The ecology of plant interactions:
A giant with feet of clay

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Abstract

Community ecologists value the phenomenological observation of plant biotic interactions because they provide assumptions to make predictions of other ecosystem features, such as species diversity, community structure, or plant atmospheric carbon uptake. However, a rising number of scientists claim for the need of a mechanistic understanding of plant interactions, due to the limitations that a phenomenological approach raises both in empirical and modeling studies. Scattered studies take a mechanistic approach to plant interactions, but we still lack an integrated theoretical framework to start approaching holistically. In this *Review and Synthesis*, we present a comprehensive foundation for the study of the mechanisms underpinning the net interaction between two plants. First, we recapitulate the elementary units of plant interactions, i.e. all the known biophysical processes affected by the presence of an influencing plant and the possible phenotypic responses of influenced plants to these processes. Following, we discuss how a net interaction between two plants may emerge from the simultaneous effect of these elementary units. We then touch upon the spatial and temporal variability of this net interaction, and scrutinize how that variability may be linked to the underlying biophysical processes. We conclude by arguing how these processes can be integrated in a mechanistic framework for plant interactions, and why it must necessarily focus on the individual scale, incorporate the spatial structure of the community, and explicitly account for environmental factors.

Keywords: Biotic interactions, Community ecology, Ecological modelling, Ecological patterns and processes, Spatial ecology, Theoretical ecology

Introduction

Biotic interactions are fundamental ecological predictors, and its theoretical treatment produces predictions of major ecological features of plant communities. For instance,

45   plant-animal interactions shape plant communities in several ways: herbivory promotes plant biodiversity (Janzen 1970) and limits plant productivity (Polis 1999), and pollination prevents plant species extinction (Goulson et al. 2015). Biotic interactions, however, are more intense between phylogenetically related taxa (Violle et al. 2011) and the interactions among plants themselves (hereafter plant interactions) are of special

50   relevance, as plants intensively, ubiquitously compete with each other for the same resources. Based on assumptions about the nature of *net interactions*, theoretical ecologists explain and predict ecosystem structure and dynamics, from the landscape to the terrestrial scale. For instance, plant *net interactions* allow to forecast climate change scenarios (Brooker 2006) and explain the plant community efficacy at up-taking

55   atmospheric carbon thereby buffering atmospheric climate change (Franklin et al. 2016). Plant interactions also shape the diversity and distribution of land plants in the globe (Tirado and Pugnaire 2005, Bulleri et al. 2016) and their persistence under anthropogenic climate change conditions (Valladares et al. 2015). Additionally, spatial models for vegetation dynamics in semiarid drylands predict the existence of sudden, hard-to-revert

60   desertification events (Rietkerk et al. 2002). It is indisputable that all these predictions are transcendental.

Pushed by overarching ecological theories, empiricists have tended to observe and report the *net interactions* among plants. For instance, an ecological theory of biodiversity maintenance states that more intense intraspecific *interference* relative to interspecific

65   *interference* stabilizes species coexistence (Chesson 2000) –species coexistence being axiomatic to species diversity. Under these lenses, many empirical studies compare

intraspecific with interspecific *net interactions* in order to explain biodiversity variability

across biomes, providing support to theoretical predictions (Lamanna et al. 2017, Adler

et al. 2018). A different theory states that *facilitation* by nurse plants promotes

70 coexistence, expands species' niches, and ultimately leads to higher biodiversity in

stressful habitats (Callaway 1995, Bulleri et al. 2016). To validate it, hundreds of

empirical studies have reported and quantified positive interactions among plants

(Soliveres and Maestre 2014). Similarly, theory predicts that vegetation patchiness could

be used as an indicator of imminent desertification transitions in drylands, where local

75 facilitation is a driving process (Kéfi et al. 2007). Following, empiricists became

interested in relating vegetation cover and patch size distributions to the provision of

ecosystem functionality (Berdugo et al. 2017). These observational studies clearly

provide phenomenological support for ecological theory.

While the relevance of these theories and their observational support is beyond argument,

80 a rising number of scientists yearn for a finer mechanistic understanding of the plant

interaction processes that lay the foundation for them. On the one hand, theories that rely

on assumed *net interactions* among plants risk misleading the mechanisms behind their

predictions. For instance, models for vegetation pattern formation reproduce the same

family of patterns regardless of whether *net interactions* among plants are assumed to be

85 purely competitive (Martínez-García et al. 2013a, 2014) or a combination of facilitation

and interference, each of them dominating at different distances from the influencing

plant (Rietkerk et al. 2002). Hence, while the vegetation patterns produced by both these

models can be observed in drylands around the world (Borgogno et al. 2009a), the actual

mechanisms creating these patterns still remain uncertain. On the other hand,

90 observational studies reporting *net interaction* patterns in nature may not be free from

methodological and statistical biases (Rinella et al. 2020). Disentangling biases from the

data used in these studies is tricky without more information about the mechanisms underpinning plant interactions, and a rising number of empiricists and statisticians claim for studies that tackle that type of knowledge (Detto et al. 2019).

95   Shedding light on the mechanisms that underpin the assumed or observed *net interactions* is an essential pending task for plant interaction ecologists. Here, we present a summarizing revision of the literature on the mechanisms underpinning plant interactions, hoping to establish a novel conceptual framework for its study. Indeed, *pairwise interactions* between organisms of a biological community can be decomposed in various

100   nested elements: Each *pairwise interaction* is composed of two *net interactions* going in opposite directions –from one individual to another– which, in turn, integrate several trophic and non-trophic *interaction forces* (Callaway and Walker 1997) (**Figure 1**). What is mechanistic and what is, by opposition, phenomenological will depend to a large extent on one's standing point (what is mechanistic to one can be seen as phenomenological to

105   other interested in a deeper level of detail). We consider these *interaction forces* as the basic mechanisms explaining plant interactions. On the other hand, observing or assuming the overall biological effect of a neighbor on a focal individual (the *net interaction*) without any further consideration will be considered a phenomenological approach. In this article, we first recapitualte the elemental *biophysical processes* by

110   which plants can interact with each other. Second, we address plant phenotypical responses to these *interaction forces* from the necessary but not widespread game theory perspective. Third, we analyze how *interaction forces* and plant strategies may integrate into a directional *net interaction*, i.e. the overall biological effect of one plant on another. Fourth, we tackle the effects that the distance between the pair of interacting plants has

115   on the *interaction forces* and the *net interaction*. Fifth, we discuss how *net interactions* may change in space and time, and how that relates to the elemental mechanisms of plant

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interactions. Sixth, based on all of the above, we propose the development of *plant interaction models* (PIMs): models based in *biophysical* and physiological *processes* in which plant *net interactions* are not included but rather emerge from a precise description

120   of their underlying *interaction forces*. We argue that PIMs need to explicitly account for the discrete plant individuals, the spatial configuration of the community, and the environmental variables that drive the various *biophysical processes*. Contrarily, an overarching focus on the species identity of the interacting individuals should be discouraged in mechanistic plant interaction studies. Overall, we identify the strengths

125   and weaknesses of this broad area of plant ecology, concluding that we have a lengthy path ahead in order to properly understand plant biotic interactions mechanistically.

Unfortunately, lexical arbitrariness leads to confusion in the biotic interaction literature. An established definition of the existing terms referring to biotic interaction levels and mechanisms would make literature more clear and comprehensible (Trinder et al. 2013).

130   A paradigmatic example illustrating this confusion is the word *competition*, which is used interchangeably to refer to different things. In community-level biotic interaction charts, *competition* is used to refer to the negative *pairwise interaction* (-/-), as opposed to, for instance, mutualism (+/+) (e.g. in Godsoe et al. 2017). In some fields, such as plant positive interactions research, it is common to use *competition* to refer to a negative *net*

135   *interaction*, as opposed to *facilitation* (Filazzola and Lortie 2014). Finally, in an ecophysiology context, *competition* is the fight among individuals for a specific resource (Grime 1973), regardless of whether the net interactive effect is positive or negative, hence being an *interaction force*. This last definition is also backed by the Merriam Webster dictionary in which competition is defined as "active demand by two or more

140   organisms or kinds of organisms for some environmental resource in short supply". This problem similarly affects other related terms (West et al. 2007). To avoid confusion

within this text, and hopefully to contribute a more clear use of the words across sub-disciplines, we propose a glossary of biotic interaction terms in **Table 1**, and consistently use *italics* thorough the text to highlight the words that are defined on it.

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1- The biophysical processes underpinning plant interactions

A first, necessary step to properly discuss how a *net interaction* can be mechanistically explained is to become aware of and bear in mind the several, somewhat independent *biophysical processes* underneath it. In the context of plant interactions, *biophysical*

150   *processes* can be classified in *primary processes* (the direct effects of the influencing plants in their immediate surrounding), intermediary processes (any *biophysical process* mediating between the above and the following), and *interaction forces* (the biophysical changes resulting from the influencing plant that directly affect the influenced plant, i.e. the proximal cause of the interaction).

155   The main *primary processes* are the effects of plant canopy casting shade (Valladares et al. 2016), baffling wind (Leonard and Croft 2006), intercepting rainfall (Muzylo et al. 2009), and transpirating water (Flerchinger et al. 2015); the effects of both plant canopies and root crowns producing litter (Xiong and Nilsson 1999); and the effects of root crown absorbing soil water (Lambers et al. 2008a), exuding plant water (Prieto et al. 2012),

160   absorbing mineral nutrients (Lambers et al. 2008b), altering soil physical structure (Angers and Caron 1998), and exuding metabolites (Bertin et al. 2003). These *primary processes* ultimately affect, sometimes antagonistically, several *interaction forces*, as it is, for example, the case of shade in hot, semi-arid habitats (**Figure 2**).

