

Article

A solution of the cosmological constant and DE and arrow of time, using Model of a nonsingular universe from Rosen from Volume (56) Ettore Majorana International science series, physics, 1991Andrew Beckwith ¹

1 Physics Department, Chongqing University, College of Physics, Chongqing University Huxi Campus, No. 44 Daxuechen Nanlu, Shapinba District, Chongqing 401331, People's Republic of China, rwill9955b@gmail.com

Abstract:

We reduplicate the Book "Dark Energy" by M. Li, X-D. Li, and Y. Wang, given zero-point energy calculation with an unexpected "length" added to the "width" of a graviton wave just prior to specifying the creation of "gravitons", using the Rosen and Israelit model of a nonsingular universe. In doing so we are in addition to obtaining a wavelength 10^{30} times greater than Planck's length so we can calculate DE, may be able to with the help of the Rosen and Israelit model have a first approximation as to the arrow of time, and a universe with massive gravity. We have left the particulars of the nonsingular starting point undefined but state that the Rosen and Israelit model postulates initial temperatures of 10^{-180} Kelvin and also a value of about Planck temperature, at 10^{-3} centimeters radii value which may satisfy initial conditions asked by t'Hooft for describing an arrow of time. A key assumption is that the DE is formed at 10^{-3} cm, after an expansion of 10^{30} times in radii, from the Planck length radius nonsingular starting point. The given starting point for DE in this set of assumptions is where there is a change in the cosmic acceleration, to a zero value, according to Rosen and Israel, with time $t = 1.31 \times 10^{-42}$ seconds. Which may be where we may specify a potential magnitude, V , which has ties into inflaton physics. The particulars of the model from Rosen and Israelit allow a solution to be found, without discussion of where that nonsingular starting point came from, a point the author found in need of drastic remedies and fixes.

Keywords: Minimum scale factor, cosmological constant, space-time bubble, DE, Arrow of time

1. Introduction

What we are doing is to try to confirm if we can apply the techniques of the following reference to the problem of DE and the arrow of time, and heavy gravity. After work I did in [1] was allegedly not credible, due to people having doubts as to the existence of a multiverse and equating two first integrals as I did, via early pre Planckian space-time, the following reference was accessed [2]. And then applied to [3] and the work on heavy gravity in [4]. In doing so we will keep in mind the t'Hooft memorandum as to the arrow of time, which is in [5] as a basic organizational principle for our discussion, i.e. formation of our program is assuming initial conditions for using [4] in the expansion of the universe say after 10^{-42} seconds

$$m_g = \frac{\hbar\sqrt{\Lambda}}{c}$$

(1)

Whereas we ask for initial conditions for the arrow of time, and Λ and DE formation

2. Methods for defining DE and heavy gravity

We will first start off with the redone calculation as to the Vacuum energy as given in [3] and how we rescale them to be in sync as to the observed experimentally given

value for vacuum energy which is of the present era. This methodology is consistent with the Zero-point energy calculation, we start off with the following as given by [3]

$$\frac{1}{2} \cdot \sum_i \omega_i \equiv V(\text{volume}) \cdot \int_0^{\lambda} \sqrt{k^2 + m^2} \frac{k^2 dk}{4\pi^2} \approx \frac{\lambda^4}{16\pi^2}$$

$$\xrightarrow{\lambda=M_{\text{Planck}}} \rho_{\text{boson}} \approx 2 \times 10^{71} \text{GeV}^4 \approx 10^{119} \cdot \left(\rho_{\text{DE}} = \frac{\Lambda}{8\pi G} \right) \quad (2)$$

In stating this we have to consider that $\rho_{\text{DE}} = \frac{\Lambda}{8\pi G} \approx \hbar \cdot \frac{(2\pi)^4}{\lambda_{\text{DE}}^4}$, so then that

the equation we have to consider is a wavelength $\lambda_{\text{DE}} \approx 10^{30} \ell_{\text{Planck}}$ which is about 10^{30} times a Plank length radius of a space-time bubble. That would

