

DFT-Assisted Low-Dimensional Carbon-based Electrocatalysts Design and Mechanism Study: A Review

Yun Han^{1,2}, Hongzhe Xu^{1,2}, Qin Li^{1,2}, Aijun Du^{3}, Xuecheng Yan^{*1}*

¹ Queensland Micro- and Nanotechnology Centre, Griffith University, Nathan Campus, QLD 4111, Australia.

² School of Engineering and Built Environment, Griffith University, Nathan Campus, QLD 4111, Australia.

³ School of Chemistry and Physics and Centre for Materials Science, Queensland University of Technology, Gardens Point Campus, Brisbane 4001, Australia.

Corresponding author E-mail: aijun.du@qut.edu.au (A. Du), x.yan@griffith.edu.au (X. Yan)

Abstract

Low-dimensional carbon-based (LDC) materials have attracted extensive research attentions in electrocatalysis because of their unique advantages such as structural diversity, low cost, and chemical tolerance. They have been widely used in a broad range of electrochemical reactions to relief environmental pollution and energy crisis. Typical examples include hydrogen evolution reaction (HER), oxygen evolution reaction (OER), oxygen reduction reaction (ORR), carbon dioxide reduction reaction (CO₂RR), and nitrogen reduction reaction (NRR). Traditional “trial and error” strategies seriously slowed down the rational design of electrocatalysts for these important applications. Recent studies show that the combination of density functional theory (DFT) calculations and experimental research is capable of accurately predicting the structures of electrocatalysts, thus could reveal the catalytic mechanisms. Herein, current well-recognized collaboration methods of theory and practice are reviewed. The history of modern DFT, commonly used calculation methods, and basic functionals are briefly summarized. Special attention is paid to descriptors that are widely accepted as a bridge links the structure and activity, and the breakthroughs for high-volume accurate prediction of electrocatalysts. Importantly, correlating multiple descriptors are used to systematically describe the complicated interfacial electrocatalytic processes of LDC catalysts. In addition, machine learning and high-throughput simulations are crucial in assisting the discovery of new multiple descriptors and reaction mechanisms. This review will guide the further development of LDC electrocatalysts for extended applications from the aspect of DFT computations.

Keywords: Density functional theory, Descriptor, Carbon-based materials, Electrocatalysis, Low dimension.

1. Introduction

Environmental pollution and energy crisis are the two main critical issues of modern society caused by the excessive use of fossil fuels. Acid rain, haze and greenhouse effect have disastrously affected the normal life of human beings.¹⁻³ On the one hand, great efforts have been devoted to the investigation and utilization of renewable clean energy and the efficient conversion between electrical and chemical energy, i.e., electrocatalytic hydrolysis and fuel cells.^{4, 5} Greenhouse gases recycling, on the other hand, is also regarded as one of the most promising techniques to reducing air pollution, for example, the reduction of CO₂. Therefore, effective electrochemical reactions, such as hydrogen evolution reaction (HER) and oxygen evolution reaction (OER) for water splitting, oxygen reduction reaction (ORR) for fuel cell and carbon-dioxide reduction reaction (CO₂RR) are highly expected to solve the above issues (Figure 1).^{6, 7} However, the performance of these electrochemical reactions is severely hampered by their sluggish kinetics, which can be significantly improved with the introduction of efficient electrode catalysts.^{8, 9}

Noble metal-based materials such as platinum (Pt) and ruthenium (Ru) are widely used as the benchmark catalysts. However, the scarcity and high cost impede their industrial mass production. Therefore, non-noble metal even metal-free electrocatalysts have been intensively studied and remarkable progress has been reached.¹⁰⁻¹³ Up to now, low-dimensional carbon materials, such as 2D graphene nanosheets (G), 1D carbon nanotubes (CNT) and 0D fullerenes have been widely used for fabricating a series of non-noble metal and even metal-free catalysts for energy conversion. This is because of their unique properties such as tunable molecular structures, spatial confinement and surface effect, abundance and excellent oxidation and corrosion resistance. Various defects and heteroatoms are embedded into carbon substrates, such as transition metals, nitrogen, boron, *etc.*, which can greatly improve their catalytic efficiency.¹⁴⁻²⁴

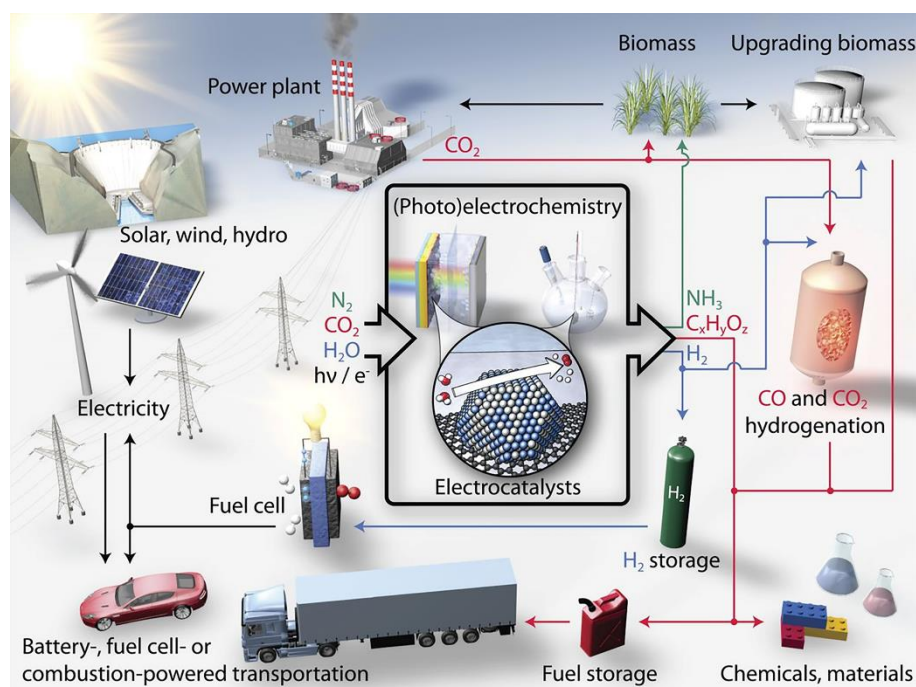


Figure 1. Schematic of a sustainable energy landscape based on electrocatalysis. Reproduced with permission.⁶ Copyright 2017, American Association for the Advancement of Science.

It is difficult to reveal the catalytic mechanism and actual active sites of electrocatalysts only *via* experimental study. For instance, previous studies show that pyridinic nitrogen is responsible for the ORR in N-doped carbon-based metal-free catalysts,^{25, 26} while other studies suggest that the active sites are graphitic nitrogen.^{27, 28} Therefore, the current quest is to develop appropriate methodologies to provide a comprehensive understanding of the catalyst structures at electronic levels, which will promote the comprehension of the reaction mechanisms and guide future experimental study.²⁹ Nowadays, based on the first principles, the modern density functional theory (DFT) calculation has become an irreplaceable modeling toolkit for scientists in a variety of research areas. Two main strategies of DFT calculation assisted design of electrocatalysts have been established by theoretical and experimental chemists. The first one is dominated by theoretical calculations, dedicated to achieving a rational design of high-performance catalysts. It is crucial to identify the most important parameters to reveal the relationships between structures and performance, which is the so-called descriptors and can considerably boost the traditional trial and error approach. Machine-learning and high-throughput calculations also have been developed to efficiently screen active sites and descriptors for the targeted catalysts. The second one is dominated by experimental testing and

characterizations, assisted by calculating the change during the catalysis process such as step-energy, molecular and electronic structure, and electron transition that can reveal the reaction mechanism accurately. In this review, we will mainly summarize the history and concepts of modern DFT, the heterogeneous electrocatalytic surface-related descriptors, the combination of experiment and calculation, and recent achievements of low-dimensional carbon-based electrocatalysts for energy storage and conversation applications.

2. Overview of DFT

Quantum chemistry is mainly based on quantum mechanics principles, and the main goal of all first principle calculations is to obtain the electronic wave function ψ that characterizes the state of the system, for which the Schrödinger equation must be solved. Theoretical computing has received increasing attention from the chemistry community as computer technology has progressed. However, the traditional Wave Function Theory (WFT) method has two fatal shortcomings. First, the wave function ψ of a system with N electrons will contain $3N$ coordinate variables. Therefore, a $3N$ -dimensional wave function image, which is difficult to describe visually, will be a stumbling block in solving the Schrödinger equation. Second, the Schrödinger equation for a multi-electron system is too computationally intensive to be calculated accurately. Modern DFT has become a viable option to solve these drawbacks.

2.1 History of Modern DFT

The homogeneous electron-gas model, commonly known as the Thomas-Fermi model, was proposed by Thomas and Fermi in 1927, and it has established a firm foundation for DFT. The ground state energy of the electron system is directly represented in terms of electron density instead of wave function, which drastically reduces the system's freedom degree.^{30, 31} In 1964, based on the Thomas-Fermi model, Hohenberg and Kohn proposed an inhomogeneous electron-gas model and proved two theorems served as the fundamentals of modern DFT.³² The first theorem asserted that the nuclear potential energy $V(r)$ of all electrons in a system has n interacting electrons is a unique function of the electronic density $\rho(r)$. This could be presented as Hohenberg-Kohn equation as shown in Eq. 2.1.

$$E_V[\rho] = \rho(r)V(r)dr + F_{HK}[\rho] \quad \text{Eq. 2.1}$$

Here, $F_{HK}[\rho] = T[\rho] + E_{ee}[\rho]$, $T[\rho]$ is the sum of electronic kinetic energy, $E_{ee}[\rho]$ is electron–electron repulsion. The second theory proposed a density minimum principle, stating that the ground state energy of any trial electron density $\rho(r)$ cannot be lower than the true ground system. Then the Euler-Lagrange equation can be obtained as shown in Eq. 2.2.

$$\mu = \frac{\delta E_V[\rho]}{\delta \rho(r)} = V_{cxt}(r) + \frac{\delta F_{HK}[\rho]}{\delta \rho(r)} \quad \text{Eq. 2.2}$$

Therefore, if $F_{HK}[\rho]$ is confirmed, $\rho(r)$ and $E_V[\rho]$ can be solved by Eq. 2.2. However, the exact expression for $F_{HK}[\rho]$ remains unknown until now. In 1965, Kohn and Sham³³ revealed a brand-new approach to approximately derive the $F_{HK}[\rho]$. $F_{HK}[\rho]$ can be divided into three parts and can be presented as:

$$F_{HK}[\rho] = T_s[\rho] + J[\rho] + E_{xc}[\rho] \quad \text{Eq. 2.3}$$

Where, $T_s[\rho]$ and $J[\rho]$ are the kinetic energy and coulombic correlation energy of independent electrons, respectively. $E_{xc}[\rho]$ is a functional with small magnitude called exchange–correlation (XC) energy that can be approximated, and it can be presented as:

$$E_{xc}[\rho] = T[\rho] - T_s[\rho] + V_{ee}[\rho] - J[\rho] \quad \text{Eq. 2.4}$$

By variation, we can get the famous Kohn-Sham equation:

$$\hat{H}_{KS}\phi_i \equiv \left[-\frac{1}{2}\nabla^2 + V(r) + \int \rho(r')/|r-r'|dr' + V_{xc}(r) \right] \phi_i(r) = \varepsilon_i \phi_i(r) \quad \text{Eq. 2.5}$$

And XC potential can be defined by:

$$V_{xc}(r) = \delta E_{xc}[\rho]/\delta \rho(r) \quad \text{Eq. 2.6}$$

Overall, there is no approximation and the Kohn-Sham equation is accurate. However, the $E_{xc}[\rho]$ component of the Kohn-Sham equation still lacks a rigors expression form, making it impossible to use in practical calculations. Instead, several types of approximate XC generalized functionals must be built to gradually approximate the real system.