A review of the plant interaction literature allowed us to identify twenty one types of

165   *interactions forces* (classified in four groups: *competition*, climate amelioration, soil

amelioration and other cases) that should be considered in order to understand mechanistically each single *net interaction* (**Figure 3**). The full literature review explaining each of these mechanisms of interaction, including references to studies addressing them, can be seen as an electronic supplementary material attached to this

170   *Review and Synthesis* (**SM: A review of plant interaction mechanisms**).

2- The phenotypic response of plants to interactions

From a mechanistic perspective, recognizing the *interaction forces* by which an influencing plant affects an influenced partner is as important as it is understanding how

175   the influenced plant phenotypically responds to them. After reviewing the *interaction forces* in the previous section, we now discuss observed plant phenotypical responses. Indeed, plants can sense their surrounding habitat (McNickle et al. 2009) and show plastic phenotypical responses to the presence of neighbors (Abakumova et al. 2016, Turcotte and Levine 2016). Game theory, originally developed to study the interaction among

180   rational decision-makers, became an important framework to investigate evolutionary questions towards the end of the XX century (Maynard Smith 1982). More recently, it has become a very successful framework to study plant phenotypical responses to biotic interactions in an evolutionary context (Mcnickle and Dybzinski 2013). In times of classic optimality (Parker and Maynard Smith 1990), game theory revolutionized the field of

185   evolutionary ecology, because it demonstrated that "non-optimal" traits may evolve when the payoffs (that is, the difference between the reproductive benefits of a given strategy and the costs of adopting it) of a resource-allocation strategy are evaluated in the presence of interacting individuals. We distinguish henceforth an individual optimal (the strategy maximizing the net reward for an individual regardless of what other individuals in the

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population do), from a collective optimal (the strategy maximizing the overall net reward

for a whole population of individuals), and from an evolutionary stable strategy (ESS, a

strategy that maximizes the net reward for an individual that selfishly interacts with other

individuals of the population, i.e. a strategy that cannot be invaded by any other strategy

adopted other individuals engaged in the game). While game theory provides methods to

solve for collective optimization (Pareto-optimality, see Pulliam et al. 1982), it is often

assumed that individual responses to biotic *interaction forces* follow ESS. We hope that

the following two examples –the arms race of plants in competition for light and the

tragedy of the commons in competition for soil resources– will clarify, for unfamiliar

readers, the meaning of this important game-theoretical concepts and models.

Game theory predicts that plants competing for light should engage in an arms race

(Falster and Westoby 2003, Dybzinski et al. 2011). In ecology, an arms race can be

defined as a reciprocal, unstable runaway escalation between two interacting parts

(Dawkins and Krebs 1979). To understand the arms race in competition for light, let's

picture a plant as a photosynthetic crown placed on top of a woody trunk. The crown area

of plant will determine its potential to intercept light and therefore, its yield. The

individual optimal strategy for plants is to invest all their resources into growing a flat

photosynthetic crown at the ground level (**Figure 4a**). By increasing the sunlight

interception, the plant will multiply the amount of foraged resource at each time step.

However, in interaction with neighbor plants, competition for light is asymmetric (taller

individuals get most of the resource and shaded individuals almost none). Therefore, a

plant may benefit from investing some resources into growing its trunk, surpassing the

height of its neighbors, and thereafter growing its crown. Nevertheless, if neighbors show

this same behavior, all plants in the community end up investing most of their resources

into conflict without getting any clear benefit from it (**Figure 4b**). Indeed, trees invest

215   about 80% of their biomass in growing robust columns of wood on top of which they

place their leaf canopy (Poorter et al. 2015). If trees cooperated, they would have the

exact same crown area exposed to sunlight, but at the level of the ground (**Figure 4c**),

thereby intercepting the same light at a much lower cost. In that case, all the energy

gathered from sunlight could be invested in reproduction.

220   When it comes to competition for soil resources, game theory predicts that plants engage

in a tragedy of the commons (Gersani et al. 2001, Zea-Cabrera et al. 2006). That is, the

collective action of a group of individuals acting independently and according to their

own self-interest leads to the depletion of the shared resource (Hardin 1968). To

understand this counterintuitive concept of a tragedy of the commons in competition for

225   soil resources, let's now imagine that a plant has access to a patch of soil with 100 units

of resource. In this patch, the plant can grow roots at a cost of 8.66 units of resource per

root, and each new root increases total foraging by half the amount of remaining resource

in the patch, i.e. the first root would uptake 50 units, the second root would increase the

total uptake by 25 units, the third root by 12.5, and so on. For a single plant, this increase

230   in uptake is the marginal gain that each consecutive root has for the plant. Importantly,

this means that the allocation of new roots reduces the resource uptake per root of

preexisting roots (hereafter, new roots "steal" resources from pre-existing roots). For

example, in the two-root scenario the average uptake per root is $75/2 = 37.5$, therefore the

second root has stolen from the first one 37.5-25=12.5 units of resource. In this

235   hypothetical scenario, the plant will not grow more than three roots, because the marginal

benefit of a fourth root is lower than its allocation cost (6.25<8.66) (**Figure 4d**). Next,

consider that a second plant accesses the same patch inhabited by the three-rooted plant.

The marginal benefit of the new plant allocating a first root is 23.43 (which coincides

with the average uptake per root [50+25+12.5+6.25]/4). Notice that the marginal benefit

240 of the second plant allocating its first root is different from the first plant allocating a

fourth root (6.25). This is due to the fact that, because new roots reduce resource uptake

of pre-existing roots, the new plant steals from its neighbor! The second plant still benefits

from allocating a second and a third root in the same patch, and this whole process repeats

if a third individual colonizes the patch, then a fourth, and so on (**Figure 4e**). The more

245 plants colonize the patch, the more roots, and the less efficiently plants forage resources.

This exploitative process can continue with a limit set by the point at which the cost of a

root equals the average uptake per root (with 11 roots in our example). As plants

increasingly deplete the resource in the patch, the net gain goes to zero. This theoretical

prediction is supported by some empirical evidence of increased root allocation of plants

250 in response to the presence of neighbors (Maina et al. 2002, O'Brien et al. 2005, but see

Semchenko et al. 2007). In our example, the collective optimum (maximization of the net

gain) is attained with three roots, regardless of how many plants they belong to (**Figure

4f**).

In their review, Mcnickle and Dybzinski (2013) address cases, beyond competition for

255 light and competition for soil resources, in which plants may engage in a tragedy of the

commons, such as the case of attracting or repelling allies or enemies. As in the examples

addressed before, the allocation of resources to plant defenses against enemies must not

be seen as an individual optimization of developing defenses. The strategy of the

neighbors must be considered too, since neighbors can deflect enemies to the focal plant

260 by investing more in its own defense. Similarly, low plant investment in attracting allies

can limit the availability of such allies in the non-attractive local environment, yet too

much investment by neighbors can increase competition for them by decreasing the rate

at which they visit the focal plant. While necessary to capture the relevant ecological

responses of plants to *interaction forces*, Mcnickle and Dybzinski (2013) conclude that

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265   the game theoretical approach is still not widespread in the plant community ecology

literature.

3- Scaling up to the net interaction

The different *interaction forces* and the phenotypical responses of plants scale-up leading

270   to the emergence of *net interactions*. Our understanding of this integration process is very

poor (Filazzola and Lortie 2014). A first step towards linking *net interactions* to the

underpinning mechanisms is to have a clear idea of what a *net interaction* is. In general,

the *net interaction* is the net effect the neighbor has on the fitness of the focal plant, i.e.

the success at passing its genes to the next generation (Hamilton 1964). While simple to

275   state from a theoretical perspective, evaluating the actual fitness of an individual plant is

almost impossible empirically. Hence, researchers need to resort to indicators that can be

measured in the field, such as the allocation of biomass into reproduction, hereafter

fecundity. The fitness-fecundity relation depends on many factors –differences between

pollen or ovules (Primack and Hyesoon Kang 1989), seed number to seed size ratio

280   (Geritz et al. 1999), diminishing returns of increased seed sets (Campbell et al. 2017)–

but fecundity is generally considered a good indicator of fitness. *Net interactions* are often

assessed by comparing a plant's fecundity measures in the presence and (all else equal)

in the absence of a neighbor of interest (**Figure 5**, red arrow). Proxies such as dry biomass

or growth rates tend to correlate well with fecundity in plants, and are often used as

285   surrogates (Younginger et al. 2017). Indexes to calculate the *net interaction* based in this

type of observations exist (Armas et al. 2004). A recent study has showed that the

direction of the observed *net interaction* among plants may, however, depend on the

fecundity surrogate (dry biomass, seed germination, or plant survival), indicating that

empirical observations of *net interactions* must be interpreted with caution (Lozano et al.

