19

21

23

32

Disclaimer/Publisher's Note: The statements, opinions, and data contained in all publications are solely those of the individual author(s) and contributor(s) and not of MDPI and/or the editor(s). MDPI and/or the editor(s) disclaim responsibility for any injury to people or property resulting from any ideas, methods, instructions, or products referred to in the content.

Article

Laser-Metal Interaction with a Pulse Shorter the Ion Period: Ablation Threshold, Electrons Emission and Ions Explosion

Eugene G. Gamaly^{1*} and Saulius Juodkazis ^{2,3}

- Laser Physics Centre, Department of Quantum Science and Technology, Research School of Physics, The Australian National University, Canberra ACT 2601, Australia; eugene.gamaly@anu.edu.au
- Optical Sciences Centre and ARC Training Centre in Surface Engineering for Advanced Materials (SEAM), School of Science, Swinburne University of Technology, Hawthorn, Victoria 3122, Australia; sjuodkazis@swin.edu.au
- WRH Program International Research Frontiers Initiative (IRFI) Tokyo Institute of Technology, Nagatsuta-cho, Midori-ku, Yokohama, Kanagawa 226-8503 Japan
- * Correspondence: E.G.G. eugene.gamaly@anu.edu.au

Abstract: Laser energy per unit surface, necessary to trigger the material removal, decreases with the pulse shortening becoming the pulse-time independent in the sub-picosecond range. These pulses are shorter the electron-to-ion energy transfer time and electronic heat conduction time minimizing the energy losses. The electrons receiving the energy larger than the threshold, drag the ions off the surface in the mode of electrostatic ablation. We show that the pulse shorter than the ion period (Shorter-the-Limit (StL)) ejects conduction electrons with the energy larger than the work function (from a metal) leaving the bare ions immobile in a few atomic layers. The electrons emission is followed by the bare ion's explosion, ablation, and THz radiation from expanding plasma. We compare this phenomenon to the classic photo effect, nanocluster Coulomb explosions, show differences and consider possibilities for detecting the new mode of ablation experimentally by emitted THz radiation and consider applications of high-precision nano-machining with this low intensity irradiation.

Keywords: ultra-short laser pulses; laser pulses shorter than the ion period; non-equilibrium ablation; Coulomb explosion; micromachining; THz emission

1. Introduction

The Coulomb forces are entirely responsible for the keeping the solid intact. Quantum effects in solids significantly modify the Coulomb interactions. In the unperturbed metal the conduction electrons' wave functions are periodic (Bloch waves) allowing the conductivity electrons propagate through a metal being not affected by the ions' cores attraction. Intense ($\sim 10^{14}~\rm W/cm^2)$ sub-picosecond laser pulse excites electrons while the ions cores remain unperturbed. The conductivity electrons oscillate with the energy comparable to the Fermi energy, violating the Braggs conditions, destroying the Bloch wave function, and converting a metal into plasma. The multi-particle Coulomb interaction between electrons and ions is restored during the time depending on the electron-to-ion mass ratio. This time is in a range from few fs to a few tens of femtosecond depending on ion's mass.

Sub-picosecond pulse duration (from few tens of picoseconds to few tens of femtoseconds) is shorter than the electron-to-ion energy transfer time and electronic heat conduction time. It is established experimentally [1,2] that the energy density per unit area triggering the material ejection (threshold fluence) does not depend on the pulse duration. The analysis shows that the collective electrostatic field of hot electrons drags cold ions off the skin layer of laser-excited solid [3]. The electron's energy is proportional to the absorbed energy per unit surface. The threshold achieved when the absorbed energy per electron in the outmost surface layer is equal to the sum of the work function of electron and the

37

41

43

45

48

54

62

75

cohesion energy of atom. The calculated threshold coincides well with the measured data. Hence, it is obvious that the laser-matter interaction in this mode occurs during the longer time than necessary for the collective electrostatic field restoration.

The subject of this paper is the analysis of the laser-metal interaction with a pulse duration shorter than that necessary for the collective electrostatic field restoration. First, we identify the limit of the restoration time in a solid and in plasma. Then, we analyse the electrostatic ablation mode and compare it to the shorter-the-limit (StL) pulse-metal interaction. The laser excited conduction electrons in this mode have no time to affect the ion's cores. Therefore, an electron getting energy larger than the work function leaves the surface with the kinetic energy, $\epsilon_{kin} = \epsilon_e - w_e$, like in the classical photo-effect (ϵ_e is the energy of electron and w_e is its work function; Fig. 1).

However, in the Millikan's experiments [4] (Nobel's prize 1923) the intensity of the UV photons, $\hbar\omega > w_e$ (the energy of photons per unit surface/unit time) was very low $10^{-7} - 10^{-3}$ W/cm². Hence a photon interacted with electron as a particle swiftly knocking it off the potential well, the work function's deep. The number density of affected ions was much lower the initial density, ions' spatial separation very big preventing any ion/ion interaction. The long interaction time (minutes) allowed the weak electric currents from the bulk of metal restoring the neutrality.

Unlike the photo-effect, during more intense StL-metal interaction the electrons get energy larger than work function from flow of photons, as electro-magnetic wave, at, $\hbar\omega \ll w_e$, while the unperturbed positively charged ions remain immobile inside a few close-to-surface atomic layers during the interaction time shorter than that necessary for restoring the collective Coulomb force of ions. After the end of the pulse the joint electric field of the positive charges ejects the surface ions. The acceleration of ions (proportional to the surface charge density) exceeds that of electrostatic ablation by two orders of magnitude. The electrons emission is followed by the ions' explosion, ablation, and THz radiation from the expanding plasma. We discuss the experiments for the possible verification of the STL pulses action and consider applications of the high precision nano/ micro-machining.

2. Hierarchy of the time scales in the electron-ion interactions

There are two domains of the electron-ion Coulomb interactions. First domain includes particle-to-particle collisions of momentum and energy exchange in plasma. Second group deals with the collective electrons-ions interactions in plasma and solids when a particle is under the action of multiple fields of surrounding positive/negative charges.

