







Article

Assessment urban transport service and Pythagorean Fuzzy Sets CODAS method: A case of study of Ciudad Juárez

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Abstract: The purpose of this research article is to provide a comprehensive method that allows the evaluation of the public transportation in their different transport lines that offer in Ciudad Juárez, Chihuahua. This study presents a description of the public transport system as part of the literature review that describes an appropriate model based on the more outstanding publications about urban mobility and public transportation for passengers' as well as success cases published which serves as a starting point to check the actual state of the public transportation system based on the Pythagorean Fuzzy CODAS to analyze and evaluate the alternatives through criteria that defines the general performance. The integration of these methods provides an adequate methodology for decision-making concerning urban planning and mobility to detect and improve the performance of criteria not considered within sustainable urban mobility plans.

Keywords: CODAS; Pythagorean Fuzzy Sets; Public Transportation; COVID-Criteria

1. Introduction

The tendency in the search for problems of transportation and urban mobility solutions, as well as in urban planning and Geographic Information Systems (SIG), has increased in the worldwide, especially when talking about public passenger transportation because there is an area of opportunity to implement public politics in cities with high population density. In other words, it is necessary to make objective and impartial decisions, that is with a technical approach that helps to cover all the relevant aspects that affect the quality. However, the greatest obstacle that has arisen is the integration of qualitative information within the projects with a large number of criteria to assess the quality of the service provided by a public transportation system are usually obtained thought opinions and interpretations of the users and experts, that is why the contribution of multicriteria decision methods (MCDM) to reduce the bias and improve information analysis is highlighted. One of the most important sets are the Pythagorean Fuzzy Sets (PFS) considered a new generation of the Fuzzy Sets (FS) and Intuitionistic Fuzzy Sets (IFS) [1] as part of the MCDM, similarly, this fuzzy sets have generated hybridizations with some MCDM, as is the example of the MOORA method with IFS [2] which, for the transportation area and urban mobility allows hierarchigin the route alternatives and detect the route with the best characteristics for given criteria [3]. Thus, the assumptions of rating criteria according to the opinion in linguistic terms of experts in the subject, followed by a mathematical analysis in some matrix represented by fuzzy numbers to evaluate the alternatives and establish and hierarchical order [4]. In the last decade, new methods for assessing MCDM problems

have emerged as a response to include some characteristic which the actual methods not considered [5] as the COmbinative Distance-based Assessment (CODAS) method developed by [6] that has the goal of determine the which is the best alternative based on the Euclidean distance as the primary measure and the Taxicab distance (or Manhattan) that is the secondary measure when the Euclidean distances are incomparable.

1.1. Multicriteria decision making

In the last three decades, multicriteria decision making (MCDM) have been take on vital importance in mathematics problems and computational sciences, their principal characteristic is the valuation as applied science which has the objective of determine the value of something such as a product or service, using elements of comparison where a professional evaluate all the criteria for every alternative that usually is subjective and quantitative information [7]. [8] present two categories, see , with the classification of the methods of multicriteria decision: first, the Multi-attribute Decision Making (MADM) used to resolve discrete problems where the alternatives are predetermined and the professional evaluate “a priori” every criteria, and the Multi-Objective Decision Making (MODM) that is used to resolve continue problems where the alternatives are not predetermined and will have some continue solutions respect of two or more criteria named Pareto’s border where the professional participate a posteriori [9]. The MCDM usually are used to obtain the best alternative to fully satisfy a range of indicate of performance [10] and are based on the criteria with best preferred aspects according to the objectives of every problem or project, these criteria also are considered in a process of evaluation.

In general, the MCDM consist in assign choice weights, analyze via pair-wise ranking of the alternatives respect of a criterion and establish the importance and preference criteria or alternatives in an evaluation’s matrix to homogenize because in the multicriteria decision making the information can be qualitative data too, therefore suggest that the evaluation be with an objective vision where the intuition of every decision maker (professional) represent their experience in individual evaluation [3]. Also is describe as the process of the evaluation and selection of the best alternative of the universe [11] because we can classify as necessary to reduce bias and expose the problem with precision.

Table 1. Multi-criteria decision methods and their approaches

Method	Author
SAW	[12]
COPRAS	[13]
TOPSIS	[14]
VIKOR	[15]
MAUT	[16]
MAVT	[17,18]
AHP	[19]
F-AHP	[20,21]
MACBETH	[22]
PROMETHEE	[23–25]
ELECTRE	[26]
WSM	[27]
WPM	[28]
SMART	[29]
SMARTER	[30]
MOORA	[4]
MULTIMOORA	[31]
WASPAS	[32]
MAUA	[33]
ARAS-F	[34]
KEMIRA	[35]
ARAS	[36]
SWARA	[37]
NAIADE	[38]
EDAS	[39]

Furthermore, there were different methods of multicriteria to solve problems of transport and urban mobility, also applied in urban planification and Geographic Information System (GIS) for select the best alternative in a project and to implement politics publics, because this is necessary to design indicators for monitoring it [40]. The principal MCDM are Analytic Hierarchy Process (AHP), Analytic Network Process (ANP), [41]; Multicriteria Optimization and Compromise Solution (compromiso (VIKOR, ViseKriterijumsa Optimizacija i Kompromisno Resenje); Preference Ranking Organization Method for Enrichment of Evaluations (PROMETHEE) [42]; Elimination and Choice Expressing Reality (ELECTRE); and Multi-Objective Optimization on the basis of the Ratio Analysis (MOORA) introduced by [4], among other relevant methods, see the synthesis in the **Table 1**.

Thus,[6] were the first to developed the combinative distancebased assessment (CODAS) method based into crisp sets or ordinal information to assessment some alternatives. This method is based on the combination of the Euclidean distance as the primary unit and the Taxicab (or Hamming) distance as the secondary unit to compared between them respect to the negative-ideal point; Ghorabae applied CODAS method to select a industrial robot using criterios of its operation. Also, [43] used linguistic variables and trapezoidal fuzzy numbers to extend the CODAS to evaluate market segmentation, they results were compare with ranking of Fuzzy EDAS and Fuzzy TOPSIS methods for the same problem. [44] proposed an integration of the multi-criteria decision making to solve problems about maintenances for industrial process, therefore to calculate the weights of criteria and subcriteria is used Geometric Mean (GM) method, then the weights calculated are include in the proposed method to rank the alternatives of the strategy maintenance.

Thereby,[45] applied CODAS methods using crisp sets in a case study of supplier selection for a steelmaking company in Libya. They used sensivility analysis to measure the validaty and stability of this method. Time after, [46], developed an integration of the CODAS method using Pythagorean fuzzy sets and applying the proposal to select a supplier in a manufacturing firm.[47] introduced an application with WDBA to select the optimum alternative with CODAS method, the principal characteristic that provided WDBA is to compare the shortest distance with the negative-ideal solution. [48] developed a problema to select the best location to install a desalination plant using the geographic

information of Libya as criteria. [49] evaluated model of business intelligence for enterprise systems, the model consists in fuzzy numbers to calculate criteria weights and to evaluate alternatives with intuitionistic fuzzy logic with interval values.

[50] used the pairwise to determine the importance level of the criteria and, then the method integrates CODAS crisp to select wave energy technology as a case of study. IVIF-CODAS method was used by [51] to select sustainable material in construction projects with incomplete weight information, Roy developed a sensitivity analysis to validate IVIF-CODAS changing weights of criteria reaching a high degree of stability. [52] developed a case study for personnel selection with linguistic terms of uncertainty (Hesitant Fuzzy Linguistic Term Sets, HFLTS); in a similar case of application using this information type [53] appraise organizational and technological into industry 4.0.

