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Investigating the Converter-Driven Stability of an Offshore HVDC System

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Abstract: Offshore wind farms are increasingly built in the North Sea and the number of HVDC systems transmitting the wind power to shore increases as well. To connect offshore wind farms to adjacent AC transmission systems, onshore and offshore modular multilevel converters transform the transmitted power from AC to DC and vice versa. Besides, modern wind farms mainly use wind turbines connected to the offshore point of common coupling via voltage source converters. However, converters and their control systems can cause unwanted interactions, referred to as converter-driven stability problems. The resulting instabilities can be predicted by applying an impedance-based analysis in the frequency domain. Considering that the converter models and system data are often confidential and cannot be exchanged in real systems, this paper proposes an enhanced impedance measurement method suitable for black-box applications to investigate the interactions. The proposed method is applied to assess an offshore HVDC system’s converter-driven stability, using impedance measurements of laboratory converters and a wind turbine converter controller replica. The results show that the onshore modular multilevel converter’s interactions with AC grids of moderate short-circuit ratios can lead to instabilities. The offshore system analysis reveals that considering the offshore grid topology is crucial for assessing interactions between the wind turbine controllers and the offshore modular multilevel converter. It is shown that different stability margins result from varying offshore grid layouts.

Keywords: Converter-driven stability; HVDC; Offshore, MMC, Converter, Replica, impedance-based stability analysis, Interactions.

1. Introduction

With the increasing number of High-Voltage Direct Current (HVDC) links integrated into the Alternating Current (AC) transmission system, converters and, therefore, power electronics relying on complex control systems play a more dominant role in system stability. In particular, remote offshore wind farms are connected by high-voltage cables and rely on HVDC technology due to the high reactive power demand of AC-based systems. Besides, modern wind farms utilize mainly fully-scaled Voltage Source Converters (VSCs) for the offshore grid connection. VSCs and state-of-the-art HVDC converters, such as Modular Multilevel Converters (MMCs), have response times that are significantly faster compared to traditional power system components [1]. Several interactions of converters with the connected AC system or other converters have been reported. For instance, in 2014, the offshore wind farm Bard Offshore 1 had to be shut down due to high oscillations. Also, the 2015-commissioned HVDC INELFE system connecting Spain and France experienced resonances between the HVDC system and the AC grid [2,3]. Furthermore, unexpected oscillations were observed in a weak part of China Southern Grid’s transmission system after a Static Synchronous Compensator (STATCOM) was put into operation [4].
Consequently, electromagnetic phenomena need to be considered for assessing the stability of modern power systems. Hence, the classical power system stability classification was extended to consider the impact of power-electronic interfaced technology [5]. Whereas this interaction phenomenon is often referred to as harmonic stability in the literature [6,7], the updated stability definition classifies the aforementioned interaction incidents as converter-driven stability with fast interactions [5]. Converter-driven instabilities are mainly caused by the converters’ control system that interacts with the AC grid impedance [5,8]. However, disclosing manufacturer-specific converter control systems is highly improbable due to intellectual property concerns [9], making it challenging to model the converters’ real frequency behavior. Also, Transmission System Operators (TSOs) are unlikely to share details of their grid models with other parties.

A promising method to investigate converter-driven stability problems is the Impedance-based Stability Criterion (IbSC) that models a system as two subsystems with frequency-dependent impedances and uses classical control theory to assess the stability in the frequency domain [10,11]. The IbSC allows for a direct and straightforward stability assessment. By providing Phase Margins (PMs), it indicates how close a system is to instability [6,12]. It can also be consecutively applied to assess the stability of large-scale systems by defining different interfaces, and subsystems [13]. Moreover, due to little computation times, numerous scenarios can be investigated, which would not be possible when using Electromagnetic Transient (EMT) simulations [6,12]. The IbSC requires frequency-dependent impedance models of the system components which can be derived analytically using small-signal linearization techniques [14–16] or numerically on the basis of EMT simulations or measurements using frequency sweep techniques [17,18].

In the literature, stability analyses often utilize analytical impedance models derived based on the full knowledge of the system [12,19–21]. However, while this approach offers excellent insight into the cause of interactions, it does not allow for stability analyses of black-boxed systems and is not applicable for industrial applications. Moreover, analytical models often simplify the electrical structure of converters so that the real frequency behavior of components might not be considered [22–24]. Also, the models often neglect control loops, assuming that they are not relevant [14]. Due to the three-phase nature of the transmission system, authors advocate modeling the impedances in the dq-domain [25,26]. Couplings between phases and frequencies are included in the models using a 2x2 impedance matrix. The authors demonstrate that neglecting the coupling can result in false stability predictions [26,27]. However, approaches that rely on impedance representations in the dq-domain require the definition of a common reference angle $\theta$ for the impedances [28–30]. Therefore, this approach makes it challenging to use different entities’ impedance models (e.g., converter manufacturer and TSO). They would have to align their models on a reference angle which is not applicable for industrial studies.

As a result, utilized approaches are not aimed at investigating real and industrial systems. They cannot be applied to black-boxed systems such as converter controller replicas, representing the frequency behavior of industrial control systems. Thus, this paper builds upon a frequency-sweep approach to assess the converter-driven stability [31,32]. Not requiring full-system knowledge, this approach makes it possible to employ impedance models of a black-boxed system such as a converter controller replica or measurement-based models of physical laboratory converters. Besides, models can be provided by different entities for the stability assessment. In this paper, the proposed impedance derivation method in [31,32] is extended to include additional coupling currents resulting from the frequency sweep measurements. To determine these additional coupling currents, the spectrum of physical MMCs is analyzed using a laboratory system – here referred to as the MMC Test Bench (TB). The derived MMC impedances are used to investigate the stability of an MMC in grid-following control mode and the adjacent AC system, representing the onshore side of an HVDC link.
On the offshore side, the stability of a wind farm and the offshore MMC operating in grid-forming control mode is investigated utilizing the impedance measurement of an offshore Wind Turbine (WT) VSC controller replica.

