

# Micromechanical Modeling of Nacre-mimetic $Ti_3C_2$ -MXene Nanocomposites with Viscoelastic Polymer Matrix

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## Abstract

A new two-dimensional nanomaterial – Titanium Carbide MXene ( $Ti_3C_2$ -MXene) – was reported in 2011. In this work, the microscale models of  $Ti_3C_2$ -MXene nanomaterial are considered with polymer matrix. The nanocomposites are modeled using nacre-mimetic brick-and-mortar assembly configurations due to enhanced mechanical properties and interlocking mechanism between the  $Ti_3C_2$ -MXene (brick) and polymer matrices (mortar). The polymer matrix material (Epoxy-resin) is modeled with elastic and viscoelastic behavior (Kelvin-Voigt Model). The Finite Element Method is used for numerical analysis of the microscale models with the multi-point constraint method to include  $Ti_3C_2$ -MXene fillers in the polymer matrix.  $Ti_3C_2$ -MXenes are considered as thick plate elements with transverse shear effects. The response of elastic and viscoelastic models of polymer matrix are studied. Finally, a tensile and compressive load is applied at the microscale and the effective load transfer due to nacre-mimetic configuration is discussed. This paper provides nacre-mimetic models to pre-design the nanocomposite for optimal performance with damage resistance and enhanced strength.

## 1. Introduction

MXenes are two-dimensional (2D) nanomaterials discovered in 2011 [1]. Titanium Carbide MXenes ( $Ti_3C_2$ -MXenes) was the first inorganic 2D nanomaterial discovered and was synthesized by etching the precursor MAX phase compound – Titanium Aluminum Carbide ( $Ti_3AlC_2$ ). Over the past decade, various investigations on the physical and chemical properties of MXenes [2–4] have been conducted and optimization challenges of the synthesis process of MXenes have also been addressed [5].  $Ti_3C_2$ -MXenes have also been used to form nanocomposites in the literature

with the use of polymers as matrix material [6]. The experimental investigations of the  $\text{Ti}_3\text{C}_2\text{-MXenes}$ /Polymer nanocomposites have provided promising results with regards to tailoring the physical properties of the nanocomposites like conductivity [7,8], elasticity [9], and tensile strength [7,10,11], electromagnetic shielding [12], etc. These demonstrations emphasize the importance of good electromechanical properties of  $\text{Ti}_3\text{C}_2\text{-MXenes}$  for use with polymers to form nanocomposites. Along with the classical process of vacuum-assisted filtration to form films of  $\text{Ti}_3\text{C}_2\text{-MXene}$  and  $\text{Ti}_3\text{C}_2\text{-MXene}$  nanocomposites ( $\text{Ti}_3\text{C}_2\text{-MXNC}$ ) for various applications, there have been recent developments of using bioinspired nacre-mimetic brick-and-mortar assembly of  $\text{MXenes}$  with polymers in the literature [11,13]; that promise both good physical properties and an option to tailor the physical properties with the pre-design of the nacre-mimetic assembly process.

Along with the experimental investigations into  $\text{Ti}_3\text{C}_2\text{-MXenes}$  and its nanocomposite properties, there has been mathematical modeling of the  $\text{Ti}_3\text{C}_2\text{-MXNC}$ . There have been applications of both analytical and numerical methods available in continuum mechanics theory to  $\text{Ti}_3\text{C}_2\text{-MXNC}$  at the microscale [14–16]. All these works consider the elastic behavior of polymer matrices. With the formation of polymer nanocomposites, the viscoelastic properties of the polymers would play a major role in the nonlinear response of the stress-strain behavior which is observed with many tensile tests conducted on the  $\text{Ti}_3\text{C}_2\text{-MXNC}$  samples [7]. In this paper, the response of the  $\text{Ti}_3\text{C}_2\text{-MXNC}$  is studied using an epoxy-resin polymer matrix, subjected to quasi-static tensile load. Bioinspired nacre-mimetic brick-and-mortar assembly micromechanical modeling along with finite element analysis (FEA) technique (numerical method) is used for these nanocomposites [17]. The polymer matrices are modeled with elastic and viscoelastic (Kelvin-Voigt) behavior. The effective load transfer capability of  $\text{Ti}_3\text{C}_2\text{-MXNC}$  is described using the quasi-static compressive loading for elastic behavior of the  $\text{Ti}_3\text{C}_2\text{-MXene}$ /Epoxy-resin nanocomposite. The properties, modeling, and results are discussed in the succeeding sections. For modeling purposes, the weight fraction of  $\text{MXene}$  and polymers are used in this paper and the units used are mm, N,  $\text{t/mm}^3$  unless otherwise stated.