In a different view of application [54] used SWARA as tool to calculate criteria weights and CODAS under crisp sets to select material for dam construction based on the technical specifications (chemical and physics) of each alternative. [55] are very recognized to develop and work with multi-criteria decision making, they developed a model of decision making based in CODAS under intuitionistic fuzzy to determine and prioritize strategies of SCL (Smart City Logistic). [56] assess the performance of bank institutions using entropy method to calculate weights criteria and CODAS to assess the stability and level of performance. Also, Ouhibi and Moalla proposed multiple classification and categories under incremental positions for central profiles and limits used to compare the distances of the CODAS method. [57] work with a method to select the best alternative to install wind generation plants.

Using the best and worst (BWM) method, [58] evaluated the weights of the criteria and the linguistic variables with 2-tuple interval values. To select computer system to work in the cloud according to criteria of availability, reliability, security, maintenance, among others [59] developed a special application using Interval-Valued Intuitionistic Fuzzy CODAS for Multiattribute Decision-Making Method in Tehran. In another order of ideas, [5] which performed a comparison of MOORA with CODAS methods under Pythagorean Fuzzy Sets to show the benefits and disadvantages between these methods. Flores Ruvalcaba found that weight of the criteria in CODAS method just considers necessary one expert to apply the method through linguistic terms does not have a step for calculate the contribution of the stakeholders, this is stakeholders are named Decision Makers (DM) in MCDM. [60] developed an interesting model of aggregation with pythagorean fuzzy sets with CODAS and pure linguistic information with application to financial strategies of multi-national companies.

1.2. Weights of the criteria and decision makers

The contributions of criteria in multi-criteria decision making is expressed through the integration of the DM's opinions. [2] use the Intuitionistic Fuzzy Weighted Average (IFWA) for rating the k th DM, then [61] change the information type using Pythagorean Fuzzy Set (PFS) instead of Intuitionistic Fuzzy Set (IFS), therefore they used the same configuration, named as fuzzy weighted arithmetic Pythagorean, that is based on the geometry like Pythagorean fuzzy weighted arithmetic averaging (PFWAA) operator, this operator can be used with PFS because is an extension of IFS [62] and can provide better certainty to reduce uncertainty.

Table 2. Pythagorean Fuzzy Numbers of the criteria and DMs

Criteria Term	Symbol	μ	ν
Very Unimportant	VU	0.10	0.90
Unimportant	U	0.35	0.60
Medium	M	0.50	0.45
Important	I	0.75	0.40
Very Important	VI	0.90	0.10

Entropy is another method that works on a predefined decision matrix of criteria. The concept of entropy has two sides, first, when the concept refers to a measure of a certain property of a system

like a temperature; second, when the concept is subjective and can be used as a tool to build models [63]. This method can be combined with MCDM to evaluate alternatives though the weight of the criteria because all criteria do not have same degree of importance in decision-making in real life. The entropy method of the set of normalized outcomes of the j th criterion is given by the degree of diversity of the information.

1.2.1. The criteria for public transportation

The criteria for public transportation are based in their contribution of the operation's performance and the quality of the service. Also, the COVID-19 pandemic that appears in Wuhan, China on December 2019 [64], then covered Mexico on March 2020 influences in the service and operation due to the interaction of different mass of people inside buses throughout the day because the COVID-19 is highly deadly and and contagious through contact with body fluids [65]. Thus, the risk conditions are increase due to the lack of sanitation protocols, the use of face masks, and healthy distance between users as minimum of 6 feets as recommend the World Health Organization (WHO) [66].

Table 3. The decision criteria

Criteria	Reference
Average travel time, Convenience, Security, Reliability, Flexibility, Precision, Operational risk, Quality of service, Energy consumption, Available, Accessibility	[67]
Timeliness, Average travel time, Convenience, Intramodality, Security, cost, System coverage, Service timetable, Reliability, Velocity, Comfortable, Available, Mobility impact	[10]
Frequency, Security, Cost, Comfortable and Accessibility	[68]
Timeliness, Average travel time, Cost, System coverage	[42]
Cost, Occupancy, Comfortable, Accessibility, Information	[69]
Visual information of COVID-19 of mask, Training protocols of COVID-19, identify safe seats	[66]

2. Basic concepts of Pythagorean Fuzzy Set

In this section, we described some basic concepts of PFSs, introduced by Yager are explained as follows.

A Pythagorean fuzzy set give the characteristic of the membership and non-membership degrees that must be equal or less than 1, and that is the principal difference with Intuitionistic Fuzzy Sets (IFS) introduced by Atanassos in 1986 because in IFS the contribution or membership and non-membership degrees in general are more than 1.

Definition 1. Let a set X be a universe of discourse. A PFS P is represented as the next form equation: $\tilde{P} = \{ \langle x, P(\mu_P(x), \nu_P(x)) \rangle \mid x \in X \}$ Here $\mu_{P(x)}$ and $\nu_{P(x)} \in X \rightarrow [0, 1]$ depict the degree of membership and non-membership function of the fuzzy set P ; $\mu_{P(x)} \in [0, 1]$ depict the membership degree of $x \in X$ in P . For all PFS it is necessary the next condition:

$$(\mu_P(x))^2 + (\nu_P(x))^2 \leq 1$$

Also, the degree of hesitancy that is called indeterminacy grade or Pythagorean index degree, $\pi_P(y)$, of x in P can be calculate as follows:

$$\pi_P(y) = \sqrt{1 - ((\mu_P(x))^2 + (\nu_P(x))^2)}$$

Where $(\mu_P(x))^2 + (\nu_P(x))^2 \leq 1$ is for each $x \in X$.

Definition 2. Consider two PFNs [60] as $\tilde{P}_1 = \{(x, P_1(\mu_{P1}(x), \nu_{P1}(x))) \mid x \in X\}$ and $\tilde{P}_2 = \{(x, P_1(\mu_{P2}(x), \nu_{P2}(x))) \mid x \in X\}$ the following basic operations are valid:

$$\tilde{P}_i = (\mu_{Pi}, \nu_{Pi})$$

$$\tilde{P}_1 \oplus \tilde{P}_2 = \left(\sqrt{1 - (1 - \mu_{P1}^2)(1 - \mu_{P2}^2)}, \nu_{P1} \cdot \nu_{P2} \right)$$

$$\tilde{P}_1 \otimes \tilde{P}_2 = \left(\mu_{P1} \cdot \mu_{P2}, \sqrt{1 - (1 - \nu_{P1}^2)(1 - \nu_{P2}^2)} \right)$$

$$\lambda \tilde{P} = P \left(\sqrt{1 - (1 - \mu_P^2)^\lambda}, (\nu_P)^\lambda \right), \lambda \geq 0 \text{ and } \lambda \in R$$

Table 4. Pythagorean Fuzzy Numbers of the alternatives

Alternative Term	Alternative Symbol	μ	ν	π
Extremenly Low	EL	0.10	0.99	0.10
Very Low	VL	0.10	0.97	0.22
Low	L	0.25	0.92	0.30
Medium Low	ML	0.40	0.87	0.29
Medium	M	0.50	0.80	0.33
Medium High	MH	0.60	0.71	0.37
High	H	0.70	0.60	0.39
Very High	VH	0.80	0.44	0.41
Extremenly High	EH	1	0	0

3. The proposed methodology

This section describes the method proposed for CODAS with multi-criteria decision-making and Pythagorean Fuzzy Sets, following the methodology show in Figure 1.

