Article

An Exhaustive Review of Bio-Inspired Algorithms and its Applications for Optimization in Fuzzy Clustering

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- 1 Abstract: In recent years, new metaheuristic algorithms have been developed taking as reference
- the inspiration on biological and natural phenomena. This nature-inspired approach for algorithm
- 3 development has been widely used by many researchers in solving optimization problem. These
- 4 algorithms have been compared with the traditional ones algorithms and have demonstrated to
- 5 be superior in complex problems. This paper attempts to describe the algorithms based on nature,
- 6 that are used in fuzzy clustering. We briefly describe the optimization methods, the most cited
- 7 nature-inspired algorithms published in recent years, authors, networks and relationship of the
- works, etc. We believe the paper can serve as a basis for analysis of the new are of nature and bio-inspired optimization of fuzzy clustering.

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11 Keywords: FUZZY; CLUSTERING; OPTIMIZATION ALGORITHMS

1. Introduction

Optimization is a discipline for finding the best solutions to specific problems. Every day we developed many actions, which we have tried to improve to obtain the best solution; for example, the route at work can be optimized depending on several factors, as traffic, distance, etc. On other hand, the design of the new cars implies an optimization process with many objectives as wind resistance, reduce the use of fuel, maximize the potency of motor, etc. These best solutions are found by adapting the parameters of the algorithm to give either a maximum or a minimum value for the

solution. Therefore, in the last years many optimization methods have been developed with the aim of improving existing solutions.

Nowadays, many optimization algorithms based on nature can be found in the literature, it is calculated there are more than 150 different algorithms, and improved algorithms for finding the best results on the optimization problems [1–11]. However, it is not our aim to analyze all methods. Instead, our approach will be on the bio-inspired algorithms that are dealing with fuzzy clustering. Therefore, we have selected only a few algorithms in this review. Although, we have worked with different algorithms in different ways, for example, with parameter adaptation using fuzzy logic, original methods, the selected methods were chosen because they have demonstrated are good alternative for solving many optimization problems, and we have experience working with them. However, we focused with the applications about optimization fuzzy clustering.

Nature inspired algorithms can be classified as those based on biology and those inspired on natural phenomena. The algorithms based on biology can be further divided into those based on evolution and those based on swarm behavior. The evolutionary algorithms include the Genetic Algorithms, Differential Evolution, Cultural Evolution, Evolutionary Strategies, Genetic Programming. The swarm category includes Particle Swarm Optimization, Ant Colony Optimization [12], Artificial Bees [13], Termites [14], Bats [15], Birds [16], Cats [17], Bacterial Foraging [18], Cuckoo Search [19], Firefly algo-

39 rithm [20] and others. Also, there are algorithms based on the physical laws; for example,

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40 Simulated Annealing, the Gravitational Search algorithm and the Big Bang Big Crunch 41 algorithm.

42 2. Literature Review

In this section, we made a general review about the methods using optimization fuzzy clustering with different bio-inspired optimization methods. However, in the 44 45 following sections a deep study is developed doing specific queries of Web of Science, and the tool VoSviewer to calculate the clusters of the analyzed works. InTable 1, is 46 presented a list with the most popular bio-inspired optimization algorithms based on swarms, physics, populations, chemistry and evolution. This table shows many methods 48 in chronological orders that have been used since 1975 to date. However, only are some methods but can be useful to expand the knowledge about these methods and to 50 51 observe the inspiration type. We made the query in Web of Science: 'Optimization fuzzy 52 clustering', we found a total of 2208 papers with this topic. However, in this paper only is presented a description of the most recent works, but with the query above mentioned can be seen the updated works. Figure 1, shows the countries with major number of 54 55 publications.

Recently, multi-view clustering research has attracted considerable attention because of duo the rapidly increasing demand for unsupervised analysis of multi-view data in practical applications. In [21], was presented a novel Two-level Weighted Collaborative Multi-view Fuzzy Clustering (TW-Co-MFC) approach to address the aforementioned issues. In this method, TW-Co-MFC, a two-level weighting strategy is devised to measure the importance of views and features, and a collaborative working mechanism is introduced to balance the within-view clustering quality and the cross-view clustering 63 consistency.

Also, in [22], authors proposed the image segmentation using Bat Algorithm with 64 Fuzzy C Means clustering. The proposed segmentation technique was evaluated with 65 existing segmentation techniques. On the other hand, in [23], the authors presented hybridization of SKH and RKFCM clustering optimization algorithm for efficient 67 68 moving object exploration.

