Optimal Power Flow Considering Intermittent Solar and Wind Generation using Multi-Operator Differential Evolution Algorithm

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Abstract

In this paper, a multi-operator differential evolution algorithm (MODE) is proposed to solve the Optimal Power Flow (OPF) problem and is called MODE-OPF. The MODE-OPF utilizes the strengths of more than one differential evolution (DE) operator in a single algorithmic framework. Additionally, an adaptive method (AM) is proposed to update the number of solutions evolved by each DE operator based on both the diversity of population and quality of solutions. This adaptive method has the ability to maintain diversity at the early stages of the optimization process and boost convergence at the later ones. The performance of the proposed MODE-OPF is tested by solving OPF problems for both small and large IEEE bus systems (i.e., IEEE-30 and IEEE-118) while considering the intermittent solar and wind power generation. To prove the suitability of this proposed algorithm, its performance has been compared against several state-of-the-art optimization algorithms, where MODE-OPF outperforms other algorithms in all experimental results and thereby improving a network's performance with lower cost. MODE-OPF decreases the total generation cost up to 24.08%, the real power loss up to 6.80% and the total generation cost with emission up to 8.56%.

Keywords: Evolutionary Algorithms, differential evolution, constraints handling techniques, optimal power flow, renewable energy

1. Introduction

The complexity of electric power system is gradually increasing due to a number of reasons, including high power demand and intermittent power generation from renewable energy sources (RESs), in addition to its well-known large scale, several dynamic/static states and difficult interfaces among components. Effective management and control of such a system are crucial to maintain a reliable, secure power supply [1]. However, it is one of the most challenging tasks for the system operators because of the close monitoring required of the large range of data that need to be measured, computed and controlled with appropriate actions [2]. To manage the utility grid effectively and efficiently,

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optimal power flow (OPF) and economic dispatch are generally performed by the network operators [3]. Economic dispatch deals with the least-cost generation dispatch to fulfil the power demand, but it ignores power flow constraints that may violate the physical limits of a transmission network.

The OPF problem, one of the fundamental tools to maintain reliable, economic power system operation, has drawn the attention of researchers since it was introduced by [4]. The problem is to optimize a chosen objective function, such as total generation cost and active power loss, through the appropriate selection of the control variables while fulfilling many inequality and equality constraints, such as power flow equations, and the bounds of control and dependent variables. The control variables, including real powers and bus voltage of generators, switchable reactive power of Volt-Amps-Reactive (VAR), and tap settings of transformers, are chosen in a way that minimizes system losses and maintains dependent variables (generator reactive power, load bus voltage and network line flow) within acceptable ranges [5]. As the OPF problem has many control variables that are not all continuous variables, such as the outputs of VAR that are discrete variables, it is a non-convex, non-linear, multi-modal, and large-scale constrained optimization problem [6]. Therefore, solving it is a challenging task in power system optimization and is of current interest to many power companies.

There are a number of solution approaches in the literature that deals with the OPF problems. One approach involves mathematical techniques that are widely utilized to determine the optimal values of all control variables in power system operation. The mathematical approach, including linear programming [7], nonlinear programming [8], quadratic programming [9], interior point method [10] and Newton-based methods [11], provides the optimal solution of OPF problems; however, several drawbacks of this approach are also inevitable. For example, some of the noticeable shortcomings of existing mathematical approaches include no guarantee of accuracy for the linear program, poor convergence and algorithm complication for the non-linear programming, the sensitivity of initial guess for the Newton-based algorithm, solving complexities aroused for non-linear and quadratic objective functions in the interior point algorithm [12]. In addition, mathematical approaches have issues in finding global optima (i.e., trapping in local optima) and specific objective function restrictions, such as prohibited operating zones, valve point effects and piece-wise quadratic cost function [3, 13]. It is noteworthy that power system operators require a more robust, faster OPF solver to reach an effective decision for the economic operation of a network. Therefore, it becomes important to propose and develop effective optimization algorithms that can address the issues of traditional mathematical or exact approaches.

In recent decades, many evolutionary-based optimization algorithms have been developed to successfully find the optimal solution of complex OPF problems. [5] developed a particle swarm optimization (PSO) algorithm to solve the OPF problem of several objective functions with mild constraints, such as minimization of fuel cost and voltage profile. In [14], an enhanced genetic algorithm (GA) was presented to solve the OPF with continuous (active power output) and discrete (transformer tap setting) control variables. The problem-specific operators were included to boost the efficiency of the algorithm. Teaching-learning based optimization (TLBO) algorithm was applied in [15] to find the optimal solution for OPF problems. An enhanced artificial bee colony (ABC) algorithm based on orthogonal learning was presented in [16]to handle the OPF problem. The performance of the algorithm was boosted by maintaining a balance between the exploration and exploitation search. In [17], a hybrid algorithm based on PSO and gravitational search algorithms was presented. An improved colliding bodies optimization (ICBO) algorithm was developed in [18] to solve the OPF problem and the performance of the ICBO was compared with the CBO and other well-known approaches. A modified Sine-Cosine technique with a Lévy flight was integrated to improve the exploration of the algorithm [19]. In [20], a moth swarm algorithm to solve the OPF problem was presented, where an adaptive crossover with mutation scaled by Lévy flights was used for maintaining solutions diversity. An enhanced social spider

optimization algorithm was developed in [21] to individually optimize fuel cost, voltage deviation, power loss and polluted emission. The algorithm was improved by adding three modifications: changing the movement strategy of male and female spiders, and fixing the female spider rate. A hybrid approach of moth swarm algorithm and gravitational search algorithm was developed in [22] to efficiently solve the OPF problem. A black hole algorithm was used in [15] to solve the OPF problem. Despite some success, there are still a number of shortcomings in these approaches, such as the problem formulations in unconstrained optimization that may lead to violation of constraints, in addition to the improving performance of algorithms for solving the problem with the intermittent nature of renewable energy sources.

The differential evolutionary (DE) algorithm developed by [23] has good convergence, robustness and the ability to obtain the global optimal. Consequently, DE has achieved better results in solving benchmark problems as compared to other algorithms and it has been applied in many fields to solve complex problems [24]. DE and DE variants (success-history based adaptive DE) are also successfully applied in the power systems to solve the complex problem of OPF. In [25], a parallel DE algorithm was presented that uses small-population for solving short-term hydro-thermal scheduling problem with power flow constraints. A DE algorithm to solve OPF problem was employed in [26], who also evaluated the performance of proper constraint handling techniques —self-adaptive penalty (SP), the superiority of feasibly solutions and an ensemble of these two constraint handling techniques. In [27], the grey wolf optimizer (GWO) and DE algorithms were developed to find the optimal solution of the OPF problem. Hybrid DE and harmony search (HS) algorithms were developed in [28] who replaced operation of the evolution algorithm by a pitch adjustment operation and then a harmony algorithm was used to improve the global convergence. An enhanced adaptive DE algorithm that considers SP constraint handling technique was also developed in [12] to determine the near-optimal solution of the OPF problem. The performance of the algorithm was enhanced using four operators: crossover rate (Cr) sorting mechanism, re-randomizing Cr and scale factor (F), dynamic population reduction strategy, and SP constraint linear technique.

Although several optimization algorithms and DE algorithms have been introduced to find the optimal or near-optimal solution of optimization problems, especially OPF problems in the literature, no single evolutionary algorithm (EA) or search operator has consistently been the best solution to all of the problems [29, 30, 31]. As a result, many researchers and practitioners proposed several innovations that use multiple EAs in a single algorithmic system, called multi-methods or multi-operators, to satisfy this constraint [32, 33, 29]. Nevertheless, there is still scope for progress in their efficiency by developing an effective algorithm for a better, faster and reliable solution of the complex problem. This encourages us to develop an effective advanced multi-operator DE variant, called MODE-OPF, that uses many DE mutation operators in a single algorithmic system to solve OPF. In order to emphasize the most effective DE mutation strategy during the optimization process, an adaptive method (AM) process that uses both the diversity of the population and the quality of solutions has been proposed. We design this AM in a way that is capable of managing the diversification and intensification properties throughout the optimization process. Additionally, instead of considering all constraints to calculate the constraints violation, MODE-OPF starts with a number of them and then gradually increases the number of constraints until satisfying all of them.

MODE-OPF starts with a random initial population of NP solutions. Then, the fitness function value and the total constraint violation of each individual is computed with the number of current objective function evaluation. The whole population is evolved by a number of DE mutation strategies, (i.e., each DE operator produces equal number of new solutions). The diversity for the solutions generated by each DE operators and the quality of solutions are computed and recorded. Based on these two criteria and at the end of each iteration, the number of solutions evolved by each DE operator

are updated as described in Subsection 3.2, with a minimum number of solutions are preserved. This process lasts until the maximum number of fitness evaluation exhausted. Five different objective functions (consequently referred as cases) are considered to demonstrate the efficacy of the proposed MODE-OPF approach. Numerous experiments are performed for modified IEEE 30-bus system and IEEE 118-bus system. The efficacy of this proposed approach is validated by a rigorous comparison against different state-of-the-art algorithms for those IEEE bus systems.

The major contributions of this paper are as follows:

1. A multi-operator DE (MODE) has been proposed in order to solve the optimal power flow (OPF) optimization problems.
2. An adaptive method (AM) has been developed, based on both the diversity of the solutions generated by each DE operators and the quality of solutions. This AM favors diversity at the early stages and quality at the later stages of the evolutionary process. Based on this AM the number of solutions evolved by each DE operator is updated.
3. This paper employs a unique way of handling constraints different from conventional ones to improve its performance, i.e., the proposed approach starts with a subset of the constraints to satisfy, and then gradually adds another subset until all constraints are satisfied.
4. To demonstrate the effectiveness of the algorithm proposed, a modified IEEE 30-bus and an IEEE 118-bus networks are used, where intermittent wind and solar power generation are modeled to the problem formulation using different probability distribution functions.

The rest of the paper is organized as follows. Section 2 introduces the OPF mathematical formulation. The proposed algorithm and its components are given in Section 3. Section 4 introduces the experimental results and comparison with rival algorithms. Conclusions and some future works are presented in Section 5.

2. Mathematical model and constraints of OPF

The target of the OPF problem is to operate a power system effectively and efficiently by optimizing control variables by considering either one or multiple objective functions after maintaining physical and thermal limits of the network. Mathematically, the OPF problem can be formulated as a non-linear constrained optimization problem as follows:

Minimize $F(x, u)$

Subject to $g(x, u) \leq 0$

and $h(x, u) = 0$

where u is a vector of independent or control variables; x is a vector of dependent or state variables; $F(x, u)$ is the objective function; $g(x, u)$ is the inequality constraints and $h(x, u)$ is the equality constraints. The control variables, u, and the state variables, x, in power system are defined in the following subsection.

2.1. Control variables

There is a set of variables that are adjusted by conducting an optimization algorithm to achieve optimal operation of the power system, termed as control or independent variables. They are optimally set by solving the OPF problem using optimization algorithms in order to maintain a reliable, secure and economic power supply to consumers. In our study, eleven control variables are considered to optimally

solve the OPF problems for improving the network's performance with minimum operational cost. The control variables include the power settings of all the generators (except the swing generator) and the bus voltages of all the generators. Without losing generality, this paper uses fixed tap settings of all transformers at 1 p.u to create the same facility of analysis with the existing literature [12, 26, 34, 35]. The set of control variables can be expressed as follows:

$$u^T = [P_{G_2} \; ... \; P_{G_{NG}}, V_{G_1} \; ... \; V_{G_{NG}}]$$

where NG is the number of generators; P_G is the active power generation, including solar and wind generators, at PV buses (except the slack bus); V_G is the voltage magnitude of generators at PV buses, including solar and wind generators.

2.2. State variables

The state variables are the set of variables that represent the unique state of a power system. The state variables are dependent on the control variables. Mathematically, the state variables can be expressed in vector form as follows:

$$x^T = [P_{G_1}, V_{L_1} \; ... \; V_{L_{NL}}, Q_{G_1} \; ... \; Q_{G_{NG}}, S_{l_1} \; ... \; S_{l_{nl}}]$$

where P_{G_1} is the active power at the slack bus; V_L is the voltage magnitude at PQ buses (load buses); Q_G is the reactive power generation of generating units and S_l is the transmission line loadings (or line flow). NL, NG and nl are the number of load buses, the number of generators and the number of transmission lines, respectively.

2.3. Objective functions

The target of the optimization problem is to solve a chosen function while maintaining the thermal and physical constraints of a power system. In this study, we have minimized five single objective functions to demonstrate the performance of the proposed EA. Minimizing each objective function has its own purposes to optimize parameters, as illustrated in Figure 1. The mathematical problem formulations of objective functions are provided in the following subsection.

2.3.1. Case 1: Operating cost

The operating cost of generators generally depends on running cost (i.e., the fuel cost of thermal generators), but in the case of wind and solar generators, there is virtually no operating cost, except some of the factors that need to be considered for reducing the payback period. It is well-known that renewable powers are intermittent in nature, leading to complexity to fulfil the power supply committed. The deficit in total output power must be compensated by a spinning reserve. The problem formulations of operating costs are presented below.

Thermal Generators: Achieving the minimum operating cost of generating units is the main goal of economic power dispatch problem. Each generating unit has its own operating cost represented by a quadratic function. The cost function of generators in terms of cost per hour ($/h) for generating power (in MW) can be expressed as follows:

$$F = \sum_{i=1}^{NG} [a_i + b_i P_{Gi} + c_i P_{Gi}^2] \tag{1}$$

where a_i, b_i and c_i are the cost coefficients of the ith generating unit.
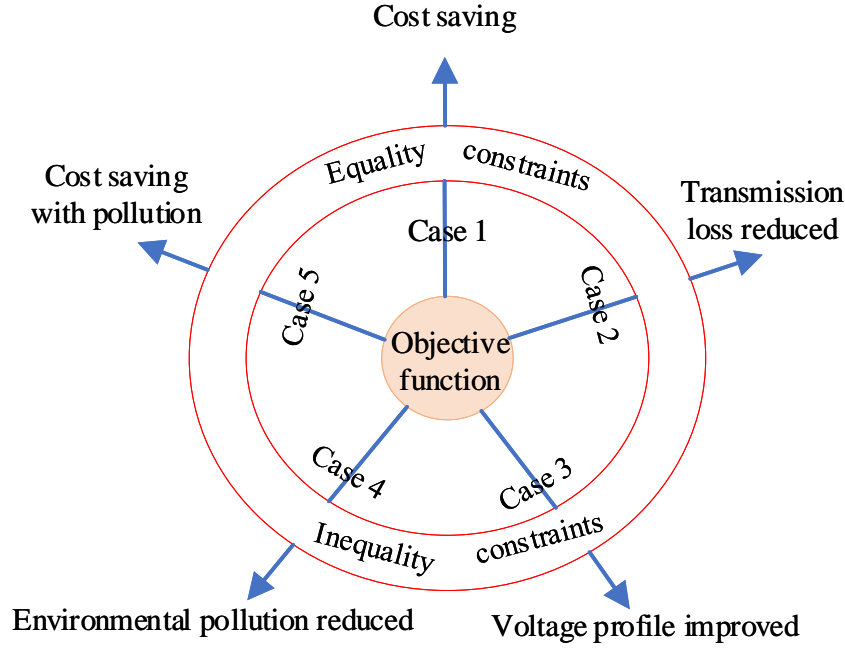
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Figure 1: Objective functions of OPF problems.