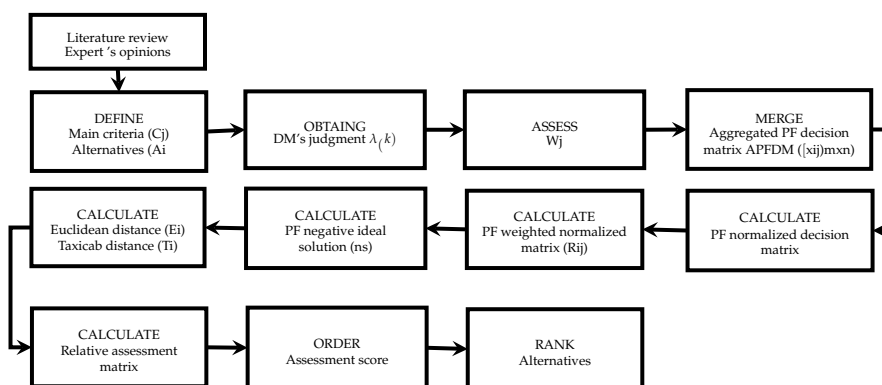


Figure 1. PF-CODAS Methodology (Source: The authors)

In addition, the major contribution is the way of calculate the Pythagorean Fuzzy weight of criteria and the contribution of the expertise of the Decision Makers (DMs) for evaluate every alternative; also it can see how to select the best threshold parameter "τ" to analyze the distances Euclidean and Taxicab for two alternatives in the next steps.

Step 1. Define criteria and alternatives. Decision criteria are the group of criteria that can describe the best way of performance of an alternative. The alternatives of set A_i with $i=1, 2, \dots, m$ each of them evaluated for decision criteria of set C_j with $j=1, 2, \dots, n$.

Step 2. Integrate a group of DMs to assess the group of decision criteria representative of the alternatives.

Where $DM = DM_1, DM_2, \dots, DM_k, \dots, DM_l$ is a set of Decision Makers. The expertise for each DM is established using linguistic terms expressed by pythagorean fuzzy numbers shown in **Table 2**. The overall contribution of every Decision Maker defined as $DM_k = \{\pi_k, \nu_k, \mu_k\}$ with the corresponding weight of k th DM is calculate using the concept proposed by Boran [61]:

$$\lambda_k = \frac{\left(\mu_k + \pi_k \left(\frac{\mu_k}{\mu_k + \pi_k}\right)\right)}{\sum_{k=1}^l \left(\mu_k + \pi_k \left(\frac{\mu_k}{\mu_k + \pi_k}\right)\right)} \quad (1)$$

Where $\sum_{k=1}^l \lambda_k = 1$

Step 3. Determine the importance of criteria. Using the using linguistic terms expressed by pythagorean fuzzy numbers shown in **Table 4** the group of DMs analyze the criteria that describe all alternatives, then every DMs give an evaluation for each criteria to be considered and determine what is the contribution of each one to the problem.

Construct the matrix of asses for each criterion by k th DMs.

$$\tilde{w}_j = PFWA = \left(\tilde{w}_j^{(1)}, \tilde{w}_j^{(2)}, \dots, \tilde{w}_j^{(k)}\right) \quad (2)$$

$$\tilde{w}_j = \lambda_1 \cdot \tilde{w}_j^{(1)} \oplus \lambda_2 \cdot \tilde{w}_j^{(2)} \oplus \dots \oplus \lambda_k \cdot \tilde{w}_j^{(k)} \quad (3)$$

$$\tilde{w}_j = \left(\sqrt{1 - \prod_{j=1}^l (1 - \mu_{ij}^2)^{\lambda_k}}, \prod_{j=1}^l (v_{ij})^{\lambda_k}\right) \quad (4)$$

$$\tilde{w}_j = \frac{\left(\mu_k + \pi_k \left(\frac{\mu_k}{\mu_k + \pi_k}\right)\right)}{\sum_{k=1}^l \left(\mu_k + \pi_k \left(\frac{\mu_k}{\mu_k + \pi_k}\right)\right)} \quad (5)$$

Step 4. Construct the Pythagorean fuzzy decision matrix for alternative assessment is given in the following equation:

The individual opinion of DM in linguistic terms are transformed using the linguistic variables of the **Table 4**, then all opinions of each DM are included into an aggregated pythagorean fuzzy decision matrix (APFDM) as follows:

Where $\tilde{x}_{ij} \geq 0$ and $\tilde{x}_{ij} = (\mu_p, \nu_p)$ and $0 \leq (\mu_p(x))^2 + (\nu_p(x))^2 \leq 1$

$$\tilde{x}_{ij} = APFDM \left(\tilde{x}_{ij}^{(1)}, \tilde{x}_{ij}^{(2)}, \dots, \tilde{x}_{ij}^{(k)}\right) \quad (6)$$

$$\tilde{x}_{ij} = \lambda_1 \cdot \tilde{x}_{ij}^{(1)} \oplus \lambda_2 \cdot \tilde{x}_{ij}^{(2)} \oplus \dots \oplus \lambda_k \cdot \tilde{x}_{ij}^{(k)} \quad (7)$$

$$\tilde{x}_{ij} = \left(\sqrt{1 - \prod_{j=1}^l (1 - \mu_{ij}^2)^{\lambda_k}}, \prod_{j=1}^l (v_{ij})^{\lambda_k}\right) \quad (8)$$

Then, the APFDM is defined as:

$$\tilde{X} = [x_{ij}]_{m.n} = \begin{bmatrix} \tilde{x}_{11} & \tilde{x}_{12} & \dots & \tilde{x}_{1n} \\ \tilde{x}_{21} & \tilde{x}_{22} & \dots & \tilde{x}_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ \tilde{x}_{m1} & \tilde{x}_{m2} & \dots & \tilde{x}_{mn} \end{bmatrix} \quad (9)$$

Step 5. Calculate the Pythagorean fuzzy normalized matrix using linear normalization as in the following equation

$$\eta_{\mu_{ij}} = \frac{\tilde{x}_{ij}}{\max_i \tilde{x}_{ij}}, \eta_{\nu_{ij}} = \frac{\min_i \tilde{x}_{ij}}{\tilde{x}_{ij}} \quad \text{if } j \in N_b \quad (10)$$

$$\eta_{\mu_{ij}} = \frac{\min_i \tilde{x}_{ij}}{x_{ij}}, \eta_{\nu_{ij}} = \frac{\tilde{x}_{ij}}{\max_i x_{ij}} \quad \text{if } j \in N_c \quad (11)$$

where N_b and N_c represent the sets of benefit and cost criteria, respectively.