Another recent study on this area is shown in [24], where the authors presented 69 a hybrid interval type-2 semi-supervised possibilistic fuzzy c-means clustering and 70 71 particle swarm optimization for satellite image analysis.

Also, in [25] a fuzzy based unequal clustering and context aware routing proce-72 dure with glow-worm swarm optimization was developed in random way point based 73 dynamic wireless sensor networks. Based on fuzzy systems the unequal clustering 74 is formed and the optimal cluster head is nominated to convey the information from cluster member to base station to increase the system lifespan and to decrease the energy 77 consumption.

Table 1: Popular Bio-inspired Optimization Algorithms based on swarms, physics, populations, chemistry and evolution.

Year	Algorithms and references
2021	Horse herd optimization algorithm [26]
2020	Mayfly Optimization Algorithm [27]
2020	Chimp Optimization Algorithm [28]
2020	Coronavirus Optimization Algorithm [29]
2020	Water strider algorithm [30]
2020	Newton metaheuristic algorithm [31]
2020	Black Widow Optimization Algorithm [32]
2019	Harris hawks optimization [33]
2019	Sailfish Optimizer [34]
2019	Spider Monkey Optimization [35]
2017	Grasshopper Optimisation Algorithm [36]
2017	Fractal Based Algorithm [37]
2017	Bacterial Foraging Inspired Algorithm [18]
2017	Rain-fall Optimization Algorithm [38]
2016	Dragonfly algorithm [39]
2016	Sperm Whale Algorithm [40]
2015	Water Wave Optimization [41]
2015	Ant Lion Optimizer [42]
2014	Symbiotic Organisms Search [43]
2013	Egyptian Vulture Optimization Algorithm [44]
2013	Dolphin echolocation [45]
2012	Great Salmon Run [46]
2012	Big Bang-Big Crunch [47]
2012	Flower Pollination Algorithm [48]
2011	Spiral Optimization Algorithm [49]
2011	Galaxy-based Search Algorithm [50]
2010	Japanese Tree Frogs [51]
2010	Bat Algorithm [15]
2010	Termite Colony Optimization [14]
2010	Firefly Algorithm [20]
2009	Cuckoo Search [19]
2009	Glowworm Swarm Optimization [52]
2009	Bee Colony Optimization [53]
2009	Gravitational Search Algorithm [54]
2008	Fast Bacterial Swarming Algorithm [55]
2007	River Formation Dynamics [56]
2007	Imperialistic Competitive Algorithm [57]
2008	Roach Infestation Optimization [58]
2006	The bees Algorithm [13]
2006	Cat Swarm Optimization [17]
2004	BeeHive [59]
2003	Queen-Bee Evolution [60]
2001	Harmony Search Algorithm [61]
1995	Particle Swarm Optimization [16]
1992	Genetic Programming [62]
1992	Ant Colony Optimization [12,63]
1989	Tabu Search [64]
1975	Genetic Algorithms [65]

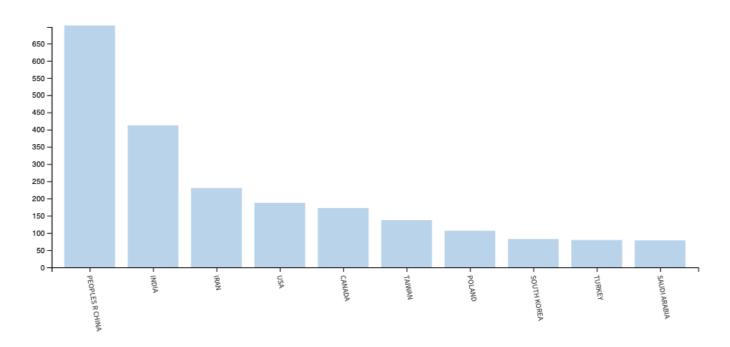


Figure 1. 2,208 papers of Web of Science for topic: (Optimization fuzzy clustering) by Countries.

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78 3. Bio-Inspired Optimization Methods

This section presents the algorithms used as reference in this study. After making a complete review of the methods above mentioned. We decide to include, in making our study, some important and relevant methods along the history. Though, there are many algorithms, it is impossible to include all methods. However, with these selected methods it is possible to give us an idea of the relationship of authors, citations, cluster of work networks with specific queries from high impact journals and other important information. The main aim of this section is to briefly outline the basic concepts of several bio-inspired optimization algorithms for a better comprehension of the importance of 87 this area. The selected algorithms are presented in the following sub-sections.