, we have after 10^{-42} seconds

$$\lambda_{\text{DE}} \approx 10^{30} \ell_{\text{Planck}} \quad (3)$$

We then have to consider how to reach the experimental conditions for when

$$\rho_{\text{DE}} = \frac{\Lambda}{8\pi G} \approx \hbar \cdot \frac{(2\pi)^4}{\lambda_{\text{DE}}^4} \quad (4)$$

a nonsingular expansion point for Cosmology, will after 10^{-42} seconds lead to Eq. (4). That means a discussion of what Rosen and Israelit did in [2]. Our point to applying [2] to Eq. (3) is that we have a factor of 10^{30} expansion as to where we can at least measure the onset of DE, for reasons which will be in the next section so Eq. (4) has a value of roughly DE in magnitude as given in [3]

2.1 Looking now at Rosen and Israelit, in terms of Thermodynamics of a non-singular universe

[2] will be relevant for several reasons

A. We will be able to come up with an initial temperature of 10^{-180} Kelvin, at a radius of about Planck length, in value. Almost absolute zero

B. The temperature of space-time will be of the order of Planck Temperature after expansion of about 10^{30} times from the initial nonsingular configuration

C. For making effective use of [3] we will be looking at Eq. (1) to Eq.(4) as being measured after 10^{-42} seconds, which is roughly Planck Time, in this model. I.e. the convention is that we will be using is that Eq.(1) to Eq.(4) will be what [2] calls the pre-matter radiation transition point, in the history of the universe, i.e. go to pages 153 to 154, of [2] and one sees that what I am doing is specifying the formation of Eq. (1) to Eq. (4) at the time the acceleration of the universe stops in its earliest phase, with the formation of DE, and cosmological Constant. We should also keep in mind that A. and B. and C will allow an arrow of time forming due to the

reasons brought up in [5] whereas we have the following Entropy value of [6]

$$S \sim 3 \cdot [1.66\sqrt{g_*}]^2 T^3 \quad (5)$$

Whereas we have that [7] gives us a value $g_* \approx 100 - 110$. Hence it is time to do the

treatment of the temperature values, of what that says about Entropy, and the arrow of time

2.2 Underlying thermodynamics of the Rosen-Israelit nonsingular model

In this section we outline temperature values T at beginning of expansion, at the end of expansion up to when DE is formed and answer if [5] criteria as to forming the arrow of time can be formed according to [5]. While noting the issue of causality and causal relations, in the context of the arrow of time[8] where we take into consideration the following, namely that

Quote

The causal sets program[8] is an approach to quantum gravity. Its founding principles are that spacetime is fundamentally discrete (a collection of discrete spacetime points, called the elements of the causal set) and that spacetime events are related by a partial order. This partial order has the physical meaning of the causality relations between spacetime events

End of quote

What we will assert is that the Rosen result, given in [2] may permit the introduction of the partial order in space-time which may allow for the introduction of quantum gravity

2.3. Formal development of the thermodynamics of space-time and its relations to DE

The key point of this mini chapter will be to summarize the derivation of the temperature[2]

$$T = (\rho_p / \sigma)^{1/4} \cdot \frac{\bar{a}r^7}{(\bar{a}^4 + r^4)^2} \quad (6)$$

Whereas $(\rho_p / \sigma)^{1/4} = 1.574 \times 10^{32} K(kelvin)$, and $\bar{a} = 10^{-3} cm$, whereas

$$\begin{aligned} r_{initial} &= (3/8\pi\rho_p)^{1/2} = 5.58 \times 10^{-34} cm \\ \Rightarrow T_{initial} &= 2.65 \times 10^{-180} K(kelvin) \end{aligned} \quad (6a)$$

$$\begin{aligned} r_{DE-formation} &= \bar{a} = 10^{-3} cm \\ \Rightarrow T_{DE-formation} &= 7.41 \times 10^{31} K(kelvin) \end{aligned} \quad (6b)$$

