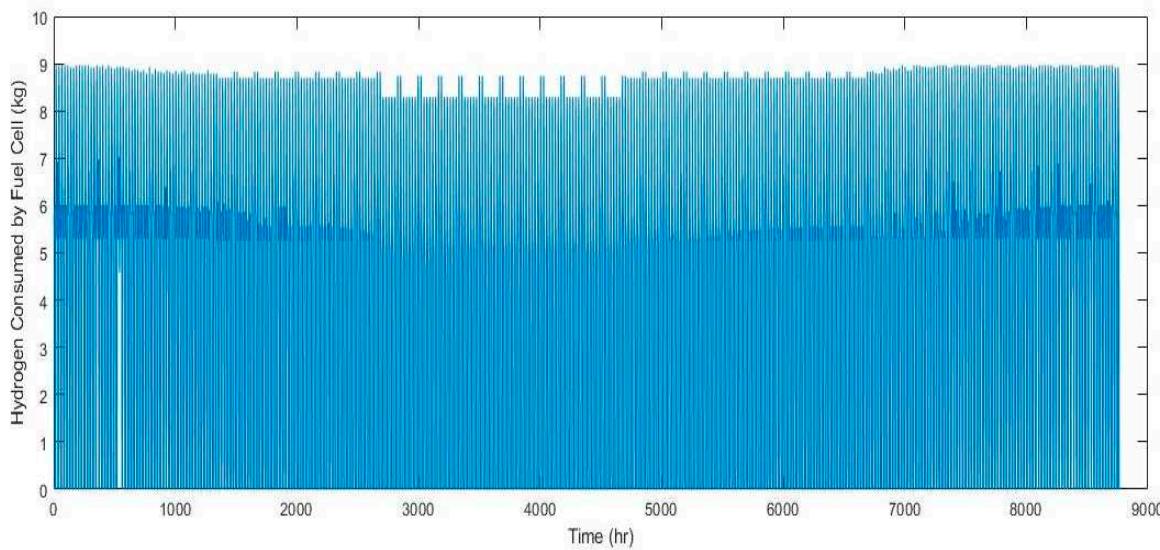


Figure 9. e. Hydrogen Consumption using Fuel Cell.

Referring to cost equations in paper and System cost per 1 kW as illustrated in Table 2, the economic model of the hybrid system will be evaluated as shown in Table 2 and Figure 10.

Consider Electrical selling price (ESP) =0.0788 \$/kWhr (NREA et al.,2020), Project lifetime =25 years, Annual discount rate = 10% and assuming no decommissioning cost paid.

Table 2. Cost analysis of the hybrid PV/hydrogen System.

Month	Solar PV	Fuel Cell	Electrolyzer	Hydrogen Tank
Capital Cost (\$)	1,793,000	750,000	960,000	2000
Maintenance Cost (\$)	-	816,934	2,178,490	
Replacement Cost (\$)	-	750,000	960,000	
Annual revenue (\$)			228,928	
Annual net income (\$)			109,111	
Net present Value (\$)			-2,514,595*	
Present value of O&M (\$)			2,995,424	
Present value of costs			6,500,424	
Levelized annual cost (\$)			716,139	
Levelized Cost of energy (\$/kWhr)			0.247	

* net present cost was found to be with negative value indicating that the project will not be profitable with the currently selling prices for Solar PV plants announced by the government and the tariff prices will drastically increase in case of using hydrogen system as an energy storage system.

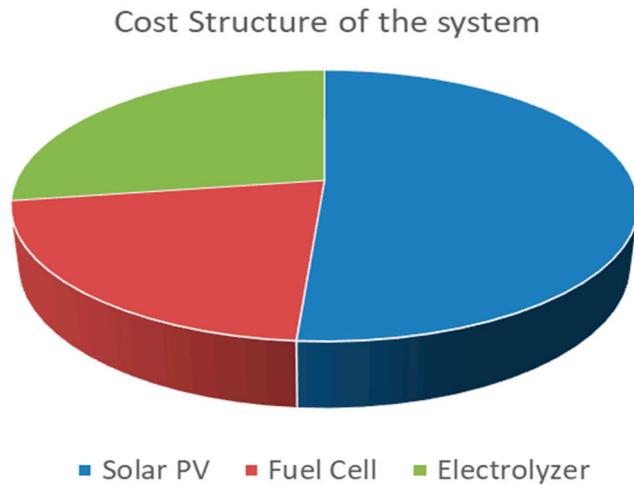


Figure 10. Cost structure of hybrid solar PV/hydrogen system.

4.1.b. Evaluation using HOMER Tool

HOMER -Pro [35] is an optimization model which performs thousands of simulations as discussed before and gives best possible design for the system. PV/FC configuration was set up as shown in Figure 11. and simulated in the site of Cairo International Airport and load profile was inserted in the program for one year as shown in Appendix B.2. This simulation was performed on HP laptop with specs of Intel® Core™ i5 CPU with 2.20 GHz Processor with Installed memory 4.00 GB.

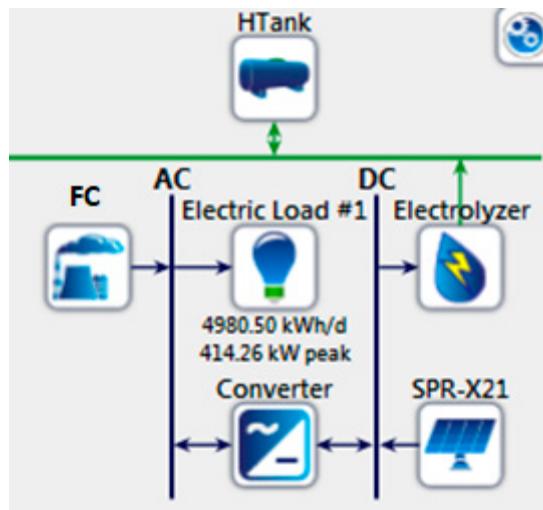


Figure 11. HOMER configuration (Surplus Mode) [35].

Detailed specs of the hybrid system components are being illustrated in Table 3, where data has been collected from commercial datasheets during the selection process.

Table 3. System Components Specs.

Photovoltaic Modules		Hydrogen Tank	
Rated Power (kW)	0.335	Capacity of hydrogen	100 kg
Type	monocrystalline	tank	
Abbreviation:	SPR-X21		
Panel Type:	Flat Type	Efficiency	98%

Rated Capacity(kW):	0.335		
Temperature coefficient:	-0.3	Lifetime	15 years
Operating temperature(C):	43	Initial tank level	10% relative to tank size
Efficiency (%):	21	Capital	\$14/kg
Manufacturer:	Sun Power	Replacement	\$14/kg
Model	SunPower X21-335-BLK	O&M	\$10/year/kg
Fuel Cell		Electrolyzer	
Nominal Power	250 kW	Nominal Power	300 kW
H2 consumption rate	5800 Btu/kWhr	H2 production rate	60 Nm3/hr
Input Pressure	15 psig	Output pressure	10 barg-27barg
AC Power Production	5	AC power consumption	5 kWhr/Nm3
Nominal efficiency	90%	Nominal efficiency	80%
Manufacturer	ES5-EA2AAN	Manufacturer	Hydrogenics
Model	Bloom Energy	Model	HySTAT-60-10
Capital	\$3000/kW	Capital	\$1200/kW
Replacement	\$3000/kW	Replacement	\$1200/kW
O&M	\$0.01/hour/kW	O&M	\$100/year/kW

An optimization analysis is used to find the best possible hybrid power system configuration based on the desired constraints at the lowest net present cost using the cycle charging control (CC). Cycle charging, combined dispatch and load following are three main controllers in HOMER where you apply the best controller that fits the application. It was found that cycle charging was the best controller to fully utilize the hydrogen system other than the other controllers which were not using the electrolyzer and hydrogen tank in simulation.

The optimized sizing results are illustrated in Table 4. The total electrical production from the hybrid power system the solar PV system (76.2%) and 748,235 kWh/year from the Genset (Fuel cell) (23.8%). This represents a renewable fraction of 100%. The proposed hybrid power system meets the AC primary load of 1,582,615 kWh/year (58% of the total production) The hybrid system is also used to power the electrolyzer 1,063, 082 kWh/year (42%) for hydrogen production and produces some excess power 214 kWh/year. As a result, the unmet electric load by Solar PV (main source of power) is 235,003 kWh/yr. and the total excess electricity is 366,370 kWh. This result is a crucial factor for determining the reliability criteria for the whole hybrid system. As shown in section 6.10, energy profiles were conducted to judge the performance of the system and check the accuracy of using DBM in evaluating annual energy production and hydrogen production. To validate these figures, HOMER pro was also used to conduct energy profiles for solar PV, fuel cell, electrolyzer and hydrogen tanks production/consumption as shown in Figures (12.a.b.c.d.e).

Solar PV was operating in range of 0-1800 kW, Fuel Cell in range of 0 -250 kW, Electrolyzer in range of 0-700 kW. These ranges were found in the same ranges of operation that was conducted by DBM method as shown in Figure 13. However, hydrogen tank storage was found to be varying between -50 to 200 kg which is different than DBM results. This stems from the fact that there is no proper power management controller for utilizing the hydrogen production and preventing any stresses on the hydrogen tanks as shown in Figure 12.d.

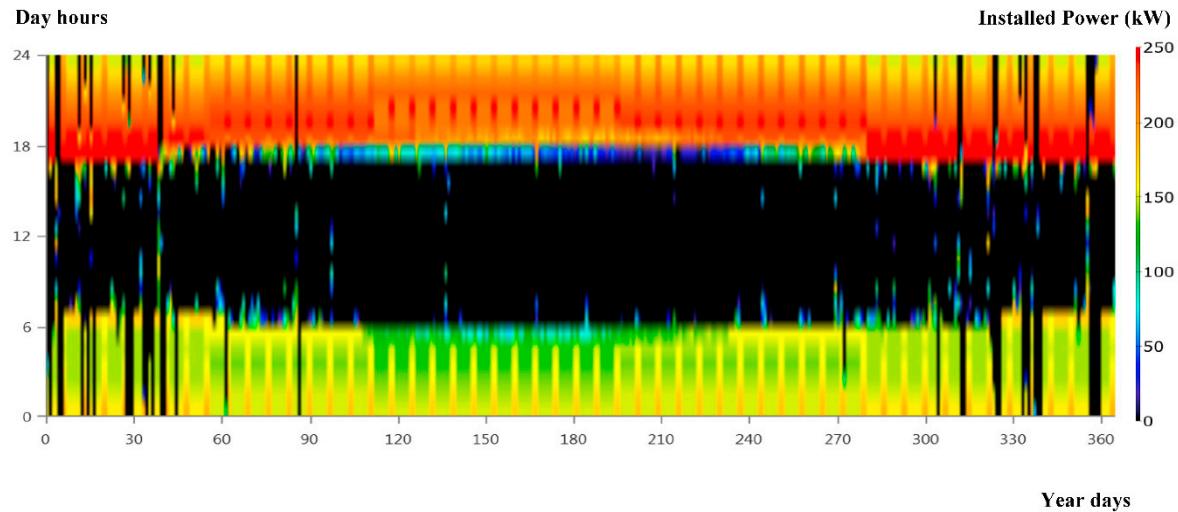


Figure 12.a. Generic 250kW Fuel Cell Output (kW) [35].

