

Using a Product Life Cycle Cost Model to Solve Supplier Selection Problems in the High-technology Company

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Abstract: Using the PLCC advantages generates revenue and lowers costs more than might be anticipated. It ensures better decisions by using a more perfect and practical assessment of revenues and costs. Although the supplier selection (SC) product life cycle cost (SCPLCC) is an important consideration among corporations, SCPLCC problem has become associated with deciding how one supplier should be selected from possible alternatives. In this study, we applied two types of goal programming, multiobjective linear programming and revised multichoice goal programming to develop a PLCC-based concept to solve the SCPLCC problem and construct a decision-making tool for application to a case of supply chain management in a Taiwanese light-emitting diode company in the high-tech industry. Our study main contribution Company managers can easily use the two approaches of the SCPLCC model with different parameters to solve SCPLCC model problems. Finally, we comparing five models found RMCGP with weighted linear goal programming had an adequate effect for application to the PLCC concept for high-technology company; this cloud make company decision-makers focus on low PLCC and select better supplier.

Keywords: supplier selection; product life cycle cost; geometric averaging-weighting; multiobjective linear programming; revised multichoice goal programming.

1. Introduction

Due to the globalization of commercial markets and the improvements in information technology, a well-made supply chain management (SCM) system is regarded as an important tool for gaining competitive advantage [1, 2]. In higher levels of the supply chain, supplier selection (SC) continues to be an crucial component in manufacturing procurement and, a major activity of professionals in the industry [3,4,5]. With the beginning of globalization, managing SC actions has turned into more multifaceted. SCM is an essential element of most businesses and is critical to corporation achievement and customer

satisfaction. A supply chains (SCs) represents the pathways between suppliers and buyers (customers or consumers) [6].

In sum, for an industrial company, the primary goal is to make the correct product, for the correct customer, in the correct amount, at the correct time. Today's purchasing companies demand an advanced buyer equal of enactment from their supplier while the two parties maintain a respectful relationship. Although the SC product life cycle cost (SCPLCC) is an important consideration among corporations, the literature on this topic is limited. SCPLCC has become associated with deciding how one supplier should be selected from possible alternatives.

Therefore, optimization of the supplier base is a must for identifying high performing suppliers in supply chains. The SCPLCC problem-solving approach has been discussed for difficult problems in the literature for the following reasons:

(1) Attempts to incorporate information vagueness into the SCPLCC problem are scarce in the literature. The multiobjective linear programming (MOLP) model can account for the variation or imprecision of a decision maker's (DM's) aspiration level (i.e., the intermediate control variables) created thus producing a more assured key point for DM policy [7]. In our study, a fuzzy MOLP model and revised multi-choice goal programming (RMCGP) model were used to close the literature's gap. RMCGP with weighted linear goal programming had an adequate effect for application to the PLCC concept for high-technology company.

(2) We extended the work of Amid et al. [7], and used Wang's [5] study to handle the product life cycle cost (PLCC) problem, and we cited and modified the auto parts manufacturer' example data set from Kumar et al. [8] to solve the SCPLCC problem.

(3) Our study advantages by using MOLP and RMGCP SCPLCC models that incorporated geometric averaging-weighting to solve the SCPLCC model problem, the DM can understand the differences between giving or not giving all the objectives and constraints in the SC decision equal importance [9]. Our SCPLCC model can help DMs determine the appropriate prioritization of supplier and allow purchasing managers to manage SC performance on the basis of minimizing net cost, rejection, late delivery, and PLCC goals. Our study main contribution Company managers can easily use the two approaches of the SCPLCC model with different parameters to solve SCPLCC model problems [10].

The paper is organized as follows: First, we review the literature on the quantitative techniques of the SC decision in Section 2. In Section 3, the explanation formation and solution of the SCPLCC problems achieved by using the two approaches are presented. In Section 4 presents the problem-solving process of the two goal programming (GP) approaches based on the modified auto parts manufacturer' example data set [8] for solving SCPLCC problems to demonstrate the process, we adopted it to a light-emitting diode (LED) company in Taiwan. In Section 5, conclusions are drawn regarding the advantages of SC with these two approaches in real business-world applications.

2. Literature review

The criteria for SC and supplier rating have been a focus of research since the 1960s. Dickson [11] identified a list of at least 50 distinct factors presented by various authors in the literature that are meaningful in SC. Different methods have been used for SC, such as linear weighting methods, mathematical programming models [e.g. linear programming (LP), GP]. Goal Programming (GP) is a technique in the field of multi-criteria decision making (MCDM). GP is to minimize the unwanted deviations of the objective values determined by the decision-maker to reach an acceptable resolution.

In the present study, we classified research on SC into two major categories [e.g., Qualitative factor approach and integrated factor approach] and several representative publications are listed in Table 1. Methodical models for SC have comprised diverse methods from simple weighted scoring methods to compound mathematical programming, and the best researchers have utilized multiple elements in their selection criteria [12]. These methods often include a large degree of subjectivity in the DM process.

Table 1. Summary of the recent studies using mathematical programming models for supply chain

Author(s)/year	Category	Supply chain	Methods	Cost	Rejection	Delivers	PLCC	Capacity	Budget
MO' Ath et al. (2017) [13]	Integrated	✓	WGP,LP				✓		✓
Umarusman (2018) [14]	Qualitative	✓	criterion	✓	✓	✓			
Budzinski et al. (2019) [15]	Integrated	✓					✓		
Ojo et al. (2020) [16]	Qualitative	✓	GP						✓
Hocine et al. (2020) [17]	Integrated	✓	WA-FMC GP	✓					✓
Hardy et al. (2020) [18]	Qualitative	✓							
AI-Huaain et al. (2020) [19]	Qualitative	✓	GP	✓				✓	✓
Bibhas and Sushil (2020) [20]	Qualitative	✓	Game Theoretic	✓					✓
Biswarup and Bibhas (2021) [21]	Qualitative	✓	Game Theoretic	✓	✓				✓
Bahareh et al. (2021) [22]	Qualitative	✓	FGP		✓				
Nasr et al. (2021) [23]	Qualitative	✓	FGP	✓		✓			
Mabrouk (2021) [24]	Qualitative	✓	Fuzzy set	✓		✓			
This study	Integrated	✓	MOLP,R MCGP	✓	✓	✓	✓	✓	✓

The incorporation of data fuzziness in SCPLCC has not been prominent in the literature. Kumar et al. [24] presented a fuzzy goal programming models to minimize the total tolerable weighted variations of variables. In the present study, we first attempted to use two fuzzy programming approaches to close this gap in knowledge.

3. Methods

Zimmermann [25] used the approach of Bellman and Zadeh [26] to solve a fuzzy linear programming problem and demonstrated that an LP problem with a fuzzy goal and fuzzy restrictions might be reformulated such that it can be solved as a conventional LP problem. Indices, decision variables, and parameters are accounted for in the construction of a multiobjective LP model in accordance with a set of assumptions. The enriched multiobjective LP model is expressed as follows:

Assumptions

- (i) Only one item is purchased from one supplier.
- (ii) Quantity discounts are not considered.
- (iii) The suppliers do not have shortages of the item.
- (iv) The lead time and demand of the item are constant and known with confidence.

Sets of indices, parameters and decision variables for the SCPLCC model are defined in Table 2.

Table 2. Terminology [fuzzy parameters are indicated by a tilde (~)].

