

Article

Deep Learning for Wave Energy Converter Modeling Using Long Short Term Memory

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Abstract: Accurate forecasts of ocean waves energy can not only reduce costs for investment but it is also essential for management and operation of electrical power. This paper presents an innovative approach based on the Long Short Term Memory (LSTM) to predict the power generation of an economical wave energy converter named "Searaser". The data for analyzing is provided by collecting the experimental data from another study and the exerted data from numerical simulation of Searaser. The simulation is done with Flow-3D software which has high capability in analyzing the fluid solid interactions. The lack of relation between wind speed and output power in previous studies needs to be investigated in this field. Therefore, in this study the wind speed and output power are related with a LSTM method. Moreover, it can be inferred that the LSTM Network is able to predict power in terms of height more accurately and faster than the numerical solution in a field of predicting. The network output figures show a great agreement and the root mean square is 0.49 in the mean value related to the accuracy of LSTM method. Furthermore, the mathematical relation between the generated power and wave height was introduced by curve fitting of the power function to the result of LSTM method.

Keywords: Searaser; Flow-3D; Prediction; Long short term memory; deep neural network; Root mean error.

1. Introduction

Based on the available data, fossil fuels are still the most important source of energy in the world [1]. As known fossil fuels harm the environment by global warming and climate change [2]. Therefore, in recent years, the interest in investment on systems that use fossil fuel investment has declined. On the other hand, interest in developing non-petroleum-based sources of fuel, especially on the renewable source of energy, has increased tremendously. Among the different sources of renewable energy, solar energy, wind power, tidal energy and geothermal energy are the most well-known ones [3]. Ocean wave energy has the second largest potential among all ocean renewable energy sources [4].

Absorbing the wave energy and transforming it into electricity implies wave energy converters (WECs) that use the motion of ocean surface waves to convert ocean wave energy into electricity. In general, there are different types of WEC systems [5,6]. Due to the important role of WECs in producing electricity from ocean waves, the precise forecast can not only reduce costs for investment but also be essential for management and operation of electrical power. Due to this fact, investors around the world need to know information about predicting the potential for power generation by WEC systems [7]. In these

fields, especially utilizing the output power from WEC systems several studies were done through numerical simulations and experiments [8,9]. In this study, a new wave energy converter named "Searaser" was chosen because of the lower price than similar types in the market and as it is considered as clean electricity producer with no climate gas emissions involved [10].

Even though ocean waves are quite clean, safe, reliable and affordable a source of energy, they have unpredictable uncertainties with their usage. The unwanted uncertainty can threat the reliability and stability of the ocean energy systems, especially with the large-scale integration ones [11,12]. Hence, it is essential to properly forecast ocean wave energy to save construction costs and pilot projects during the electrical power generation. As known, the power density of wave energy is not only more abundant in the natures than wind and solar energy but also easier to forecast [13,14]. In fact, accurately predicting the power of ocean waves due to random data is still a challenging task in engineering. Because of the time-consuming and expensive calculations of solving equations with complex boundary conditions, researchers are looking for a way to replace numerical solutions. One of the areas that can make predictions in this area with minimal time and cost is the use of artificial intelligence in the field of estimating the production capacity of energy systems. Therefore, the artificial intelligence (AI) researchers in the field of engineering have been developing the methods to predict the generated electrical power of ocean waves energy systems from effective parameters [15,16]. Zhenqing et al. [17] studied and simulated ocean waves and suggest a prediction model by using machine learning methods and genetic algorithm. The main goal of this study is to demonstrate converters by considering different wave periods, wave height and water depth. They concluded that optimizing the converters help to solve other technical problems in this field. Li et al. [18] conducted a study on the parameters affecting the wave power. They provided an artificial neural network to have an accurate prediction that creates relation between the height of the free surface of a wave and its force through a machine learning algorithm. They identified a relation between the power capture efficiency and other parameters by analyzing the errors. Gomez et al. [19] did a research about utilizing latest machine learning methods to introduce a new software tool with a user-friendly guide interface to predict output using the integration of meteorological data from two data sources. Butt et al. [20] presented a novel method of artificial intelligence to forecast systems. They predicted the load on the next 24 hours of simulation. By evaluating results by different kinds of error they concluded that these systems are so efficient in better maintenance operations. Cheng et al. [21] utilized LSTM method for predicting the power demand. By comparing three different AI methods, they concluded that the LSTM method decreases 21.80% and 28.57% in forecasting error. Lin et al. [22] studied the power prediction of systems by LSTM error and optimised results. They concluded that the output results of LSTM algorithm are more accurate than those of the other methods. Also, Ni et al. [23] utilized deep learning method to predict the power of wave energy converter. They experimentally concluded that the high frequency waves can effect directly on the efficiency of the modeling when they compare different kinds of deep learning methods. But among all these recent studies, the relationship between the wind speed which is significant in these kinds of simulations has been presented. Therefore, how to estimate the output power directly from wind speed and build an accurate model for optimizing its efficiency are two essential issues in the WEC improvements and output electrical power, which has not yet been clarified and evident. In order to address the gaps in the studies that have been done so far, this research has tried to predict the amount of power produced by Searaser using two methods of artificial intelligence and numerical solution at the same time. The novelties of the recent research are as following.

- The numerical analysis of a Searaser in the form of the computational fluid dynamics is proposed by Flow-3D software, which completely demonstrates the ocean wave parameters and perfectly combines with the latest algorithm of long short-term memory.

- The artificial intelligence model is reasonably utilized to predict output electrical power based on a wind flow speed and a mathematical relation between wave height and output power, can be obtained to help the WEC industry and investors to predict output power saving time and cost.

2. Materials and Methods

2.1 Dataset

To use supervised learning in the field of machine learning, it is necessary to give data to the algorithm. The input data to the utilized algorithm of this research includes two categories of data obtained from numerical solution of equations by Flow-3D simulation software and experimental data that He [24] used in his studies. For details, by using computational fluid dynamic and numerically solving the governing equations, a relationship between wave height and output power was found and the experimental data of He's study [24] demonstrates the relation between wind flow speed and wave height which is shown as Figure1. By collecting this data, we can reach the main goal of this research, which is to find a relationship between wind speed and output power.