88 3.1. Genetic Algorithms

John Holland, from the University of Michigan initiated his key work on genetic 89 algorithms at the beginning of the 1960s. His first achievement was the publication of Adaptation in Natural and Artificial Systems in 1975, developing a popular method in 91 the evolutionary computation field, known as genetic algorithm. In the simple genetic 92 algorithm, the representation used is a bit string. Each position in the string is assumed 93 to represent a particular feature of an individual, and the value stored in that position represents how that feature is coded in the solution. Usually, the string is "evaluated as 95 a collection of structural features of a solution that have little or no interactions". The analogy may be drawn directly to genes in biological organisms. Each gene represents an 97 entity that is structurally independent of other genes. The main reproduction operator 98 used is bit-string crossover, in which two strings are used as parents and new individuals 99 are formed by swapping a sub-sequence between the two strings. Another popular 100 operator is bit-flipping mutation, in which a single bit in the string is flipped to form 101 a new offspring string. A variety of other operators have also been developed, but 102 are used less frequently. A primary distinction that may be made between the various 103 104 operators is whether or not they introduce any new information into the population. Crossover, for example, does not while mutation does. All operators are also constrained 105 to manipulate the string in a manner consistent with the structural interpretation of 106 genes. For example, two genes at the same location on two strings may be swapped

between parents, but not combined based on their values. Traditionally, individuals are selected to be parents probabilistically based upon their fitness values, and the offspring that are created replace the parents. For example, if N parents are selected, then N offspring are generated which replace the parents in the next generation [65].

112 3.2. Particle Swarm Optimization

Particle Swarm Optimization (PSO) is a population based stochastic optimization technique developed by Eberhart and Kennedy in 1995, inspired by social behavior of bird flocking or fish schooling.

PSO shares many similarities with evolutionary computation techniques such as the Genetic Algorithms (GA). The system is initialized with a random population solutions and searches for optima by updating generations. However, unlike the GA, the PSO has no evolution operators such as crossover and mutation. In PSO, the potential solutions, called particles, fly through the problem space by following the current best particles [1,11,66].

Another reason that PSO is attractive is that there are few parameters to adjust. One version, with slight variations, works well in a wide variety of applications. Particle swarm optimization has been used for approaches that can be used across a wide range of applications, as well as for specific applications focused on a specific requirement.

126 3.3. Cuckoo Search Algorithm

Cuckoo Optimization Algorithm is based on the life of a bird called 'cuckoo'. The 127 basis of this novel optimization algorithm is specific breeding and egg laying of this bird. 128 Adult cuckoos and eggs are used in this modeling. The cuckoos which are adult lay 129 eggs in other birds' habitat. These eggs grow and become a mature cuckoo if they are 130 not found and not removed by host birds. The immigration of groups of cuckoos and 131 environmental specifications hopefully lead them to converge and reach the best place for reproduction and breeding. The objective function is in this best place [19]. CSA is a 133 new continuous over all aware search based on the life of a cuckoo bird. Similar to other 134 meta heuristic, CSA begins with a main population, a group of cuckoos. These cuckoos lay some eggs in the habitat of other host birds. A random group of potential solutions 137 is generated that are considered to represent the habitat in CSA.

138 3.4. Bat Algorithm

Bat algorithm (BA) is a bio-inspired algorithm inspired on bat behavior and BA has been found to be very efficient. If we idealize some of the echolocation characteristics of, we can develop various bat-inspired algorithms or bat algorithms. For simplicity, we now use the next idealized rules:

- 1. All bats use echolocation to sense distance, and they also 'know' the difference between food/prey and background barriers in some unknown way.
- 2. Bats fly randomly witch velocity v_i at position x_i witch a fixed frequency, varying wavelength and loudness A_0 to search for prey. They can automatically adjust the wavelength (or frequency) of their emitted pulses and adjust the rate of pulse emission r [148] [0, 1], depending on the proximity of their target.
- 3. Although loudness can vary in many ways, we assume that the loudness varies from a large (positive) A_0 to a minimum constant value A_{min} .

For simplicity, the frequency f is in [0, {max}], the new solutions and velocity at a specific time step t are represented by a random vector drawn from a uniform is distribution [15].