290   2017). From a mechanistic perspective, this is a non-surprising finding as *biophysical*

processes may affect differentially these measures: For instance, **(21)** attracting allies

such as pollinators will increase the focal plant's seed yield but it seems unlikely that it

would affect its not somatic plant biomass, **(1)** competition for light seen as an arms race

should increase plant biomass at the expense of reproductive allocation, and **(10)** increase

295   soil moisture will potentiate plant somatic growth but there is uncertainty on how it should

affect reproductive yield. All in all, two main questions need to be addressed in order to

dive into the mechanisms underpinning plant *net interactions*:

First, how can we make a connection between *biophysical processes* and the observable

net interaction? This question remains open, and very few studies have tried to address

300   the complexity of this problem. For instance, Valladares et al. (2016) reviewed how the

net interaction results from the integration of several *biophysical processes* focusing on

a *primary process*: canopy shade. Canopy shade is an interesting example, as it is linked

to diverse *biophysical processes* of different nature (light, water, and thermic stress) that

affect antagonistic *interaction forces* (see **Figure 2**). Shading is a ubiquitous competitive

305   mechanism that generates plant stress because it limits sunlight energy. However, in hot

arid conditions, shade activates positive *interaction forces*, potentially reducing water

stress, heat stress, and even photoinhibition of photosynthesis. This approach (i.e.

focusing on a *primary process*) is particularly interesting for empirical researchers

because *primary biophysical processes*, like shade, can be artificially manipulated in

310   experimental setups keeping all the other variables under control (De Castanho and Prado

2014). A different way to tackle the integrative study of the interaction mechanisms is

from a resource-based perspective. For instance, Butterfield et al. (2016) simulated water

flows in soils and plants in order to test whether facilitation interactions could emerge,

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and, if so, under which conditions. Of course, water-related *interactions forces* are not

315   imposed in their model, but they rather emerge from the abiotic and biotic water

movements. This alternative approach (focusing on *biophysical processes* around a

specific resource) is advantageous for modeling, as models can simulate the flow of a

resource through the ecosystem physical parts. A resource-based theoretical approach

requires modeling the fluxes of a given resource in the habitat of the focal plant with and

320   without the interacting neighbor, and the difference in environmental stress between both

conditions is a mechanistic explanation to the difference in fitness that the focal plant

experiences (**Figure 5**, water flows and blue arrow).

Second, how do plants respond phenotypically to several *interaction forces* entangled

with each other in highly nonlinear ways (Meron 2015)? Ecologist have long been

325   interested in the study of plant strategies to cope with resource co-limitation. For instance,

Bloom et al. (1985) developed the optimal foraging hypothesis, stating that plants will

adapt their phenotype so that all essential resources are equally limiting. More recently,

and in the frame of evolutionary game theory, McNickle et al. (2016) developed a triple

game theory model of allocation of biomass to leaves, stem and roots. They noticed that,

330   while classic-optimality life-history models predict that plants should allocate all their

resources into reproduction after reaching a threshold size (Bazzaz et al. 1987),

observations from forests show that trees invest less than 10% to reproduction (Luyssaert

et al. 2007). From an original approach that combines the ESS of plants in aboveground

and belowground competition, they predicted that plants forage inefficiently, over-

335   allocating resources into roots, stems, and leaves, at the expense of their lifetime

fecundity. The model, in which allometries emerge naturally from allocation strategies

rather than being imposed, was surprisingly successful at predicting the physiognomy of

vegetation in the different biomes. For instance, plants with less stem than roots or leaves

were more abundant in habitats corresponding to shrubland biomes, while plants

340   investing most to stems dominated in wet tropical climates.

4- The effect of the distance between plants on interactions

The zone of influence of a plant, defined as the space circumscribing all other individuals

that interact with the focal plant, is a concept developed in the late sixties (Opie 1968)

345   underscoring for the first time the importance of spatial configuration in plant community

ecology. The introduction of this concept fostered the development of statistical methods

to infer the range and sign of *net interactions* between plants from spatial point patterns,

starting with the Ripley's K index (Ripley 1978). Statistical spatial correlations can be

used as a proxy to many ecological processes (McIntire and Fajardo 2009), providing an

350   alternative approach to empirically reporting *net interactions* from the observation of

fitness differences. For instance, clumped vegetation patterns must be observed when

there is *facilitation* (Haase et al. 1996) but over-dispersed patterns emerge under

interference when *competition* is asymmetric (Stoll and Bergius 2005). The field of

spatial plant ecology has been extensively developed (for a comprehensive review of

355   spatial correlation techniques see Dray et al. 2012, and of the ecological importance of

patterns and scale see Chave 2013). Here, we focus on the scarcer literature studying

mechanisms underpinning the change in *net interaction* with increasing distance between

two plants.

Probably, the first *interaction force* that was explicitly suggested to vary with the distance

360   between two plants is the effect of a plant attracting enemies (herbivores or diseases) to

another plant, as stated by the famous Janzen-Connell hypothesis (Janzen 1970, Connell

1971). Generally, all *interaction forces* in **Figure 3** and all *biophysical processes*

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described in Section 1 must vary in intensity with the distance from an influencing plant.

Normally, they may progressively lose strength with increasing distance to the plant

365   center. In a very particular case, two antagonistic *interaction forces* are spatially

complementary: **(3)** competition for runoff water happens in bare soils at intermediate

distances from the plant because plants **(10)** increase soil moisture under their canopy.

Indeed, both *interaction forces* rely on the same *primary process*: the ability of the

influencing plant to increase infiltration by altering the soil's structure (**Figure 6a**). This

370   particular case underscored for the first time the possible emergence of scale dependent

feedbacks (SDF) in *net interactions*, meaning that the *net interaction* may switch sign at

different plant-plant distances. Based in these specific two *interaction forces*, one can

expect *facilitation* when plants are close by, but *interference* when they are farther away

(Bromley et al. 1997). This particular type of SDF is sufficient to give rise to particular

375   spatial patterns in semi-arid open-canopy vegetation, such as vegetated spots or bands

(Hillerislambers et al. 2001), as well as to globally bistable systems threatened by

catastrophic, irreversible desertification events (Rietkerk et al. 2004). These models of

spatial pattern formation have received great attention until today (Rietkerk and van de

Koppel 2008, Borgogno et al. 2009b, Zelnik et al. 2013, Martínez-García and López

380   2018). However, from a mechanistic point of view, they are probably excessively

simplistic because they only account for two complementary *interaction forces*.

All *interaction forces* must vary with space, and at least to a certain extent, they are

spatially independent from each other. To understand the change in *net interaction* with

increasing distance between the plants, which may be either a sign switch or just a

385   strength decay, the scaling-up of *interaction forces* to *net interactions* needs to be applied

independently at each distance from the influenced plant. Very few studies have done so,

but a particular example serves to illustrate this idea. The example is provided by the

work by Trautz et al. (2017), who studied two independent, antagonistic water-mediated *interaction forces*: **(3)** competition for soil water and **(6)** increase in atmospheric water

390   potential. Competition for soil water had a stronger (negative) effect on water stress for the focal plant within the root crown of the influencing plant. However, by transpiring water that is transported by wind, the influencing plant reduced water stress in its surroundings outside its root crown (**Figure 6b**). This study has two important implications. First, it shows how *interaction forces* spatially independent from each other

395   may cause a shift in *net interaction* with the distance between plants (the former case was based in two dependent *interaction forces*). Second, it shows that, when investigating different water-related *biophysical processes,* one could find cases of SDF different from the classic SDF used in spatial pattern formation studies (e.g. *interference* when the plants are close by and *facilitation* when they are farther away). However, it still leaves open

400   the question of what *net interaction* would result from the integration of all the water-related *biophysical processes* (shown in **Figure 5**).

To end this section, we discuss how individual phenotypic responses to *interaction forces* change with distance between individuals. Because most game-theoretical models investigating plant behavioral responses are not spatially-explicit, this question remains

405   largely unexplored. There is very little literature addressing this problem, as indeed most game theoretical models of plant ecology are not spatially explicit. However, a recently published theory, based in the exploitative response of plant roots to water dynamics in the soil, predicts that plants over-proliferate roots and thus engage in a tragedy of the commons in response to near neighbors, but under-proliferate roots when neighbors are

410   further apart (**Figure 6c**) (Cabal et al. 2020). This novel theory reconciles the two seemingly opposing hypotheses in root foraging literature discussed above, root territoriality (which intuitively led to assume under-proliferation) and the tragedy of the

commons. It also highlights the importance of incorporating spatial processes in plant game-theoretical models.

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5- A dynamic view of the net interaction

The *biophysical processes* and the plant phenotypic response to *interaction forces* vary with time and space. This might be due to changes in the distance between the plants, in the functional traits of the interacting plants, and in the environmental conditions (**Figure 7**). In order to mechanistically explain the *net interaction* between two given plants in a given location and moment, researchers need to account for the dynamism of these drivers. In the previous section, we reviewed the case of the distance between plants. In the following, we will discuss how spatiotemporal changes in environmental conditions and plant functional traits modify *net interactions*, and their implications for a mechanistic study of plant interactions.

Firstly, the environment quality is a major driver of changes in *net interactions*. Grime (1973) reported, for the first time, on more intense *competition* with increasing environmental quality. Later, *facilitation* among plants started to interest community ecologists (Hunter and Aarssen 1988), leading to the development of the stress gradient hypothesis (SGH). The SGH states that positive *interaction forces* may dominate with increasing environmental stress, allowing the emergence of *facilitation* (Bertness and Shumway 1993). It mostly predicts the prevalence of *facilitation* or *interference* in relation to spatial variation in habitat conditions (Maestre et al. 2005), but temporal heterogeneity may also produce switches in the sign of *net interaction* at the scale of days (Wright et al. 2015), seasons (Breshears et al. 1998, Kikvidze et al. 2006) and even between years (Valladares and Pearcy 2002, del Río et al. 2014). A variation of the SGH

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(the so called hump-shaped SGH) suggests that, while *facilitation* may emerge under increasing stress in mild environments, the *net interaction* may switch back to *interference* under extreme stress conditions (Holmgren and Scheffer 2010). This

440　collapse of facilitation has been reported in water-limited habitats (Maestre et al. 2003), cold climates (Koyama and Tsuyuzaki 2013), and along gradients of grazing intensity (Michalet et al. 2014). Nevertheless, *facilitation* has been reported in one of the most inhospitable land surfaces on earth: Antarctica (Molina-Montenegro et al. 2013).