Index	
i	key index for supplier, for all $i = 1, 2 \dots n$
j	key index for objectives function, for all $j = 1, 2 \dots J$
k	key index for constraints, for all $k = 1, 2 \dots K$
Decision variable	
x_i	Order quantity given to the supplier i
Parameters	
\tilde{D}	Aggregate demand of the item over a fixed planning period
n	Number of suppliers competing for selection
p_i	Price of a unit item of ordered quantity x_i to supplier i
R_i	Percentage of the rejected units delivered by supplier i
L_i	Percentage of the units delivered late by supplier i
C_i	PLCC ordered quantity x_i to supplier i
\tilde{U}_i	Upper limit of the quantity available for supplier i
r_i	Vendor rating value for supplier i
P	Least total purchasing value that a vendor can have
f_i	Supplier quota flexibility for supplier i
F	Least value of flexibility in supply quota that a supplier should have
B_i	Budget constraint allocated to each supplier

Model: SCPLCC problem.

We can formulate the multiobjective SCPLCC problem with four fuzzy objectives and fuzzy crisp constraints as follows:

$$\text{Minimize: } Z_1 \cong \sum_{i=1}^n P_i x_i \quad (1)$$

$$\text{Minimize } Z_2 \cong \sum_{i=1}^n R_i x_i \quad (2)$$

$$\text{Minimize } Z_3 \cong \sum_{i=1}^n L_i x_i \quad (3)$$

$$\text{Minimize } Z_4 \cong \sum_{i=1}^n C_i x_i \quad (4)$$

Then, we can subject the problem to the following constraints:

$$\sum_{i=1}^n x_i \geq \tilde{D} \quad (\text{aggregate demand constraint}) \quad (5)$$

$$x_i \leq \tilde{U}_i \quad \forall i; i = 1, 2, \dots, n \text{ (capacity constraint)} \quad (6)$$

$$\sum_{i=1}^n r_i(x_i) \geq P \quad (7)$$

$$\sum_{i=1}^n f_i(x_i) \leq F \quad (8)$$

$$P_i x_i \leq B_i, \quad i = 1, 2, \dots, n \text{ (budget constraint)} \quad (9)$$

$$x_i \geq 0, \quad i = 1, 2, \dots, n \text{ (non-negativity constraint)} \quad (10)$$

This model has four main fuzzy objectives goals: minimization of total net cost; minimization of reject items, minimization of net late-delivered items, and the supplier's realization of the PLCC. The aggregate demand constraint ensures that the required quantity of supplied product items over a fixed planning period is satisfied. The supplier product capacity constraint limits supply on the basis of uncertain aggregate demand being set at 10% of the deterministic model. The budget constraint means that no one supplier can spend more than the budgeted amount of money allocated to it. Lastly, the nonnegativity constraint prohibits negative orders. Generally, the tilde symbol (\sim) indicates that the situation is fuzzy, and in this model, both the objective functions and demand constraints were fuzzy parameters [9].

The fuzzy decision can be either symmetric or asymmetric depending on whether the weights are equal or unequal and on the objectives and restrictions [9,25]. This problem is characterized by the following membership function (MF):

$$\mu_d(x) = \min(\mu_g(x), \mu_c(x)).$$

A general linear MOLP model for supplier selection with minimization (Z_1, Z_2, Z_3, Z_4) and maximization of objective function (Z_2) fuzzy and crisp constraints is expressed as follows [9]:

$$Z_1 = Z_3 = Z_4 = \sum_{i=1}^n c_{ki} x_i, \quad k = 1, 2, 3, 4 \quad Z_2 = \sum_{i=1}^n c_{ti} x_i, \quad t=2$$

$$\text{s.t.} \quad \sum_{i=1}^n a_{ri} x_i \geq d_r, \quad r = 1, 2, \dots, m \text{ for fuzzy restrictions (capacity constraint 1,2,3,4)}$$

$$\sum_{i=1}^n b_{si} x_i \geq d_s, \quad s = 1, 2, \dots, m \text{ for crisp restrictions (budget constraint 1,2,3,4)}$$

$$x_i \geq 0, \quad i = 1, 2, \dots, n.$$

The treatment of objectives and restrictions in fuzzy LP is the same because they are defined through an individual MF. In Figure 1, the fuzzy objective functions and constraints of the SCPLCC problem are presented.

The membership function (Z_k) and maximization goals (Z_l) are given as follows:

$$\mu_{z_k}(x) = \begin{cases} 1 & \text{for } Z_k \leq Z_k^- \\ \mu_{z_k} = \frac{(Z_k^+ - Z_k(x))}{(Z_k^+ - Z_k^-)} & \text{for } Z_k^- \leq Z_k(x) \leq Z_k^+ \\ 0 & \text{for } Z_k \geq Z_k^+ \end{cases} \quad (11)$$

($k=1, 2, \dots, p$)

$$\mu_{z_l}(x) = \begin{cases} 1 & \text{for } Z_l \geq Z_l^+ \\ \mu_{z_l} = \frac{(Z_l(x) - Z_l^-)}{(Z_l^+ - Z_l^-)} & \text{for } Z_l^- \leq Z_l(x) \leq Z_l^+ \\ 0 & \text{for } Z_l \leq Z_l^- \end{cases} \quad (12)$$

($l=p+1, p+2, \dots, q$)

where Z_k^- and Z_l^+ can be obtained through solving the multiobjective problem as a single objective using only one objective each time, Z_k^+ is the maximum value (worst solution) of the negative objective Z_k^- and Z_l^- is the minimum value (worst solution) of the positive objective function Z_l^+ [8,27,28].

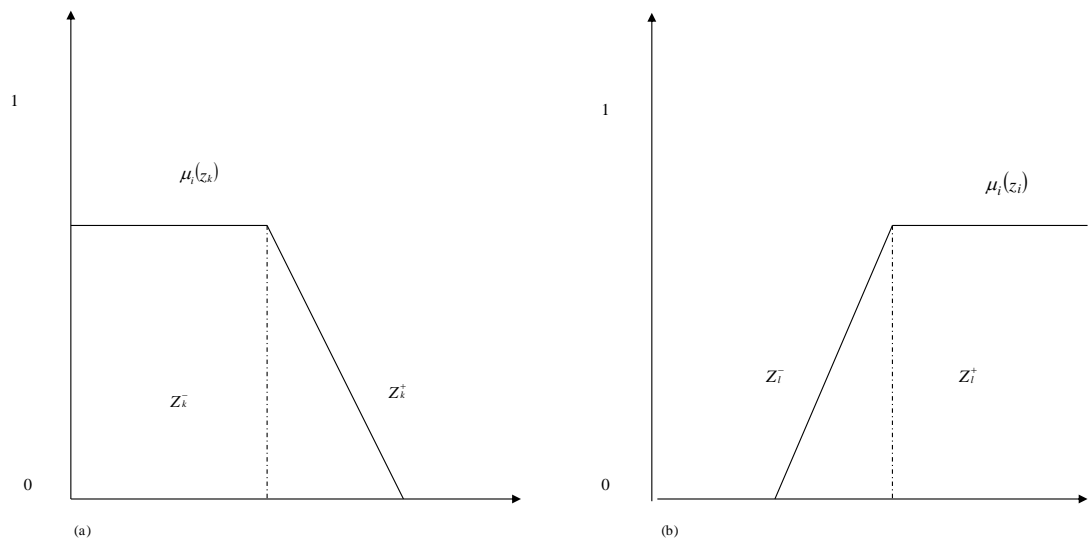


Figure 1. Objective function as a fuzzy number. (a) minimum Z_k^- and (b) maximum Z_l^+ .

3.1. Solution to the SCPLCC Problem by using the Weighted Additive Approach

This section specifies the convex (weighted additive; WA) model that enables DMs to select different weights for various purposes.

