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Article

High Thermoelectric Performance of a Novel Monolayer γ -PbSnX₂ (X=S, Se, Te): Predicted by First-Principles

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Abstract: Two-dimensional (2D) of transition metal dichalcogenides (TMDCs) are potential candidates for thermoelectric (TE) applications due to their unique structural properties. In this paper, we constructed an 2D monolayer TMDCs semiconductor γ -PbSnX₂ (X=S, Se, Te) and first-principles calculations and Boltzmann transport theory are used to study the thermoelectric performance. We found that γ -PbSnX₂ had an ultra-high carrier mobility up to $4.04 \times 10^3 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$ leading to a metal-like electrical conductivity. Meanwhile, γ -PbSnX₂ both have high Seebeck coefficients, resulting in high power-factors, and also shows intrinsic low lattice thermal conductivity of 6-8 W/mK at room temperature. The lower lattice thermal conductivity and high power-factors resulted in excellent thermoelectric performance. The high ZT values of γ -PbSnS₂ and γ -PbSnSe₂ were as high as 2.65 and 2.96 at 900 K, respectively. The result suggests that the monolayer γ -PbSnX₂ are better candidates for excellent thermoelectric performance.

Keywords: thermoelectric properties; TMDCs; first-principles; Boltzmann transport equation

1. Introduction

The world's energy demand is increasing due to the development of science and technology. Thermoelectric modules can directly convert electricity into thermal energy for cooling and heating and can also harvest waste heat for electrical power and have thus attracted significant attention [1,2]. The performance of thermoelectric materials is usually evaluated by the dimensionless figure of merit (ZT), which is defined as $ZT = S^2 \sigma T / (\kappa_e + \kappa_l)$, where S is the Seebeck coefficient, σ is the electrical conductivity, T is the absolute temperature, κ_e and κ_l are the electronic thermal conductivity and lattice thermal conductivity [3,4]. The higher ZT value means the better efficiency μ of thermoelectric conversion.

However, due to the Wiedemann-Franz law, there is a coupling relationship between electronic transport coefficients, which makes it a significant challenge to improve ZT and enhance thermoelectric performance[5]. To improve thermoelectric performance, many advanced methods have been proposed, which can be divided into two main categories, namely phonon engineering and electronic engineering, for optimizing phonon and electronic transport properties, respectively[6–12]. The phonon engineering is focused on the modulation of lattice thermal conductivity by suppress the mean free path of phonon. The electron engineering aims in the modulation of power factor and Seebeck coefficient under the optimum carrier concentration. Such as strain engineering [13–18], doping defects[19–21], molecular junction [4,22–24], superlattices[25–27] and heterostructure[28,29].

Two-dimensional materials are very promising candidates for thermoelectricity because of the increase in the Seebeck coefficient due to the increase in the density of states near the Fermi energy level[30,31]. In particular, single layers of transition metal dichalcogenides (TMDCs), such as MX₂ (M=Mo, W, Ti, and X=S, Se, Te), have attracted a large attention in last decades du to their unique semiconducting characteristics[31–33]. Recently, a novel type of 2D TMDCs, (AX)₂ (A=Si, Ge, Sn,

Pb;X=Se, Te), has been predicted theoretically from ab initio calculations[34]. Dong et al. reported that the γ -SnX (X = S, Se, or Te) has high thermoelectric performance due to the low thermal conductivity[35]. And then, Jia et al. reported that reported high thermoelectric properties due to strong anharmonic effects in monolayer (PbX)₂(X=S, Se, Te)[36]. Thus, the γ -phase TMDCs are very promising candidates for thermoelectricity.

In this work, we constructed a series of 2D γ -phase TMDCs, i.e., γ -PbSnX₂(X=S, Se, Te), based on γ -AX(A=Pb, Sn and X=S, Se, Te). And investigate the thermoelectric transport properties by using first-principles calculations combined with the Boltzmann transport equation. The results show that these materials have high power factors and low lattice thermal conductivity, leading to high figure of merit (ZT). The studies indicate that these materials are potential candidates for high temperature thermoelectric materials. thermoelectric performance.