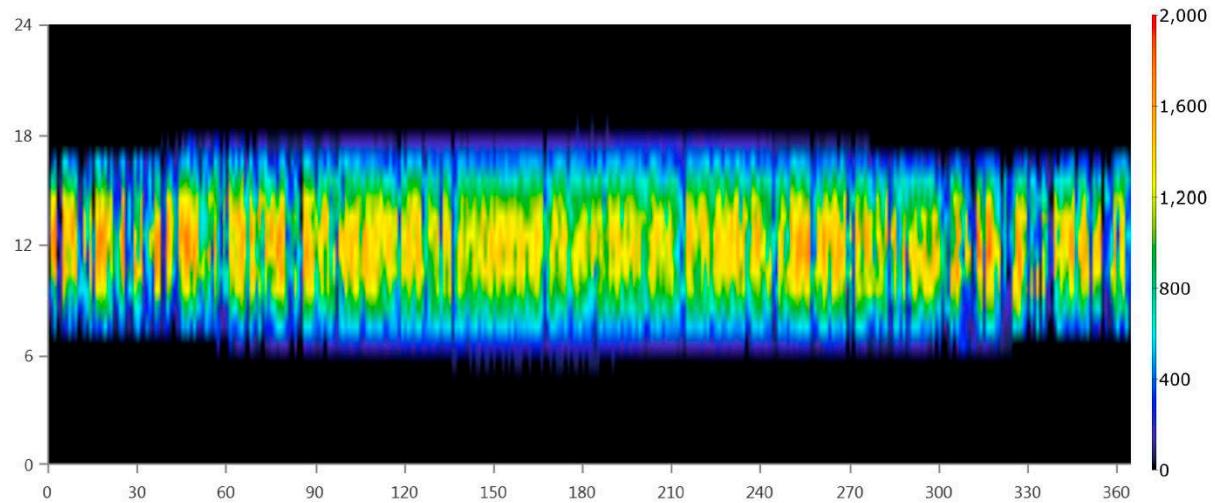


Figure 12. b. SunPower X21-335-BLK Output (kW) [35].

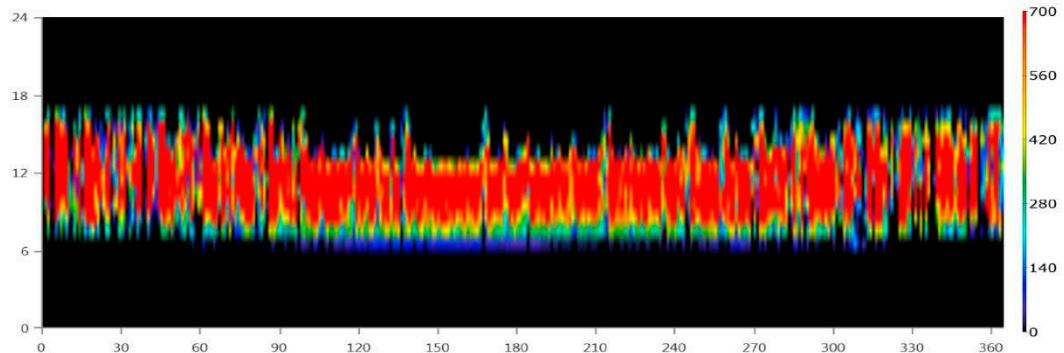


Figure 12. c. Generic Electrolyzer Input Power (kW) [35].

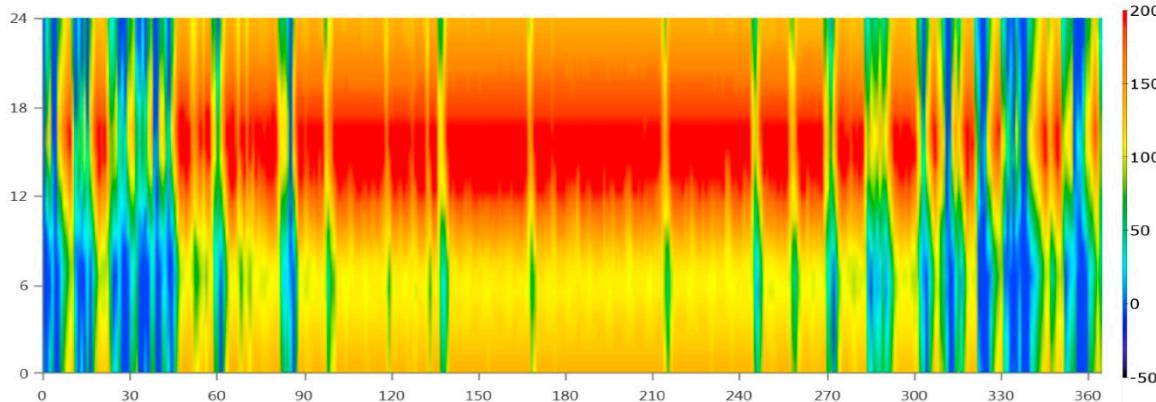


Figure 12.d. Hydrogen Tank Level (kg) [35].

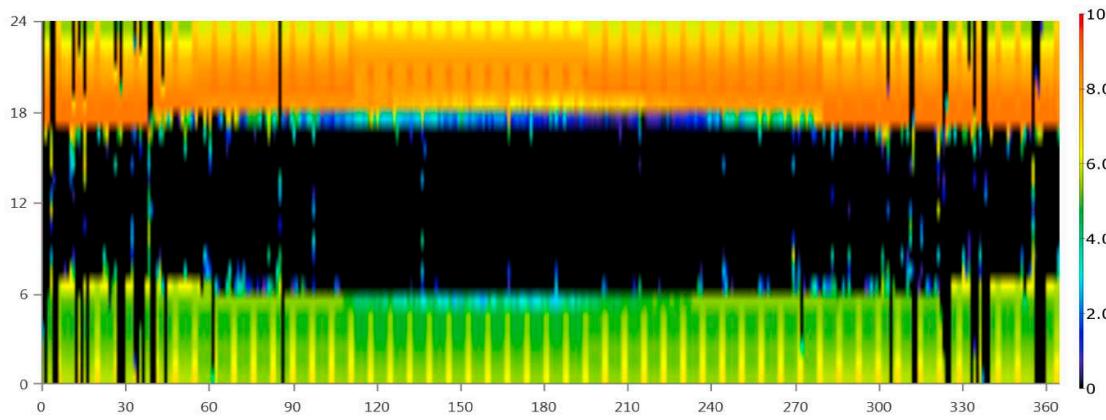


Figure 12.e. Stored Hydrogen Consumption (kg/hr) [35].

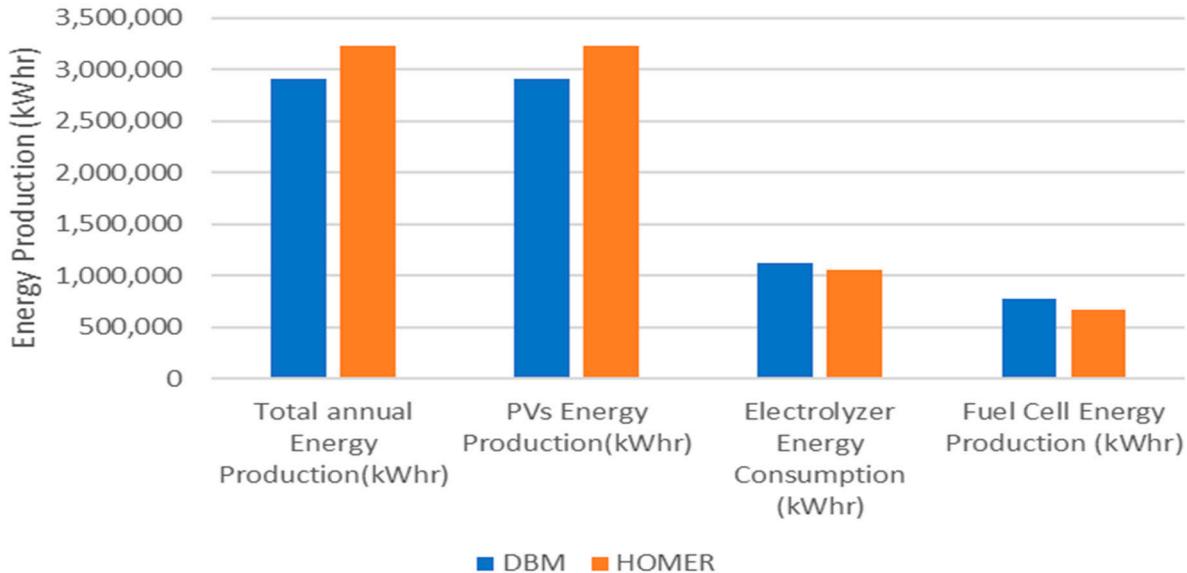


Figure 13. Comparison between DBM and HOMER Energy Results.

4.2.a. Sizing Methodology of Solar PV/Wind/Hydrogen system: Case Study 2

In this section, several cases have been discussed showing different renewable energy penetration percentages for WTGs and PVs. Adverse nature of wind-PV system can compensate the intermittency nature of each of system and therefore improve the overall reliability of the hybrid

system. Hybrid PV, wind turbines, fuel cell and electrolyzer are being sized and utilized in serving the community load as discussed before in the previous sections. The methodology in this section is the DBM, where three different cases were sized and checked for their constraints and load demand satisfaction. Sizing methodology was applied as discussed before. Starting from 250 kW WTG to 750 kW WTGs on a step of 250 kW and calculating PV energy required to satisfy the balance of generation. During this study, critical month of design for this system was found to be on January, when there is no surplus energy production. This observation was used for applying DBM which uses the critical month for sizing optimization and calculating energy production. Figures (14,15,16,17) were conducted using DBM for different mixes between solar PV and wind turbines to get the monthly energy profile for each month and select the best configuration that yields the maximum energy production.