2.2 Exchange–Correlation (XC) Functional

Some of the approximations such as local density approximation (LDA), generalized gradient approximation (GGA), meta-GGA, and hybrid functional can be shown as the well-known Jacob's ladder from Hartree world to Chemical accuracy heaven (Figure 2).³⁴⁻³⁶



Figure 2. Illustration of Jacob's Ladder of DFT. Reproduced with permission.³⁶ Copyright 2020, John Wiley and Sons.

The approximation for LDA is that the charge density changes slowly with position and behaves similar to local heterogeneous electron cloud, so the XC energy can be presented as:

$$E_{XC}^{LDA}[n] = \int dr n(r) \epsilon_{XC}(n) \quad \text{Eq. 2.7}$$

However, the LDA method is rough in calculating the actual system and will overestimate the binding energy of the electron density because of their localized character.

To improve the accuracy of the LDA method, GGA method describes electron density with the assistance of density gradient, and can be presented as:

$$E_{XC}^{GGA} \propto \int dr f(n, \nabla n) \quad \text{Eq. 2.8}$$

BLYP,^{37, 38} PW91,^{39, 40} and PBE⁴¹ are the commonly used approximated density functionals of GGA method.

Based on the GGA method, meta-GGA, such as TPSS, TPSSh, and M06-L,⁴²⁻⁴⁴ introduced kinetic energy density variables, but with better accuracy accompanied by a significant increase in computational cost.

By partially combining accurate XC functional in the DFT, the hybrid functional could improve the calculation accuracy. The most popular one is the B3LYP functional,⁴⁵ which can be described as:

$$E_{XC}^{B3LYP} = A \cdot E_X^{LDA} + (1 - A)E_X^{HF} + B \cdot \Delta E_X^{Bec} + C \cdot E_C^{LYP} + (1 - C)E_C^{VWN} \quad \text{Eq. 2.9}$$

Calculations involving periodic systems frequently employ the HSE functional,⁴⁶ which is represented by the following equation:

$$E_{XC}^{HSE} = A \cdot E_X^{HF,SR} + (1 - A)E_X^{PBE,SR} + E_X^{PBE,LR} + E_C^{PBE} \quad \text{Eq. 2.10}$$

2.3 Periodic System

To deal with periodic systems, supercell models (primitive cells in three dimensions (X, Y, and Z) with periodic repetition) are frequently used. Vacuum space greater than 10 Å is added in the Z-direction to eliminate the interaction. In condensed matter physics, Bloch's theorem states that solutions to the Schrödinger equation in a periodic potential take the form of a plane wave modulated by a periodic function, and can be written as:

$$\Psi(r) = u_k(r)e^{ikr} \quad \text{Eq. 2.11}$$

Where r is the position, Ψ is the wave function, k is the wave vector. Based on the Bloch theorem, electronic band structure is involved to investigate the surface science, and electronic states at numerous k points should be calculated. In practical calculations, however, a finite number of k points are used, the higher the density of the k points, the lower the inaccuracy will be. In general, the numbers of k points for metal systems are higher than that of the oxide systems.

For periodic systems, electron wave function can be expanded with numerous plane-wave functions. However, only plane-wave basis sets with kinetic energy lower than the cut-off

energy are considered in practical calculations, which would result in a systematic error.^{47, 48} Therefore, pseudopotential that can replace the true atomic potential of the nucleus and inner electrons, is introduced to reduce the systematic error. Currently, the most widely used plane wave methods are ultra-soft pseudopotentials (US-PP) plane wave method and projector augmented wave (PAW) method.⁴⁹

2.4 DFT+U Scheme

DFT calculations cannot adequately describe systems with physical properties that are controlled by many-body electronic interactions (correlated systems), because it is typically challenging to model the dependence of the XC functional on electronic charge density. The over-delocalize valence electrons and over-stabilize metallic ground states are considered to be the main problems of DFT to describe correlated systems. Therefore, the DFT+U approach has been developed to enhance the description of the ground state of correlated systems.⁵⁰ The key advantage of the DFT+U method is that it is within the realm of DFT, which makes it easy to implement in the existing DFT codes and its computational cost is only slightly higher than that of normal DFT computations. The local and semi-local density functionals that allow LDA+U and GGA+U computational operations can be enhanced with this ‘U’ correction. The primary function of the ‘U’ correction is to add an additional Hubbard-like term to the strong on-site Coulomb interaction of localized electrons. The on-site Coulomb term U and the site exchange term J are the two parameters that represent the strength of the on-site interactions for the purpose of practical DFT+U implementation in computational chemistry. Parameters ‘U and J’ are typically derived semi-empirically, although *ab initio* computations can yield them.⁵¹

$$E(DFT + U) = E(DFT) + \frac{U_{eff}}{2} \sum_{\sigma} Tr[\rho^{\sigma} - \rho^{\sigma} \rho^{\sigma}] \quad \text{Eq. 2.12}$$

It has become a standard to use the parameter: $U_{eff} = U - J$ in place of the interaction parameter U in the simplified LDA+U form. U_{eff} is frequently preferred, because the ‘J’ parameter has been shown to be essential for describing the electronic structure of specific classes of materials, typically those subject to high spin-orbit coupling.

2.5 Molecular Dynamics Simulation

Molecular dynamics (MD) simulation, which is based on Newton's laws of motion, can simulate the trajectory of each atom in a system at a certain temperature, thus the system's dynamic properties can be calculated. However, the standard DFT can only be used to calculate a system's static properties at 0 K. Briefly, for a given configuration and initial velocity of each atom, the MD simulation can be divided into three steps. First of all, the forces acting on each atom in the system are calculated to determine the system's acceleration. Secondly, the configuration of the system after Δt time can be obtained according to the Newton's three laws. Thirdly, the calculation of the forces in the first step is continued based on this configuration, and the results of the system evolving with time can finally obtain by repeated recurrence.

MD simulation can be further classified into two types: Classic MD simulation and *ab initio* MD (AIMD) simulation, depending on how the forces are calculated in the first step. Classic MD simulation builds the potential energy function from the empirical force field and calculates the force at each step using the gradient of the potential energy function. AIMD simulation, on the other hand, can be used to accurately calculate the force at each step by the *ab initio* quantum chemical method.⁵²⁻⁵⁴

2.6 Transition State Theory

The transition state (TS), also known as the saddle point, is the highest energy point on the potential energy surface (PES) where the reactants (initial state, IS) generate products (final state, FS) along the minimum energy path. Within the transition state theory (TST), we assume that IS and TS are in the quasi-equilibrium, and the main task is to find out the free energy barrier for the transition, which is the energy difference between IS and FS. Based on TST, transition rate can also be calculated. The Dimer method⁵⁵ and the climbing image nudged elastic band (CINEB) approach⁵⁶ are the two most popular calculating techniques.

The dimer method can be used to find out the saddle points by two images of the system, which is the so-called 'dimer'. Driving by the saddle point search algorithm, dimer is moved uphill on the potential energy surface, away from the vicinity of the potential energy minimum of the IS and toward a saddle point. The dimer is rotated along the way to identify the potential energy mode with the lowest curvature at the dimer's location. Since the Dimer technique only uses the

first derivatives of the energy, the major benefit is not requiring the time-consuming computation of the minimal eigenvalue of the Hessian matrix. The Dimer technique also has the advantage of having less stringent initial configuration requirements.

The nudged elastic band (NEB) method is an efficient method for identifying the minimum energy path (MEP) between a given initial and the final state of a transition, which has also been widely used to estimate transition rates. A set of images between the IS and FS of the system are created, often on the order of 4-20. Then the adjacent images are connected by a collection of spring interactions, which can form an elastic band and ensure the continuity of the path. The band is brought to the MEP by an optimization process that minimizes the force acting on the images. The drawback of the NEB method is that it requires the intermediates be evenly spaced throughout the optimization process, the predicted TS may be slightly deviated from the actual TS. The CINEB method was developed to address this issue, and the force on the highest image is the full force resulting from the potential with the component along the elastic band inverted, showing that it will not be impacted by spring forces. As a result, the intermediate will gradually move to the direction of higher energy and reaches the actual TS.

3. Theoretical Guidance in Catalyst Design and Mechanism Study

Nowadays, a series of well-known carbon-based electrocatalysts have been fabricated through the combinations of various modification methods and substrate materials, such as heteroatom doped graphene, defective graphene, Mxene, heteroatom doped carbon nanotubes/ribbons and modified carbon dots.⁵⁷⁻⁶⁵ However, the design of state-of-the-art electrocatalysts still relies on inefficient trial-and-error approaches, and the catalytic mechanism is still controversial and difficult to reveal only through experimental research. DFT calculations are thus utilized to address two issues: 1) predicting catalytic performance and guiding the synthesis of electrocatalysts. 2) investigating and corroborating the mechanism of electrocatalysis in conjunction with experimental study.

3.1 Application of Theoretical Guidance in Designing Electrocatalysts: Descriptors

To predict the performance of electrocatalysts, computational scientists mainly focus on the most important microscopic properties of the catalysts that determine the macroscopic catalytic performance. Since early 20th century, catalysts with high activity, according to the traditional

Sabatier principle, should bind atoms and molecules with an ideal bond strength: not too weak to activate the reactants, and not too strong to desorb the products. Therefore, a volcano shape relationship between bond strength and catalytic activity has been proposed to represent the predictivity of many descriptors.⁶⁶ Due to the lack of quantitiveness and inability to undergo experimental validation, this principle is not very predictive. The "bond strength" between the relevant intermediates and the catalysts has been described during the past decades by the extraction of electronic and structural properties such as the descriptors.

3.1.1 *d*-Band Center Theory

The well-known *d*-band center theory proposed by Nørskov *et al.* has laid the foundation for a series of descriptors.⁶⁷⁻⁶⁹ It explains the interactions between atoms or molecules and the surface based on adsorbate orbitals and *d*-orbitals of atoms on the surface. The energy of the *d* states (the center of the *d* states) relative to the Fermi level is a good first indicator of the bond strength. The higher the *d* states are in energy relative to the Fermi level, the higher in energy the antibonding states and the stronger the bond will be (Figure 3).