Step 6. Calculate the Pythagorean fuzzy weighted normalized matrix called \tilde{R}_{ij}

$$\tilde{R}_{ij} = \{\tilde{r}_{ij}\} = \tilde{w}_j \otimes \tilde{x}_{ij} \quad (12)$$

$$\tilde{R}_{ij} = \left\{ \left\langle x, \sqrt{1 - (\mu_{\tilde{x}_i}(x))^{w_j}}, \prod_{j=1}^l (\nu_{x_i}(x))^{w_j} \right\rangle x \in X \right\} \quad (13)$$

$$\tilde{R} = [x_{ij}]_{m.n} = \begin{bmatrix} \tilde{x}_{11} & \tilde{x}_{12} & \dots & \tilde{x}_{1n} \\ \tilde{x}_{21} & \tilde{x}_{22} & \dots & \tilde{x}_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ \tilde{x}_{m1} & \tilde{x}_{m2} & \dots & \tilde{x}_{mn} \end{bmatrix} \quad (14)$$

Step 7. Determine the Pythagorean fuzzy negative ideal solution as given in the following equations:

$$\tilde{n}s = [\tilde{n}s_j]_{1xm} \quad (15)$$

$$\max_i \tilde{r}_{\mu_{ij}}, \min_i \tilde{r}_{\nu_{ij}} \quad \text{if } j \in N_b \quad (16)$$

$$\min_i \tilde{r}_{\nu_{ij}}, \max_i \tilde{r}_{\mu_{ij}} \quad \text{if } j \in N_c \quad (17)$$

Step 8. Calculate the Pythagorean fuzzy Euclidean and Taxicab distances of alternatives from the negative ideal solution as the following equations:

$$E_i = \sqrt{\sum_{j=1}^m (\tilde{u}_{\mu_{ij}} - \tilde{n}s_{\mu_{ij}})^2 + (\tilde{u}_{\nu_{ij}} - \tilde{n}s_{\nu_{ij}})^2} \quad (18)$$

$$T_i = \sum_{j=1}^m |(\tilde{u}_{\mu_{ij}} - \tilde{n}s_{\mu_{ij}}) + (\tilde{u}_{\nu_{ij}} - \tilde{n}s_{\nu_{ij}})| \quad (19)$$

Step 9. Construct the relative assessment matrix based on the Pythagorean fuzzy Euclidean and Taxicab distances as given in the following equations:

$$R_a = [h_{ik}]_{n \times n} \quad (20)$$

$$h_{ik} = (E_i - E_k) + (\psi(E_i - E_k) \times (T_i - T_k)) \quad (21)$$

where $k \in \{1, 2, \dots, n\}$ and c denotes a threshold function to recognize the equality of the Euclidean distances of two alternatives as given in the following equation:

$$\psi(x) = \begin{cases} 1 & \text{if } |x| \geq \tau \\ 0 & \text{if } |x| < \tau \end{cases} \quad (22)$$

If the difference between Euclidean distances of two alternatives is less than, these two alternatives are also compared by the Taxicab distance.

Step 10. Calculate the assessment score of each alternative as given in the following equation:

$$H_i = \sum_{k=1}^n h_{ik} \quad (23)$$

Step 11. Rank the alternatives according to the decreasing values of assessment score (H_i). The alternative with the highest H_i is the best alternative among the alternatives. In the Figure 3 can see that difference between Euclidean distances of two alternatives is less than, these two alternatives are also compared by the Taxicab distance.

4. Numerical case

This illustrative case belongs an assessment of public transportation system in Ciudad Juárez, in which several criteria described the principal characteristics that must have a good service to the users. **Step 1.** Define criteria and alternatives. The Table 3 contains the criteria and their explanation, it is very important consider the type of criteria this means that some criteria are of benefits (minimum values are ideal) and another are of cost (high values are ideal). In order to explain what the alternatives assessment in this proposal are, the modal distribution of public transportation system in Ciudad Juárez. Here, alternatives assessment in this proposal are described as follows in Table 5:

Table 5. Alternatives of public transportation

Line	Ramal	Status	Symbol
1-A	Paseo de la Victoria (Express)	In service	R1
1-A	Morelos	In service	R2
1-A	Unitec	In service	R3
1-A	Tradicional	In service	R4
1-B	Talamas (Express)	In service	R5
Universitaria	Universitaria	In service	R6

Step 2. Integrate a group of DMs to assess the group of decision criteria representative of the alternatives is shown in Table 6.

Table 6. The contribution of every Decision Makers

Decision Maker	1	2
Linguistic Term	D	Ap
PF number	{ 0.90, 0.10, 0.42}	{ 0.10, 0.90, 0.42}

Step 3. The importance of criteria is shown in Table 7.

Table 7. Alternatives of public transportation

Sym.	Name	Type	DM1	DM2	μ_k	ν_k	π_k	$W(\lambda_j)$
C1	Frequency	Benefit	VI	I	0.891	0.115	0.44	0.052
C2	Timeliness	Benefit	I	M	0.734	0.405	0.546	0.0441
C3	Average travel time	Cost	VI	I	0.891	0.115	0.44	0.052
C4	Convenience	Benefit	I	M	0.734	0.405	0.546	0.0441
C5	Intramodality	Benefit	M	VI	0.588	0.387	0.71	0.0413
C6	Security	Benefit	VI	M	0.884	0.116	0.452	0.0521
C7	Cost	Cost	VI	VI	0.9	0.1	0.424	0.0521
C8	System coverage	Benefit	M	M	0.5	0.45	0.74	0.0361
C9	Service timetable	Benefit	M	M	0.5	0.45	0.74	0.0361
C10	Reliability	Benefit	VI	VI	0.9	0.1	0.424	0.0521
C11	Velocity	Cost	VI	VI	0.9	0.1	0.424	0.0521
C12	Occupancy	Benefit	I	I	0.75	0.4	0.527	0.0444
C13	Flexibility	Benefit	M	M	0.5	0.45	0.74	0.0361
C14	Precision	Benefit	M	M	0.5	0.45	0.74	0.0361
C15	Operational risk	Cost	VI	VI	0.9	0.1	0.424	0.0521
C16	Comfortable	Benefit	I	I	0.75	0.4	0.527	0.0444
C17	Quality of service	Benefit	I	I	0.75	0.4	0.527	0.0444
C18	Energy consumption	Benefit	VI	VI	0.9	0.1	0.424	0.0521
C19	Mobility impact	Benefit	VI	VI	0.9	0.1	0.424	0.0521
C20	Disponibile	Benefit	M	M	0.5	0.45	0.74	0.0361
C21	Accessibility	Benefit	VI	VI	0.9	0.1	0.424	0.0521
C22	Information in stations	Benefit	M	M	0.5	0.45	0.74	0.0361
C23	Visual information on buses	Benefit	VI	VI	0.9	0.1	0.424	0.0521
C24	Protocols of COVID-19	Benefit	M	M	0.5	0.45	0.74	0.0361
C25	Identify safe seats and place	Benefit	VI	VI	0.9	0.1	0.424	0.0521

Step 4. Construct the Pythagorean fuzzy decision matrix for alternative assessment, then calculate the aggregated pythagorean fuzzy decision matrix that which is in Table 8 using Linguistic Terms.

Table 8. The evaluations of criteria for each alternative

Criteria	R1	R2	R3	R4	R5	R6	R1	R2	R3	R4	R5	R6
C1	H	MH	MH	M	MH	VH	M	MH	H	H	MH	VH
C2	VL	L	L	L	VL	VL	M	ML	L	M	VL	M
C3	ML	M	ML	M	H	VH	L	M	VH	MH	H	VH
C4	MH	M	M	MH	MH	H	H	M	M	M	ML	MH
C5	M	MH	MH	M	L	L	ML	MH	M	M	L	M
C6	M	MH	H	ML	MH	ML	M	MH	H	ML	MH	ML
C7	H	H	H	H	H	ML	H	H	H	H	H	ML
C8	M	H	MH	MH	ML	M	M	H	H	M	ML	M
C9	M	ML	M	MH	ML	L	M	M	M	M	ML	L
C10	ML	M	MH	ML	ML	H	ML	M	MH	ML	ML	H
C11	L	H	M	MH	M	M	MH	H	MH	MH	VH	VH
C12	MH	M	M	L	MH	H	H	M	M	L	H	VH
C13	MH	L	VL	VL	VL	L	H	L	VL	M	L	L
C14	MH	H	M	MH	ML	L	MH	MH	M	H	ML	L
C15	VH	M	M	M	ML	MH	VH	M	H	M	M	H
C16	ML	M	ML	M	L	L	M	M	MH	M	L	M
C17	M	MH	M	ML	ML	ML	MH	MH	ML	M	MH	MH
C18	ML	MH	M	M	ML	M	ML	MH	M	M	ML	M
C19	H	H	H	H	MH	MH	MH	H	H	H	MH	MH
C20	ML	M	ML	H	ML	H	ML	M	ML	M	M	H
C21	L	MH	ML	MH	VL	L	M	MH	M	MH	VL	M
C22	VL	M	MH	ML	VH	VH	VL	M	M	ML	M	M
C23	ML	ML	ML	ML	L	M	ML	M	ML	M	M	M
C24	MH	M	M	ML	ML	MH	M	ML	ML	ML	ML	M
C25	EL	L	ML	L	L	VL	VL	M	L	L	L	ML

Step 5. The Pythagorean fuzzy normalized matrix using linear normalization is in Table 9a.