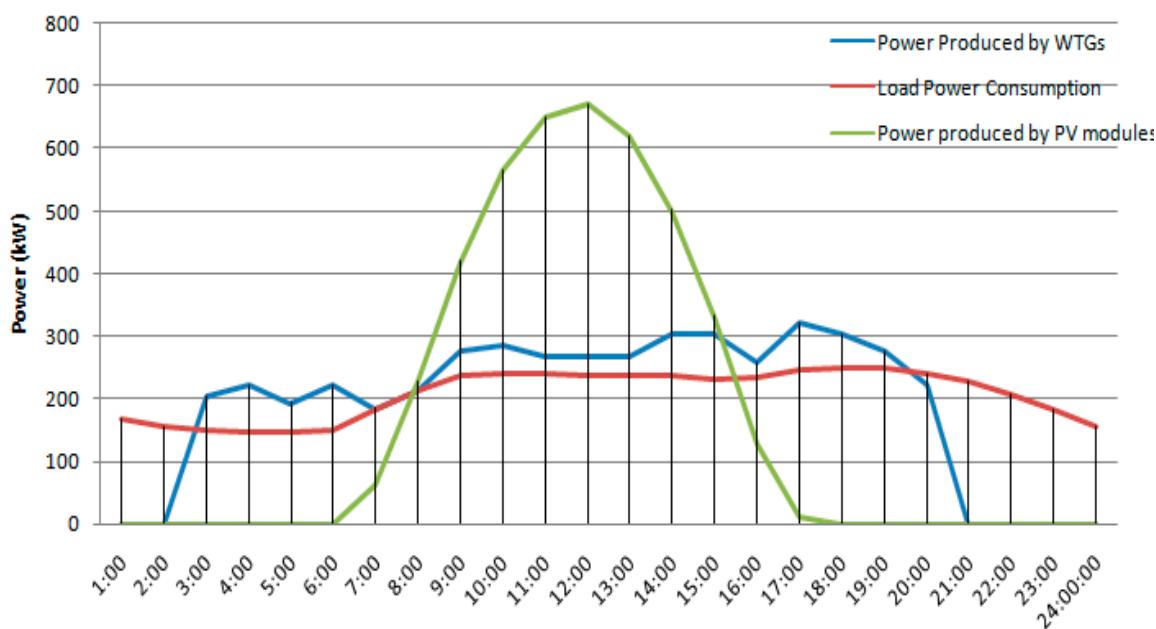
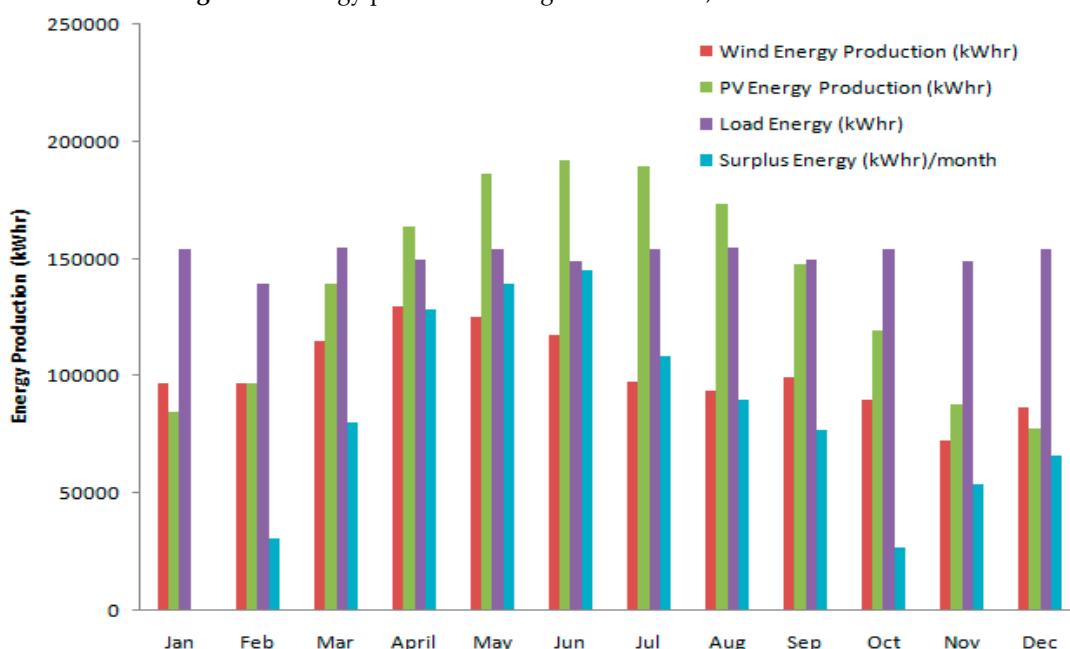
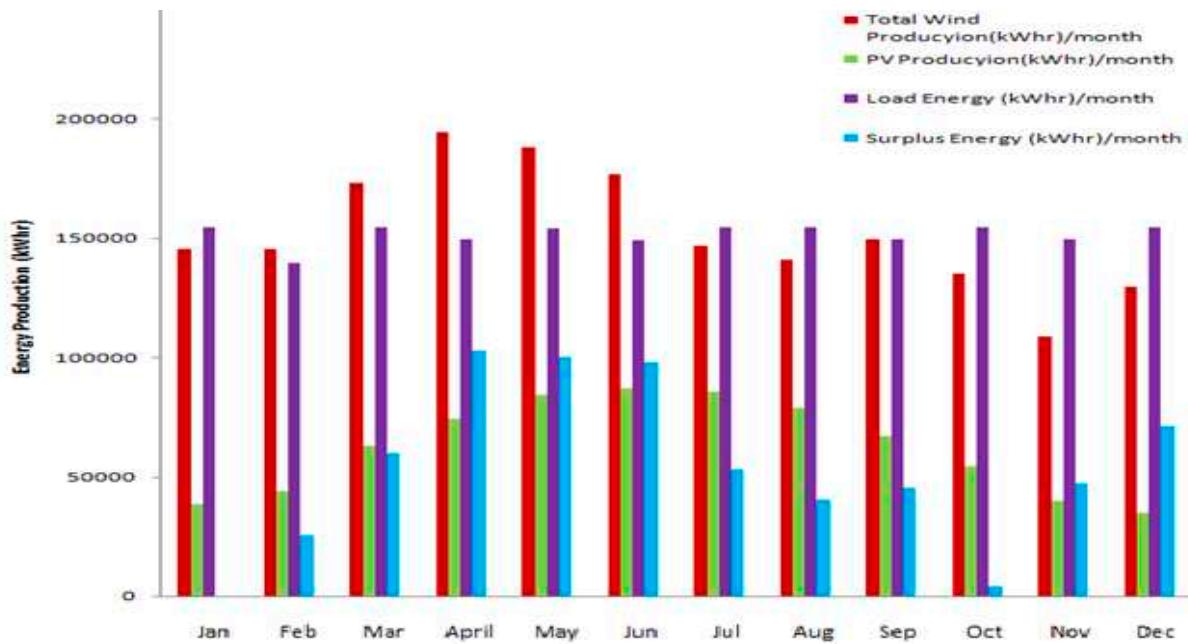
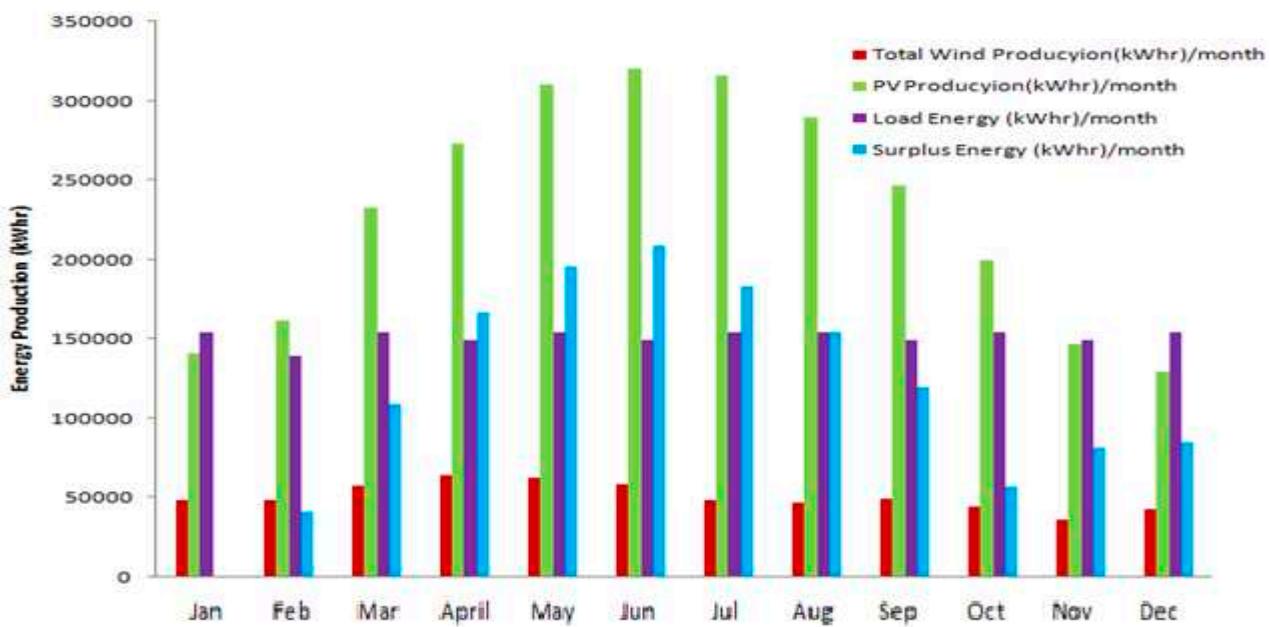


Figure 14. Power Curves for hybrid solar PV/Wind/Hydrogen system.

Figure 15. Energy production using 500kW WTGs, 4200 m² of PV modules.



Figure 16. Energy production using 750 kW WTGs, 1900 m² of Solar modules.Figure 17. Energy production using 250 kW WTGs, 7000 m² of Solar module.

Figures below were used for selecting the configuration that yields the maximum energy production. System 1 in Figure 15 was found to have the highest annual energy production with higher ratio of solar PV installed capacity compared to the installed wind turbine. As a result, system 1 was used in this paper for full simulation for 8760 hours and conducting energy profiles for all system components as shown in Figures (18.a.b.c.d.e.f).