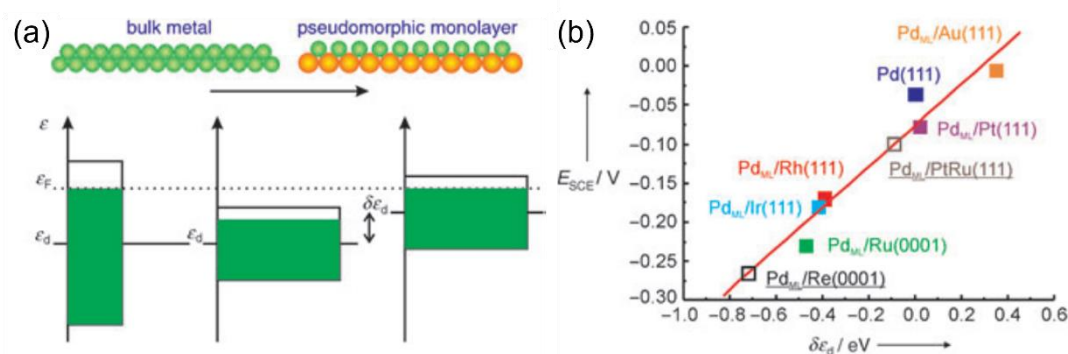


Figure 3. Illustration of the use of the *d*-band model. (a) The main origin of a shift in the *d*-band center ϵ_d is a change in the interatomic distances within an overlayer. (b) Electrochemically measured changes in the hydrogen adsorption energy (E_{SCE}) for Pd overlayers on a number of metals are shown to scale well with the calculated shift of the *d*-band center ($\delta\epsilon_d$). Reproduced with permission.⁷⁰ Copyright 2005, John Wiley and Sons.

The *d*-band center theory can also be applied on low-dimensional carbon-based

electrocatalysts.⁷¹⁻⁷⁵ For instance, Deng *et al.* designed a series of N-doped graphene-supported transition metal atom-pair catalysts (TM APCs) models for efficient NRR.⁷⁶ Twenty kinds of transition metal atoms were systematically studied and were proven by COHP and orbital interaction analysis, the *d*-band center can be used as a descriptor to describe the NRR performance of the TM APCs. For defective graphene-supported Fe and Al nanoparticles, Lim and co-workers found that the *d*-band center of the Fe and Al nanoparticles shift closer to the Fermi level, indicating a potential increase in the catalytic reactivity associated with the graphene surface. Zhou *et al.* systematically explored the HER activity of transition metals, transition metal oxides and carbides substrates covered by nitrogen-doped graphitic sheets and found that the HER activity is correlated to the C *p_z*-band center, which is similar to the *d*-band center theory and determined in turn by the degree of electronic coupling between the graphitic sheet and the metal substrate, enabling the rational design of high-performance hybrid graphitic carbon/transition metal electrocatalysts.⁷⁷

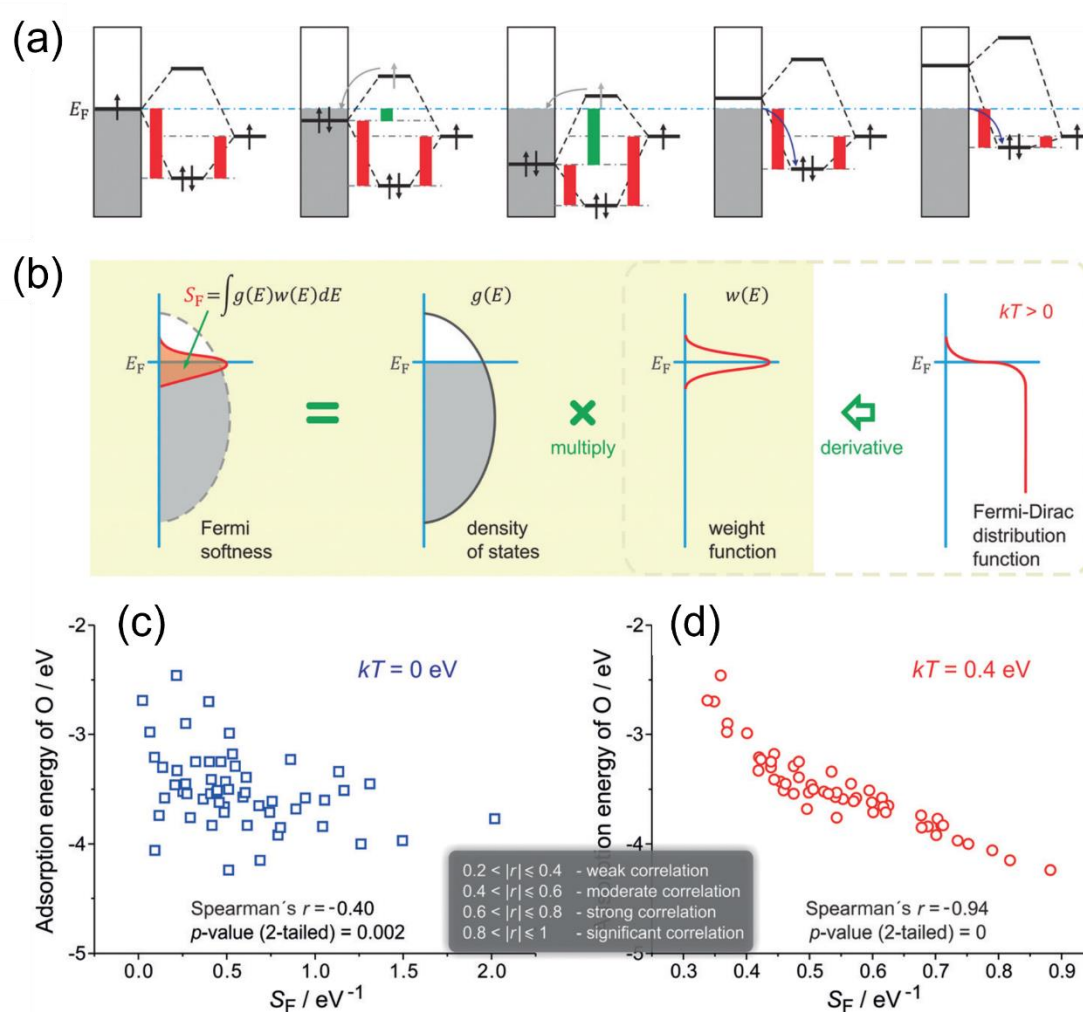


Figure 4. Definition of Fermi softness (S_F) and its correlation with surface reactivity. Reproduced with permission.⁷⁸ Copyright 2016, John Wiley and Sons.

3.1.2 Fermi Softness

When oxygen atoms adsorbed on Pt₃Y (111) surface, even though the surface d -band center of Y is higher than that of Pt, the binding strength of Pt-O is stronger than Y-O, defying the d -band center theory. However, it can be reasonably explained by the “Fermi softness” (S_F), which was developed by Huang and co-workers for describing the electronic structures of a solid surface.⁷⁸ All the band's occupied and unoccupied states contribute to the bonding, but those closer to the Fermi level (E_F) are more significant (Figure 4A). To determine a weighted summation of the density of states of a solid surface ($\int g(E)w(E)dE$), a reactivity weight function $w(E)$ with a Fermi level peak is created (Figure 4B). The resultant property is the finite-temperature chemical softness, known as S_F , which is an accurate descriptor of the surface reactivity. This property is obtained when such a weight function is defined as the derivative of the Fermi-Dirac distribution function at a certain non-zero temperature. For example, the S_F is identical to the density of states at Fermi level ($g(E_F)$) without spreading (i.e., $kT = 0$ eV), which does not closely resemble the surface reactivity (Figure 4C). Then, the S_F displays a substantial association with the surface reactivity when the nominal electronic temperature is changed to 0.4 eV (Figure 4D).

Fermi softness can also be an efficient descriptor to predict the catalytic performance of carbon-based catalysts.⁷⁹⁻⁸³ Gao and co-workers designed a series of catalysts named Fe/GS, which are composed of Fe atom serves as the active site and different graphene such as single and double vacancy graphene serves as the substrate.⁸¹ They further demonstrated that Fermi softness of Fe/GS and the O₂ adsorption energy exhibit a strong positive linear correlation ($R^2 = 0.81$) at $kT = 1.15$ eV. Fermi softness is also used to describe the adsorption activity of Mn-modified graphene catalyst by Wu's group.⁸⁴ They discovered a substantial negative correlation ($R^2 = 0.93$) between Fermi softness and adsorption energy at $kT = 2.8$ eV. The Fermi softness is increased with the increase of the adsorption energy.

3.1.3 Linear Scaling Relationships

In multi-step catalytic processes, the adsorption and desorption of the intermediates occur during the concerted proton–electron transfer steps, and the adsorption energies of the intermediates follow a linear scaling relationship.^{85, 86} For example, the relationship between the adsorption energies of the intermediates of OER and ORR, such as *O, *OH, and *OOH, can be presented by:

$$\Delta G_2^{(i)} = A_{1,2}^{(i)} \cdot \Delta G_1^{(i)} + B_{1,2}^{(i)} \quad \text{Eq. 3.1}$$

Where $\Delta G_1^{(i)}$ and $\Delta G_2^{(i)}$ represent the chemisorption energies of oxygen intermediates.^{87, 88} Fundamentally, the quantity of valence electrons of the atoms attached to the surface has a significant impact on the slope of Eq. 3.1 on closed-packed and low-index surfaces. Since the oxygen atom in OH* only requires one electron to comply with the octet rule, whereas O* requires two, the slope between the adsorption energies of *OH and *O is roughly 1/2. Scaling relationships offer a chance for using a few descriptors to fully present the numerous factors affecting a full catalytic reaction. Combined with the Sabatier principle, volcano curves can be derived from this linear relationship to reveal the connection between structures and performance. In many cases, ΔG_{OH} and $\Delta G_O - \Delta G_{OH}$ are considered as the descriptors for ORR and OER, respectively.⁸⁹⁻⁹¹ According to the statistical findings, the free energy difference for monodentate adsorbates can be concluded as $\Delta G_{OOH} = \Delta G_{OH} + 3.2 \pm (0.2) \text{ eV}$.⁸⁵

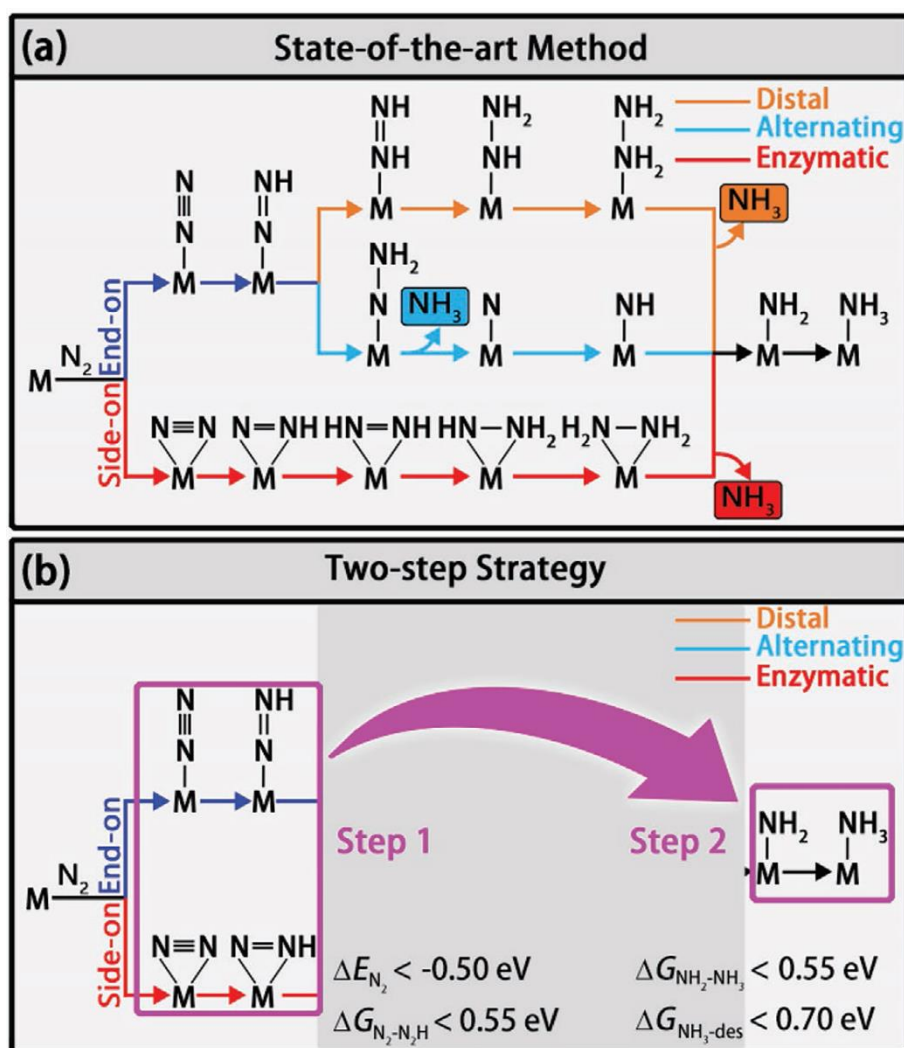


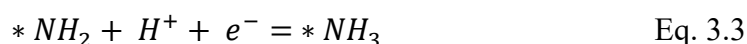
Figure 5. (a) Schematic depiction of different mechanisms for N_2 reduction. (b) Flowchart of the two-step screening procedure for NRR catalysts. Reproduced with permission.⁹² Copyright 2018, John Wiley and Sons.