Time scales in plasma are straightforward. The shortest is the electron-electron (e-e) and electron-ion (e-i) momentum exchange time, $t_m = \nu_{ei}^{-1} \propto \frac{e_e^{3/2}}{n_e} > \omega_{pe}^{-1}$, where ν_{ei} is the frequency of e-i collisions, n_e the electrons' number density, and ω_{pe} is the electron plasma frequency. Maximum momentum exchange rate is around electron plasma frequency. Hence the momentum exchange time is around ~ 0.1 fs for the solid density plasma. The energy exchange time is larger on the ratio of ion mass M_{ion} to the electron mass m_e : $t_m = \nu_{ei}^{-1} \frac{M_{ion}}{m_e}$. It is of a few-ps range for the mass ratio of 10^5 . We start with the collective interactions in plasma where physics is straightforward.

2.1. Time scales for the electron-ion collective coupling in plasma

In the cold, non-magnetic quasi-neutral plasma (equal number of positive and negative charges) on each charge always acts an unbalanced force from the neighbours making any charge moving and therefore the electrons density fluctuating (direct consequence of the Gauss theorem). The sum of electro-static fields forces the electrons oscillate with the electron plasma frequency, $\omega_{pe}^2 = (4\pi e^2 n_e)/m_e$ after the time, $t_{C,e} \approx \omega_{pe}^{-1}$; in SI units $\omega_{pe}^2 = e^2 n_e/(\varepsilon_0 m_e)$ with $\varepsilon_0 \equiv \frac{1}{\mu_0 c^2}$. Thus, the electrons start oscillating after the time, $t_{C,e}$,

Conversion between proportionality constants of the Coulomb's force acting on separated electric charges and magnetic force between currents is $2k_{el} = c^2 k_{mag}$, where the electric and magnetic constants $k_{el,mag}$ depend on definition (units) of charge and current, respectively, $k_{el} = 1$ (CGS) and $k_{el} = \frac{\mu_0 c^2}{4\pi}$ (SI).

93

100

103

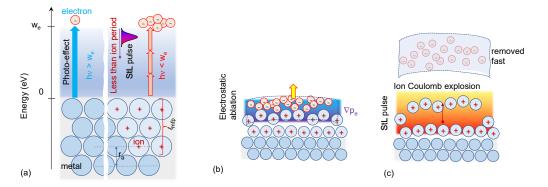


Figure 1. The schemes of the different interaction regimes. (a) Left: knock off electron by single UV photon in classic photo-effect; Right: absorption of the multiple photons of StL laser pulse followed by an electron ejection. (b) In electrostatic ablation, the ions are driven by the gradient of the electronic pressure, ∇p_e . (c) In StL interaction mode the ions are driven by the Coulomb repulsion layer by layer with the outmost surface layer moving first and fastest. The energy scale is the work function, w_e ; the space scales are the mean free path of an electron, l_{mfp} , and inter-atomic distance, r_a .

from the moment the electronic plasma is instantaneously created ($\sim 10^{-16}$ s). The sum of the electro-static fields of the oscillating electrons forces heavy ions oscillating with the ions' plasma frequency, $\omega_{pi}^2 = (4\pi e^2 n_e)/M_i$. The time when the Coulomb fields of the multiple electrons starts affecting the ions is $t_{C,i} \approx \omega_{pi}^{-1} = t_{C,e} \sqrt{M_i/m_e}$ ($\sim 10^{-14}$ s). Electron plasma frequency from Al to Ag is in a range $(1.97-1.21)\times 10^{16}$ s⁻¹ making the time when ion's motion begins, $t_{C,i} \approx (0.5-0.82)\times 10^{-16} \sqrt{M_i/m_e}$ [s].

2.2. Time for the perturbation of ion core positions in a cold solid

At zero approximation the ions are assumed immobile, and electrons are moving in the Coulomb field of the stationary ions. The full energy of a solid (nonrelativistic Hamiltonian in the quantum treatment) includes the kinetic energy of electrons and ions, electron-electron and ion-ion Coulomb interaction, and electron-ion interactions [5]. The effective potential energy as well as the energy of the Coulomb interaction between the nuclei in equilibrium approximates well by the energy of two charges interaction, $U_0 \approx \frac{e^2}{2r_B} = \frac{m_e e^4}{2\hbar^2}$, here r_B is the Bohr radius. The ion core motion under the action of the electron's Coulomb field in a cold solid can be considered as a perturbation. It is the second term in the expansion of the core's potential energy into the series on the deviation of ion core's position from the equilibrium, δR . The expansion of the potential near the equilibrium reads:

$$U = U_0 + \delta U_0 \approx U_0 + \frac{1}{2} \frac{\partial^2 U(R)}{\partial R^2} \delta R^2. \tag{1}$$

The second term is the potential energy of nucleus oscillations:

$$\delta U_0 \approx \frac{U_0 \delta R^2}{2r_R^2}.$$
 (2)

The minimum momentum of a nucleus estimates from the uncertainty relations, $p_i \geq \hbar/\delta R$. Then the ion's kinetic energy follows, $p_i^2/2M_i \geq \hbar^2/(2M_i\delta R^2)$. Equalising the potential energy to the kinetic energy of the core (the Virial theorem) one obtains the nucleus displacement, $\delta R \approx (2m/M_i)^{1/4} \times r_B$. Hence the ions energy increase from Eqn. 2 is:

$$\delta U_0 = \epsilon_{ion} \approx \frac{U_0}{2} \sqrt{\frac{2m_e}{M_i}}.$$
 (3)

130

The minimum time when ion starts moving after receiving the energy from the electrons Coulomb field follows from the uncertainty relation:

$$t_{ion} pprox rac{\hbar}{\epsilon_{ion}} = rac{\sqrt{2}\hbar}{U_0} \sqrt{rac{M_i}{m_e}} = \sqrt{2}t_{at} \sqrt{rac{M_i}{m_e}},$$
 (4)

here, the characteristic atomic time is, $t_{at} = \hbar/U_0 = 0.48 \times 10^{-16}$ [s] for $U_0 = 13.6$ eV. Thus, $t_{ion} \approx \sqrt{\frac{M_i}{m_e}} \times 0.68 \times 10^{-16}$ [s]. This estimate based only on the fundamental constants and mass ratio. Therefore, it sets the minimum time for electron affect an ion by its electric field in a solid.