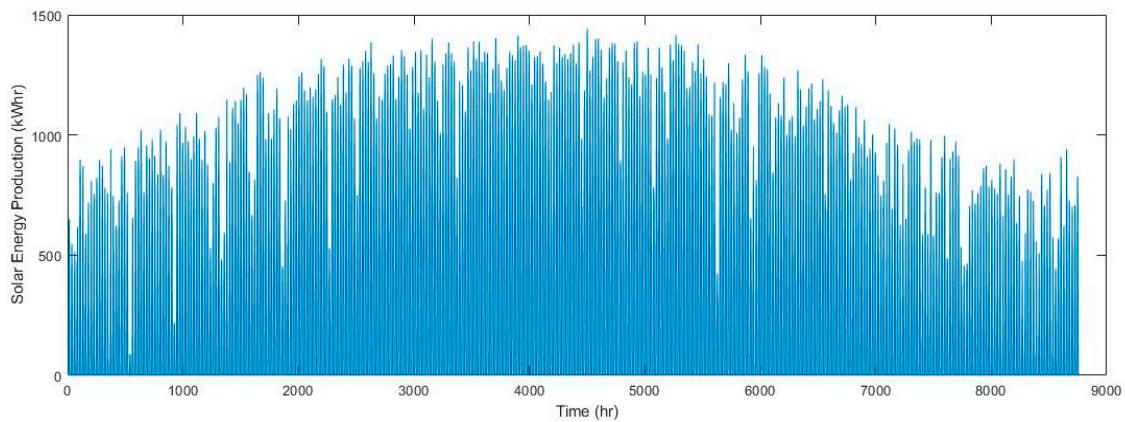


Figure 18. a. Solar energy production using DBM.

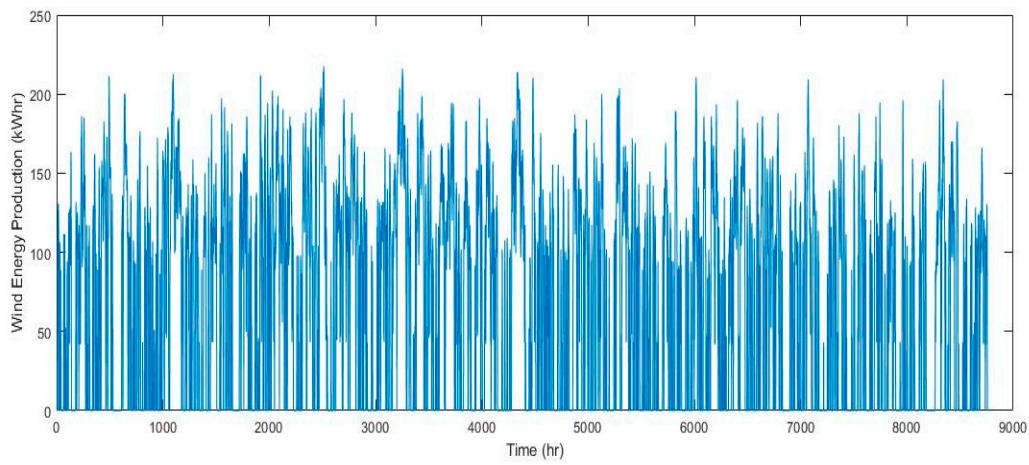


Figure 18. b. Wind energy production using DBM.

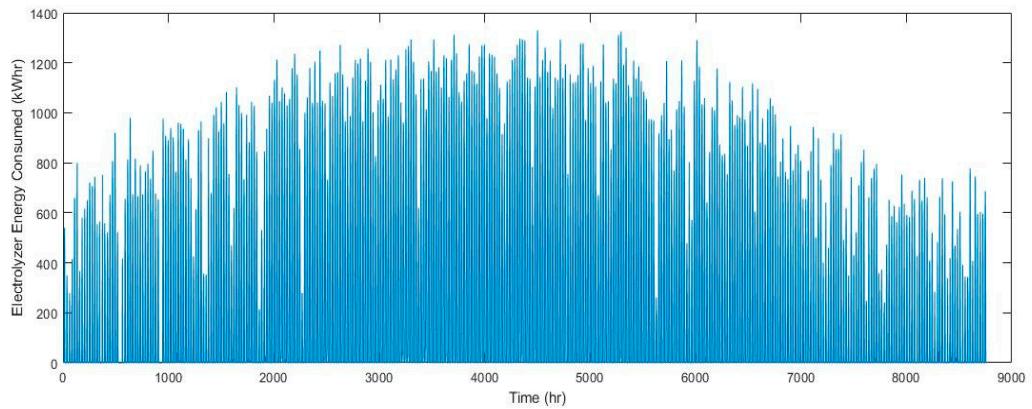


Figure 18. c. Electrolyzer energy consumed for hydrogen production.

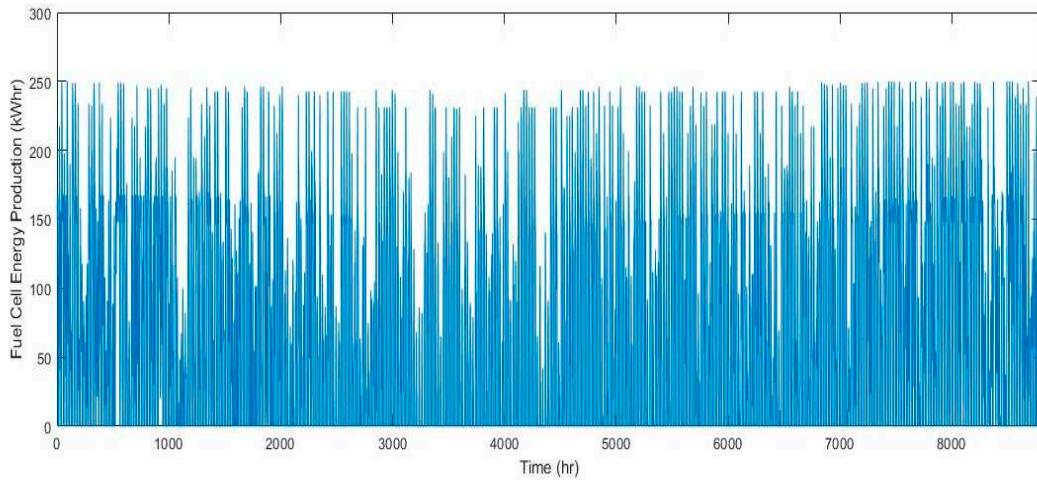


Figure 18. d. Fuel Cell energy production using DBM.

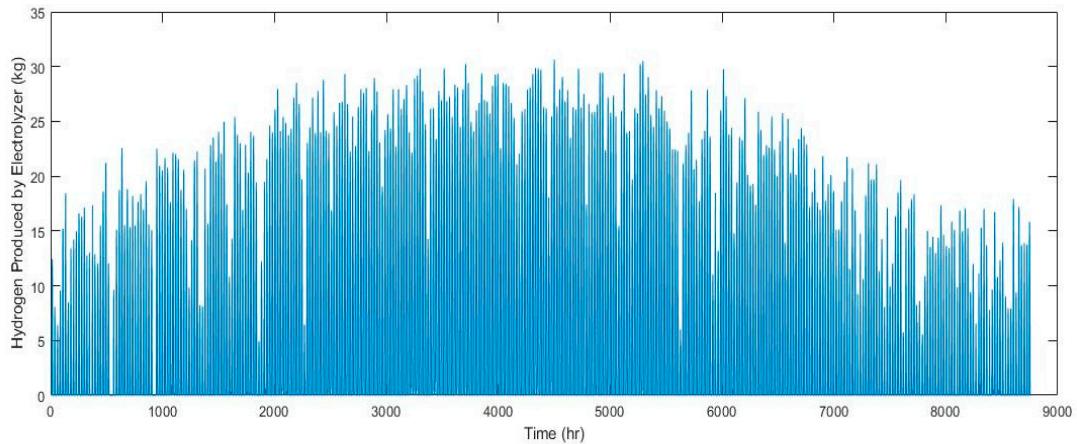


Figure 18. e. Hydrogen consumed by Fuel Cell.

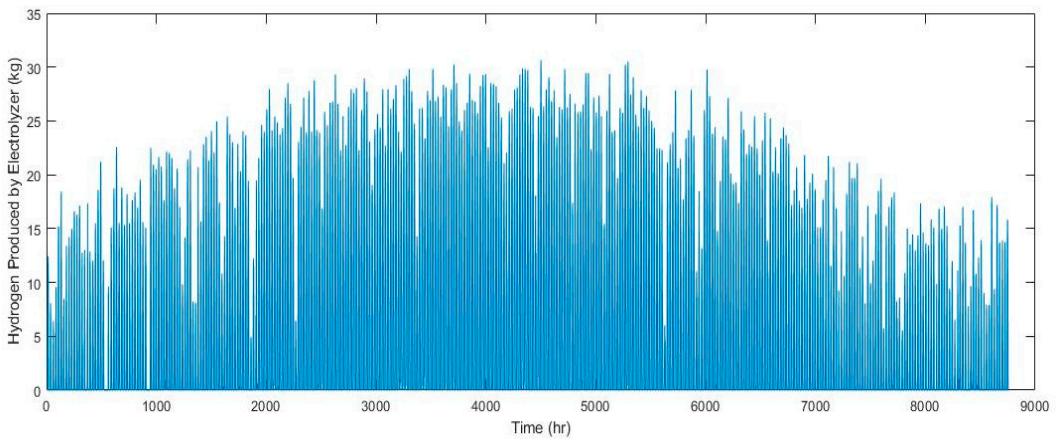


Figure 18. f. Hydrogen produced by Electrolyzer.

4.2. b. Sensitivity Analysis

Sensitivity is a measure of how the optimal mix of components changes for any parametric variations in the lifelong of the system. Optimal system design depends on interplay with various necessary input variables. When these input cases change, it is good to know how the optimum

system changes with variation of the variables. two separate sensitivity cases were carried out using variables of sensitivities like, design dependence on primary load, design dependence on diesel fuel, design dependence on maximum annual capacity shortage and minimum renewable fraction. The optimal system type, line graph and surface plot were used to make notes of the optimization results. In Figures 19,20, surface plot graph showing PV array capacity and wind turbine quantity variations with primary load. Considering only two of the sensitivity cases (solar PV and wind turbines installed capacity).

By keeping the other two variables as fixed (load and price) at 100% and minimum renewable fraction).