2. Computational method

In this work, we performed first-principles simulations using the Vienna Ab initio Simulation Package (VASP) software based on density functional theory (DFT) [37,38]. The generalized gradient approximation (GGA) method with the Perdew-Burke-Ernzerhof (PBE) exchange-correlation (XC) functional was employed [39]. The total energy convergence criterion of 10⁻⁸ eV, the force convergence criterion of 0.001 eV/Å, and the kinetic energy cutoff of 500 eV were used to optimize crystals [40]. A set of 15× 15 × 1 Monkhorst-Pack k-points [41] was used to sample the Brillouin zone. A 20 Å vacuum layer was set in the direction of the z-axis to avoid the interaction of periodic layers along the z-axis and the DFT-D3 method was used to correct van der Waals (VDW) interactions [42]. A hybrid functional (HSE06) was used to calculate the electronic band properties of materials. The thermoelectric transport coefficient was calculated by solving the Boltzmann transport equation with BoltzTraP-package [43]. The relaxation time was calculated by using the deformation potential theory and effective mass approximation. The 3×3×1 supercell was used to calculate the second-order and third-order force constants of the materials through the finite displacement method. The cutoff radius of the third order force constant was set as the sixth-nearest neighbors. Lattice thermal conductivity was obtained by solving the Boltzmann transport equation by ShengBTE, and the grid density of 60×60×1 k-points was used to ensure convergence[44].

3. Results

This section may be divided by subheadings. It should provide a concise and precise description of the experimental results, their interpretation as well as the experimental conclusions that can be drawn.

3.1. Structure and stability

The monolayer γ -PbSnX₂(X=S, Se, Te) can be constructed from γ -AX (A=Pb, Sn and X=S, Se, Te) monolayer by replacing one layer of chalcogen Pb/Sn atoms with another layer of chalcogen Sn/Pb atoms in the middle side, showing a hexagonal lattice structure with a *P3m1* space group (Figure 1). The calculated lattice constants of γ -PbSnS₂, γ -PbSnSe₂, and γ -PbSnTe₂ are a = b = 3.96 Å, 4.11 Å, and 4.37 Å, respectively. The specific crystal structure parameters are shown in Table 1.

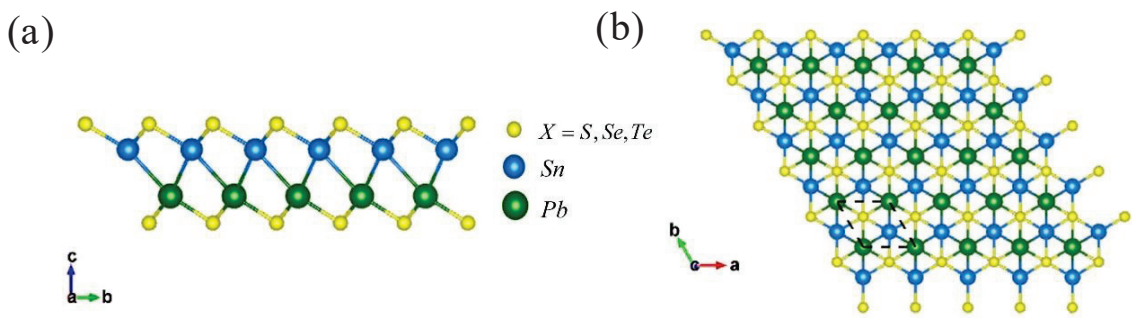


Figure 1. a Side view and a top view of the optimized γ -PbSnX₂ (X=S, Se, Te) monolayer structure

Table 1. Structural parameters for the γ -PbSnX₂(X=S, Se, Te). Here **a** is the lattice constant, **d**_{Sn–X}, **d**_{Pb–X} and **d**_{Pb–Sn} are the Sn–X, Pb–X and Pb–Sn bond lengths, and **h** is the vertical distance between the two outermost X atoms in Angstroms, as shown in Figure 1.

Material	a (Å)	d _{Sn–X} (Å)	d _{Pb–X} (Å)	d _{Pb–Sn} (Å)	h (Å)	$\alpha=\beta$	γ
PbSnS ₂	3.96	2.64	2.68	3.58	5.49	90°	120°
PbSnSe ₂	4.11	2.77	2.81	3.51	5.52	90°	120°
PbSnTe ₂	4.37	2.97	3.01	3.46	5.59	90°	120°