The paper is structured as follows: First, the IbSC is presented, and an overview of the impedance derivation approach is given. The IbSC is validated by comparing the stability predictions to the results of an EMT time-domain simulation. Subsequently, section 3 demonstrates the extended frequency-sweep approach and shows how the additional measurements are incorporated in the impedance models. Section 4 presents the Control Hardware in the Loop (CHiL) TB setup for the WT VSC controller replica impedance measurement. Based on the derived impedance models, the following stability analysis in section 5 presents and discusses the results of the onshore and offshore test case. Concluding the paper, the main findings are given in section 6.

2. Impedance-based Stability Assessment

2.1. Impedance-based Stability Criterion

Initially developed for the design of input filters of converters [10,33], the IbSC is a widely used method to assess converter-driven stability in the frequency domain. Because the method avoids time-consuming EMT simulations, it facilitates the analysis of numerous test cases [6,12]. Assuming that a system can be divided into two separate subsystems, the stability can be assessed by classical control theory tools such as the Nyquist criterion or Bode plots analyzing the loop gain of the system. Figure 1 shows the equivalent circuit diagram of a system divided into two subsystems representing a converter and an AC grid, aiming to assess interactions between the subsystems’ impedances.

Figure 1. Equivalent circuit diagram of investigated system.

The frequency behavior of the subsystems is modeled by the respective admittance $Y_C(j\omega)$ and impedance $Z_G(j\omega)$ with $\omega = 2\pi$. Deriving the current to

$$I_C(j\omega) = I_C(j\omega) \frac{1}{1 + Y_C(j\omega)Z_G(j\omega)} - U_g(j\omega) \frac{Y_C(j\omega)}{1 + Y_C(j\omega)Z_G(j\omega)} \tag{1}$$

which can be rearranged to

$$I_C(j\omega) = \left[I_C(j\omega) - U_g(j\omega) \cdot Y_C(j\omega)\right] \cdot \frac{1}{1 + Y_C(j\omega) \cdot Z_G(j\omega)} \tag{2}$$

shows that the system resembles that of a negative feedback loop system, as shown in Figure 2.
As a result, the feedback loop gain $Y_C (j\omega) Z_G (j\omega)$ can be evaluated by the simplified Nyquist criterion to determine the stability of the overall system. Assuming an open-loop stable system that does not contain any right-half plane poles, the system’s stability can be graphically assessed. This assumption implies that both subsystems’ impedances and admittances need to be individually stable. This means that the subsystem with the admittance $Y_C$ is stable if it can operate in ideal grid conditions (infinite short-circuit power) and that the subsystem with the impedance $Z_G$ is stable in no-load conditions [11]. These conditions are typically fulfilled, since a converter should be able to operate stably in ideal conditions, and the AC grid should be stable when not connected to the converter. In addition to the Nyquist plot, a Bode plot analysis offers a more intuitive stability assessment. By calculating the phase difference of $Y_C (j\omega)$ and $Z_G (j\omega)$ at the magnitude intersection frequencies, the PM can be determined showing how close the system is to instability. However, considering only the PM for stability assessments can lead to false stability predictions in certain situations when the slope of the impedance phase is not evaluated [34]. As a result, additional magnitude and phase conditions should be considered [34] if the results are not verified by additional Nyquist plots.

2.2. Impedance Model Derivation

Using the IbSC to assess converter-driven stability requires the derivation of impedance models that represent the frequency behavior of the investigated components and systems. Impedance models are typically derived in the dq-domain [6,27] or in positive and negative sequence [35,36]. As pointed out in section 1, dq-domain impedance models contradict the objective of this work that the impedance models can be derived independently and exchanged between two different parties without harmonization [29]. However, sequence-domain impedance models do not inherently consider couplings between frequencies [26]. Thus, in this work, impedances are derived in the sequence domain that allows for separate positive- and negative-sequence impedance models [35]. To determine the impact of couplings, the frequency spectrum is evaluated for potential coupling frequencies that affect the impedances [37].

Impedance models of active components such as MMCs can be derived analytically by deriving transfer functions based on the electrical model and the block diagrams of the converter control system [19,20,24]. While this approach offers insight into the causes and dependencies of different controllers and parameters on the system stability, it requires full knowledge of the converter and its control system. Therefore, analytically-derived impedances cannot be used when investigating the frequency behavior of black-boxed manufacturer converters such as converter controller replica systems.
The stability is assessed for different AC grid impedances with varying short-circuit power $S_{SC,G}$. Simulating the same system and scenarios in the time-domain verifies the frequency-domain results. Figure 4 shows the system used for the validation. On the Direct Current (DC) side of the MMC, the voltage is held constant to $U_{DC}$. The simulated MMC model is based on a Type 5 Average Value model consisting of controlled voltage sources that represent the Submodule (SM) string of each arm [38]. The parameters of the simulated MMC model are given in Table 1. The MMC control system is a cascaded vector control and is designed as an energy-based control, where the energy control loops of the MMC are explicitly implemented [39]. The AC grid is modelled as a Thevenin equivalent voltage source $U_G$ with the grid impedance $Z_G = R_G + j2\pi f_G I_G$. Its parameters are given in Table 2 and depend on the Short-Circuit Ratio (SCR) that is defined as

\[
Z_G = \frac{U_G}{I_G} = R_G + j2\pi f_G I_G
\]
\[ SCR = \frac{S_{DC,G}}{P_{n,MMC}}. \] (3)

Typically, the SCR is considerate high for \( SCR \geq 5 \), moderate for \( 3 < SCR < 5 \), low for \( SCR \leq 3 \), and very low for \( SCR \leq 2 \) [40].