154 4. Experimental Results

In this section, is presented the obtained results with the different tools available in the literature for building the networks clusters, relationships, citations, with the analyzed methods. To validate the queried information of Web of Science, the VosViewer

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tool [67] was used. However, this type of studies can be made by other similar tools to make bibliometric analysis. For example, Bibliometrix [68] is a free tool that provides 159 various routines for importing bibliographic data from SCOPUS and Clarivate Analytics' Web of Science databases; Bibliotool [69], is a set of python scripts written by Sebastian 161 Grauwin. They can read ISI data in CSV format and do some studies including co-162 occurrence map and bibliographic coupling; finally, CiteSpace [70] is a free Java-based 163 software for visualizing and analyzing trends and patterns in the scientific literature. It 164 165 is designed as a tool for progressive knowledge domain visualization.

166 4.1. Study with Genetic Algorithms

In this section, is presented the obtained results of the queries in Web of Science with 168 the topic 'optimization fuzzy clustering with genetic algorithms'. First, it was necessary to access the web of science, and then make the desired queries. Once the information was extracted, and using the Vos Viewer tool, it was possible to calculate the related works, citations, authors, etc. Figure 2, represents a map based on network data collected from the bibliographic database in Web of Science. The type of analysis represented in this Figure is by co-occurrence, the unit of analysis was by keywords, the minimum number of documents of an author was 5, minimum number of citations was 0, the counting method was full counting, minimum number of occurrences of a keyword was 5; and finally, for each of the 92 keywords, the total strength of the co-ocurrence links with other keywords was calculated. On VosViewer, if the keyword 'genetic algorithm' is selected, we can appreciate the number of clusters is 7 for this selection, with 88 links, 179 and 141 occurrences.

Figure 3, represents the selection of the keyword 'genetic algorithm' that corre-180 181 sponding to the information obtained from Figure 2.

Figure 4, shows the total of papers collected from Web of Science and that were 182 used to make the calculus above described in Figure 2 and Figure 3. It can be seen how 183 the number of citations and papers with the analyzed topic has been increasing in recent 185 vears

Also, with this information was possible to observe, the record by authors, where 186 in Figure 5, it can be appreciated that two authors are the leaders in this area with the 188 topic 'optimization fuzzy clustering with genetic algorithms'.

189 4.2. Study with Particle Swarm Optimization

In this section, is presented the obtained results of the queries in Web of Science with 191 the topic 'optimization fuzzy clustering with genetic algorithms'. First, it was necessary to access the web of science, and then make the desired queries. Once the information was extracted, and using the Vos Viewer tool, it was possible to calculate the related works, citations, authors, etc. Figure 6, represents a map based on network data collected from the bibliographic database in Web of Science. The type of analysis represented in this Figure is by co-occurrence, the unit of analysis was by keywords, the minimum number of documents of an author was 5, minimum number of citations was 0, the counting method was full counting, minimum number of occurrences of a keyword was 5; and finally, for each of the 116 keywords, the total strength of the co-ocurrence links with other keywords was calculated. On VosViewer, if the keyword 'particle swarm optimization' is selected, we can appreciate the number of cluster is 8 for this selection, with 108 links, and 234 occurrences.

Figure 7, represents the selection of the keyword 'genetic algorithm' that corre-203 204 sponding to the information obtained from Figure 6.

Figure 8, shows the total of papers collected from Web of Science and that were 205 used to make the calculus above described in Figure 6 and Figure 7. It can be seen how 206 the number of citations and papers with the analyzed topic has been increasing in recent 207 208 years.

A VOSviewer

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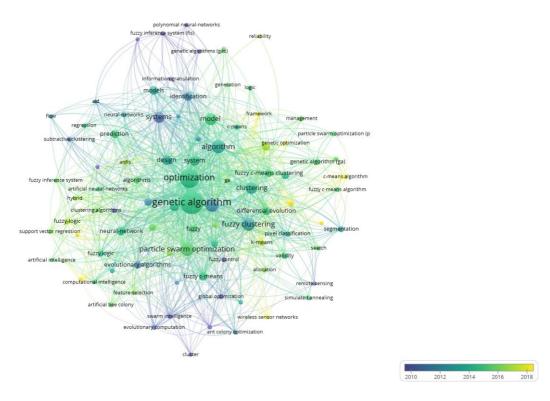


Figure 2. Total cluster obtained with the search 'optimization fuzzy clustering with genetic algorithms' from VOS viewer

Also, with this information was possible to observe, the records by authors, where 209 in Figure 9, it can be appreciated that two authors are the leaders in this area with the 211 topic 'optimization fuzzy clustering with particle swarm optimization'.