From a mechanistic point of view, environmental conditions modify the *biophysical*

445　*processes* that underpin plant interactions. While many studies report changes in *net interactions* across stress conditions, very few studies accurately report the *biophysical processes* responsible for those changes. We have argued that by modeling the *biophysical processes* related to a specific resource, we could explain mechanistically the difference in fitness a that plant experiences in the presence of a neighbor (see **Figure 5**).

450　Indeed, the model we used as an example to illustrate this in Section 3 (Butterfield et al. 2016) incorporates environmental variation. By running their simulation under different environmental conditions, the authors could compare changes in water stress in the presence or absence of a shrubby neighbor in different habitat conditions. They concluded that the effect of a shrub on altering water stress conditions was different under changing

455　precipitation regimes. They found, for instance, that the positive effect of shrubs on superficial soil water decays with a decrease in precipitation, giving support to a hump-shaped SGH. Also Anthelme et al. (2012) evaluated empirically the effect of nurse plants along an altitude gradient. They observed *interference* in low altitudes but *facilitation* at higher stress conditions. They then measured the *interaction forces* involved and

460　identified **(9)** soil nutrient enrichment and **(10)** increase in soil water as the main drivers.

The type of data they gathered represents a first step towards the mechanistic understanding of shifts in *net interaction* across environmental gradients.

Secondly, the functional traits of the two interacting plant are a major driver of changes in *net interactions*. Global-scale studies relate the intensity and the sign of the *net*
465   *interaction* between plants to their functional traits (Kunstler et al. 2016, Fichtner et al. 2017). Plant functional traits have an evident genetic background that is species-specific (Pereira and Des Marais 2020). As a consequence, interaction studies report co-occurring cases of *interference* and *facilitation*, where shifts in *net interaction* depend only on the species identity of the influenced (Choler et al. 2001) or the influencing (Pugnaire et al.
470   2004) individuals. However, functional traits are far from being solely restricted to species identity (Cadotte et al. 2011). They vary with ontogeny, plant size being a paradigmatic example of that change. Some studies have reported shifts in the *net interaction* with increasing size of the influencing plants (Miriti 2006), of the influenced plant (Soliveres et al. 2010), and when both plants grow together (Schiffers and
475   Tielbörger 2006) within species pairs. Both species identity and the size of the individuals should be considered together as drivers of plant functional traits that affect *net interactions* (Álvarez-Yépiz *et al.*, 2014). Additionally, modern functional ecology underscores the need to account for the ample environmentally-induced phenotypic plasticity that ultimately has strong effect in plant *net interactions* (Valladares et al. 2007).
480   From a mechanistic approach, the functional traits of the influencing plant modify the *biophysical processes* underpinning plant interactions. For instance, shorter plants will have a smaller zone of influence (Casper et al. 2003), plants with higher specific root length may compete for soil resources more efficiently (Erktan et al. 2018), plants with deeper roots can increase superficial soil water trough hydraulic lift (Walter 1971), or
485   plants with higher leaf-area index will produce a more intense shade (Jordan 1969). The

treatment of functional traits variation needs to be careful, as the plant will respond with plasticity to both the *interaction forces* from other plants (already tackled in Section 2) and to abiotic factors addressed here. Discerning the phenotypic plasticity of a plant in response to environmental change, and the phenotypic variation produced within a given

490   habitat by the presence of neighboring plants is an arduous task.

Environmental sciences need to provide predictions of major ecologic features in the frame of the current anthropogenic global crisis. Understanding global-scale spatial and temporal vegetation responses to climate change, mediated at least partially by plant interactions, is necessary to provide these answers (Scheiner et al. 2011). Our current

495   understanding of plant ecophysiology presumably provides tools to start approaching a theoretical treatment of this problem, but its complexity, as depicted through this Concepts and Synthesis, is enormous. Some studies have tackled multi-level effects phenomenologically. For instance, Wright et al. (2014) showed how both biotic (ontogeny) and abiotic (circadian cycles and seasons) temporal factors together drive

500   complex, continuous changes in the *net interaction* between two plants. Bonanomi et al. (2016) provided an example of how both the direct abiotic effect of environmental stress and plasticity in the phenotypic response of influencing plants to that stress drive in combination spatial changes in the *net interaction*. Metz and Tielbörger (2016) considered the spatiotemporal variation altogether, reporting *facilitation* only in certain

505   locations and at specific times at which stressful environmental conditions arise. However, we are still far from a mechanistic framework that, based on *biophysical processes*, would allow us to predict how *net interactions* vary in time and space with the distance between plants, the functional traits of the plants, and the environmental conditions in which the interaction takes place.

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6- Conceptual approaches to plant interactions

Plant communities can be studied at various scales, from plant foraging organs, to individuals, to populations, to the whole community (**Figure 8a**). In this section, after recapitulating the strengths and weaknesses of models that focus on each of them, we

515   discuss the necessity of developing a new approach to plant community ecology in which plant *net interactions* are not assumed but emerge naturally from a detailed description of their underlying *biophysical* and physiological *processes*: the *plant interaction models* (PIMs). We claim that PIMs need to abandon the current focus on the species identity of interacting individuals and, at least in their initial development, they should move towards

520   an explicit description of discrete plant individuals, the spatial structure of the community, and surrounding environmental factors. The development of this models may open the doors for a new conceptual approach to the mechanistic study of plant interactions, yielding hypothesis that could be empirically tested.

Following the course of history, the first approach to study populations of interacting

525   agents dates back to the logistic equation for intraspecific competition (Verhulst 1845). Later work by Lotka, Volterra, and others extended this model to systems with more than one species and to other ecological interactions, specially prey-predator (Lotka 1920, 1924, Volterra 1926). At least two factors explain the great success of this family of demographic models during the last century. First, they provide good fits to empirical

530   observations. Notably remarkable are the experiments by Gause et al. (1934) to test intraspecific competition in populations of paramecia and the data from the Hudson's Bay Company on fluctuations of lynxes and hares in Canada, that confirmed predictions of prey-predator models (Hewitt 1921). Second, because demographic models focus on the species identity of the interacting agents and are mathematically tractable (Wangersky

535   1978), they allowed researchers to identify simple rules that allow coexistence between

antagonistic species (Hardin 1960). The term "species interactions" has, indeed, been widely used to refer to this demographic approach (see Thompson 1999), yet we refrain from its use as it may lead to confusion. Despite being initially well received and generally acknowledged for several decades (Jeltsch et al. 2008), this approach may

540   currently be no longer so popular among plant ecologists (Reiners et al. 2017).

A first, evident limitation of this population-level approach is based on the fact that plants are sessile organisms and thus interact only with their neighbors. The concerns for the poor suitability of these models to plant communities was probably first raised by Fagerström (1988), who highlighted that sessile organisms must only compete with close

545   neighbors, and supported the use of spatially explicit approaches. Interactions in both Verhulst and Lotka-Volterra equations rely on the so-called law of mass action, which assumes that individuals occupy the entire population range uniformly and are equally likely to interact with each other provided that their trajectories intersect by chance (Hutchinson and Waser 2007, O'Dwyer 2020). These assumptions have been shown

550   inaccurate for many motile organisms, which often show non-uniform space occupation patterns (i.e., home-range), long range perception, and complex foraging behaviors (Hein and McKinley 2013, Hein and Martin 2020, Martinez-Garcia et al. 2020). In sessile communities, the interaction is highly dependent on the distance between individuals and population-level models based on the law of mass action are an overlying approach (see

555   section 4). In addition to the limitations caused by model assumptions, plant demographic empirical studies are generally labor intensive, as they require large sample sizes, long-term, long-range data sets, and large arrays of variables (Ehrlén et al. 2016). The analysis of demographic-level data to asses biotic interaction may be prone to strong statistical biases in the detection of negative density-dependences, which questions a large body of

560   literature explaining plant species biodiversity across biomes (Detto et al. 2019). This

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problem is magnified by the fact that most species coexistence studies are observational, making difficult to control for the variability in neighbors and leading to omitted variable biases in estimated effects of neighbors on targeted plants (Rinella et al. 2020).

Besides these concerns, we argue that these population-level models are by itself limited by the strong focus given to the species identity of the interacting individuals. We have reviewed in detail the several *biophysical processes* that affect plant interactions, and shown that the effect of many of them acting simultaneously may depend significantly on factors that are not related to species identity. One example is the distance between plants, which may be responsible for a switch in the sign of the interactions between any pair of individuals. Another is the ontogeny of a plant, which may have a higher impact on plant functional traits than species identity. As a simple example, a tree seedling has functional traits that resemble more those of herbaceous plants than those of adult individuals of its own species (Niklas et al. 2007), the most obvious one being its overall size. Therefore, the way this seedling interacts with other plants will be more similar to the way herbaceous plants rather than adult trees of its own species do. All in all, the ontogeny or the distance between two plants have mechanistic effects on the *net interaction* that may eclipse the potential effects of species identity. In summary, this non-spatial demographic approach, also termed well-mixed, is unable to incorporate all the mechanistic complexity underpinning plant interactions, and hence it is necessarily phenomenological.

All the abovementioned concerns claim for the need of a better mechanistic consideration of plant-to-plant interactions that, at least, incorporates explicitly the spatial structure of the community. Two alternative modeling approaches developed during the last decades of the XXth century: The individual-based approach (Bella 1971) and the plant-*continuum* approach (Lefever and Lejeune 1997, Klausmeier 1999). Most individual-based models (IBM) are computer simulations of individuals interacting in a spatial environment

composed of independent grid cells of the size of the crown of an adult plant. The first

vegetation dynamics IBM of this kind is probably *jabowa* (Botkin et al. 1972), and this

approach has received considerable attention since. Various modeling advances have

been developed, such as *foret* (Shugart, and West 1980) which incorporated dependence

590   between the cells in the grid, and *sortie* (Pacala et al. 1996) which was the first fully

spatially-explicit IBM. The other alternative to well-mixed demographic-level models is

the plant-*continuum* approach, based in partial differential equations (PDEs) for the

evolution in time and space of the density of vegetation biomass (Holmes et al. 1994).