![Diagram of MMC connected to AC grid](image)

**Figure 4.** MMC connected to AC grid.

**Table 1.** Simulated MMC model parameters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Variable</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Converter power</td>
<td>( P_{n,MMC} )</td>
<td>1200 MW</td>
</tr>
<tr>
<td>DC voltage</td>
<td>( U_{DC,u} )</td>
<td>640 kV</td>
</tr>
<tr>
<td>Arm inductance</td>
<td>( L_{Arm} )</td>
<td>46.2 mH</td>
</tr>
<tr>
<td>Resistance arm inductance</td>
<td>( R_{Arm} )</td>
<td>0.08 Ω</td>
</tr>
<tr>
<td>On resistance</td>
<td>( R_{SM,\text{on}} )</td>
<td>0.08 Ω</td>
</tr>
<tr>
<td>Number of SMs</td>
<td>( n_{SM} )</td>
<td>350</td>
</tr>
<tr>
<td>SM capacity</td>
<td>( C_{SM} )</td>
<td>8.8 mF</td>
</tr>
<tr>
<td>AC primary voltage</td>
<td>( U_{AC,1} )</td>
<td>400 kV</td>
</tr>
<tr>
<td>AC secondary voltage</td>
<td>( U_{AC,2} )</td>
<td>350 kV</td>
</tr>
<tr>
<td>Transformer reactance</td>
<td>( R_{AC,1} )</td>
<td>0.316 (21) Ω</td>
</tr>
<tr>
<td>Transformer inductance</td>
<td>( L_{AC,1} )</td>
<td>0.403 mH</td>
</tr>
<tr>
<td>Transformer reactance</td>
<td>( R_{AC,2} )</td>
<td>0.726 Ω</td>
</tr>
<tr>
<td>Transformer inductance</td>
<td>( L_{AC,2} )</td>
<td>0.924 (73) mH</td>
</tr>
</tbody>
</table>

### 2.3.1. Frequency-Domain Stability Assessment

The converter-driven stability of the AC grid and the simulated MMC model circuit is assessed by the \( \text{IbSC} \). Controlling the grid current, the MMC impedance \( Z_{MMC}(j\omega) \) represents the converter admittance in the equivalent circuit diagram shown in Figure 1, resulting in the loop gain \( Z_{G}(j\omega) \). For simplicity, hereinafter, the argument of the variables is indicated by the frequency only, while still referring to a complex variable. The PMs of the system are then derived at the intersection frequencies \( f_{PM} \) where

\[ |Z_{G}(f_{PM})| = |Z_{MMC}(f_{PM})|. \] (4)

Subtracting the phase angle difference at \( f_{PM} \) from 180° makes it possible to graphically determine the PMs of the Bode plot with
Table 2. AC grid impedance parameters.

<table>
<thead>
<tr>
<th>SCR</th>
<th>$S_{SC,G}$ [GVA]</th>
<th>$R_G$ [$\Omega$]</th>
<th>$L_G$ [mH]</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>4.8</td>
<td>3.3168</td>
<td>105.58</td>
</tr>
<tr>
<td>5</td>
<td>6.0</td>
<td>2.6534</td>
<td>84.46</td>
</tr>
<tr>
<td>6</td>
<td>7.2</td>
<td>2.2112</td>
<td>70.38</td>
</tr>
<tr>
<td>7</td>
<td>8.4</td>
<td>1.8953</td>
<td>60.33</td>
</tr>
</tbody>
</table>

$$PM = 180^\circ - \arg\left(\frac{Z_G(f_{PM})}{Z_{MMC}(f_{PM})}\right) = 180^\circ - \arg(Z_G(f_{PM}) - Z_G(f_{PM})).$$ (5)

To assess the system’s overall stability, both positive- and negative-sequence systems need to be considered [35]. If either the positive-sequence or the negative-sequence system analysis determines an unstable system, the overall system is considered to be unstable. If both positive- and negative-sequence systems are stable, then also the overall system is concluded to be stable. Therefore, Figure 5 and 6 depict the Bode plots for positive- and negative-sequence impedances. They show that the magnitude of the MMC intersects those of the AC grid at frequencies close to 100 Hz and 200 Hz, respectively. Furthermore, the plots reveal that with decreasing SCR, the intersection frequencies decrease also. For lower frequencies, the differences of the phase angle increase, potentially reaching 180° and leading to a negative PM.

Figure 5. MMC impedance and AC grid impedance for different SCRs.
Figure 6. MMC impedance and AC grid impedance for different SCRs.

Figure 7. Close up of MMC and AC grid impedance intersections for (a) positive-sequence and (b) negative-sequence impedances.

Figure 7 (a) and (b) show a close-up of the Bode plots around the intersection frequencies for the different SCRs. Marking the magnitudes and phase angles at $f_{PM}$, they reveal that for a $SCR = 4$, the phase difference exceeds $180^\circ$ for the positive-sequence
impedance. The PMs given in Table 3 show that for a SCR = 4 and $f_{PM, pos} = 91$ Hz, the PM is negative indicating that the system becomes unstable when the SCR is decreased from 5 to 4. Because the the PM provides only a sufficient stability condition [34], the results of the Bode plot analysis are verified by additional Nyquist plots presented in Figure A1 in the appendix, showing a clock-wise encirclement of the $(-1, j0)$ point for SCR = 4 and the positive-sequence impedance.