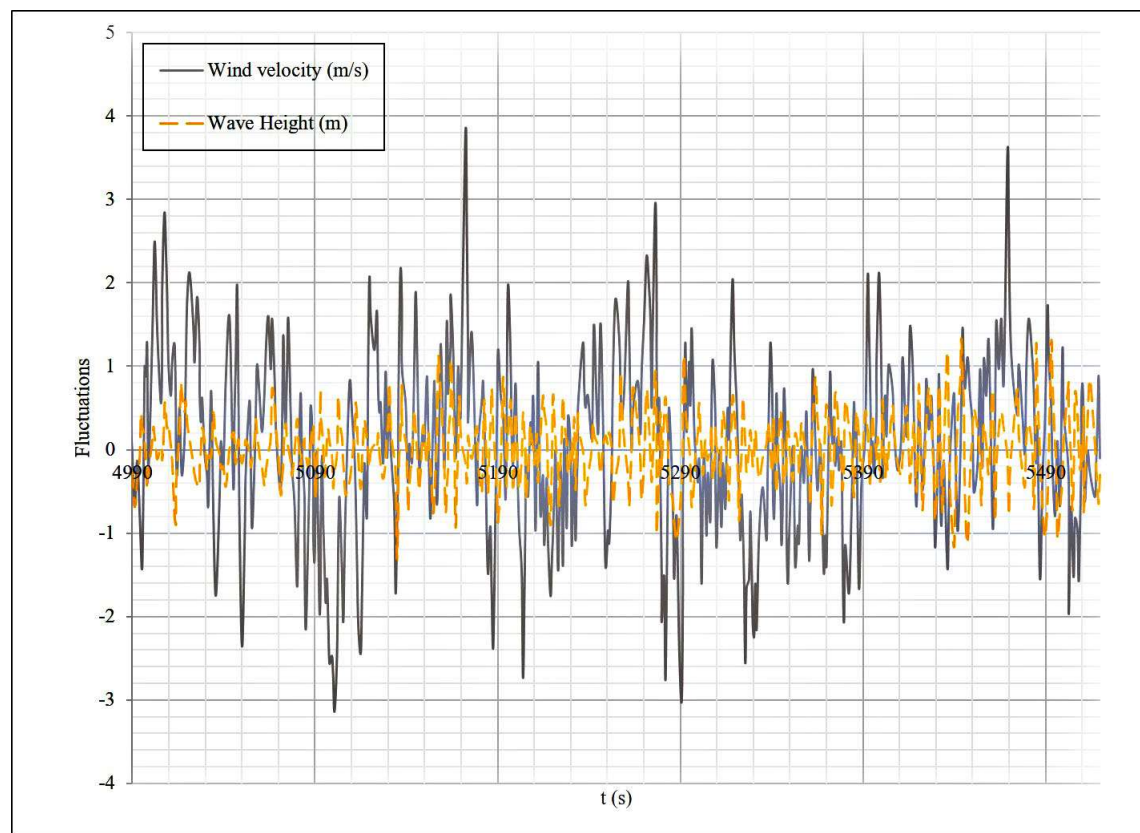


Figure 1. The wind speed and wave height fluctuation in simulation time.

As shown in Figure 1, the wind velocity and wave height are variable with the time and it causes uncertain and various output power which was demonstrated as a result of simulation part.

2.2 Geometry and description

Electricity generation industry in the field of wave energy converter has been improving and Alvin Smith registered a novel technology named as "Searaser" [25]. Searaser harnesses the motion of ocean waves by pumping pressurized water up into high reservoirs and then back down into hydro-power turbines to create electricity on demand. In

this study the performance of a Searaser with geometric dimensions based on the data extracted from the patent was numerically evaluated [25]. The geometry of Searaser is presented in Figure 2. In Figure 2, the three-dimensional structure of the Searaser is designed by a software and presents as a two-dimensional sketch for presenting more information. As shown, part 1 is a buoy which floats on the ocean's water and it forced upward of the related buoyancy force. For moving downward, the gravity force dominates other forces during passing wave motions by considering the effect of wall friction on a Searaser body. The buoy moves in a chamber which indicates as part 2. Addition to these main parts, different components of Searaser was introduced.

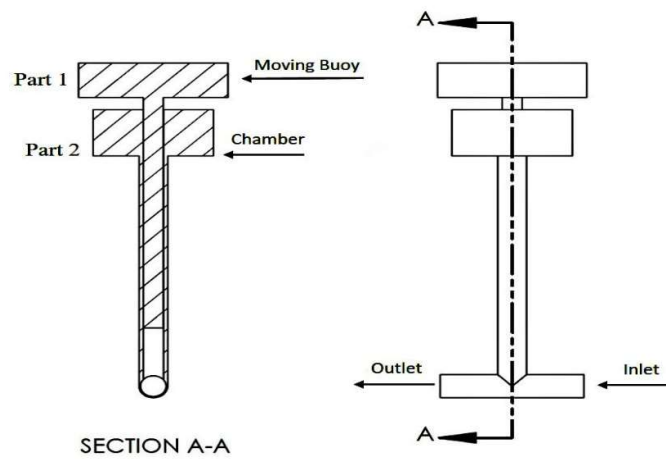


Figure2. The cross-section of a Searaser with introducing different components.

As presented in Figure 2, the inlet and outlet components are designed for the water flow to enter and exit during the buoy movements as the known piston-cylinder mechanism.

2.3 Governing equations

Flow 3D is utilized as a considering numerical solution software to analyze the solid-fluid interactions between Searaser structure and ocean waves. This study used volume fraction technique which is introduced as a ratio of the open to the whole volume within a computation cell. The named technique used for such a complicated structure to utilized the governing equations which are dedicated as Equation 1 and 2[26].

$$\vec{F} = m \frac{d\vec{V}_G}{dt} \quad (1)$$

$$\vec{T}_G = [\vec{J}] \cdot \frac{d\vec{\omega}}{dt} + \vec{\omega} \cdot ([\vec{J}] \vec{\omega}) \quad (2)$$

Where m is the Buoy mass, and V_G is the velocity of center of mass. Simplification of Equation 1 was done by assuming the fact that the buoy movement is divided into two main parts; rotational and translational one caused by 6 degree of freedom. Hence, by assuming the buoy as a rigid body, all of the movement takes place in the center of mass. In this study, the "o" index introduced the buoy center of mass. Equation 3 shows the buoy movement velocity [27].

$$\vec{V}_o = \vec{V}_{T_r} + \vec{V}_{r_o} \quad (3)$$

By utilizing the \vec{V}_o as a buoy velocity, the Equation 1 should be presented as Equation 4 [29].

$$\vec{F} = m \frac{d\vec{V}_o}{dt} \quad (4)$$

The total applied force to the Searaser was calculated as the summation of gravity and hydrodynamic forces (Equation 5). Similar to this, the torques with the same indexing were applied to the “o” point respectively (Equation 6). So the fluid governing equations can be written as Equation 7 and 8 [28].

$$\vec{F} = \vec{F}_g + \vec{F}_h \quad (5)$$

$$\vec{T}_o = \vec{T}_g + \vec{T}_h \quad (6)$$

$$\frac{v_f}{\rho} \frac{\partial \rho}{\partial t} + \frac{1}{\rho} \nabla(\rho \vec{u} A) = -\frac{\partial v_f}{\partial t} \quad (7)$$

$$\frac{\partial \vec{u}}{\partial t} + \frac{1}{v_f} (\vec{u} A_f \cdot \nabla \vec{u}) = -\frac{1}{\rho} [\nabla p + \nabla \cdot (\tau A_f)] + \vec{G} \quad (8)$$

Where ρ is the density, A_f is the area fraction, V_f is the volume fraction, \vec{u} is the velocity of the fluid, and G is gravity. For the coupling of the motion Equation 7 and 8 should be solved in each time step and the situation that is done by FAVOR technique in Flow-3D.

Hence, for different wave heights which were modified, Equation 9 was used as a power-height relation [29].

$$P = \frac{1}{64\pi} \rho g^2 H_s^2 T \quad (9)$$

To solve these equations, the specific boundary conditions and simplified assumptions should be applied. It should be noted that the numerical solution model in this problem is the finite difference method and Range-Kutta 3rd order method has been used to solve the category of partial derivative equations.