3.1.4 Multiple Descriptors

The excellent descriptors include e_g -filling,^{93, 94} average O-2p-state energy ($\bar{\epsilon}_{2p}$),^{95, 96} surface distortion,⁹⁷ and generalized coordination numbers (\overline{CN}).^{98, 99} Normally, single descriptor cannot completely predict the performance and synergistic effect of complicated mixed-phase catalysts. Some interface parameters that can demonstrate or influence electron distribution reconfiguration, for instance, adsorption energy,¹⁰⁰⁻¹⁰² charge transfer,^{103, 104} surface properties (defects/microstructure/facet),^{105, 106} and bond length¹⁰⁷⁻¹⁰⁹ may serve as the descriptors to

predict the best catalysts. Furthermore, a variety of descriptors have been used for the description of the reactions with the assistance of machine learning and high-throughput calculations.

The complex NRR can occur through different mechanisms, including distal, alternating, and enzymatic (Figure 5a). To identify the viable routes and theoretical onset potentials by the classical approach, all chemical intermediates will be systematically investigated, which will be inefficient for large-scale catalyst screening. Ling *et al.* focused on two “stable to instable” transitions in the NRR process (Eq. 3.2 and 3.3) and set up a two-step method (Figure 5b) to efficiently and accurately screen the nitride-doped-graphene supported single atom catalysts (N-G-supported SACs).⁹²



In the first step, the systems with low activity are disregarded by using the descriptors ΔE_{N_2} (adsorption energy of N_2) and $\Delta G_{N_2-N_2H}$ (free energy change of Eq. 3.2). In the second step, among the systems that met the requirements of the step one, high performance catalysts are sought after using the descriptors ΔG_{NH_3-des} (free energy for NH_3 desorption) and $\Delta G_{NH_2-NH_3}$ (free energy change of Eq. 3.3). Out of 540 N-G-supported SACs systems, ten interesting candidates with high NRR catalytic activity were selected using the two-step high-throughput screen approach. For example, W_1C_3 demonstrates the best performance with an incredibly low onset potential of 0.25 V. Zhou and co-workers also used multiple descriptors to predict the NRR catalytic performance of transition metal atoms filled boron nitride nanotubes (BNNTs).⁵⁷ The diameter of BNNTs, work function and electron transfer from metal to BNNTs, which have negative correlations with the adsorption energy of N_2 , can serve as efficient descriptors to select highly active catalysts.

3.2 Application of Theoretical Calculations in Revealing the Reaction Mechanism

With the development of modern characterization techniques, an increasing number of *in situ* characterization tools are used to observe the catalytic reaction processes, aiming to accurately uncover the catalytic mechanism. However, it is still difficult to identify the actual active site

and reaction intermediates of complex catalytic reactions by pure experimental study. For example, through different reaction routes, the products of CO₂RR can be carbon monoxide, formic acid, ethylene, or ethanol. Depending on whether the adsorption sites change or not during the catalytic processes, the actual reaction paths and intermediates, the competition between carbon-carbon coupling reaction and HER are all unknown and difficult to elucidate experimentally.¹¹⁰ Theoretical calculation is a key method to compensate for experimental shortcomings because it can investigate the electronic-scale change during the catalytic reaction. In the past decades, the use of theoretical simulations in defective electrocatalysis has greatly aided the design of novel catalysts.¹¹¹⁻¹¹⁴

With the assistance of DFT calculations, Zhang *et al.* systematically investigated the origins of the high-performance atomic Co-Pt embedded into nitrogen doped graphene (A-CoPt-NC).¹¹⁵ A stable adsorption state of the intermediate in the HER is proved by the electron distribution calculations. The disappearance of charge depletion on the surface of the outer layer can improve the adsorption of protons to the catalyst. Li and co-workers synthesized a new type of high-performance HER electrocatalyst.¹¹⁶ Carbon quantum dots were used to support ruthenium nanoparticle (Ru@CQDs), and it shows superior catalytic activity and durability in alkaline conditions than the state-of-the-art commercial Pt/C catalyst. DFT calculations provide compelling evidence to the excellent HER catalytic activity of Ru supported in the N-doped CQDs layer. The calculation results show the synergistic effect of doped N atoms and Ru clusters, both are beneficial to reduce the dissociation energy of H₂O. The electron transfer from Ru and H₂O to C atoms, which is proved by the difference charge density analysis, can polarize Ru clusters, thus contributed to the dissociation of H₂O. Meanwhile, the dissociated H atoms are held together by Ru and H interactions to form the H₂ molecule (Figure 6).

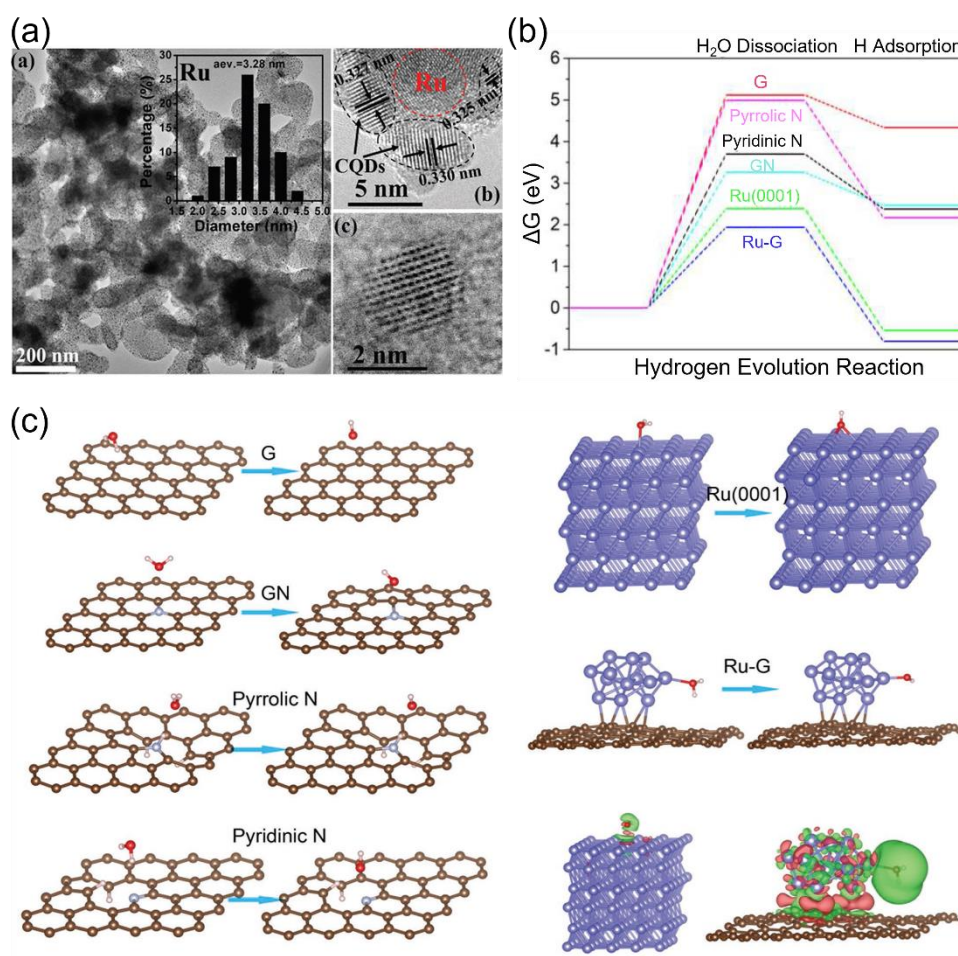


Figure 6. (a) TEM and HRTEM images of Ru@CQDs. (b) Calculated HER relative energy diagram. (c) Adsorption and dissociation of the H₂O molecule on different surfaces. Reproduced with permission.¹¹⁶ Copyright 2018, John Wiley and Sons.

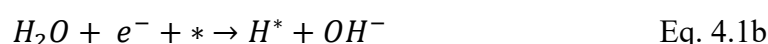
As can be seen from the above discussions, theoretical calculation is an indispensable method to investigate the relationship between structures and performance. A plausible reaction model will be built to thoroughly study the basic reaction path of the reaction and identify the crucial steps that determine the reaction rate, and then to optimize the chemical reaction conditions. It is obvious that theoretical calculations are beneficial in identifying the basic process and reaction paths of the electrocatalysis at the atomic level. Furthermore, the design of catalysts and the controlled synthesis of the desired structures can be aided by the DFT simulations, which can be utilized as a prediction tool. Theoretical modellings can also be used in catalyst structure optimization, validation of the design outcomes, and support experimental study.

4. Recent Advances in Computational Studies on Low-Dimensional Carbon-based Electrocatalysts

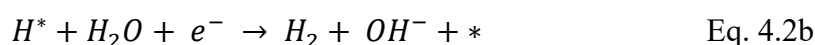
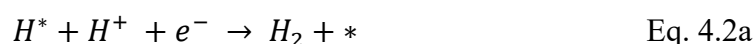
4.1 Hydrogen Evolution Reaction (HER)

Hydrogen is one of the most promising clean energy sources to replace fossil fuels, it also has the highest energy density among existing fuels. Water splitting is a sustainable way of producing hydrogen compared to industrial reduction of natural gas (CH₄). Hydrogen evolution reaction (HER) is the cathodic half-cell reaction of water electrolysis,⁷ the large overpotential restricts its practical application and high performance electrocatalysts are needed to boost the HER. Noble metal-based catalysts such as Pt/C and RuO₂ are commonly considered to be the most efficient HER electrocatalysts, however, the scarcity and low durability limit their mass industrial production.^{117, 118} To date, many high performance low-dimensional carbon-based non-noble metal even metal-free electrocatalysts have been designed and fabricated to be the alternatives of noble metal materials. In this part, the fundamental concepts and recent development on HER electrocatalysts will be summarized.