PDE models for studying vegetation dynamics can be classified in two classes:

595   ecohydrological models, which consist of systems of two or more equations to describe

the interaction between vegetation and resources, usually water (Klausmeier 1999,

Rietkerk et al. 2002), and kernel-based models (Lefever and Lejeune 1997), which use a

single equation to describe the evolution of vegetation biomass. From a more biological

perspective, ecohydrological models explicitly describe scale-dependent feedbacks

600   between water and vegetation (**Figure 6a**), whereas kernel-based models follow an even

more phenomenological approach and encapsulate every feedback between plants and

their environment in the sign of the *net interaction* among plants. More sophisticated

models lying in each of these classes also include interactions between vegetation and

other organisms (Gilad et al. 2004, Bonachela et al. 2015, Tarnita et al. 2017), landscape

605   topography (von Hardenberg et al. 2001, Gilad et al. 2007), and different sources of

environmental or demographic stochasticity (D'Odorico et al. 2006, Butler and

Goldenfeld 2009, Martínez-García et al. 2013b, Eigentler and Sherratt 2020).

In their review, Meron et al. (2019) stand up in *pro* of the plant-*continuum* approach,

which, due to its higher mathematical tractability has indeed contributed crucially to our

610   qualitative understanding of several ecosystem-level processes in drylands, with special

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emphasis on desertification transitions (Rietkerk et al. 2002, Bonachela et al. 2015, Meron 2018, Fernandez-Oto et al. 2019). Moreover, the authors defend that, unlike IBMs in which the smallest scale is that of the individual, the plant-*continuum* approach incorporates a higher resolution in spatial processes because it describes continuous

615 biomass densities. As a result, it can capture processes that occur in a small area element, as small as needed. In doing so, however, plant-continuum models lose the track of individual plants and do not permit to quantify population sizes. We will in the following explain why, based in all the facts exposed through this *Review & Synthesis*, we consider that the individual-level is the correct biological scale to study mechanistically plant

620 interactions.

First of all, we agree with (Meron et al. 2019) that IBMs are mathematically less tractable than the ordinary differential equations of well-mixed demographic models or the partial differential equations of plant-continuum models. IBMs require, to a large extent, intensive computer simulations, but tools to treat them analytically also exist, e.g.,

625 moment closure methods such as the pair approximation (Matsuda et al. 1992, Ellner 2001, Iwasa 2010), and IBMs are suitable to model plant interactions in all the remaining characteristics shown in **Table 2.** In addition, while Meron et al. (2019) defend that plant-*continuum* models can function at finer spatial scales than IBM because they model biomass densities rather than individuals, we do not see a reason to state that spatially

630 explicit IBMs cannot incorporate processes happening at finer spatial scales that the individual scale, especially when they account for an explicit description of environmental conditions. Moreover, existing PDE-based models deliberately simplify many factors to keep mathematical tractability, which makes most of their results independent of the assumed *net interactions*. For instance, they predict that the shape of

635 the spatial distribution of plants correlates with water availability. Specifically, as

precipitation declines, prior to completely dying out, vegetation transitions from fully covering the system, to leaving regularly spaced gaps of bare soil, to forming labyrinthic shapes that resemble a tiger bush, to arranging in isolated spots. Worryingly, this sequence of patterns and the way they correlate with precipitation ranges is independent

640   of the *net interactions* that a specific model assumes (von Hardenberg et al. 2001, Rietkerk et al. 2002, Martínez-García et al. 2013a). Finally, plant-*continuum* models cannot track population sizes and individual growth properly. Using mortality as an example, individuals die with increasing cumulative probability, i.e. they do not only die due to resource limitations but also with the age of individuals, a feature that plant-

645   *continuum* models cannot incorporate. In addition, when an adult individual dies, a large, discrete spatial portion of biomass disappears altogether, whereas plant-*continuum* models only produce modular progressive decreases of biomass density.

But, probably, the most important strength of the individual-level approach is its potential to incorporate functional trait variation and game theoretical responses to *interaction*

650   *forces*. Functional trait ecology is a rising field that underscores the importance of phenotypic plasticity in plant traits rather than taxonomical identity in community ecology processes (McGill et al. 2006). Population-level approaches cannot incorporate this variability within taxa, and plant-*continuum* models do not incorporate it within the modeled plant mass. Indeed, neither of these approaches have the correct resolution to

655   incorporate phenotypic plasticity, which is inherently individual-level. Only trait-based IBMs can accurately represent the diversity and spatial complexity depicted by plant functional traits (Zakharova et al. 2019). The game theoretical response of plants to interactions is a paradigmatic example of the inevitability of an individual-level resolution in vegetation models. As we have shown with two examples in section 2,

660   individual plants may behave inefficiently when foraging a shared resource according to

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game theoretical ESS (Rankin et al. 2007). In particular, we have discussed in section 4 how a plant allocation to roots may change from over-allocation (tragedy of the commons) when close to neighbors, to under-allocation when farther away. How could phenomena like these be modeled without incorporating explicitly the individual plants

665   in space? Demographic and plant-*continuum* models are favored by their simplicity and mathematical tractability. However, they are problematically constrained in how much complexity they can account for, and thus cannot describe the highly complex mechanisms that underlie plant interactions.

To solve this problem, we argue that a new approach should be taken to study plant

670   interactions. Such new family of models, which we call *plant interaction models* (PIM), should focus on the individual and how it interacts with *biophysical processes*. This shift is mathematically challenging and will require, at least in the first steps, intensive computation. *Plant interaction models*, however, incorporate advantageous features from the population-level approach, such as the possibility of tracking population sizes, others

675   from the plant-*continuum* approach, such as high resolution in spatial processes, and unique features, such as accurately accounting for functional traits and the phenotypic plasticity of plants. By integrating all these features in a single theoretical framework, researchers will be able to investigate how their joint effect spontaneously generates a variety of *net interactions* that ultimately drive the dynamics of plant communities. PIM

680   not only have the potential to model plant interactions mechanistically, but also to produce hypothesis that can be tested empirically. For instance, researchers may be able to better understand plant facilitation, investigating in which conditions these positive interactions emerge and which positive *interaction forces* may be their principal drivers. For instance, PIMs may produce a better understanding of the nature of scale dependent

685   feedbacks in the wild, shedding light on the direction of the sign switch and the spatial

changes in *interaction forces* that drive it. This will ultimately allow researchers to understand how and in which conditions the changes of the *net interaction* with the distance between the plants is behind vegetation patterns. Another example is given by the possibility to yield testable predictions on the temporal dynamic of the

690   interference/facilitation switches, and how these may affect the species coexistence in mild and stressful habitats.

Conclusions

Although often assumed to be the net effect of a neighbor on a focal individual, we have

695   shown that plant interactions actually rely on copious *biophysical processes* and counterintuitive dynamical responses of plants. Concerns have been raised about the problems underlying the use of a phenomenological approach to plant interactions, claiming for the need to develop a mechanistic understanding that backup some relevant predictions on biodiversity patterns, climate change forecasts, or ecosystem dynamics.

700   We propose a new conceptual approach to the study of plant interactions from a mechanistic perspective, integrating the *biophysical processes* and the evolutionary stable strategies (ESS) of plants in relation to the spatial configuration of the sessile community, the functional traits of the plants, and the environmental conditions. We highlight that an individual-level approach is necessary for a fully comprehensive mechanistic study of

705   plant interactions, which can integrate *biophysical processes*, short-scale spatial structure, plant phenotypic plasticity, and ESS. The development of individual-based models incorporating *biophysical processes* and plants' ESS in which *net interactions* emerge are necessary to advance our mechanistic knowledge of plant interactions. Empirical studies reporting the mechanisms underpinning *net interactions* among individuals controlling

710　　for (but not focused in) the species identity of the individuals interacting may also significantly enrich our knowledge of this field. Only by incorporating the high complexity of mechanisms underpinning *net interactions* from an individual-level approach will the plant interaction ecology firmly stand on its own two feet.

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Tables

1080   **Table 1:** Glossary

Biophysical process	A local modification of the physical (or chemical) environment that is a direct or indirect result of the presence of a plant.	
Primary (biophysical) process	A biophysical process by which a plant directly modify its direct physical surroundings.	
Interaction force	A biophysical process by which a plant affects the environment of a neighboring plant in a way that has an effect on its fitness.	
	Competition	(*sensu* Grime, 1973) Trophic interaction force; plants compete for each quantum of light, molecule of water, or ion nutrient.
Net interaction	The net outcome of all the interaction forces, giving the net biological effect of a plant on the fitness of a neighboring plant.	
	Facilitation	(*sensu* Callaway, 1995) Positive directional net interaction.
	Interference	(*sensu* Harper, 1961) Negative directional net interaction.
Pairwise interaction	The complete (bidirectional) biotic interaction between two plants.	
Plant Interaction Model (PIM)	Family of models that focus on detailed description of the biophysical processes and plant phenotypic responses letting the net interaction emerge. As we argue they must be individual-based, incorporate the spatial structure of the community, and explicitly account for environmental factors.	

Table 2: The three classic modeling approaches to plant biotic interactions (from

1085   different biological scales): classic demographic models (population), individual-based

models (individual), plant-*continuum* models (foraging organs). ✖ cannot incorporate, ~

can poorly incorporate, ✔ can accurately incorporate.