One can see the proximity of this result to the estimate for the solid density plasma, $t_{C,i} \approx (0.5-0.82) \times 10^{-16} \sqrt{\frac{M_i}{m_e}}$ [s]. In plasma this time depends on the electrons number density explicitly reflecting the collective nature of the effect that is in the above estimate implicit. It is legitimate assuming that in a shorter time the sum of forces of chaotically directed fields of the multiple charges do not build yet, i.e., ions are not moving. Hence the electrons excited during the period shorter than $t_{C,i}$ have not interacting with the core ions.

3. Ablation of metal by different pulses: long (electrostatic mode) and short (StL mode)

Let us compare the ablation of a metal in two different experiments by two pulses (both shorter the electron-to-ion energy transfer time) of different duration delivering the same energy per pulse at the same focal spot (same fluence). The longer pulse interacts in the regime of electrostatic ablation, while the shorter pulse ablates the same metal in the StL interaction mode. The electron temperature distribution in the skin layer depends on the absorbed fluence. The number of conduction electrons remains practically unchanged in the considered intensity range. Therefore, assumption that the absorption coefficient and skin length at two different intensities is approximately the same is reasonable. The processes in the considered experiments depend only on the ablation mode (pulse duration). The pulses are of the high contrast (no pre-plasma, step-like density gradient to the end of the pulse) incident along the normal to the surface. The laser energy is absorbed on the conduction electrons in the skin layer. Solution of 1D Maxwell equation in a metal allows calculation of absorbed energy density through the Poynting vector. Then, from the energy equation for electrons follows the electron energy space and time dependence in the form:

$$\epsilon_e(x,t) = \epsilon_e(0,t) \times e^{-\frac{2x}{l_s}},$$
 (5)

where $\epsilon_e(0,t) = \frac{2A}{n_e l_s} F(0,t)$ and the fluence is a time integral of intensity $F(0,t) = \int_0^t I(0,\tau) d\tau$. 132 Here A is the Fresnel absorption coefficient (ratio of the absorbed to the incident energy), l_s 133 is the skin length (for E-field), n_e is the electron number density (see details in Appendix). 134

3.1. Electrostatic ablation

Pulse duration for the electrostatic ablation should be in a range, $t_{C,i} < t_{pulse} < t_{ei}^{en}$, larger than that for building the collective Coulomb force and much less the electron-to-ion energy transfer time. Electrostatic ablation of metal surface has been experimentally verified by 15 fs laser pulses [6]. The threshold fluence from Eqn. 5 is defined as the electron energy necessary for removal of ion from the outmost surface layer. This energy equals to the sum of the cohesion energy and work function, $\epsilon_e(0,t_p)=\epsilon_b+w_e$. The threshold for metals, $F_{th}(0,t_p)=\frac{(\epsilon_b+w_e)n_el_s}{2A}$, agrees well with the measurements [1,2]. Let us define the ablation depth l_{abl} from the similar condition, $\epsilon_e(l_{abl},t_p)=\epsilon_b+w_e$. Then the energy of electron in the outmost surface layer is $\epsilon_e(0,t_p)=(\epsilon_b+w_e)e^2$ as well as the incident laser fluence $F=e^2F_{th}(0,t_p)$; e=2.71 is the Napier's number.

155

156

157

164

168

181

The momentum equations for electrons and ions are the following:

$$m_e \frac{\partial v_e}{\partial t} = eE_{elst} + \frac{1}{n_e} \nabla p_e, \tag{6}$$

$$M_i \frac{\partial v_i}{\partial t} = e E_{elst}, \tag{7}$$

where p_e is the electron pressure. Here the electric field is the coarse-grained field associated with the collective interaction of plasma charges [7]. In considering the ions motion the electron's inertia can be ignored, $n_e e E_{elst} \approx -\nabla p_e$. The collective action of hot electrons drives the cold ions motion off the metal:

$$M_i \frac{\partial v_i}{\partial t} = eE_{elst} = -\nabla \epsilon_e = \frac{2\epsilon_e}{l_s}.$$
 (8)

Electronic heat conduction smoothing the gradient well after the end of the pulse. The cooling time, when the gradient along with the ions acceleration goes to zero, is $t_{cool} = l_s^2/D_{heat}$ where the diffusion coefficient is defined by the e-i momentum exchange rate v_{ei}^{mom} as $D_{heat} = v_e^2/[3v_{ei}^{mom}]$. It is in picoseconds range. Thus, the number of ablated ions (focal area is known), their acceleration and final velocity can be calculated.

3.2. Ultra-short pulse $t_{C,i} > t_{pulse}$ interaction

Let us now consider much shorter pulse, $t_{C,i} > t_{pulse}$, interaction with the same metal and the same absorbed surface energy density. The electrons energy space distribution created by the long and short pulse is the same. Now, the conduction electrons can get the energy larger the work function during the period shorter that necessary for building the link to ions. The state is very similar to that in the classical photo-effect with the difference that this state has been created by the multiple photon's absorption by electrons (Fig. 1). The electrons in a few atomic layers at the distance of the electronic mean free path from the metal-vacuum boundary can escape a metal with the kinetic energy, $\epsilon_{kin} = \epsilon_e - w_e$, leaving N atomic layers with the positively charged ions. This number equals to the electron's mean free path by the atomic monolayer thickness, $N = l_{mfp}/r_a$. The focal spot area, S_f , with the depth, l_{mfp} , atomic number density, n_a , became positively charged with the surface charge density, $\sigma = en_a N \times r_a$ (Fig. 1). In accord to electrostatics [8] the charged thin infinite plate creates the equal electric fields perpendicular to the plane in the positive and negative directions. Each field is proportional to the surface charge density, $E_{els} = 2\pi\sigma$. Thus, the single charged ion of mass M_i is under action of this force pulling ion off:

$$\frac{dv_{ion}}{dt} = 2\pi e^2 n_a N \times \frac{r_a}{M_i} = N\omega_{pi}^2 r_a / 2. \tag{9}$$

Note, that maximum acceleration of two repelling ions (at the small displacements, $\zeta \ll r_a$ equals to $\omega_{pi}^2 r_a/3$ [9], while in the ideal case of electrostatic charged plate acceleration is constant in space. The acceleration by charged plate is enhanced by the multiple contribution of the surface charges. However, the acceleration is not constant in space in the reality. The force has a maximum in the central part of the focal spot decreasing with the distance to the focal boundary.