When solving the SCPLCC problem model, the weights of the membership functions of goals (objectives) and constraints are calculated according to a supertransitive approximation; thus, these weights are assigned separately. In these equations, α_j is the weighting coefficient that indicates the relative importance of the fuzzy goals and fuzzy restrictions.

The following crisp simplex objective programming function is the same as that of the fuzzy model.

$$\text{Max } \sum_{j=1}^s \alpha_j \lambda_j^* \quad (13)$$

$$\lambda_j \leq \mu_{\bar{z}_j}(x) \quad j = 1, 2, \dots, q, \text{ for all objective functions} \quad (14)$$

$$\gamma_r \leq \mu_{h_r}(x) \quad r = 1, 2, \dots, h, \text{ for all constraints} \quad (15)$$

$$g_m(x) \leq b_m, \quad m = 1, \dots, p, \quad (16)$$

$$\lambda \in [0, 1] \quad (17)$$

$$\sum_{j=1}^s \alpha_j = 1, \quad \alpha_j \geq 0, \quad (18)$$

$$x_i \geq 0, \quad i = 1, 2, \dots, n. \quad (19)$$

See Amid et al. [7] for a more detailed discussion of this model.

3.1.1. Use Lin's Weighted Max–Min Approach

Lin [29] suggested and proofed a weighted max–min approach that can catch an ideal resolution within a feasible area such that the ratio of the achievement level is as approximates equals to the ratio of the weight as possible. He highlighted that the WA model of Tiwari et al. [30] gives objectives of heavy weight relatively greater achievement values. However, the proportion of the achievement levels is not essentially the same as that of the objective weights [8,29]. Thus, for the solution of the SCPLCC problem model, the equations for Lin's weighted max–min model can be expressed as follows [8]:

$$\text{Max } \lambda \quad (20)$$

Subject to

$$w_j \lambda \leq \mu_{\bar{z}_j}(x) \quad j = 1, 2, \dots, q, \quad \text{for all objection functions} \quad (21)$$

$$\gamma_r \leq \mu_{h_r}(x) \quad r = 1, 2, \dots, h, \quad \text{for all constraints} \quad (22)$$

$$g_m(x) \leq b_m, \quad m = 1, \dots, p, \quad (23)$$

$$\lambda \in [0, 1] \quad (24)$$

$$\sum_{j=1}^s \alpha_j = 1, \quad \alpha_j \geq 0, \quad (25)$$

$$x_i \geq 0, \quad i = 1, 2, \dots, n. \quad (26)$$

See Amid et al. [8] for more detailed on this model.

3.2. Revised MCGP Approach to Solving the SCPLCC Problem

To address this SCPLCC problem issue, we used the revised MCGP (also known as the (RMCGP)) achievement function (AF) model developed by Chang [31], and the two RMCGP AF models are presented as follows:

1. RMCGP AF model –type I is used in the case of “more is better” (i.e., achievement is the upper bound):

$$\begin{aligned} &\text{Minimize} \quad \sum_{i=1}^n [w_i(d_i^+ + d_i^-) + \alpha_i(e_i^+ + e_i^-)] \\ &\text{Subject to} \quad f_i(X)b_i - d_i^+ + d_i^- = b_i y_i \quad i = 1, 2, \dots, n, \end{aligned} \quad (27)$$

$$y_i - e_i^+ + e_i^- = g_{i,\max} \quad i = 1, 2, \dots, n, \quad (28)$$

$$g_{i,\min} \leq y_i \leq g_{i,\max} \quad (29)$$

$$d_i^+, d_i^-, e_i^+, e_i^- \geq 0, \quad i = 1, 2, \dots, n, \quad (30)$$

$X \in F$ where F is a feasible set and X is unrestricted in sign.

Note that $b_i \in \{0, 1\}$ is a control variable attached to $|f_i(X) - y_i|$, which can be either achieved or released in Equation (27). In terms of real conditions, b_i is subject to some constraints in guiding the relationships between the goals included in the SCPLCC model's problem.

2. RMCGP AF model –type II is used in the case of “less is better” (i.e., achievement is the lower bound):

$$\begin{aligned} &\text{Minimize} \quad \sum_{i=1}^n [w_i(d_i^+ + d_i^-) + \alpha_i(e_i^+ + e_i^-)] \\ &\text{Subject to} \quad f_i(X)b_i - d_i^+ + d_i^- = b_i y_i \quad i = 1, 2, \dots, n, \end{aligned} \quad (31)$$

$$y_i - e_i^+ + e_i^- = g_{i,\min} \quad i = 1, 2, \dots, n, \quad (32)$$

$$g_{i,\min} \leq y_i \leq g_{i,\max} \quad (33)$$

$$d_i^+, d_i^-, e_i^+, e_i^- \geq 0, \quad i = 1, 2, \dots, n, \quad (34)$$

$X \in F$ where F is a feasible set and X is unrestricted in sign.

All variables use the definitions given in case I of the RMCGP AF model. All mixed-integer terms in Equations (27) and (29) can easily be linearized using the linearization method developed by Chang [31]. For example as presented in Equations (27), (29) and (30), no selection limitations exist for a single goal, but some dependent relationships between goals do exist. Thus, we can add the auxiliary constraint $b_i \leq b_{i+1} + b_{i+2}$ to the RMCGP AF model, where b_i , b_{i+1} and b_{i+2} are binary variables. Therefore, b_{i+1} or b_{i+2} must equal 1 if $b_i = 1$. This means that if goal 1 has been accomplished, then either goal 2 or goal 3 must have also been accomplished Chang [39] presented a case regarding the managerial implications of these restrictions.

3.3. SCPLCC Problem-Solving Process

A comprehensive solution to the SCPLCC problem can be obtained to complete the following steps:

Step 1: Construction the SCPLCC problem model.

- Step 2: Solve this MOLP problem with geometric averaging-weighting and obtain the value of the four objectives goals. This value is the min. (i.e., lower) and max. (i.e., upper) bounds of the ideal value of the four objective goals.
- Step 3: Replicate the procedure for the residual objectives individually. Define the lower and upper bounds of the optimal values for each of the objectives matching to the set of restraints.
- Step 4: Process these values as the lower and upper bounds of the ideal values for crisp construction of the SCPLCC problem.
- Step 5: After steps 2, 3, and 4, for each objective function, find a lower bound and an upper bound matching the established resolutions for each objective goal. Let Z_j^- and Z_j^+ denote the lower and upper bounds for the j th objective goal (Z_j) [8].
- Step 6: For the objective functions find the MF in relation to Equations (11) and (12).
- Step 7: Perform geometric averaging-weighting for the criteria
- Step 8: Express and solve the corresponding crisp geometric averaging WA model for the SCPLCC problems in relation to Equations (13) - (19).
- Step 9: Express and solve the corresponding crisp geometric averaging-weighted max-min model for the SCPLCC problem in relation to Equations (20) - (25).
- Step 10: Express RMCGP with both geometric averaging-weighted and no-penalty-weighted construction of the fuzzy optimization problem as expressed in Equations (27) and (30).
- Step 11: Express RMCGP with the geometric averaging-weighted and penalty-weighted construction of the fuzzy optimization problem, consistent with Equations (27) and (34).
- Step 12: Solve the RMCGP with both geometric averaging-weighted and penalty-weighted GP constructions of the fuzzy optimization SCPLCC model problem, and compare the two GPs.