212 4.3. Study with Cuckoo Search Algorithm

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In this section, we present the obtained results of the queries in Web of Science with the topic 'optimization fuzzy clustering with Cuckoo Search Algorithm'. The main difference with the other analyzed algorithms was that only 23 papers were found with the reviewed topic. Also, it was necessary to access the web of science, and then make the desired queries. Once the information was extracted, and using the Vos Viewer tool, it was possible to calculate the related works, citations, authors, etc. Figure 10, represents a map based on network data collected from the bibliographic database in Web of Science. The type of analysis represented in this Figure is by co-occurrence, the unit of analysis was by keywords, the minimum number of documents of an author was 5, minimum number of citations was 0, the counting method was full counting, minimum number of occurrences of a keyword was 5; and finally, for each of the 3 keywords, the total strength of the co-occurrence links with other keywords was calculated. On VosViewer, we can appreciate the number of clusters is 2 as can be seen in Figure 10 with only 1 link. 226 With these results, it can be seen that this method has not been widely used or combined 227 with fuzzy clustering.

Figure 11, shows the total of papers collected from Web of Science and that were 228 used to make the calculus above described in Figure 10. It can be seen how the number 229 230 of citations and papers are less than the other analyzed methods.

Also, with this information was possible to observe, the records by authors, where 231 in Figure 9, it can be appreciated that two authors are the leaders in this area with the 233 topic 'optimization fuzzy clustering with cuckoo search algorithm'.

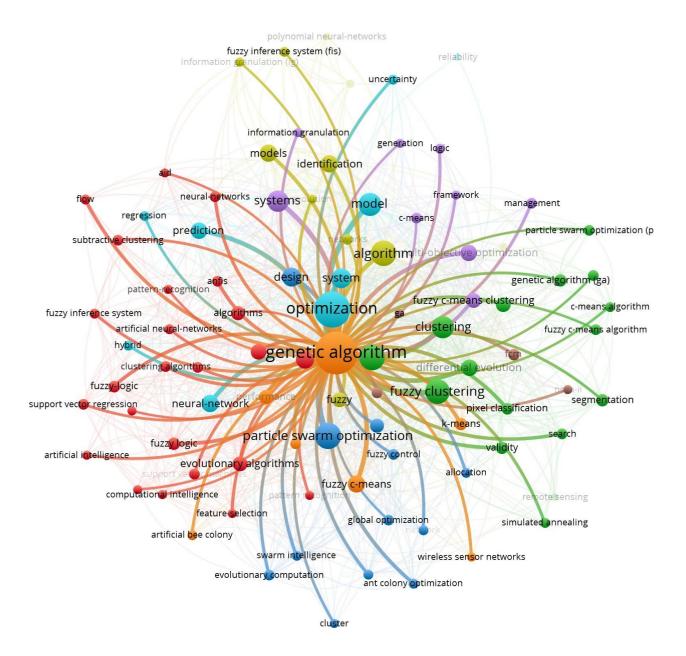


Figure 3. Represent the selection of the keyword 'genetic algorithm'.

234 4.4. Study with Bat Algorithm

In this section, is presented the obtained results of the queries in Web of Science with 235 the topic 'optimization fuzzy clustering with Bat Algorithm'. The main difference with 236 the other analyzed algorithms was that only 23 papers were found with the reviewed 237 topic. Also, it was necessary to access the web of science, and then make the desired 238 queries. Once the information was extracted, and using the Vos Viewer tool, it was 239 possible to calculate the related works, citations, authors, etc.Figure 13, represents a 240 map based on network data collected from the bibliographic database in Web of Science. 241 The type of analysis represented in this Figure is by co-occurrence, the unit of analysis was by keywords, the minimum number of documents of an author was 5, minimum 243 number of citations was 0, the counting method was full counting, minimum number of occurrences of a keyword was 5; and finally, for each of the 3 keywords, the total 245 strength of the co-occurrence links with other keywords was calculated. On VosViewer, we can appreciate the number of clusters is 1 as can be seen in Figure 13 with only 1 link. 247