For the finite plate and in plasma the space scale, where this acceleration is reasonable to consider constant, must be much less the size of the plate (focal spot). Taking conservatively this scale as r_a one gets the maximum velocity as, $v_{i,max} \approx \sqrt{N\omega_{pi}^2 r_a^2}$. For Ag ($\omega_{pi} = 2.53 \times 10^{13} \text{ s}^{-1}$, $r_a = 1.59 \times 10^{-8} \text{ cm}$, $N \sim 9$) the velocity range is $v_{i,max} = (12-4) \times 10^5 \text{ cm/s}$; and the acceleration range $(5-0.45) \times 10^{19} \text{ cm/s}^2$, orders of magnitude larger than in electrostatic ablation.

Hence there are few major differences with the electrostatic ablation. First, part of electrons is ejected most probably isotropic. Second, part of bare ions is accelerated by the Coulomb repulsion with acceleration couple of orders of magnitude higher than during

198

201

202

210

218

222

224

225

227

the electrostatic ablation. Third, the ablation threshold reached at the electron's energy slightly above the work function making electrons from couple of the outmost surface layer to leave letting an ion to be repulsed.

4. Radiation from the ablated plasma

The ablated plasma is a current flowing mainly perpendicular to the sample surface decelerating slowly before attending the constant velocity. Let us compare the radiation of plasma flow in two ablation modes. We consider ablation of Ag target with the same incident (and absorbed) surface energy density producing the identical space energy distribution and ablation depth equal to the skin depth. The total number of ablating particles in both cases is the same. However, in the case of StL pulse there are two groups of ions with different accelerations.

4.1. Radiation from the electrostatically ablated plasma

Frequency spectrum and total power of radiation emitted by the time-dependent current depends on the full number of emitting charges, their acceleration, and its duration. Ag ions' acceleration in the electrostatic ablation mode is, $\frac{\partial v_i}{\partial t} = \frac{2\epsilon_\ell}{M_i l_s} = 2.3 \times 10^{17} \text{ cm/s}^2$ while the number of ablated ions constitutes, $N_{abl} = 2.5 \times 10^{11}$ ions (see Appendix for details).

The Fourier transform of the time-dependent current defines the frequency spectrum of the emitted radiation: $\mathbf{j}_{\omega} = \int \mathbf{j}(t)e^{i\omega t}dt$. The acceleration of ions decreases because the electronic heat conduction leads to the flattening the electronic pressure gradient. The acceleration decreases from the maximum to zero due to the skin layer cooling, the characteristic time, $T \sim 1$ ps and inverse is a characteristic frequency of emitted radiation ~ 1 THz. The direction of the emission is perpendicular to the direction of nonrelativistic acceleration. The power of the radiation emitted by the current is given by the Larmor formula [10]:

$$P = \frac{2}{3c^3}(\ddot{d})^2,\tag{10}$$

here $\ddot{d} = \sum e\dot{v}$ is the sum taken over all dipoles' acceleration \dot{v} in the current. The power of the emitted radiation is proportional to the square of the particles number and their deceleration. One can estimate the total energy emitted by the current as the following:

$$\epsilon_{Rad} = T \times P \approx \frac{2T}{3c^3} \left(eN_{abl} \frac{dv_i}{dt} \right)^2.$$
 (11)

Taking acceleration 2.3×10^{17} cm/s², $N_{abl} = 2.5 \times 10^{11}$ ions, $T \sim 10^{-12}$ s one gets total energy of radiation 1.88×10^{-12} J (the power of 1.88 W). Hence, the ratio of the total emitted energy to laser energy of 3 μ J constitutes $\sim 6 \times 10^{-7}$.

4.2. Radiation from the plasma ablated by StL pulse

The total number of ablated atoms remains the same. However, the structure of the plasma outflow is different. First, the electrons from a few atomic layers with thickness of electronic mean free path are moving out. Then the bare ions abandoned by electrons are expelled by repulsion. Finally, the bulk of the ablated material are removed with low velocity and the features like considered in the previous paragraph.

The number of ions in layers from where electron escaped is $N_{exp} = (l_{mfp}/l_s)N_{abl} \sim 7.5 \times 10^9$. The mean free path of an electron $l_{mfp} = \nu_e/\nu_{ei}^{mom} \sim 1.48 \times 10^{-7}$ cm extends to 9 monolayers. The electrons from these layers are emitted during the STL pulse. The removal of ions by repulsion occurs layer by layer with gradually decreasing acceleration in accord with diminishing number of layers:

$$\frac{dv_{ion}}{dt} = N\omega_{pi}^2 r_a/2. \tag{12}$$

252

For Ag, the acceleration range of exploding ions is $10^{19}-10^{20}$ cm/s², while the velocity range is $v_{i,max}=(12-4)\times 10^5$ cm/s. The time for reaching the constant velocity of expansion is a few hundred fs (100-400 fs). Therefore, the frequency of radiation is in a range (10-2.5) THz. Now estimates for the power and total energy of radiation are straightforward by Eqs. 10-11: P=(3.2-320) W, the total energy (taking $T=2.5\times 10^{-13}$ s) is around 2.5×10^{-11} J. Hence, only 3% of ablated ions emit by the order of magnitude larger energy in a bit higher frequency range. The plasma plume produced by the StL pulse contains major part of slow ions emitting less than 10% radiation in THz range. About \sim 3% of total ablated fast ions emit the major radiation in a slightly higher frequency range. Two radiation peaks of different height are separated in time.