HER is a two proton-electron transfer steps (PETS) process, the first step is Volmer reaction, i.e., the adsorption of hydrogen, which can be present by Eq. 4.1a (acidic condition) and 4.1b (alkaline condition).



The second step can be the Heyrovsky reactions or Tafel reaction, Eq. 4.2a (acidic condition) and 4.2b (alkaline condition) show the Heyrovsky reactions, and Eq. 4.3 show the Tafel reaction.



In which, * represents the active site on the catalyst surface.

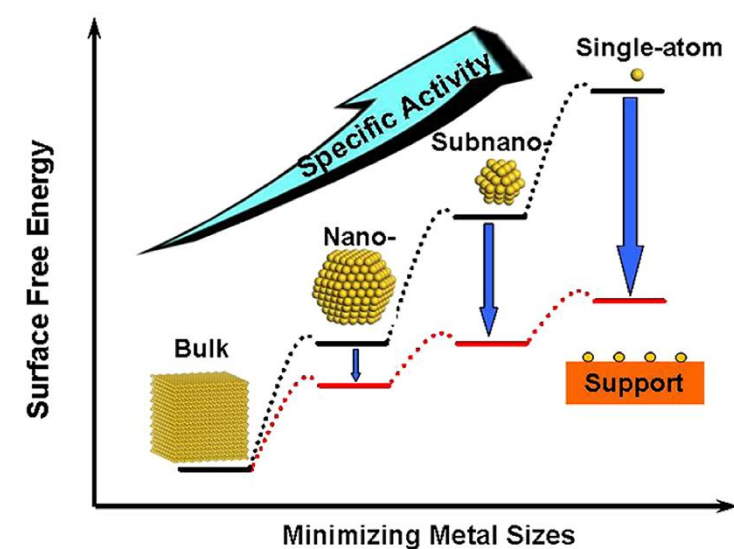


Figure 7. Schematic illustration of the changes of surface free energy and specific activity per metal atom with metal particle size and the support effects on stabilizing single atoms. Reproduced with permission.¹¹⁹ Copyright 2013, American Chemical Society.

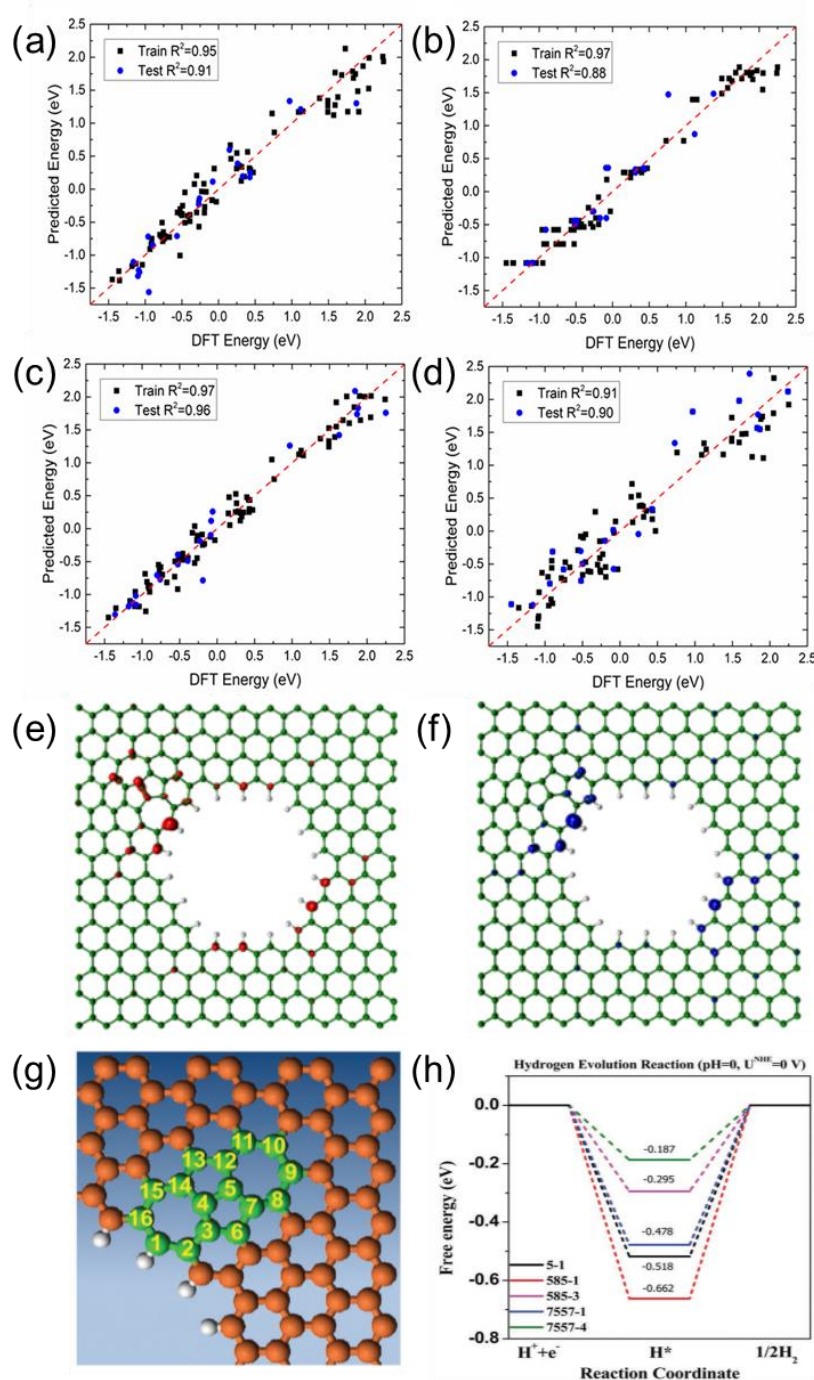


Figure 8. Comparison of DFT calculated versus machine learning predicted ΔG_H using (a) kernel ridge regression, (b) random forest regression, (c) neural network regression, and (d) SISSO regression. Reproduced with permission.¹³¹ Copyright 2020, American Chemical Society. (e) HOMO and (f) LUMO orbitals for 7557 defect. (g) Mechanism study model of 7557defect. (h) Schematic energy profiles for the HER pathway. Reproduced with permission.¹⁶ Copyright 2016, John Wiley and Sons.

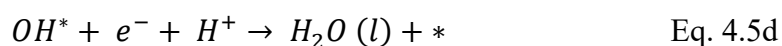
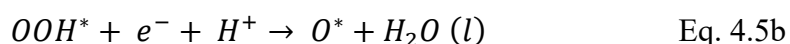
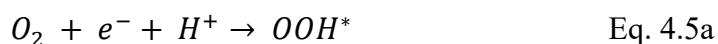
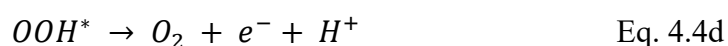
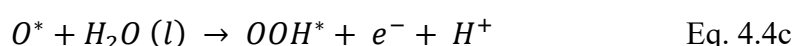
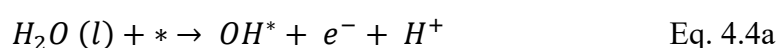
For the design of low-cost and efficient electrocatalysts, it is crucial to reduce the amount of precious metals being used, which can be achieved in two ways. Firstly, the specific activity per metal atom usually increases with the downsize of metal particles (Figure 7).¹¹⁹ Therefore, a new kind of electrocatalyst called single-atom catalyst (SAC), which contains isolated metal atoms singly dispersed on supports, has attracted extensive research attentions. Alternatively, non-noble metal atoms or functional groups can also be anchored on the substrate to tune the electronic structures of noble-metal active sites.¹²⁰⁻¹²⁴ Ye and co-workers designed a novel Pt SAC, using aniline-stacked graphene as the support (Pt SASs/AG). It shows excellent HER performance with $\eta = 12$ mV at 10 mA cm^{-2} and a mass current density of $22400 \text{ Ag}_{\text{Pt}}^{-1}$ at $\eta = 50$ mV, which is 46 times higher than that of the commercial 20 wt% Pt/C.¹²⁵ Moreover, the Pt SASs/AG catalyst presents outstanding stability. With the assistance of DFT calculations, they found that the interaction between the atomical Pt and the nitrogen of aniline makes the *d*-band center of Pt downshift to -2.465 eV, which is close to that of Pt (111) (-2.687 eV). Additionally, the density of states (DOS) near the Fermi level of Pt in Pt SASs/AG catalyst is as large as that of the Pt in Pt (111), eventually promoted the HER activity.

Secondly, non-noble metal atoms such as transition metals are used to replace noble metals for preparing efficient HER catalysts, and even metal-free catalysts with excellent performance were designed and synthesized experimentally.^{24, 126-130} For example, using the first principle DFT calculations, 3D, 4D, and 5D transition metal SACs in N-doped 2D graphene and nanographene of various sizes are screened for HER by Fung *et al.*¹³¹ For most SACs, a *d*-band center downshift will occur when moving from graphene to nanographene, indicating that the hydrogen adsorption on metal SACs can be tuned by adjusting the size and dimension of the substrate. V, Rh, and Ir embedded on N-doped nanographene show much better HER activity than those on the extended 2D graphene. The machine learning models (kernel ridge regression, decision trees (random forest), and neural networks) and SISO (Sure Independence Screening and Sparsifying Operator) method are employed to accurately predict the ΔG_H using various proposed descriptors, the results are shown in Figure 8 (a) to (d). Topological defect-based and complex defect-based carbon materials are also promising electrocatalysts. Yao and co-workers synthesized a series of defective carbons *via* a facile nitrogen removal procedure from N-doped graphene, and the edge-defect model called 7557-4 shows outstanding HER performance with the lowest calculated free energy of 0.187 eV (Figure 8 (g) and (h)).¹⁶ DFT calculations were also performed to better understand the underlying catalytic mechanisms. The analysis of the frontier molecular orbitals shows that the catalytic activity of edge atoms is laid on their most

contribution to the highest occupied molecular orbital (HOMO) and lowest unoccupied molecular orbital (LUMO), which are highly correlated with the catalytic reactions (Figure 8 (e) and (f)).