For realistic and precise modeling of fuel cost, the valve-point effect (a ripple like effect on fuel cost as shown in Figure 2) of generating units need to be included in the cost function. This signifies the fuel cost of the units is not continuous but non-linear. The incremental fuel cost of the generation units with value-point loading is represented as follows [12]:

$$F_C = \sum_{i=1}^{NG} [a_i + b_i P_{Gi} + c_i P_{Gi}^2 + |d_i \times \sin(e_i \times (P_{Gi}^{\min} - P_{Gi}))| \,]$$

(2)

where d_i and e_i are the coefficients that represent the valve-point loading effect.
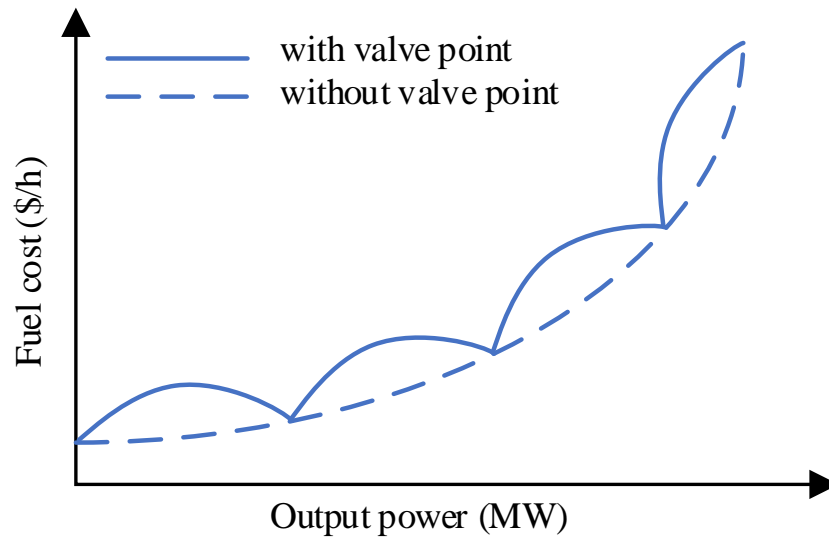
Figure 2: Objective function for a single generator with valve-point effect.

Wind generators: Although the operating cost of a wind generator can be considered to be zero,

maintenance and renewal cost of wind power can be expressed as follows:

$$C_{WT} = c_{wt} \times P_{WT} \tag{3}$$

where P_{WT} is the scheduled power committed to supply the network and c_{wt} is the cost coefficient of wind generators.

As power generation from wind farm is intermittent, it may not supply the power committed (i.e., overestimated power supply). Therefore, the cost of extra power supply from spinning reserve can be applied as follows: [34]:

$$C_{RWT} = c_{rwt} \int_0^{P_{WT}} (P_{WT} - p_w) f_w(p_w) dp_w \tag{4}$$

where c_{rwt} and p_w are the reserve cost for overestimating wind power and available wind power at that time. P_{WT} is the scheduled wind power and $f_w(p_w)$ is the probability density function.

If available power generation is higher than the scheduled power committed, then extra power is generally wasted– called the underestimate amount. This causes delay in the payback period; therefore, a penalty is imposed on underestimate amount as follows:

$$C_{PWT} = c_{pwt} \int_{P_{WT}}^{P_{WR}} (p_w - P_{WT}) f_w(p_w) dp_w \tag{5}$$

where c_{pwt} and P_{WR} are the penalty cost for underestimating wind power generation and the rated wind power output.

The power output of wind generators can be expressed in terms of wind speed as follows [36]:

$$p_w = \begin{cases} 0 & \text{if } v_f < v \ \text{ or } \ v < v_c \\ P_{RWT} \left(\frac{v^3 - v_c^3}{v_r^3 - v_c^3} \right) & \text{if } v_c \le v \le v_r \\ P_{RWT} & \text{if } v_r < v \le v_f \end{cases} \tag{6}$$

where v_r is the rated wind speed, 16 m/s; v_c refers to cut-in wind speed, 3 m/s; v_f is the cut-off wind speed (25 m/s), and v represents wind speed.

As the output power of wind generators are a mixture of discrete and continuous, its probability can be calculated as follows [35]:

$$f_w(p_w = 0) = 1 - e^{-\left(\frac{v_c}{\alpha}\right)^\beta} + e^{-\left(\frac{v_f}{\alpha}\right)^\beta} \tag{7}$$

$$f_w(p_w = P_{WR}) = e^{-\left(\frac{v_r}{\alpha}\right)^\beta} + e^{-\left(\frac{v_f}{\alpha}\right)^\beta} \tag{8}$$

$$f_w(p_w) = \frac{\beta(v_r - v_c)}{\alpha \beta P_{WR}} \left[v_c + \frac{p_w}{P_{WR}}(v_r - v_c) \right]^{\beta-1} e^{-\left(\frac{v_c + \frac{p_w}{P_{WR}}(v_r - v_c)}{\alpha} \right)^\beta} \tag{9}$$

where v_c, v_f and v_r are the cut-in, cut-out and rated wind speed, respectively.

As wind speed distribution can be represented by Weibull probability density function (PDF), the probability of wind speed v m/s can be written as follows [37]:

$$f_v = \left(\frac{\beta}{\alpha} \right) \left(\frac{v}{\alpha} \right)^{\beta-1} e^{-(v/\alpha)^\beta} \tag{10}$$

where α is the Weibull scale parameter of PDF and β is the Weibull shape parameter of PDF. Figure 3 and 4 represent the Weibull fitting and wind speed probability distribution by generating 8000 Monte-Carlo scenarios. The β of Weibull shape is 2 for the both wind speed distributions, and α is 9 for wind speed of windfarm 1 and 10 for wind speed of windfarm 2.

Solar generators: The cost of solar power generation (C_{PS}) for maintenance, renewal and payback period can be determined by the following equation [38]:

$$C_{PS} = c_{sc} \times P_{PS} \tag{11}$$

where c_{sc} and P_{PS} are the solar cost coefficient and the scheduled power generation, respectively. For the overestimate of solar power generation, the reserve cost (C_{rs}) can be incorporated as follows [38]:

$$C_{RS} = c_{rs} * f_s(p_s < P_{PS}) * [P_{PS} - E(p_s < P_{PS})] \tag{12}$$

where c_{rs}, p_s, $f_s(p_s < P_{PS})$ and $E(p_s < P_{PS})$ are the reserve cost coefficient of overestimation, the available solar power generation, the probability of power shortage from scheduled generation, and the expectation of solar power generation, respectively.

The underestimate of the solar power generation, leading to power wastage, should be penalized and therefore it (C_{PS}) can be formulated as follows:

$$C_{PS} = c_{ps} * f_s(p_s > P_{PS}) * [E(p_s > P_{PS}) - P_{PS}] \tag{13}$$

where c_{ps}, $f_s(p_s > P_{PS})$ and $E(p_s > P_{PS})$ are the penalty cost coefficient of underestimate in solar power generation, the probability of power generation exceeded from scheduled, and the expectation of the power higher than P_{PS}, respectively.

The probability of solar irradiance (G_s) can be represented by the Lognormal PDF with mean, μ, and standard deviation, σ, as follows [39]:

$$f_G = \frac{1}{G_s \sigma \sqrt{2\pi}} e^{\left\{ \frac{-(ln\ G_s - \mu)^2}{2\sigma^2} \right\}} \quad \text{if} \quad G_s > 0 \tag{14}$$

Figure 5 demonstrates solar irradiation probability distribution and Lognormal fitting by applying 8000 scenarios of Monte Carlo simulation. For the Lognormal fitting, we have used $\mu = 5$ and $\sigma = 0.6$. Power generation from solar irradiation can be written as follows [40]:

$$p_s = \begin{cases} P_{RS} \left(\frac{G_s^2}{G_{sd} R_c} \right) & \text{if} \ \ 0 < G_s < R_c \\ P_{RS} \left(\frac{G_s}{G_{sd}} \right) & \text{otherwise} \end{cases} \tag{15}$$

where G_{sd} and R_c are the solar irradiance at standard value (1000 W/m^2), and a certain irradiance point set (120 W/m^2), respectively. P_{RS} is the rated solar power generation.

Please note that the reserve cost of wind turbines and solar generators are different from one another due to their level of uncertainty involvement, government promotion on specific power generation and their individual payback period considered.

2.3.2. Case 2: Real power loss

As power flows through the transmission line, there is power loss during power transfer from generating stations to substations due to the existence of resistance across the line. The real power loss
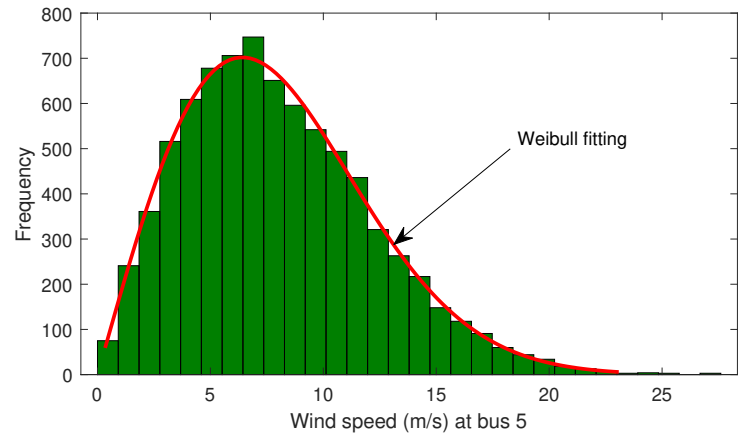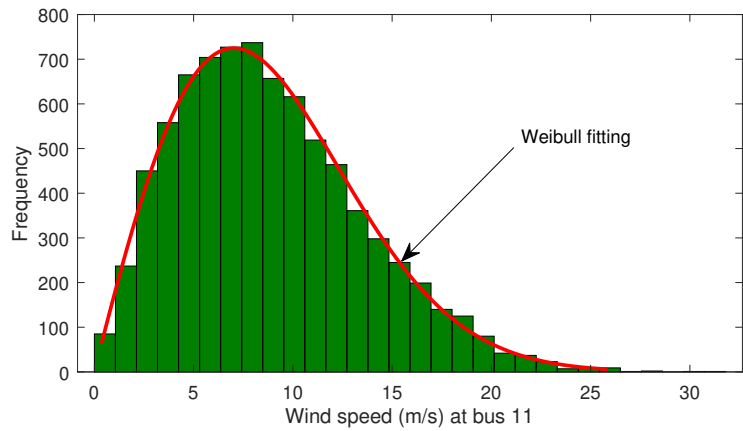
Figure 3: Wind power distribution at bus 5

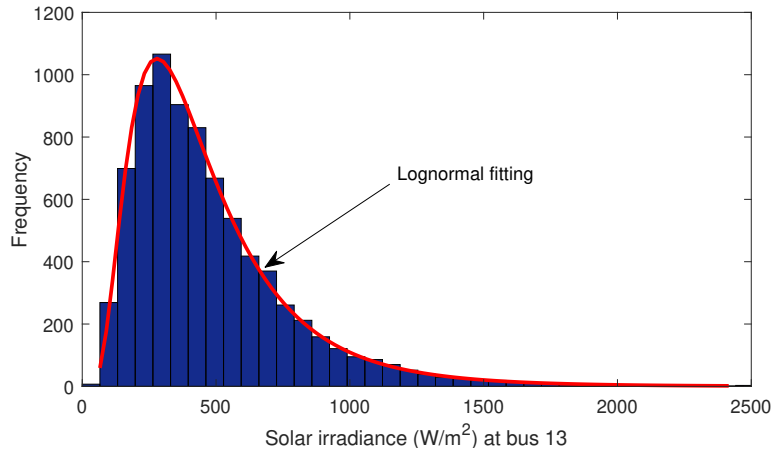Figure 4: Wind power distribution at bus 11

Figure 5: Solar irradiance distribution at bus 13

(in MW) can be reduced by formulating a cost function as follows:

$$F_{loss} = \sum_{i=1}^{nl} \sum_{j \neq i}^{nl} G_{ij}[V_i^2 + V_j^2 - 2V_iV_j\cos(\delta_i - \delta_j)] \tag{16}$$

where G_{ij} is the conductance of a branch between i and j buses; δ_i and δ_j are the voltage angle at bus i and j, respectively; V_i and V_j are the voltage magnitude at buses i and j, respectively.

2.3.3. Case 3: Voltage deviation

The voltage profile of a network can be improved by defining an objective function in terms of voltage deviation at load buses. It is essential to maintain a voltage profile within predefined acceptable ranges to uphold the stability and security of the power system. The voltage profile deviation is expressed as the cumulative deviation of voltages of all the load buses from the reference voltage, 1 p.u. Therefore, the objective function for minimizing voltage deviation (F_{VD}) can be expressed as follows:

$$F_{VD} = \sum_{i=1}^{NL} |V_{Li} - V_{\text{ref}}| \tag{17}$$

where V_{ref} is the reference voltage that is preferable to maintained at the network.

2.3.4. Case 4: Emission control

As conventional power generating units emit harmful and greenhouse gases, such as SO_x, NO_x and CO_2, into the environment, there is a recent trend to impose a penalty for minimizing gas emission. The minimization of these gas in terms of tonnes per hour (t/h) can be described by the following objective function:

$$F_E = \sum_{i=1}^{NG} \left[\alpha_i + \beta_i P_{Gi} + \gamma_i P_{Gi}^2 + \omega_i e^{\mu_i P_{Gi}}\right] \tag{18}$$

where α_i, β_i, γ_i and ω_i are the emission coefficients corresponding to the ith generator.

2.3.5. Case 5: Operating cost with emission

It is sometimes important to consider both the operating cost and greenhouse gas emission control simultaneously to promote renewable energy usages and fulfil the requirement of operating a generating station. Therefore, power generating cost and carbon emission cost are combined in this objective function. The cost function can be defined as follows:

$$F_{CE} = F_C + C_t.F_E \tag{19}$$

where C_t represents the carbon tax and it is considered 20 ($/h) [38].

2.4. Constraints

While minimizing the objective function of the OPF problem, it is essential to fulfill the equality and inequality constraints to reliably and securely operate a power system. The constraints of the OPF problem are described in the following subsection.

2.4.1. Equality constraints

The total power generation should be equal to the total power demand of the network considering power losses in the transmission, otherwise, an unbalanced situation will create, leading to unstable in the power system. The equality constraints embody the non-linear power flow equations as follows:

(a) Real power constraints

$$P_{G_i} - P_{D_i} - V_i \sum_{j=i}^{NB} V_j [G_{ij}\cos(\theta_{ij}) + B_{ij}\sin(\theta_{ij})] = 0 \tag{20}$$

(b) Reactive power constraints

$$Q_{G_i} - Q_{D_i} - V_i \sum_{j=i}^{NB} V_j [G_{ij}\sin(\theta_{ij}) - B_{ij}\cos(\theta_{ij})] = 0 \tag{21}$$

where $\theta_{ij} = \theta_i - \theta_j$, P_D is the active power demand, Q_D is the reactive power demand, NB is the number of buses, G_{ij} and B_{ij} are the conductance and susceptance between buses i and j, respectively.

2.4.2. Inequality constraints

There are a number of inequality constraints that reflect the physical limits of the power system and system operation. These are expressed mathematically below.