We will be deriving Eq.(6) as a summary of what to expect in this treatment of nonsingular space-time To do so we start off with [2] in pre matter and radiation periods with entropy S, $\rho = \rho(T), P = P(T)$

$$dS(V, T) = \frac{1}{T} \cdot [d(\rho V) + PdV] \quad (7)$$

$$V = V(volume) = 2\pi^2 r^3 \quad (7a)$$

And an integrability condition on Eq. (6) leading to

$$\frac{dP}{dT} = \frac{1}{T} \cdot (\rho + P) \quad (7b)$$

Then the integral of Eq. (7) is given as

$$S = \frac{V}{T} \cdot (\rho + P) \quad (7c)$$

Also, we look at a given value of pressure as given in [2] for which

$$P = \frac{\rho}{3} \cdot \left(1 - \frac{4\rho}{\rho_p} \right) \quad (8)$$

Put Eq. (7d) into Eq. (7b) and then one will get after integrating Eq. (7b)

$$\rho \cdot \left(1 - \frac{\rho}{\rho_p} \right)^7 = \sigma T^4 \quad (8a)$$

Here, [2] treated σ as the Stephan-Boltzman constant, and so then if we add in the energy equation

$$\dot{\rho} + 3 \cdot (\dot{r} / r) \cdot (\rho + P) = 0 \quad (8b)$$

Then we put in Eq. (8) into Eq. Eq. (8b) we obtain

$$\rho = \tilde{a}^4 \rho_p / (\tilde{a}^4 + r^4) \quad (8c)$$

We claim that Eq. (8c) put into Eq. (8a) we will then obtain Eq. (6) with the conditions as we specified. We assert that we obtain through Eq. (6), Eq. (6a) and Eq.(6b) when the temperature is in the vicinity of Planck temperature, that then we can introduce conditions for which we have Eq. (4) implemented[3]. Where we have a value of Planck's constant is at the value given in Eq. (6b) which [2] is the prematter - radiation boundary, so then that we are initiating DE as a function as the onset of the radiation era of cosmology, and when DE commences we have by Eq.(1) conditions for the onset of gravitational physics

2.4 Analysis of the interrelationship between terms in the inflaton, for cosmology, inhomogeneity and Temperature T, at the prematter-radiation boundary

We are going to use the following result from [9] of

$$\frac{H^2}{\dot{\phi}} \approx 10^{-5} \quad (9)$$

Whereas, we are using by [10] , page 481 of that reference

$$H = 1.66 \sqrt{g_*} \cdot \frac{T_{temp}^2}{m_p} \quad (9a)$$

Whereas we have from [11] the following time derivative value of the inflaton leading to, if we use Eq. (9) and also Eq. (9a)

$$\begin{aligned}
 a(t) &= a_{initial} t^\nu \\
 \Rightarrow \phi &= \ln \left(\sqrt{\frac{8\pi G V_0}{\nu \cdot (3\nu-1)}} \cdot t \right)^{\frac{\nu}{16\pi G}} \\
 \Rightarrow \dot{\phi} &= \sqrt{\frac{\nu}{4\pi G}} \cdot t^{-1} \\
 \Rightarrow \frac{H^2}{\dot{\phi}} &\approx \sqrt{\frac{4\pi G}{\nu}} \cdot t \cdot T^4 \cdot \frac{(1.66)^2 \cdot g_*}{m_p^2} \approx 10^{-5}
 \end{aligned} \tag{10}'$$

If we make use of Planck units, for $t \sim$ Planck time, $G = 1$, and Planck mass set = 1, and Planck Temperature T set also to 1 then Eq.(10) says that the coefficient ν just before turnabout, i.e. where the acceleration of inflation stopped is still very large, but not infinite, whereas if we do not do such Planck units, the terms t times T , representing time, t , and the 4th power of temperature T , mean that if we have, indeed nearly Plank temperatures, for T , that the time element t would be very small and so verifying the largeness of coefficient ν just before we have a cessation of acceleration, initially