5. Discussion and conclusion

The non-relativistic StL laser pulse (ponderomotive potential 10-20 eV) excites free electrons in the conduction band of metal during the time shorter that for restoring electronion Coulomb coupling. Excited electrons escape from a few close to surface atomic layers after getting energy larger the work function. These layers become positively charged creating electrostatic field perpendicular to the surface accelerating and ejecting ions by the Coulomb explosion. Let's discuss the proximity and difference of this phenomenon to the classic photo effect and the Coulomb explosion of nanoclusters.

In the classic photo-effect, the UV photon with the energy larger the work function knocks the conduction electron off the surface in the single photon-electron collision (Fig. 1). To consider a photon as a quantum particle the number of photons per cube of photons wavelength should be less than one [11]. The intensity in the Millikan's experiments [4] has been in a range $10^{-7} - 10^{-3}$ W/cm² well in accord with the above criterion leaving the rest of conduction electrons in a free state (not affected by the ions cores). Therefore, an electron after collision escaped the metal with the kinetic energy in accord to the Einstein formula $\epsilon_{kin} = \hbar \omega - w_e$.

In the StL pulse-metal interaction the high-frequency laser field convert electrons into plasma state thus destroying free electron-ion core relations of metal in contrast to the classic photo-effect. However, an electron absorbs energy during the period shorter that needed for the restoration of the collective electron-ion coupling. The electron which received energy more than the work function escapes a metal not being affected by ions cores due to the extremely rapid nature of interaction. Ions in a few atomic layers left immobile and charged. Then the Coulomb repulsion drives ions out of metal.

The phenomenon of the Coulomb explosion of small [12] and large molecules [13] and nanoclusters [14–16] has been studied more than three decades. The relativistic laser beam with the ponderomotive potential around MeV ionises nanocluster up to several electrons per atom. Electrons are accelerated and swiftly ejected from a cluster with the energy comparable to the ponderomotive potential leaving ions immobile and positively charged. The cluster acquires a big total positive charge resulting in the Coulomb explosion. Kinetic energy of exploded ions reaches MeV depending on the total charge of the cluster. Recent studies provides new insights into ablation at ultra-relativistic intensities showing a steplike electrostatic potential which drives disassembly of the solid [17]. In the StLmetal interaction the similar events develop on the much smaller energy scale and on the similar short time scale. The laser ejected electrons are followed by fast ions (few percent) accelerated by explosion and followed by the slow ions of conventional ablation. Analysis shows that ablated flow of fast ions is much intense source of THz radiation than that of slow current. Using the light metals (like Al) and energetic lasers one can create StL-pulse-generated point source of THz radiation (controlled by choice of metal, pulse duration, laser energy, focal spot size).

Summing up the presented analysis suggests that the intense laser pulse with duration less than the ion period (few tens fs) is capable swiftly eject the conduction electrons from a few near-surface atomic layers followed by the flow of energetic ions ejected by the Coulomb repulsion and emission of THz radiation. As it follows from the above in this

293

304

311

313

interaction regime (StL) is possible to remove a few atomic layers from a metal by the action of a single laser pulse (see Sec. H). The number of the atomic layers removed by explosion, i.e., the electron's mean free path, is controlled by the absorbed surface energy density delivered by laser. Indeed, mean free path of electron in the Coulomb collisions is, $l_{mfp} \propto \epsilon_e^2$, while $\epsilon_e \propto F$. For experimental realisation and monitoring the StL pulse ablation, detection of THz emission reported for generation of single-cycle circularly polarised pulses under 40 fs pulsed irradiation of water micro-flow [18] can be used.

Appendix A Classical photo-effect

In the Millikan's experiments (1916) photo effect has been induced by UV radiation of the mercury discharge. Intensity at 365 nm (3.4 eV) was $10-10^4$ erg/cm²s ($10^{-7}-10^{-3}$ W/cm²). Flow of photons maximum was 1.8×10^{15} photons/cm²/s. UV photon swiftly knocks electron out of the surface layer. Positive charges are equalising by the slow currents from the bulk. The quantum description of the photon as a particle is necessary when the number density of photons is less one photon per cubic of photon's wavelength [11].

Appendix B Properties of metals at room temperature

Conduction electrons density n_e is in 10^{23} cm $^{-3}$, inter atomic distance, $r_a = (4\pi n_e/3)^{-1/3}$ in 10^{-8} cm (Å), plasma frequency in 10^{16} s $^{-1}$, effective electron's mass is in units of free electron mass. Ion frequency: Ag, $m_e/M_i = 5.08^{-6}$, $\omega_{vi} = 2.53 \times 10^{13}$ s $^{-1}$ ($t_{Ci} = 36.7$ fs).

Metal:	n_e	M_i	r_a	ω_{pe}	m_{ef}	C_e	ϵ_F	ϵ_b	$ w_e $
units	10^{23} cm^{-3}	at.mass	Å	$10^{16} \mathrm{s}^{-1}$	m_e	$\frac{3}{2}k_B$	eV	eV	eV; (max)
Al	1.806	26.982	1.09	1.97	1.48	0.46	11.63	3.065	4.2; (100)-plane
Cu	0.845	63.546	1.41	1.395	1.38	0.70	7.0	3.173	4.48-4.98
Au	0.59	196.97	1.38	1.126	1.14	0.69	5.52	3.81	5.47; (100)-plane
Ag	0.585	107.86	1.59	1.121	1.0	0.79	5.48	2.95	4.52-4.74

Table A1. Parameters of metals which can be used for experiments with StL pulses. The maximum value of w_e is shown and for which crystallographic plane [19].