(a) Generator constraints

All the voltage, active power and reactive power of generators should be restricted by their upper and lower limits as follows:

$$V_{G_i}^{\min} \le V_{G_i} \le V_{G_i}^{\max}, \qquad i = 1, 2, ..., NG \tag{22}$$

$$P_{G_i}^{\min} \le P_{G_i} \le P_{G_i}^{\max}, \qquad i = 1, 2, ..., NG \tag{23}$$

$$Q_{G_i}^{\min} \le Q_{G_i} \le Q_{G_i}^{\max}, \qquad i = 1, 2, ..., NG \tag{24}$$

where $V_{G_i}^{\min}$ and $V_{G_i}^{\max}$ are the minimum and maximum generation voltage of the ith generating units, respectively; $P_{G_i}^{\min}$ and $P_{G_i}^{\max}$ are the minimum and maximum active power output of the ith generating units, respectively; and $Q_{G_i}^{\min}$ and $Q_{G_i}^{\max}$ are the minimum and maximum reactive power output of the ith generating unit, respectively. It should be noted that $i = 3$ and $i = 5$ are the limits of wind power generators and $i = 6$ solar generators. As the OPF problem is solved in a real-time power dispatch mode, these limits become the same with the thermal generators. In practice, these limits vary in every hour as power generation from renewable energy sources are intermittent and these can be calculated using probability distribution function. Although rooftop solar panels are not generally prepared for reactive power supply, solar and wind power generators in utility-scale have the capability to supply reactive powers into the grid [41, 42].

(b) Security constraints

The security constraints include voltage magnitudes at load buses and transmission line flow. The operational limits of these components must be fulfilled by their upper and lower limits as follows:

$$V_{L_i}^{\min} \le V_{L_i} \le V_{L_i}^{\max}, \qquad i = 1, 2, ..., NL \tag{25}$$

$$S_{l_i} \le S_{l_i}^{\max}, \qquad i = 1, 2, ..., nl \tag{26}$$

where $V_{L_i}^{\min}$ and $V_{L_i}^{\max}$ define the minimum and maximum load voltages of the ith unit; S_{l_i} is the apparent power flow limit of the ith branch.

3. Proposed Algorithm

As previously mentioned, the DE algorithm,s performance may change during the evolutionary stages; i.e. one DE operator can do better in the early stages of optimization process, then get poorer in subsequent stages or vice versa [32, 30, 29]. Also, according to the free-lunch theorem, a single DE operator can perform well for some problems, but it can perform poorly for others. Moreover, balancing the diversification and intensification during the optimization process is crucial in designing optimization algorithms [43]. Thus, there is a great need to design multi-operator and multi-method-based algorithms, in which a selection strategy should be used to emphasize the better operator at each optimization stage and managing the balance between the exploration and exploitation. This paper proposes a multi-operator DE (MODE) optimization algorithm to solve the OPF problem, while its main steps are presented in Algorithm 1 and shown in Figure 6.

The proposed MODE-OPF starts with a random initial population of size NP solutions (i.e., x and u are generated). Then, the objective function value ($F(x, u)$) and total constrained violation ($\psi(x, u)$) for each candidate solution is computed. Initially, each DE operator is used to guide the same number of solutions PS_{op} towards the optimal solution, i.e., new individuals are produced by its assigned DE mutation strategy. The objective function value and constraint violations for the newly generated populations are computed. Then, a pairwise comparison between each parent's solution and its corresponding offspring's solution is conducted (discussed in Subsection 3.4), with the winner survives and enters the new generation. Subsequently, at the end of each generation, the improvement rate value is computed (discussed in Subsection 3.2), based on which, the number of individuals that evolved by every DE mutation strategy is updated. A minimum number of individuals evolved by each DE mutation strategy was set. Indeed, at the end of each generation, a linear population size reduction (LPSR) mechanism is used by deletin the worst individual from the population [44, 43], as in Equation 27. This is done to maintain the population's diversity at the early iterations and enhancing the algorithm's convergence in the later ones.

$$NP_{t+1} = round[(\frac{NP_{min} - NP_{init}}{MAX_{FES}}) \times FES + NP_{init}] \tag{27}$$

where NP_{init} is the initial population size, NP_{min} the minimum number of solutions the solver can use, FES the current number of function evaluated (FES) and MAX_{FES} the largest number of FES.

The following subsections provide detail information about the components of the proposed MODE-OPF.

3.1. DE mutation strategies

MODE-OPF uses the following DE mutation strategies to evolve the whole population as they perform well in solving unconstrained and constrained optimization problems [33, 45, 31].

- DE/rand-to-ϕbest/1/bin with archive

$$u_{i,j} = \begin{cases} x_{r1,j} + FF_i.(x_{\phi,j} - x_{r1,j} + x_{r2,j} - x_{r3,j}) \\ \qquad \text{if } (rand \leq Cr_i \text{ or } j = j_{rand}) \\ x_{i,j} \qquad\qquad\qquad \text{otherwise} \end{cases} \tag{28}$$

- DE/current-to-ϕbest/1/bin with archive

$$u_{i,j} = \begin{cases} x_{i,j} + FF_i.(x_{\phi,j} - x_{i,j} + x_{r1,j} - x_{r3,j}) \\ \qquad \text{if } (rand \leq Cr_i \text{ or } j = j_{rand}) \\ x_{i,j} \qquad\qquad\qquad \text{otherwise} \end{cases} \tag{29}$$

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Start

Define input parameters, $n_{op}, NP, FES_{MAX}, t, FES$

Generate an initial population of size NP, with the variables of each solution must be within the boundaries.

Compute objective function value and constraint violations of each solution, and update number of fitness evaluations (*FES*)

$FES \leq FES_{MAX}$

No

Update the values of *F* and *Cr* as in Section 3.3

Distribute population randomly over , $Y_{op}, \forall op = 1, 2, ..., n_{op}$ where Y_{op} each is of size PS_{op} as discussed in Section 3.2

Op1 evolves Y1 | *Op2 evolves Y2* | ··· | $Op_{n_{op}}$ *evolves* $Y_{n_{op}}$

Evaluate fitness function values and calculate the constraint violations of the new generated population;

Compute the improvement index value (IIVop) and update the number of individuals evolved by each operator as discussed in Section 3.2

Update *FES, FES←FES+NP* and Update *NP* (equation 16)

Yes

Stop

Figure 6: Flowchart of the proposed MODE-OPF

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Algorithm 1 MODE-OPF algorithm

1: **Define** nop, MAX_{FES}, NP, $t \leftarrow 1$ and $FES \leftarrow 0$;
2: Generate an initial random population (Y) of size NP, with the variables of each solution must be within their boundaries;
3: Evaluate $F(X, u)$ and calculate the constraints violations $(\psi(x, u))$;
4: Update number of fitness evaluations $FES \leftarrow FES + NP$;
5: Divide Y into n_{op} sub-populations, each with size (PS_{op})
6: **while** $FES \leq MAX_{FES}$ **do**
7:     Distribute Y randomly over $Y_{op}, \forall op = 1, 2, ..., n_{op}$, where each Y_{op} is of size PS_{op};
8:     Generate new population using the assigned DE operators, i.e., each operator op evolves its assigned number of individuals NP_{op};
9:     **for** $op = 1 : n_{op}$ **do**
10:         Generate new solutions using the op^{th} DE operators;
11:         Evaluate fitness function values and calculate the constraint violations of the new generated population;
12:         Compute the improvement index value (IIV_{op}) and update the number of individuals evolved by each operator as discussed in Section 3.2;
13:         Update the values of FF and Cr as in Section 3.3;
14:     **end for**
15:     Update FES, $FES \leftarrow FES + NP$;
16:     Update NP (equation 27);
17:     $t \leftarrow t + 1$; and go to **step 6**;
18: **end while**

- DE weighted-rand-to-ϕbest

$$u_{i,j} = \begin{cases} FF \times x_{r_1,j} + (x_{\phi,j} - x_{r_2,j}) \\ \qquad \text{if } (rand \leq Cr_i \text{ or } j = j_{rand}) \\ x_{i,j} \qquad\qquad\qquad \text{otherwise} \end{cases} \tag{30}$$

where $r_1 \neq r_2 \neq r_3 \neq i$ are integers numbers randomly generated, $\overrightarrow{x}_{r1}$ and $\overrightarrow{x}_{r2}$ randomly picked up from the entire population, with $x_{\phi,j}$ drawn up from the best 10% of individuals in the entire population and $\overrightarrow{x}_{r3}$ from the union of the whole population and archive. An archive to maintain the population's diversity, is used. New candidates that are worse than their parent ones kept in the archive [46]. To make space for the newly generated individuals, once the archive size is greater than its default size, the worst individuals are removed from it.

Note that the proposed framework is flexible to adopt more operators.

3.2. Updating number of solutions evolved by operator op (NP_{op})

As we previously mentioned, the solutions' quality and sub-population's diversity are used to update the number of individuals evolved by each DE mutation operator. Consequently, this method is referred as adaptive method (AM). For the solutions' quality, the best individual at the end of each iteration (t) that is found by each DE operator is used to calculate the normalized quality $(Qual_{op})$ for operator op as

$$Qual_{op} = \frac{F_{t,op}^{best}}{\sum_{op=1}^{n_{op}} F_{t,op}^{best}}, \forall op = 1, 2, ..., n_{op} \tag{31}$$

where $F_{t,op}^{best}$ is the best objective function value obtained by DE operator op at generation t. Note, as we deal with constrained optimization problem, $F_{t,op}^{best}$ is determined based on both the fitness function values and the total constraint violations. This is done by sorting the solutions based on both fitness function values and total constraint violations [47].

Similarly, for the diversity obtained from each DE search operator (Div_{op}) which is the mean deviation of each solution obtained from op of the best solution computed as

$$Div_{op} = \frac{1}{NP_{op}} \left(\sum_{i=1}^{NP_{op}} dis(\overrightarrow{U}_{op,i} - \overrightarrow{U}_{op}^{best}) \right), \forall op = 1, 2, ..., n_{op} \tag{32}$$

where $dis(\overrightarrow{U}_{op,i} - \overrightarrow{U}_{op}^{best})$ is the Euclidean distance between the ith solution and best one obtained by each operator op. Also the diversity index is calculated by:

$$DI_{op} = \frac{Div_{op}}{\sum_{op=1}^{n_{op}} Div_{op}}, \forall op = 1, 2, ..., n_{op} \tag{33}$$

Based on the above equations, the improvement index value (IIV_{op}) is calculated as:

$$IIV_{op} = (1 - c) \times (1 - Qual_{op}) + c \times DI_{op}, \forall op = 1, 2, ..., n_{op} \tag{34}$$

Note: to satisfy the aim of maximizing the IIV_{op}, we subtracted $Qual_{op}$ from 1. In this paper, in order to put more weight on the DE operator that generate more diverse population at the early stages of the optimization process, while focus on the one that has a faster convergence at the later stages, the parameter c is defined in Equation 35.

$$c = 1 - \frac{FES}{MAX_{FES}} \tag{35}$$

Finally, the number of individuals that each DE mutation strategy (NP_{op}) evolves is computed by

$$NP_{op} = max \left(0.1, min \left(0.9, \frac{IIV_{op}}{\sum_{op=1}^{n_{op}} IIV_{op}} \right) \right) \times NP, \tag{36}$$
$$\forall op = 1, 2, ..., n_{op}$$

Note: $\sum_{op=1}^{n_{op}} NP_{op} = NP$, i.e., the sum of all individuals evolved by each DE mutation strategy must be equal to the whole population size. Also, as one of the DE operators may differently behave during the different stages of the evolutionary process, i.e., it may perform good at the early stages and behave differently at the the latter stage [29]. Thus, we use a minimum value (0.1) to give a chance of the low-performing operators to be applied.

3.3. Managing FF and Cr

The DE's performance is highly dependent upon its search operators (mutation and crossover) and its control parameters (NP, FF and Cr). However, choosing their values is challenging. Thus, in this paper, a self-adaptive method is used to update the values of FF and Cr [33, 31]. To do this, the following steps are performed:

- A recording memory that has L elements for μFF and μCr is initialized, with the values of all elements are initially set to 0.5.

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- Each individual $\overrightarrow{U}_i$ is associated with its own FF_i and Cr_i values, such that:

$$FF_i = randci(\mu FF_{r_i}, 0.1) \tag{37}$$

$$Cr_i = randni(\mu Cr_{r_i}, 0.1) \tag{38}$$

where r_i is picked randomly from $[1, L]$, randci and randni are values randomly generated by using Cauchy and Normal distributions with variance 0.1, mean μFF and μCr, respectively [44].

- At the end of each iteration t, FF_i and Cr_i used by the successful individuals are saved in SFF and SCr, and then the elements of the recording memory are updated as follows:

$$\mu FF_l = mean_{WL}(SFF) \text{ if } SFF \neq \text{ null} \tag{39}$$

$$\mu Cr_l = mean_{WA}(SCr) \text{ if } SCr \neq \text{ null} \tag{40}$$

where $1 \leq l \leq L$ is the the location in the recording memory to be updated, with its initial value is 1, and then increased whenever a new element is stored into the recording memory, and if its size is larger than L, it is reset to 1. The Lehemer mean $(mean_{WL}(SFF))$ and the weighted mean $(mean_{WA}(SCr))$ are calculated as follows:

$$mean_{WL}(SFF) = \frac{\sum_{\zeta=1}^{|SFF|} \omega_\zeta SFF_\zeta^2}{\sum_{\zeta=1}^{|SFF|} \omega_\zeta SFF_\zeta} \tag{41}$$

$$mean_{WA}(SCr) = \sum_{\zeta=1}^{|SCr|} \omega_\zeta SCr_\zeta \tag{42}$$

where —SFF— and —SCr— are the number of successful FF and Cr saved in SFF and SCr with —SCr—=—SF — and ω_ζ is the weight calculated by:

$$\omega_\zeta = \frac{\gamma_\zeta}{\sum_{\zeta=1}^{|S_{Cr}|} \gamma} \tag{43}$$

The values of γ_ζ are calculated based on the following scenarios:

1. Feasible to feasible: the violation of the best solution equal zero at both generations $t-1$ and t;
2. Infeasible to feasible: at iteration $t-1$, the best candidate solution in the population is infeasible and then it becomes feasible at generation t; and
3. Infeasible to infeasible: the best candidate solution in the population is infeasible in generations $t-1$ and t.

First, for each successful solution $(h \in 1, 2, ..., |S_{Cr}|)$ which falls in scenario (i), its γ_h is calculated as [33, 31]:

$$\gamma_h = \beta_{h=} max\left(0, \frac{\psi_{h,t-1} - \psi_{h,t}}{\psi_{h,t-1}}\right) + max\left(0, \frac{F_{h,t-1} - F_{h,t}}{F_{h,t-1}}\right) \tag{44}$$

Then, for each successful solutions which exists in scenarios 2 or 3, its γ_h is computed as:

$$\gamma_h = max(0, \beta_h) + \frac{\psi_{h,t-1} - \psi_{h,t}}{\psi_{h,t-1}} + max\left(0, \frac{F_{h,t-1} - F_{h,t}}{F_{h,t-1}}\right) \tag{45}$$

3.4. Constraints handling

It is well known that the greater the number of constraints (equality and inequality) exist in any constrained optimization problem, the more complex and complicated will be that problem. One way of dealing with this issue is to use a subset of the constraints to calculate the total constraints violations, and gradually increase this number until the total number of constraints are handled. In this paper, we used the constrained handling technique proposed in [48]. The method starts by sorting all the constraints based on their sum of the constraint violations of all the solutions in the initial population. It begins by ordering the constraints according to the sum of the constraint violations of all the individuals in the initial population from the most violated to least violated constraint or vice versa. Then, instead of using all constraints, the proposed MODE-OPF starts with a small number of them (Con_n) (the ones with the largest total violation) for a predetermined number of iterations (W), then a new subset is appended to the current set, and the method tries to attain the feasible region of both the new and previous subsets of constraints. This process lasts until all the constraints are handled and the final feasible region is reached.