If instead of using Eq.(9) for H , we use instead from [11] the following value of H as given in [11] only

$$H^2 = V_0 \exp \left(-\sqrt{\frac{16\pi G}{\nu}} \phi \right) = V_0 \cdot \left(\sqrt{\frac{8\pi G V_0}{\nu \cdot (3\nu-1)}} \cdot t \right)^{\frac{1}{2} \sqrt{\frac{\nu}{\pi G}} - 4 \sqrt{\frac{\pi G}{\nu}}} \tag{11}$$

We then will get

$$\frac{H^2}{\dot{\phi}} \approx \sqrt{\frac{4\pi G}{\nu}} \cdot V_0 \cdot \left(\sqrt{\frac{8\pi G V_0}{\nu \cdot (3\nu-1)}} \right)^{\frac{1}{2} \sqrt{\frac{\nu}{\pi G}} - 4 \sqrt{\frac{\pi G}{\nu}}} t^{\frac{1}{2} \sqrt{\frac{\nu}{\pi G}} - 4 \sqrt{\frac{\pi G}{\nu}} + 1} \approx 10^{-5} \tag{11a}$$

If we wish to just focus upon a general value for this 10^{-5} value, semi independent of time we can set

$$\frac{1}{2} \cdot \sqrt{\frac{\nu}{\pi G}} - 4 \sqrt{\frac{\pi G}{\nu}} + 1 = 0 \tag{11b}$$

A particular solution if we look at Planck units for which $G=1$ is $\nu = 5$ which would then put very precise conditions upon V_0 , i.e. in Planckian units with $G=1$ we would have in Plank units, normalized to = 1

$$\sqrt{\frac{4\pi}{5}} \cdot V_0 \cdot \left(\sqrt{\frac{8\pi V_0}{5 \cdot (14)}} \right)^{\frac{1}{2} \sqrt{\frac{5}{\pi}} - 4 \sqrt{\frac{\pi}{5}}} \approx 10^{-5} \tag{11c}$$

Note this is a particular solution but it would serve to put in approximate values for V_0 about the time we would have the formation of DE, and the cosmological constant, at a time step value approximately

10^{-42} seconds, at the time we have the first case of when the velocity would be maximized in inflation at the boundary of pre-matter and radiation, to quote [2]

2.3 What does Eq. (5) tell us about the arrow of time, problem ? using [2] ?

Were this to be true and the near zero temperature as given by Eq. (6a) versus the near Planck temperature at Eq.(6b), then going to the entropy expression of Eq. (5), we do have in this situation matching the requirements given by 't Hooft, [5] for which we can state that the construction of Eq.(5) combined with 't Hooft's particular solutions for initial conditions to the arrow of time, may indeed give a consistent arrow of time solution

2.4. What about the matter of Causal relations and initial conditions, using Dowker's construction and discussion of Posets ?

The author in [12]. had this initial construction, i.e. and is replicated for the record with several given Changes. We first give an initial equations of [7], [13] and then afterwards relate it to the Dowker [8] results. Here, the idea would be, to make the following equivalence, i.e. look at, [7] where we have what we call Initial entropy value for when we identify the cosmological constant. The value of Eq.(12) is assumed to be in magnitude about 10^{90} or so, which is the value of entropy if we use the following sort of model

$$\left[\left[\frac{\Lambda_{Max} r^4}{8\pi G} \right] \cdot (4/3) \cdot \left[\frac{2\pi^2 g_*}{45} \right]^{1/3} \right]^{3/4} \sim S_{initial} \quad (12)$$

We furthermore, make the assumption of a minimum radius of [14,15] where the r in Eq.(12) is the same in Eq. (13) below, and in magnitude 10^{30} times larger than when Entropy was effectively zero.

$$R_{initial} (\text{when } \Lambda \text{ forms}) = \text{radius is } 10^{30} \text{ Planck length} \quad (13)$$

This Eq. (12) will be put as the minimum value of r, where we have in this situation [16, 17] with M the amount