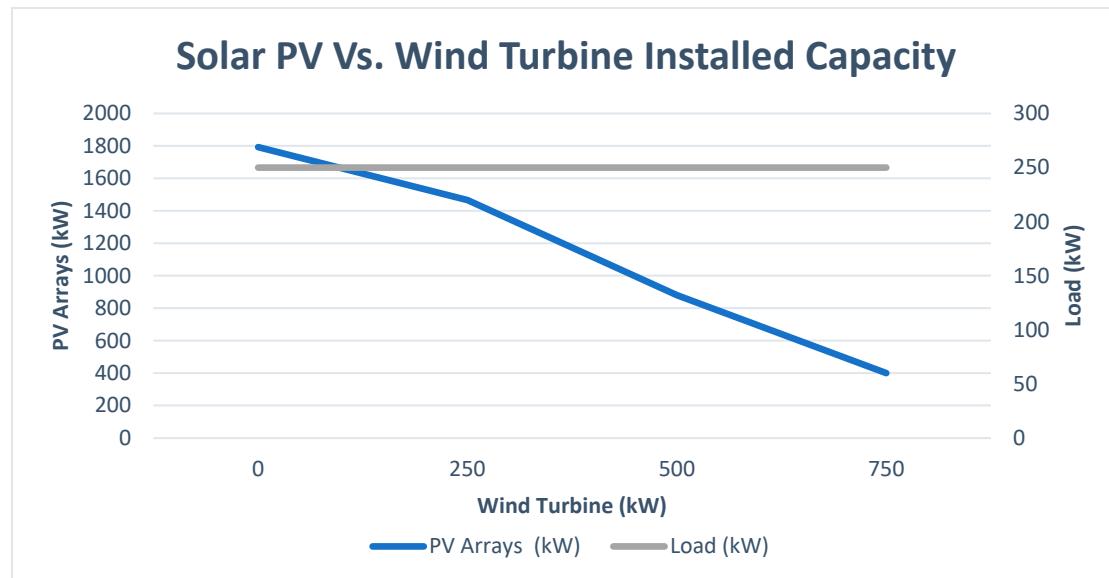


Figure 19. ratio of solar PV to wind turbines installed capacity

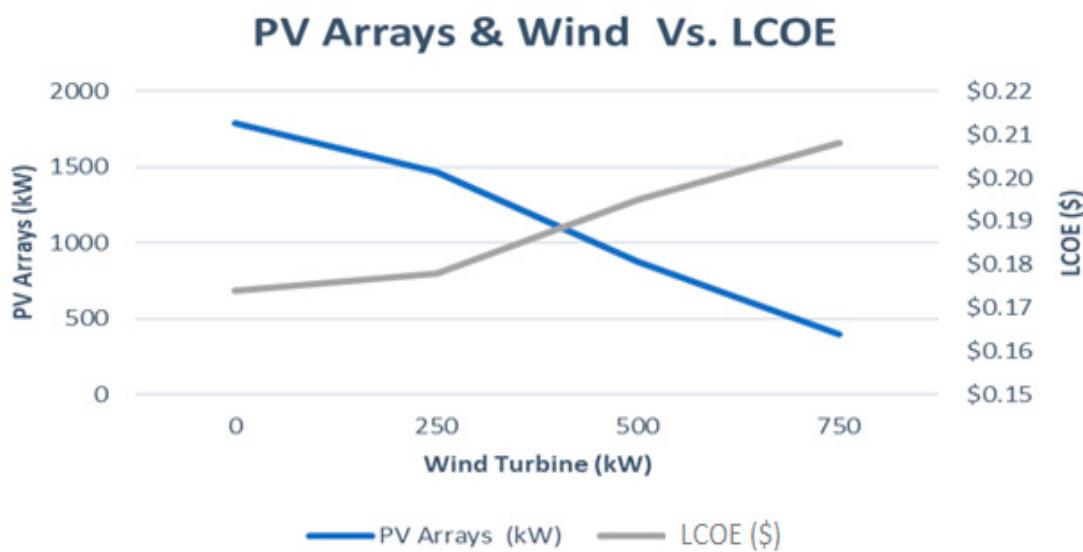


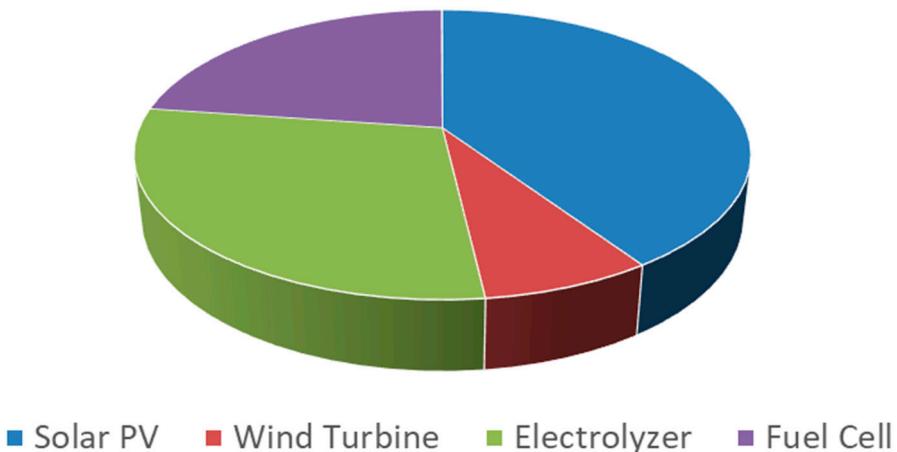
Figure 20. LCOE variation with PV to wind ratio.

Consider ESP =0.0788 \$/kWhr (NREA-Egypt), Project lifetime =25 years, Annual discount rate = 10% and assuming no decommissioning cost paid. Additionally, a sensibility analysis was conducted as shown in Figure 21 for studying the effect of ratio of PV and wind installed capacity on the leveledized cost of energy.

Table 4. Cost analysis of the hybrid system.

Month	Solar PV	Wind Turbine	Electrolyzer	Fuel Cell	Hydrogen Tank
Capital Cost (\$)	1,340,000	250,000	960,000	750,000	2000
Maintenance Cost (\$)	-	113,463	2,178,490	816,934	
Replacement Cost (\$)	-	-	960,000	750,000	
Annual revenue (\$)			263,678		
Annual net income (\$)			139,323		
Net present Value (\$)			-2,037,360		
Present value of O&M (\$)			3,108,886		
Present value of costs			6,410,886		
Levelized annual cost (\$)			706,275		
Levelized Cost of energy (\$/kWhr)			0.2116		

Cost Structure of the hybrid system

**Figure 21.** Cost structure of system 1.

Simulation of HOMER was conducted for 8760 hours as shown in Figures [22.a.b.c.d.e] to deduce the operation profiles of fuel cell, solar PV, wind turbine and hydrogen tanks respectively.

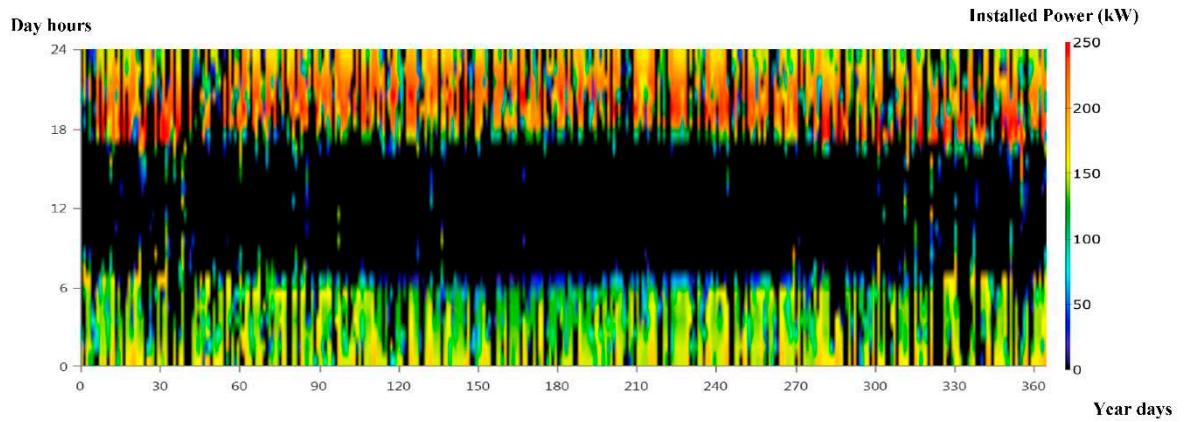


Figure 22. a. Fuel Cell operation using HOMER [35].

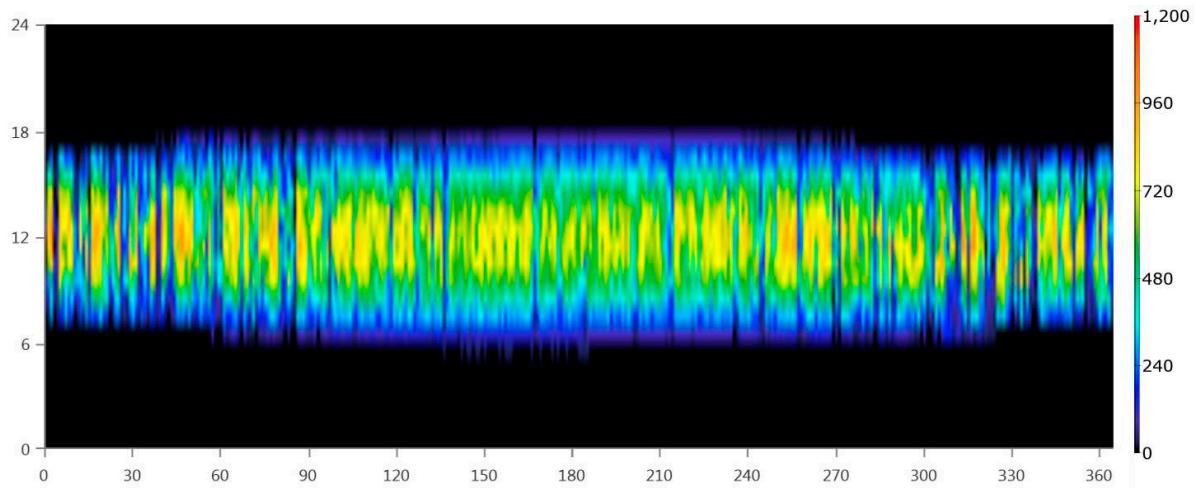


Figure 22. b. Solar PV operation using HOMER [35].

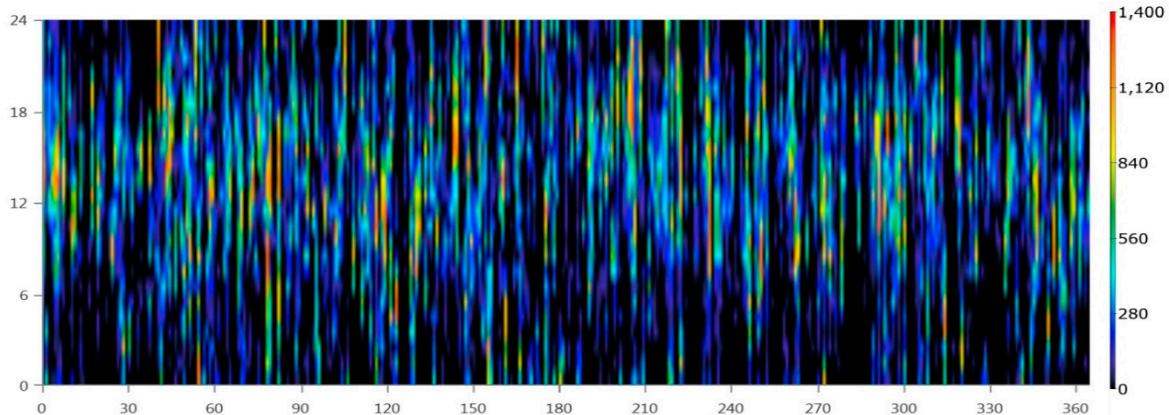


Figure 22. c. Wind turbine operation using HOMER [35].