To select between any solution B_{new} and its parent B_{old}, the method developed by Deb [47] is adopted and it has three scenarios:

1. If both B_{old} and B_{new} are feasible and $f(B_{new} < f(B_{old})$, the B_{new} is selected;
2. If both B_{old} and B_{new} are infeasible and $\psi(B_{new}) < \psi(B_{old})$, then B_{new} is chosen, where ψ is computed using Equation 46; and
3. If B_{new} is feasible and B_{old} is infeasible, then B_{new} is preferred.

$$\psi(\overrightarrow{x}_i) = \sum_{k=1}^{K} max(0, g_k(\overrightarrow{x}_i)) + \sum_{e=1}^{E} max(0, |h_e(\overrightarrow{x}_i)| - \delta_e) \tag{46}$$

where $g_k(\overrightarrow{x}_i)$ and $h_e(\overrightarrow{x}_i)$ are the kth inequality and e^{th} equality constraints, respectively. For each equality constraint h_e, δ_e was set to a value of 0.0001 [31].

4. Experimental results and Analysis

In this paper, to test the performance of the proposed MODE-OPF, an updated IEEE 30-bus system has been considered in line to the recent papers published in [12, 39, 49, 38] as depicted in Figure 7. In this modified system, the conventional thermal generators are substituted for wind turbines on bus 5, 11 and the solar generators on bus 13. The intermittent power generation cost for the wind power generators are determined by the combination of scheduling cost, overestimated cost and underestimated cost, represented in Eqs. (3), (4), and (5), respectively. Similarly, the cost of intermittent solar power is estimated by adding the cost involve in scheduling, overestimating and underestimating as represented in Eqs. (11), (12) and (13), respectively. Bus 1 of the network is used as the swing or slack bus that is responsible for maintaining balanced active and reactive power flow in the network while fulfilling equality constraints. As swing bus is considered as a reference bus, its voltage magnitude and angle are 1 p.u. and 0 degree, respectively. All other bus voltages and angles are computed with respect to the swing bus using load flow study. The power flow problem is solved using the Newton-Raphson iterative method under the MATPOWER tool [50]. Table 1 shows the parameters of renewable energy sources and the coefficients of thermal generators are shown in Table 2. Table 4 presents the lower and upper bounds of the control and state variables [38].

We coded and implemented all the algorithms in MATLAB R2018b and ran them on a PC with 16GB RAM, core I7 processor with a 3.4GHz and Windows10. Note that all the rival algorithms are

executed 30 times, with the best, median, average, worst and standard deviation of results reported. Results are recorded with a stopping condition equal to 20000 and 100000 fitness evaluations (i.e., FES_{MAX} equal to 20000 or 100000) for IEEE 30 and IEEE 118 bus systems, respectively. The parameter settings of the competitive algorithms are taken from their original sources. For a fair comparison, the population sizes of all the compared algorithms including the proposed one is set to 50. To test and judge the performance of the proposed MODE-OPF, we carried out a comparison with the following algorithms:

1. A genetic algorithm with multi-parent crossover (GA-MPC) [51];
2. An enhanced JADE algorithm with self-adaptive penalty constraint handling method (EJADE-SP) [12];
3. A DE with an ensemble of constraints handling technique (ECHT-DE) [52];
4. A unified DE for constrained optimization (UDE) [53];
5. An LSHADE with competing strategies for constrained optimization (LSHADE44) [54];
6. A composite DE algorithm for solving constrained optimization problems (COPs) (C^{2}oDE) [55];
7. A feasibility rule with the incorporation of objective function information (FROFI). [56]

We conducted two non-parametric tests (Wilcoxon signed-ranked test with a 0.05 significance and Friedman's ranking test) [57] to statistically compare the rival algorithms. Two algorithms Alg_1 and Alg_2 are compared using the Wilcoxon signed-rank test, with one of the following signs used.

- The "+ " sign that means Alg_1 algorithm is significantly superior to Alg_2;
- The "− " sign that means Alg_1 is significantly inferior to Alg_2; and
- The "≈" sign that means there is no significant difference between Alg_1 and Alg_2.

Table 1: Parameters of solar and wind generation [58]

# of wind-farms	# of turbine	Ratings	Total rated power	Solar power rating
1 (bus 5)	25	3 MW	75 MW	50 MW (bus 13)
2 (bus 11)	20	3 MW	60 MW	

Table 2: Coefficient of thermal power generator

Generators	a($/h)	b($/MWh)	c ($/MW^{2}h)	d($/h)	e (rad/MW)	α (t/h)	β(t/p.u.MWh)	γ(t/p.u.MW^{2}h)	ω(t/h)	μ(p.u.MW^{-1})
P_{G1} (bus-1)	30	2	0.00375	18	0.037	0.04091	-0.05554	0.0649	0.0002	6.667
P_{G2} (bus-2)	25	1.75	0.0175	16	0.038	0.02543	-0.06047	0.05638	0.0005	3.333
P_{G4} (bus-8)	20	3.25	0.00834	12	0.045	0.05326	-0.0355	0.0338	0.002	2

4.1. Effect of number of used DE operators

The proposed MODE-OPF uses more than one DE mutation strategies in a single algorithmic system. Thus, in order to design an effective multi-operator algorithm, it is mandatory to know which combination of single operators is better to be used in the framework [32, 45]. To do this, in this section a comparison is conducted between seven variants of the proposed algorithm. These variants share the same structure and components of the proposed algorithm and they are different only in the number and operators they used. These variants are as follows:

1. Var1: DE/rand-to-ϕbest/1/bin with archive is used to evolve the entire population.
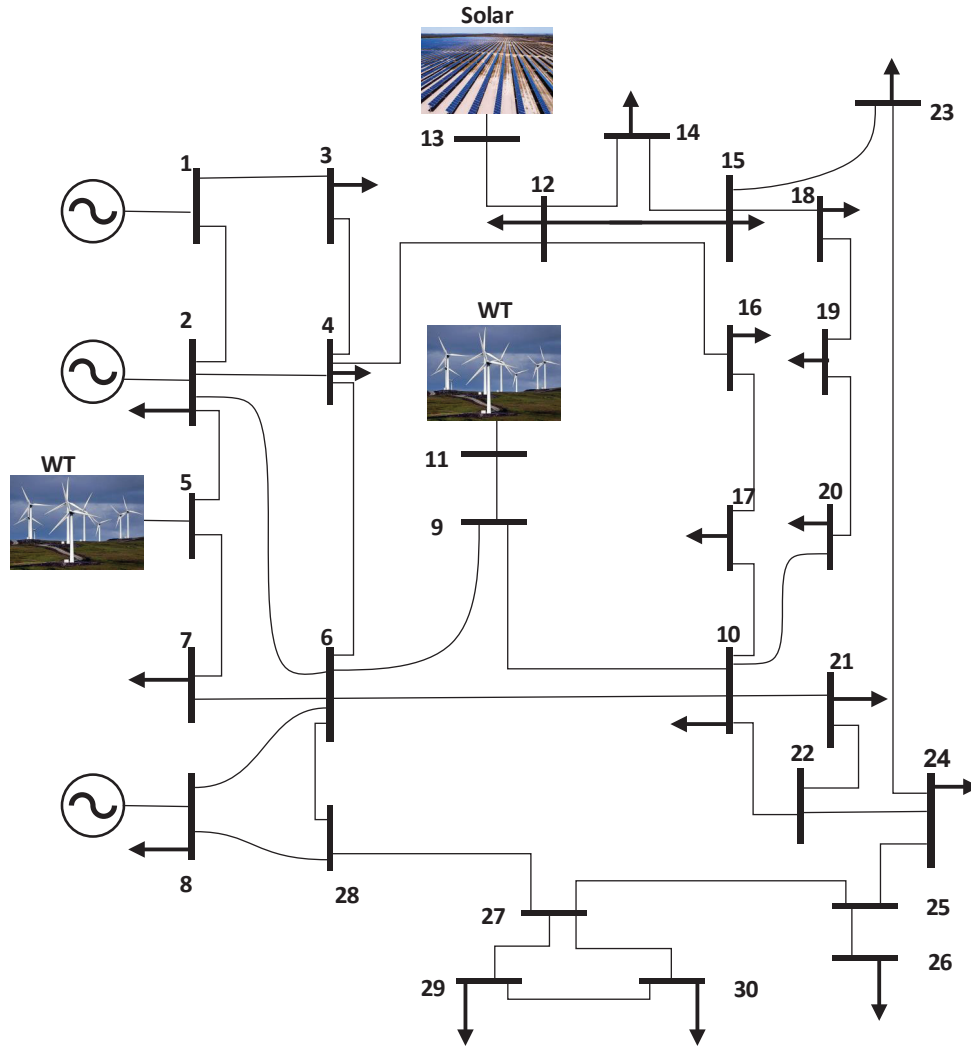2. Var2: DE/current-to-ϕbest/1/bin with archive is used to evolve the entire population.

Figure 7: Diagram of modified IEEE 30-bus test system

Table 3: An overview of IEEE 30-bus system

Items	Quantity	Details
Buses	30	[59]
Branches	41	[59]
Thermal generators	3	Buses: 1 (swing), 2 and 8
Wind generators	2	Buses: 5 and 11
Solar generators	1	Bus: 13
Control variables	11	Active power of five generators except swing bus, and bus voltages of all generators (six)
Connected load	–	283.4 MW, 126.2 MVAr
Load bus voltage allowed	24	[0.95–1.05]

Table 4: The lower and upper bounds of state and control variables of 30-bus system

Control variables	LB	UB	State variables	LB	UB
P_{G_2}	20	80	P_{G_1}	30	140
P_{G_3}	0	75	Q_{G_1}	-20	150
P_{G_4}	10	35	Q_{G_2}	-20	60
P_{G_5}	0	60	Q_{G_3}	-15	40
P_{G_6}	0	50	Q_{G_4}	-30	35
v_1	0.95	1.10	Q_{G_5}	-25	30
v_2	0.95	1.10	Q_{G_6}	-20	25
v_5	0.95	1.10			
v_8	0.95	1.10			
v_{11}	0.95	1.10			
v_{13}	0.95	1.10			

3. Var3: DE/weighted-rand-to-ϕbest/1/bin is used to evolve the entire population.
4. Var4: Both DE/rand-to-ϕbest/1/bin with archive and DE/current-to-ϕbest/1/bin with archive are used to generate new solutions.
5. Var5: Both DE/rand-to-ϕbest/1/bin with archive and DE/weighted-rand-to-ϕbest/1/bin with archive are used to generate new solutions.
6. Var6: Both DE/current-to-ϕbest/1/bin and DE/weighted-rand-to-ϕbest/1/bin with archive are used to generate new solutions.
7. Var7: All three operators (DE/rand-to-ϕbest/1/bin with archive, DE/current-to-ϕbest/1/bin with archive and DE/weighted-rand-to-ϕbest/1/bin) are used to evolve the entire population.

All seven variants are tested and compared against each other by solving the OPF optimization problem with the objective function to minimize the cost of generation (case 1). The parameters values used in these variants and the proposed MODE-OPF algorithm through the paper were set as follows: the maximum number of solutions NP_{init} equal to 50, while the minimum number of individuals NP_{min} equal to 30. The value of ϕ was set to 0.11 for the first two DE operators and 0.5 for the third, the archive rate (A) to 1.4, and the memory size (L) to 5 [29]. The window size, W, was set at a value of 50 [48].

Table 5 presents the summary of the results obtained from the seven variants. From Table 5, it is clear that Var4 obtains the best median, best average and best maximum values of the generation cost, while Var1 archives the best minimum value in comparison to others with a very different value in cost from Var4 (0.0000014).

Table 5: Comparative summary of seven variants for the algorithm proposed on Case 1

Algorithms	Best	Median	Mean	Worst	Std.
Var1	**782.3592750**	782.3755527	782.3683531	782.3759836	0.0080680
Var2	782.3592753	782.3755724	782.3686045	782.3756127	0.0081140
Var3	782.3592852	782.3755351	782.3702135	782.3760232	0.0071990
Var4	782.3592758	**782.3593466**	**782.3653462**	**782.3755806**	0.0082426
Var5	782.3592910	782.3755744	782.3708036	782.3757930	**0.0072119**
Var6	782.3592818	782.3693282	782.3676928	782.3756323	0.0080616
Var7	782.3592764	782.3594074	783.668761	782.3762862	0.0079734

To further statistically compare all seven variants, we carried out a Wilcoxon signed-rank test [36]. The summary of the experimental results obtained from the Wilcoxon signed-rank test is presented in Table 6. It can be concluded from Table 6 that Var4 is statistically better than Var3, Var5 and Var6, while there is no significant difference statistically between Var4 and other variants, although there is a bias in the results towards Var4.

Table 6: Results obtained by the Wilcoxon test for algorithm Var4 on Case 1

Algorithms	R^+	R^-	Exact P-value	Dec.
Var4 vs. Var1	297.0	168.0	0.181242	$\approx$
Var4 vs. Var2	302.0	163.0	0.149929	$\approx$
Var4 vs. Var3	342.0	123.0	0.023665	$+$
Var4 vs. Var5	360.0	105.0	0.00847	$+$
Var4 vs. Var6	363.5	101.5	0.006694	$+$
Var4 vs. Var7	237.0	228.0	0.917878	$\approx$

As a further analysis, Friedman's rank test has been conducted among the seven variants, while the results are depicted in Figure 8. It is seen in Figure 8 that Var4 has the first rank, followed by Var7, then Var1. From the above analysis, it can be concluded that using two DE mutation strategies (Var4: DE/rand-to-ϕbest/1/bin with archive and DE/current-to-ϕbest/1/bin with archive) is better than all other variants based on both Wilcoxon signed-rank and Friedman rank tests.
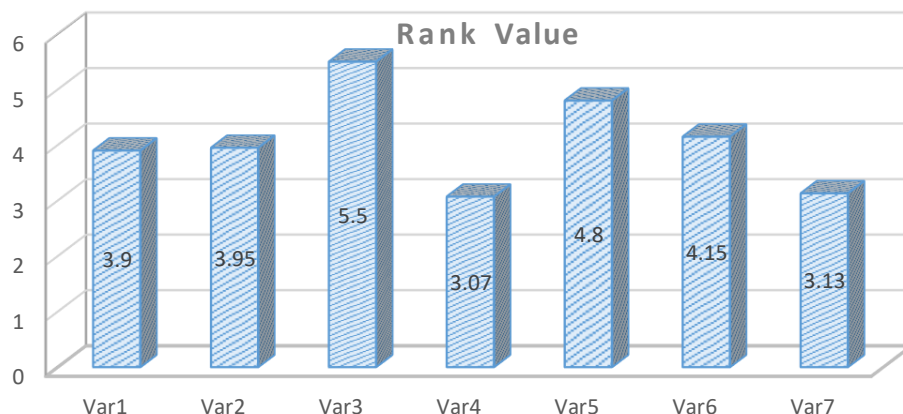
Figure 8: Average ranking achieved by Friedman's ranking test to compare the seven variants on Case 1

4.2. Comparison with the state-of-the-art algorithms for the IEEE 30-bus system

As previously stated, the performance of the proposed MODE-OPF is tested by optimizing five different objective functions of the power flow optimization problems. These five cases are discussed in details by providing their mathematical formulations at Subsection 2.3. In the following subsections, the detailed results obtained from the proposed algorithm along with a comparison with the state-of-the-art algorithms are discussed.

4.2.1. Results of case 1

The objective function at this case is to find the optimal settings of generators for which power generation cost can be minimized (i.e., the operating cost of power generation can be saved). The lower value in solving the objective function represents the minimum operating cost of generating units per hour to run the power system efficiently and effectively. Table 7 presents the summary of comparison for

generation cost obtained from the proposed MODE-OPF and the rival algorithms based on minimum, maximum, median, average and standard deviation of the generation cost. Considering the summary of the fuel cost obtained in Table 7, MODE-OPF is better than EJADE-SP, C²oDE, LSHADE44, UDE, ECHT-DE and FROFI in regards to minimum, median, average and maximum cost generation. Therefore, it can be concluded that the proposed solver has the capability to reduce the total fuel cost by 0.0048%, 2.11%, 1.64%, 24.08%, 2.40% and 4.39% as compared to EJADE-SP, C²oDE, LSHADE44, ECHT-DE, FRORI and GA-MPC, respectively. It can be also observed from Figure 15 that the fuel cost is less as compared to the other cases while other parameters like power losses, voltage deviation and emission are higher as shown in Table 18.