Space-time matter energy at the start of the radiation era, and $l \approx 10^{29} - 10^{30} \text{ start-radius}$ as given in Eq. (6b), with the start radius when we have almost zero entropy. If so then we have at 10^{-3} centimeters

$$\#bits \sim \left[\frac{E}{\hbar} \cdot \frac{l}{c} \right]^{3/4} \approx \left[\frac{Mc^2}{\hbar} \cdot \frac{l}{c} \right]^{3/4} \quad (14)$$

Needless to say we would have entropy defined as Eq.(14) to the $4/3^{\text{rd}}$ power, as to have a linkage between

Entropy, bits and also the grid points in a space-time lattice which may give us quantum gravity. Afterwards

we likely to keep fidelity with the results we have worked with prior to this section have an invariant cosmological constant and would be applying our inquiry as to the application of Eq.(12) as of about where the cosmological constant formed up in an identifiable manner. Meaning, after 10^{-42} seconds, and at a radius of 10^{-3} centimeters, in line with the mass M being the “equivalent matter energy” at the boundary between pre matter states, and radiation as given in [2]. Keep in mind that the Energy E as given in Eq.(14) would have

a temperature dependence as given in Eq.(6b) with an input parameter of E which can go into Eq.(14)

$$E = \frac{k_B(\text{dim-space-time})}{2} \cdot T \quad (15)$$

The points where we have bits, as computationally given would be the grid points to the Poset argument as in [8]

Whereas we can give the following relationship as to specify the inter-relationship between E and time. We pick

Entropy as represented by an energy term E driving the entropy as given by T temperature dependence

As given in Eq.(15), whereas we use the cube of the same Temperature T driving entropy in Eq. (12)

2.5 Coming up with a “modified HUP so as to obtain the grid points implied by Eq. (14)

Shalyt-Margolin and Tregubovich (2004, p.73)[18], Shalyt-Margolin (2005, p.62)[19][20] have this

Relationship. Here Delta E is assumed to be consistent in a change in energy from almost zero to the

Energy value givein in Eq. (15)

$$\begin{aligned} \Delta t \geq \frac{\hbar}{\Delta E} + \gamma t_P^2 \frac{\Delta E}{\hbar} \Rightarrow (\Delta E)^2 - \frac{\hbar \Delta t}{\gamma t_P^2} (\Delta E)^1 + \frac{\hbar^2}{\gamma t_P^2} = 0 \\ \Rightarrow \Delta E = \frac{\hbar \Delta t}{2 \gamma t_P^2} \cdot \left(1 + \sqrt{1 - \frac{4 \hbar^2}{\gamma t_P^2 \cdot \left(\frac{\hbar \Delta t}{2 \gamma t_P^2} \right)^2}} \right) = \frac{\hbar \Delta t}{2 \gamma t_P^2} \cdot \left(1 \pm \sqrt{1 - \frac{16 \hbar^2 \gamma t_P^2}{(\hbar \Delta t)^2}} \right) \end{aligned} \quad (16)$$

For sufficiently small γ . The above could be represented by[20]

$$\begin{aligned} \Delta E \approx \frac{\hbar \Delta t}{2 \gamma t_P^2} \cdot \left(1 \pm \left(1 - \frac{8 \hbar^2 \gamma t_P^2}{(\hbar \Delta t)^2} \right) \right) \\ \Rightarrow \Delta E \approx \text{either } \frac{\hbar \Delta t}{2 \gamma t_P^2} \cdot \frac{8 \hbar^2 \gamma t_P^2}{(\hbar \Delta t)^2}, \text{ or } \frac{\hbar \Delta t}{2 \gamma t_P^2} \cdot \left(2 - \frac{8 \hbar^2 \gamma t_P^2}{(\hbar \Delta t)^2} \right) \end{aligned} \quad (17)$$

This would lead to a minimal relationship between change in E and change in time as

represented by Eq. (17), so that we could to first order, say be looking at something very close to the traditional Heisenberg uncertainty principle results of approximately

$$\Delta E \approx \frac{\hbar \Delta t}{2 \gamma t_P^2} \cdot \frac{8 \hbar^2 \gamma t_P^2}{(\hbar \Delta t)^2} \equiv \frac{4 \hbar}{\Delta t} \quad (18)$$