The electron heat capacity is estimated from $C_e \approx \frac{3}{2}k_BT_e(2x-x^2)$, where $x=k_BT_e/\epsilon_F$ attains the ideal gas value at x=1 [20]; the Fermi energy ϵ_F . The electron heat capacity near the ablation threshold $k_BT_e=\epsilon_b$, where ϵ_b is the binding energy defined as the potential barrier against free motion of atoms through the solid. For example, for Au $\epsilon_b=3.81\,\mathrm{eV/atom}$ (the cohesive energy per atom), $\epsilon_F=5.52\,\mathrm{eV}$, $x\approx\epsilon_b/\epsilon_F=0.69$ and $C_e=1.355\,\mathrm{[k_B]}$, close to 1.5 as for the ideal gas.

Appendix C Optical properties of the electronic plasma

The Drude-like dielectric permittivity reads [20]:

$$\varepsilon_{re} = 1 - \frac{\omega_{pe}^2}{\omega^2 + \nu_{ei}^2}, \quad \varepsilon_{im} = \frac{\omega_{pe}^2}{\omega^2 + \nu_{ei}^2} \times \frac{\nu_{ei}}{\omega}, \tag{A1}$$

and is related to the real and imaginary parts of the complex refractive index $\tilde{n} \equiv n + i\kappa$ via $\varepsilon_{re} = n^2 - \kappa^2$ and $\varepsilon_{im} = 2n\kappa$; $\kappa^2 = (|\varepsilon_{re}| - \varepsilon_{re})/2$ and $n^2 = (|\varepsilon_{re}| + \varepsilon_{re})/2$, where the complex modulus $|\varepsilon_{re}| = \sqrt{\varepsilon_{re}^2 + \varepsilon_{im}^2}$. The Fresnel absorption coefficient reads $A = \frac{4n}{(n+1)^2 + \kappa^2}$.

Electron-ion momentum and energy transfer rates. Near the maximum it defines as, $v_{ei} \approx v_e/r_a$. Taking the electron velocity on the atomic scale, 2×10^8 cm/s, one gets the rate of the order of the electron plasma frequency. We consider conditions when electrons energy is of the same order of magnitude as the Coulomb energy and Fermi energy. The plasma is

326

328

330

331

332

334

337

338

non-ideal, unscreened and collision rate decreases. Cauble and Rozmus predicted [21] that in the solid density non-ideal plasma the e-i collision rate estimates as the following:

$$v_{ei}^{mom} \approx \omega_{ei} \frac{\ln \Lambda}{10N_D},\tag{A2}$$

where the logarithm $\ln \Lambda$ and the number of particles in the Debye sphere N_D for the ideal plasma are [7]:

$$\Lambda \approx (9N_D)/Z, \ \ N_D = 1.7 \times 10^9 \sqrt{\theta_e^3/n_e},$$
 (A3)

where θ_e is the electron temperature, Z is the charge state. Taking $\epsilon_e=10$ eV and $n_e=0.585\times 10^{23}~{\rm cm}^{-3}$ (Ag), one obtains $\Lambda=2$ (the ref. [10] gives 0.69), $N_D=0.22$ and $\nu_{ei}^{mom}\approx 0.3\omega_{ei}\sim 3\times 10^{15}~{\rm s}^{-1}$.

The electron-to-ions energy transfer time is, $t_{ei}^{en} = \left[v_{ei}^{mom} \times \frac{m_e}{M_i}\right]^{-1}$; for Ag, it is 65 ps.

At $\omega=1.88\times10^{15}~\rm s^{-1}$ (wavelength of 1002 nm), $\omega_{pe}=1.21\times10^{16}~\rm s^{-1}$, $\nu_{ei}^{mom}\approx3\times10^{15}~\rm s^{-1}$, one gets $\varepsilon_{im}=16$ and $\varepsilon_{re}=-9$, i.e., n=2.16, $\kappa=3.7$ and A=0.365; the skin depth $l_s=43$ nm; the constant $C_0=\frac{2A}{n_e l_s}=3\times10^{-18}~\rm cm^2$ is used in calculation of electron energy (see below).

Oscillation energy (ponderomotive potential) is given by [22]: $\varepsilon_{osc} = 9.375(1 + \alpha^2) \times \frac{I}{10^{14} \; [\text{W/cm}^2]} \times \lambda_{\mu\text{m}}^2 \; [\text{eV}]$; here $\alpha = \pm 1$ for circular polarisation and $\alpha = 0$ for linear polarisation. Intensity I is averaged over many laser pulse periods.

Appendix D The electron's energy space and time dependence in the skin layer

The electron's energy time/space dependence in the skin layer (normal skin) in 1D approximation follows from the energy equation under assumption that the electron's density and optical properties are time/space independent, and the pulse duration is much shorter the electron-to-ions energy transfer time, $t_{ei}^{en} = \left[v_{ei}^{mom} \times \frac{m_e}{M_i}\right]^{-1}$. The electrons contain all the absorbed energy. Energy equation for electrons (no losses) is:

$$n_e \frac{\partial \epsilon_e}{\partial t} = Q_{abs}(x, t). \tag{A4}$$

Here the absorbed energy density reads:

$$Q_{abs}(x,t) = \frac{2AI(t,0)}{l_s} e^{-2x/l_s} \text{ [W/cm}^3].$$
 (A5)

The Fresnel absorption coefficient A and skin depth l_s are the following:

$$\frac{2A}{l_s} = \frac{4\omega\varepsilon_{im}}{c \times |1 + \sqrt{\varepsilon}|^2}, \quad l_s = \frac{c}{\omega\kappa},\tag{A6}$$

c is the speed of light. Integration the electron energy equation by time gives the electron energy:

$$\epsilon_e(x,t) = C_0 \times F(0,t) \times e^{-2x/l_s},$$
(A7)

where $C_0 = \frac{2A}{n_e l_s}$, $F(0,t) = \int_0^t I(0,\tau) d\tau$. Threshold for Ag $\epsilon_e(0) = \epsilon_b + w_e = 7.5$ eV at wavelength $\lambda = 1 \ \mu$ m, has fluence $F_{th} = 0.4 \ \mathrm{J/cm^2}$.