Table 7: Case 1: Comparative summary of the algorithms

Algorithms	Best	Median	Mean	Worst	Std.
GA-MPC	782.4032000	784.8747000	787.9558267	835.9240000	11.1466094
EJADE-SP	782.3593253	782.4638016	782.3716416	782.3751388	0.0190688
C²oDE	782.3804017	782.4352287	782.3987796	782.3969633	0.0136890
LSHADE44	782.3757000	782.7229000	782.4513700	782.3790500	0.1097607
UDE	782.3592753	782.7213908	782.4037119	782.3755732	0.0897619
ECHT-DE	782.6001000	782.8470000	782.6924167	782.6882000	0.0568796
FROFI	782.3833028	782.4983369	782.4169422	782.4159308	0.0239930
MODE-OPF	**782.3592764**	**782.3762862**	**782.3653462**	**782.3594074**	**0.0079734**

Referring to the summary of the results obtained from the Wilcoxon signed-rank test as shown in Table 8, the proposed MODE-OPF is significantly better than all the competing algorithms (EJADE-SP, C²oDE, LSHADE44, UDE, ECHT-DE, FROFI and GA-MPC) with the p-value less than 0.05 in all cases. Meanwhile, Figure 9 demonstrates the Friedman rank test and it is observed that the proposed MODE-OPF was ranked first, followed by EJADE-SP, and then UDE.

Table 8: Case 1: Results obtained by the Wilcoxon test for the algorithm proposed

Algorithms	R^+	R^-	Exact P-value	Dec.
MODE-OPF vs. EJADE-SP	339.0	126.0	0.02774	+
MODE-OPF vs. C²oDE	465.0	0.0	1.8626E-9	+
MODE-OPF vs. LSHADE44	460.0	5.0	1.8626E-8	+
MODE-OPF vs. UDE	351.0	114.0	0.013664	+
MODE-OPF vs. ECHT-DE	465.0	0.0	1.8626E-9	+
MODE-OPF vs. FROFI	465.0	0.0	1.8626E-9	+
MODE-OPF vs. GA-MPC	465.0	0.0	1.8626E-9	+

4.2.2. Results of case 2

The net power obtained by the distribution grid is the difference between the overall power output and transmission power losses. Thus, the minimization of power losses is the best way to increase the performance of the distribution system. As a result, the minimization of power losses is a vital problem in the power systems. In case 2, the proposed MODE-OPF is used to minimize the power loss, which is considered as the fitness function for this case. The summary of the results for minimum, median, average and maximum obtained from the proposed MODE-OPF, EJADE-SP, C²oDE, LSHADE44, UDE, ECHT-DE and FROFI is presented in Table 9. Considering the summary of the statistical results from which it is clear that the proposed MODE-OPF achieved the best average and best maximum
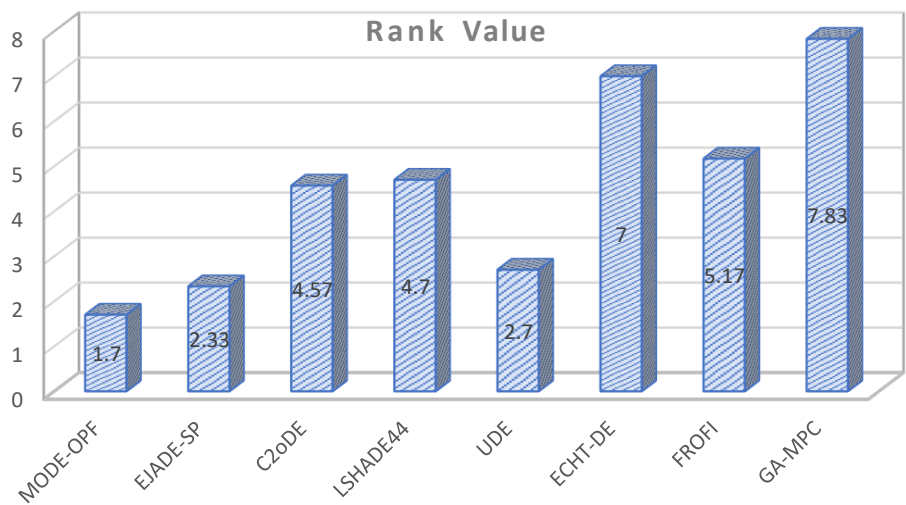
Figure 9: Case 1: Average ranking achieved by Friedman's ranking test
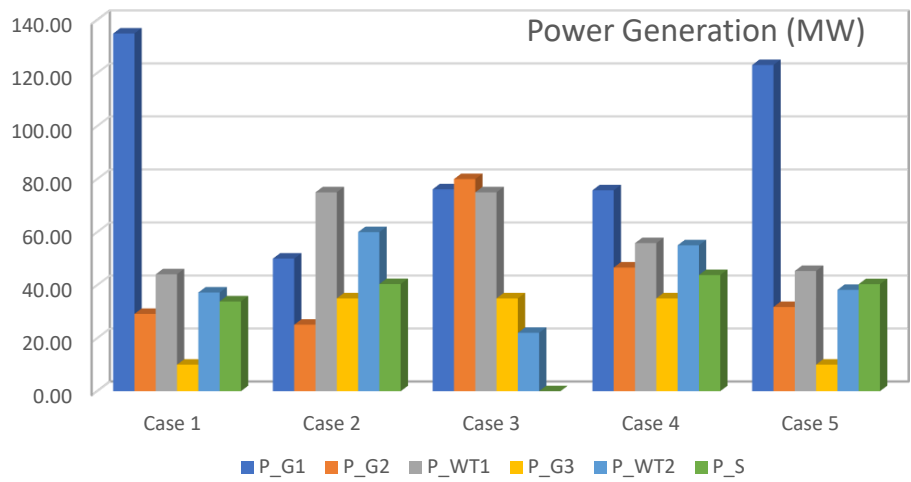
Figure 10: Power generation commands for all the generators

values, while EJADE-SP obtained the best minimum and median values. Therefore, it can be concluded that the proposed solver has the capability to reduce the average of the power loss by 0.98%, 0.16%, 0.63%, 0.13%, 6.80%, 0.25% and 22.13%, as compared to EJADE-SP, C²oDE, LSHADE44, UDE, ECHT-DE, FRORI and GA-MPC, respectively. It can be also observed from Figure 16 that the real power loss is less in this objective function as compared to the other methods while operating cost has increased slightly than Case 1. Power loss has been minimized by reducing thermal power generation and supplying more renewable power at bus 5, 11 and 13, as demonstrated in Figure 10. As higher power is generated from renewable energy sources, leading to less emission as shown in Figure 18, the cumulative voltage deviation has increased.

Table 9: Case 2: Comparative summary of algorithms

Algorithms	Best	Median	Mean	Worst	Std.
GA-MPC	2.1347500	2.2197700	2.2952036	3.5394740	0.3042764
EJADE-SP	**2.073124000**	**2.074089000**	2.083661733	2.103725000	0.014396839
C²oDE	2.074268000	2.074929000	2.075417500	2.081397000	0.001516278
LSHADE44	2.074141000	2.074187500	2.080185800	2.162454000	0.019715889
UDE	2.074121398	2.074121407	2.075107860	2.103714801	0.005402989
ECHT-DE	2.114171000	2.141488500	2.141869033	2.162325000	0.013077309
FROFI	2.074726206	2.075962943	2.076313577	2.078697183	0.001066128
MODE-OPF	2.073235906	2.074121590	**2.073858007**	**2.074127798**	**0.000410967**

Table 10 presents the results of the Wilcoxon signed-rank test, from which it can be seen that MODE-OPF is significantly better than C²oDE, LSHADE44, ECHT-DE, FRORI and GA-MPC with a p-value less than 0.05, while there is no statistical difference with EJADE-SP and UDE. Note the p-value when comparing MODE-OPF with EJADE-SP is 0.061 which is slightly greater than 0.05. For further analysis, Friedman's rank test is conducted to rank the proposed algorithm and the rival algorithms with the result depicted in Figure 11. It is clear from this figure that MODE-OPF and UDE are ranked first, EJADE-SP is ranked second, while GA-MPC is ranked last.

Table 10: Case 2: Results obtained by the Wilcoxon test

Algorithms	R^+	R^-	Exact P-value	Dec.
MODE-OPF vs. EJADE-SP	323.0	142.0	0.06356	$\approx$
MODE-OPF vs. C²oDE	465.0	0.0	1.8626E-9	+
MODE-OPF vs. LSHADE44	465.0	0.0	1.8626E-9	+
MODE-OPF vs. UDE	239.0	226.0	≥ 0.2	$\approx$
MODE-OPF vs. ECHT-DE	465.0	0.0	1.8626E-9	+
MODE-OPF vs. FROFI	465.0	0.0	1.8626E-9	+
MODE-OPF vs.GA-MPC	465.0	0.0	1.8626E-9	+

4.3. Results for case 3

Voltage deviation is defined as the discrepancy between nominal and real voltage. The lower the deviation of the generated voltage, the better the voltage condition of the system. Thus, optimizing (minimizing) the voltage deviation is crucial in the power network. Therefore, the objective function in this case is used to minimize the voltage deviation from the reference voltage, 1 p.u. The voltages of 24 load buses in IEEE 30-bus system can vary in between 0.95 p.u. and 1.05 p.u. Therefore, the maximum
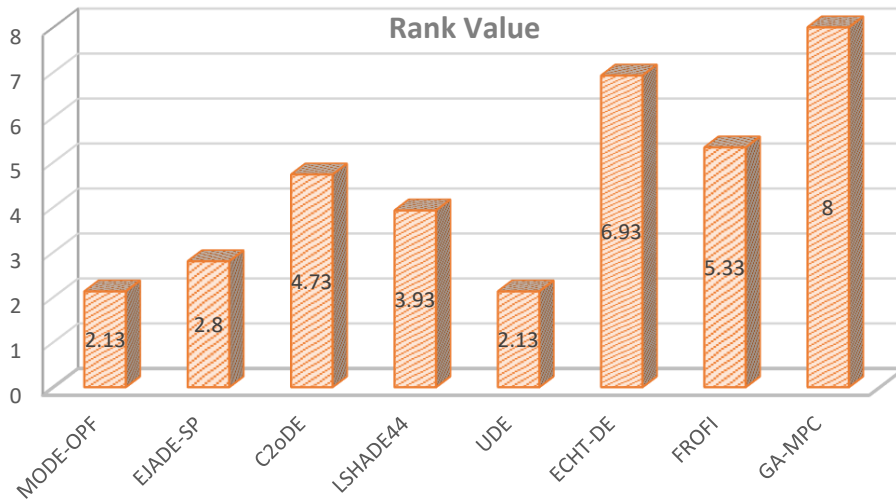
Figure 11: Case 2: Average ranking achieved by Friedman's ranking test

permissible voltage deviation for the cumulative approach is theoretically 1.2 p.u. (i.e., 24× 0.05 p.u.) during the network operation. It can be observed from Table 18 that cumulative voltage deviation for all the cases is within permissible ranges. The voltage deviation of all the cases for 30 buses is depicted in Figure 21. It is also found that the objective function determines the minimum voltage deviation from the reference voltage, 1 p.u. as illustrated in Figure 17. The summary of the results for minimum, median, average and maximum obtained from the proposed MODE-OPF and the state-of-the-art algorithms is given in Table 11. In regards to the minimum voltage deviation, MODE-OPF is able to obtain the best minimum value similar to both EJADE-SP and LSHADE44. Additionally, the proposed MODE-OPF obtains the best median, the best average and the best maximum voltage deviation values.

Table 11: Case 3: Comparative summary of algorithms

Algorithms	Best	Median	Mean	Worst	Std.
GA-MPC	0.3756540	0.3770276	0.3790136	0.4023681	0.0062173
EJADE-SP	**0.3752297**	0.3757606	0.3757257	0.3757625	0.0001348
C^2oDE	0.3752298	0.3752486	0.3754349	0.3757626	0.0002506
LSHADE44	**0.3752297**	0.3754566	0.3754991	**0.3757620**	0.0002544
UDE	0.3755108	0.3755807	0.3755746	0.3755817	0.0000177
ECHT-DE	0.3758577	0.3760752	0.3760738	0.3763896	0.0001167
FROFI	0.3752349	0.3756336	0.3755222	0.3757691	0.0002483
MODE-OPF	**0.3752297**	**0.3752297**	**0.3754068**	**0.3757620**	**0.0002547**

Table 12 presents the results obtained from the Wilcoxon signed-rank test from which the proposed MODE-OPF is significantly superior to EJADE-SP, LSHADE44, UDE, ECHT-DE, FROFI and GA-MPC with very small p-values less than 0.05. The proposed MODE-OPF has no significant difference with C^2oDE, but a very small P-value less than 0.1 (0.083). For further analysis, we conducted the Friedman rank test to rank the proposed algorithms with the state-of-the-art algorithms. Figure 12 depicts the result obtained from the Friedman test, from which the proposed MODE-OPF is ranked first followed by EJADE-SP then UDE, while GA-MPC has the last rank.

Table 12: Case 3: Results obtained by the Wilcoxon test for algorithm Proposed

Algorithms	R^+	R^-	Exact P-value	Dec.
MODE-OPF vs. EJADE-SP	426.0	39.0	1.3966E-5	$+$
MODE-OPF vs. C^{2}oDE	316.0	149.0	0.08794	$\approx$
MODE-OPF vs. LSHADE44	333.0	132.0	0.03842	$+$
MODE-OPF vs. UDE	410.0	55.0	9.902E-5	$+$
MODE-OPF vs. ECHT-DE	465.0	0.0	1.8626E-9	$+$
MODE-OPF vs. FROFI	370.0	95.0	0.003744	$+$
MODE-OPF vs. GA-MPC	465.0	0.0	1.8626E-9	$+$
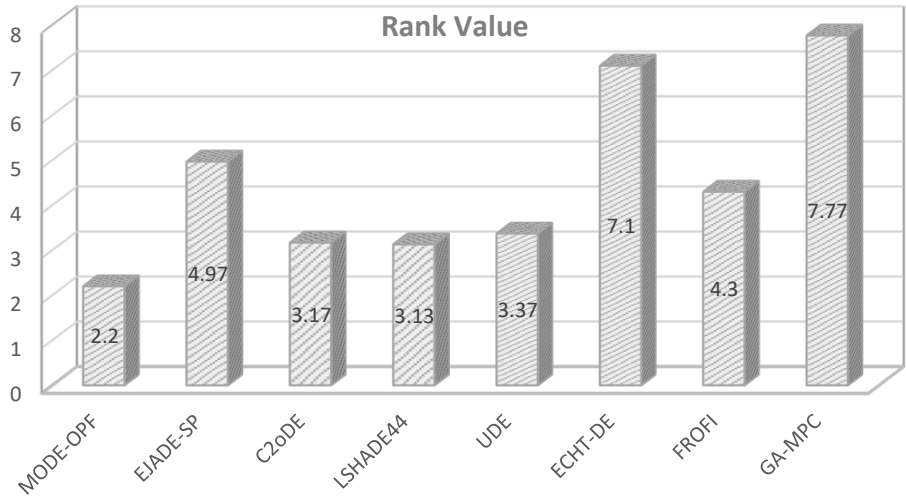
Figure 12: Case 3: Average ranking achieved by Friedman's ranking test

4.4. Results for Case 4

As power and electricity are produced from conventional sources (for example, fossil fuels), toxic gases are released into the air. Indeed, because of global warming and deforestation, emissions have recently gained growing attention. Therefore it is very important to reduce and minimize the emission in a power system network. As a result, the objective function of Case 4 is used to minimize emission. The summary of the results for minimum, median, maximum and average obtained from MODE-OPF and the competitive algorithms is presented in Table 13. As clear from Table 13, the proposed algorithm obtains the second minimum emission value after EJADE-SP with a very small difference (0.0000002). For the median, average and maximum emission values, the proposed MODE-OPF is able to obtain the best values similar to EJADE-SP. Figure 18 demonstrates the emission of all the five case studies from where it is clear that the objective function reduces the emission by utilizing renewable energy generation that is slightly less than Case 2. As higher renewable energy utilization in Case 2, 3 and 4, the lower emission is observed as compared to Case 1 and Case 5.