## 2. Modeling and Methods

### 2.1 Geometric and Elastic properties of $\text{Ti}_3\text{C}_2\text{-MXene}$

$\text{Ti}_3\text{C}_2\text{-MXene}$  monolayers are modeled as a 2D sheet with lateral dimensions of 2 microns and thickness of 2 nanometers for modeling in FEA software – MSC Marc. The elastic properties of  $\text{Ti}_3\text{C}_2\text{-MXene}$  [18] are: Young's

modulus (E) of 312.5 GPa, Poisson's ratio ( $\mu$ ) of 0.2265, Shear modulus (G) of 141 GPa, Density ( $\rho$ ) of  $\sim 3.2 \times 10^{-9} \text{ tmm}^{-3}$  and maximum allowable tensile strength of  $17.3 \pm 1.6 \text{ GPa}$ .

## 2.2 Elastic properties of epoxy-resin

The material properties of the epoxy-resin polymer used in this paper are [17]: Young's modulus (E) of 3.0741 GPa, Poisson's ratio ( $\mu$ ) of 0.29, density ( $\rho$ ) of  $1.1 \times 10^{-9} \text{ tmm}^{-3}$ , and allowable maximum stress of 49.9 MPa.

## 2.3 Viscoelastic modeling of epoxy-resin polymer

Viscoelasticity involves both elastic and viscous behavior modeled together. Among the general viscoelastic models used for polymers, Kelvin-Voigt (KV) model is quite popular and simple for usage. This allows for the rate of change of inelastic strain to be a function of total stress and previously calculated strain in the integration process. An addition creep strain ( $\varepsilon_{ij}^k$ ) is assumed with the general elastic model to implement the KV model in MSC Marc [19]. The constitutive relationship is defined by the equation below, where  $\sigma_{kl}^k$  is deviatoric stress at the end of increment of time.

$$\frac{d}{dt} \varepsilon_{ij}^k = A_{ijkl} \sigma_{kl}^k - B_{ijkl} \varepsilon_{kl}^k \quad \dots\dots \text{Equation (1)}$$

The total strain is given by equation 2 below which contains the instantaneous elastic strain component  $\varepsilon_{ij}^e$ , and KV model strain component  $\varepsilon_{ij}^k$  defined by Equation 1. The time dependency of the strain components introduces the viscoelastic behavior to the implemented models and simulations.

$$\varepsilon_{ij} = \varepsilon_{ij}^e + \varepsilon_{ij}^k \quad \dots\dots \text{Equation (2)}$$

## 2.4 Numerical modeling of Ti<sub>3</sub>C<sub>2</sub>-MXene/Epoxy-resin nanocomposite

The finite element method-based numerical method is used for the analysis of the micromechanical models developed in this paper. The multi-point constraints (MPCs) method available in the FEA environment is used to embed the 2D MXene sheets in the polymer matrix, thus, linking the nodal degrees of freedom of the MXene 2D element with the polymer matrix element. MXene monolayer or flakes of the dimensions mentioned in section 2.1 are created using thick plate elements in MSC Marc software [16] to construct the microscale model. These MXene flakes are embedded in an epoxy-resin matrix which forms the representative volume element (RVE)

structure used for analysis. The perfectly bonded interface assumption is used between the MXenes and epoxy-resin polymer to set up the MPC equations. The MXene flakes with the elastic properties provided in section 2.1 are distributed in the polymer matrix based on bioinspired nacre-mimetic brick-and-mortar assembly [16] to provide enhanced and controllable mechanical properties for the  $\text{Ti}_3\text{C}_2\text{-MXNC}$ .

The RVE cube of  $3.3\ \mu\text{m}$  as the side length is considered. This RVE cube is assigned the epoxy-resin material properties and subdivided into several eight-node three-dimensional brick elements with trilinear interpolation. While the thick plate elements used for the  $\text{Ti}_3\text{C}_2\text{-MXene}$  flakes use a modified version of the first-order shear deformation theory to incorporate formulation of parabolic distribution of transverse shear strains and satisfies the zero transverse shear stress requirements on the plate surface. Virtual tensile and compression quasi-static loading is applied to the RVE models simulating the physical testing conditions in the universal testing machine. To study the micromechanical model response, the quasi-static uniaxial displacement boundary condition is provided at one end and fixed boundary condition at the other for the tensile loads [20]. While one end of the RVE is fixed when a uniaxial compressive load is applied to the models. Finally, the load-displacement relationship of the RVE with viscoelastic matrix behavior is found using the tensile loading condition.