2.4 Boundary conditions and grid generation

To simplify the procedure, the sine waves with a different magnitude in wave characteristics were used. Equation 10 shows the sine wave equation [30].

$$W = A \sin(\omega t + \phi) \quad (10)$$

In this equation, A shows the wave amplitude which is gained from He's study [23]. The other wave characteristics were assumed constant. In addition to consider sine wave as an inlet of the specific control volume, other boundary conditions are shown in Figure 3.

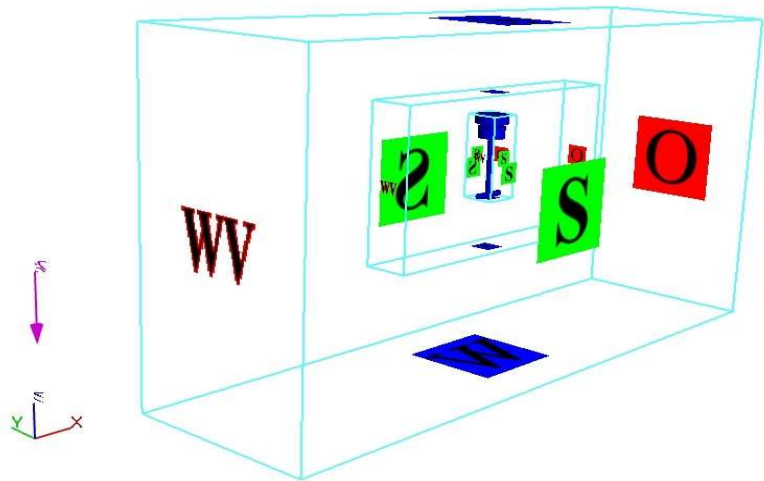
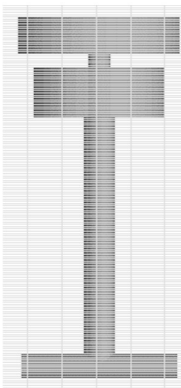
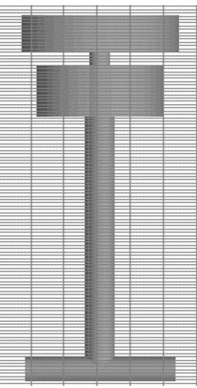
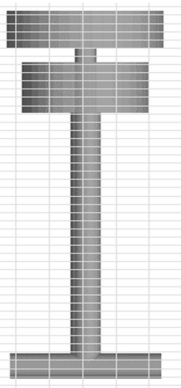


Figure 3. Different boundary conditions of numerical solution.

As shown in Figure 3 “VW” is a linear wave inlet of the control volume, “S” is the symmetric condition for three different wall, “W” is a wall with slip boundary condition and “O” is the outflow when the water is not allowed to enter the outflow boundary. The reason of using three different domains for numerical solution is to use different grid sizes. Whatever goes inside the blocks, the grid size becomes smaller because the computational accuracy is more essential than outer blocks in this region. So the inner block has the smallest grid size among the others. Similar to the other computational fluid dynamic studies, the grid generation and independencies should be analyzed to find the suitable grid size which has the best accuracy due to the least computational time which is shown as in Table1.

Table 1. The Grid generation information.

Title	1	2	3
Mesh Block (Number 1)			
Total number of elments	7,000,000	5,000,000	1,000,000
Run time	5 days 7 hr	4 days 1 hr	2 days 20 hr
The accuracy of Searaser displacement parameter	95%	93%	85%

As presented in Table1 the best selected total grid is 5,000,000 grids due to the related accuracy. It shows that this grid size can be selected because it is as accurate as 7,000,000 grids due to the fact that it has higher computing speed and lower computational cost. Furthermore, it presents the accuracy in displacement for each grid size during the whole of calculation time when the input wave height is assumed 1m [31]. According to the harmonic linear motion of buoy in a chamber, the special generator will convert these motions to electricity by utilizing the Faraday's law of induction.

2.5 Machine learning LSTM method of prediction

The electrical power of ocean waves forecasting models has become stable and highly credible after decades of considerable improvements. However, the models require large amount of data to train, which usually takes longer time even for a small-scale forecast. For that reason, the machine learning and deep learning algorithms were emerged and bloomed to improve accuracy and promptness of the prediction. Recurrent Neural Network (RNN) are types of Neural Networks designed to use sequential data such as time-series. In RNNs, the outputs can be fed back into the network as inputs creating a recurrent structure. RNNs are trained by backpropagation. During backpropagation, RNNs suffer from gradient vanishing problem. The gradient is the value used to update Neural Networks' weight. The gradient vanishing problem is when gradient shrinks as it back propagates through time. Therefore, layers that get a small gradient do not learn and cause the network to have short-term memory [32].

Long Short-Term Memory (LSTM) is a specialized RNN to mitigate the gradient vanishing problem. LSTMs can learn long-term dependencies using a mechanism called gates. Figure 4 presents an architecture of LSTM cell. These gates can learn what information in the sequence is important to keep or throw away. LSTMs have three gates; input, forget and output [33].

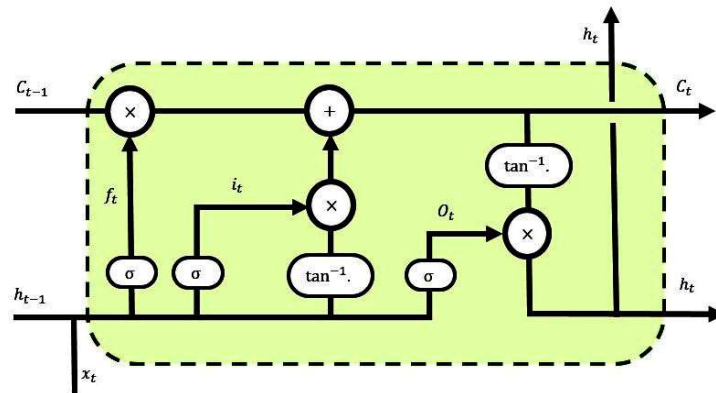


Figure 4. The architecture of LSTM cell.

To save the data information that is utilized in the specific storage within hidden layers, the "cell" has been introduced. As presented in Equations 11 and 12, f_t and i_t indicate the input gate and forget gate for controlling each cell state [34].

$$f_t = g(W_f \cdot [h_{t-1} X_t] + b_f) \quad (11)$$

$$i_t = g(W_i \cdot [h_{t-1} X_t] + b_i) \quad (12)$$

Where g indicates a non-linear sigmoid function for activation procedure. i and f indexes represent the input and forget parameters, W and b presents the weight matrix and

bias function, h_{t-1} introduces the output vector of the last time step and X_t shows the input vector of the current time step.