### Table 3. Phase Margins for positive- and negative-sequence impedances.

<table>
<thead>
<tr>
<th>SCR</th>
<th>$f_{PM, pos}$</th>
<th>$PM_{pos}$</th>
<th>$f_{PM, neg}$</th>
<th>$PM_{neg}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>91 Hz</td>
<td>$-10^\circ$</td>
<td>172 Hz</td>
<td>17°</td>
</tr>
<tr>
<td>5</td>
<td>106 Hz</td>
<td>8°</td>
<td>189 Hz</td>
<td>30°</td>
</tr>
<tr>
<td>6</td>
<td>119 Hz</td>
<td>20°</td>
<td>208 Hz</td>
<td>41°</td>
</tr>
<tr>
<td>7</td>
<td>133 Hz</td>
<td>31°</td>
<td>227 Hz</td>
<td>51°</td>
</tr>
</tbody>
</table>

#### 2.3.2. Time-Domain Validation

The results of the frequency-domain stability assessments are verified by time-domain simulations of the same system in Matlab/Simulink. Therefore, the MMC model is connected to AC grids with varying SCRs. To ensure an initial stable operation point, the MMC is initially started when being connected to a strong AC grid. Figure 8 shows the current at the MMC AC terminal. After $t = 4$ s, the MMC is switched to an AC grid impedance with SCR = 7. Every two seconds, the AC grid impedance is reduced by an SCR value of 1. As predicted in the frequency-domain analysis, the system remains stable for AC grid impedances with an SCR = 7 to 5. The current and voltages in Figure 9 show that high oscillations occur and an unstable operation point is reached when switching to an AC grid with SCR = 4.

![AC Terminal Current](image)

**Figure 8.** AC terminal current when MMC is connected to AC grids with decreasing SCR.

Figure 10 shows the frequency spectrum of the AC terminal current and voltage after switching. Showing oscillations with a frequency of 94.5 Hz, the spectrum agrees with the previously predicted instability at $f = 91$ Hz. Thus, the results demonstrate that the IbSC is able to accurately assess the converter-driven stability of a system using numerically derived impedance models.
Figure 9. AC terminal current (a) and voltage (b) when switched to an AC grid with SCR = 4.

Figure 10. Fourier spectrum of phase a of the AC terminal current (a) and voltage (b) when connected to an AC grid with SCR = 4.

3. Extended MMC Impedance Derivation Method

Representing the frequency behavior of the MMCs, in this work, the corresponding impedance models are derived based on physical laboratory converters using the MMC TB laboratory at RWTH Aachen University. Thus, inaccuracies due to model simplifications can be avoided, and the impedance derivation method is demonstrated in a laboratory environment. First, the frequency spectrum of the MMC TB response is evaluated when being subjected to different perturbation signals to determine relevant frequency components. The MMC TB laboratory consists of several real-time simulators and low-voltage MMCs with the parameters given in Table 4 [41]. For measuring the MMC impedances, two MMCs are physically connected through Pi-sections on the DC side and coupled with real-time simulators through power amplifiers on the AC side [32]. The control system is identical to the controls of the simulated MMC model. The MMC TB impedance $|Z_{TB}|e^{j\theta}$ is scaled up according to the scaling factors $|k|$ and $k_\phi$.
to align with the AC grid impedance and the 1 MW wind turbine VSC. The scaled MMC TB impedance is

\[ Z_{TB,scaled} = |k| \cdot |Z_{TB}| e^{\rho_{TB} - k_{\phi}} \]  

with

\[ |k| = \sqrt{\frac{r_{FS}^2 + (\omega \cdot l_{FS})^2}{r_{TB}^2 + (\omega \cdot l_{TB})^2}} \]  

and

\[ k_{\phi} = \arctan \frac{r_{FS}}{\omega \cdot l_{FS}} - \arctan \frac{r_{TB}}{\omega \cdot l_{TB}}. \]

The equivalent resistance \( r_{FS} \) and inductance \( l_{FS} \) are calculated using the simulated full-scale MMC parameters given in Table 1, while \( r_{TB} \) and \( l_{TB} \) are based on the MMC TB parameters given in Table 4 as described in [32].

Table 4. MMC Test Bench parameters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Variable</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nominal output power</td>
<td>( P_{n,MMC} )</td>
<td>6 kW</td>
</tr>
<tr>
<td>Nominal DC voltage</td>
<td>( U_{DC,n} )</td>
<td>400 V</td>
</tr>
<tr>
<td>Nominal DC current</td>
<td>( I_{DC,n} )</td>
<td>15 A</td>
</tr>
<tr>
<td>Nominal frequency</td>
<td>( f_n )</td>
<td>50 Hz</td>
</tr>
<tr>
<td>Nominal AC primary voltage (3-phase)</td>
<td>( U_{AC,1} )</td>
<td>400 V (Line-to-line RMS)</td>
</tr>
<tr>
<td>Nominal AC secondary voltage (3-phase)</td>
<td>( U_{AC,2} )</td>
<td>208 V (Line-to-line RMS)</td>
</tr>
<tr>
<td>Nominal AC RMS current at ( f_n )</td>
<td>( I_{AC,n} )</td>
<td>16.7 A</td>
</tr>
<tr>
<td>MOSFET switching frequency</td>
<td>( f_{sw} )</td>
<td>0-10 kHz</td>
</tr>
<tr>
<td>Number of cells (submodules)</td>
<td>( n_{SM} )</td>
<td>10</td>
</tr>
<tr>
<td>Nominal cell voltage</td>
<td>( U_{cell,n} )</td>
<td>40 V</td>
</tr>
<tr>
<td>Cell capacitor</td>
<td>( C_{SM} )</td>
<td>4.92 mF</td>
</tr>
<tr>
<td>Arm inductor</td>
<td>( L_{Arm} )</td>
<td>2.5 mH</td>
</tr>
<tr>
<td>Transformer rated power</td>
<td>( S_{Tr} )</td>
<td>8 kVA</td>
</tr>
<tr>
<td>Transformer vector group</td>
<td></td>
<td>( Y / \Delta ) (Ynd11)</td>
</tr>
</tbody>
</table>