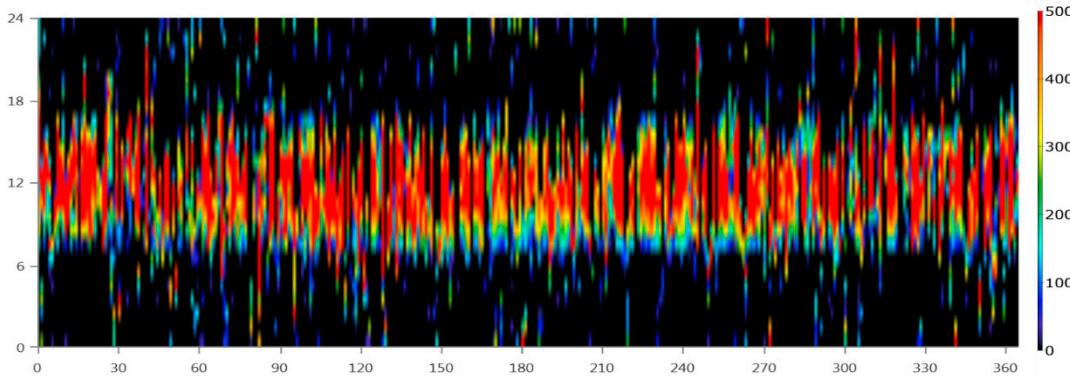


Figure 22. d. Electrolyzer operation profile [35].

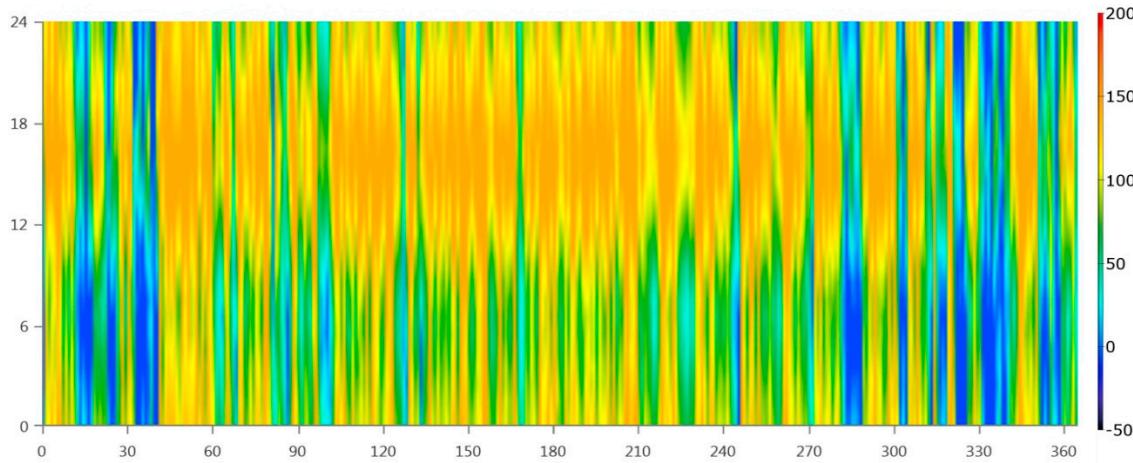


Figure 22. e. Hydrogen tanks storage level using HOMER [35].

A final comparison for the hybrid systems discussed in three case studies is conducted in terms of the sizing of the system components and cost results as shown in Table 5.

Table 5. Comparison between thesis sized hybrid systems.

Point of Comparison	PV/FC/ELZ	WIND/FC/ELZ	PV/WIND/FC/ELZ
Energy Production using DBM (kWhr)	2,905,172	3,223,807	3,377,699
Energy Production using HOMER (kWhr)	3,138,000	3,396,359	3,262,563
Absolute difference (%)	-5%	-5.3%	+3.5%
Installed Capacity using DBM (kW)	PV: 1793 kW FC: 300 kW ELZ:800 kW H2 tank: 100 kg	WTG: 1340 kW FC:300 kW ELZ:1000 kW H2 tank: 100 kg	PV: 1466 kW WTG: 250 KW FC: 300 kW ELZ:800 kW H2 tank: 100 kg (best techno-economic config.)

Installed Capacity using HOMER	PV: 1803 kW FC: 200 Kw ELZ:400 kW H2 tank:100 kg	WTG: 1980 kW FC:200 kW ELZ:500 kW H2 tank:150 kg	PV:1032 kW WTG:1320 kW FC:250 kW ELZ:500 KW H2 tank:150 kg
Levelized cost of energy-DBM	\$0.247	\$0.237	\$0.211
Levelized cost of energy-HOMER	\$0.332	\$0.310	\$0.232
Greenhouse emissions	Only manufacturing material	Only manufacturing material	Only manufacturing material

Based on the comparison and cost analysis study conducted in Table 5, hybrid PV/Wind with high penetration of solar PV modules was selected for the implementation in the site of Cairo International Airport to supply the community load of 250 kW peak. Finally, a comparison of installed capacities deduced by DBM and HOMER in the selected site for implementation was conducted as shown in Figures 23,24. It was observed that HOMER favors the wind energy penetration rather than solar PV. However, this penetration affects the utilization of the installed wind turbines resulting in a lower capacity factor of turbines.

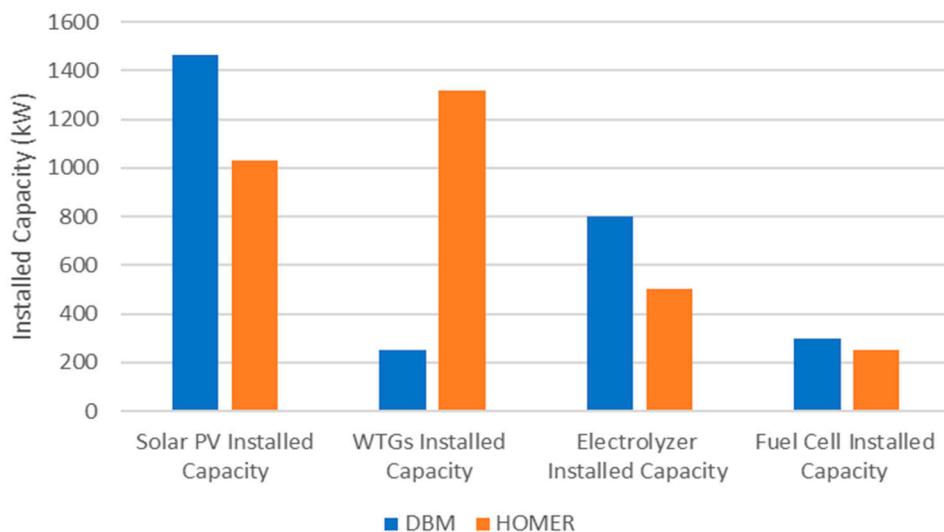


Figure 23. Comparing between installed capacities of hybrid system (PV/WTG/Hydrogen).

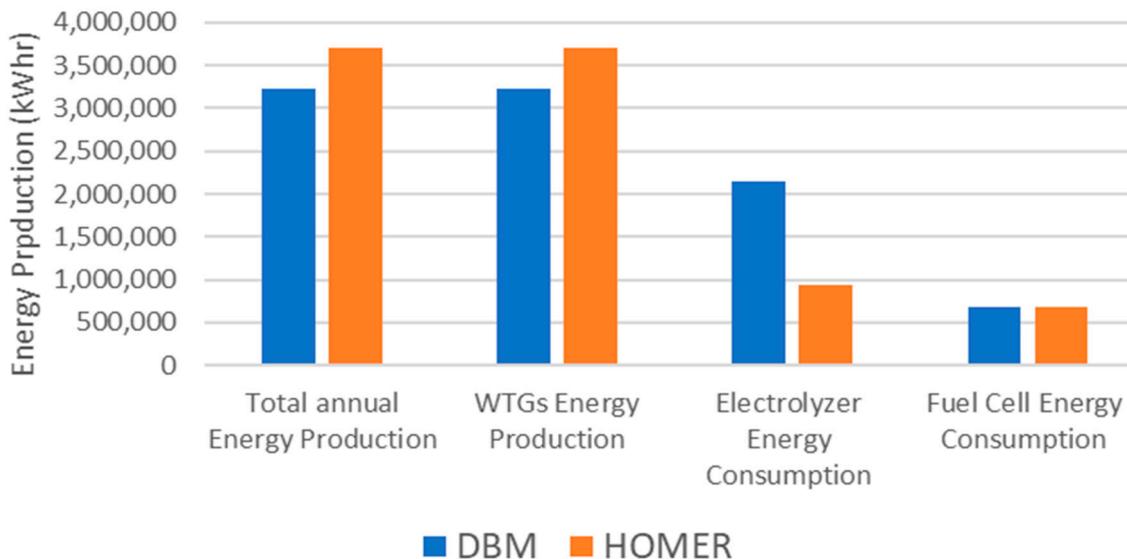


Figure 24. Comparing installed capacity for WTG standalone system.

Conclusion

Our work introduced a deterministic approach for sizing optimization of hybrid energy systems that serves as a reliable benchmark for comparison with existing methods. Unlike software tools like HOMER and other metaheuristic methods, which often require significant computational resources and longer convergence times, our proposed method offers a more efficient and time-effective solution. This deterministic balanced method not only streamlines the optimization process but also maintains accuracy and reliability, making it a valuable addition to the field of hybrid energy system design.

Additionally, this work discussed and simulated hybrid off-grid system to utilize excess of energy production in summer and spring times in the studied location. In fact, excess energy production in summer was due to solar PV modules and that was found in spring was due to WTGs. This means that optimal sizing methodologies have managed to sustain the balance of generation throughout the year and producing an excess of generation in certain times of the year due to the natural response of the renewable resources in the studied location towards the meteorological conditions. Consequently, this excess energy produced can be fully utilized in an energy storage element, in the proposed system that will be the hydrogen tanks. Hydrogen tanks can be then used as the infrastructure for hydrogen refueling stations for the city. Not only will these stations utilize the excess energy produced, but they will also introduce the power to gas concepts in the automotive industry, making the studied system an exemplar model for an energy hub for electricity and fuel production.

The best configuration found for this studied location was Solar PV/wind hybrid system with high penetration of solar PV. This configuration lead to the highest energy production with the minimum levelized cost of energy. HOMER software was the verification tool for DBM method, where the absolute difference between the two methods was in the range of 5%. However, HOMER in wind standalone system was exceeding energy production than DBM by 5.3% and given that the HOMER and DBM were having the same input data (weather data and load profile). Also, HOMER software was preferring the wind energy penetration rather than the solar energy and that was obvious in the hybrid mix of wind and PV modules, which was opposite to the DBM method which achieved a lower cost with the highest penetration of solar PV and maintaining the highest annual energy production.