Equation 13 presents the relation to obtain an input's current state.

$$C'_t = \tanh(W_c \cdot [h_{t-1} \cdot X_t] + b_c) \quad (13)$$

As shown in Equation 13, c index introduces the recent state of each parameters. Eq. 14 describes the current cell, that i is considered to utilize both of the forget and input gates.

$$C_t = f_t * C_{t-1} + i_t * C'_t \quad (14)$$

By using the output gate of each cell as is written in Eq. 15, the output of the whole network of a long short-term memory has been presented as Eq. 16.

$$O_t = g(W_o \cdot [h_{t-1} \cdot X_t] + b_o) \quad (15)$$

o index introduces the cell output parameters.

$$h_t = O_t * \tanh(C_t) \quad (16)$$

The essential task in algorithm designing procedure of neural network is to select the best number of neurons and relative layers. In machine learning systems which contain neurons, the connection links between them are introduced as weighted activation. According to proposed usage, it was modeled by input layer. To analyze procedure, hidden layers were used by considering several neurons which transferred data from input to output neuron. The network's dataset was split into training and testing sets. The main crucial task in optimization is to minimize a difference between predicted and actual data [35,36].

The LSTM model has been utilized with 10 LSTM layers of 10 neurons and "Sigmoid" as an activation function. The optimized train size is 90% of total 591 input data and the test size is 10%. Furthermore, the epoch size is 7 and walk-forward validation method were used. The back propagation algorithm was utilized for administrated learning technique [37]. Figure 6 shows the neural network details which is used in this research.

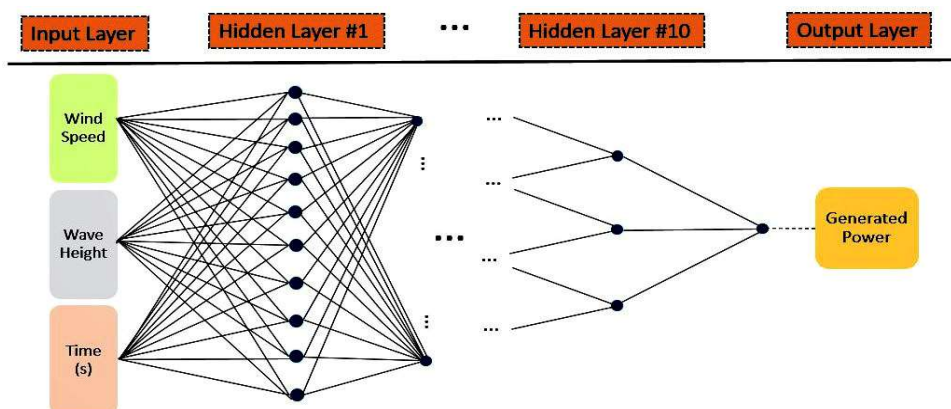


Figure 5. The specific neural network of recent study.

As presented in Figure 5, the recent study utilized a proposed LSTM Network with an input layer time-series parameters which are followed by an LSTM layer. These layers learn the relation between different parameters in time steps and serialized input data. Moreover, during each of the layers, the LSTM layer's neuron is connected to the next

layer’s neuron for each LSTM cell. The artificial intelligence predictions have been done by utilizing equations of LSTM method. Hence, decreasing rank procedure of the input data was done by Mahalanobis distance (MD) method to reduce the predicting time of the overall procedure. Our study is a kind of regression prediction which can find a relation between the input and output data. Table 2 presents the LSTM parameters which were introduced as effective parameters on output generated power of Searaser.

Table 2. The detailed information of LSTM method.

LSTM parameters	Recent study parameters
C_{t-1}	Input parameters
	1.Wave Height
	2.Time
	3.Wind slow velocity
h_t	4.Number
	Output parameters
	1.Generated power

In this study, by using the numerical solutions, the collected dataset from simulation and experimental study was imported to the LSTM Network, and then it would predict the output parameters. Next, the data that was gained by numerical solution would be compared with the predicted data from LSTM method. Finally, the correlation matrix has been applied on a recognition step of the occurrence of faults.

3. Results and discussion

This section describes the results of evaluation of the wave power generation prediction based on the proposed LSTM Network. Accordingly, the result of numerical solutions and the prediction plots of correlation parameters were presented and compared with each other. Furthermore, the Searaser’s performance was demonstrated for various input linear-sine waves the information of which exists in Figure3. The wave height moves the buoy in z direction and its motion will be converted to the electricity. The Equation 9 demonstrates that the output power depends on the wave height and wave period of each time. Furthermore, the other parameters become constant during the simulation. Figure 6 shows the numerical solution of the simulation. It shows the relation of the generated power with the whole simulation time.

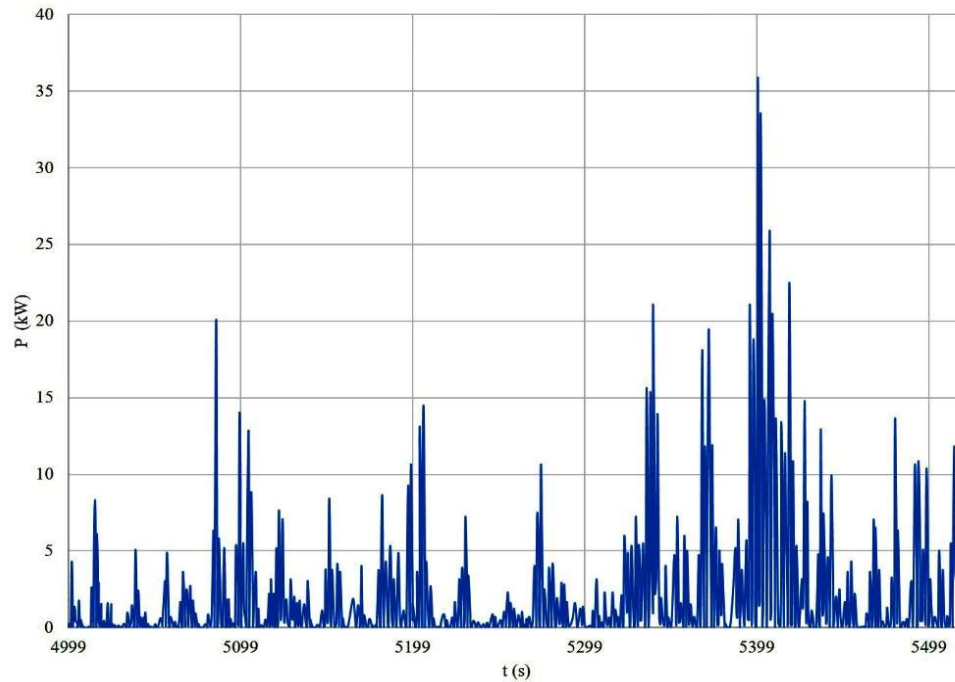


Figure 6. The variation of generated power with simulation time

The instability of the generating power at different times during the simulation is presented. This is caused by the variation of wave heights.

To illustrate the correlation between all of the effective variables with LSTM method further, the predicted plots were presented as a matrix of figures. The scatter plot of predicted magnitudes was shown in Figure7.

Figure 7 presents a matrix whose intersection of each row and column shows a graph showing the relationship between the two parameters. Using this type of display causes the dependence of all parameters on each other to be well shown.