3.1. Spectrum Analysis

The impedance derivation method introduced in section 2.2 is applied to measure the impedance of the MMC TB converters. A preceding analysis investigates the spectrum of the MMCs signals to determine with what frequencies the MMC TB responds to a perturbation. When operating in grid-following control mode, the MMC is perturbed by a voltage source, causing the converter to respond with a current. Applying a voltage perturbation at 40 Hz, 70 Hz, 80 Hz and 90 Hz, the corresponding current spectrum is analyzed. Figure 11 shows the effect of the perturbations on the current spectrum. As expected, the converter also responds with a current at 40 Hz, 70 Hz, 80 Hz and 90 Hz. However, for positive-sequence perturbations, the spectrum depicted in Figure 11 (a) contains also current responses at 60 Hz and 140 Hz for a 40 Hz perturbation, at 30 Hz and 170 Hz for a 70 Hz perturbation, at 20 Hz and 180 Hz for a 80 Hz perturbation, and at 10 Hz and 190 Hz for a 90 Hz perturbation. In fact, for a 40 Hz perturbation, the response at 60 Hz exceeds that at 40 Hz, indicating a high degree of coupling in that frequency region. The results indicate a pattern in the current responses. When being subjected to a voltage perturbation with \( f = f_{pert} \), the MMC responds with a current with \( f = 100 \text{ Hz} - 2f_{pert} \) and \( f = 100 \text{ Hz} + 2f_{pert} \) in addition to a current at \( f = f_{pert} \).
These currents are referred to as (mirror) frequency coupling [27,37,42] and are subsequently defined as a negative and positive coupling current dependent on the perturbation frequency with

\[ f_{\text{pert}}^{-} = 2f_{G} - f_{\text{pert}} \] \hspace{1cm} (9)

and

\[ f_{\text{pert}}^{+} = 2f_{G} + f_{\text{pert}}. \] \hspace{1cm} (10)

They can be interpreted as couplings between the positive and negative sequences or cross-couplings of the non-diagonal elements in a dq-domain impedance matrix [26,30]. They are seen in VSCs including MMCs and can be caused by the grid frequency used in the dq-transformation of the converters’ control systems. Also, controllers that control the d- and q-axis current differently can be responsible for the coupling frequencies [42]. Furthermore, the effect was also seen in STATCOM measurements in the China Southern Grid [4]. The Phase-Locked loop (PLL) was considered responsible for transforming a component at the frequency \( f \) into two simultaneous components in the stationary frame, one at \( f_{G} - f \) and the other at \( f_{G} + f \) [4]. However, different parts of the control system, such as the Pulse-Width Modulation (PWM) can also produce the coupling currents [43].

The spectrum depicted in Figure 11 (b), shows that no significant current magnitudes at frequencies other than the perturbation frequency can be seen for a negative-sequence perturbation.
Figure 12. MMC Test Bench current response to a voltage perturbation with frequency $f_{\text{pert}}$.

Figure 12 shows the perturbation response current $I(f_{\text{pert}})$ as well as the previously identified coupling currents $I(2f_G - f_{\text{pert}})$ and $I(2f_G + f_{\text{pert}})$ when the MMC TB is subjected to a perturbation voltage source with frequencies ranging from 1 Hz to 10 kHz. This means that for instance, for a perturbation frequency with $f = 40$ Hz the current response at 40 Hz, at 60 Hz, and at 140 Hz can be seen in the Bode plot. The current trajectories reveal that the current’s magnitude at $f = f_{\text{pert}}^+$ is significantly smaller than at $f = f_{\text{pert}}^-$. Furthermore, the plot shows that the frequency coupling effect is only significant at frequencies close to the grid frequency. However, as already seen in the spectrum analysis, the current response at $f_{\text{pert}}^-$ exceeds that at the perturbation frequency between 30 Hz and 60 Hz. The response at the coupling frequencies converges to zero for higher frequencies, and the MMC responds with the current at $f_{\text{pert}}$ only.

When operating in grid-forming control mode, the converter is perturbed with a current source and responds with a voltage to the perturbation. In this case, the converter reacts only with voltages at $f_{\text{pert}}$ as it can be seen in the voltage spectrum in Figure A2 of the appendix.

To conclude, the coupling current is only significant for the given system when
- the MMC operates in grid-following control mode,
- the MMC is subjected to a positive-sequence perturbation,
- the perturbation frequency is below 200 Hz.

3.2. Coupling Modeling

As demonstrated in the previous section, the MMC responds to a positive-sequence voltage perturbation at $f_{\text{pert}}$ not only with a current at the same frequency but also with a current at $f = 2f_G - f_{\text{pert}}$ when operating in grid-following control mode. Figure 13 illustrates how the additional current introduces a dependency of the grid impedance on the measured current response at $f_{\text{pert}}$. 
The admittance $Y$pling current on the converter impedance can be subsequently included in the converter
frequency, through the parallel converter and grid and converter admittance so that it can be expressed by
\[ Y = \frac{i_c}{f} \] (11)

Figure 13 illustrates that the current $i_c$ at a same frequency and also with a second coupling current $i_c$ at frequency $f = f_{pert}$. Additionally, the converter also responds to the additional perturbation $u_c$ with a current $i_c$ at frequency $f = 2f_G - (2f_G - f_{pert})$.

