Light Dispersion in Gravitational Field

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Abstract: In any region of a space, the gravitational field cannot be eliminated. The speed of light in a vacuum has never been observed and cannot be observed with current technology. Till now, only the speed of light in a gravitational field has been observed. Here, it is presented that light could be dispersion in a gravitational field analogous to the dispersion of light in the Newtonian prism experiment. The relativistic mass density on the surface of a neutron star is on the level of $10^{17} \mathrm{kg} m^{-3}$ while on the surface of the Earth is only $6.63 \times 10^{-7} \mathrm{kg} m^{-3}$, the speed of light acted by the gravitational field of a neutron star is much larger than that by the Earth. Therefore, light dispersion in strong gravitational field could be generally observed from the picture of a star and it should have been observed through the spectroscopic binary system.

Keywords: dispersion of light; gravitational field; fundamental physics constant; vacuum; speed of light; spectroscopic binary system

1. Introduction

In the Maxwell equations, the speed of light is expressed as

$$c = \frac{1}{\sqrt{\varepsilon_0 \mu_0}} \tag{1}$$

ε_0 and μ_0 are the electric constant and magnetic constant in a vacuum. Partly for the Maxwell equations and partly for Einstein's theory of relativity, in current physics, a very special role has been given to the speed of light from 1900s. It is believed, in the vacuum, the speed of light is a constant $c = 3 \times 10^8 m/s$ which is the fastest speed in the universe. But, now, it was observed that the mass density of the gravitational field on the surface of the neutron star can be larger than the density of the neutron star which is almost $10^{17} \mathrm{kg} m^{-3}$. [1] It is clearly unsuitable to treat a space filled with a field with a relativistic mass density of $10^{17} \mathrm{kg} m^{-3}$ as a vacuum. And, now, we cannot make the gravitational field eliminated from a space. So, we cannot have a vacuum which is radically "empty". No vacuum does exist in our real world. Therefore, the speed of light need be understood with that it is always being acted by a gravitational field. The neutron stars can bend the light emitted on their far side around towards the front of the star.[2] The motion of a light in a super strong gravitational field is radically different from that in a weak field. Therefore, the action of the strong gravitational field on the speed of light need be studied to have a better understand for the speed of light. Here, it is presented that light should be dispersion in gravitational field. And, the action of the centripetal force of the field on the speed of light is discussed.

2. Result

Light dispersion in general medium was well studied. The speed of light in the medium can be written as

$$\frac{c}{n} = \frac{1}{\sqrt{\varepsilon_r \mu_r}} \tag{2}$$

Where, c is the speed of light measured on the Earth, n is the refractive index, ε_r and μ_r are the electric constant and magnetic constant in a medium. (Note: c is also called the speed of light in a vacuum. The current concept of vacuum is presented by Torricelli in 1643.[3] In this vacuum, the gravitational field is not eliminated.) From the Newton's prism experiment, we know, for a material with a certain ε_r and μ_r, the refractive indexes n are different for the light ray with different frequencies.

By analogy to other medium, it could be assumed that the electric constant and magnetic constant are different in the gravitational fields with different field strength. Therefore, Equation (1) can be rewritten as

$$c_l = \frac{1}{\sqrt{\varepsilon_l \mu_l}} \tag{3}$$

Where, l indexes the location. It means that for the location around the Earth, the speed of light is $c = \frac{1}{\sqrt{\varepsilon_0 \mu_0}} = 3 \times 10^8 m/s$ while around a neutron star, the ε_l and μ_l are different which results in that the speed of light is no longer $c = 3 \times 10^8 m/s$.

Diffraction is produced from the property of wave, including sound wave, electromagnetic radiation, and small moving particles.[4] The Huygens' principle[5] told us that as a plane wave is propagated from one medium into another one, this wave is refracted for that there is a time delay between different sides of the wavefront. Therefore, refraction of light is due to the wave propagation. As a light enters a strong gravitational field from a vacuum (or a weak field), the Huygens' principle shall certainly function. A refraction is produced in this process. In addition, a gravitational field can make light redshift and bent. It clearly shows that the motion of a light is changed as it enters a gravitational field.

Dispersion had been studied for a long history.[6] Cauchy, Briot, Hartmann, Corady and Sellmeier presented the dispersion formula. It showed that, for a given material, the refraction index is only determined with the wavelength of the light.