Approach	Analytical tractability	Spatial processes	Biophysical processes	Population size	Trait variability	Game theory	Foundational paper and recent literature review for each approach
Population	✔	✖	~	✔	✖	✖	(Lotka 1924), (Jeltsch et al. 2008)
Individual	✖	✔	✔	✔	✔	✔	(Botkin et al. 1972), (Shugart et al. 2018)
Continuum	✔	✔	~	✖	✖	✖	(Lefever and Lejeune 1997), (Meron et al. 2019)

1090   **Figures**

a- Communitywise

b-Pairwise

c- Mechanistically

Increase humidity   Attract pollinators
Competition for light
Repel hervibores   Reduce abrassion
Reduce evaporation
Increase infiltration
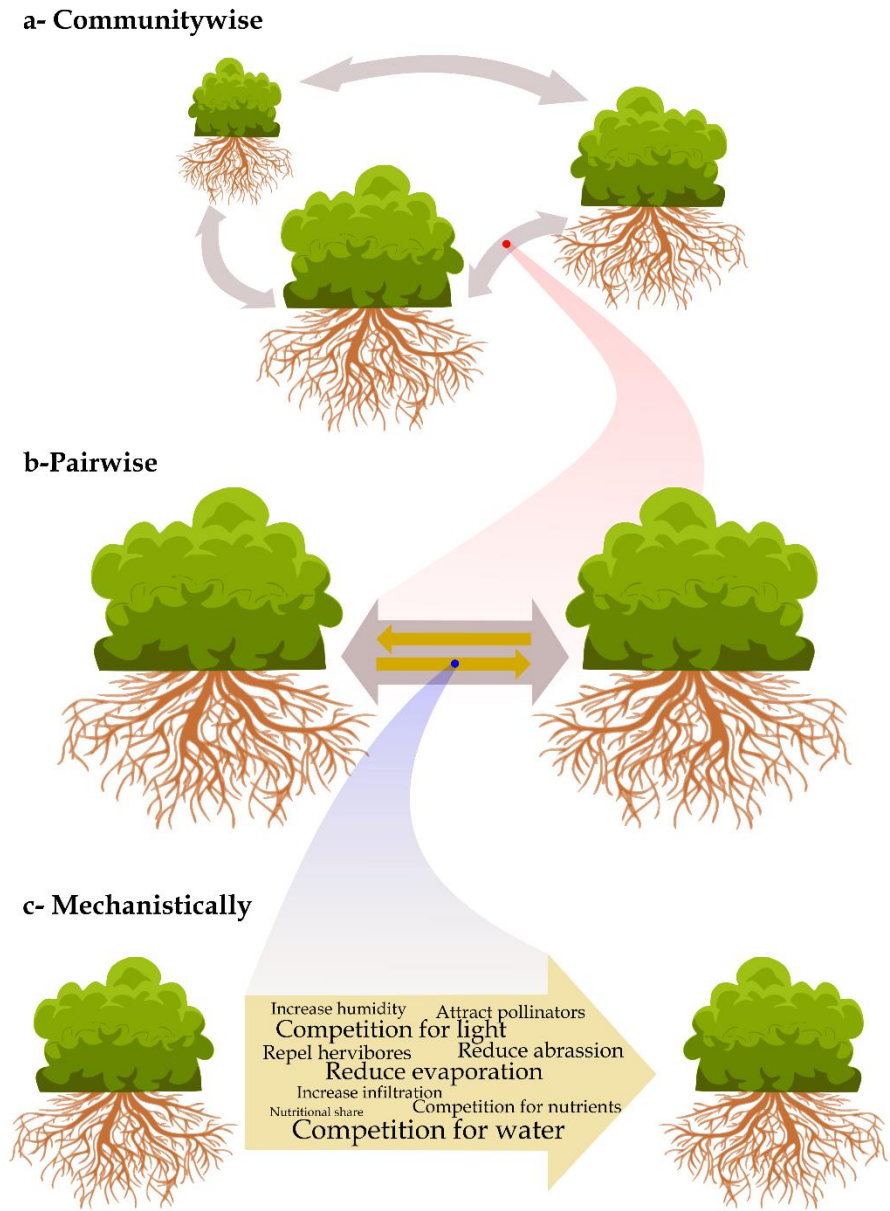Nutritional share   Competition for nutrients
Competition for water

Figure 1: Nested levels of biotic interactions among individuals: a- Communitywise, individuals can be assumed to interact with one another in *pairwise interactions*. b-Each *pairwise interaction* is actually composed of two directional *net interactions*. c- At the

1095   mechanistic level, the *net interaction* is the observable outcome of a diverse set of *biophysical mechanisms*.
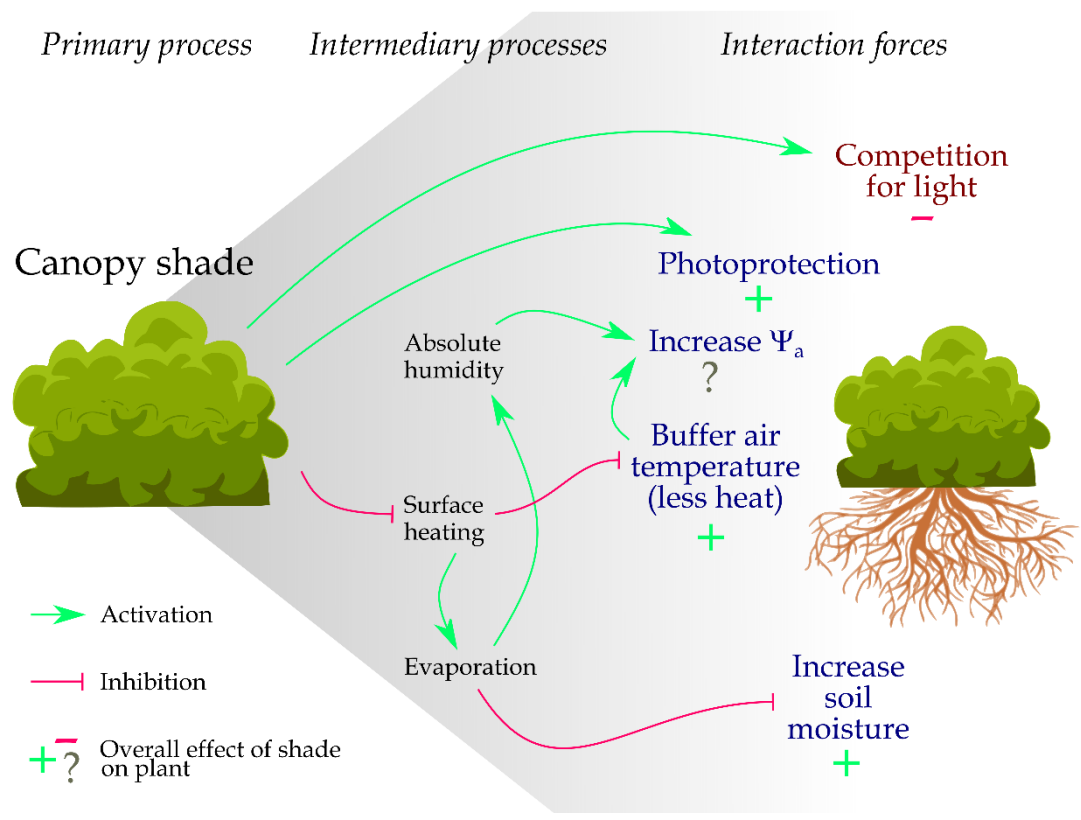
Figure 2: Schematic example of how a primary process, canopy shade, affect *interaction forces* in hot semi-arid and arid systems. The primary biophysical processes of plant interaction are defined as the direct biophysical modification of the habitat by a plant, ultimately (not directly) affecting the success of other plants growing nearby.
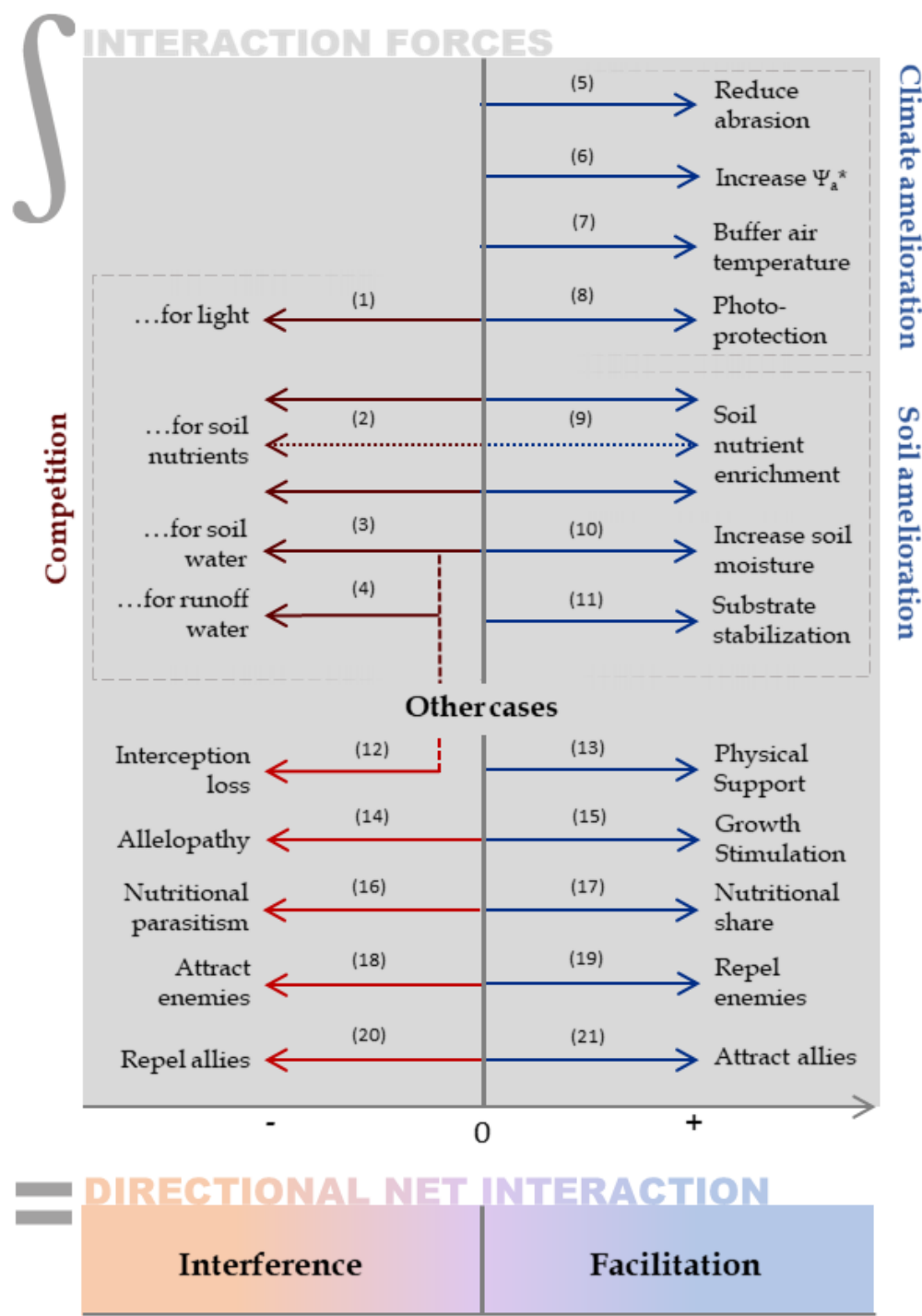
1100