As a result, the current response at $f = f_{pert}$ consists of the converter response to the voltage perturbation $U_{pert}(f_{pert})$, and that to the additional voltage perturbation $u_c(2f_G - f_{pert})$. The latter introduces a non-desirable dependency of the converter impedance on the grid impedance, which nullifies the advantage of the IbSC that both subsystems’ impedances can be independently derived. While the measurement setup can include the grid impedance, this approach would further increase the required number of measurement series. Every grid impedance would require a new measurement and therefore, this approach is not feasible. Thus, the converter impedance is measured in ideal conditions, not including the grid impedance. The impact of the additional coupling current on the converter impedance can be subsequently included in the converter impedance model by an additional parallel impedance [37].

The additional impedance $Z_{e,c}(f)$ depends on the grid impedance as well as the additional current $i_{e,c}$, and is added in parallel to the converter impedance $Z_{MMC}$. For simplification, it will be derived as the admittance $Y_{e,c}$ so that the overall converter admittance

\[ Y_{MMC}(f_{pert}) = \frac{I_{pert}(f_{pert}) + i_{e,c}(f_{pert})}{U_{pert}(f_{pert})} = \left( \frac{I_{pert}(f_{pert})}{U_{pert}(f_{pert})} \right) + \left( \frac{i_{e,c}(f_{pert})}{U_{pert}(f_{pert})} \right). \] (12)

The admittance $Y_{e,c}$ is derived on the basis of the model presented in [44] which maps the current $i_c(2f_G - f_{pert})$ to the perturbation voltage $U_{pert}(f_{pert})$ by defining a admittance

\[ Y_c(f_{pert}) = \frac{i_c(2f_G - f_{pert})}{U_{pert}(f_{pert})}. \] (13)

Figure 13 illustrates that the current $i_c(2f_G - f_{pert})$ leads to a voltage $u_c(2f_G - f_{pert})$ through the parallel converter and grid and converter admittance so that

\[ u_c(2f_G - f_{pert}) = \frac{i_c(2f_G - f_{pert})}{Y_{pert}(2f_G - f_{pert}) + Y_G(2f_G - f_{pert})}. \] (14)

The converter responds to this additional perturbation with the current $i_c$ at the same frequency and also with a second coupling current $i_{e,c}$ at frequency $f = f_{pert}$ as derived in (11). It can be expressed by

\[ i_{e,c}(f_{pert}) = Y_c(2f_G - f_{pert}) \cdot u_c(2f_G - f_{pert}). \] (15)

Replacing $i_{e,c}(f_{pert})$ in the right summand of (12) by (15) gives
Phase Angle [deg]
Preprints
-180
-135
-90
-45
0
45
90
135
180
Magnitude [dB+]
Positive Sequence
Zc,c= 0
Low ZG
High ZG
101 102
Frequency [Hz]
-180
-135
-90
-45
0
45
90
135
180

\[ Y_{c,c} = \frac{Y_c(2f_G - f_{pert}) \cdot u_c(2f_G - f_{pert})}{U_{pert}(f_{pert})}. \]  \tag{16}

Now \( u_c(2f_G - f_{pert}) \) in (16) can be represented by (14) so that

\[ Y_{c,c} = \frac{Y_c(2f_G - f_{pert})}{U_{pert}(f_{pert})} \cdot \frac{i_c(2f_G - f_{pert})}{Y_{pert}(f_{pert}) + Y_G(2f_G - f_{pert})}. \]  \tag{17}

Then \( Y_c \) as in (13) can be used to replace \( \frac{i_c(2f_G - f_{pert})}{U_{pert}(f_{pert})} \) in (17) which results in

\[ Y_{c,c}(f_{pert}) = \frac{Y_c(2f_G - f_{pert}) \cdot Y_c(f_{pert})}{Y_{pert}(2f_G - f_{pert}) + Y_G(2f_G - f_{pert})}, \]  \tag{18}

as in [44]. The resulting admittance considers the influence of the grid impedance by integrating the current \( i_c(f_{pert}) \) into the overall impedance model \( Z_{MMC}(f_{pert}) \). Including the admittance \( Y_{c,c}(f_{pert}) \) into the overall impedance model requires to record also the signals \( i_c(2f_G - f_{pert}) \) and \( U_{pert}(f_{pert}) \) as shown in (13) and (18). Consequently, the impedance measurement method in [31] is extended to also record the voltage \( U_{pert} \) at \( f_{pert} \) and the coupling current \( i_c \) at \( 2f_G - f_{pert} \) which can be seen in Figure 12. Equation (18) also shows that the converter admittance \( Y_c \) and the grid admittance \( Y_G \) need to be obtained also for the coupling frequency \( 2f_G - f_{pert} \) for deriving \( Y_{c,c}(f_{pert}) \). Hence, the derived admittances are additionally shifted so that the corresponding values at \( 2f_G - f_{pert} \) can be added to the model.

Figure 14 shows the impact of including the coupling current in the overall MMC impedance model. A low SCR (SCR = 2) and consequently high grid impedance \( Z_G \) significantly influences the MMC impedance trajectory at frequencies below 50 Hz. A higher SCR (SCR = 6) shows a significantly reduced impact with the overall impedance almost matching the impedance when no coupling is modeled and \( Z_{c,c} = 0 \). Figure 14 also demonstrates that the coupling current does not affect the overall impedance at higher frequencies. Therefore, the coupling current is neglected in the impedance modeling for frequencies higher than 200 Hz.

**Figure 14.** MMC TB impedance with no coupling modeled (\( Z_{c,c} = 0 \)), high SCR (low \( Z_G \)) and low SCR (high \( Z_G \)).
4. WT VSC controller Replica System

The VSC of the wind turbine determines the frequency behavior of the offshore wind farm. The related impedance models are derived in the DNV GL Smart Grid Lab in Arnhem, The Netherlands. The goals of the laboratory are [45,46]:

- Propose a Power Hardware in the Loop (PHiL) test circuit to derive the impedance model of the power converter unit of a vendor-specific wind turbine (i.e., the power converter unit of a commercial 1-MW wind turbine generator). Further details for the PHiL TB can be found in [45].
- Establish a CHiL TB to derive the impedance model a VSC WT controller replica that can be used for the grid integration of offshore wind power plants.
- Compare the PHiL impedance of the VSC with its equivalent CHiL and provide suggested practices for potential industrial applications.