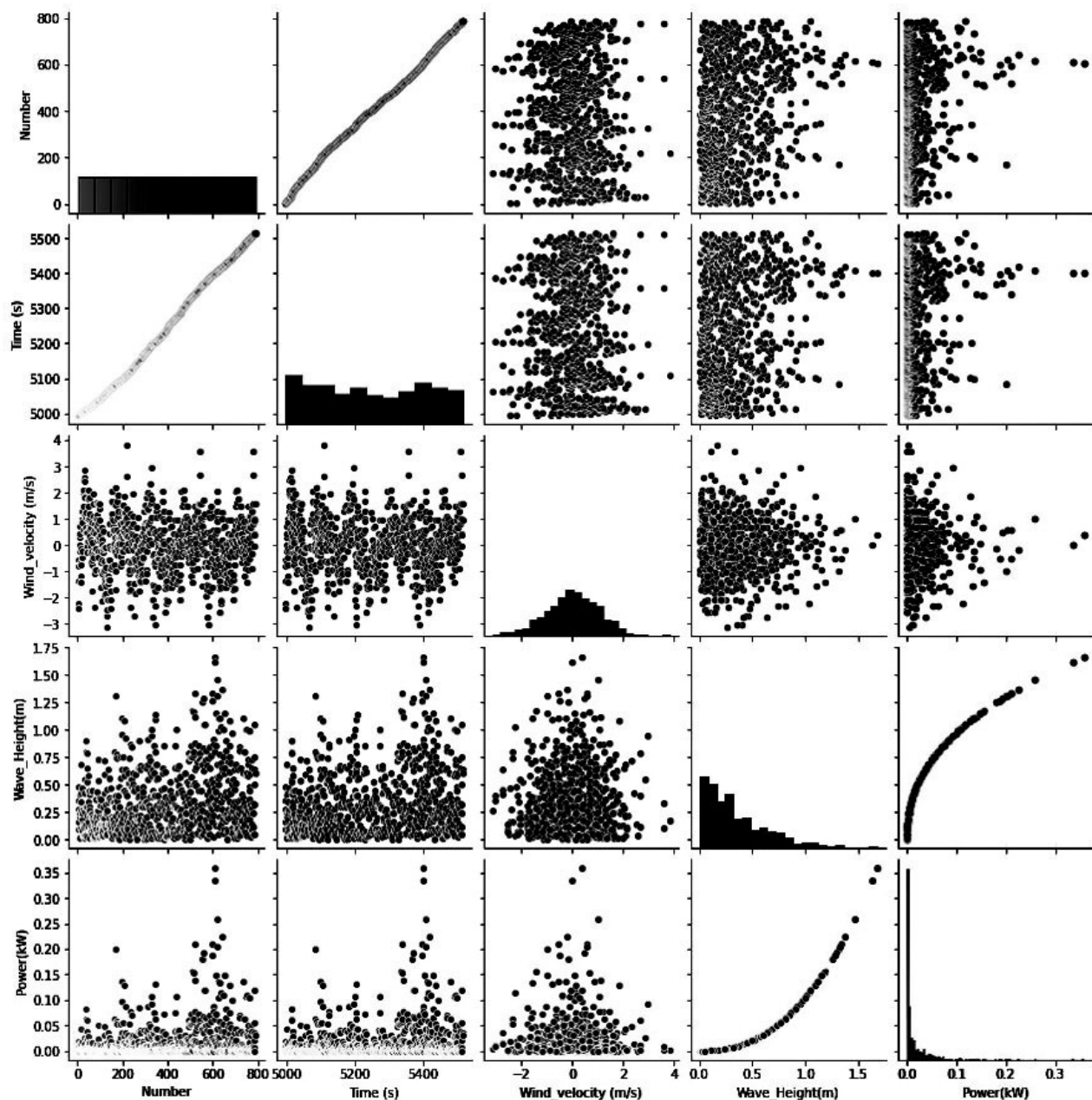


Figure 7. The correlation of different parameters with each other.

As presented in Figure 7, the correlation of different parameters is shown as scatter figures. Figure 8 is a more comprehensive type of Figure 7. As Figure 8 shows, the gradient descent for both parameters in each curve is calculated, which can be reached in Figure 7 by connecting the extreme points of each curve.

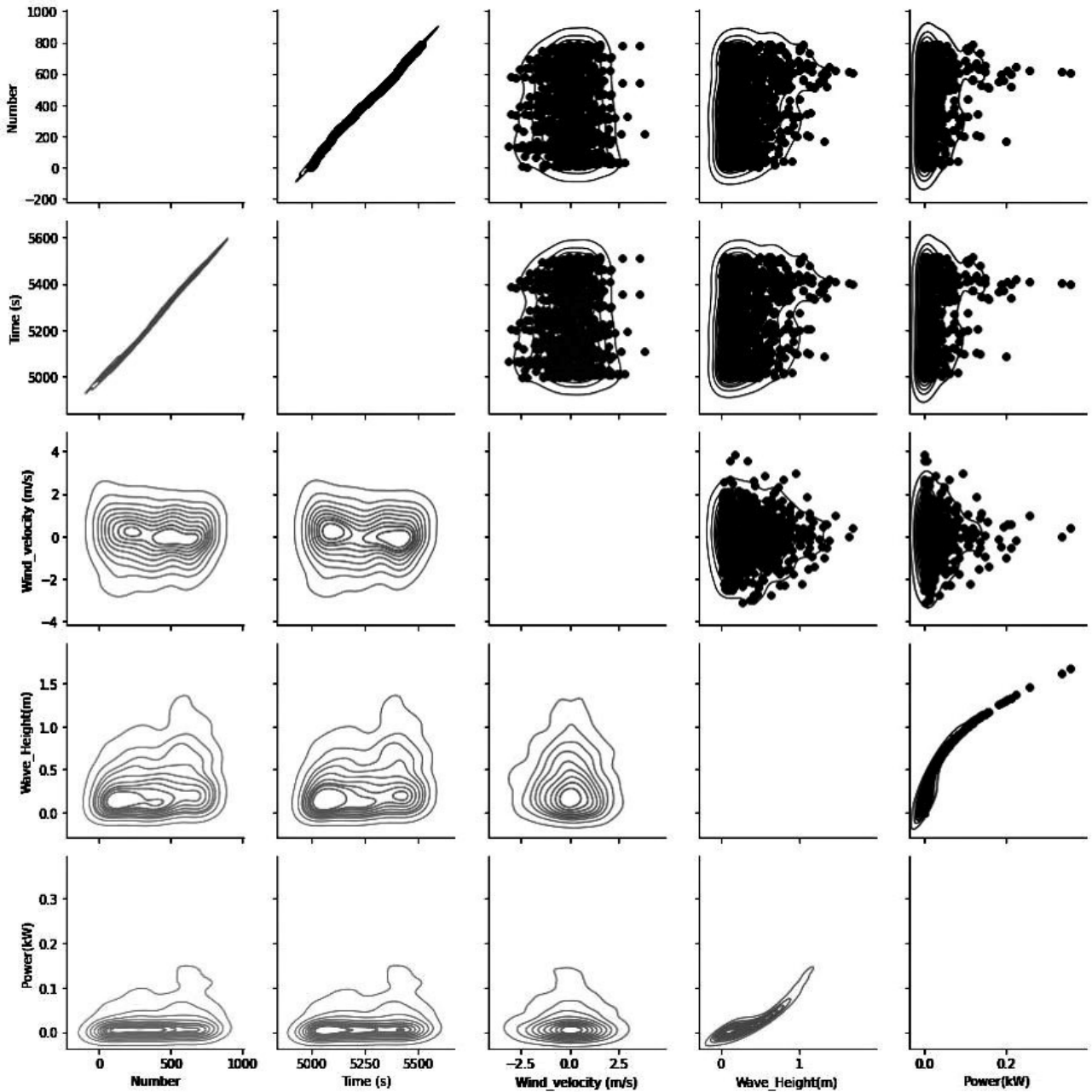


Figure 8. The linearization of scatter data within the correlation of different parameters with each other.