Table 9a. Pythagorean Fuzzy Normalized Matrix

	C1		C2		C3		C4		C5		C6		C7		C8		C9	
	μ	ν	μ	ν	μ	ν	μ	ν	μ	ν	μ	ν	μ	ν	μ	ν	μ	ν
R1	0.857	0.713	0.668	0.953	1.000	1.000	0.885	0.874	0.819	0.880	0.714	0.750	0.571	0.690	0.714	0.750	0.845	0.898
R2	0.750	0.620	0.935	0.992	0.776	0.914	0.723	0.763	1.000	1.000	0.857	0.845	0.571	0.690	1.000	1.000	0.696	0.833
R3	0.765	0.630	0.867	0.986	0.813	0.929	0.723	0.763	0.986	0.988	1.000	1.000	0.571	0.690	0.874	0.859	0.845	0.898
R4	0.660	0.566	1.000	1.000	0.759	0.904	0.855	0.849	0.833	0.888	0.571	0.690	0.571	0.690	0.845	0.835	1.000	1.000
R5	0.750	0.620	0.347	0.935	0.555	0.686	0.846	0.842	0.417	0.772	0.857	0.845	0.571	0.690	0.571	0.690	0.676	0.826
R6	1.000	1.000	0.668	0.953	0.485	0.503	1.000	1.000	0.481	0.783	0.571	0.690	1.000	1.000	0.714	0.750	0.423	0.781

Table 9b. Pythagorean Fuzzy Normalized Matrix

Table with 9 columns (C10-C18) and 7 rows (R1-R6). Each cell contains two values representing membership (mu) and non-membership (nu) degrees.

Table 9c. Pythagorean Fuzzy Normalized Matrix

Table with 9 columns (C19-C25) and 7 rows (R1-R6). Each cell contains two values representing membership (mu) and non-membership (nu) degrees.

Step 6. Calculate the Pythagorean fuzzy weighted normalized matrix called \tilde{R}_{ij} and create the respective matrix as shown in Table 10a.

Table 10a. Pythagorean fuzzy weighted normalized matrix

Table with 9 columns (C1-C9) and 7 rows (R1-R6). Each cell contains two values representing membership (mu) and non-membership (nu) degrees.

Table 10b. Pythagorean fuzzy weighted normalized matrix

Table with 9 columns (C10-C18) and 7 rows (R1-R6). Each cell contains two values representing membership (mu) and non-membership (nu) degrees.

Table 10c. Pythagorean fuzzy weighted normalized matrix

Table with 9 columns (C19-C25) and 7 rows (R1-R6). Each cell contains two values representing membership (mu) and non-membership (nu) degrees.

Step 7. The Pythagorean fuzzy negative ideal solution is displayed in Table 11a.

Table 11a. Pythagorean Fuzzy Negative Ideal Solution

Table with 9 columns (C1-C9) and 1 row (ns). Each cell contains two values representing membership (mu) and non-membership (nu) degrees.

Table 11b. Pythagorean Fuzzy Negative Ideal Solution

Table with 9 columns (C10-C18) and 1 row (ns). Each cell contains two values representing membership (mu) and non-membership (nu) degrees.

Table 11c. Pythagorean Fuzzy Negative Ideal Solution

Table with 9 columns (C19-C25) and 1 row (ns). Each cell contains two values representing membership (mu) and non-membership (nu) degrees.

Step 8. The Pythagorean fuzzy Euclidean and Taxicab distances is displayed Table 12a and 13a

Table 12a. Pythagorean fuzzy Euclidean distance

	C1	C2	C3	C4	C5	C6	C7	C8	C9
R1	0.576	0.723	0.792	0.580	0.643	0.675	0.000	0.724	0.645
R2	0.653	0.523	0.009	0.693	0.000	0.575	0.000	0.000	0.733
R3	0.644	0.596	0.012	0.693	0.427	0.000	0.000	0.623	0.645
R4	0.706	0.000	0.007	0.606	0.633	0.751	0.000	0.646	0.000
R5	0.653	0.865	0.001	0.613	0.842	0.575	0.000	0.790	0.743
R6	0.001	0.723	0.001	0.000	0.815	0.751	0.751	0.724	0.849

Table 12b. Pythagorean fuzzy Euclidean distance

	C10	C11	C12	C13	C14	C15	C16	C17	C18
R1	0.751	0.810	0.601	0.000	0.628	0.001	0.629	0.606	0.702
R2	0.675	0.000	0.704	0.854	0.000	0.011	0.000	0.000	0.000
R3	0.575	0.002	0.704	0.942	0.720	0.007	0.605	0.632	0.595
R4	0.751	0.000	0.863	0.889	0.614	0.011	0.000	0.712	0.595
R5	0.751	0.001	0.601	0.929	0.787	0.778	0.801	0.698	0.702
R6	0.000	0.001	0.000	0.854	0.872	0.002	0.766	0.698	0.595

Table 12c. Pythagorean fuzzy Euclidean distance

	C19	C20	C21	C22	C23	C24	C25
R1	0.367	0.790	0.794	0.955	0.646	0.000	0.892
R2	0.000	0.724	0.000	0.761	0.630	0.597	0.657
R3	0.000	0.790	0.691	0.702	0.646	0.597	0.000
R4	0.000	0.477	0.000	0.815	0.630	0.697	0.714
R5	0.575	0.783	0.930	0.001	0.767	0.697	0.714
R6	0.575	0.000	0.794	0.001	0.000	0.000	0.892

Table 13a. Pythagorean fuzzy Taxicab distance

	C1	C2	C3	C4	C5	C6	C7	C8	C9
R1	0.748	0.850	0.890	0.756	0.797	0.818	0.017	0.848	0.799
R2	0.804	0.721	0.088	0.833	0.009	0.749	0.017	0.012	0.854
R3	0.798	0.770	0.105	0.833	0.644	0.017	0.017	0.782	0.799
R4	0.840	0.003	0.081	0.774	0.791	0.867	0.017	0.798	0.008
R5	0.804	0.930	0.002	0.779	0.917	0.749	0.017	0.889	0.860
R6	0.025	0.850	0.031	0.010	0.903	0.867	0.867	0.848	0.921

Table 13b. Pythagorean fuzzy Taxicab distance

	C10	C11	C12	C13	C14	C15	C16	C17	C18
R1	0.867	0.900	0.765	0.010	0.785	0.030	0.790	0.775	0.838
R2	0.818	0.018	0.834	0.923	0.013	0.103	0.005	0.008	0.009
R3	0.749	0.039	0.834	0.971	0.844	0.082	0.775	0.792	0.767
R4	0.867	0.009	0.929	0.942	0.775	0.103	0.005	0.844	0.767
R5	0.867	0.024	0.765	0.964	0.885	0.882	0.895	0.835	0.838
R6	0.017	0.024	0.018	0.923	0.934	0.037	0.875	0.835	0.767

Table 13c. Pythagorean fuzzy Taxicab distance

	C19	C20	C21	C22	C23	C24	C25
R1	0.599	0.889	0.888	0.977	0.802	0.009	0.944
R2	0.008	0.848	0.014	0.866	0.792	0.769	0.807
R3	0.008	0.889	0.826	0.829	0.802	0.769	0.006
R4	0.008	0.680	0.014	0.899	0.792	0.835	0.842
R5	0.758	0.885	0.964	0.023	0.876	0.835	0.842
R6	0.758	0.012	0.888	0.023	0.005	0.009	0.943

Step 9. Construct the relative assessment matrix based on the Pythagorean fuzzy Euclidean and Taxicab distances as the Table 14.