For this work, the CHiL impedance models the frequency behavior of the wind turbine VSC. The CHiL TB depicted in Figure 15 is configured with the following key components:

1. The OPAL-RT real-time simulator consisting of OP5700.
2. A 1 MW WT VSC controller replica from MingYang Wind Power.

![Figure 15. CHiL TB setup for the WT VSC controller replica impedance measurement.](image)

The real-time simulator OPAL-RT OP5700 is the core of the system. It simulates a single wind turbine, including a wind turbine’s electrical subsystem, the generator, filters, transformer, the offshore AC-grid, and breakers. The simulations are FPGA-based. The MingYang Wind Power WT VSC controller replica connects to the OP5700 system through digital and analog channels [45,46]. The real-time simulator measures the grid side current and voltage signals $I_{g,abc}$ and $V_{g,abc}$, and the generator side current and voltage signals $I_{gen,abc}$ and $V_{gen,abc}$. The analog output interface exports the signals. The OP5700 communicates with the WT VSC controller replica through 10 V analog signals. The controller replica then measures the terminal voltage and current coming from the controller replica. Using its time-stamped digital input interface, the OP5700 can interface with the controller replica’s measured signals. The resulting dq-impedance models used for the stability analysis are transformed into the sequence domain [47] and adjusted for outliers [41].
5. Stability Analysis

Using the scaled MMC TB and the WT VSC controller impedances, the converter-driven stability of a wind farm connected to the AC onshore grid by an HVDC link is assessed. Figure 16 depicts the investigated system.

![HVDC system connecting offshore windfarm to AC system.](image)

The AC onshore grid is connected to an MMC operating in grid-following control mode and controlling the DC voltage. At the same time, the offshore wind farm is synchronized with an MMC operating in grid-forming control mode and providing the AC voltage magnitude and frequency. Hence, two test cases are defined to assess the stability of the system. The onshore test case investigates interactions between the AC onshore grid and the grid-following MMC and the offshore test case investigates interactions between the grid-forming MMC and the offshore wind farm. 600 MW are transmitted from the offshore wind farm to the shore, meaning that the impedance models are derived for 0.5 pu active power setpoint.

5.1. Onshore Test Case

Similar to the validation test case, different SCRs are defined to investigate AC onshore grids with varying grid strengths. Investigating the positive-sequence impedance ratio first, Figure 17 depicts the positive-sequence Nyquist plots of the impedance ratio $Z_G(f)/Z_{MMC}(f)$ with Figure 17 (b) showing a close-up around the $(-1, j0)$ point.

![Nyquist plots of MMC in grid-following control mode and AC grid for different SCRs with positive-sequence perturbation.](image)

The Nyquist plots show that for an SCR = 3.5, the $(-1, j0)$ point is encircled, indicating an unstable system. The Bode plots in Figure 18 further reveal that the phase difference of the AC grid and MMC impedances reaches 180° for SCR = 3.5 and below.
Figure 18. Bode plots of MMC in grid-following control mode and AC grid for different SCRs with positive-sequence perturbation.

Figure 19 depicts the Nyquist plots of the negative-sequence impedance ratio. They show that for the negative-sequence impedance ratio, the \((-1, j0)\) point is not encircled for the examined AC grid impedances. The Bode plots in Figure 20 show that even for an SCR = 3, the phase difference does not exceed 180°.

Figure 19. Nyquist plots of MMC in grid-following control mode and AC grid with negative-sequence perturbation.
To determine the onshore system’s overall stability and its proximity to instability, Table 5 presents the minimum PMs of the positive- and negative-sequence systems, showing a negative and zero PM for the positive-sequence systems with $\text{SCR} = 3$ and $3.5$. Thus, the frequency-domain stability assessment demonstrates that already for a moderate $\text{SCR}$, the converter-driven stability is threatened due to unwanted interactions between the onshore MMC and the adjacent AC system.

Table 5. Phase Margins of MMC in grid-following control mode and AC grid for different SCRs.

<table>
<thead>
<tr>
<th>SCR</th>
<th>$f_{\text{pos}}$ [Hz]</th>
<th>$PM_{\text{pos}}$ [deg]</th>
<th>$f_{\text{neg}}$ [Hz]</th>
<th>$PM_{\text{neg}}$ [deg]</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>95</td>
<td>-8</td>
<td>169</td>
<td>7</td>
</tr>
<tr>
<td>3.5</td>
<td>105</td>
<td>0</td>
<td>179</td>
<td>15</td>
</tr>
<tr>
<td>4</td>
<td>114</td>
<td>8</td>
<td>190</td>
<td>22</td>
</tr>
<tr>
<td>4.5</td>
<td>121</td>
<td>14</td>
<td>199</td>
<td>28</td>
</tr>
<tr>
<td>5</td>
<td>129</td>
<td>20</td>
<td>209</td>
<td>34</td>
</tr>
<tr>
<td>5.5</td>
<td>137</td>
<td>25</td>
<td>220</td>
<td>40</td>
</tr>
</tbody>
</table>

5.2. Offshore Test Case

The offshore test case investigates interactions between a grid-forming MMC and wind farm consisting of 600 wind turbines with 1 MW nominal power each. The WT are arranged in a radial grid layout illustrated in Figure 21.
Figure 21. Offshore wind farm grid layout.