Appendix E Electrostatic Ablation of Ag

Ablation depth, number of ablated atoms, cooling time for the skin layer for Ag target. For, $F=7.39\times F_{th}=2.96~\mathrm{J/cm^2}$ at laser pulse energy $\sim 3~\mu\mathrm{J}$, $\epsilon_e(0)=55.8~\mathrm{eV}$, $v_e=34.43\times 10^8~\mathrm{cm/s}$, ablation depth $x_{abl}=\frac{l_s}{2}\ln\left[\frac{\epsilon_e}{\epsilon_b+w_e}\right]$ equals to l_s . The ablation volume assuming $S_{foc}=10^{-6}~\mathrm{cm^2}$ is $V_{abl}=4.3\times 10^{-12}~\mathrm{cm^3}$, $N_{abl}=2.5\times 10^{11}~\mathrm{ions}~v_{ei}^{mom}\approx34.5$

363

370

376

379

381

383

 $0.3\omega_{ei}\sim 3\times 10^{15}~{
m s}^{-1}$. Heat diffusion coefficient for Ag $D_{heat}=v_e^{2/3}v_{ei}^{mom}=21.8~{
m cm}^2/{
m s}$, cooling time $t_{cool}=l_s^2/D_{heat}=0.85~{
m ps}$. The ions removal from these layers occurs under the electrostatic force of hot electrons acting as a gradient of the electronic energy.

Electrostatic ablated Ag ions' acceleration. $\frac{\partial v_i}{\partial t} = \frac{2\epsilon_e}{M_i l_s} = 2.3 \times 10^{17} \, \mathrm{cm/s^2}$ (for $\epsilon_e = 55.8 \, \mathrm{eV}$, $l_s = 43 \, \mathrm{nm}$, $M_i = 107.86$). The average electrons' velocity is around $10^8 \, \mathrm{cm/s}$ and the motion of electrons is chaotic after a few electron-electron collisions. The ions motion is directional (along the electron pressure gradient when exciting beam is at the normal to the target surface). Thus, for the Gauss intensity distribution across the focal spot, the main current is directed at the normal at ions' velocity more than two orders of magnitude lower than that of electrons.

Appendix F Radiation from the ablated plasma

Unit vector along the current is \mathbf{r} , direction to the detector located at the distance R_0 , is \mathbf{n} . The size of the emitter, r, is much smaller than the distance to observation, $r \ll R_0$. The emitted wave arrives at detector as a plane wave. The vector potential of the emitted field reads:

$$\mathbf{A} = \frac{1}{cR_0} \int \mathbf{j} \times dV. \tag{A8}$$

The polarisation of the emitted field depends on the mutual directions of the current and the direction to the observation point:

$$\mathbf{H} = \left(\frac{d\mathbf{A}}{dt} \times \mathbf{n}\right)/c, \quad \mathbf{E} = \left[\left(\frac{d\mathbf{A}}{dt} \times \mathbf{n}\right) \times \mathbf{n}\right]/c, \tag{A9}$$

where \times is the sign of the vector product. Power of the emitted radiation at the observation point located at the distance, R_0 , into the unit of the solid angle Ω is $dI = \left(\frac{cE^2}{4\pi}\right)R_0^2d\Omega$. Distance from the source to the measurement point is larger than the wavelength of emitted radiation and much larger than the size of the source.

Radiation of the ablated ion current. Estimate of the vector potential for the ablation case:

$$\mathbf{A} \approx \frac{1}{cR_0} eZ N_{abl} \mathbf{v}_i, \tag{A10}$$

here $N_{abl} = \int n_i dV$ is the full number of ablated ions, $V_{abl} = l_{abl} \cdot S_{foc}$ is the total ablated volume, $N_{abl} = 2.5 \times 10^{11}$ ions of an ionisation number of an atom Z = 1 (for the conditions introduced above in Sec. E for Ag). Estimate for the electric field:

$$\mathbf{E} \approx \frac{1}{cR_0} eZ N_{abl} \frac{d\mathbf{v}_i}{dt}.$$
 (A11)

Ions' acceleration $\frac{\partial v_i}{\partial t} = \frac{2\epsilon_e}{M_i l_s} = 1.45 \times 10^{17} \text{ cm/s}^2$. Taking for the estimate the distance to observation point $R_0 = 1$ cm one gets the field $E = 580 \text{ V/m} (1.93 \times 10^{-2} \text{ CGSE})$.

Appendix G Absence of the Debye screening

During the interaction time shorter the ion period (StL) the space and time dependence of the electron temperature is strong while the electron density remains practically unperturbed, $en_eE \approx -n_e\nabla T_e$. Therefore, assumptions of the static limit and space independence of the electron temperature (isothermal equation of state [7]; see Kruer, p.14 [7]), essential for deriving the Debye screening, are both inapplicable, $en_eE \neq -T_e\nabla n_e$. The absence of screening is due to lack of collective interaction of multiple charges.

Appendix H Nanomachining: removal of a few mono-atomic layers

To remove few atomic layers with a thickness equal to the mean free path of electron, energy of electrons should be slightly above the work function ($l_{mfp} \approx$ nanometre) the laser

393

398

399

401

402

403

404

405

407

410

411

412

413

414

415

416

417

422

423

424

425

427

430

431

432

433

434

435

436

437

shall deliver to the Ag surface the energy density (see Sec. D): $F = \frac{w_e}{C_0} \times \exp\left[\frac{2l_{mfp}}{l_s}\right] \text{ J/cm}^2$. For Ag hit by 1000 nm light only 5% of the surface energy density of 0.247 J/cm² is spent for a few atomic layers' removal. The number of the atomic layers removed by explosion, i.e., the electron's mean free path, is controlled by the absorbed surface energy density delivered by laser. Indeed, mean free path of electron in the Coulomb collisions is, $l_{mfp} \propto \epsilon_e^2$, while $\epsilon_e \propto F$.