4. Practical Example

The company for which the SCPLCC problem model was tested is part of a multinational group [LED research & development (R&D) sector]] and manufactures electric light parts. External purchases annually accounted for over 75% of total costs. The company is a made-to-order firm, and its management intended to improve the efficiency of the purchasing process and re-consider the company's sourcing strategies. The management felt that evaluating and certifying there a vendor is essential to ensuring reductions in product inventory and the time to market. They had been encouraged to develop longer-term trust-based relationships with fewer vendors. Management appointed a team to recommend three or four suitable vendors. The team consisted of several managers from various departments such as purchasing, marketing, quality control, production, engineering and R&D. The team members organize several meetings to create a profile of the contending vendors. They establish an initial set of three suppliers and evaluated them. An SCPLCC problem model was developed for the selection and quota allocations of the vendors under uncertain environments. The team considered the following four main objective functions; minimization of net cost, net rejections, the net late deliveries, and PLCC; these were all subject to a few practical constraints regarding the demand of the item, vendor capacity limitations, vendor budget allocations, and other factors. The price quoted (P_i in New Taiwan Dollars), the percentage of rejections (R_i), the percentage of late deliveries (L_i), the PLCC (C_i), cost suppliers capacities (U_i), supplier quota flexibility (F_i) on a scale of 0 to 1, percentage of rejections (R_i) on a scale of 0 to 1, and the budget allocations for the suppliers (B_i) were considered. The three supplier profiles are presented in Table 3.

Table 3. Supplier source data for the problem.

Supplier no.	P _i (\$)	R _i (%)	L _i (%)	C _i (\$)	U _i (Units)	R _i	F _i	B _i (\$)
1	3	0.05	0.04	1.92	5,000	0.88	0.02	25,000
2	2	0.03	0.02	1.04	15,000	0.91	0.01	100,000
3	6	0.02	0.08	3.94	6,000	0.97	0.06	35,000

In this case demonstration, the linear MF was used to fuzzifying the right-hand side of the restrictions in the preceding SCPLCC model. The values of net cost, rejections, late deliveries and supplier capacity at the lowest and highest level of MF must be defined per Equations (11) and (12). The levels of uncertainty for all of the fuzzy parameters are assumed to be 10% of the deterministic model. The data sets for the values at the lowest and highest aspiration levels of the MFs are listed in Table 4.

Table 4. Limiting values in the membership function for net cost, rejections, late deliveries, PLCC, vendor capacities and budget information.

	(Min.) $\mu = 1$	(Max.) $\mu = 0$
Net cost objective goal	57,000	71,833
Rejection objective goal	413	521
Late deliveries objective goal	604	816
Product life cycle cost objective goal	10,000	90,000
Capacity constraints		
Supplier 1	5,000	5,500
Supplier 2	15,000	16,500
Supplier 3	6,000	6,600
Budget constraints		
Supplier 1	25,000	27,500
Supplier 2	100,000	110,000
Supplier 3	35,000	38,500

4.1. Application of WA Approach to the Numerical Example

The example used was solving the problem by using Tiwari, Dharmar and Rao's WA approach [30]. Before starting the solution, the weights of four goals and six restrictions were determined using supertransitive approximation. Thus, we assumed that the following binary comparison matrix consists of obtain net cost, rejection of late deliveries, PLCC, Supplier 1 constraints, Supplier 2 constraints, and Supplier 3 constraints:

$$A = \begin{pmatrix} \text{Net cost} \\ \text{Rejection} \\ \text{Late deliveries} \\ \text{Product lifecycle cost} \\ \text{Vendor 1 capacity} \\ \text{Vendor 2 capacity} \\ \text{Vendor 3 capacity} \\ \text{Vendor 1 budget constraints} \\ \text{Vendor 2 budget constraints} \\ \text{Vendor 3 budget constraints} \end{pmatrix}$$

$$\Rightarrow \begin{pmatrix} 1 & 6 & 4 & 9 & 3 & 4 & 9 & 9 & 8 & 2 \\ 1/6 & 1 & 1/2 & 3 & 1/3 & 1/3 & 2 & 4 & 5 & 1/4 \\ 1/4 & 2 & 1 & 4 & 1/2 & 1/2 & 3 & 5 & 6 & 1/3 \\ 1/9 & 1/3 & 1/4 & 1 & 1/5 & 1/2 & 2 & 3 & 3 & 1/6 \\ 1/3 & 3 & 2 & 5 & 1 & 1 & 4 & 6 & 7 & 1/2 \\ 1/4 & 3 & 2 & 5 & 1 & 1 & 4 & 6 & 7 & 1/2 \\ 1/9 & 1/2 & 1/3 & 2 & 1/4 & 1/4 & 1 & 3 & 4 & 1/5 \\ 1/9 & 1/4 & 1/5 & 1/2 & 1/6 & 1/6 & 1/3 & 1 & 2 & 1/8 \\ 1/8 & 1/5 & 1/6 & 1/3 & 1/7 & 1/7 & 1/4 & 1/2 & 1 & 1/9 \\ 1/2 & 4 & 3 & 6 & 2 & 2 & 5 & 8 & 9 & 1 \end{pmatrix}$$

The supertransitive approximation method [32] is used to obtain the comparison matrix, and the following weights are obtained [9]: $w_1 = 0.2958$, $w_2 = 0.0579$, $w_3 = 0.0863$, $w_4 = 0.0365$, $w_5 = 0.1291$, $w_6 = 0.1254$, $w_7 = 0.0392$, $w_8 = 0.0199$, $w_9 = 0.0151$, $w_{10} = 0.1949$.

4.2.1. Solving the SCPLCC Example by Using the WA Approach

For this SCPLCC example, the optimal quota allocations (i.e., purchasing order), supplier product capacity limitations, and budget restrictions among the different vendors were obtained using the Zimmermann WA method [33] as shown in Equations (13) - (19). This SCPLCC problem can then be reformulated as the following program:

$$\begin{aligned} \text{Maximize} \quad & 0.2958\lambda_1^* + 0.0579\lambda_2^* + 0.0863\lambda_3^* + 0.0365\lambda_4^* + 0.1291\lambda_5^* \\ & + 0.1254\lambda_6^* + 0.0392\lambda_7^* + 0.0199\lambda_8^* + 0.0151\lambda_9^* + 0.1949\lambda_{10}^* \end{aligned}$$

Subject to

$$\begin{aligned} \lambda_1^* &\leq (71833 - (3x_1 + 2x_2 + 6x_3)) / (71833 - 57000) \\ \lambda_2^* &\leq (521 - (0.05x_1 + 0.03x_2 + 0.01x_3)) / (521 - 413) \\ \lambda_3^* &\leq (816 - (0.04x_1 + 0.02x_2 + 0.08x_3)) / (816 - 604) \\ \lambda_4^* &\leq (90000 - (1.92x_1 + 1.04x_2 + 3.94x_3)) / (90000 - 10000) \\ \mu_1^* &\leq (71833 - (3x_1 + 2x_2 + 6x_3)) / (71833 - 57000) \\ \mu_2^* &\leq (521 - (0.05x_1 + 0.03x_2 + 0.01x_3)) / (521 - 413) \\ \mu_3^* &\leq (816 - (0.04x_1 + 0.02x_2 + 0.08x_3)) / (816 - 604) \\ \mu_4^* &\leq (90000 - (1.92x_1 + 1.04x_2 + 3.94x_3)) / (90000 - 10000) \\ Z_1 &= 3x_1 + 2x_2 + 6x_3 \\ Z_2 &= 0.05x_1 + 0.03x_2 + 0.01x_3 \\ Z_3 &= 0.04x_1 + 0.02x_2 + 0.08x_3 \\ Z_4 &= 1.92x_1 + 1.04x_2 + 3.94x_3 \\ x_1 + x_2 + x_3 &= 20000 \\ \lambda_5^* &\leq (5500 - x_1) / (5500 - 5000) \\ \lambda_6^* &\leq (16500 - x_2) / (16500 - 15000) \\ \lambda_7^* &\leq (6600 - x_3) / (6600 - 6000) \\ \mu_5^* &\leq (5500 - x_1) / (5500 - 5000) \\ \mu_6^* &\leq (16500 - x_2) / (16500 - 15000) \\ \mu_7^* &\leq (6600 - x_3) / (6600 - 6000) \\ 0.88x_1 + 0.91x_2 + 0.97x_3 &\geq 18400 \end{aligned}$$

$$\begin{aligned}
0.02x_1 + 0.01x_2 + 0.06x_3 &\leq 600 \\
\lambda_8^* &\leq (27500 - 3x_1)/(27500 - 25000) \\
\lambda_9^* &\leq (110000 - 2x_2)/(110000 - 100000) \\
\lambda_{10}^* &\leq (38500 - 7x_3)/(38500 - 35000) \\
x_i &\geq 0 \text{ and integer, } i = 1, 2, 3.
\end{aligned}$$