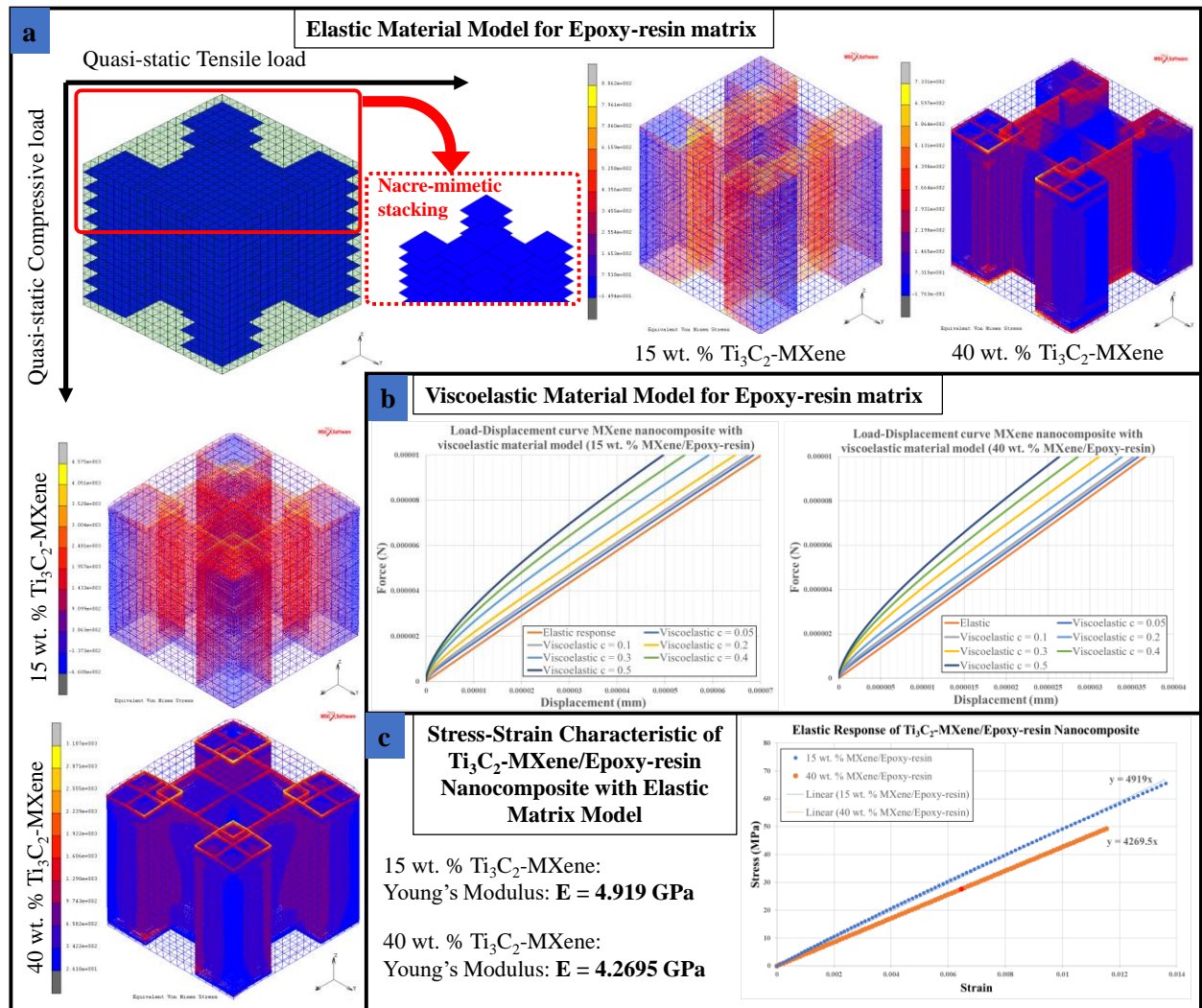
### 3. Results

#### 3.1 Elastic and Viscoelastic response of the $\text{Ti}_3\text{C}_2\text{-MXene/Epoxy-resin}$ nanocomposite with quasi-static tensile load