Table 13: Case 4: Comparative summary of the algorithms

Algorithms	Best	Median	Mean	Worst	Std.
GA-MPC	0.0958581	0.0960947	0.0971113	0.1131335	0.0038195
EJADE-SP	**0.0958325**	**0.0958327**	**0.0958327**	**0.0958329**	0.0000001
C^{2}oDE	0.0958328	0.0958355	0.0958364	0.0958449	0.0000033
LSHADE44	0.0958327	0.0958330	0.0958338	0.0958394	0.0000016
UDE	0.0958327	0.0958328	0.0958329	0.0958337	0.0000002
ECHT-DE	0.0958416	0.0958591	0.0958633	0.0959138	0.0000162
FROFI	0.0958373	0.0958480	0.0958478	0.0958698	0.0000082
MODE-OPF	0.0958327	**0.0958327**	**0.0958327**	**0.0958329**	**0.0000000**

For further analysis, we have conducted the Wilcoxon signed-rank test to see if there is a significant difference between the proposed algorithm (MODE-OPF) and other algorithms, with the results presented in Table 14. It can be concluded from this table that MODE-OPF is significantly better than C^{2}oDE, LSHADE44, UDE, ECHT-DE, FROFI and GA-MPC. However, there is no significant difference between the proposed algorithm and EJADE-SP. For a more statistical test, we have conducted the Friedman rank test in order to rank all the competing algorithms, with the results shown in Figure 13. It is clear that MODE-OPF is ranked first, followed by EJADE-SP in the second position, then UDE in the thied position, while GA-MPC comes in the last position.

Table 14: Case 4: Results obtained by the Wilcoxon test for algorithm Proposed

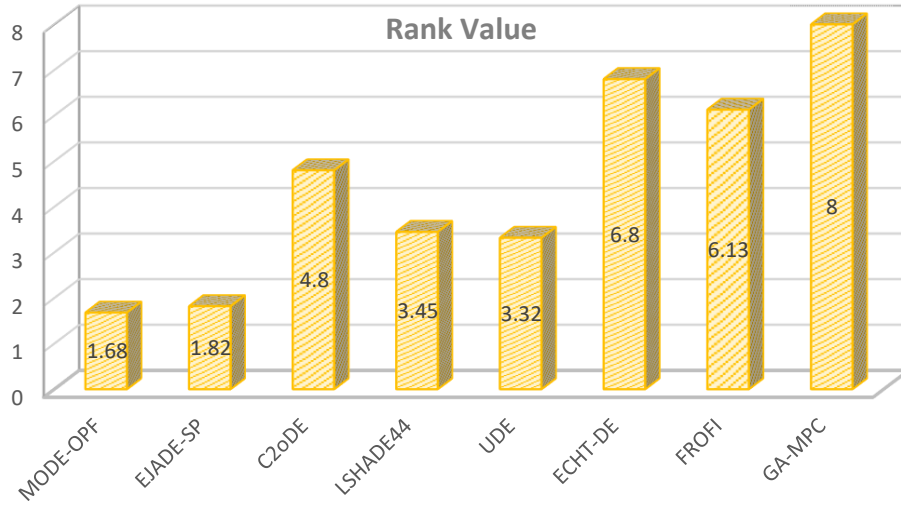| Algorithms	R^+	R^-	Exact P-value	Dec.
MODE-OPF vs. EJADE-SP	231.0	234.0	≥ 0.2	$\approx$
MODE-OPF vs. C^{2}oDE	465.0	0.0	1.8626E-9	+
MODE-OPF vs. LSHADE44	417.0	18.0	9.424E-7	+
MODE-OPF vs. UDE	463.5	1.5	4.657E-9	+
MODE-OPF vs. ECHT-DE	465.0	0.0	1.8626E-9	+
MODE-OPF vs. FROFI	465.0	0.0	1.8626E-9	+
MODE-OPF vs. GA-MPC	465.0	0.0	1.8626E-9	+

Figure 13: Case 4: Average ranking achieved by Friedman's ranking test

4.4.1. Results of case 5

In this situation, we considered emission and generation costs. The summary of the statistical results are presented in Table 16, from which the proposed MODE-OPF has the ability to obtain better results than all other rival algorithms for best, median, mean and worst objective function values. EJADE-SP is able to obtain the best minimum value, but not the best for other criteria. This proves the robustness of the proposed MODE-OPF. Therefore, it can be concluded that the proposed solver has the capability to reduce the average of both emission and total generation cost by 1.1%, 0.83%, 2.70%, 1.32%, 8.56%, 1.1% and 28.95%, as compared to EJADE-SP, C^{2}oDE, LSHADE44, UDE, ECHT-DE, FRORI and GA-MPC, respectively. It can be observed from Table 19 that the minimum operating cost is achieved by this case study, which is \$ 811.23. Therefore, we can conclude that combining the two cases (i.e., 1 and 4) provides the lowest operational cost with low environmental pollution.

Table 15: Case 5: Comparative summary of the algorithms

Algorithms	Best	Median	Mean	Worst	Std.
GA-MPC	811.260700	812.453150	813.587130	827.368900	4.239141
EJADE-SP	**811.226920**	811.227010	811.242495	811.521965	0.053385
C^{2}oDE	811.230000	811.240800	811.239783	811.245200	0.005216
LSHADE44	811.227000	811.243900	811.258470	811.615700	0.074488
UDE	811.227002	811.243869	811.244706	811.367322	0.024636
ECHT-DE	811.284000	811.311950	811.317110	811.401000	0.028397
FROFI	811.234212	811.243417	811.242496	811.248956	0.004073
MODE-OPF	**811.226920**	**811.227002**	**811.231500**	**811.243869**	0.007587

Considering the Wilcoxon's signed-rank test, as in the last column of Table 16, the proposed MODE-OPF is significantly better than all other competing algorithms with p-values less than 0.05. Furthermore, referring to Friedman's ranking test as depicted in Figure 14, the proposed algorithm is ranked first, EJADE-SP ranked second and UDE ranked third, while GA-MPC ranked last.

4.4.2. Convergence, computational time and voltage curves

The efficiency of the proposed MODE-OPF is further assessed by plotting the convergence graphs for all cases, as depicted in Figure 20. From Figure 20, it is clear that the proposed algorithm converges

Table 16: Case 5: Results obtained by the Wilcoxon test

Algorithms	R^+	R^-	Exact P-value	Dec.
MODE-OPF vs. EJADE-SP	332.0	133.0	0.04048	+
MODE-OPF vs. C^{2}oDE	393.0	72.0	5.548E-4	+
MODE-OPF vs. LSHADE44	422.0	43.0	2.366E-5	+
MODE-OPF vs. UDE	384.0	51.0	1.2406E-4	+
MODE-OPF vs. ECHT-DE	465.0	0.0	1.8626E-9	+
MODE-OPF vs. FROFI	442.0	23.0	1.192E-6	+
MODE-OPF vs. GA-MPC	465.0	0.0	1.8626E-9	+
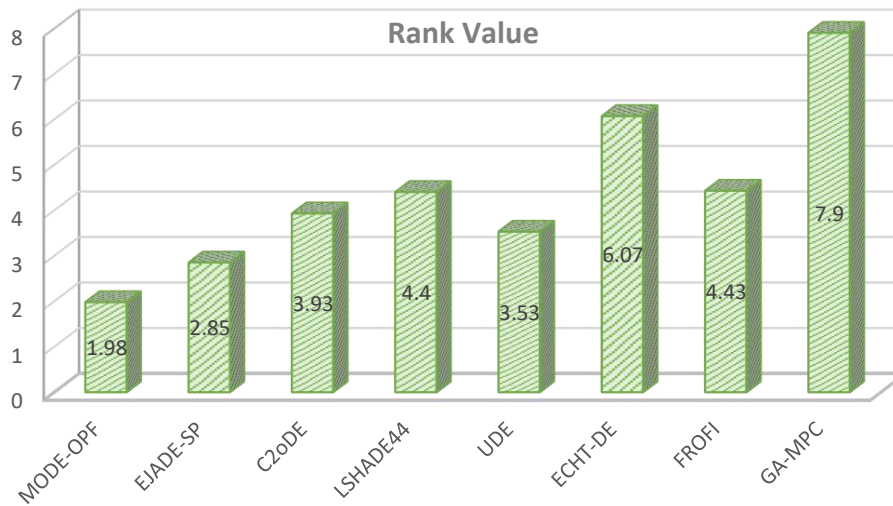
Figure 14: Case 5: Average ranking achieved by Friedman's ranking test
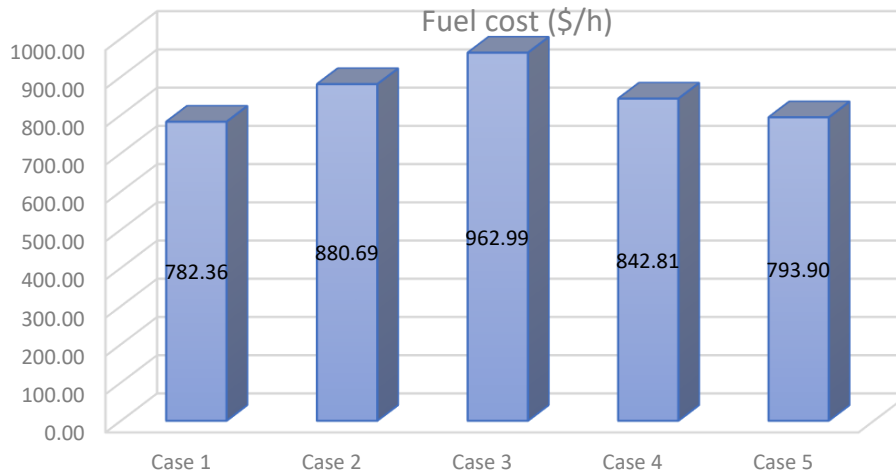
Figure 15: Fuel costs of all the cases

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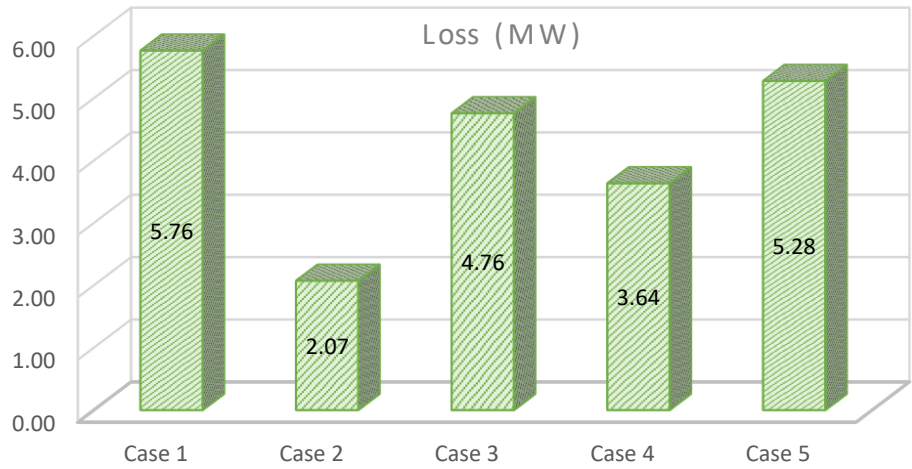
Figure 16: Real power loss of the network
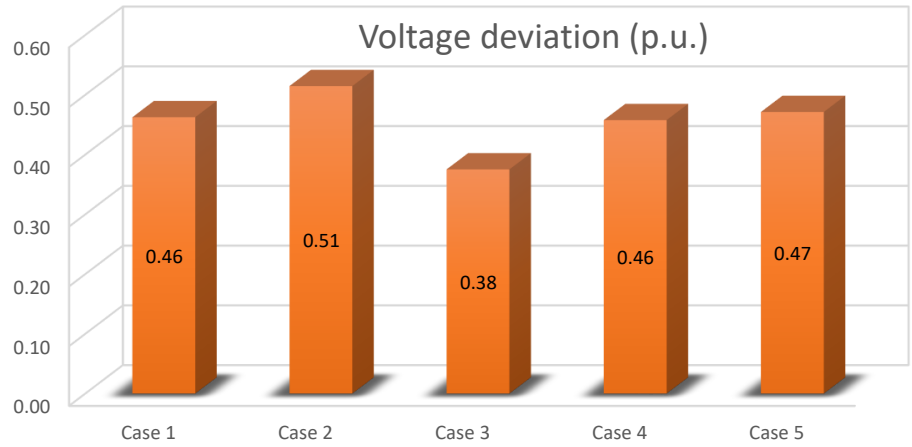
Figure 17: Cumulative voltage drop of the network
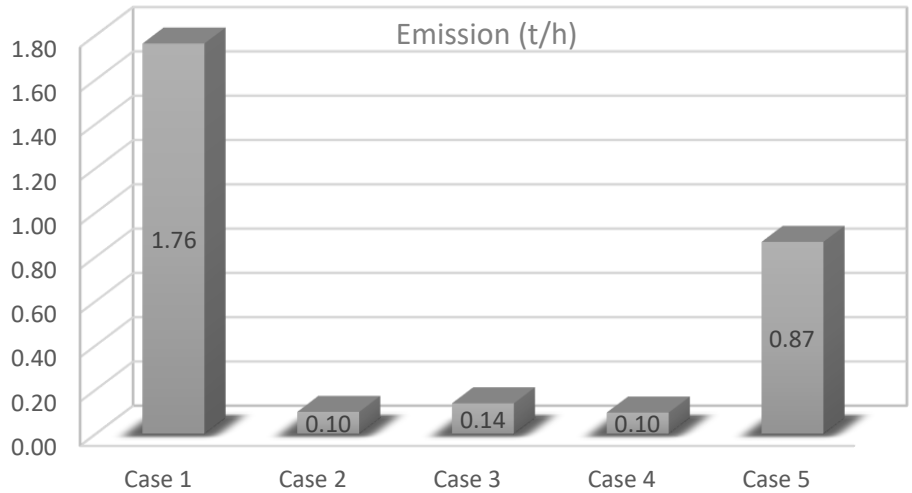
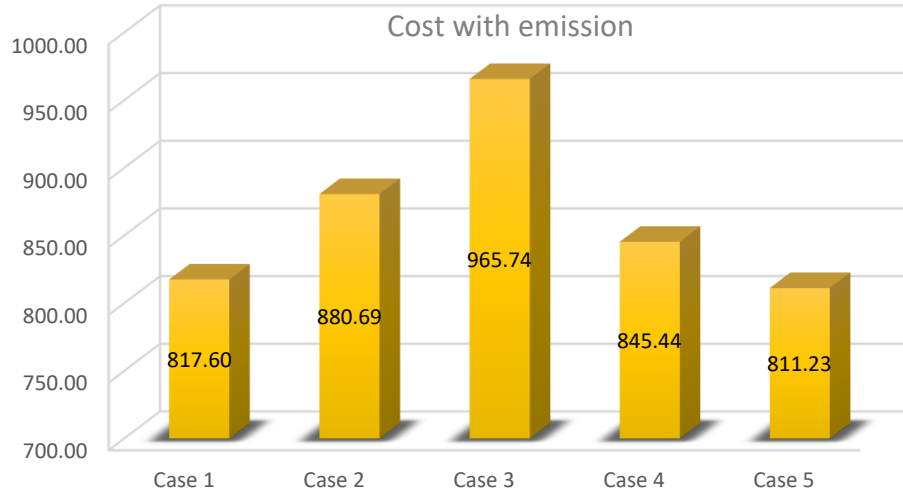Figure 18: Emission of generators for all the cases

Figure 19: Generation cost and emission cost together

faster than all other algorithms. For example, in case of 1, the proposed algorithm (MODE-OPF) has the fastest convergence followed by EJADE-SP, then C²oDE. Again, we consider case 3, MODE-OPF has the fastest convergence, followed by UDE and then ECHT-DE.