The numerical example of the SCPLCC problem was then solved using LINGO software (2002) [34], and the following solution was obtained:

$$\begin{aligned}
x_1 &= 240 & x_2 &= 15,570 & x_3 &= 4,190 & \mu_1 &= 0 & \mu_2 &= 0 & \mu_3 &= 0 \\
\mu_4 &= 0 & \mu_5 &= 0 & \mu_6 &= 0 & \mu_7 &= 0.3066 & \mu_8 &= 1 \\
\mu_9 &= 1 & \mu_{10} &= 0.0011 \\
z_1 &= 57,000 & z_2 &= 521 & z_3 &= 656.20 & z_4 &= 33,162.20.
\end{aligned}$$

4.2.2. Solving the SCPLCC Example by Using the Weighted Max-Min Approach

For this illustrative SCPLCC example, the optimal quota allocations (i.e., purchasing order), supplier product capacity limitations, and budget constraints among the different supplier were obtained using the weighted max-min (Lin, 2004) approach as expressed in Equations (20)-(26). This SCPLCC problem can then be reformulated as the following program:

$$\begin{aligned}
&\text{Maximize } \lambda \\
&\text{Subject to} \\
&0.2958\lambda \leq (71833 - (3x_1 + 2x_2 + 6x_3))/(71833 - 57000) \\
&0.0579\lambda \leq (521 - (0.05x_1 + 0.03x_2 + 0.01x_3))/(521 - 413) \\
&0.0863\lambda \leq (816 - (0.04x_1 + 0.02x_2 + 0.08x_3))/(816 - 604) \\
&0.0363\lambda \leq (90000 - (1.92x_1 + 1.04x_2 + 3.94x_3))/(90000 - 10000) \\
&0.2958\mu \leq (71833 - (3x_1 + 2x_2 + 6x_3))/(71833 - 57000) \\
&0.0579\mu \leq (521 - (0.05x_1 + 0.03x_2 + 0.01x_3))/(521 - 413) \\
&0.0863\mu \leq (816 - (0.04x_1 + 0.02x_2 + 0.08x_3))/(816 - 604) \\
&0.0363\mu \leq (90000 - (1.92x_1 + 1.04x_2 + 3.94x_3))/(90000 - 10000) \\
&Z_1 = 3x_1 + 2x_2 + 6x_3 \\
&Z_2 = 0.05x_1 + 0.03x_2 + 0.01x_3 \\
&Z_3 = 0.04x_1 + 0.02x_2 + 0.08x_3 \\
&Z_4 = 1.92x_1 + 1.04x_2 + 3.94x_3 \\
&x_1 + x_2 + x_3 = 20000 \\
&0.1291\lambda \leq (5500 - x_1)/(5500 - 5000) \\
&0.1254\lambda \leq (16500 - x_2)/(16500 - 15000) \\
&0.0392\lambda \leq (6600 - x_3)/(6600 - 6000) \\
&0.88x_1 + 0.91x_2 + 0.97x_3 \geq 18400 \\
&0.02x_1 + 0.01x_2 + 0.06x_3 \leq 600 \\
&0.0199\lambda \leq (27500 - 3x_1)/(27500 - 25000) \\
&0.0151\lambda \leq (110000 - 2x_2)/(110000 - 100000) \\
&0.1949\lambda \leq (38500 - 6x_3)/(38500 - 35000) \\
&x_i \geq 0 \text{ and integer, } i = 1, 2, 3.
\end{aligned}$$

The numerical example of the SCPLCC problem was then solved using LINGO software (2002), and the following solution was obtained:

$$\begin{aligned}
x_1 &= 0 & x_2 &= 15,750 & x_3 &= 4,250 & \lambda &= 0.9595 & \mu_1 &= 0 \\
\mu_2 &= 0 & \mu_3 &= 0 & \mu_4 &= 0 & \mu_5 &= 0 & \mu_6 &= 0 \\
\mu_7 &= 0.3066 & \mu_8 &= 1 & \mu_9 &= 1 & \mu_{10} &= 0.0011 \\
z_1 &= 57,000 & z_2 &= 515 & z_3 &= 655 & z_4 &= 33,125.
\end{aligned}$$

4.2.3. Solving the SCPLCC Example by Using the RMCGP Approach

We now consider a RMCGP problem with goals and constraints that cannot be solved by current GP methods. For this illustrative application, optimal quota allocations (i.e., purchasing order), supplier product capacity, and financial budget constraints among different suppliers were considered. This SCPLCC problem was then formulated as follows:

Main goals:

$$(G_1) \quad 3x_1 + 2x_2 + 6x_3 = 57,000 \text{ } (G_1, \text{MIN.}) \text{ or } 71,833 \text{ } (G_1, \text{MAX.})$$

$$(G_2) \quad 0.05x_1 + 0.03x_2 + 0.01x_3 = 413 \text{ } (G_2, \text{MIN.}) \text{ or } 521 \text{ } (G_2, \text{MAX.})$$

$$(G_3) \quad 0.04x_1 + 0.02x_2 + 0.08x_3 = 604 \text{ } (G_3, \text{MIN.}) \text{ or } 816 \text{ } (G_3, \text{MAX.})$$

$$(G_4) \quad 1.92x_1 + 1.04x_2 + 3.94x_3 = 10,000 \text{ } (G_4, \text{MIN.}) \text{ or } 90,000 \text{ } (G_4, \text{MAX.})$$

Capacity constraints:

$$(G_5) \quad x_1 = 5,000 \text{ } (G_5, \text{MIN.}) \text{ or } 5,500 \text{ } (G_5, \text{MAX.}) \text{ } (X_1, \text{Supplier 1 product capacity})$$

$$(G_6) \quad x_2 = 15,000 \text{ } (G_6, \text{MIN.}) \text{ or } 165,000 \text{ } (G_6, \text{MAX.}) \text{ } (X_2, \text{Supplier 2 product capacity})$$

$$(G_7) \quad x_3 = 6,000 \text{ } (G_7, \text{MIN.}) \text{ or } 165,000 \text{ } (G_7, \text{MAX.}) \text{ } (X_3, \text{Supplier 3 product capacity})$$

$$x_1 + x_2 + x_3 = 20,000 \quad (\text{Total demand constraint})$$

Budget constraints:

$$(G_8) \quad 3x_1 = 25,000 \text{ } (G_8, \text{MIN.}) \text{ or } 27,500 \text{ } (G_8, \text{MAX.}) \text{ } (X_1, \text{Vendor 1 budget constraint})$$

$$(G_9) \quad 2x_2 = 100,000 \text{ } (G_9, \text{MIN.}) \text{ or } 110,000 \text{ } (G_9, \text{MAX.}) \text{ } (X_2, \text{Vendor 2 budget constraint})$$

$$(G_{10}) \quad 6x_3 = 35,000 \text{ } (G_{10}, \text{MIN.}) \text{ or } 110,000 \text{ } (G_{10}, \text{MAX.}) \text{ } (X_3, \text{Vendor 3 budget constraint})$$