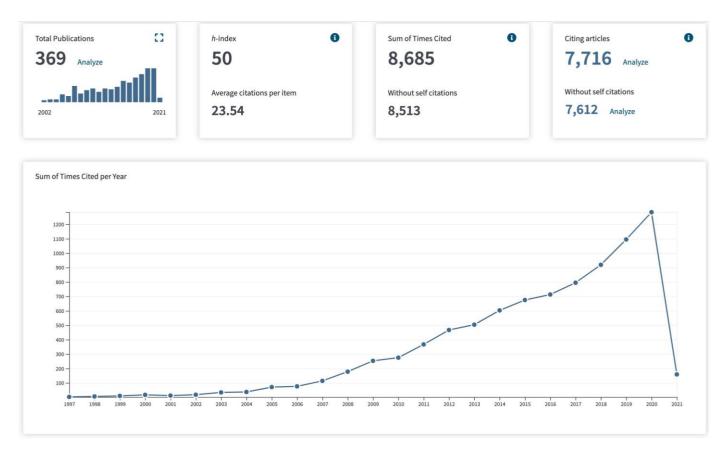


Figure 4. Citation report for 369 results from Web of Science Core Collection

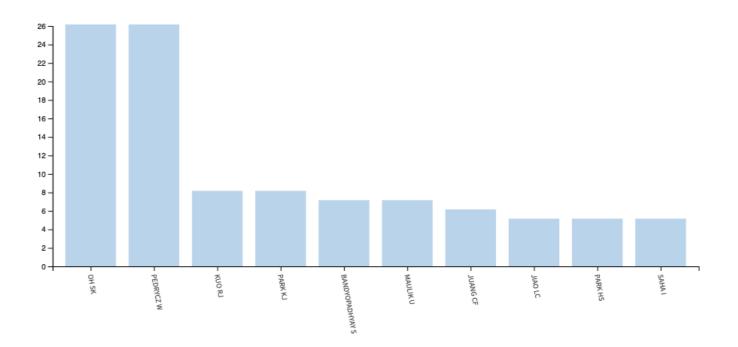


Figure 5. Record by authors for TOPIC: (optimization fuzzy clustering with genetic algorithms)

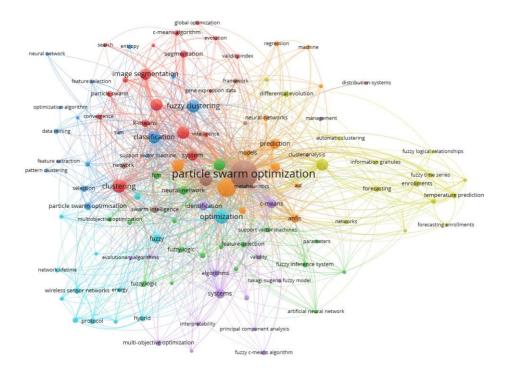


Figure 6. Total cluster obtained with the search 'optimization fuzzy clustering with particle swarm optimization' from VOS viewer

²⁴⁸ With these results, it can be seen that this method has not been widely used or combined ²⁴⁹ with fuzzy clustering.

Figure 14, shows the total of papers collected from Web of Science and that were used to make the calculus above described in Figure 13. It can be seen how the number 252 of citations and papers are less than the other analyzed methods.

Also, with this information was possible to observe, the record by authors, where in Figure 15, it can be appreciated that two authors are the leaders in this area with the topic 'optimization fuzzy clustering with bat algorithm'.

256 4.5. Analysis by authors

VOSviewer

In this section is presented an analysis by authors, considering the total cites from web of science, we can appreciate that the author with more works in this area with the analyzed algorithms in this paper is Witold Pedrycz from the University of Alberta, Canada. According with the information collected of Web of Science, Figure 16 shows the total of the publications of this author.

Figure 17, was calculated in Vos Viewer and represents the relationship authors with Witold Pedrycz in the area of fuzzy clustering. The graph, was made considering global work with a total of 1001 works collected from Web of Science.

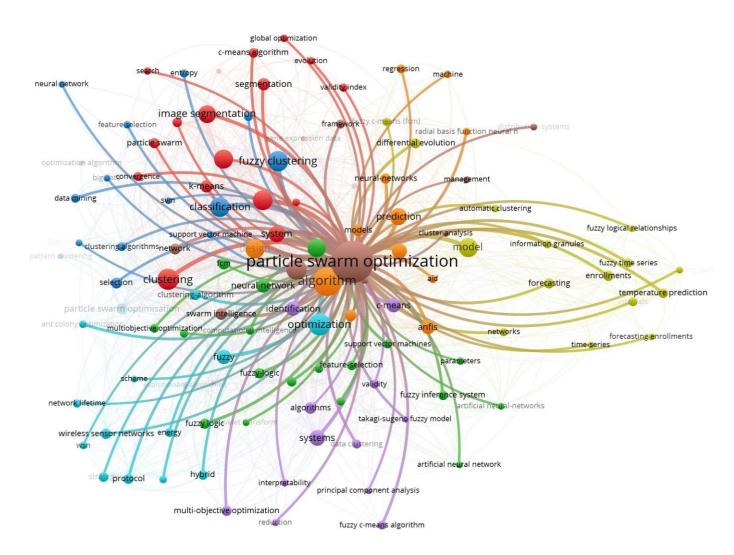


Figure 7. Representing the selection of the keyword 'particle swarm optimization'.