We verified the structure stability of monolayer γ -PbSnX₂(X=S, Se, Te). Figure 2(a-c) shows the phonon dispersion curve of γ -PbSnX₂. Each unit cell of the γ -PbSnX₂ monolayer has 4 atoms, with 3 acoustic and 9 optical branches. The phonon frequencies of the γ -PbSnX₂ monolayer are all positive, indicating the dynamic stability of the γ -PbSnX₂ monolayer. They all have very low phonon frequencies and lead to a decrease in their phonon frequencies as the atomic mass of sulfur group elements increases. More interestingly, an apparent coupling occurs between optical and acoustic phonon modes in γ -PbSnX₂ monolayers, which might lead to a low lattice thermal conductivity because of the anharmonic scattering. Moreover, we used ab initio molecular dynamics (AIMD) simulations to determine the stability of γ -PbSnX₂ at 900 K. The simulation results of AIMD are shown in Figure 2(d-f). The total energy is almost unchanged at a temperature of 900 K for 10 ps. These results indicate that γ -PbSnX₂ has a stable structure at 900 K.

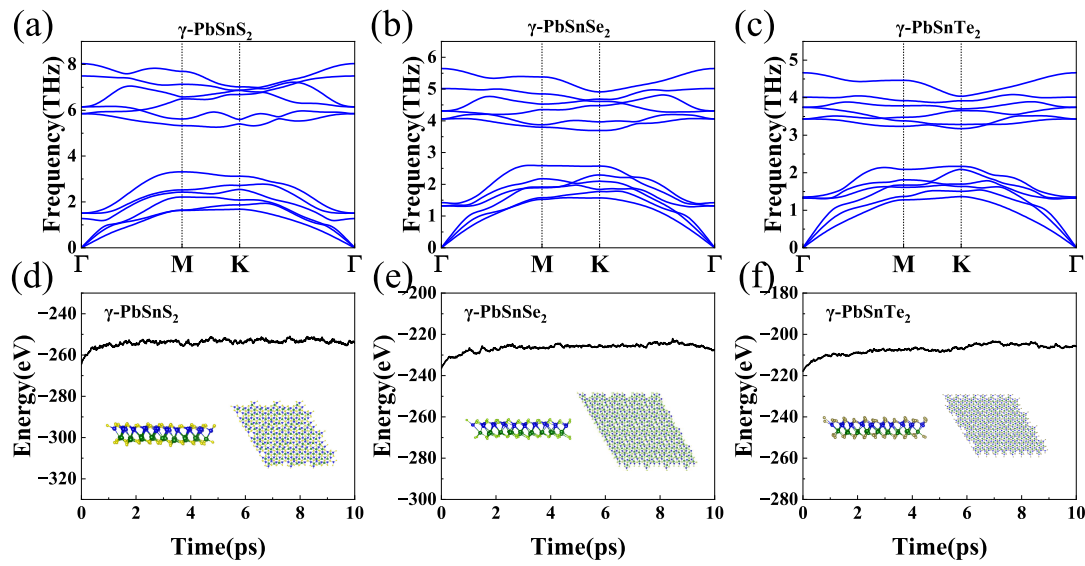


Figure 2. a-c Phonon dispersions for γ -PbSnX₂ (X=S, Se, Te). d-f Total potential energy fluctuation and structures in AIMD simulations of γ -PbSnX₂ (X=S, Se, Te)

3.2. Electronic band structure

Figure 3 shows the electronic band structures of γ -PbSnX₂ (X=S, Se, Te) monolayers calculated by the PBE and HSE06 exchange-correlation functionals, respectively. The corresponding band gap values are given in Table 2. They are both indirect band gaps with conduction band minimum (CBM) at the high symmetry point Γ (0, 0, 0) and valence band maximum (VBM) between the high symmetry points Γ (0,0,0) and K (1/3, 1/3, 0). The band gap calculated by HSE06 is large than that calculated by PBE. It is noted that the PBE functional often underestimates the band gap value, while the HSE functional can give a reliable band gap value compared with experiment. The band gap of γ -PbSnS₂, γ -PbSnSe₂ and γ -PbSnTe₂ are 0.86 (1.37) eV, 0.63 (1.08) eV and 0.61 (0.98) eV, respectively. The band gaps calculated by all the methods gradually decrease as the atomic number of the substituted chalcogenide element (S, Se, and Te) increases. Such moderate bandgaps indicate that thermoelectric properties of the γ -PbSnX₂ monolayer can be easily optimized at a reasonable doping concentration for 2D materials. Except for the band gap, there is no significant change in the type and shape of their energy bands, so we next to calculate the effective mass and carrier mobility of these materials by using the PBE generalization function. The partial density of states (PDOS) of the γ -PbSnX₂ is shown in Figure 3(d-f), with the valence bands closer to the Fermi energy level. The valence bands around the Fermi level originate from the S, Se and Te atoms, and the conduction bands are jointly contributed by Sn or Pb, S, Se and Te atoms. Figure 3(d-f) shows that γ -PbSnS₂, γ -PbSnSe₂ and γ -PbSnTe₂ all have very sharp density of state peaks at the Fermi energy level attachment, where γ -PbSnS₂ has a higher density of state peak than γ -PbSnSe₂ and γ -PbSnTe₂.