To find a higher correlated parameter among others neglected during predicting procedure, the correlation matrix could be prepared as Figure 9. This matrix shows the relation of different quantities with heat-map visualization method. It demonstrates the magnitudes with colors from lighter to darker one. The lighter color shows the best relation, so it is easy to infer that the prediction procedure finds a good relation between wave height and power.

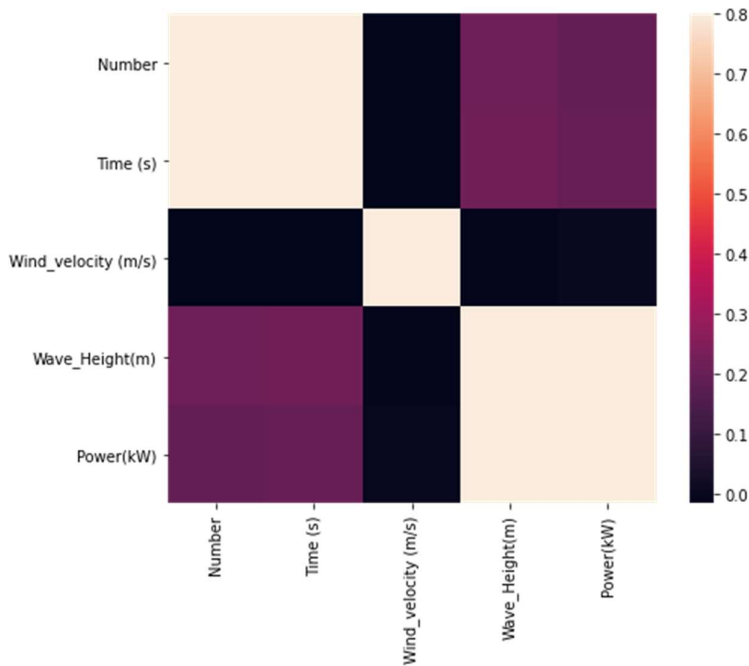


Figure 9. The correlation matrix of different parameters with each other.

For comparative analysis, it is necessary to compare the predicted production power graphs with numerical solution values to prove the efficiency of this method in using this field as shown in Figures 9 and 10. For this reason, Figure 10 shows the power curve in terms of simulation time. It presents the bar graph and the differences between two type of values shows obviously.

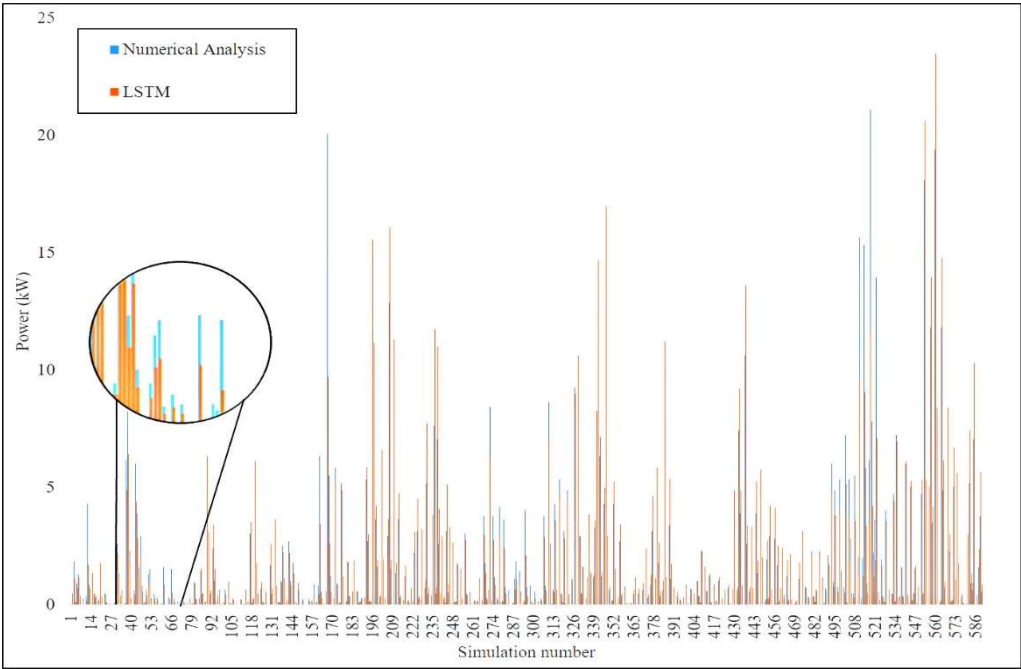


Figure 10. Comparative analysis of the numerical solution and LSTM method.

To evaluate the results of the simulation, it is necessary to make a comparison with another study. Figure 11 shows that to achieve larger powers, it is necessary for wave-lengths with higher altitudes to collide with the wave converter. Furthermore, the main claim of our study is to introduce a relation between the generated power and wave height. For this purpose, the output data of LSTM method were used and compared with numerical analysis which was done by simulation software. Furthermore, it presents this relation and the curve fitting operation and the mathematical relation introduced as a power function.