4.2 Oxygen Evolution Reaction (OER) and Oxygen Reduction Reaction (ORR)

Oxygen evolution reaction (OER, $2H_2O(l) \rightarrow O_2(g) + 4e^- + 4H^+$) is the anode half-cell reaction of water splitting containing 4 electron transitions, as shown in Eq. 4.4. Oxygen reduction reaction (ORR, $O_2(g) + 4e^- + 4H^+ \rightarrow 2H_2O(l)$, Eq. 4.5) is the reverse reaction of the OER, which is the cathodic reaction of fuel cells and zinc-air batteries.¹³²



Both the OER and ORR are restricted by the slow kinetic and high reaction energy barriers, thus electrocatalysts are needed to accelerate the reaction rate and improve the efficiency. However, the high cost and low abundance of current commercial noble-metal-based catalysts, i.e., Pt/C for ORR, RuO₂ and IrO₂ for OER severely hinder their widespread applications. Similarly, the strategies of lowering the cost and improving the performance of the HER catalysts are also applicable to the OER and ORR electrocatalysts, and great achievements have been achieved.^{60, 133-137} Zhang *et al.* anchored atomically distributed Ni atoms onto N-doped hollow carbon matrix (HCM@Ni-N).¹³⁸ In alkaline conditions, the HCM@Ni-N only requires

an OER overpotential of 304 mV to reach the current density of 10 mA cm^{-2} , which is much lower than that of the RuO_2 (393 mV), suggesting excellent OER activity of the prepared catalyst. Through the calculated distributions of charge density, they found that the electronic distribution of N-doped HCM was changed obviously after the Ni decoration (Figure 9a). At the same time, under the influence of Ni-N interaction, the $3d$ orbital of Ni in HCM@Ni-N shows a leftward shift and the d -band center of the Ni was downshift from -0.94 eV to -2.04 eV (Figure 9b). According to the d -band center theory, this change could facilitate the desorption of adsorbates and reduce the energy barrier. The free energy pathways of the OER can also be calculated by DFT simulations and they are in good agreement with the experimental results (Figure 9c and d). By encapsulating Co and $\beta\text{-Mo}_2\text{C}$ into N-doped carbon nanotubes ($\text{Co}/\beta\text{-Mo}_2\text{C}@\text{N-CNT}$), Ouyang and co-workers successfully fabricated a bifunctional electrocatalyst for the HER and OER in an alkaline electrolyte.¹³⁹ Based on the heterointerface between Co and $\beta\text{-Mo}_2\text{C}$, the OER activity of $\beta\text{-Mo}_2\text{C}$ is enhanced significantly. With the assistance of DFT calculations, they proved that the cooperation of N-CNTs, Co and $\beta\text{-Mo}_2\text{C}$ resulted in the low energy barriers of the intermediates, thus greatly improved the HER and OER kinetics.

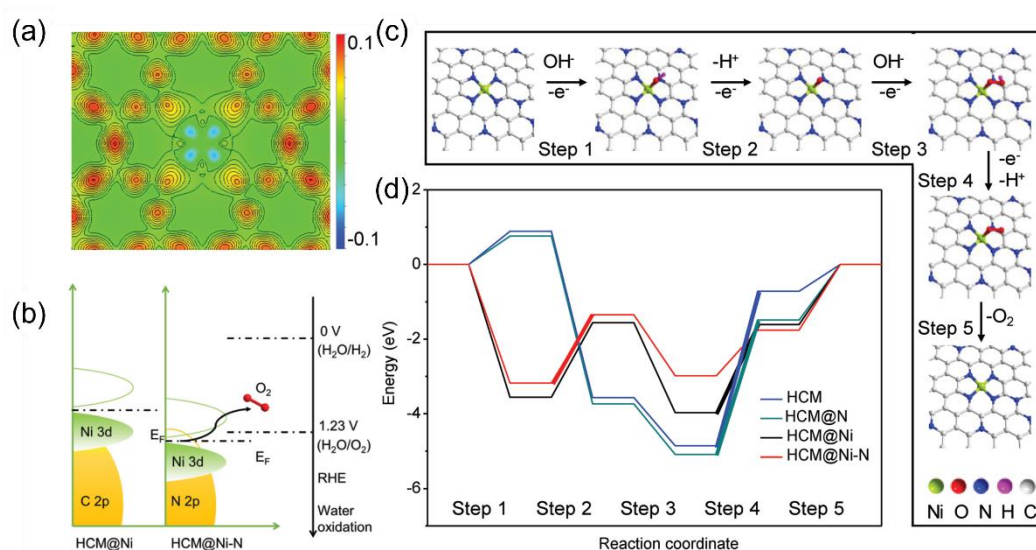


Figure 9. (a) Calculated distribution of charge density for HCM@Ni-N. (b) Schematic band diagrams of HCM@Ni and HCM@Ni-N. (c) Proposed mechanism of O_2 evolution over HCM@Ni-N. (d) Free energy diagram at 0 V for OER over HCM, HCM@N, HCM@Ni, and HCM@Ni-N. The bold lines indicate the rate-determining step. Reproduced with permission.¹³⁸ Copyright 2019, John Wiley and Sons.

Under the guidance of DFT calculations, Wang *et al.* successfully synthesized a series of topological carbon defects through a facile N-removing strategy, among which adjacent pentagons (A-C5) show the best catalytic performance for the ORR and the edge divacancy defects (C585-2) are favourable for the HER.¹⁴⁰ DFT calculations were applied to investigate the relationship between the original carbon structure, the type of N configuration obtained, and the corresponding defect structures, for example, perfect carbon network versus graphitic-N versus C585 (Figure 10 a), edge-rich hexagonal structure versus pyridinic-N versus S-C5 (Figure 10 b), and edge-rich pentagon versus pyrrolic-N versus A-C5 (Figure 10 c). By a spontaneous gas-foaming method, Jiang and co-workers fabricated a range of promising trifunctional electrocatalysts called defect-rich N-doped ultrathin carbon nanosheets for HER, OER and ORR.¹⁴¹ In rechargeable Zn-air batteries, NCN-1000-5 exhibits a high energy density (806 W h/kg), a low charge/recharge voltage gap (0.77 V) and extremely long cycle life (over 300 h). DFT calculations were used to identify the intrinsic active sites for the electrochemical reactions. The catalytic performance of various active sites for the ORR and OER were investigated, the results are shown in the volcano plot (Figure 10 d). The armchair edge carbon atoms, which are adjacent to the graphitic-N, possess the lowest overpotential, thus they should be the optimal catalytic active center for the specific electrocatalysis (Figure 10 e-g).

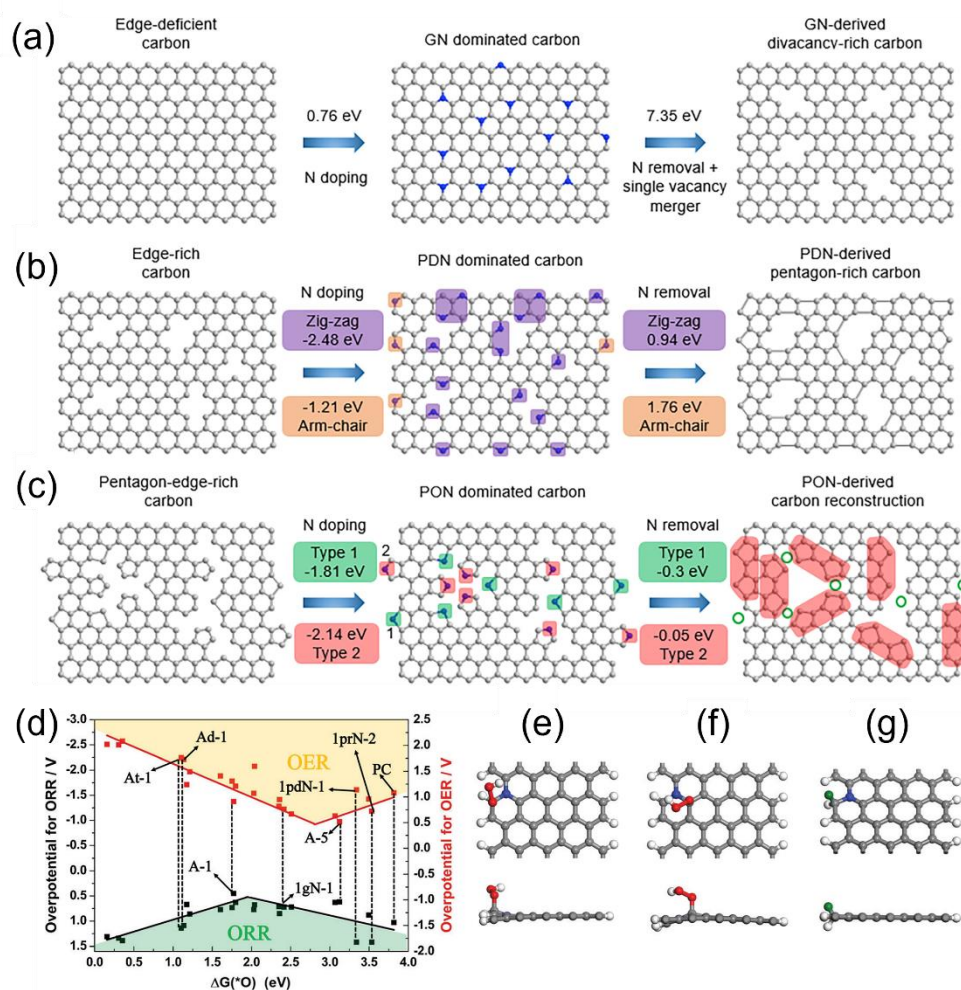
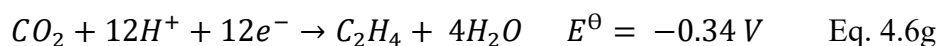
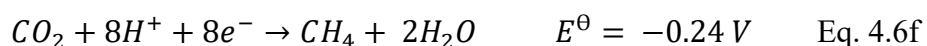
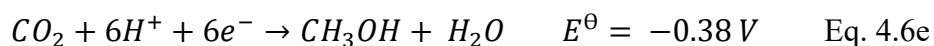
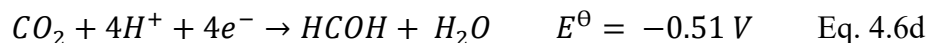


Figure 10. Computational simulation of specific N-doping and removing process in different carbon models: (a) Schematic and formation energy calculation of transformation from edge-deficient carbon to GN dominated carbon and then to divacancy-rich carbon. (b) Schematic and formation energy calculation of transformation from edge-rich carbon to PDN dominated carbon and then to pentagon-rich carbon. (c) Schematic and formation energy calculation of transformation from pentagon-edge-rich carbon to PON dominated carbon and then to special carbon reconstruction. Reproduced with permission.¹⁴⁰ Copyright 2020, Elsevier. (d) The volcano plot for the ORR and OER by plotting the overpotential as a function of $\Delta G(*O)$ at various possible active sites. The top and side views of the active site (e) A-1 for the ORR, (f) A-3 for the OER with OOH adsorbed, and (g) A-1 for the HER, the green ball representing the adsorbed H ($\theta = 2.27\%$). Reproduced with permission.¹⁴¹ Copyright 2008, Royal Society of Chemistry.