Through the RMCGP no-penalty weighted method [31] with a geometric averaging-weighted approach [9,31], this SCPLCC Problem was then expressed as the following program:

$$\begin{aligned} \text{Min} = & 0.2958(d_1^- + e_1^-) + 0.0579(d_2^- + e_2^-) + 0.0863(d_3^- + e_3^-) + 0.0365(d_4^- + e_4^-) \\ & + 0.1291(d_5^- + e_5^-) + 0.1254(d_6^- + e_6^-) + 0.0392(d_7^- + e_7^-) \\ & + 0.0199(d_8^- + e_8^-) + 0.0151(d_9^- + e_9^-) + 0.1949(d_{10}^- + e_{10}^-) \end{aligned}$$

s.t.

$$(3.1x_1 + 2x_2 + 7x_3)b_1 - d_1^+ + d_1^- = y_1b_1 \quad \text{for the net cost goal, wherein less is better}$$

$$y_1 - e_1^+ + e_1^- = 57000 \quad \text{for representing } |y_1 - g_{1,\min}|$$

$$57000 \leq y_1 \leq 71833 \quad \text{for the bounds of } y_1$$

$$(0.05x_1 + 0.03x_2 + 0.01x_3)b_2 - d_2^+ + d_2^- = y_2b_2 \quad \text{for the rejection goal, wherein the less is better}$$

$$y_2 - e_2^+ + e_2^- = 413 \quad \text{for representing } |y_2 - g_{2,\min}|$$

$$413 \leq y_2 \leq 521 \quad \text{for the bounds of } y_2$$

$$(0.04x_1 + 0.02x_2 + 0.08x_3)b_3 - d_3^+ + d_3^- = y_3b_3 \quad \text{for the late deliveries goal, wherein less is better}$$

$$y_3 - e_3^+ + e_3^- = 604 \quad \text{for representing } |y_3 - g_{3,\min}|$$

$$604 \leq y_3 \leq 816 \quad \text{for the bounds of } y_3$$

$$(1.92x_1 + 1.04x_2 + 3.94x_3)b_4 - d_4^+ + d_4^- = y_4b_4 \quad \text{for the PLCC goal, wherein less is better}$$

$$y_4 - e_4^+ + e_4^- = 10000 \quad \text{for representing } |y_4 - g_{4,\min}|$$

$$1000 \leq y_4 \leq 90000 \quad \text{for the bounds of } y_4$$

$$x_1b_5 - d_5^+ + d_5^- = y_5b_5 \quad \text{for the supplier 1 capacity constraint}$$

	goal, wherein less is better
$y_5 - e_5^+ + e_5^- = 5000$	for representing $ y_5 - g_{5,\min} $
$5000 \leq y_5 \leq 5500$	for the bounds of y_5
$x_2 b_6 - d_6^+ + d_6^- = y_6 b_6$	for the supplier 2 capacity constraint
	goal, wherein less is better
$y_6 - e_6^+ + e_6^- = 15000$	for representing $ y_6 - g_{6,\min} $
$15000 \leq y_6 \leq 16500$	for the bounds of y_6
$x_3 b_7 - d_7^+ + d_7^- = y_7 b_7$	for supplier 3 capacity constraint goal,
	wherein less is better
$y_7 - e_7^+ + e_7^- = 6000$	for representing $ y_7 - g_{7,\min} $
$6000 \leq y_7 \leq 6600$	for the bounds of y_7
$3 x_1 b_8 - d_8^+ + d_8^- = y_8 b_8$	for the supplier 1 budget constraint goal,
	wherein less is better
$y_8 - e_8^+ + e_8^- = 25000$	for representing $ y_8 - g_{8,\min} $
$25000 \leq y_8 \leq 27500$	for the bounds of y_8
$2 x_2 b_9 - d_9^+ + d_9^- = y_9 b_9$	for the supplier 2 budget constraint goal,
	wherein less is better
$y_9 - e_9^+ + e_9^- = 100000$	for representing $ y_9 - g_{9,\min} $
$100000 \leq y_9 \leq 110000$	for the bounds of y_9
$6 x_3 b_{10} - d_{10}^+ + d_{10}^- = y_{10} b_{10}$	for the supplier 3 budget constraint goal,
	wherein less is better
$y_{10} - e_{10}^+ + e_{10}^- = 35000$	for representing $ y_{10} - g_{10,\min} $
$35000 \leq y_{10} \leq 38500$	for the bounds of y_{10}
$b_1 = b_2 + b_3 + b_4 + b_5 + b_6 + b_7 + b_8 + b_9 + b_{10}$	for ensuring the net cost goal, rejection
	goal, or late delivery goals, and zero should be achieved.
$b_2 + b_3 + b_4 + b_5 + b_6 + b_7 + b_8 + b_9 + b_{10} = 1$	Added auxiliary constraints can force the
	net cost goal (such that the lower-bound goal is achieved) and either the rejection goal or the late delivery goal is achieved
$Z_1 = 3x_1 + 2x_2 + 6x_3$	
$Z_2 = 0.05x_1 + 0.03x_2 + 0.01x_3$	
$Z_3 = 0.04x_1 + 0.02x_2 + 0.08x_3$	
$Z_4 = 1.92x_1 + 1.04x_2 + 3.94x_3$	
$x_1 + x_2 + x_3 = 20000$	
$0.88x_1 + 0.91x_2 + 0.97x_3 \geq 18400$	
$0.02x_1 + 0.01x_2 + 0.06x_3 \leq 600$	

$$x_i \geq 0 \text{ and } i = 1, 2, 3.$$

$$d_i^+, d_i^-, e_i^+, e_i^- \geq 0 \quad (i = 1, 2, \dots, 10)$$

$$b_i \geq 0 \quad (i = 1, 2, \dots, 10) \text{ are binary variable.}$$

The numerical example of the SCPLCC problem was then solved using LINGO software [34], and the following solution was obtained:

$$\begin{aligned} x_1 &= 5,000 & x_2 &= 9,166.67 & x_3 &= 5833.33 & y_1 &= 57,000 & y_2 &= 410 & y_3 &= 604 \\ y_4 &= 10,000 & y_5 &= 5,000 & y_6 &= 15,000 & y_7 &= 6,000 & y_8 &= 25,000 \\ y_9 &= 100,000 & y_{10} &= 35,000 & b_1 &= 1 & b_2 &= 0 & b_3 &= 0 \\ b_4 &= 0 & b_5 &= 1 & b_6 &= 0 & b_8 &= 0 \\ b_9 &= 0 & b_{10} &= 0 \\ z_1 &= 68,383.33 & z_2 &= 583.33 & z_3 &= 850 & z_4 &= 42,116.67 \end{aligned}$$

Thus, the RMCGP method with a geometric averaging-weighted (no-penalty weighted) approach could solve the SCPLCC problem with minimization of the net cost, rejection, late delivery, and PLCC as the goals.