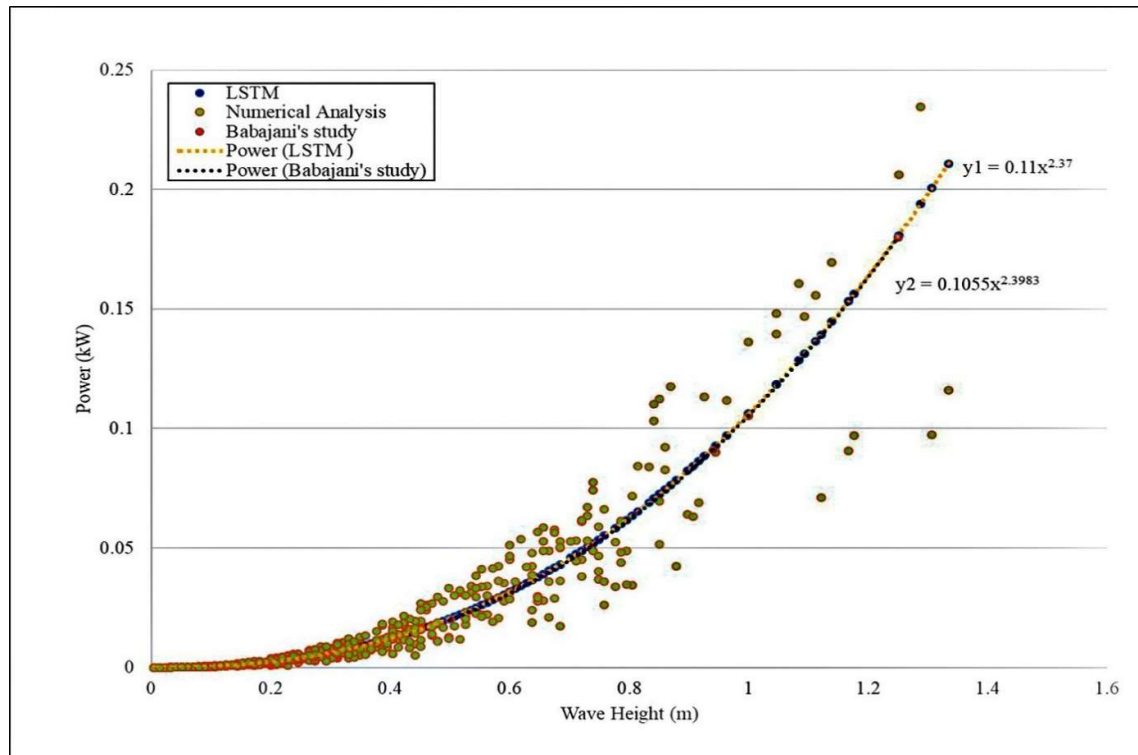


Figure 11. The relation between generated electrical power with wave height.

As shown in Figure 11, the recent study is compared with Babajani's study [31]. Among the differences for the difference between the results, we can point to a different input. Wider inputs are used and the results are more acceptable. The difference in the numerical results obtained from the simulation is only 0.05%, and this shows that the results can be trusted. As can be deduced from the comparison of the curves obtained in Figure 11, there is a good match between the two methods of numerical solution and LSTM. Numerical solution takes 4 days 1 hr, but predicting results by artificial intelligence takes only 2 minutes and 23 seconds. By obtaining mathematical equations from figure diagrams, a relation can be provided that from now on replaces a numerical solution that increases speed and accuracy. Regarding scalability, one important aspect is to assess the power extraction by the Searaser in the same real scale. Due to the fact, in this study, Searaser was numerically simulated by the data extracted from the patent scale. Therefore, the scale was 1:1 and the simulation results were close to reality. Furthermore, the data were curve fitted and two mathematical relations were presented to attribute the output power by the Searaser converter and the wave height, one of which was the relation provided by Babajani [31] and the other the relation presented by recent research. Equations 17 and 18 represent y1 and y2 in Figure 11.

$$P = 0.11H^{2.37} \quad (17)$$

$$P = 0.1055H^{2.3983} \quad (18)$$

In the following, we will examine one of the objectives of this study, which is the power diagram in terms of wind speed. Figure 12 shows this relationship extracted from the LSTM method.

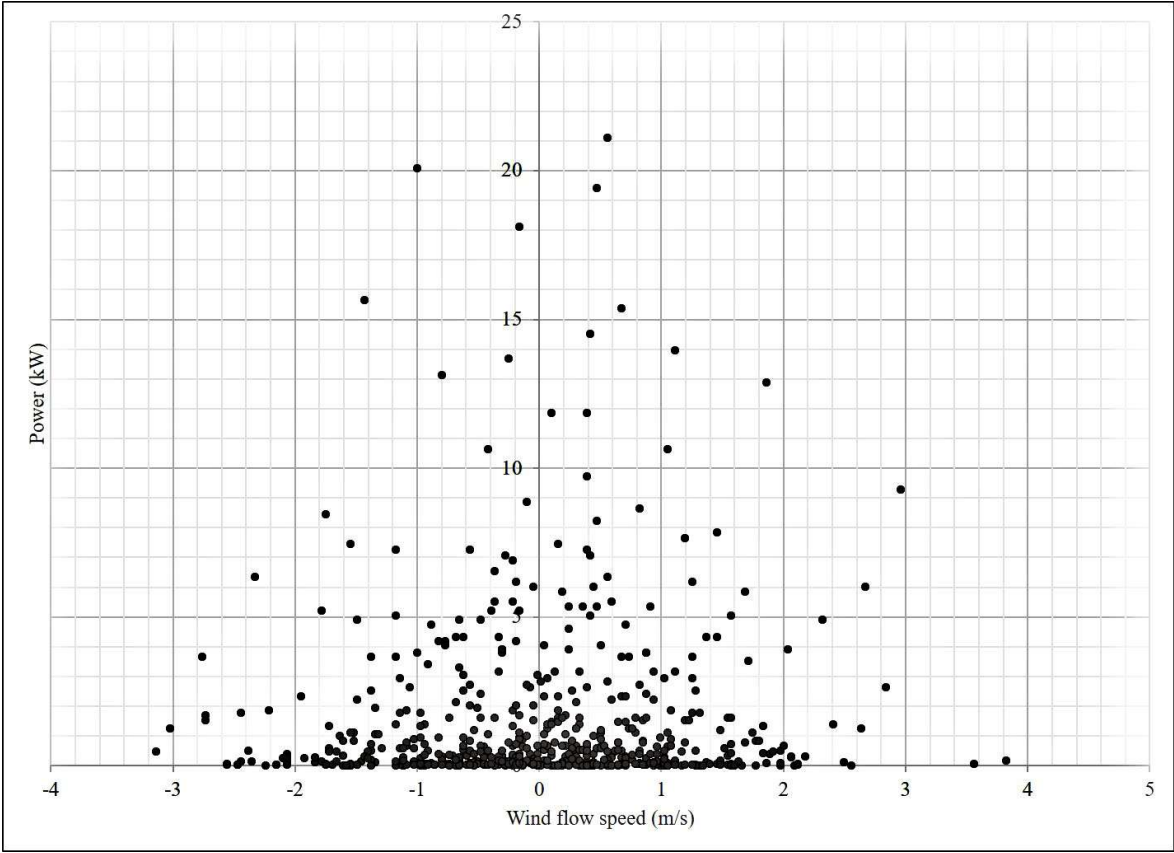


Figure 12. The relationship between output power and wind speed.

As can be deduced from Figure 12, the data frequency is low wind speed, and this chart is a reliable way to predict similar models because it is a combination of experimental card and simulation data modeled by artificial intelligence.

To represent the effect of selected parameter, the respective comparative analysis is displayed here. Root mean square error (RMSE) of these relations is presented as in Table 3.

Table 3 shows that there is a good agreement between two utilized methods and it can be concluded that the LSTM method is much faster and more accurate in predicting values.