The  $\text{Ti}_3\text{C}_2\text{-MXene/Epoxy-resin}$  nanocomposite micromechanical model is implemented with 15 and 40 wt. % of  $\text{Ti}_3\text{C}_2\text{-MXene}$  in the epoxy-resin matrix. The qualitative responses of the microscale models for the elastic matrix model are shown in Figures 1 (a). Figure 1 (b) includes a variation of the damping ratio (c) for the KV model from 0.05-0.5 for both 15 and 40 wt. % of  $\text{Ti}_3\text{C}_2\text{-MXene/Epoxy-resin}$  nanocomposite models, demonstrating the effect of damping on the overall MXNC material response. With the increase in the weight fraction of  $\text{Ti}_3\text{C}_2\text{-MXNC}$  from 15 to 40 percent, the stiffness of the equivalent elastic model (simplified spring model capturing the effective behavior) increases from 140 N/m to 270 N/m (from elastic response plotted in Figure 1 (b)). The estimates of the effective Young's modulus of the  $\text{Ti}_3\text{C}_2\text{-MXNC}$  are 4.919 and 4.2695 GPa for 15 and 40 wt. % of  $\text{Ti}_3\text{C}_2\text{-MXene}$  in the epoxy-resin matrix, respectively, shown in Figure 1 (c).

### 3.2 Elastic response of the $\text{Ti}_3\text{C}_2\text{-MXene/Epoxy-resin}$ nanocomposite with a quasi-static compressive load

The nanocomposites models with the same weight fractions described in section 3.1 are subjected to compressive load, where the loading is perpendicular to the stacking of the MXenes in the bioinspired configuration. The qualitative responses of the microscale models are given in Figure 1 (a).



**Figure 1 (a)** Elastic material model of epoxy-resin is used for 15 wt. % and 40 wt. % MXene/Epoxy-resin nanocomposite with quasi-static loading ( $1e-6 \text{ N}$ ) being tensile in the vertical direction (downward) and compressive in the horizontal direction (right). All the analysis results are shown with the equivalent Von-mises stress distribution.

(b) The load v/s displacement characteristics of the quasi-static virtual tensile tests conducted on both 15 wt. % and 40 wt. % MXene/Epoxy-resin nanocomposite are plotted. The epoxy-resin matrix material is modeled with Kelvin-Voigt viscoelastic model in MSC Marc. (c) Numerical results of the stress-strain relationship for 15 wt. % and 40 wt. % MXene/Epoxy-resin nanocomposite models are provided with Young's modulus estimations.

#### 4. Discussion and Conclusions

The bioinspired nacre-mimetic brick-and-mortar assembly model of  $Ti_3C_2$ -MXene in an epoxy-resin polymer matrix is developed with both elastic and viscoelastic material properties of the polymer. The microscale models are implemented with the multi-point constraints method in FEA with  $Ti_3C_2$ -MXene embedded inside the polymer with the nacre-mimetic configuration. The nacre-mimetic topological distribution of  $Ti_3C_2$ -MXene flakes results in an interlocking mechanism at the flake edges. The nacre-mimetic assembly configuration provides an opportunity to tailor the polymer intercalation between the  $Ti_3C_2$ -MXene flakes by assembly control; this also helps in the pre-design of the nanocomposite before the experimentation and in estimating the elastic properties of the composite. The results with elastic material behavior of the epoxy-resin with both tensile and compressive load indicate effective load transfer from the polymer to the  $Ti_3C_2$ -MXene flakes or filler material, thus, resulting in increased load-bearing capacity of the  $Ti_3C_2$ -MXNC. This is also due to the interlocking mechanism provided by the nacre-mimetic distribution. The viscoelastic material model of the polymer allows for the nonlinear response behavior of the nanocomposite to be modeled and an initial implementation with results is provided in this paper. The ability to control the assembly of  $Ti_3C_2$ -MXene in polymer, demonstrated in the literature, is modeled within the numerical method framework to design nanocomposites. Such a design approach can result in the increased mechanical performance of the nanocomposite by considering the trade-off between the load bearing capacity and the damage propagation path. Finally, the nacre-mimetic modeling of  $Ti_3C_2$ -MXNC in combination with the experimental methods would result in effective implementation in mechanical and aerospace applications.

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## Conflict of Interest

There are no conflicts to declare.

## Data Availability

Data sharing not applicable to this article as no datasets were generated or analyzed during the current study.

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