Therefore, light dispersion in a gravitational field is such a result that only is produced by the property of wave propagation which can be well understood with classic physics.

The dispersion in gravitational field could be observed from the picture of a star with a strong field. For convenience, here, only the simplest case that the light ray is vertical to the surface of the media is studied. In the case, there is not refraction for the light. As the light emitted by a star is running through the gravitational field of the star, under the condition that the field is uniform, the light cannot be refracted by the field.

It is well known, for a star with a distance L relative to the observer, this star at the present position and at the present time t cannot be observed for that a time $t - t' = L/c$ is needed for the light running from the star to the observer. Therefore, it only can be observed at the retarded time $t' = t - L/c$ and at the retarded position which, at the retarded time, the star is at. Therefore, the observed picture of the star is that the star is at the retarded position and at retarded time.

In a medium, the speed of light is determined with $c_\omega = \frac{c}{n_\omega}$, where ω is the frequency of the light. Because of dispersion, for the speed of the light with different frequencies, the retarded time is determined with

$$t_\omega = n_\omega L/c \tag{4}$$

In Equation (4), n_ω is with different value. Therefore, under the condition of dispersion, there shall be two (or more) retarded positions for a star as shown in the Figure 1.

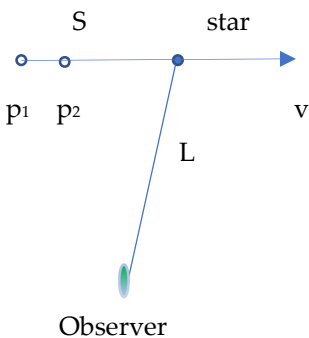



Figure 1. The double retarded positions of a star. A star is moving along the velocity v. p_1 is the first retarded position of the star which is determined with $t_{\omega 1} = n_{\omega 1}L/c$. And, p_2 is the second retarded position which is determined with $t_{\omega 2} = n_{\omega 2}L/c$. S is the distance between the two retarded positions p_1 and p_2.

The distance S between two retarded positions p_1 and p_2 is determined with

$$S = v(n_{\omega 1} - n_{\omega 2})L/c \tag{5}$$

From Figure 1 we know, observed on the Earth, the picture of a star is directly determined with S. As S>2r, (where, r is the radius of the star,) a star shall appear two pictures in different colors as shown in Figure 2A. As S<2r, the picture of a spherical star appears as a dumbbell in two colors as shown in Figure 2B.

A   B

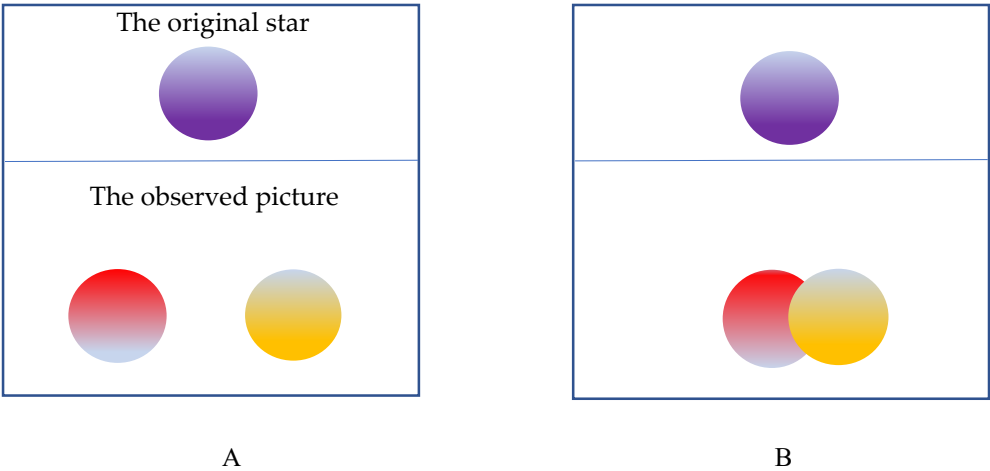



Figure 2. The picture of a star with a strong gravitational field. The original star is one sphere in violet. **A**. As S>2r, there should be two observed pictures in red and yellow respectively for the original violet star. **B**. As S<2r, the observed picture should be a dumbbell in red and yellow.