Analysis Variables	RSME Value
Power Output, Wave height	0.56
Power Output, Simulation Time	0.42
Power Output, Wave height, Simulation Time	0.49

4. Conclusions

In this study, the power characteristics of Searaser are presented by analysing numerical and experimental data. A LSTM Network has been developed for predicting the power output of Searaser. By capability of the proposed LSTM prediction method, there can also be found a relationship between wind speed and the output Power of Searaser. According to the obtained results and the comparison between the two methods studied, it can be inferred that the LSTM Network is able to predict Power in terms of height more accurately and faster than the numerical solution and they were in a good agreement with the result of the numerical analysis. The comparison between the two methods shows that results of the machine learning method are so accurate and RSME value of the parameters are 0.49 as a mean value. This study makes progress on Energy management and investment for ocean renewable energy systems. The present study also exhibits some limitations, which open paths for future researches. Therefore, this study can be improved by analyzing more effective parameters on output power of ocean waves such as temperature, climate change, etc. Moreover, better results can be achieved by using accurate methods as well as the developing and upgrading WEC systems.

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References

1. Arutyunov VS, Lisichkin GV. Energy resources of the 21st century: problems and forecasts. Can renewable energy sources replace fossil fuels? Russian Chemical Reviews. 2017;86(8):777.
2. Perera F. Pollution from fossil-fuel combustion is the leading environmental threat to global pediatric health and equity: solutions exist. International journal of environmental research and public health. 2018;15(1):16.
3. Sinsel SR, Riemke RL, Hoffmann VH. Challenges and solution technologies for the integration of variable renewable energy sources—a review. renewable energy. 2020;145:2271-2285.
4. Aderinto T, Li H. Ocean wave energy converters: Status and challenges. Energies. 2018;11(5):1250.
5. Jiang B, Li X, Chen S, et al. Performance analysis and tank test validation of a hybrid ocean wave-current energy converter with a single power takeoff. Energy Conversion and Management. 2020;224:113268.
6. Ahamed R, McKee K, Howard I. Advancements of wave energy converters based on power take off (PTO) systems: A review. Ocean Engineering. 2020;204:107248.
7. Ocean Energy Systems. Annual Report Ocean Energy Systems 2016. 2017. Available online: <https://report2016.ocean-energy-systems.org/> [accessed on 21 December 2020]
8. Ruehl K, Forbush DD, Yu Y-H, et al. Experimental and numerical comparisons of a dual-flap floating oscillating surge wave energy converter in regular waves. Ocean Engineering. 2020;196:106575.
9. Giorgi G, Gomes RP, Henriques JC, et al. Detecting parametric resonance in a floating oscillating water column device for wave energy conversion: Numerical simulations and validation with physical model tests. Applied Energy. 2020;276:115421.
10. Shahriar T, Habib MA, Hasanuzzaman M, et al. Modelling and optimization of Searaser wave energy converter based hydroelectric power generation for Saint Martin's Island in Bangladesh. Ocean Engineering. 2019;192:106289.
11. Reikard G, Robertson B, Bidlot J-R. Wave energy worldwide: simulating wave farms, forecasting, and calculating reserves. International journal of marine energy. 2017;17:156-185.
12. Pena-Sanchez Y, Garcia-Abril M, Paparella F, et al. Estimation and forecasting of excitation force for arrays of wave energy devices. IEEE Transactions on Sustainable Energy. 2018;9(4):1672-1680.
13. Sang Y, Karayaka HB, Yan Y, et al. 1.18 ocean (marine) energy. 2018.
14. Reikard G, Robertson B, Bidlot J-R. Combining wave energy with wind and solar: Short-term forecasting. Renewable Energy. 2015;81:442-456.
15. Bento P, Pombo J, Mendes R, et al. Ocean wave energy forecasting using optimised deep learning neural networks. Ocean Engineering. 2021;219:108372.
16. Ni C, Ma X. Prediction of wave power generation using a convolutional neural network with multiple inputs. Energies. 2018;11(8):2097.

17. Liu Z, Wang Y, Hua X. Prediction and optimization of oscillating wave surge converter using machine learning techniques. *Energy Conversion and Management*. 2020;210:112677.
18. Li L, Gao Y, Ning D, et al. Development of a constraint non-causal wave energy control algorithm based on artificial intelligence. *Renewable and Sustainable Energy Reviews*. 2020:110519.
19. Gómez-Orellana AM, Fernández JC, Dorado-Moreno M, et al. Building Suitable Datasets for Soft Computing and Machine Learning Techniques from Meteorological Data Integration: A Case Study for Predicting Significant Wave Height and Energy Flux. *Energies*. 2021;14(2):468.
20. Butt FM, Hussain L, Mahmood A, et al. Artificial Intelligence based accurately load forecasting system to forecast short and medium-term load demands. *Mathematical Biosciences and Engineering: MBE*. 2020;18(1):400-425.
21. Cheng Y, Xu C, Mashima D, et al., editors. *PowerLSTM: power demand forecasting using long short-term memory neural network*. International Conference on Advanced Data Mining and Applications; 2017: Springer.
22. Lin Z, Cheng L, Huang G. Electricity consumption prediction based on LSTM with attention mechanism. *IEEE Transactions on Electrical and Electronic Engineering*. 2020;15(4):556-562.
23. Ni C, Ma X, Wang J, editors. Integrated deep learning model for predicting electrical power generation from wave energy converter. 2019 25th International Conference on Automation and Computing (ICAC); 2019: IEEE.
24. He J. Coherence and cross-spectral density matrix analysis of random wind and wave in deep water. *Ocean Engineering*. 2020;197:106930.
25. Smith A. Patent Application Publication US 2013/0052042 A1. Pumping Device.
26. Pedrycz W, Skowron A, Kreinovich V. *Handbook of granular computing*. John Wiley & Sons; 2008.
27. Bhinder M, Mingham C, Causon D, et al., editors. Numerical and experimental study of a surging point absorber wave energy converter. Proceedings of the 8th European Wave and Tidal Energy Conference, Uppsala, Sweden; 2009.
28. Hirt C. *Flow-3D Users Manual*, Flow Sciences. Inc; 1988.
29. Gomes RP, Henriques JC, Gato LM, Falcão AD. Hydrodynamic optimization of an axisymmetric floating oscillating water column for wave energy conversion. *Renewable Energy*. 2012 Aug 1; 44: 328-39.
30. Elsayed MA. Wavelet bicoherence analysis of wind-wave interaction. *Ocean Engineering*. 2006;33(3-4):458-470.
31. Babajani A. Hydrodynamic Performance of a Novel Ocean Wave Energy Converter. *American Journal of Fluid Dynamics*. 2018;8(3):73-83.
32. López E, Valle C, Allende H, et al. Wind power forecasting based on echo state networks and long short-term memory. *Energies*. 2018;11(3):526.
33. Duan Y, Yisheng L, Wang F-Y, editors. Travel time prediction with LSTM neural network. 2016 IEEE 19th international conference on intelligent transportation systems (ITSC); 2016: IEEE.
34. Ma X, Tao Z, Wang Y, et al. Long short-term memory neural network for traffic speed prediction using remote microwave sensor data. *Transportation Research Part C: Emerging Technologies*. 2015;54:187-197.
35. Li H. *Wave Energy Potential, Behavior and Extraction*. MDPI; 2020.
36. Aderinto T, Li H. Ocean wave energy converters: Status and challenges. *Energies*. 2018;11(5):1250.
37. Nezhad MM, Groppi D, Rosa F, et al. Nearshore wave energy converters comparison and Mediterranean small island grid integration. *Sustainable Energy Technologies and Assessments*. 2018;30:68-76.