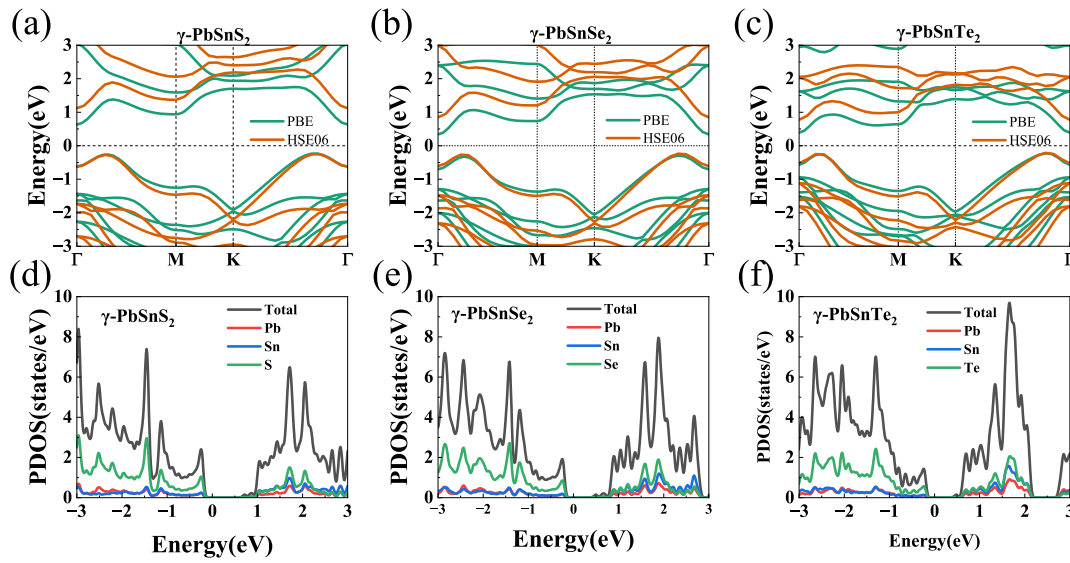


Figure 3. (a-c) Band structures of γ -PbSnX₂ (X=S, Se, Te) calculated by PBE and HSE06 functionals, respectively. (d-f) Partial density of states (PDOS) of the γ -PbSnX₂. The Fermi level was set as zero.

Table 2. Bandgap of γ -PbSnX₂ (X=S, Se, Te) calculated by PBE and HSE06.

Material	Structure	Gap-type	E _g (PBE)	E _g (HSE06)
PbSnS ₂	hexagonal (2D)	Indirect	0.86 eV	1.37 eV
PbSnSe ₂	hexagonal (2D)	Indirect	0.63 eV	1.08 eV
PbSnTe ₂	hexagonal (2D)	Indirect	0.61 eV	0.98 eV

3.3. Carrier mobility and relaxation time

We use the BoltzTraP-package based on the semi-classical Boltzmann transport equation to estimate the electrical properties of the monolayer γ -PbSnX₂ (X=S, Se, Te). Before that, we need to calculate the relaxation time of the carriers of the material, because the result calculated by BoltzTraP-package needs to be multiplied by the relaxation time. Here, carrier mobilities and relaxation time of 2D materials are calculated using deformation potential theory[45–47]:

$$\mu_{2D} = \frac{e\hbar^3 C_{2D}}{k_B T |m^*|^2 E_1^2} \quad (1)$$

$$\tau = \frac{\hbar^3 C_{2D}}{k_B T |m^*| E_1^2} \quad (2)$$

where μ_{2D} is the carrier mobility, C_{2D} is the elastic constant, m^* is the effective mass, m_d is the average effective mass, E_1 is the deformation potential energy, and τ is the relaxation time.