Table 14. Pythagorean fuzzy relative appraisal

Route	R1	R2	R3	R4	R5	R6
R1	0.000	0.845	0.370	0.478	-0.137	0.546
R2	-0.845	0.000	-0.476	-0.368	-0.982	-0.299
R3	-0.370	0.476	0.000	0.108	-0.507	0.176
R4	-0.478	0.368	-0.108	0.000	-0.615	0.068
R5	0.137	0.982	0.507	0.615	0.000	0.683
R6	-0.546	0.299	-0.176	-0.068	-0.683	0.000

Step 10. The assessment score of each alternative Table 15.

Table 15. Assessment score and rank

Route	Hi	RANK
R1	2.101	2
R2	-2.970	6
R3	-0.116	3
R4	-0.765	4
R5	2.925	1
R6	-1.175	5

5. Comparative analysis

In order to evaluate our proposal, some variations were carried out in the decision makers' contribution with different threshold functions as suggests [6]. This sensitivity analysis is performed to determine the consistency of the changes of the alternatives for three different variation as shown in Figure 2.

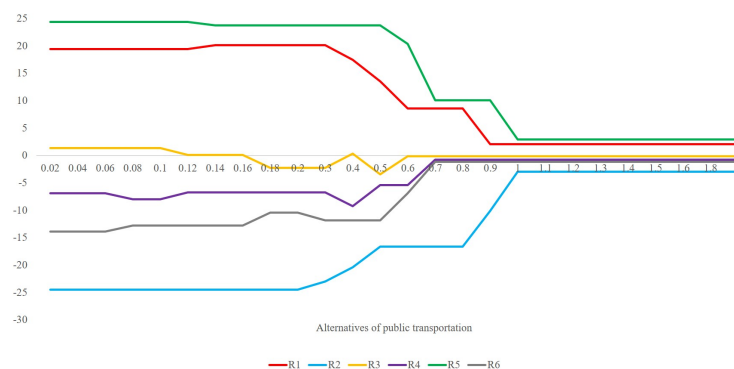


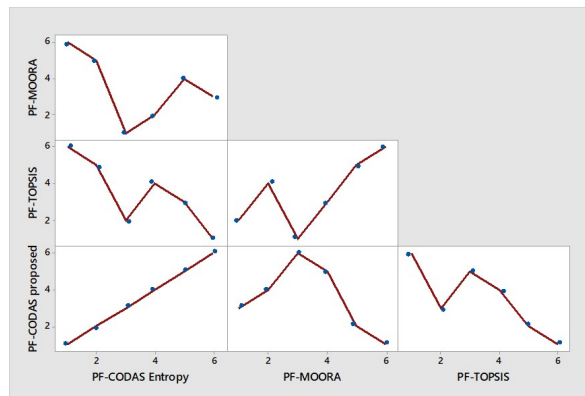
Figure 2. Sensitivity analysis of threshold function (Source: The authors)

5.1. Comparative method

Different methods were compared with the proposed method of Pythagorean Fuzzy CODAS to observe how much is the influence of the Taxicab and Euclidean distance and the threshold function respect with PF-MOORA [61], PF-TOPSIS [70] and PF-CODAS proposed with a variant with entropy to criteria weights [71].

Table 16. Comparison with other methods

	PF-CODAS Entropy	PF-MOORA	PF-TOPSIS
PF-MOORA	-0.486		
PF-TOPSIS	-0.829	0.714	
PF-CODAS propose	1.000	-0.486	-0.829

**Figure 3.** Comparison methods (Source: The authors)

6. Conclusion.

This study is to propose an integrate method under Pythagorean Fuzzy with CODAS technique that include a method to determine the criteria weights based on the expertise of the Decision Makers to the problem of the public transportation system. As we shown, the contributions of the decision makers can change the results of public transportation routes (ramales) that need attentions. This method integrates the individual contribution weight of each DM and this experience is related to the evaluation of each expert on the weight of each criteria. As well as the experience contributes in the evaluation of the criteria for each public transportation routes (the alternatives). The proposed method has a good correlation with other Pythagorean methods as shown in Table 16 and Figure 3

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References

References

- Villa Silva, A.J.; Pérez Dominguez, L.A.; Martínez Gómez, E.; Alvarado-Iniesta, A.; Pérez Olguín, I.J.C. Dimensional analysis under pythagorean fuzzy approach for supplier selection. *Symmetry* **2019**, *11*, 336.
- Perez, L.; Alvarado-Iniesta, A.; Rodríguez-Borbón, I.; Vergara, O. Intuitionistic fuzzy MOORA for supplier selection. *DYNA* **2015**, *82*, 34 – 41. doi:10.13140/RG.2.1.4307.4720.