Also, as a further comparison, the average computational running time over the 30 runs for all competing algorithms are recorded in Table 17. It can be concluded from Table 17 that the average computational time of the proposed MODE-OPF is smaller than the average computational time of all other algorithms. The proposed algorithm is able to save the time up to 25.57%, 30.88%, 49.4%, 37.45% and 34.64% for Case 1, Case 2, Case 3, Case 4 and Case 5, respectively.
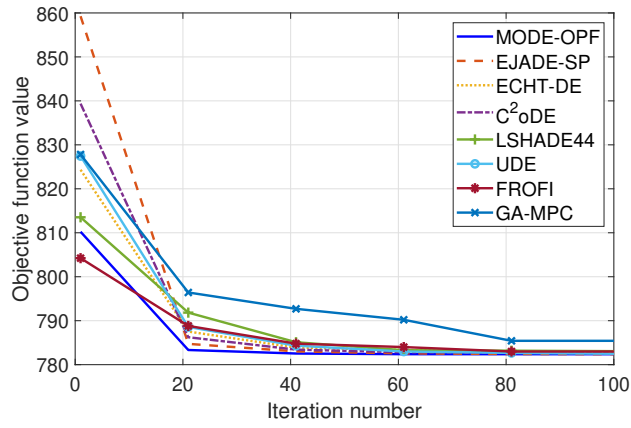
Table 17: Average computational time in seconds for the five different cases

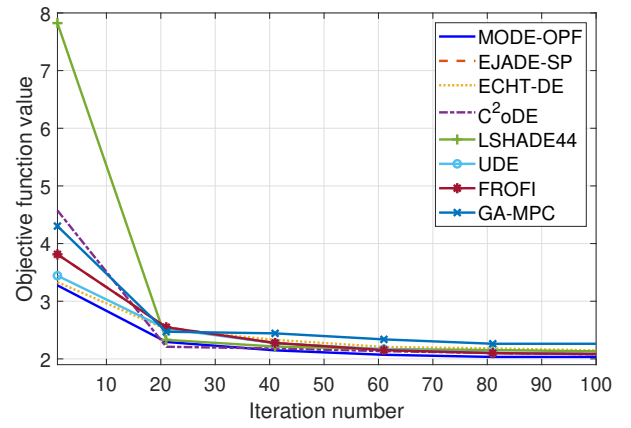| Algorithms	MODE-OPF	EJADE-SP	C²oDE	LSHADE44	UDE	ECHT-DE	FROFI	GA-MPC
Case 1	**164.297**	204.299	208.356	206.147	208.329	220.742	171.064	188.214
Case 2	**161.000**	174.838	222.336	199.094	232.918	222.410	174.422	222.013
Case 3	**142.984**	282.758	272.250	266.123	203.543	260.943	229.972	198.833
Case 4	**151.578**	173.916	239.993	242.319	191.514	229.243	193.508	186.436
Case 5	**144.320**	193.455	203.926	220.823	158.129	213.330	158.117	161.354

In a power system, the load bus voltage is a vital constraint. So, its values should be retained within a specific range, i.e., the values should be in $[0.95p.u, 1.05p.u]$ [12]. Figure 21 depicts the voltage profiles of load busses for the different five cases (case 1 to case 5). It is clear from Figure 21 that the load bus voltage always satisfies the requirements independent of any considered cases.

4.5. Comparison with the state-of-the-art algorithms for IEEE 118-bus system
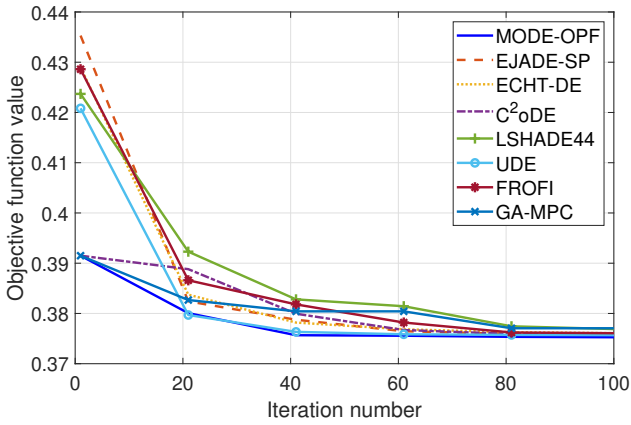
In this section, the performance of the proposed MODE-OPF is tested on the larger system (IEEE 118-bus system), while the objective is to minimize fuel cost (case 1) and power loss (case 2). For keeping the length of this manuscript within acceptable range, we have deliberately avoided the performance demonstration of MODE-OPF for this larger dataset while considering other objectives (i.e., cases 3 to 5). The calculation details of these objective functions and their associated constrained are presented in Subsection 2.3 and Subsection 2.4, respectively. MODE-OPF was run 30 times for 100,000 fitness evaluations, with population size equal to 75. Note, for a fair comparison all the compared algorithms were run to the same number of fitness evaluations (100,000) and the population size was set to a value
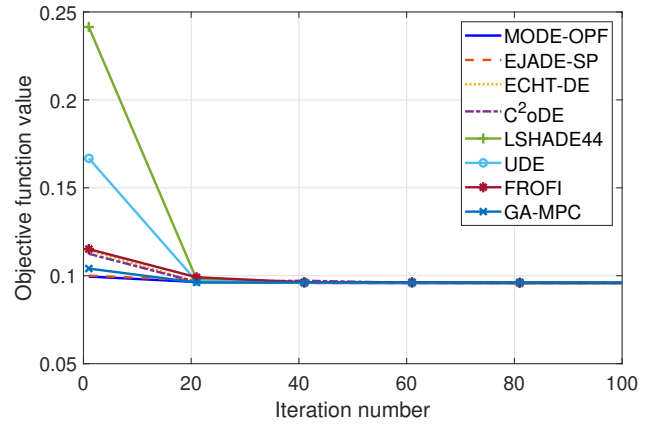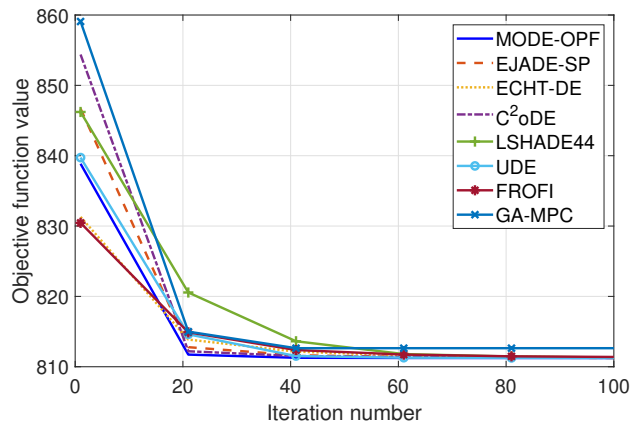
Figure 20: Convergence graphs of algorithms compared: (a) Case 1; (b) Case 2; (c) Case 3; (d) Case 4; and (e) Case 5
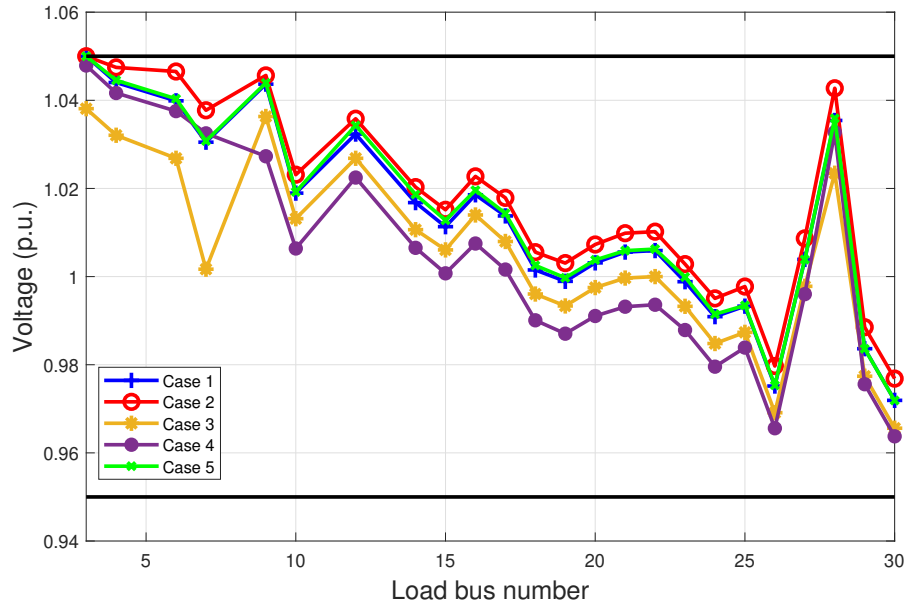
Figure 21: Voltages of all buses for the best obtained solutions for all five cases

Table 18: Optimal results obtained from MODE-OPF of the IEEE-30 bus system for Cases 1-5

Control Variable	Bounds of Variables		Case 1	Case 2	Case 3	Case 4	Case 5
	Min	Max					
P_{G_1}	30	140	134.908	50.000	76.145	75.753	123.027
P_{G_2}	20	80	29.130	25.068	80.000	46.634	31.746
P_{G_3}	0	75	44.085	75.000	75.000	55.837	45.33
P_{G_4}	10	35	10.00	35.000	35.000	35.000	10.000
P_{G_5}	0	60	37.202	60.000	22.013	55.009	38.194
P_{G_6}	0	50	33.838	40.406	0.000	43.802	40.371
V_{G_1}	0.95	1.10	1.072	1.058	1.061	1.072	1.070
V_{G_2}	0.95	1.10	1.058	1.053	1.100	1.027	1.057
V_{G_5}	0.95	1.10	1.036	1.044	0.951	1.044	1.036
V_{G_8}	0.95	1.10	1.040	1.050	1.100	1.038	1.040
$V_{G_{11}}$	0.95	1.10	1.099	1.097	1.100	1.065	1.100
$V_{G_{13}}$	0.95	1.10	1.054	1.059	1.100	1.042	1.057
Q_{G_1}	-20	150	-1.878	-5.096	-8.584	26.150	-2.794
Q_{G_2}	-20	60	13.299	7.106	60.000	-20.000	12.181
Q_{G_3}	-15	40	23.170	20.815	-30.000	32.731	22.988
Q_{G_4}	-30	35	35.000	37.903	40.000	36.729	35.120
Q_{G_5}	-25	30	30.000	30.000	30.000	22.013	30.000
Q_{G_6}	-20	25	17.216	18.596	25.000	15.995	18.196
Total fuel cost ($/h)			782.35930	880.69180	962.98720	842.81070	793.8983
Wind power cost			248.29260	464.62960	329.54980	361.88210	256.1482
Solar power cost			91.39878	113.96730	45.64850	126.66270	113.8466
Thermal generator cost			442.66790	302.09490	587.78880	354.26590	423.9035
Real power loss (MW)			5.76321	2.07324	4.75823	3.63551	5.2767
Cumulative voltage deviation			0.46252	0.51470	0.37523	0.45764	0.4713
Emission (ton/h)			1.76193	0.09894	0.13763	0.09583	0.8664
Total fuel cost +Emission			817.59798	880.69180	965.73975	845.44365	811.2270

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equal to 75. The ranges of control and state variables of the IEEE 118-bus system are presented in Table 19.

Table 19: Lower and upper bounds for IEEE 118-bus system.

Control variables	Range (MW)	Control variables	Range (MW)	Control variables	Range (p.u.)	Control variables	Range (p.u.)	Control variables	Range
$PG1$ (MW)	30–100	$PG65$	147.3–491	$VG1$ (MW)	0.95-1.1	$VG65$	0.95-1.1	$QC5$ (MVAr)	0-25
$PG4$	30–100	$PG66$	147.6–492	$VG4$	0.95-1.1	$VG66$	0.95-1.1	$QC34$ (MVAr)	0-25
$PG6$	30–100	$PG70$	30–100	$VG6$	0.95-1.1	$VG69$	0.95-1.1	$QC37$ (MVAr)	0-25
$PG8$	30–100	$PG72$	30–100	$VG8$	0.95-1.1	$VG70$	0.95-1.1	$QC44$ (MVAr)	0-25
$PG10$	165–550	$PG73$	30–100	$VG10$	0.95-1.1	$VG72$	0.95-1.1	$QC45$ (MVAr)	0-25
$PG12$	55.5–185	$PG74$	30–100	$VG12$	0.95-1.1	$VG73$	0.95-1.1	$QC46$ (MVAr)	0-25
$PG15$	30–100	$PG76$	30–100	$VG15$	0.95-1.1	$VG74$	0.95-1.1	$QC48$ (MVAr)	0-25
$PG18$	30–100	$PG77$	30–100	$VG18$	0.95-1.1	$VG76$	0.95-1.1	$QC74$ (MVAr)	0-25
$PG19$	30–100	$PG80$	173.1–577	$VG19$	0.95-1.1	$VG77$	0.95-1.1	$QC79$ (MVAr)	0-25
$PG24$	30–100	$PG85$	30–100	$VG24$	0.95-1.1	$VG80$	0.95-1.1	$QC82$ (MVAr)	0-25
$PG25$	96–320	$PG87$	31.2–104	$VG25$	0.95-1.1	$VG85$	0.95-1.1	$QC83$ (MVAr)	0-25
$PG26$	124.2–414	$PG89$	212.1–707	$VG26$	0.95-1.1	$VG87$	0.95-1.1	$QC105$ (MVAr)	0-25
$PG27$	30–100	$PG90$	30–100	$VG27$	0.95-1.1	$VG89$	0.95-1.1	$QC107$ (MVAr)	0-25
$PG31$	32.1–107	$PG91$	30–100	$VG31$	0.95-1.1	$VG90$	0.95-1.1	$QC110$ (MVAr)	0-25
$PG32$	30–100	$PG92$	30–100	$VG32$	0.95-1.1	$VG91$	0.95-1.1	$T8$ (p.u.)	0.9-1.1
$PG34$	30–100	$PG99$	30–100	$VG34$	0.95-1.1	$VG92$	0.95-1.1	$T32$ (p.u.)	0.9-1.1
$PG36$	30–100	$PG100$	105.6–352	$VG36$	0.95-1.1	$VG99$	0.95-1.1	$T36$ (p.u.)	0.9-1.1
$PG40$	30–100	$PG103$	42–140	$VG40$	0.95-1.1	$VG100$	0.95-1.1	$T51$ (p.u.)	0.9-1.1
$PG42$	30–100	$PG104$	30–100	$VG42$	0.95-1.1	$VG103$	0.95-1.1	$T93$ (p.u.)	0.9-1.1
$PG46$	35.7–119	$PG105$	30–100	$VG46$	0.95-1.1	$VG104$	0.95-1.1	$T95$ (p.u.)	0.9-1.1
$PG49$	91.2–304	$PG107$	30–100	$VG49$	0.95-1.1	$VG105$	0.95-1.1	$T102$ (p.u.)	0.9-1.1
$PG54$	44.4–148	$PG110$	30–100	$VG54$	0.95-1.1	$VG107$	0.95-1.1	$T107$ (p.u.)	0.9-1.1
$PG55$	30–100	$PG111$	40.8–136	$VG55$	0.95-1.1	$VG110$	0.95-1.1	$T127$ (p.u.)	0.9-1.1
$PG56$	30–100	$PG112$	30–100	$VG56$	0.95-1.1	$VG111$	0.95-1.1	$PG69$ (MW)	$0 - 805.2$
$PG59$	76.5–255	$PG113$	30–100	$VG59$	0.95-1.1	$VG112$	0.95-1.1		
$PG61$	78–260	$PG116$	30–100	$VG61$	0.95-1.1	$VG113$	0.95-1.1		
$PG62$	30–100			$VG62$	0.95-1.1	$VG116$	0.95-1.1		

Tables 20 and 21 present the values of the control variables and the calculated parameters of the best objective function values produced in 30 runs for fuel cost (case 1) and power loss (case 2), respectively. For case 1, the obtained value of fuel cost is 134993.01 $/h. For case 2, the obtained real power loss from MODE-OPF is 16.875146 MW.