Future Work

According to the previous results of the studied systems, it has been observed that the surplus power production, which is achieved in winter, spring and summer seasons based on system configurations has to be controlled and utilized to satisfy the power balance for other connected systems and avoid stresses on the current connected energy storage system. This approach has highlighted the concept of interconnectivity between clusters of DGs to achieve the optimal energy sharing and utilize the generated surplus power in all DGs. In future work, it was suggested to work on controlling the power sharing process between cluster of DGs and resolve the optimal power balance sharing problem on a larger scale as shown in Figure 32.

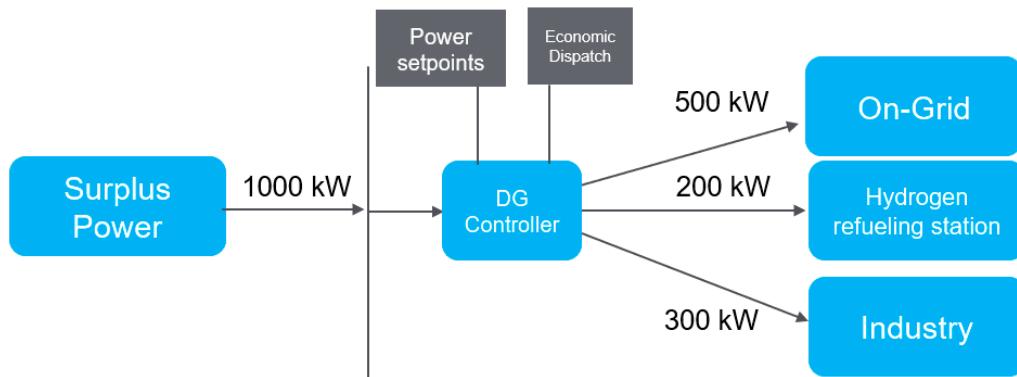


Figure 32. Power sharing between cluster of DGs.

Conflict of Interest: On behalf of all authors, the corresponding author states that there is no conflict of interest

Nomenclature

AEP : Annual energy production (kWh)

AR : Annual revenue from selling the electricity (\$/year)

ANI : Annual net income (\$/year)

COE: Cost of energy (\$)

CI : Capital investment (\$)

DC : Decommissioning costs (\$)

ESP : Electricity selling price (\$/kWh)

E^+ : Surplus energy supplied by PV arrays

E^- : Total lack of energy which will be supplied by fuel cell and electrolyzer

E^D : Energy demanded by load and supplied by solar PV arrays

E^{-1} : Lack of energy from 12:00 a.m. till sunrise

E^{-2} : Lack of energy from sunset till 12:00 a.m.

$E^{D,1}$: Energy demanded by load and supplied by solar PV arrays during sunrise

$E^{D,2}$: Energy demanded by load and supplied by solar PV arrays during sunset

ELZ: Electrolyzer

FC: Fuel cell

FV : Future value

G_t : Irradiance power (W/m²)

LAC : Levelized annual cost (\$)

LCOE : Levelized cost of energy (\$/kWh)

LSCS: Lifespan cost of the hybrid system

LIP: Load interruption probability

NPV : Net present value (\$)

O&M cost : Annual operating and maintenance cost (\$/kWh)

PVDC : Present value of the cost of decommissioning (\$)

PVC : Present value of all the costs (\$)

PVM : Present value maintenance and repair cost

PV : Photovoltaics

PV* : Present value of the cost analysis

P : Period of years (years)

P_{pv} : Solar PV power (kW)

P_l : Load power (kW)

P_{wind} : Power of wind generator (kW)

P_r : Rated electrical power output (kW)

P-PMS : Predictive Power management strategies

R : Annual discount rate (%)

P-PMS : Reactive Power management strategies

T_x : Temperature de-rating factor,

T_m : Module temperature (°C)

T_a : Reference temperature (25°C)

T_e : End time of simulation

WTG: Wind turbine generator

V_N : Rated speed (m/s)

V_D : Cut-in speed (m/s)

V_R : Cut-off speed (m/s)

V_v : Wind speed (m/s)

α : Power temperature coefficient for module selected (-0.331% °C)

η : Efficiency of the system

η_{ELZ} : Efficiency of the electrolyzer

Appendix A DBM methodology

As shown in Tables A.1, A.2,A.3,A.4,A.5 The meteorological data, location and equation functions used in interoperating the methodology of calculating the energy production for one year.

Table A1. Wind Data

LAT	LON	height (m)	YEAR	Hour	VD	VR	VN	Wspd (m/s)
30.05	31.25	84	1/1/2018	1:00	3	25	15	1.8
30.05	31.25	84	1/1/2018	2:00	3	25	15	1.3
30.05	31.25	84	1/1/2018	3:00	3	25	15	1.4
30.05	31.25	84	1/1/2018	4:00	3	25	15	1.8
30.05	31.25	84	1/1/2018	5:00	3	25	15	1.2
30.05	31.25	84	1/1/2018	6:00	3	25	15	1.4
30.05	31.25	84	1/1/2018	7:00	3	25	15	1.2
30.05	31.25	84	1/1/2018	8:00	3	25	15	1.9
30.05	31.25	84	1/1/2018	9:00	3	25	15	1.8
30.05	31.25	84	1/1/2018	10:00	3	25	15	3.8
30.05	31.25	84	1/1/2018	11:00	3	25	15	3.6
30.05	31.25	84	1/1/2018	12:00	3	25	15	3.8
30.05	31.25	84	1/1/2018	13:00	3	25	15	4.5
30.05	31.25	84	1/1/2018	14:00	3	25	15	4.9
30.05	31.25	84	1/1/2018	15:00	3	25	15	4.5
30.05	31.25	84	1/1/2018	16:00	3	25	15	5.4
30.05	31.25	84	1/1/2018	17:00	3	25	15	4.5
30.05	31.25	84	1/1/2018	18:00	3	25	15	4.7
30.05	31.25	84	1/1/2018	19:00	3	25	15	3.6
30.05	31.25	84	1/1/2018	20:00	3	25	15	3.1
30.05	31.25	84	1/1/2018	21:00	3	25	15	2.7
30.05	31.25	84	1/1/2018	22:00	3	25	15	1.8
30.05	31.25	84	1/1/2018	23:00	3	25	15	1.3
30.05	31.25	84	1/1/2018	24:00:00	3	25	15	1.2

Table A2. Solar PV Data.

LAT	LON	Height (m)	YEAR	Hour	Temperature (°C)	Irradiance (kW/m ²)
30.05	31.25	84	1/1/2018	1:00	17.9	0
30.05	31.25	84	1/1/2018	2:00	17.3	0
30.05	31.25	84	1/1/2018	3:00	16.7	0
30.05	31.25	84	1/1/2018	4:00	16.4	0
30.05	31.25	84	1/1/2018	5:00	16.1	0
30.05	31.25	84	1/1/2018	6:00	15.9	0
30.05	31.25	84	1/1/2018	7:00	15.8	0
30.05	31.25	84	1/1/2018	8:00	16.8	0.062
30.05	31.25	84	1/1/2018	9:00	18.9	0.246
30.05	31.25	84	1/1/2018	10:00	21.3	0.413
30.05	31.25	84	1/1/2018	11:00	21.2	0.172
30.05	31.25	84	1/1/2018	12:00	22.1	0.359
30.05	31.25	84	1/1/2018	13:00	22.3	0.269
30.05	31.25	84	1/1/2018	14:00	23.6	0.561
30.05	31.25	84	1/1/2018	15:00	23.7	0.316
30.05	31.25	84	1/1/2018	16:00	22.9	0.12
30.05	31.25	84	1/1/2018	17:00	21.7	0.006
30.05	31.25	84	1/1/2018	18:00	20.6	0
30.05	31.25	84	1/1/2018	19:00	20	0
30.05	31.25	84	1/1/2018	20:00	19.3	0
30.05	31.25	84	1/1/2018	21:00	18.6	0
30.05	31.25	84	1/1/2018	22:00	18	0
30.05	31.25	84	1/1/2018	23:00	17.3	0
30.05	31.25	84	1/1/2018	24:00:00	16.7	0

Table A3. Wind Energy Calculations.

A	B	C	k1	k2	k3	PN	Pout	Wind Power (kW)	Wind Energy (kWh)
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	220.2102857	0	0
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	153.2773228	0	0
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	166.8953228	0	0
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	220.2102857	0	0
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	139.543619	0	0
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	166.8953228	0	0
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	139.543619	0	0
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	233.2497672	0	0
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	220.2102857	0	229.5081058
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	459.0162116	459.0162116	448.1172487
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	437.2182857	437.2182857	448.1172487
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	459.0162116	459.0162116	495.3402487
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	531.6642857	531.6642857	551.1481376
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	570.6319894	570.6319894	551.1481376
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	531.6642857	531.6642857	574.2012857
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	616.7382857	616.7382857	574.2012857
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	531.6642857	531.6642857	541.5219153
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	551.379545	551.379545	494.2989153
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	437.2182857	437.2182857	408.9584709
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	380.6986561	380.6986561	190.349328
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	333.4002857	0	0
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	220.2102857	0	0
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	153.2773228	0	0
-0.031168831	0.138	-0.005259259	-0.00162	-0.00463	0.216	1100	139.543619	0	0

Table A4. Solar PV Energy Calculations.

Area of Modules	No. of Modules	Irradiance (kW/m ²)	PV Power (kW)	PV Energy (kWhr)	PV+Wind
7000	4375	0	0	0	0
7000	4375	0	0	0	0
7000	4375	0	0	0	0
7000	4375	0	0	0	0
7000	4375	0	0	0	0
7000	4375	0	0	0	0
7000	4375	0	0	47.282293	47.28229275
7000	4375	0.062	94.564586	233.17757	233.177574
7000	4375	0.246	371.79056	494.70937	546.8703048
7000	4375	0.413	617.62818	437.48121	539.3260351
7000	4375	0.172	257.33423	396.15366	497.9984919
7000	4375	0.359	534.97309	467.73724	580.3145712
7000	4375	0.269	400.50139	615.46173	740.7226719
7000	4375	0.561	830.42207	648.98653	774.2474735
7000	4375	0.316	467.55099	322.86852	453.3688137
7000	4375	0.12	178.18605	93.57149	224.0717825
7000	4375	0.006	8.9569305	4.4784653	127.5516278
7000	4375	0	0	0	112.3406626
7000	4375	0	0	0	92.94510702
7000	4375	0	0	0	43.26121092
7000	4375	0	0	0	0
7000	4375	0	0	0	0
7000	4375	0	0	0	0

Table A5. Hydrogen System Energy Calculations.