Table 3 shows the results of the electric and hole carrier mobilities calculated with the theory of deformation potential at 300 K. Among them, γ -PbSnS₂ and γ -PbSnSe₂ have ultra-high hole carrier mobility, especially, γ -PbSnS₂ has the highest hole mobility of $4.04 \times 10^3 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$, which is significantly higher than that of other two-dimensional semiconductors, such as MoS₂ ($285 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$)[48], SnS₂ ($756 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$)[49], SnSe₂ ($462 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$)[49], γ -PbX₂ ($780 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$)[36] and γ -SnX₂ ($1364 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$)[35]. Such high carrier mobility of γ -PbSnS₂ and γ -PbSnSe₂ is due to a combination of low effective mass and deformation potential energy. The high hole carrier mobility indicates that γ -PbSnS₂ and γ -PbSnSe₂ are potential p-type semiconductors. In addition, Hung et al. showed that high carrier mobility is one of the important parameters for screening thermoelectric

materials[50,51]. Such ultra-high carrier mobility indicates that γ -PbSnX₂ possesses excellent hole transport properties and thus are good thermoelectric materials.

Table 3. Calculated effective mass (m^*), elastic constant (C_{2D}), deformation potential (E_1), carrier mobility (μ_{2D}) and relaxation time (τ) for electrons (e) and holes (h) in monolayer γ -PbSnX₂ at 300 K.

Material	Carrier	C_{2D} (N/m)	m^* / m_0	E_1 (eV)	μ_{2D} ($\times 10^3 \text{cm}^2 \text{V}^{-1} \text{s}^{-1}$)	τ (ps)
PbSnS ₂	e	39.5	0.22	4.92	0.476	0.059
	h		0.50	1.02	4.04	1.14
PbSnSe ₂	e	42.75	0.18	5.52	0.654	0.067
	h		0.357	2.66	1.421	0.288
PbSnTe ₂	e	43.55	0.23	6.52	0.256	0.033
	h		0.596	4.14	0.245	0.083

3.4. Thermoelectric properties

We investigated the thermoelectric properties of the materials in the temperature range of 300 K to 900 K. As shown in Figure 4(a-c), all three materials have a high Seebeck coefficient at 300 K. Among them, the Seebeck coefficient of γ -PbSnS₂, γ -PbSnSe₂ and γ -PbSnTe₂ are 1400 $\mu\text{V/K}$, 800 $\mu\text{V/K}$ and 900 $\mu\text{V/K}$, respectively, which is much higher than that of most common 2D materials, such as SnTe (600 $\mu\text{V/K}$) [52], MoSe₂ (427 $\mu\text{V/K}$)[53] and WS₂ (328 $\mu\text{V/K}$)[54]. The Seebeck coefficient of γ -PbSnS₂ is higher than γ -PbSnSe₂ and γ -PbSnTe₂. This is because γ -PbSnS₂ has a higher density of states peak than γ -PbSnSe₂ and γ -PbSnTe₂ near the Fermi energy level (as shown in Figure 3), and the Seebeck coefficient is proportional to the density of states peak: $S \propto d(\text{DOS})/dE$. The high density of states peak near the Fermi energy level indicates that the material will have a higher Seebeck coefficient. Such a high Seebeck coefficient indicating that these materials may have high thermoelectric properties.

Figure 4(d-f) shows the electrical conductivities σ obtained by multiplying σ/τ by τ , where σ/τ is calculated using BoltzTraP-package and τ is the relaxation time calculated by the deformation potential theory. The electrical conductivity of γ -PbSnX₂ (X=S, Se, Te) exhibits similar behavior at different temperatures and decreases as the temperature increases. This is caused by the enhanced lattice vibrations and electron scattering at high temperature. The electric conductivity of γ -PbSnX₂ gradually decrease as the atomic number of the substituted chalcogenide element (S, Se, and Te) increases. And the value of the conductivity is related to the chemical potential. The conductivity of γ -PbSnX₂ is higher in the negative chemical potential range, which shows the characteristics of P-type semiconductors. It's worth noting that the electrical conductivity of γ -PbSnX₂ reached the same order (10^6 - $10^7/\Omega\text{m}$) as that of metals due to its ultra-high carrier mobility. The high Seebeck coefficient and conductivity indicate that they have a high power-factor ($PF = S^2\sigma$), which is important for thermoelectric devices. With the Seebeck coefficient and electrical conductivity, we evaluate the power factor (PF) of γ -PbSnX₂ (X=S, Se, Te), as show in Figure 4(g-i). All three materials have the same trend of power factor, which decreases with the increase of temperature. The γ -PbSnS₂ has the highest PF because of its highest Seebeck coefficient and electrical conductivity. And the PF values of these materials are maximum in the negative is due to their p-type properties. The PF is one of the important factors in evaluating the performance of thermoelectric materials, so a high PF predicts that the material may have high thermoelectric properties.