If light should be dispersion in gravitational field, it should be generally observed. We think, the Spectroscopic binary star could be a strong evidence for our conclusion. A spectroscopic binary is a star system that can only be seen as more than one star by looking at its spectrum; through a telescope, no matter what we do or how good our equipment is, it will always look like one star. It is highly accordant with the conclusion as described in the Figure 2A. Although it is thought that there are two stars in a spectroscopic binary system, it has not been excluded the case that it is a system that a star appears two pictures. We know, the binary stars have been well observed. But, it was presented that the Poincaré's equation of Three-Body problem is invalid.[7] (The evidence is clear: the orbits of the Sun-Earth-Moon are absolutely stable. But, in the Poincaré's equation, these orbits are chaotic.) It was also shown that the current theory of binary star is questioned. Therefore, further observation and study about the spectroscopic binary system is needed. Factually,

the spectroscopic binary system is being studied.[8,9] Here, we found that, as shown in the Figure 3, the two pictures of a star can completely appear a spectroscopic binary system. (It is noted that, any binary system is orbiting around a large center.[7])

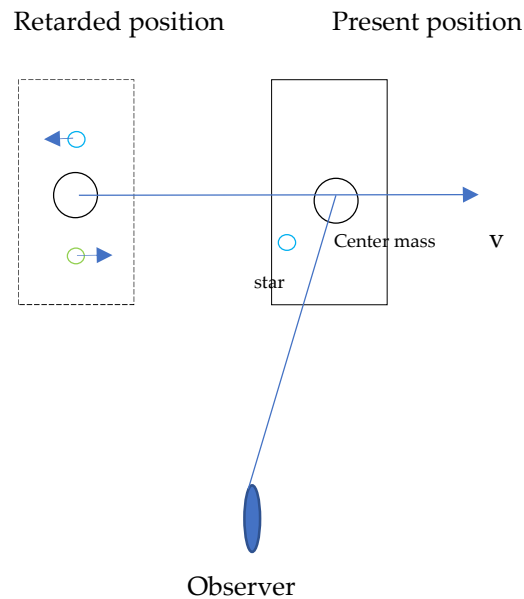
Retarded position   Present position

Observer

Figure 3. A star appears as spectroscopic binary system. A star is orbiting around a large center which cannot be observed by the observer. In the retarded position, because of the dispersion in gravitational field, there are two pictures for the star. The pictures of the star in the retarded position just appears a binary system. It is noted that the retarded positions can be combined in many cases.

And, the images of black hole[10,11] may be a possible evidence for the Figure 2B. Two features of the images of the black hole should be accordant with the Figure 2B. First, the images of the black hole are asymmetrical, or they are elongated. Second, the frequencies of the light are different at different part of the images. 2B shows that the asymmetry is produced from the difference of the frequencies. More generally, Figure 2B is suitable to the celestial body with large radius. It could show that the picture of a star is not always a sphere.

From Equation (5), assuming $(n_{\omega 1} - n_{\omega 2})$ is a constant, the picture of a star is determined with L and v as shown in Figure 3.

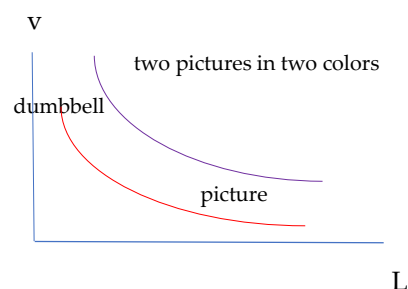



Figure 4. The distribution of the picture of a star. The picture of a star is determined with the distance between the star and observer and the velocity of the star. Out of the violet line, a star appears as two pictures in two colors. Between the two lines, the picture of a spherical star appears as a dumbbell in two colors.

From Figure 4, it can be known that, in Equation (5), as $(n_{\omega 1} - n_{\omega 2})$ can be treated as a constant and usually there is $v < 10^3 km/s$, therefore, the distance L is the main factor to the observed result. The distance between two observed picture can be very large as L is very large.

Figures 1- 4 indicates that our conclusions could be easily confirmed. 1) A large distance L is needed for the spectroscopic binary system. 2) As L is larger, the distance S between two spectroscopic binary stars is larger. 3) The frequencies of the light of the spectroscopic binary are different but the two frequencies are adjoined. 4) The spectroscopic binary has a same orbit around another center mass. It seems that some of the features of the observed spectroscopic binary is accordant with our conclusion.