Consisting of \( m \) radial lines and \( n \) wind turbines in each line, the grid layout can be varied to investigate the topology’s impact on the stability. Hence, the overall wind farm impedance \( Z_{WF}(f) \) is aggregated dependent on \( n \) and \( m \) so that

\[
Z_{WF}(t) = \frac{n}{m} Z_{WT}(f),
\]

with \( n \cdot m = 600 \) to ensure a power flow of 600 MW. As a result, the equivalent circuit diagram depicted in Figure 22 represents the offshore test case. Contrary to the validation and the onshore test case, not the MMC but the WT converters control the grid current. Therefore, a current source with parallel impedance represents the offshore wind farm. Operating in grid-forming control mode, the MMC provides the AC voltage and is therefore represented by a voltage source with series impedance.

Figure 22. Equivalent circuit diagram of offshore test case.

Deriving the equivalent loop gain accordingly, the impedance ratio \( \frac{Z_{MMC}(f)}{Z_{WF}(f)} \) is assessed for wind farm grid layouts with \( n \cdot m = 600 \) and \( n, m \in \mathbb{N} \). The Nyquist plots in Figure 23 show the grid layouts that are closest to the \((-1, j0)\) point with 600 WT in one line \((600, 1)\), 300 WT in two lines \((300, 2)\), 200 WT in three lines \((200, 1)\) and 150 WT in four lines \((150, 4)\). The Nyquist plots reveal that, although being close to the \((-1, j0)\) point, the different grid layouts do not result in an unstable system as the \((-1, j0)\) point is not encircled for positive- and negative-sequence impedance ratios. For further analysis and to determine the PMs, Figure 24 shows the Bode plots of the grid-forming MMC and the wind farm impedances.
The plots demonstrate that the wind farm impedance magnitude starts to intersect that of the MMC for grid layouts with 200 and more WTs in each line. The corresponding PMs are given in Table 6. The results show that the magnitude intersections are shifted to higher frequencies the more WTs are placed in a single line. This results in a higher phase difference since for frequencies higher than 400 Hz, the MMC phase angle increases, and those of the wind farms decrease. For the extreme case of 600 WT in one line, the PM is
as low as 16° and 14° for the positive- and negative-sequence impedances, indicating a system close to instability.

Table 6. Phase margins according to different grid layouts for positive- and negative-sequence impedances.

<table>
<thead>
<tr>
<th>n</th>
<th>f_pos [Hz]</th>
<th>PM_pos [deg]</th>
<th>f_neg [Hz]</th>
<th>PM_neg [deg]</th>
</tr>
</thead>
<tbody>
<tr>
<td>200</td>
<td>457</td>
<td>98</td>
<td>508</td>
<td>96</td>
</tr>
<tr>
<td>300</td>
<td>535</td>
<td>91</td>
<td>555</td>
<td>74</td>
</tr>
<tr>
<td>600</td>
<td>1086</td>
<td>16</td>
<td>1076</td>
<td>14</td>
</tr>
</tbody>
</table>

The offshore test case demonstrates that the wind farm grid layout is decisive for the stability of the offshore system. Besides, the graphical analysis reveals that small changes of the VSC and MMC impedance trajectory can cause the system to become unstable. For instance, changes in the converters’ control system can modify their impedances, shifting the intersection frequencies further to the right, leading to negative PMs. The offshore system’s stability analysis also demonstrates that the IbSC and measurement-based impedance models are suitable for industrial applications, allowing that the models be derived independently and exchanged without sharing crucial information about the controllers.

6. Conclusion

In this paper, enhanced frequency-dependent impedance models are successfully derived for laboratory MMCS. Together with the previous work on the impedance model of a WT VSC controller replica [46], the developed impedance models were used to investigate the converter-driven stability of an MMC HVDC connected offshore wind park using the IbSC. The results indicate that couplings between frequencies and their impact are highly dependent on the converters’ control system. Thus, preliminary spectrum analyses are recommended for the impedance derivation. However, the implications and significance of couplings for stability assessments in industrial applications still merits investigation. The work demonstrates that no confidential knowledge of the components needs to be shared among owners of different subsystems, e.g., wind turbines and MMCS, for assessing the system’s stability. Due to significantly reduced computation times compared to EMT time-domain simulations, the converter-driven stability of multiple scenarios can be investigated effectively. The onshore system results demonstrate that an MMC synchronized through a PLL with the AC onshore grid can experience converter-driven stability issues already at a moderate SCRs. Investigating various offshore grid layouts reveals that the grid topology has a substantial impact on the offshore system’s converter-driven stability; varying the grid layouts results in significantly different impedance models of the whole wind farm. Although not representing a realistic grid layout, the test case still demonstrates that the associated risk cannot be neglected, and impedance aggregation algorithms need to be appropriately considered [48], so that potential unstable scenarios are not overlooked.

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Abbreviations
The following abbreviations are used in this manuscript:

AC  Alternating Current
CHiL  Control Hardware in the Loop
DC  Direct Current
DUT  Device Under Test
EMT  Electromagnetic Transient
HVDC  High-Voltage Direct Current
FPGA  Field Programmable Gate Array
IbSC  Impedance-based Stability Criterion
MMC  Modular Multilevel Converter
PHiL  Power Hardware in the Loop
PLL  Phase-Locked loop
PM  Phase Margin
PWM  Pulse-Width Modulation
SCR  Short-Circuit Ratio
STATCOM  Static Synchronous Compensator
SM  Submodule
TSO  Transmission System Operator
TB  Test Bench
VSC  Voltage Source Converter
WT  Wind Turbine

Appendix A

Figure A1. Nyquist plots of AC grid and MMC impedance ratio of validation test case.
Figure A2. MMC TB digital twin voltage response spectrum with (a) positive-sequence and (b) negative-sequence current perturbation.

References