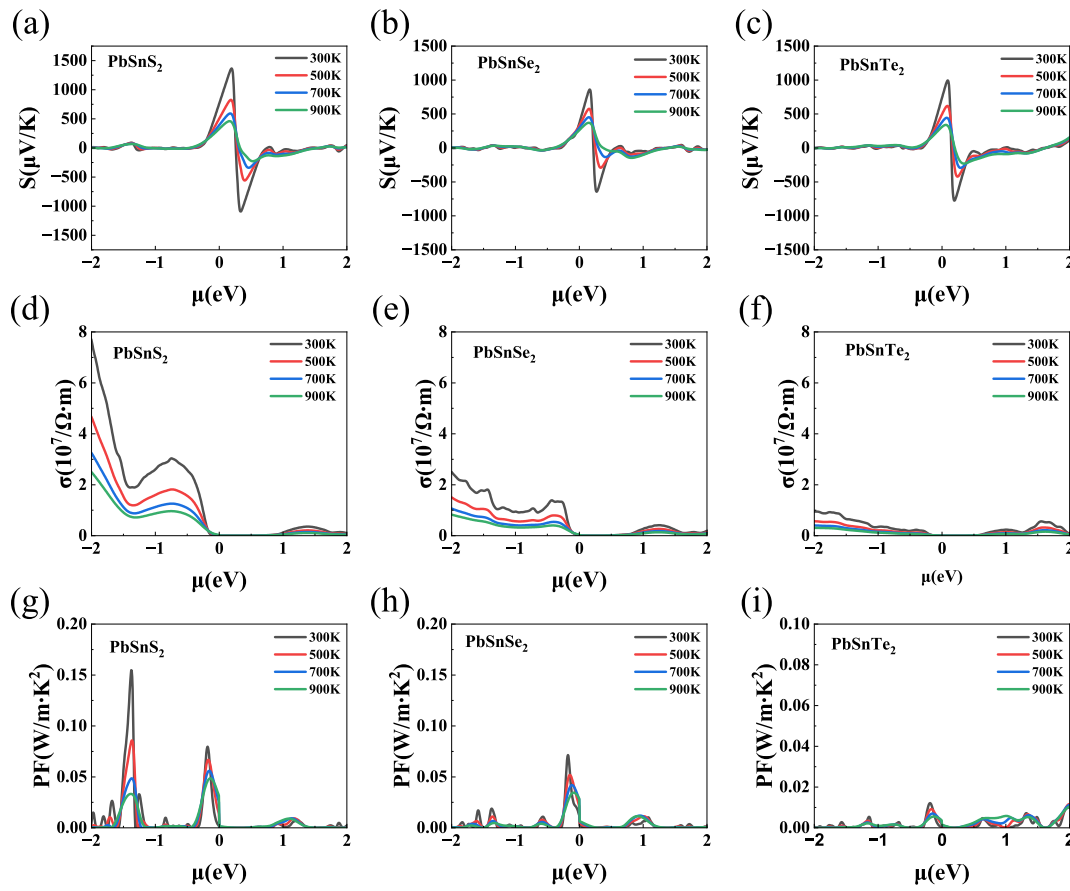


Figure 4. (a-c) Seebeck coefficients, (d-f) electrical conductivity and (g-i) Power-factor (PF) of γ -PbSnX₂ (X=S, Se, Te).