Figure 8. Citation report for 508 results from Web of Science Core Collection

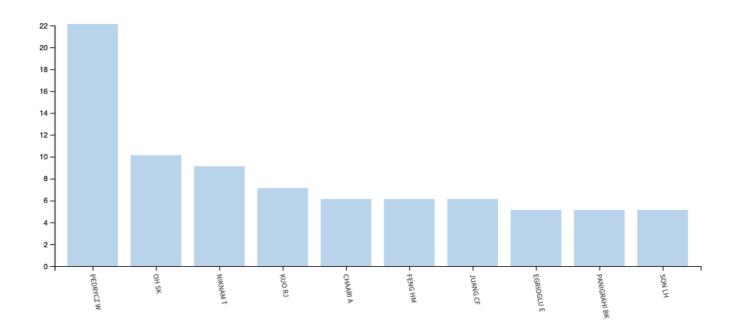


Figure 9. Record by authors for TOPIC: (optimization fuzzy clustering with particle swarm optimization)

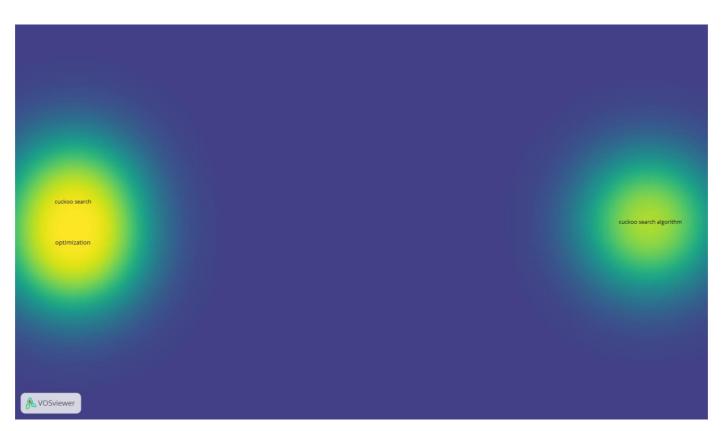


Figure 10. Total cluster obtained with the search 'optimization fuzzy clustering with cuckoo search optimization' from VOS viewer