3. y Mayor y Asociados, C. Estudio Integral para el Corredor de Transporte Público "Corredor Tecnológico", Informe 3: Factibilidad del trazo. Informe 1, IMIP, 2015.
4. Karel, W.; Brauers, W.; Zavadskas, E. The MOORA method and its application to privatization in a transition economy. *Control and Cybernetics* **2006**, *35*, 445–469.
5. Flores-Ruvalcaba, A.A.; Pérez-Domínguez, L.; García-Villalba, L.A.; Almeraz-Durán, S. Una comparación entre el método MOORA y CODAS bajo ambiente de Conjunto Pitagoreano Difuso. *Revista de Innovación Sistemática* **2019**, *3*, 9–19. doi:10.35429/JSI.2019.10.3.9.19.
6. Keshavarz-Ghorabae, M.; Zavadskas, E.K.; Turskis, Z.; Antucheviciene, J. A new combinative distance-based assessment (CODAS) method for multi-criteria decision-making. *Economic computation and economic cybernetics studies and research / Academy of Economic Studies* **2016**, *50*, 25–44.
7. Aznar Bellver, J.; Guijarro Martínez, F. *Nuevos métodos de valoración. Modelos multicriterio*; Editorial Universitat Politècnica de València, 2012.
8. Zavadskas, E.; Turskis, Z.; Kildiene, S. State of art surveys of overviews on MCDM/MADM methods. *Technological and Economic Development of Economy* **2014**, *20*, 165–179. doi:10.3846/20294913.2014.892037.
9. Penadés Plà, V. Aplicación de la toma de decisión multi-criterio al diseño sostenible de puentes de hormigón. Bachelor's thesis, 2017.
10. Keyvan Ekbatani, M.; Cats, O. Multi-criteria appraisal of multi-modal urban public transport systems. *Transportation Research Procedia*, **10**, 2015; 18th Euro Working Group on Transportation, EWGT 2015, 14-16 July 2015, Delft, The Netherlands; Elsevier: Netherlands, 2015; NordiCHI, pp. 1–11.
11. Vahdani, B.; Mousavi, S.M.; Tavakkoli-Moghaddam, R.; Hashemi, H. A new design of the elimination and choice translating reality method for multi-criteria group decision-making in an intuitionistic fuzzy environment. *Applied Mathematical Modelling* **2013**, *37*, 1781 – 1799.
12. MacCrimmon, K.R. Decisionmaking among multiple-attribute alternatives: a survey and consolidated approach. Technical report, Rand Corp Santa Monica Ca, 1968.
13. Zavadskas, E.K.; Kaklauskas, A.; Sarka, V. The new method of multicriteria complex proportional assessment of projects. *Technological and economic development of economy* **1994**, *1*, 131–139.
14. Hwang, C.L.; Yoon, K. Methods for multiple attribute decision making. In *Multiple attribute decision making*; Springer, 1981; pp. 58–191.
15. Opricovic, S. Multicriteria optimization of civil engineering systems. *Faculty of Civil Engineering, Belgrade* **1998**, *2*, 5–21.
16. Dyer, J.S. Chapter 7: "maut" multiattribute utility theory, in 'Multiple Criteria Decision Analysis: State of the Art Surveys', Vol. 78 of International Series in Operations Research & Management Science, 2005.
17. Fishburn, P.C. Methods of estimating additive utilities. *Management science* **1967**, *13*, 435–453.
18. RL, K.; Raiffa, H. Decisions with multiple objectives (preferences and value tradeoffs), 1976.
19. Saaty, T.L. What is the analytic hierarchy process? In *Mathematical models for decision support*; Springer, 1988; pp. 109–121.
20. Wang, Y.M.; Elhag, T.M.; Hua, Z. A modified fuzzy logarithmic least squares method for fuzzy analytic hierarchy process. *Fuzzy sets and systems* **2006**, *157*, 3055–3071.
21. Wang, Y.M.; Luo, Y.; Hua, Z. On the extent analysis method for fuzzy AHP and its applications. *European journal of operational research* **2008**, *186*, 735–747.
22. CA, B.E.C.; DE CORTE, J.; Vansnick, J. On the mathematical foundations of MACBETH,[in:] Multiple Criteria Decision Analysis: State of the Art Surveys, J. Figueira, S. Greco, M. Ehrgott, 2005.
23. Brans, J.P. *L'ingénierie de la décision: l'élaboration d'instruments d'aide a la décision*; Université Laval, Faculté des sciences de l'administration, 1982.
24. Brans, J.P.; Vincke, P. Note—A Preference Ranking Organisation Method: (The PROMETHEE Method for Multiple Criteria Decision-Making). *Management science* **1985**, *31*, 647–656.
25. Brans, J.; Mareschal, B. The PROMETHEE-GAIA decision support system. *Decision Support Systems* **1994**, *12*, 297–310.
26. Roy, B. Classement et choix en présence de points de vue multiples. *Revue française d'informatique et de recherche opérationnelle* **1968**, *2*, 57–75.

27. Fishburn, P.C. Additive Utilities with Incomplete Product Sets: Application to Priorities and Assignments. *Operations Research* **1967**, *15*, 537–542.
28. Triantaphyllou, E.; Mann, S.H. An examination of the effectiveness of multi-dimensional decision-making methods: A decision-making paradox. *Decision Support Systems* **1989**, *5*, 303 – 312. doi:[https://doi.org/10.1016/0167-9236\(89\)90037-7](https://doi.org/10.1016/0167-9236(89)90037-7).
29. Edwards, W.; Barron, F. SMARTS and SMARTER: Improved Simple Methods for Multiattribute Utility Measurement. *Organizational Behavior and Human Decision Processes* **1994**, *60*, 306 – 325. doi:<https://doi.org/10.1006/obhd.1994.1087>.
30. Edwards, W.; Barron, F.H. SMARTS and SMARTER: Improved simple methods for multiattribute utility measurement. *Organizational behavior and human decision processes* **1994**, *60*, 306–325.
31. Brauers, W.K.M.; Zavadskas, E.K. Project management by MULTIMOORA as an instrument for transition economies. *Technological and Economic Development of Economy* **2010**, *16*, 5–24.
32. Zavadskas, E.K.; Turskis, Z.; Antucheviciene, J.; Zakarevicius, A. Optimization of weighted aggregated sum product assessment. *Elektronika ir elektrotechnika* **2012**, *122*, 3–6.
33. Keeney, R.L.; Raiffa, H.; others. *Decisions with multiple objectives: preferences and value trade-offs*; Cambridge university press, 1993.
34. Turskis, Z.; Zavadskas, E. A new fuzzy additive ratio assessment method (ARAS-F). Case study: The analysis of fuzzy Multiple Criteria in order to select the logistic centers location. *Transport* **2010**, *25*, 423–432. doi:10.3846/transport.2010.52.
35. Krylovas, A.; Zavadskas, E.K.; Kosareva, N.; Dadelo, S. New KEMIRA method for determining criteria priority and weights in solving MCDM problem. *International Journal of Information Technology & Decision Making* **2014**, *13*, 1119–1133.
36. Zavadskas, E.K.; Turskis, Z. A new additive ratio assessment (ARAS) method in multicriteria decision-making. *Ukio Technologinis ir Ekonominis Vystymas* **2010**, *16*, 159–172. doi:10.3846/tede.2010.10.
37. Keršulienė, V.; Zavadskas, E.K.; Turskis, Z. Selection of rational dispute resolution method by applying new step-wise weight assessment ratio analysis (Swara). *Journal of Business Economics and Management* **2010**, *11*, 243–258. doi:10.3846/jbem.2010.12.
38. Munda, G. A NAIADE based approach for sustainability benchmarking. *International Journal of Environmental Technology and Management* **2006**, *6*, 65–78.
39. Ghorabae, M.K.; Zavadskas, E.K.; Olfat, L.; Turskis, Z. Multi-Criteria Inventory Classification Using a New Method of Evaluation Based on Distance from Average Solution (EDAS). *Informatica* **2015**, *26*, 435–451.
40. Duleba, S. An AHP-ISM approach for considering public preferences in a public transport development decision. *Transport* **2019**, *34*, 662–671.
41. Ceballos, B.; Lamata, M.; Pelta, D.; Sánchez, J. El método TOPSIS relativo vs. absoluto. *Recta* **2013**, *14*, 181–192.
42. Nassereddine, M.; Eskandari, H. An integrated MCDM approach to evaluate public transportation systems in Tehran. *Transportation Research Part A: Policy and Practice* **2017**, *106*, 427 – 439. doi:<https://doi.org/10.1016/j.tra.2017.10.013>.
43. Ghorabae, M.K.; Amiri, M.; Zavadskas, E.K.; Hooshmand, R.; Antuchevičienė, J. Fuzzy extension of the CODAS method for multi-criteria market segment evaluation. *Journal of Business Economics and Management* **2017**, *18*, 1–19. doi:10.3846/16111699.2016.1278559.
44. Panchal, D.; Chatterjee, P.; Shukla, R.; Choudhury, T.; Tamosaitiene, J. Integrated fuzzy AHP-CODAS framework for maintenance decision in urea fertilizer industry. *Economic Computation and Economic Cybernetics Studies and Research* **2017**, *51*, 179–196.
45. Badi, I.; Abdulshahed, A. A case study of supplier selection for a steelmaking company in Libya by using the combinative distance-based assessment (CODAS) model. *Decision Making: Applications in Management and Engineering* **2018**, *1*, 1–12. doi:10.31181/dmame180101b.
46. Boltürk, E. Pythagorean fuzzy CODAS and its application to supplier selection in a manufacturing firm. *Journal of Enterprise Information Management* **2018**, *31*, 00–00. doi:10.1108/JEIM-01-2018-0020.