The performance of the proposed MODE-OPF has been compared to EJADE-SP, C²oDE, LSHADE-44, UDE and ECHT-DE, while GA-MPC and FRORI have been excluded from the comparison as they were not able to produce feasible solutions for the IEEE 118-bus system. Table 22 presents the summary of the results obtained from MODE-OPF and the competing algorithms for case1. The proposed MODE-OPF obtains the best results for best, median, mean, worst and standard deviation. Using MODE-OPF, a saving of 277.500$, 4222.100$, 3352.800$, 42.511$ and 13409.200$ per hour is

Table 20: Simulation results obtained from MODE-OPF algorithm for case 1 of IEEE 118-bus system.

Control variables	Values (MW)	Control variables	Values (MW)	Control variables	Values (p.u.)	Control variables	Values (p.u.)	Control variables	Values
$PG1$ (MW)	30.000301	$PG65$	290.007900	$VG1$ (MW)	1.0105823	$VG65$	1.0583671	$QC5$ (MVAr)	2.28054
$PG4$	30.000096	$PG66$	289.808350	$VG4$	1.0385693	$VG66$	1.0721225	$QC34$ (MVAr)	5.92327
$PG6$	30.000071	$PG70$	30.002357	$VG6$	1.0325120	$VG69$	1.0544147	$QC37$ (MVAr)	0.01109
$PG8$	30.000000	$PG72$	30.003546	$VG8$	1.0443294	$VG70$	1.0395854	$QC44$ (MVAr)	6.96712
$PG10$	315.648560	$PG73$	30.022168	$VG10$	1.0443034	$VG72$	1.0456533	$QC45$ (MVAr)	19.95665
$PG12$	67.610082	$PG74$	30.004690	$VG12$	1.0247451	$VG73$	1.0423548	$QC46$ (MVAr)	0.90691
$PG15$	30.002392	$PG76$	30.001196	$VG15$	1.0230688	$VG74$	1.0248496	$QC48$ (MVAr)	7.61586
$PG18$	30.000116	$PG77$	30.000021	$VG18$	1.0252138	$VG76$	1.0030046	$QC74$ (MVAr)	24.99988
$PG19$	30.000657	$PG80$	349.199090	$VG19$	1.0222603	$VG77$	1.0269050	$QC79$ (MVAr)	24.95416
$PG24$	30.003568	$PG85$	30.000795	$VG24$	1.0381604	$VG80$	1.0349583	$QC82$ (MVAr)	24.99059
$PG25$	152.602370	$PG87$	31.200575	$VG25$	1.0537238	$VG85$	1.0464296	$QC83$ (MVAr)	4.35272
$PG26$	219.960740	$PG89$	383.557890	$VG26$	1.0807804	$VG87$	1.0670962	$QC105$ (MVAr)	18.00007
$PG27$	30.000013	$PG90$	30.000020	$VG27$	1.0214670	$VG89$	1.0559942	$QC107$ (MVAr)	7.52475
$PG31$	32.100013	$PG91$	30.003381	$VG31$	1.0166141	$VG90$	1.0379483	$QC110$ (MVAr)	22.04558
$PG32$	30.000000	$PG92$	30.001991	$VG32$	1.0160001	$VG91$	1.0382000	$T8$ (p.u.)	1.00028
$PG34$	30.000000	$PG99$	30.000181	$VG34$	1.0352050	$VG92$	1.0402867	$T32$ (p.u.)	1.07619
$PG36$	30.001076	$PG100$	176.002340	$VG36$	1.0296750	$VG99$	1.0306176	$T36$ (p.u.)	1.00364
$PG40$	30.000031	$PG103$	42.011701	$VG40$	1.0235645	$VG100$	1.0330692	$T51$ (p.u.)	0.99335
$PG42$	30.000005	$PG104$	30.013010	$VG42$	1.0262225	$VG103$	1.0268264	$T93$ (p.u.)	0.98511
$PG46$	35.710740	$PG105$	30.000286	$VG46$	1.0490460	$VG104$	1.0225026	$T95$ (p.u.)	0.99528
$PG49$	161.740580	$PG107$	30.010348	$VG49$	1.0599033	$VG105$	1.0195927	$T102$ (p.u.)	0.98316
$PG54$	44.400379	$PG110$	30.000001	$VG54$	1.0437102	$VG107$	1.0125182	$T107$ (p.u.)	0.94765
$PG55$	30.000000	$PG111$	40.800000	$VG55$	1.0418340	$VG110$	1.0208466	$T127$ (p.u.)	1.00670
$PG56$	30.000132	$PG112$	30.000000	$VG56$	1.0426048	$VG111$	1.0285442	Fuel cost ($/h)	134993.01000
$PG59$	125.766500	$PG113$	30.014962	$VG59$	1.0587616	$VG112$	1.0118602	$Ploss$ (MW)	59.44586
$PG61$	122.169800	$PG116$	30.000000	$VG61$	1.0611259	$VG113$	1.0286230	VD (p.u.)	1.93219
$PG62$	30.000000			$VG62$	1.0581949	$VG116$	1.0520616	$PG69$ (MW)	371.06085

Table 21: Simulation results obtained from MODE-OPF algorithm for case 2 of IEEE 118-bus system.

Control variables	Values (MW)	Control variables	Values (MW)	Control variables	Values (p.u.)	Control variables	Values (p.u.)	Control variables	Values
$PG1$ (MW)	73.720742	$PG65$	147.300420	$VG1$ (MW)	1.026833	$VG65$	1.049689	$QC5$ (MVAr)	18.048479
$PG4$	30.000000	$PG66$	147.600000	$VG4$	1.040823	$VG66$	1.029436	$QC34$ (MVAr)	0.038566
$PG6$	30.004433	$PG70$	30.000029	$VG6$	1.037155	$VG69$	1.030806	$QC37$ (MVAr)	0.000000
$PG8$	30.001938	$PG72$	30.000750	$VG8$	1.039729	$VG70$	1.030839	$QC44$ (MVAr)	3.169625
$PG10$	165.032690	$PG73$	30.026081	$VG10$	1.042859	$VG72$	1.040309	$QC45$ (MVAr)	20.742639
$PG12$	133.414890	$PG74$	99.999670	$VG12$	1.036036	$VG73$	1.037170	$QC46$ (MVAr)	10.750599
$PG15$	84.750920	$PG76$	99.999999	$VG15$	1.029931	$VG74$	1.029268	$QC48$ (MVAr)	8.594440
$PG18$	30.186756	$PG77$	99.999907	$VG18$	1.029775	$VG76$	1.019345	$QC74$ (MVAr)	19.112107
$PG19$	57.238556	$PG80$	288.217930	$VG19$	1.030083	$VG77$	1.031227	$QC79$ (MVAr)	24.997969
$PG24$	30.003725	$PG85$	30.000003	$VG24$	1.039307	$VG80$	1.036393	$QC82$ (MVAr)	23.818645
$PG25$	96.000000	$PG87$	31.200000	$VG25$	1.043698	$VG85$	1.034078	$QC83$ (MVAr)	11.785550
$PG26$	124.216760	$PG89$	212.115160	$VG26$	1.058324	$VG87$	1.052456	$QC105$ (MVAr)	20.354596
$PG27$	49.164404	$PG90$	99.138561	$VG27$	1.030552	$VG89$	1.037422	$QC107$ (MVAr)	16.786494
$PG31$	60.211705	$PG91$	30.009251	$VG31$	1.031086	$VG90$	1.028969	$QC110$ (MVAr)	15.138179
$PG32$	40.793179	$PG92$	30.006111	$VG32$	1.030975	$VG91$	1.031686	$T8$ (p.u.)	0.998960
$PG34$	68.497437	$PG99$	39.114352	$VG34$	1.032924	$VG92$	1.028674	$T32$ (p.u.)	1.074251
$PG36$	52.253846	$PG100$	105.738610	$VG36$	1.030032	$VG99$	1.032062	$T36$ (p.u.)	1.003425
$PG40$	100.000000	$PG103$	42.000207	$VG40$	1.029303	$VG100$	1.031176	$T51$ (p.u.)	0.998566
$PG42$	99.975331	$PG104$	33.044689	$VG42$	1.027713	$VG103$	1.032144	$T93$ (p.u.)	1.019130
$PG46$	82.433708	$PG105$	52.434424	$VG46$	1.027924	$VG104$	1.029039	$T95$ (p.u.)	1.018448
$PG49$	141.274360	$PG107$	57.344047	$VG49$	1.027232	$VG105$	1.028834	$T102$ (p.u.)	0.993092
$PG54$	141.222870	$PG110$	30.000035	$VG54$	1.024479	$VG107$	1.028575	$T107$ (p.u.)	0.983730
$PG55$	77.869852	$PG111$	40.800233	$VG55$	1.024688	$VG110$	1.031654	$T127$ (p.u.)	0.996027
$PG56$	99.999893	$PG112$	51.477770	$VG56$	1.024303	$VG111$	1.041056	Ploss (MW)	16.875146
$PG59$	253.224830	$PG113$	30.000512	$VG59$	1.022357	$VG112$	1.027672	Fuel cost ($/h)	155257.680000
$PG61$	78.000661	$PG116$	74.571457	$VG61$	1.024260	$VG113$	1.036436	VD (p.u.)	1.719105
$PG62$	64.841019			$VG62$	1.023360	$VG116$	1.047035	$PG69$ (MW)	2.400438

obtained in comparison with EJADE-SP, C²oDE, LSHADE-44, UDE and ECHT-DE, respectively. Table 23 presents the the results obtained from the Wilcoxon signed sum ranked test. From this table, it is clear that the proposed algorithm is statistically better than all the rival algorithms.

Table 22: Case1: Comparative summary of algorithms for IEEE 118-bus system

Algorithms	Best	Median	Mean	Worst	Std.
EJADE-SP	135270.500	145634.000	144609.717	147032.900	2950.158
C²oDE	139215.100	140617.800	140563.803	142153.500	791.440
LSHADE-44	138345.800	141460.000	141616.190	147084.200	1742.387
UDE	135035.511	135407.198	135556.783	136697.621	448.622
ECHT-DE	148402.200	156220.300	156511.647	169173.900	4641.558
MODE-OPF	**134993.000**	**135068.450**	**135077.567**	**135186.000**	**46.926**

Table 23: Case1: Results obtained by the Wilcoxon test for IEEE 118-bus system

Algorithms	R^+	R^-	Exact P-value	Dec.
MODE-OPF vs. EJADE-SP	465.0	0.0	1.8626E-9	+
MODE-OPF vs. C²oDE	465.0	0.0	1.8626E-9	+
MODE-OPF vs. LSHADE-44	465.0	0.0	1.8626E-9	+
MODE-OPF vs. UDE	456.0	9.0	6.146E-8	+
MODE-OPF vs. ECHT-DE	465.0	0.0	1.8626E-9	+

For minimizing the real power loss (case 2), the summary of the results obtained from the proposed MODE-OPF, EJADE-SP, C²oDE, LSHADE-44, UDE and ECHT-DE when solving the IEEE 118-bus system are presented in Table 24. The minimum power loss obtained by MODE-OPF, Considering the best results obtained MODE-OPF, EJADE-SP, C²oDE, LSHADE-44, UDE and ECHT-DE are 16.875150MW, 17.129120MW, 21.764760MW, 22.603160MW, 17.182191MW and 64.612650MW, respectively. It is clear that, the proposed MODE-OPF obtains the minimum value for the real power loss among all the competing algorithms. Table 25 presents the summary od the results obtained from the Wilcoxon signed ranked test, from which the proposed MODE-OPF is statistically superior to all other algorithms.

Table 24: Case2: Comparative summary of algorithms for IEEE 118-bus system

Algorithms	Best	Median	Mean	Worst	Std.
EJADE-SP	17.129120	35.316460	17.631485	18.323512	3.240519
C²oDE	21.764760	29.442960	25.208170	25.420595	2.001475
LSHADE-44	22.603160	48.072960	26.838230	27.669944	4.453681
UDE	17.182191	21.995836	17.873803	18.391651	1.274370
ECHT-DE	64.612650	99.516740	80.695495	81.569335	9.123206
MODE-OPF	**16.875150**	**17.856370**	**17.329370**	**17.341645**	**0.252547**

5. Conclusion and Future Work

In this paper, an enhanced multi-operator DE algorithm has been developed to solve the OPF problem. The proposed MODE-OPF utilizes the benefits of using multiple DE operators in a single

Table 25: Case2: Results obtained by the Wilcoxon test for IEEE 118-bus system

Algorithms	R^+	R^-	Exact P-value	Dec.
MODE-OPF vs. EJADE-SP	406.0	59.0	1.5288E-4	+
MODE-OPF vs. C^{2}oDE	465.0	0.0	1.8626E-9	+
MODE-OPF vs. LSHADE-44	465.0	0.0	1.8626E-9	+
MODE-OPF vs. UDE	436.0	29.0	3.24E-6	+
MODE-OPF vs. ECHT-DE	465.0	0.0	1.8626E-9	+

algorithmic setting, with the most appropriate one emphasized based on both population diversity and quality of solutions. Also, to balance between diversification and fast convergence, an adaptive method (AM) has been developed. The proposed algorithm is tested by solving the OPF problem with the modified IEEE-30 bus system, where solar and wind generators are modeled to ensure that the OPF problem incorporates current issues of the power industry. Five different cases are disjointly considered with five unique objective functions. The performance of the proposed algorithm is evaluated against well-performed algorithms. It is observed from the experimental results that the proposed MODE-OPF outperforms the other advanced algorithms to optimize the various objective functions. In terms of the quality of solutions, MODE-OPF is able to decrease the total generation cost up to 24.08%, the real power loss up to 6.80% and the total generation cost with emission up to 8.56%. In terms of time, the proposed MODE-OPF was able to reduce the computational time up to 25.57%, 30.88%, 49.4%, 37.45% and 34.64% for Case 1, Case 2, Case 3, Case 4 and Case 5, respectively. To further demonstrate the effectiveness of the proposed algorithm, we have solved the OPF problem of IEEE-118 bus system. The results from the analysis again indicate the superiority of the algorithm.

In future, more constraint handling techniques will be considered with the proposed algorithm. The proposed MODE-OPF will also be tested with other power system problems, such as stochastic optimal power flow problem, optimal sizing of distributed generation for active power loss minimization and wind farm layout problem.

Conflict of Interest:

All the authors declare that they have no conflict of interest.

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