Materials with high thermoelectric properties require low thermal conductivity in addition to high power-factor. Figure 5 shows the phonon transport properties of γ -PbSnX₂ (X=S, Se, Te), the results show that both γ -PbSnX₂ have a very low thermal conductivity, which is about 6-8 W/mK at room temperature and the value of lattice thermal conductivity decreasing with the increasing of temperature. In order to understand the lattice thermal conductivity of the monolayer γ -PbSnX₂, we explore the phonon-related properties such as phonon group velocity and anharmonic scattering rates. As shown in Figure 5(a-c), the three acoustic phonon branches (ZA/TA/LA) get entangled and strong coupling occurs between the optical and acoustic phonon modes, which can strengthen the phonon scattering mechanism and thus lower κ_l . Figure 5(d-f) shows the phonon group velocities of γ -PbSnX₂, and it can be seen that they are both low, and low group velocities can lead to low lattice thermal conductivity. The inverse of the phonon relaxation time in the relaxation time approximation (RTA) is equal to the total scattering rate, which is the sum of the isotopic scattering rate (τ_i^{-1}), the boundary scattering rate (τ_b^{-1}) and the anharmonic scattering rate (τ_a^{-1}). In general, higher indicates stronger phonon-phonon scattering and lower phonon relaxation time, which is beneficial for reducing the lattice thermal conductivity. As shown in Figure 5(g-i), the γ -PbSnX₂ monolayer exhibits high phonon-phonon scattering rates (anharmonic scattering rates) and they are relatively close to each other. In addition, the value of the lattice thermal conductivity increases with the atomic number of the elements (S, Se, Te), which is mainly due to the increase of the atomic mass and the decrease of the phonon frequency. In conclusion, the strong coupling between phonons, lower phonon group velocities and higher scattering rates lead to lower lattice thermal conductivity, indicating that γ -PbSnX₂ may be suitable thermoelectric performance materials.

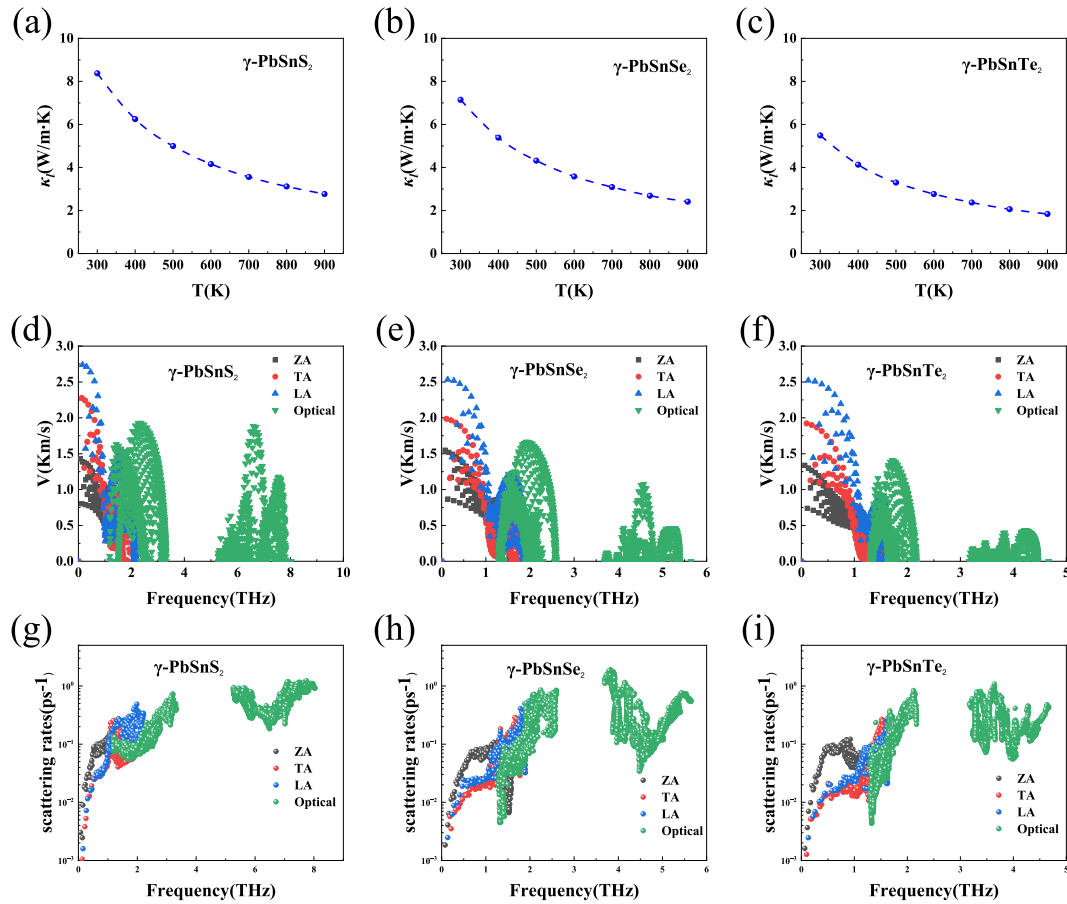


Figure 5. (a-c) Lattice thermal conductivity at different temperatures, (d-f) phonon group velocity at 300 K and (g-i) anharmonic scattering rates at 300 K of γ -PbSnX₂ (X=S, Se, Te).