47. Peng, X.; Garg, H. Algorithms for interval-valued fuzzy soft sets in emergency decision making based on WDBA and CODAS with new information measure. *Computers & Industrial Engineering* **2018**, *119*, 439 – 452. doi:<https://doi.org/10.1016/j.cie.2018.04.001>.
48. Badi, I.; Ballem, M.; Shetwan, A. Site selection of desalination plant in Libya by using Combinative Distance-Based Assessment (CODAS) method. *International Journal for Quality Research* **2018**, *12*, 609–624. doi:10.18421/IJQR12.03-04.
49. Dahooei, J.; Zavadskas, E.; Vanaki, A.; Firoozfar, H.; Keshavarz-Ghorabae, M. An evaluation model of business intelligence for enterprise systems with new extension of CODAS (CODAS-IVIF). *E+M. Ekonomija a Management = Economics and Management* **2018**, *21*, 171–187.
50. Pamučar, D.; Badi, I.; Sanja, K. A Novel Approach for the Selection of Power-Generation Technology Using a Linguistic Neutrosophic CODAS Method: A Case Study in Libya. *Energies* **2018**, *11*, 2489. doi:10.3390/en11092489.
51. Roy, J.; Das, S.; Kar, S.; Pamučar, D. An extension of the CODAS approach using interval-valued intuitionistic fuzzy set for sustainable material selection in construction projects with incomplete weight information. *Symmetry* **2019**, *11*, 393.
52. Yalcin, N.; Yapıcı Pehlivan, N. Application of the Fuzzy CODAS Method Based on Fuzzy Envelopes for Hesitant Fuzzy Linguistic Term Sets: A Case Study on a Personnel Selection Problem. *Symmetry* **2019**, *11*, 493.
53. Sansabas-Villalpando, V.; Pérez-Olguín, I.J.C.; Pérez-Domínguez, L.A.; Rodríguez-Picón, L.A.; Mendez-González, L.C. CODAS HFLTS Method to Appraise Organizational Culture of Innovation and Complex Technological Changes Environments. *Sustainability* **2019**, *11*, 1–28.
54. Ijadi Maghsoodi, A.; Maghsoodi, A.; Poursoltan, P.; Antucheviciene, J.; Turskis, Z. Dam construction material selection by implementing the integrated SWARA-CODAS approach with target-based attributes. *Archives of Civil and Mechanical Engineering* **2019**, *19*, 1194–1210. doi:10.1016/j.acme.2019.06.010.
55. Buyukozkan, G.; Göçer, F. Prioritizing the Strategies to Enhance Smart City Logistics by Intuitionistic Fuzzy CODAS. 2019 Conference of the International Fuzzy Systems Association and the European Society for Fuzzy Logic and Technology (EUSFLAT 2019). Atlantis Press, 2019, pp. 805–811.
56. Laha, S.; Biswas, S. A hybrid unsupervised learning and multi-criteria decision making approach for performance evaluation of Indian banks. *Accounting* **2019**, *5*, 169–184.
57. Kardeş, A.; Boltürk, E.; Kahraman, C. A novel neutrosophic CODAS method: Selection among wind energy plant locations. *Journal of Intelligent & Fuzzy Systems* **2019**, *36*, 1–14. doi:10.3233/JIFS-181255.
58. Ijadi Maghsoodi, A.; Rasoulipannah, H.; Martínez López, L.; Liao, H.; Zavadskas, E.K. Integrating interval-valued multi-granular 2-tuple linguistic BWM-CODAS approach with target-based attributes: Site selection for a construction project. *Computers & Industrial Engineering* **2020**, *139*, 106147. doi:<https://doi.org/10.1016/j.cie.2019.106147>.
59. Dahooie, J.H.; Vanaki, A.S.; Mohammadi, N. Choosing the Appropriate System for Cloud Computing Implementation by Using the Interval-Valued Intuitionistic Fuzzy CODAS Multiattribute Decision-Making Method (Case Study: Faculty of New Sciences and Technologies of Tehran University). *IEEE Transactions on Engineering Management* **2019**, *67*, 1–14.
60. Zhou, J.; Li, K.W.; Baležentis, T.; Streimikiene, D. Pythagorean fuzzy combinative distance-based assessment with pure linguistic information and its application to financial strategies of multi-national companies. *Economic Research-Ekonomika Istraživanja* **2020**, *33*, 974–998. doi:10.1080/1331677X.2020.1736117.
61. Perez, L.; Rodríguez-Picón, L.; Alvarado-Iniesta, A.; Cruz, D.; Xu, Z. MOORA under Pythagorean Fuzzy Set for Multiple Criteria Decision Making. *Complexity* **2018**, *2018*, 1–10. doi:10.1155/2018/2602376.
62. Akram, M.; Dudek, W.A.; Dar, J.M. Pythagorean Dombi fuzzy aggregation operators with application in multicriteria decision-making. *International Journal of Intelligent Systems* **2019**, *34*, 3000–3019.
63. de Dios Ortúzar, J. *Modelos de demanda de transporte*; Ediciones UC, 2012.
64. Zheng, R.; Xu, Y.; Wang, W.; Ning, G.; Bi, Y. Spatial transmission of COVID-19 via public and private transportation in China. *Travel Medicine and Infectious Disease* **2020**, *34*, 101626. doi:10.1016/j.tmaid.2020.101626.

65. Mogaji, E. Impact of COVID-19 on transportation in Lagos, Nigeria. *Transportation Research Interdisciplinary Perspectives* **2020**, *6*, 100154. doi:<https://doi.org/10.1016/j.trip.2020.100154>.
66. Tirachini, A.; Cats, O. COVID-19 and public transportation: Current assessment, prospects, and research needs. *Journal of Public Transportation* **2020**, *22*, 1.
67. Mavi, R.K.; Zarbakhshnia, N.; Khazraei, A. Bus rapid transit (BRT): A simulation and multi criteria decision making (MCDM) approach. *Transport Policy* **2018**, *72*, 187–197.
68. Jain, D.S.; Aggarwal, P.; Kumar, P.; Singhal, S.; Sharma, P. Identifying public preferences using multi-criteria decision making for assessing the shift of urban commuters from private to public transport: A case study of Delhi. *Transportation Research Part F Traffic Psychology and Behaviour* **2014**, *24*, 60–70. doi:10.1016/j.trf.2014.03.007.
69. Celik, E.; Bilisik, O.N.; Erdogan, M.; Gumus, A.T.; Baracli, H. An integrated novel interval type-2 fuzzy MCDM method to improve customer satisfaction in public transportation for Istanbul. *Transportation Research Part E: Logistics and Transportation Review* **2013**, *58*, 28 – 51. doi:<https://doi.org/10.1016/j.tre.2013.06.006>.
70. Akram, M.; Dudek, W.A.; Ilyas, F. Group decision-making based on pythagorean fuzzy TOPSIS method. *International Journal of Intelligent Systems* **2019**, *34*, 1455–1475.
71. Han, Q.; Li, W.; Song, Y.; Zhang, T.; Wang, R. A new method for MAGDM based on improved TOPSIS and a novel pythagorean fuzzy soft entropy. *Symmetry* **2019**, *11*, 905.

Sample Availability: Samples of the compounds are available from the authors.