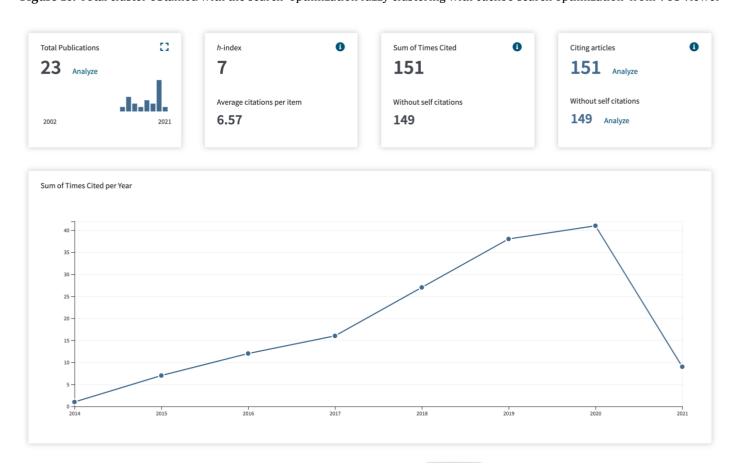


Figure 11. Citation report for 23 results from Web of Science Core Collection

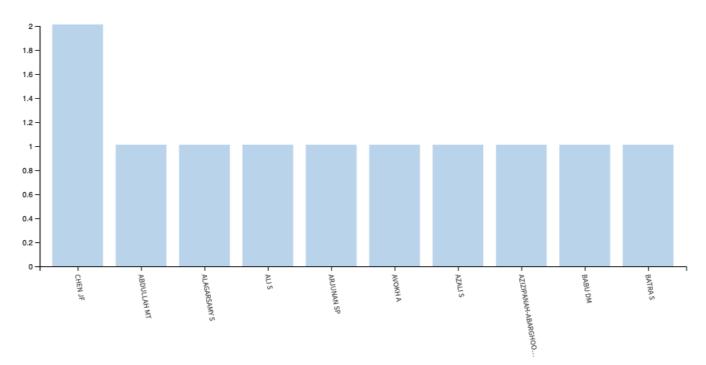
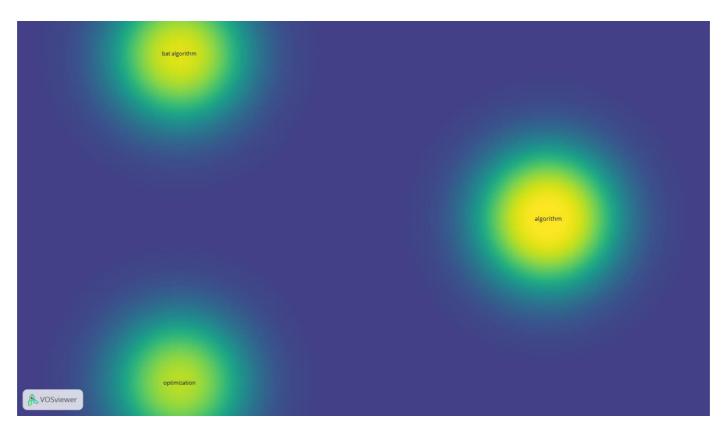


Figure 12. Record by authors for TOPIC: (optimization fuzzy clustering with cuckoo search algorithm)



 $\textbf{Figure 13.} \ \ \textbf{Total cluster obtained with the search 'optimization fuzzy clustering with cuckoo search optimization' from VOS viewer$



Figure 14. Citation report for 23 results from Web of Science Core Collection

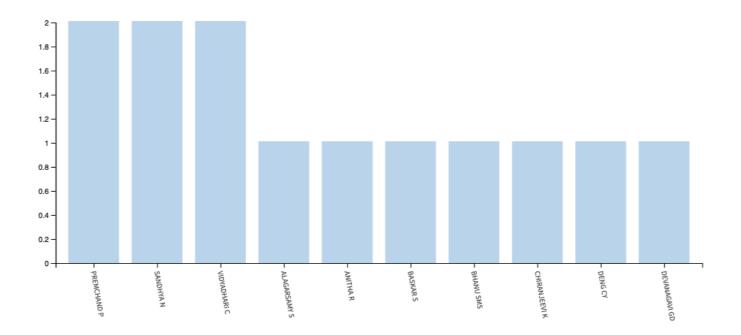


Figure 15. Record by authors for TOPIC: (optimization fuzzy clustering with bat algorithm)



Figure 16. Citation report for 1,001 results from Web of Science Core Collection by the author Witold Pedrycz.

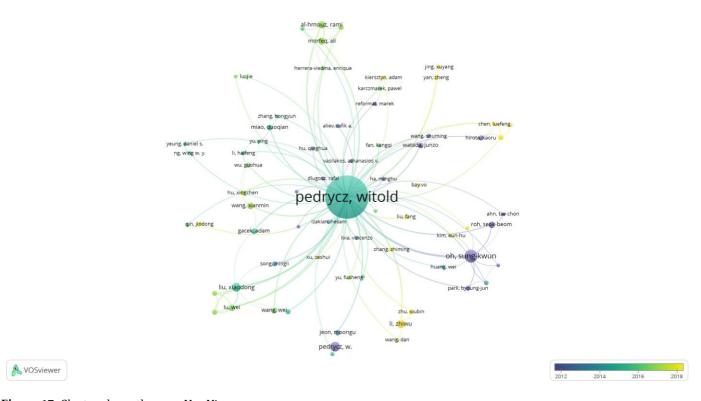


Figure 17. Clusters by authors on Vos Viewer

5. Conclusions

After reviewing the state of the art about area optimization fuzzy clustering with 266 optimization methods. We decided to make an analysis, considering four optimization 267 methods, which we have used in the last year. With all collected information of Web of 268 Science, Vos Viewer tool, we can observe that Genetic Algorithms and Particle Swarm 269 Optimization are two very popular methods that the authors have been using in the last 270 years. On the other hand, Cuckoo Search and Bat Algorithm, are two methods newer 271 than the other two. However, not many authors have attempted to make fuzzy clustering 272 using these two methods. Also, we were able to review the author with more works in this area. As a future work, this review can be extended analyzing other optimization 274 methods with fuzzy clustering. The type of queries can be made by authors, keywords, occurrences, etc. However, with the paper can be reviewed the software and tools used 276 and can be extracted all the information here presented. 277

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