A gravitational field is a centripetal force. It is more complicated than a general medium, such as a water. Therefore, a real picture of a star is more complicated than the Figure 2. First, usually, a gravitational field is not uniform. The light can be refracted by the field. Therefore, the picture is related with the refracted angle of the light and the velocity v of the star. For the combinations of the directions of the star moving and that of the refracted angle, there should be different picture. Second, light can be bent by gravity, it could result in that the motion of a light ray in a gravitational field is very complicated. As the dispersion is considered, the motion of a light ray in a strong field shall be complicated than that illustrated in the Ref.[2]. Under the conditions of both the bending of light by gravity and the dispersion, in a super strong gravitational field, for the moving of the star, the field strength is different relative to the light with different frequencies. For example, as shown in the Figure 1s in the Supplementary material A, as the light with ω_1 is being acting by the field with the strength g_1, the light with ω_2 has not arrived at g_1. The light with ω_2 only can be acted by g_2. In a super strong field, $(g_1 - g_2)$ is very large in a short distance. It results in that the lines the light with different frequencies running is radically different. And, it is emphasized that, the distance L between us and a star is very large. A little variation of the direction of a light shall result in that this light cannot be observed on the Earth. For example, as a little angle is between two light rays, one of the light rays can arrive at the Earth while another one cannot for that as L is very large, the another light shall arrive at a place very distant from the Earth. Therefore, as the angle of the light bent by gravity is very large, this effect could not be observed with a whole picture. It indicates that only the effect that in the field with proper strength could be observed wholly.

Light dispersion in free space was measured through that the speed of light can be slowed in a vacuum.[12-14] Two conclusions could be obtained from this measurement. First, the pictures analogous to that in the Figure 2 could be produced by the dispersion in free space. Second, dispersion in free space could be enlarged or varied in a strong gravitational field as sentence in the above. (please reference the Supplementary material A.)

3. Discussion

The speed of light has been regarded as a cornerstone of current physics. It is believed that the speed of light in a vacuum is a constant which is the fastest velocity in our universe. However, as pointed out in the above, the speed of light in a vacuum has never been measured and cannot be measured with current technology. In fact, in Einstein's theory of relativity, it was implied that the understandings about the speed of light can be developed. On one hand, it is claimed that the speed of light is constant in vacuum. On another hand, it is claimed that a light ray can be bent by gravity, and take the bending of light by gravity as the main evidence for the general theory of relativity. Bending of light by gravity factually implies that the speed of light can be different in different gravitational field. It is easy to know that as the field is super strong, the motion of light affected by gravity can be radically different from that on the Earth as illustrated in Ref.[2].

Till now, the only theory for the action of gravity on the speed of light is the bending of light by gravity. It is noted that it is Newton who first presented that light can be bent by gravity in 1660s.[15] And, von Soldner obtained the formula for it in 1804.[16] This formula had not been improved in Einstein's general relativity.[17] However, such old a theory need be developed. In quantum mechanics, the reflection of the frequencies of light to the gravity is an important subject.

Several other new observations about the speed of light were obtained. First, it is measured that the quantum teleportation is faster-than-light which can be used for communication[18-20]. In Refs.[18-20] it was clearly sentenced that the faster-than-light quantum teleportation can be used for communication. Second, it was measured that the speed of light in a vacuum is different due to the dispersion in free space.[12-14] It seems a strong supporter for the dispersion of light in gravitational field. Third, it was measured that the photon can be accelerated along the direction vertical to its velocity. [21-23] It may lead to the new discovery of physics. Third, it was observed that the speed of gravity is much larger than the speed of light.[24-26] And, the negative speed of light and the fast light were measured.