4.2.4. Solving the SCPLCC Example by Using RMCGP with Geometric Averaging-Weighted and Penalty-Weighted Methods

First, in this SCPLCC example, the optimal quota allocations (i.e., purchasing order), supplier product capacity limitations and budget constraints among the suppliers were obtained using the RMCGP method with a penalty-weighted approach, as expressed in Equations (27) and (30). This SCPLCC problem can then be reformulated in the following program:

$$\begin{aligned} \text{Min} &= 0.2958(5d_1^+ + d_1^- + e_1^-) + 0.0579(4d_2^+ + d_2^- + e_2^-) + 0.0863(3d_3^+ + d_3^- + e_3^-) \\ &+ 0.0365(2d_4^+ + d_4^- + e_4^-) + 0.1291(d_5^- + e_5^-) + 0.1254(d_6^- + e_6^-) \\ &+ 0.0392(d_7^- + e_7^-) + 0.0199(d_8^- + e_8^-) + 0.0151(d_9^- + e_9^-) + 0.1949(d_{10}^- + e_{10}^-) \\ \text{s.t.} \end{aligned}$$

$$\begin{aligned} (3.1x_1 + 2x_2 + 7x_3)b_1 - d_1^+ + d_1^- &= y_1b_1 \\ y_1 - e_1^+ + e_1^- &= 57000 \\ 57000 \leq y_1 &\leq 71833 \\ (0.05x_1 + 0.03x_2 + 0.01x_3)b_2 - d_2^+ + d_2^- &= y_2b_2 \\ y_2 - e_2^+ + e_2^- &= 413 \\ 413 \leq y_2 &\leq 521 \\ (0.04x_1 + 0.02x_2 + 0.08x_3)b_3 - d_3^+ + d_3^- &= y_3b_3 \\ y_3 - e_3^+ + e_3^- &= 604 \\ 604 \leq y_3 &\leq 816 \\ (1.92x_1 + 1.04x_2 + 3.94x_3)b_4 - d_4^+ + d_4^- &= y_4b_4 \\ y_4 - e_4^+ + e_4^- &= 10000 \\ 10000 \leq y_4 &\leq 90000 \\ y_5 - e_5^+ + e_5^- &= 15000 \\ x_1b_5 - d_5^+ + d_5^- &= y_5b_5 \\ 5000 \leq y_5 &\leq 5500 \\ y_6 - e_6^+ + e_6^- &= 15000 \\ x_2b_6 - d_6^+ + d_6^- &= y_6b_6 \\ 15000 \leq y_6 &\leq 16500 \\ y_7 - e_7^+ + e_7^- &= 6000 \\ x_3b_7 - d_7^+ + d_7^- &= y_7b_7 \\ 6000 \leq y_7 &\leq 6600 \\ y_8 - e_8^+ + e_8^- &= 25000 \\ 3x_1b_8 - d_8^+ + d_8^- &= y_8b_8 \\ 25000 \leq y_8 &\leq 27500 \end{aligned}$$

$$\begin{aligned}
y_9 - e_9^+ + e_9^- &= 100000 \\
2x_2b_9 - d_9^+ + d_9^- &= y_9b_9 \\
100000 &\leq y_9 \leq 110000 \\
y_{10} - e_{10}^+ + e_{10}^- &= 35000 \\
6x_3b_{10} - d_{10}^+ + d_{10}^- &= y_{10}b_{10} \\
35000 &\leq y_{10} \leq 38500 \\
b_1 &= b_2 + b_3 + b_4 + b_5 + b_6 + b_7 + b_8 + b_9 + b_{10} \\
b_2 + b_3 + b_4 + b_5 + b_6 + b_7 + b_8 + b_9 + b_{10} &= 1 \\
Z_1 &= 3x_1 + 2x_2 + 6x_3 \\
Z_2 &= 0.05x_1 + 0.03x_2 + 0.01x_3 \\
Z_3 &= 0.04x_1 + 0.02x_2 + 0.08x_3 \\
Z_4 &= 1.92x_1 + 1.04x_2 + 3.94x_3 \\
x_1 + x_2 + x_3 &= 20000 \\
0.88x_1 + 0.91x_2 + 0.97x_3 &\geq 18400 \\
0.02x_1 + 0.01x_2 + 0.06x_3 &\leq 600 \\
x_i &\geq 0 \text{ and } i = 1, 2, 3. \\
(i = 1, 2 \dots 10) \\
b_i &\geq 0 \text{ (} i = 1, 2 \dots 10 \text{) are binary variable.}
\end{aligned}$$

The numerical example of the SCPLCC problem was then solved using LINGO software [34], and the following solution was obtained:

$$\begin{aligned}
x_1 &= 0 & x_2 &= 15,750 & x_3 &= 4,250 & y_1 &= 57,000 & y_2 &= 410 & y_3 &= 604 \\
y_4 &= 10,000 & y_5 &= 5,000 & y_6 &= 15,000 & y_7 &= 6,000 & y_8 &= 25,000 & y_9 &= 100,000 \\
y_{10} &= 35,000 & b_1 &= 1 & b_2 &= 0 & b_3 &= 0 & b_4 &= 0 & b_5 &= 0 \\
b_6 &= 1 & b_8 &= 0 & b_9 &= 0 & b_{10} &= 0 \\
z_1 &= 57,000 & z_2 &= 515 & z_3 &= 655 & z_4 &= 33,125.
\end{aligned}$$

Here, the RMCGP method with the geometric averaging-weighted and penalty-weighted approaches could be suitable for solving the SCPLCC problem with the goals of minimizing the net cost, rejection, late delivery, and PLCC goals.

4.2.5. RMCGP with Averaging-Weighting Penalty-Weighted and Weighted linear Goal Programming

In order to verify RMCGP SCPLCC model problem, we modify RMCGP SCPLCC model with averaging weighted penalty-weighted linear goal programming (WLP). The objectives function is expressed mathematically in the following Equation [13]:

$$\text{MIN} = \frac{\theta_1}{T_1} dn_1^- + \frac{\theta_2}{T_2} dp_2^+ + \frac{\theta_3}{T_3} dn_3^- + \frac{\theta_4}{T_4} dn_4^- + \frac{\theta_5}{T_5} dp_5^+ + \frac{\theta_6}{T_6} dp_6^+ + \frac{\theta_7}{T_7} dn_7^- + \frac{\theta_8}{T_8} dn_8^+ + \frac{\theta_9}{T_9} dn_9^- + \frac{\theta_{10}}{T_{10}} dn_{10}^-$$

Where:

$$\begin{aligned}
\theta_i &= i^{\text{th}} \text{ the geometric averaging weighting; } i=1,2,3 \dots 10, \\
\theta_1 &= 0.2958; \theta_2 = 0.0579; \theta_3 = 0.0863; \theta_4 = 0.0365; \theta_5 = 0.1291; \theta_6 = 0.1254; \theta_7 = 0.0392; \\
\theta_8 &= 0.0199; \theta_9 = 0.0151; \text{ and } \theta_{10} = 0.1949.
\end{aligned}$$

$$T_i = i^{\text{th}} \text{ goal's normalization constant, } i=1,2,3 \dots 10,$$

$$\begin{aligned}
T_1 &= 57,000 \text{ (total net cost objective goal)} \\
T_2 &= 515 \text{ (total rejection objective goal)} \\
T_3 &= 655 \text{ (total late deliveries objective goal)} \\
T_4 &= 33,125 \text{ (total PLCC objective goal)} \\
T_5 &= 5000 \text{ (total Supplier 1 capacity constraints goal)} \\
T_6 &= 15000 \text{ (total Supplier 2 capacity constraints goal)} \\
T_7 &= 6000 \text{ (total Supplier 3 capacity constraints goal)} \\
T_8 &= 25000 \text{ (total Supplier 1 budget constraints goal)} \\
T_9 &= 100,000 \text{ (total Supplier 2 budget constraints goal)} \\
T_{10} &= 35,000 \text{ (total Supplier 3 budget constraints goal)}
\end{aligned}$$

Subsequently, the numerical example of the SCPLCC problem was then solved using LINGO software [41], and the following solution was obtained:

$x_1=1034.48$ $x_2 = 15,000$ $x_3 = 3965.51$ $y_1 = 57,000$ $y_2= 410$ $y_3 = 604$ $y_4 = 10,000$
 $y_5 = 5,000$ $y_6 = 15,000$ $y_7 = 6,000$ $y_8 = 25,000$ $y_9=100,000$ $y_{10}=35,000$
 $z_1 = 56,896.55$ $z_2 = 541.37$ $z_3 = 658.62$ $z_4 = 33,2107$.