Or

$$\Delta E \Delta t \approx 4\hbar \quad (19)$$

i.e. stepping through an iteration of delta t, per causal structure in early space-time would with refinements

help construct the grid and causal structures alluded to in [8], in particular see her discussion of the causal set given

in page 3 of [8] whereas the grid defined by [8] would reflect the computational ‘bits’ given in Eq. (14)

3. Good points and limitations as to the given analysis, and what needs to be filled in

Our analysis has given evidence that we can satisfy the “tHoof” idea of special initial conditions as to forming the arrow of time. This is important, since there is a basic symmetry in the GR equations of space-time, which means forming the arrow of time, will necessitate specialized initial conditions even if the general GR equations do NOT depend upon specialized initial conditions. In addition, in the face of virtually unanimous complaints on the part of reviewers, the author has avoided describing the particular origins of a non singular start to expansion of the universe. The Rosen and Israel model assumes this nonsingular start, as seen in [2], without trying to derive where it came from. The author states that [2] gives a thermodynamically consistent nonsingular universe model which satisfied a mathematically consistent origin to the arrow of time problem

Due to the quirkiness of the [2] model, Rosen and Israelit also called the start of this expansion as a Point of zero time. That is right. The start to expansion is called time value “zero”

The unusual nature of this designation allowed the author to then go to a minimum time step, delta t which may be measurable, if one obtains in data sets a boundary regime which delineates the start of the radiation regime in cosmology.

Now for the limitations

The author abandoned any attempt in this document to specify WHERE the nonsingular start to cosmological expansion came from. As a physics researcher, this is an appalling omission, and is only done due to the innate conservatism of the general research community. What is mandatory is that a derivational approach to the origins of this nonsingular start be somehow meshed into a research program of hopefully gravitational physics data sets. In addition, [21] in terms of holographic principle applications of an interrelationship between the mass of a graviton and information needs to be explored In lieu of specifying the time of delta t approximately 10^−42 seconds and a defined initial space-time the Following was obtained in terms of probable GW signals, from this early universe configuration

3.1 How do we obtain relic high frequency Gravity waves?

With redshift about $z = 10^{25}$ we go work with the following approximation

$$\begin{aligned} (1 + z_{\text{initial-era}}) &\equiv \frac{a_{\text{today}}}{a_{\text{initial-era}}} \approx \left(\frac{\omega_{\text{Earth-orbit}}}{\omega_{\text{initial-era}}} \right)^{-1} \\ &\Rightarrow (1 + z_{\text{initial-era}}) \omega_{\text{Earth-orbit}} \approx 10^{25} \omega_{\text{Earth-orbit}} \approx \omega_{\text{initial-era}} \end{aligned} \quad (20)$$

We postulate that we specify an initial era frequency via dimensional analysis which is slightly modified by

Maggiore for the speed of a graviton[22] whereas we use that we assume having the following relationship of

$c(\text{light-speed}) \approx \omega_{\text{initial-era}} \cdot (\lambda_{\text{initial-post-bubble}} = \ell_{\text{Planck}})$ and that dimensional comparison with initially

having a temperature built up so as $\Delta E \approx \hbar \omega_{initial-era}$ where $T_{universe} \approx T_{Plank-temerature} = 1.22 \times 10^{19} \text{ GeV}$.

If so then the initial temperature would be extremely high leading to a change in temperature from Pre Planckian

conditions to Planck era. Where we would be assuming $\omega_{initial-era} \approx \frac{c}{\ell_{planck}} \leq 1.8549 \times 10^{43} \text{ Hz}$ so then we

would be looking at having frequencies on Earth from gravitons of mass m(graviton) less than of equal to

$$\omega_{Earth-orbit} \leq 10^{-25} \omega_{initial-era} \quad (21)$$

This is what would necessitate new technological developments and likely space-borne systems to analyze

