



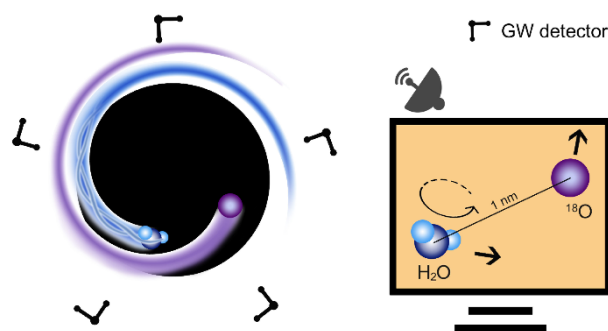
23 gravitational waves; entropy

24 General relativity points out that black holes (BHs) are regions of space-time within  
25 which everything is trapped, while quantum mechanics predicts that the BHs would  
26 evaporate through featureless Hawking radiation [1, 2]. Then the supposed “information  
27 loss” would destroy the unitarity of quantum mechanics. Physicists have proposed a  
28 variety of hypotheses to solve this problem, while there has been no final resolution yet  
29 [3].

30 More than a century ago, Albert Einstein predicted the existence of gravitational  
31 waves (GWs), which were first directly detected in 2015 from a binary BH merger event  
32 [4]. The waveforms from the inspiral, merger of the two initial BHs and the ringdown  
33 of the final BH carry to us the information about the masses, spins and some orbital  
34 elements [4-8]. From a different perspective, binary BH merger equals the infall of a  
35 smaller BH into a larger one. One may wonder, if the information of the smaller BH can  
36 be transmitted out of the larger one’s boundary (event horizon) through GWs, then why  
37 that of other matter can’t?

38 GWs are generated by time variations of the mass quadrupole and higher-order  
39 multipole moments of the source [4, 9]. When GWs are emitted, energy is carried away  
40 and thus the system pulsations are reduced. The GWs from a massive point particle  
41 falling into a BH are being calculated with increasing accuracy [5, 10-12]. The efficiency  
42 at which the energy is emitted out with GWs depends on the symmetric mass ratio of  
43 the binary system [10]. When system asymmetry increases, higher multipoles will have  
44 increasing relative importance [4, 13, 14].

45 Now we can imagine an extremely asymmetric binary system with a mass ratio of  
 46 approximately  $1 \times 10^{-57}$ : an infalling water molecule ( $\text{H}_2\text{O}$ , hydrogen-1 and oxygen-16)  
 47 and a  $15 M_{\odot}$  BH. In the present paper, only the GWs from the falling matter are  
 48 discussed for simplicity. During the infalling process, the GWs from the  $\text{H}_2\text{O}$  molecule  
 49 can be seen as single-sourced GWs containing weaker contributions from subdominant  
 50 multipoles, or as the superposition of separated waves from three atoms (H, O and H).  
 51 When the molecule falls with angular momentum, more detailed information would be  
 52 encoded in the waveform [15, 16]. If a spherical oxygen-18 atom ( $^{18}\text{O}$ ) with similar mass  
 53 falls together with the  $\text{H}_2\text{O}$  molecule, the GWs from them would be substantially  
 54 different, largely because their mass distributions and, when they spin, angular  
 55 momentum are different. Together with more contributions from higher multipoles, the  
 56 information about atomic or molecular species is encoded in the GWs.



57

58

59 **Fig. 1. An ideal scene of GW emission and detection.** An asymmetric  
 60 spinning  $\text{H}_2\text{O}$  molecule and a spherical  $^{18}\text{O}$  atom fall nonradially into a BH,  
 61 which radiates GWs carrying the specific information of the particles.  
 62 Information about the particle type, location, velocity and angular momentum  
 63 would spread and persist in the endless universe and could be theoretically

64 detected by human beings. The figure is not drawn to scale.

65 The macroscopic quantities, which correspond to the microscopic ones, such as mass  
66 distribution and temperature, will be reflected in the GW signals. Then it is inferred that  
67 every infalling macroscopic object has its specific gravitational waveforms, no matter it  
68 is an encyclopedia, a cup of hot tea, or a spinning neutron star. When a massive star  
69 collapses to form a BH, the collapse process may be near-spherical as a whole, while the  
70 motion of the inner substances is nonspherical. Thus the corresponding information will  
71 also be sent out through GWs before the BH settles down.

72 Based on the above analysis, we can obtain several qualitative deductions. First,  
73 Hawking radiation could lead to the complete mass loss of a steady BH, but not of all  
74 the matter that has fallen in it, for part of the mass has already lost in the form of GW  
75 energy before the BH turns steady again. Second, when matter falls within a BH, the  
76 surface area of the wobbling horizon will transitorily decrease owing to the asymmetric-  
77 to-symmetric mass distribution and mass loss of the dynamic system. Third, the  
78 gravitational radiation results in the space-time ripples thus leading to the entropy  
79 increase of the universe. Fourth, most, if not all, of the matter information is emitted  
80 out through GWs during the falling process, and will persist in the space-time till the  
81 end of the universe, rather than preserved inside the event horizon till the end of the BH.

82 In short, this paper gives a concise resolution of the black hole information paradox,  
83 which reconciles general relativity and quantum mechanics in the most mysterious  
84 celestial body. However, much more quantitative work is needed to complement this  
85 preliminary hypothesis.

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