Volume and speed of ablation demonstrated with bursts of $t_p \ge 300$ fs pulses [23] can potentially be improved using ablation by StL pulses, which are an order of magnitude shorter and cause energetic ion explosion from the laser-affected surface. Ablation by high repetition rate (bursts) of StL pulses harness the Coulomb explosion of the surface occurring at higher speed and can potentially improve throughput of material processing.

Author Contributions: Conceptualization, E.G.G; methodology, E.G.G; E.G.G; writing—original draft preparation, E.G.G; writing—review and editing, E.G.G and S.J.

Funding: "This research received no external funding".

Data Availability Statement: All data are provided within the main text and supplemental sections.

Acknowledgments: E.G.G. thanks Prof. Vladimir Tikhonchuk for reading the paper, discussions, comments and suggestions. S.J. is grateful for funding by the ARC Linkage LP190100505 project.

Conflicts of Interest: "The authors declare no conflict of interest."

References

1. Stuart, B.; Feit, M.; Shore, B.; Perry, M. Laser-induced damage in dielectrics with nanosecond to picosecond pulses. *Phys. Rev. Lett.* **1995**, 74, 2248–2251.

2. Stuart, B.; Feit, M.; Herman, S.; Rubenchik, A.; Shore, B.; Perry, M. Optical ablation by high-power short-pulse lasers. *J. Opt. Soc. Am. B* **1996**, *13*, 459–468.

- 3. Gamaly, E.; Rode, A.; Luther-Davies, B.; Tikhonchuk, V. Ablation of solids by femtosecond lasers: Ablation mechanism and ablation thresholds for metals and dielectrics. *Phys. Plasmas* **2002**, *9*, 949–957.
- 4. Millikan, R. A Direct Photoelectric Determination of Planck's 'h. Phys. Rev. 1916, 7, 355–388.
- 5. Il'inskii, Y.; Keldysh, L. Electromagnetic response of Material Media; Plenum Press: New York and London, 1994.
- Genieys, T.; Sentis, M.; Utéza, O. Investigation of ultra-short laser excitation of aluminum and tungsten by reflectivity measurements. Appl. Phys. A 2019, 126, 263.
- 7. Kruer, W. The Physics of Laser Plasma Interactions; Addison-Wesley: Reading, 1988.
- 8. Tamm, I. Basics of the Electricity Theory, 8 ed.; Mir Publishers: Moscow, 1976 (in Russ.).
- 9. Mourou, G.; Tajima, T.; SV Bulanov, S. Optics in the relativistic regime. Rev. Mod. Phys. 2006, 78, 309.
- 10. Landau, L.; Lifshitz, E. Teoriya Polya (The Classical Theory of Fields), 5 ed.; Nauka: Moscow, 1967 (in Russ.).
- 11. Landau, L.; Pitaevskii, L.; Lifshitz, E. *Electrodynamics of Continuous Media*; Vol. 5, Butterworth-Heinemann: Oxford, 1984.
- 12. Codling, K.; Frasinski, L.; Hatherly, P.; Barr, J. On the major mode of multiphoton multiple ionisation. *J. Phys. B: Atomic and Molecular Physics* **1987**, 20, L525.
- 13. Boll, R.; Schäfer, J.; Richard, B.; et al.. X-ray multiphoton-induced Coulomb explosion images complex single molecules. *Nat. Phys.* **2022**, *18*, 423–428.
- 14. Purnell, J.; Snyder, E.; Wei, S.; Castleman, A. Ultrafast laser-induced Coulomb explosion of clusters with high charge states. *Chem. Phys. Lett.* **1994**, 229, 333–339.
- 15. Ditmire, T.; Donnelly, T.; Rubenchik, A.; Falcone, R.; Perry, M. Interaction of intense laser pulses with atomic clusters. *Phys. Rev. A* **1996**, *53*, 3379.
- 16. Ditmire, T.; Tisch, J.; Springate, E.; Mason, M.; Hay, N.; Smith, R.; Marangos, J.; Hutchinson, M. High-energy ions produced in explosions of super-heated atomic clusters. *Nature* **1997**, *386*, 54–56.
- 17. Kraus, B.F.; Gao, L.; Fox, W.; Hill, K.W.; Bitter, M.; Efthimion, P.C.; Moreau, A.; Hollinger, R.; Wang, S.; Song, H.; et al. Ablating Ion Velocity Distributions in Short-Pulse-Heated Solids via X-Ray Doppler Shifts. *Phys. Rev. Lett.* **2022**, 129, 235001.
- 18. Huang, H.H.; Juodkazis, S.; Gamaly, E.; Nagashima, T.; Yonezawa, T.; Hatanaka, K. Spatio-temporal control of THz emission. *Communications Physics* **2022**, *5*, 134.
- 19. Weast, R.C., Ed. CRC handbook of chemistry and physics, 69 ed.; CRC Press: Boca Raton, Florida, 1989.
- 20. Gamaly, E. Femtosecond Laser Matter Interactions: Solid-Plasma-Solid transformations at the Extreme Energy Density, 2 ed.; Jenny Stanford Publishing: Singapore, 2022.
- 21. Cauble, R.; Rozmus, W. Two-temperature frequency-dependent electrical resistivity in solid density plasmas produced by ultrashort laser pulses. *Phys. Rev. E* **1995**, *52*, 2974–2981. https://doi.org/10.1103/PhysRevE.52.2974.

12 of 12

22. Gamaly, E. Femtosecond Laser Matter Interactions: Theory, Experiments, and Applications; Pan Stanford: Singapore, 2011.

23. Kerse, C.; Kalaycıoğlu, H.; Elahi, P.; Çetin, B.; Kesim, D.; Akçaalan, Ö.; Yavaş, S.; Aşık, M.; Öktem, B.; Hoogland, H.; et al. Ablation-cooled material removal with ultrafast bursts of pulses. *Nature* **2016**, *537*, 84–89.