The final point being that the brilliant work done by Rosen in [24] needs to be explored as possibly being

relevant to the origins of the nonsingular start to the cosmological expansion. The author views [23] as a

worthy starting point to quantum mechanical analogues which may explain this datum, missing in the [2]

nonsingular start to the present universe which should be explored, as to its relevance to quantum mechanics and

near space-time singularities. Rosen's [23] model may provide a bridge between interior conditions which may

exist in a nonsingular start to expansion of the universe, and what is happening in our present cosmos. That as

doing generalizations of what Ng [17] proposed as far as infinite quantum statistics for a counting algorithm

approach to early universe entropy. We also view that what is presented in [24] as to a quantum vacuum

will be decisively important to explain the transition from the preinflationary state, as implied by reference

[2] and the rapid expansion as given in Eq. (6), Eq. (6a) and Eq.(6b)

3.2 Future research objectives which will be addressed in the next publication

The author intends to answer the model dependent construction given by Ng

For Dark Energy in [25] as well as review again the following, as in [26]. In [26], there is a quantum bounce reference to the destruction of primordial black holes which is given as when the density of our universe climbs

to a value given as $\omega_Q = p_Q / \rho_Q$ is defined, with the numerator being the pressure, and denominator

density of phantom fields. which leads to [26] a density for which there is breakup of primordial black holes

$$\rho_{BH} \approx M_p^4 \cdot \left(\frac{M_p^2}{M^2} \right) \cdot \left(\frac{3}{32\pi} \right) \cdot \frac{1}{|1 + \omega_Q|} \quad (22)$$

This phenomenon of a break up of black holes due to early space-time density may be a significant Contributor to the development of Dark Energy, and we will ascertain this carefully, in a future Publication. Both [25] and [26] have model related issues which in part elaborate upon our use of [2] and [3] for DE contributions in the early universe

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References

1. Andrew Walcott Beckwith, "Using "Enhanced Quantization" to Bound the Cosmological Constant, (for a Bound-on Graviton Mass), by Comparing Two Action Integrals (One Being from General Relativity) at the Start of Inflation", pp 21-36, of " Fundamental Physics and Physics Education Research", editors of Burra G. Sidharth • Jesús Carnicer Murillo • Marisa Michelini • Carmen Perea, Published by Springer Nature Switzerland AG 2021 , in Gewerbestrasse 11, 6330 Cham, Switzerland
2. Rosen N., Israelit M. (1991) A Simple Model of the Universe without Singularities. In: Zichichi A., de Sabbata V., Sánchez N. (eds) Gravitation and Modern Cosmology. Ettore Majorana International Science Series, vol 56. Springer, Boston, MA. https://doi.org/10.1007/978-1-4899-0620-5_14
3. Miao Li (Author), Xiao-Dong Li (Contributor), Shuang Wang (Contributor), Yi Wang (Contributor), "Dark Energy", Peking University Press, World Scientific, Singapore, Republic of Singapore, 2015
4. Novello, M. (2005) The Mass of the Graviton and the Cosmological Constant Puzzle. <https://arxiv.org/abs/astro-ph/0504505>
5. Gerard 't Hooft', "time, the Arrow of time and Quantum Mechanics", Front. Phys., 29 August 2018 | <https://doi.org/10.3389/fphy.2018.00081>
6. Beckwith, A.W. (2018) Initial Conditions for Defining an Arrow of Time at the Start of Inflation? Journal of High Energy Physics, Gravitation and Cosmology, 4, 787-795. <https://doi.org/10.4236/jhepgc.2018.44044>
7. E. Kolb, and S. Turner "The Early Universe", Westview Press, Chicago, USA, 1994
8. Dowker,Fay, "Causal sets and the Deep Structure of space-time", <https://arxiv.org/abs/gr-qc/0508109>
9. Winitzki, Sergi, " Eternal Inflation", World Scientific Publishing Co., Pte. Ltd. Singapore, the Republic of Singapore, 2009
10. Sarkar, Utpal, "Particle and Astroparticle Physics", Taylor & Francis Group, New York City, New York, USA, 2008
11. Padmanabhan, Thanu, "An Invitation to Astrophysics", World Press Scientific, World Scientific Series in Astronomy and Astrophysics: Volume 8, Singapore, Republic of Singapore, 2006
12. Beckwith, A.W. (2018) How a Minimum Time Step and Formation of Initial Causal Structure in Space-Time May Void the Penrose Singularity Theorem, as in Hawking and Ellis's 1973 Write-Ups. Journal of High Energy Physics, Gravitation and Cosmology, 4, 485-49