Figure 3: Dissecting *net interactions*. Mathematical symbols on the left of the boxes are included to indicate that it is the integration of all *interaction forces* that determines a single directional *net interaction* value. Several arrows for soil nutrient forces represent the fact that there are different nutrients involved (N, P, K, etc.). Numbers nest to the arrows reference explanation in the text. *Atmospheric water potential.
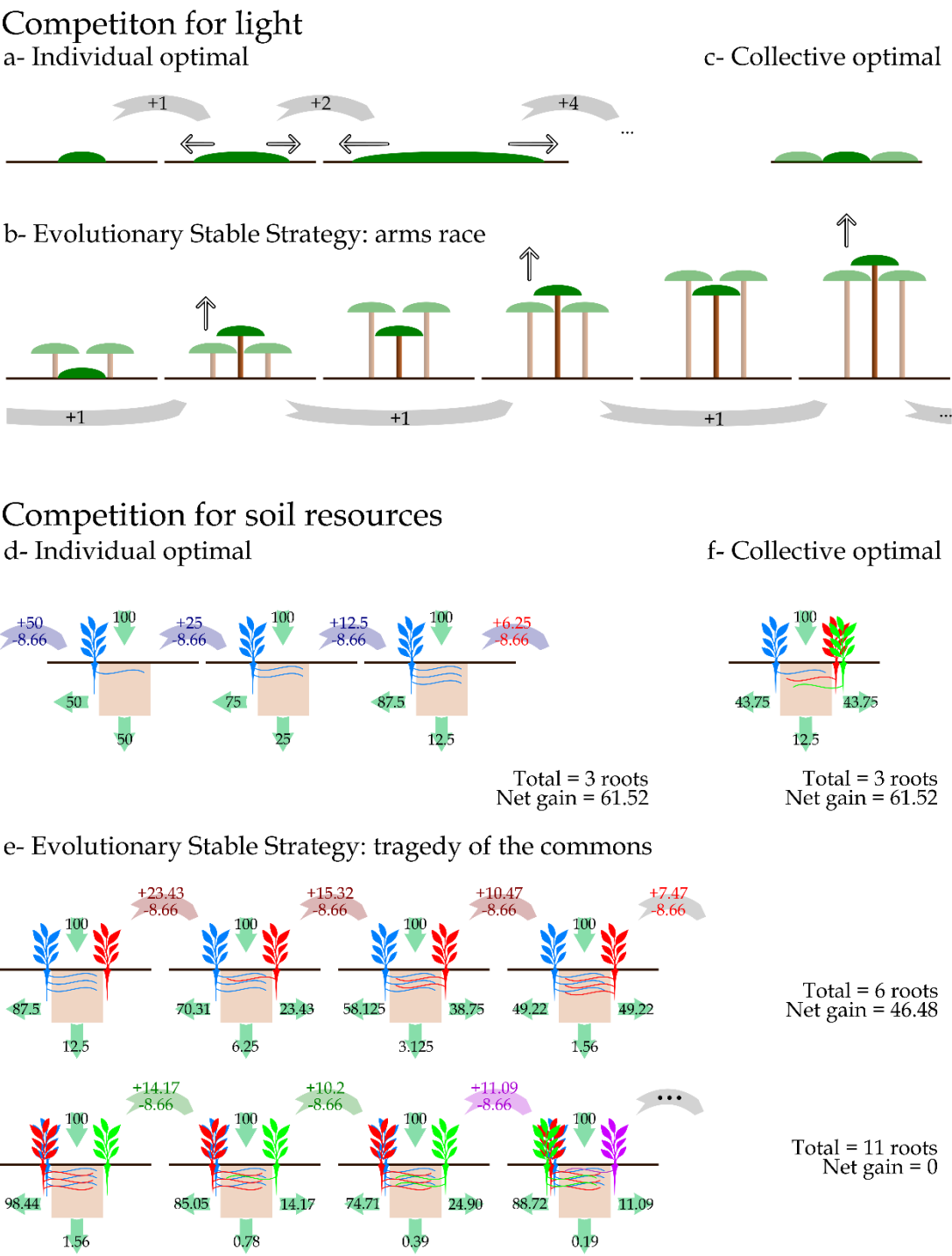
1105

Figure 4: Simplified examples illustrating the tragedy of the commons as a result of evolutionary stable strategies in plant competition for light and soil resources. In competition for light **a**- a plant with initial crown size 1 intercept 1 unit of sunlight and allocate this energy in growing out, doubling its crown area, hence its solar interception, and investing 2 in growing out in the next time step, and so on. But in the case of **b**- an

ESS, neighbors tend to overgrow the plant getting the benefit of asymmetric competition,

1115 hence the focal plant will invest 1 in growing up rather than out, reaching the canopy but

not increasing its interception area. This is different from the **c**- collective optimum in

which plant crown are territorial but plants do not invest in trunk either. In competition

for soil resources, **d**- a plant will decide whether to grow a root in a patch of soil where

100 units of resource are available depending on the marginal gain. In the case in which

1120 each root costs 8.66 units of resource, the first root uptakes 50 units, and each extra root

increase the uptake by 50% (2 roots uptake 75 units, 3 roots 87.5, 4 roots 93.75, and so

on) the plant will stop with two roots as the marginal benefit of adding a fourth root is

negative (93.75 - 87.5 - 8.66 = -2.41). One can calculate that **e**- the ESS predicts other

plants will find a marginal benefit of growing a fourth and more extra roots, as they will

1125 be stealing nutrients from other plants' roots. However, **f**- the collective optimum is

attained, like the individual optimum, when there are no more than 3 roots in the patch,

with which the plant community can maximize the net collective gain at a value of 61.52
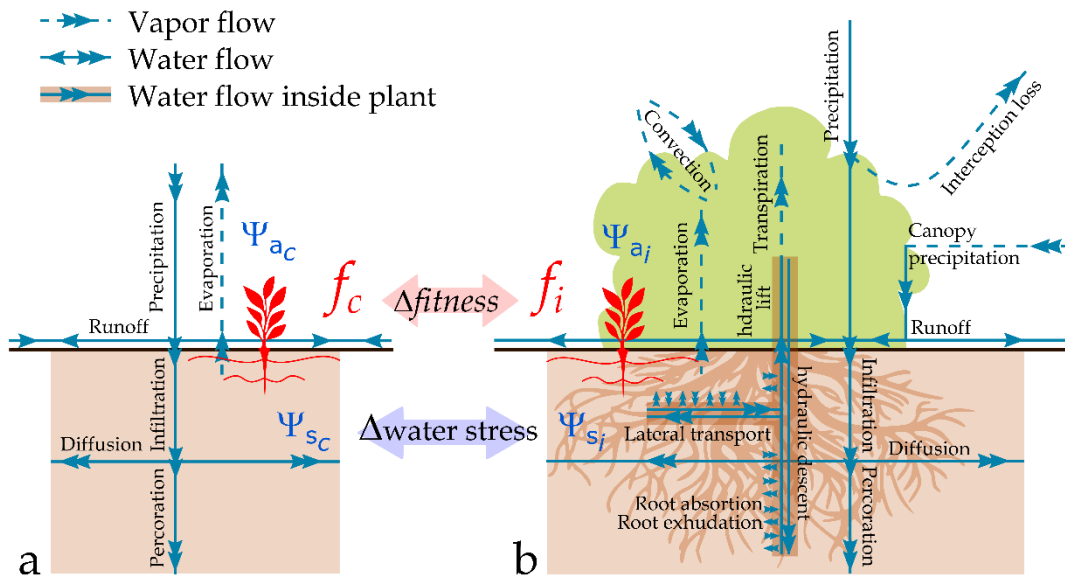
(= 87.5 - 3 * 8.66).