4.3 Carbon Dioxide Reduction Reaction (CO₂RR)

Carbon dioxide reduction reaction (CO₂RR) could convert CO₂ to many value-added chemical compounds, such as CO, CH₄, CH₃OH, and C₂H₅OH (Eq. 4.6),^{142, 143} which can be directly used as fuels to replace fossil fuels like gasoline and natural gas. Therefore, the CO₂RR may be regarded as the reverse reaction of the fossil fuel combustion and can significantly relieve the greenhouse effect. However, the hydrogen atoms necessary for the reduction of CO₂ molecule are transported from the aqueous solution, so the HER must be considered as the competitive reaction. High cost of the currently used noble metal-based catalysts and the low selectivity of CO₂RR are still the biggest obstacle for its industrialization. Therefore, developing highly efficient and selective non-noble metal CO₂RR catalysts based on earth abundant elements has attracted the most attention in this promising research field.¹⁴⁴⁻¹⁴⁹



The initial stage of CO₂ reduction is CO₂ adsorption, which is crucial step of the CO₂RR. Zhu *et al.* systematically investigated the adsorption of CO₂ on g-C₃N₄ surface by DFT calculations.¹⁵⁰ Through analyzing the electronic properties such as the band gap, density of states, work function, HOMO and LUMO, they proved that the two-coordinated N atoms, which contributed to both valence band and conduction band edge, have the most negative adsorption energy (-0.4181) for CO₂ molecule. CO₂ can be effectively captured and activated on Si due to the "acceptance and back-donation" of electrons between the Si dopant and CO₂ molecule. Accordingly, Mao and co-workers designed an experimentally synthesizable electrocatalyst called silicon-doped graphene edges (Si chain@G).¹⁵¹ The catalytic performance of the Si@ZZG (Si atoms doped into the zigzag edge of graphene) and Si@ACG (Si atoms

doped into the armchair edge of graphene) was exhaustively studied through DFT calculations (Figure 11a). CO₂ can be well captured and efficiently activated on Si@G, the binding energy at the zigzag and armchair edges is -0.65 eV and -0.83 eV, respectively. Remarkably, CO₂ can be converted to CH₃OH effectively when the Si@ACG was served as the active sites (Figure 11c). Moreover, Si chain@G with multiple Si active sites which are beneficial to product multiple-carbon productions was also investigated. They found that the Si chain@ZZG has a high selectivity to transform CO₂ to C₂H₅OH with an extreme low limiting potential of -0.6 V under the optimal theoretical reaction pathway (Figure 11b).

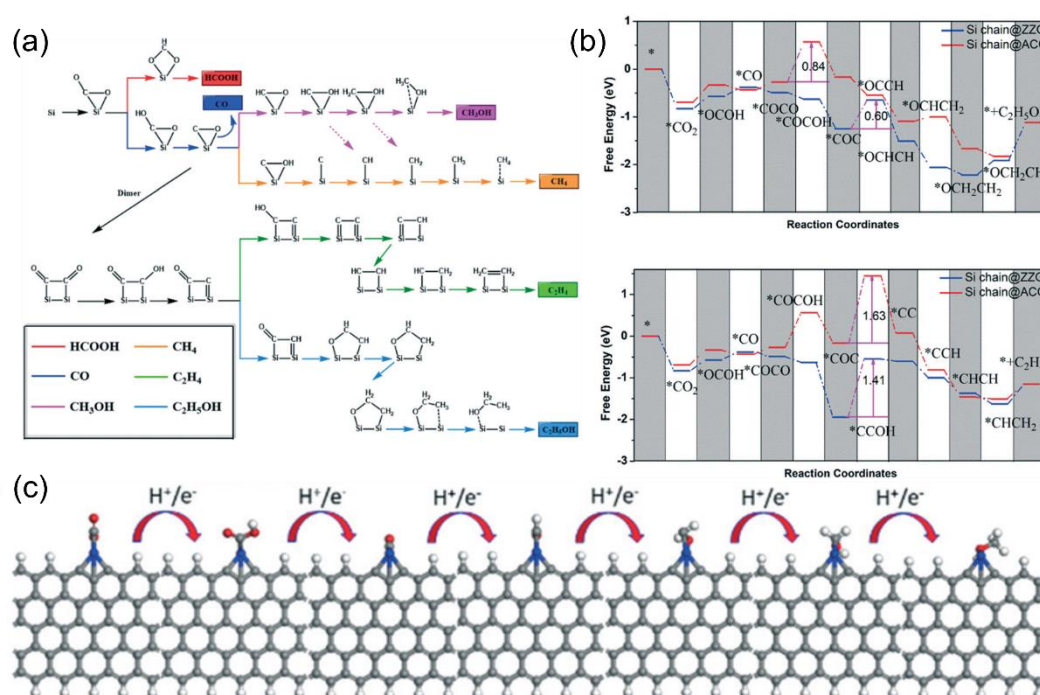


Figure 11. (a) Possible reaction pathways for the electrocatalytic reduction of CO₂ to six different products. (b) Gibbs free energy diagrams of CO₂ reduction reactions to CH₃OH and C₂H₄ on Si chain@ZZG and Si chain@ACG. (c) The optimised structures for CO₂ reduction to CH₃OH on the zigzag edge. Reproduced with permission.¹⁵¹ Copyright 2011, Royal Society of Chemistry.

Transition metal atoms can also be excellent CO₂RR active centers. Guo *et al.* established calculation models with Fe, Co and Ni single atoms embedded onto graphitic carbon nitride (Fe/Co/Ni-C₃N₄) and systematically investigated the structures of the electrocatalysts, CO₂ adsorption configurations and the reduction mechanisms.¹⁵² g-C₃N₄ with six-fold cavities was

selected as the substrate, the introduced Ni, Co, and Fe atoms are located from the corner to the center of the cavity. The PDOS of the metal d orbital and adsorbed CO_2 indicated that CO_2 could be chemically adsorbed on $\text{Co-C}_3\text{N}_4$ and $\text{Fe-C}_3\text{N}_4$, but physically adsorbed on $\text{Ni-C}_3\text{N}_4$ (Figure 12a and b). Guo also probed the reaction pathway and mechanism of different C1 products and thoroughly calculated the limiting potentials for the productions of CO, HCOOH, CH_3OH , and CH_4 . They found that $\text{Co-C}_3\text{N}_4$ has superior CO_2RR activity and selectivity for CH_3OH (Figure 12c). Currently, copper (Cu) is found to be one of the best catalysts for achieving the high activity reduction of CO_2 to hydrocarbons since $^*\text{CO}_2$ and $^*\text{COOH}$ can be effectively collected from Cu-based catalysts.¹⁵³ Due to the hydration of non-adsorbing CO_2 molecules, Pb, Hg, Cd, and Bi also demonstrate good catalytic performance for producing formate.¹⁵⁴ Other transition metals such as Ni, Fe, Pd, and Ti exhibit low CO_2RR selectivity because the HER is much favourable due to the strong H-bonding.¹⁴⁹

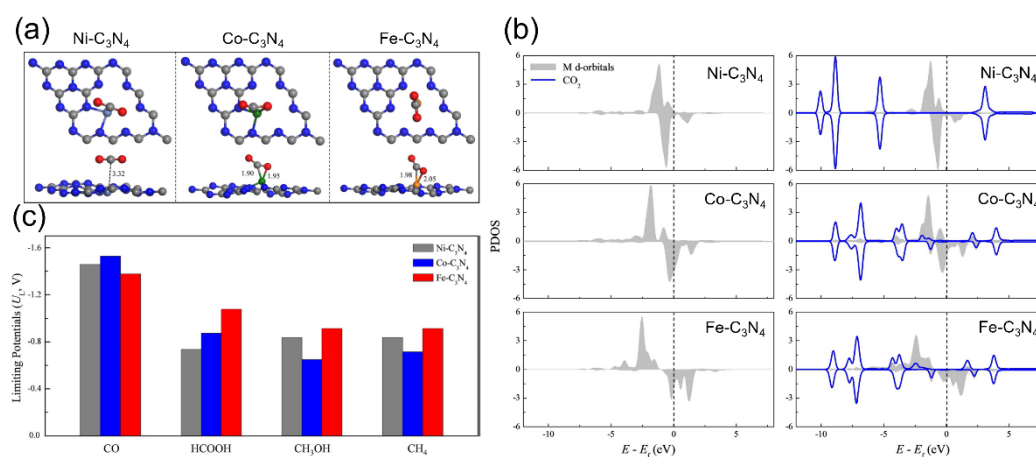


Figure 12. (a) The most stable CO_2 adsorption configurations. (b) PDOS of the metal d orbital before and after adsorption (including the adsorbent CO_2 total DOS). (c) Summary of the limiting potentials for the productions of CO, HCOOH, CH_3OH , and CH_4 . Reproduced with permission.¹⁵² Copyright 2019, John Wiley and Sons.

4.4 Nitrogen Reduction Reaction (NRR)

Nitrogen is the most abundant element in the earth and it is essential for all the organisms such as animals and plants. Ammonia (NH_3) is one of the most important industrial compounds due to its wide use in different fields. However, the ultra-stable $\text{N}\equiv\text{N}$ triple bond greatly impedes the nitrogen fixation reaction. The industrial Haber-Bosch process uses N_2 and H_2 as the raw

materials, consuming excessive energy because of the high reaction temperature (350-550 °C) and pressure (150-350 atm).^{155, 156} Therefore, the conversion of N_2 to NH_3 under ambient conditions is a promising research area. Recently, electrocatalytic nitrogen reduction reaction (NRR) has attracted increasingly research attentions because of its obvious advantages such as low energy consumption, reduced reaction temperature, and enhanced productivity.¹⁵⁷⁻¹⁶⁴ Figure 13 shows the possible reaction pathways of the catalytic conversion of N_2 to NH_3 .

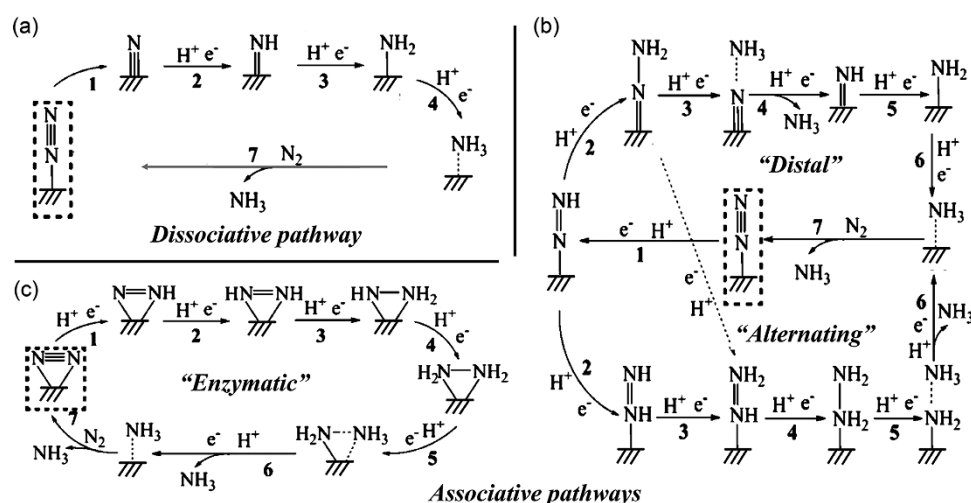


Figure 13. Schematic depiction of the dissociative pathways and the associative pathways (including distal, alternating, and enzymatic pathway) for catalytic conversion of N_2 to NH_3 . Reproduced with permission.¹⁵⁷ Copyright 2016, American Chemical Society.

The first and also an important step of the NRR is the adsorption of N_2 to the active sites, which requires the atoms contain not fully occupied orbitals to accept the lone-pair electrons from the σ orbital of N_2 . Therefore, transition metals would be excellent electron acceptors due to their half-occupied d orbitals and have the potential to be promising NRR electrocatalysts.¹⁶⁵⁻¹⁶⁷ Ling and co-workers established a computational model which anchored Mo atoms onto N-doped carbon ($Mo_1-N_1C_2$) and investigated its NRR catalytic performance using the first principle calculations.¹⁶⁸ Firstly, the bonding energy of N_2 adsorbed on $M_1-N_1C_2$ ($M = Cu, Pd, Pt$, and Mo) is investigated, only $Mo_1-N_1C_2$ shows strong adsorption of N_2 with the adsorption energy of -1.19 and -1.18 eV for side-on and end-on adsorption, respectively. In addition, the $N\equiv N$ bond length has increased from 1.12 Å (isolated N_2 molecule) to 1.18 Å (side-on) and 1.14 Å (end-on) (Figure 14 a-c). Accordingly, Mo is selected as the potential electrocatalyst, and the

possible reaction pathways are calculated. As shown in Figure 14 d, Mo₁-N₁C₂ has an extreme low overpotential of 0.24 V and can catalyze the NRR through an enzymatic pathway. It is worth noting that the generated NH₃ can be removed quickly from the Mo₁-N₁C₂ catalyst with a free-energy uphill of only 0.47 eV, which is significantly lower than that of the previously reported catalysts.