13. Mukhanov, V. "Physical Foundations of Cosmology", Cambridge University Press, New York City, New York, USA, 2005
14. Camara, C.S., de Garcia Maia, M.R., Carvalho, J.C. and Lima, J.A.S. (2004) Nonsingular FRW Cosmology and Non Linear Dynamics. Arxiv astro-ph/0402311 Version 1.
15. Beckwith, A. (2016) Gedanken Experiment for Refining the Unruh Metric Tensor Uncertainty Principle via Schwarzschild Geometry and Planckian Space-Time with Initial Nonzero Entropy and Applying the Riemannian-Penrose Inequality and Initial Kinetic Energy for a Lower Bound to Graviton Mass (Massive Gravity). Journal of High Energy Physics, Gravitation and Cosmology, 2, 106-124.
<https://doi.org/10.4236/jhepgc.2016.21012>
16. Park, D., Kim, H. and Tamarayan, S. (2002) Nonvanishing Cosmological Constant of Flat Universe in Brane-World Scenario. Physics Letters B, 535, 5-10. [https://doi.org/10.1016/S0370-2693\(02\)01729-X](https://doi.org/10.1016/S0370-2693(02)01729-X)
17. Ng, Y.J. (2007) Holographic Foam, Dark Energy and Infinite Statistics. Physics Letters B, 657, 10-14. <https://doi.org/10.1016/j.physletb.2007.09.052>
18. Shalyt-Margolin, A. E., (2006) Deformed Density Matrix and 21 Quantum Entropy of the Black Hole, Entropy 8, no 1, 31 – 43
19. Shalyt-Margolin, A.E., (2005, 1) The Density Matrix Deformation in Physics of the Early Universe and Some of its Implications, "Quantum Cosmology Research Trends .Chapter2." Horizons in World Physics, Vol. 246, 49–91, Nova Science Publishers, Inc., Hauppauge, NY
20. Shalyt-Margolin, A.E., Tregubovich, A.Ya., (2004) Deformed Density Matrix and Generalized Uncertainty Relation in Thermodynamics, Modern Physics Letters A.19. no 1, 71–81
21. Ioannis Haranas1 and Ioannis Gkigkitzis," The Mass of Graviton and Its Relation to the Number of Information according to the Holographic Principle", Hindawi Publishing Corporation International Scholarly Research Notices Volume 2014, Article ID 718251, 8 pages <http://dx.doi.org/10.1155/2014/718251>
22. Maggiorie, Michele, " Gravitational waves, Volume 1, theory and Experiment", Oxford University Press, New York City, New York, USA, 2008
23. Nathan Rosen," Quantum Mechanics of a Miniuniverse", International Journal of Theoretical Physics, Vol. 32, No. 8, 1993
24. Wang, Qingdi; Zhu, Zhen; [Unruh, William G.](#) (2017). "How the huge energy of quantum vacuum gravitates to drive the slow accelerating expansion of the Universe". *Physical Review D*. 95(10): 103504. [arXiv:1703.00543](#)
25. Ng, Y. Jack, Holographic Foam Cosmology: From the Late to the Early Universe. Symmetry 2021, 13, 435. <https://doi.org/10.3390/sym13030435>
26. Katherine Freeze, Mathew Brown, and William Kinney, "The Phantom Bounce, A new proposal for an oscillating Cosmology", pp 149-156, of " The Arrows of Time, A debate in cosmology", Fundamental theories in physics, Volume 172, with Laura Mercini-Houghton, and Rudy Vaas , editors, Springer Verlag, Heidelberg, Federal Republic of Germany, 2012