Thus, a RMCGP SCPLCC model with averaging weighted penalty-weighted goal programming and with a weighted linear GP solution result should have similar obtained values. The model indicated that Supplier 2 was suitable.

4.3. Summarize Results of the all Types GP Approaches

After solving the SCPLCC problem, we summarized the results of all GP approaches, as presented in Table 5.

Table 5. Results of all GP approaches.

Approach	Zimmermann's additive weighted(FMOLP)	Lin's weighted max-min (FMOLP)	RMCGP with averaging weighted NO penalty-weighted	RMCGP with geometric averaging weighted penalty-weighted	RMCGP with geometric averaging weighted penalty-weighted and WLGP
Objective					
Net cost z1	57,000	57,000	68,383.33	57,000	56,896.55
Rejection z2	521	515	583	515	541.37
Late deliveries z3	656	655	850	655	658.62
Product Life cycle cost z4	33,162	33,125	42,116.67	33,125	33210
Order quantity x1	240	0	15,000	0	1,034.48
Order quantity x2	15,570	15,750	9,166.67	15,750	15,000
Order quantity x3	4,190	4,250	5,833.33	4,250	3,965.51
Capacity restrictions					
Supplier 1	5,500 (max.)	5,500	5,000 (y_5)	5,000 (y_5)	5,000 (y_5)
Supplier 2	1,6500	16,500	15,000 (y_6)	15,000 (y_6)	15,000 (y_6)
Supplier 3	6,600	6,600	6,000 (y_7)	6,000 (y_7)	6,000 (y_7)
Budget restrictions					
Supplier 1	27,500	27,500	25,000(y_8)	25,000 (y_8)	25,000(y_8)
Supplier 2	110,000	110,000	100,000 (y_9)	100,000 (y_9)	100,000 (y_9)
Supplier 3	38,500	38,500	35,000 (y_{10})	35,000 (y_{10})	35,000 (y_{10})

4.4. Discussion of the Two Approaches' Results

After solving the SCPLCC problem, we found that Lin's [29] weighted max-min approach and the RCMCGP method with geometric averaging and penalty-weighted approaches produced the same solution.

Regarding the RCMCGPs with a geometric-averaging-weighted (no-penalty-weighted restrictions) approaches, the solution results were $x_1 = 5,000$ (due to an absence of penalty-weighted constraints), $b_1=1$ and $b_5=1$, and the lower bound Supplier 1 order quantity was 5,000 ($x_1=5,000$) (Table 5).

Regarding the others RCMCGP with geometric averaging-weighted and penalty-weighted approaches, the solution results were $b_1=1$ and $b_6=1$, and the upper bound Supplier 2 order quantity was over 15,000, ($x_2=15,750$). To ensure that the net cost rejection or late delivery goal is met, zero should be obtained (e.g., $b_1 = 1$, $b_6 = 1$, and the b_i auxiliary constraints should be used when adjusting the purchasing quantity (Table 5).

In order to compare the verification and increase the accuracy, use RCMCGP with geometric averaging weighted penalty weighted and a WLGP model to prove the correctness. Thus, RCMCGP SCPLCC models with averaging weighted penalty-weighted goal programming and with a weighted linear GP solution result have obtained the same results (Table 5 the fifth model).

5. Conclusions and Managerial Implications

5.1. Conclusions

SC is one of the most important activities in SCM. Because many factors (i.e., net cost, rejection, late delivery, PLCC SC strategy in a high-tech company, achieving only one objective is insufficient for reducing the PLCC. In other studies, SC models for solving this SCPLCC problem have seldom examined. In the present study, we first attempted to solve the SCPLCC problem with two approaches, both of which considered geometric-averaging-weighted methods. The solution results for the two approaches-presented in this paper should be useful for determining vendors quotas in SCM when the three capacities and budget constraints of each vendor are uncertain (i.e., given a minimum or maximum bound). The first approach, which used the uncertainty of the fuzzy model, used a linear MF, and the entire formulation was solved through a fuzzy multiobjective programming approach. The SCPLCC problem was then transformed through weighted max-min and additive-weighted MOLP and its equivalent crisp single-objective LP programming. The second approach, which used geometric averaging-weighted RCMCGP and a penalty-weighted approach emphasized supplier upgrades, such as increased product quality, reduced PLCC, and guided the relationships between goals in the multiple objective problems.

5.2. Managerial Applications

Our study has of the following managerial implications:

(i) The SCPLCC problem can easily be solved with commercially available LP software such as LINDO and LINGO.

(ii) Our solution of the SCPLCC problem is more comprehensive than LP, and GP, and other deterministic methods that are used for information vagueness, and our solution is captured in two approaches. The SCPLCC problem is transformed into a weighted max-min fuzzy programming model that yields less computational complexity and makes the application of fuzzy methodology more understandable [8].

(iii) In real-world situations of designing SCM, the designer need not provide deterministic values of system parameters, such as product capacity and constraints.

(iv) In the RCMCGP approach [31], auxiliary constraints can guide the relationships between goals in the multiple objective problems. For the SCPLCC problem example, auxiliary constraints (b_i) — can force achieved goals (e.g., can adjust vendor order quota

allocation). RMCGP problem exist within many managerial DM problems. We modified Chang [31] proposed RMCGP with weighted GP to solve the SCPLCC problem by using multiplicative terms of binary variables to account for the multiple target levels. Under some conditions, DMs may want to make a decision toward a goal that can be achieved from a particular aspiration level (i.e., one goal mapping many aspiration levels) [35]. These RMCGP problems exist in many managerial decision-making situations. Little [36] suggested that the model developed in the present paper here satisfies the main demands formulated for operational models and argued that a truly useful model must be simple, robust, easily controllable, adaptive, complete on important SCPLCC issues, and easily communicated. Our SCPLCC problem model appeared to satisfy the first four qualifications in particular [13].

We demonstrated our SCPLCC based PLCC concept model by using a real-world example LED company in Taiwan. In practice, high-tech companies can easily apply our example to select supplier in a fuzzy environment by using the two GP approaches, because precise knowledge of all the parameters is not required. In real cases, the two methods for solving SCPLCC problems can help DMs determine the appropriate prioritization of supplier and allow purchasing managers to manage supply chain performance on the basis of net cost, rejection, late delivery, and PLCC goals. Company managers can easily use the two approaches of the SCPLCC problem model with different parameters to solve SCPLCC problems.

5.3. Limitations

To eliminate the drawbacks of the two of GP approaches and obtain precise outcomes, we compared the models with the RMCGP and weighted GP approaches to verify the SCPLCC problem. If DMs use a new RMCGP method combination multi-criteria decision-making approach, it can be a different result in unclear situation.

5.4 Future Directions

Our SCPLCC models can integrate other GP modes, such as De Novo programming and other multicriteria decision-making approaches such as rough sets [37,38] or neutrosophic sets [39], to solve SCPLCC problems with a multisupplier situation.

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