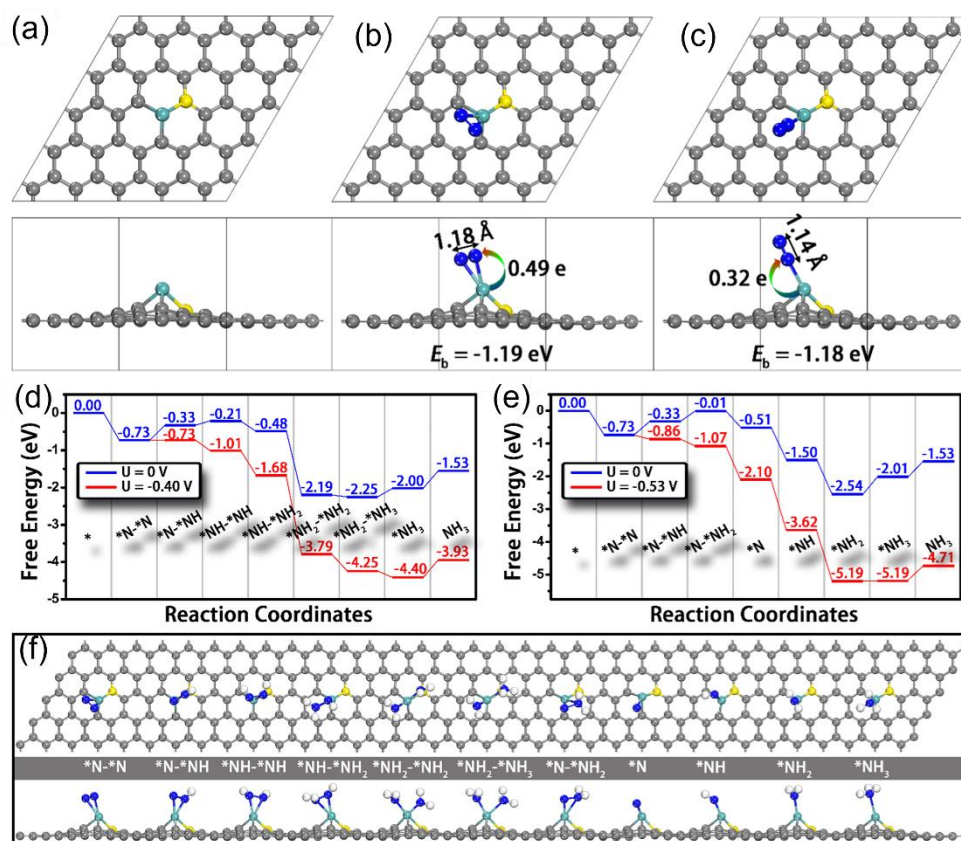


Figure 14. Top and side views of the structures of (a) Mo₁-N₁C₂, Mo₁-N₁C₂ with N₂ adsorption through (b) side-on and (c) end-on patterns. N-N bond lengths and charge transfer from Mo₁-N₁C₂ to N₂ are also presented. Free-energy diagrams for N₂ reduction through (d) enzymatic and (e) consecutive mechanisms at different applied potential as well as (f) the corresponding structures of the reaction intermediates. Gray, cyan, yellow, and blue balls represent the C, Mo, doped N, and adsorbed N atoms, respectively. Reproduced with permission.¹⁶⁸ Copyright 2018, American Chemical Society.

In recent years, metal-free catalysts have also emerged as an important category of electrocatalysts for ammonia formation. Boron (B) has the potential to be used in NRR

processes because of its Lewis acid-like characteristics and electron-deficient, which is different from other main group elements. The outer orbital of B undergoes hybridization to produce sp^2 orbitals, which can accept electron from the N_2 σ -bond and donate electron from the filled $2p$ orbitals to the antibonding π^* -orbitals of N_2 . This finding has been supported by a number of recent investigations.¹⁶⁹⁻¹⁷¹ For instance, Yu's group reported that B doped graphene could effectively catalyze the NRR with a very high Faradic efficiency of 10.8% for NH_3 production in aqueous solutions under ambient conditions at -0.5 V (versus RHE), with the electron redistribution at the active site constituting the reduction process.¹⁷¹ However, the theoretically calculated overpotential remains very high, so there is still a great need for more suitable substrates to sustain B atoms. In addition, the detailed mechanism of the N_2 activation and reduction for non-metallic catalysts is yet to be uncovered, suggesting that new methods of nitrogen capture and activation should be exploited to increase the efficiency of the nitrogen fixation.

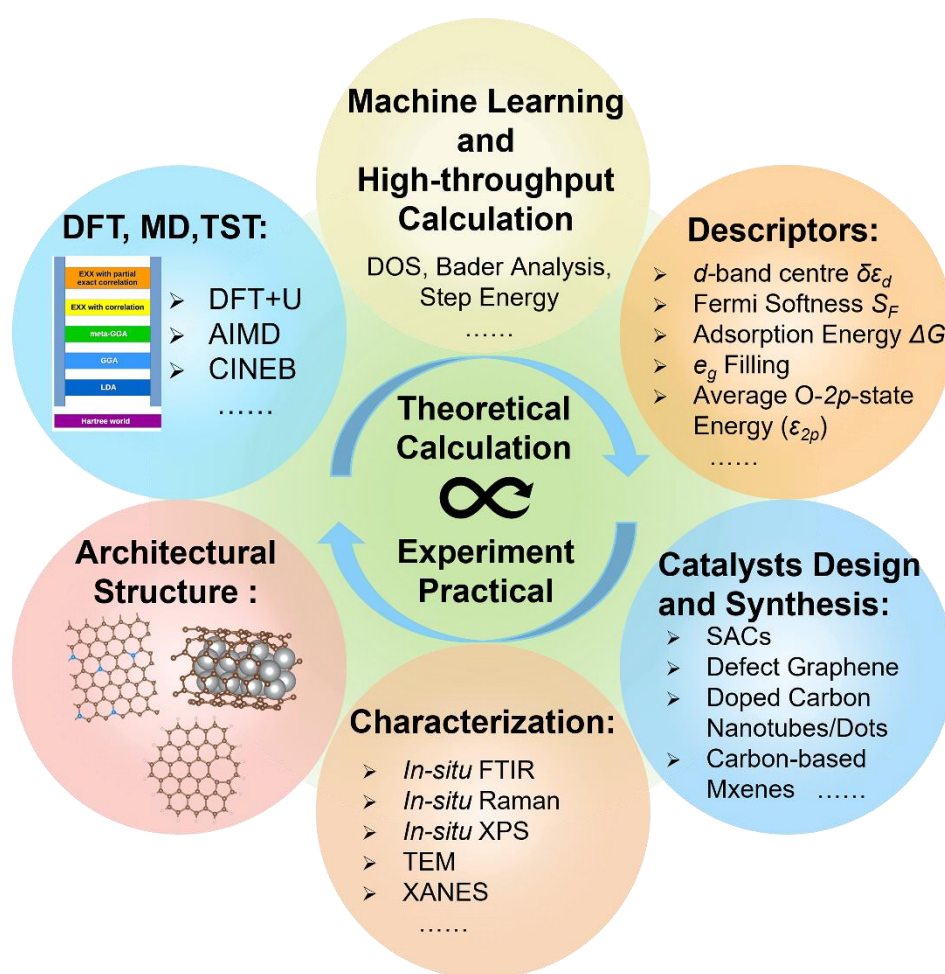


Figure 15. Schematic illustration showing the combination of theoretical calculations and experimental studies.

5. Conclusions and Outlook

In summary, we have briefly introduced the development of modern DFT, and reviewed the application of theoretical calculations such as descriptors suit in material screening and mechanism investigating in carbon-based heterogeneous catalysts. Afterward, recent achievements of carbon-based electrocatalysts were presented. As shown in Figure 15, the development of supercomputer technology improves the accuracy of the theoretical calculations. With the assistance of machine learning and high-throughput computing, the prediction and screening ability of computational simulation has gradually enhanced and become more closely integrated with experimental work. Besides, DFT calculations can simulate more realistic reaction environment and material structures, which could improve the efficiency and accuracy of the mechanism explanation. Particularly, low-dimensional carbon-based materials have demonstrated a tremendous potential in the field of electrocatalysis due to their distinctive features, including 1) diverse and controllable structures as well as excellent environmental tolerance; 2) inherent substrate materials can be easily doped by heteroatoms; 3) various defects can serve as the active sites. However, severe limitations in the rational design and practical use of carbon-based electrocatalysts still exist. More universal, accurate and measurable descriptors should be developed, and additional research attention should be focused on the synthesis of catalysts. The following important issues and challenges deserve further investigations.

- (1) Microkinetic modelling is a bridge that can connect quantum-chemical data with macroscopic behaviours in surface reactions. However, most attention has been focused on the analysis of the reaction energy and thermodynamics, more advancements in kinetic modelling are needed to fully comprehend the relationships between coverage, potential dependency of activation energies, adsorbate-adsorbate interactions, and pH effects.
- (2) Existing theoretical approaches and functionals describing interface charge cannot meet the requirement of evaluating kinetics and reaction barriers of elementary steps under realistic reaction environments. For example, the widely used CHE model does not yet consider the non-electrochemical processes, proton-electron transfer, or the recombination of electrons and holes. For interfacial catalytic processes, multiscale modelling can facilitate the understanding of the transport effects.

- (3) The combination of multiple descriptors to effectively describe the relationship between structures and performance is required since it may be impossible to accurately predict the activity trends of complicated multi-phase catalysts only using one descriptor. Importantly, machine learning and high-throughput calculations should be valued to uncover more general descriptors and new reaction mechanisms.
- (4) The synthesis of electrocatalysts with abundant active sites is also crucial, for instance, the formation process of specific defect structures, the synthesis of SACs with specific density are yet to be improved. Theoretical scientists have been focusing on improving the activity of electrocatalysts. However, rational design and synthesis strategies for large-scale production of carbon-based electrocatalysts are also one of the stumbling blocks for practical applications. More attention should be focused on the synthesis of electrocatalysts with targeted structural characteristics for a specific reaction.
- (5) Scaling relationship between oxygen adsorbates in OER, ORR, and CO₂RR has the possibility to develop efficient descriptors. However, it also restricts the lowest overpotential of electrocatalytic reactions, for example, the predicted lowest overpotential is (3.2–2.46) eV/2e \approx 0.4 V for both ORR and OER. Therefore, how to break the scaling relationship is also a prospective research topic in the near future.

Conflict of Interest

The authors declare no conflict of interest.

Acknowledgements

The authors would like to thank Australian Research Council (ARC DP200103043) for financial support during this work.

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