Figure 5: Schematic of two approaches to the *net interactions*. Phenomenological studies observe the effect of a neighbor (shrubby plant) on a focal plant (red plant), by measuring a fitness surrogate of the focal plant when growing **a**- alone (control, f_c), or **b**- in the presence of that neighbor all else equal (interacting, f_i). Alternatively, an integrative mechanistic study is based in comparing the control and the interacting physical environment of the focal plant. A possible approach to the mechanistic study would be to focus on a resource and consider how the neighbor alters the resource dynamics. In the figure, the resource is water, and modeling water fluxes **a**- with and **b**- without the shrubby plant allows to compare the water stress to which the plant is exposed through predictions of soil water potentials (Ψ_s) and atmospheric water potentials (Ψ_a).
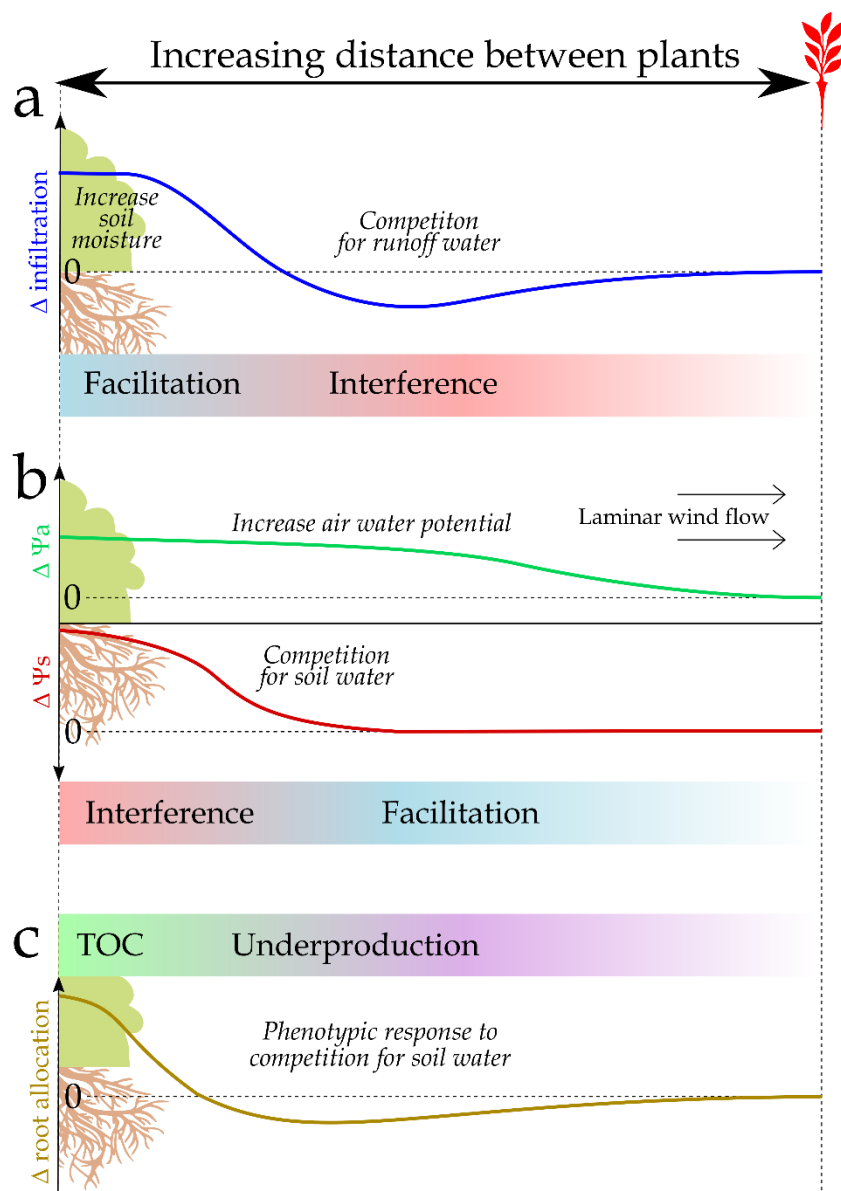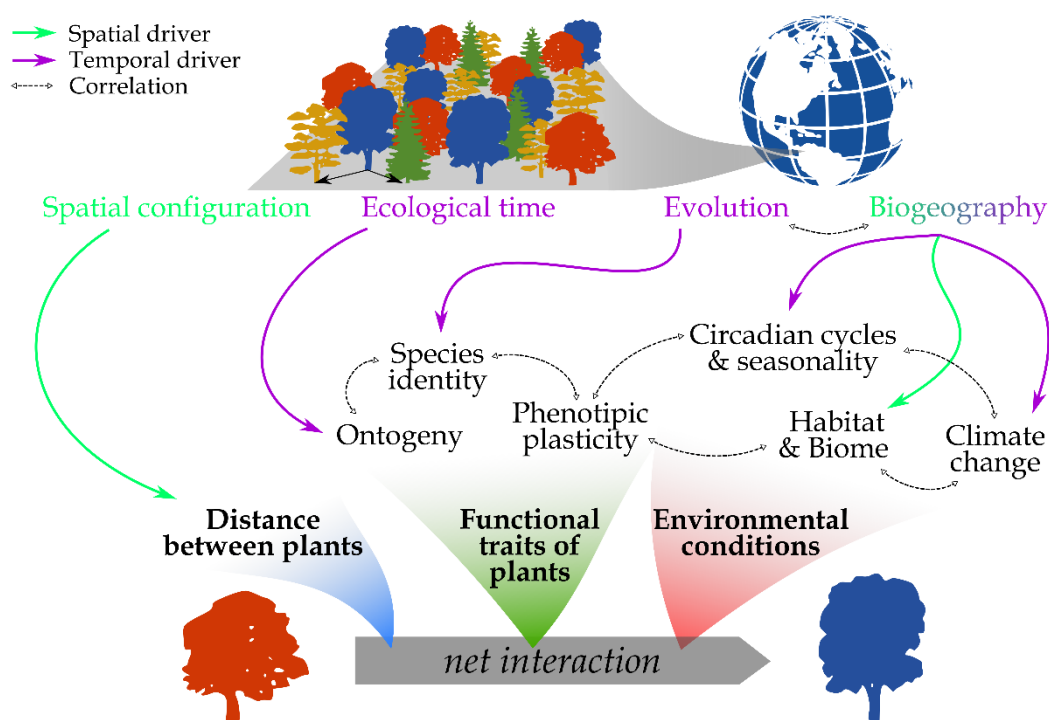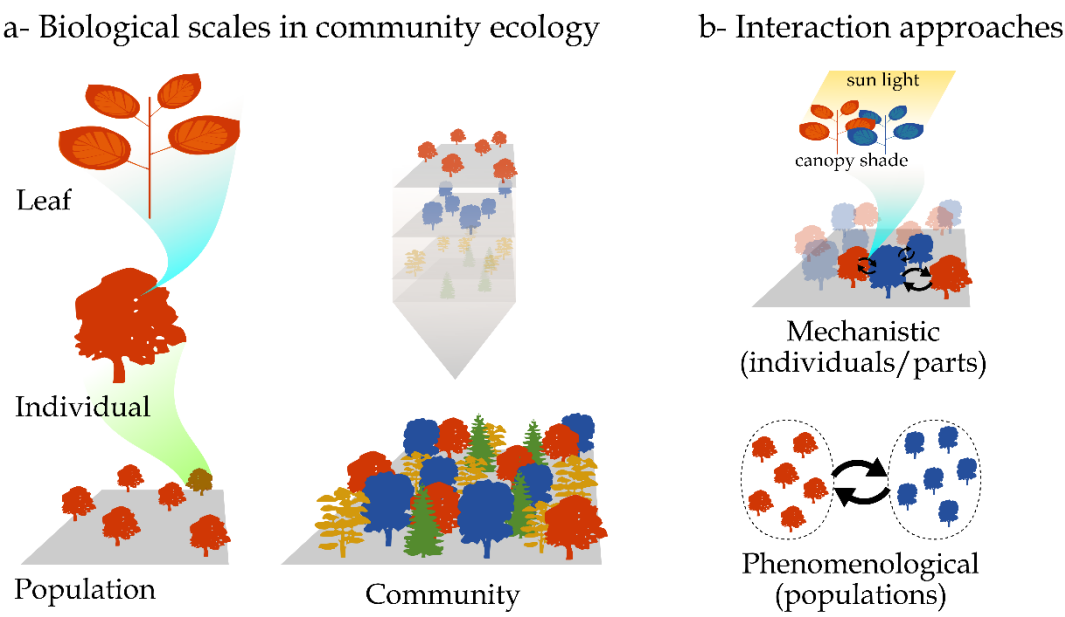
Figure 6: Schematic of how the distance between plants is an important driver of some interaction mechanisms. **a**- The classic SDF showing how short-range *facilitation* and long-range *interference* may emerge by plants altering soil infiltration capacity of soil. **b**-An alternative SDF showing how short-range *interference* and long-range *facilitation* may emerge from combining the *interactions forces* of competition for soil water and increase in atmospheric water potential acting at independent spatial scales. **c**- The space-dependent phenotypic response of plants to competition for soil resources.

Figure 7: Schematic of the main spatial and temporal drivers of the *net interaction*, mediated mechanistically by the distance between plants, the functional traits of the two plants, and the environmental conditions in which the interaction takes place.

a- Biological scales in community ecology   **b- Interaction approaches**

Leaf

Individual

Population

Community

sun light

canopy shade

Mechanistic
(individuals/parts)

Phenomenological
(populations)

1155   **Figure 8:** Schematic of **a**- the different biological scales of plant communities that are of

interest for ecologists and **b**- some examples of how the biotic interactions among plants

can be approached from these different scales.