Load(kW)	Loadenergy(kWhr)	Electrolyzer Energy Available (kWhr)	Hydrogen Produced by Electrolyzer (kg)	Fuel Cell Energy Produced (kWhr)	Hydrogen consumed by Fuel Cell (kg)
167.5	162.5	0	0	162.5	5.828114407
157.5	153.75	0	0	153.75	5.514292862
150	148.75	0	0	148.75	5.334966265
147.5	147.5	0	0	147.5	5.290134616
147.5	148.75	0	0	148.75	5.334966265
150	167.5	0	0	167.5	6.007441005
185	200	0	0	200	7.173063886
215	226.25	0	0	226.25	8.114528521
237.5	238.75	0	0	9.24189418	0.331463487
240	240	208.1172487	4.796969221	0	0
240	238.75	209.3672487	4.82578092	0	0
237.5	237.5	257.8402487	5.943052508	0	0
237.5	237.5	313.6481376	7.229388586	0	0
237.5	235	316.1481376	7.287011984	0	0
232.5	233.75	340.4512857	7.847183975	0	0
235	241.25	332.9512857	7.674313781	0	0
247.5	248.75	292.7719153	6.748205041	0	0
250	250	244.2989153	5.630933452	0	0
250	245	163.9584709	3.77913769	0	0
240	233.75	0	0	43.40067196	1.556578963
227.5	217.5	0	0	217.5	7.800706976
207.5	195	0	0	195	6.993737289
182.5	170	0	0	170	6.097104303
157.5	162.5	0	0	162.5	5.828114407

A.6 Load Profiles

Based on RTS Model, the load profile was generated based on the percentages standards for the peak power for the system which is 250 kW in this analysis.

Table A.6.1 RTS Load Profile.

Time (hr.)	Winter weeks (1-8&44-52)		Summer Weeks(18-30)		Spring/Fall weeks (9-17&31-43)	
	% of Peak Power	Power (kW)	% of Peak Power	Power (kW)	% of Peak Power	Power (kW)
0	67	167.5	64	160	63	157.5
1	63	157.5	60	150	62	155
2	60	150	58	145	60	150
3	59	147.5	56	140	58	145
4	59	147.5	56	140	59	147.5
5	60	150	58	145	65	162.5
6	74	185	64	160	72	180
7	86	215	76	190	85	212.5
8	95	237.5	87	217.5	95	237.5
9	96	240	95	237.5	99	247.5
10	96	240	99	247.5	100	250
11	95	237.5	100	250	99	247.5
12	95	237.5	99	247.5	93	232.5
13	95	237.5	100	250	92	230
14	93	232.5	100	250	90	225
15	94	235	97	242.5	88	220
16	99	247.5	96	240	90	225
17	100	250	96	240	92	230
18	100	250	93	232.5	96	240
19	96	240	92	230	98	245
20	91	227.5	92	230	96	240
21	83	207.5	93	232.5	90	225
22	73	182.5	87	217.5	80	200
23	63	157.5	72	180	70	175

Table A.6.2 Load Profile for Winter weeks.

Hours		Winter weeks			
		Weekday(%)	Peak Load (kW)	Weekend(%)	Peak Load (kW)
12	1	67	168	78	195
1	2	63	158	72	180
2	3	60	150	68	170
3	4	59	148	66	165
4	5	59	148	64	160
5	6	60	150	65	163
6	7	74	185	66	165
7	8	86	215	70	175
8	9	95	238	80	200
9	10	96	240	88	220
10	11	96	240	90	225
11	Noon	95	238	91	228
Noon	1	95	238	90	225
1	2	95	238	88	220
2	3	93	233	87	218
3	4	94	235	87	218
4	5	99	248	91	228
5	6	100	250	100	250
6	7	100	250	99	248
7	8	96	240	97	243
8	9	91	228	94	235
9	10	83	208	92	230
10	11	73	183	87	218
11	12	63	158	81	203

Table A.6.3. Load Profile for Summer Weeks.

Hours	Summer Weeks (18-30)				
	Weekday(%)	Peak Load (kW)	Weekend(%)	Peak Load (kW)	
12	1	64	74	185	
1	2	60	70	175	
2	3	58	66	165	
3	4	56	65	162.5	
4	5	56	64	160	
5	6	58	62	155	
6	7	64	62	155	
7	8	76	66	165	
8	9	87	81	202.5	
9	10	95	86	215	
10	11	99	91	227.5	
11	Noon	100	93	232.5	
Noon	1	99	93	232.5	
1	2	100	92	230	
2	3	100	91	227.5	
3	4	97	91	227.5	
4	5	96	92	230	
5	6	96	94	235	
6	7	93	95	237.5	
7	8	92	95	237.5	
8	9	92	100	250	
9	10	93	93	232.5	
10	11	87	88	220	
11	12	72	80	200	

Table A.6.4 Load Profile for Spring/Fall Weeks.

Hours		Spring/Fall weeks (9-17&31-43)			
		Weekday(%)	Peak Load (kW)	Weekend(%)	Peak Load (kW)
12	1	63	157.5	75	187.5
1	2	62	155	73	182.5
2	3	60	150	69	172.5
3	4	58	145	66	165
4	5	59	147.5	65	162.5
5	6	65	162.5	65	162.5
6	7	72	180	68	170
7	8	85	212.5	74	185
8	9	95	237.5	83	207.5
9	10	99	247.5	89	222.5
10	11	100	250	92	230
11	Noon	99	247.5	94	235
Noon	1	93	232.5	91	227.5
1	2	92	230	90	225
2	3	90	225	90	225
3	4	88	220	86	215
4	5	90	225	85	212.5
5	6	92	230	88	220
6	7	96	240	92	230
7	8	98	245	100	250
8	9	96	240	97	242.5
9	10	90	225	95	237.5
10	11	80	200	90	225
11	12	70	175	85	212.5

Appendix B Software Tools

B.1 METEONORM Model



Figure B1. METEONORM software.

B.2 HOMER Model

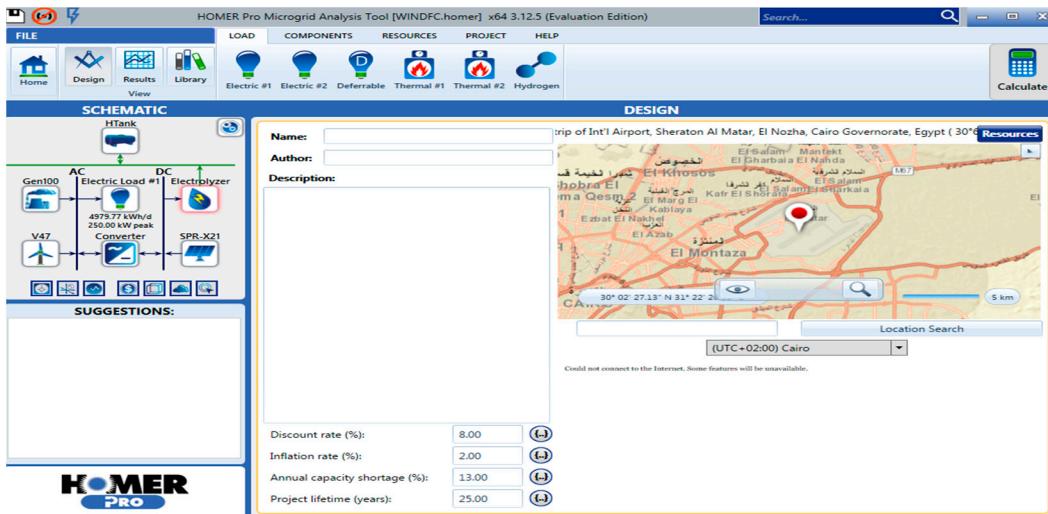


Figure B.2.1. HOMER Configuration.

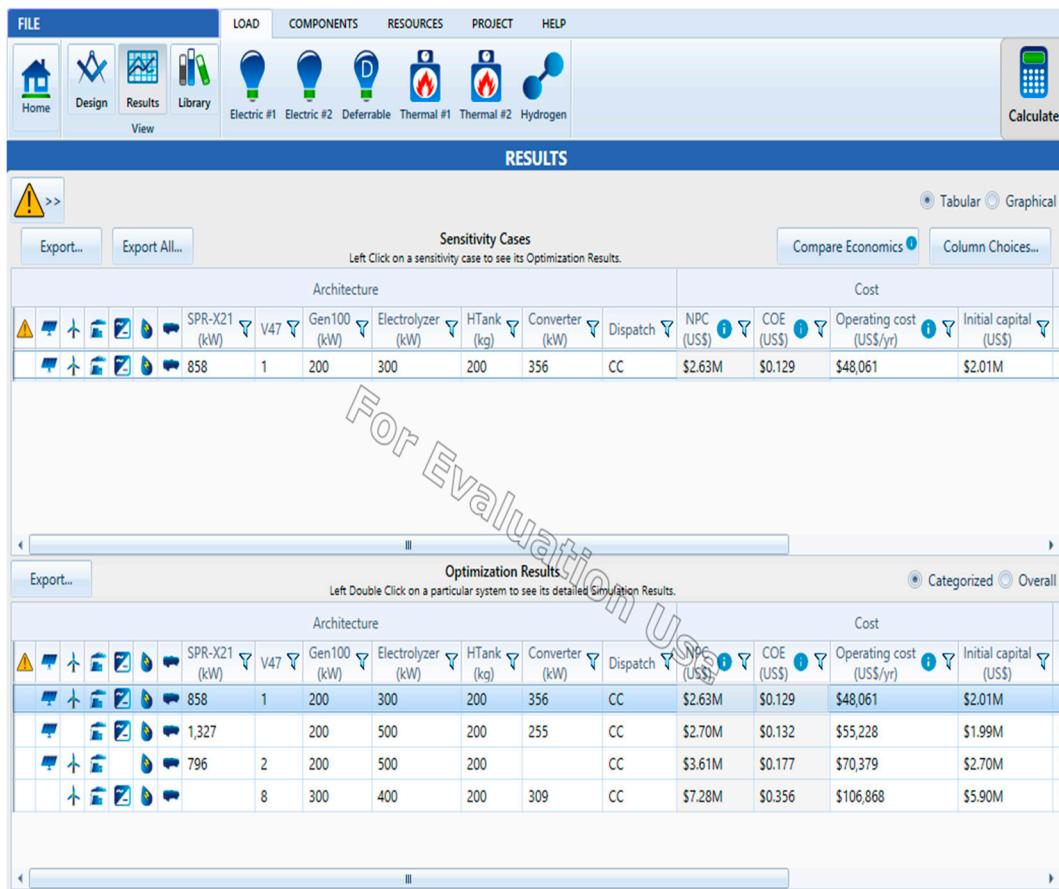


Figure B.2.2. HOMER Results

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