And, we emphasize that the speed of light is with particular characteristic. First, in $m = \frac{m_0}{\sqrt{1-v^2/c^2}}$, no other particle is faster than light, and the velocity and mass of a particle are varied according to this formula. Second, astronomical observation shows that the speed of light is not affected by the movement of the source. If the speed of light was affected by the speed v of the source, the speed of light emitted from the sources should be c'= c+v. Because of the orbital motion of the celestial body, relative to the observer on the Earth, it should lead to that, from distant celestial bodies, the light emitted later could arrive at the Earth earlier. If it was so, for the binary star, it should appear that there are many stars, generally called as the "Phantom Phenomenon". Third, the Fizeau experiment[27] also shows the special relationship between the speed of light and the source. In Fizeau experiment, the speed of light is not completely independent of the speed of the source, but the relationship is different from that of general objects such as that between the speed of a boat and that of the water in a river. Now, we have not known the reason for the particularities of the speed of light.

Additionally, it was well known that, there are many different cases for Equation (2). ε_r and μ_r are certain for a material. But, sometimes, μ_r is negative. For some materials, there are $n \to \sqrt{\varepsilon_r}$. So, Equation (2) has not been completely understood.

These new observations and the particular characteristic showed that the speed of light is very complicated. It need be further studied and understood. As the strong gravitational field on the light is studied, some new features of the speed of light shall be discovered.

4. Conclusion

Light dispersion in gravitational field should have been observed through the spectroscopic binary system. The speed of light with the electric constant and magnetic constant is the fundamental physics constant in modern physics. Light dispersion in gravitational field means that a new understanding is needed for the fundamental constant. It is noted that, in the past time, the observation and experiment are mainly based on the physical event about the Earth and the solar system. These physical constants are universal to the solar system. The gravitational field in the solar system is very weak. The observational and experimental result acted by the field is correspondingly weak. Therefore, this field can be approximately treated as a vacuum. For example, although we have well known that a light ray is always being bent by the gravity of the Earth, we also treated this light ray as a straight line. But, for a super strong gravitational field with a relativistic mass density of 10^{17}kgm^{-3}, the effect of the field on the observation is very large. It is clear, as the light ray emitted by a neutron star can be moved around the star by the gravitational field of the star,[2] the speed of this light cannot be still understood as that this ray is moving in a vacuum. Therefore, although the concept of the speed of light in a vacuum is still useful in current theory of physics, it need be developed for studying the strong field. Factually, both observation and experiment showed that the speed of light can be varied by gravity and by the objects in laboratory.[18-23] The conditions for the new understanding about the fundamental physics constant were found. The deep space time is around the corner, the strong gravitational field is becoming one of the important

subjects in physics. The new understanding should be helpful to better understand the physics fundamental constant in the future.

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Supplementary material A

The enlarged effect of the dispersion of light in a strong gravitational field

Under the condition that light dispersion, as a light ray with two (or more) frequencies is running through a gravitational field as shown in Figure 1s, because the speed of light is

$$c_\omega = c/n_\omega$$

As $n_{\omega 1} < n_{\omega 2}$, there is $c_{\omega 1} > c_{\omega 2}$. In this case, as the light with the frequency of ω_1 has arrived at point P$_1$ where the field strength is $g_1 = G\frac{M}{R^2}$, the light with the frequency of ω_2 only arrived at point P$_2$ where the field strength is $g_2 = G\frac{M}{(R+r)^2}$. In a super strong field, $(g_1 - g_2)$ is very large. Under the condition that the light can be bent with $\varphi = 2G\frac{M}{rc^2}$, the line that the light with ω_1 running is greatly different from that with ω_2.
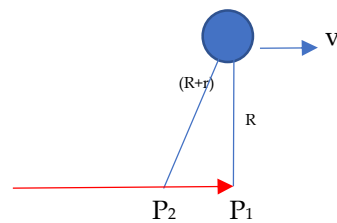
Figure 1SB. The enlarged effect of dispersion of light in strong gravitational field. The star is moving along v. The light with two frequencies is running along the red arrow. At point P$_1$ the field strength is $g_1 = G\frac{M}{R^2}$ while at point P$_2$ the field strength is $g_2 = G\frac{M}{(R+r)^2}$. As the time that the light with the frequency of ω_1 arrived at point P$_1$ and the light with ω_2 arrived at P$_2$ is same, and the light is bent by gravity at P$_1$ and P$_2$, there shall be a difference between the bent angle of the light with ω_1 and that of the light with ω_2. In a super strong field, $(g_1 - g_2)$ is a very large value. This difference is also very large. For the moving of the star, this difference shall be enlarged with time. In the field with proper strength, a spectrogram by gravity should be observed.