After all transport coefficients were obtained, the dependence of ZT on the chemical potential of γ -PbSnX₂ monolayer at different temperatures was calculated, as shown in Figure 6. All of γ -PbSnX₂ exhibited the maximum thermoelectric properties in the negative chemical potential range due to their higher hole mobility. The ZT values for all three materials showed the same trend, increasing with increasing temperature. Among them, the ZT value of γ -PbSnTe₂ is lower, reaching a maximum of only 1.4 at 900 K, which is due to its low power factor. And, γ -PbSnS₂ and γ -PbSnSe₂ reached ultra-high ZT values of 2.65 and 2.96 at 900 K due to a combination of their low lattice thermal conductivity and high power-factor. Such ultra-high ZT values of γ -PbSnX₂ are contributed to their low thermal conductivity along with their high power-factor. Such high ZT values indicates that γ -PbSnS₂ and γ -PbSnSe₂ are good performing high temperature thermoelectric materials.

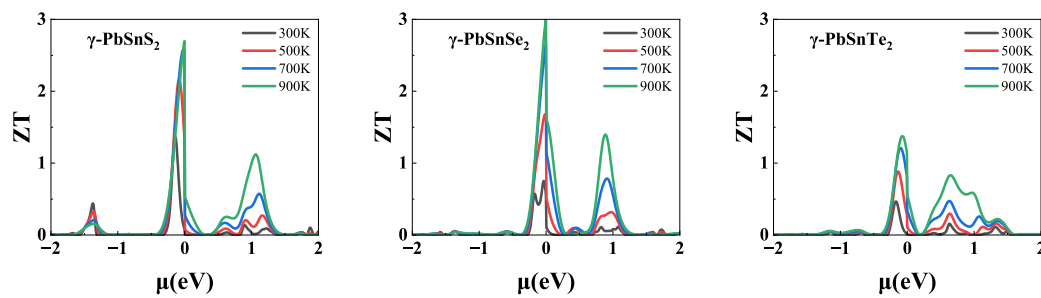


Figure 6. (a-c) Lattice thermal conductivity at different temperatures, (d-f) phonon group velocity at 300 K and (g-i) anharmonic scattering rates at 300 K of γ -PbSnX₂ (X=S, Se, Te).

4. Conclusions

In this study, we constructed a series of 2D monolayer material γ -PbSnX₂ (X = S, Se, Te) based on γ -(AX)₂ (A=Sn,Pb and X=S,Se,Te) and calculated its thermoelectric properties using Boltzmann transport theory combined with first-principles. The results show that these materials are narrow bandgap semiconductors with bandgap values of 0.98-1.37 eV by HSE06 functional. They have high hole carrier mobilities, in particular, γ -PbSnS₂ has a hole carrier mobility of $4.04 \times 10^3 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$. And they both have low lattice thermal conductivity and high power-factors. The ZT values of γ -PbSnS₂, γ -PbSnSe₂ and γ -PbSnTe₂ at 900K were 2.65, 2.96 and 1.36, respectively. Such high thermoelectric performance indicates that γ -PbSnX₂ are excellent thermoelectric materials. Our theoretical study may help to discover a new stage to experimentally optimize the thermoelectric properties.

Author Contributions: Conceptualization, D.C. and D.Z.; methodology, D.C.; software, D.C. and D.Z.; validation, L.N., Z.J., T.L., R.W. and C.K.; formal analysis, X.X.; investigation, D.C. and D.Z.; resources, C.K.; data curation, D.C.; writing—original draft preparation, D.C.; writing—review and editing, C.K.; project administration, C.K.; funding acquisition, C.K. and R.W. All authors have read and agreed to the published version of the manuscript.

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Conflicts of Interest: The authors declare no conflict of interest.

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