

1 Article

2 Determination of Initial-Shear-Stress Impact on 3 Ramsar-Sand Liquefaction Susceptibility through 4 Monotonic Triaxial Testing

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17 **Abstract:** Liquefaction risk assessment is critical for the safety and economics of structures. As the
18 soil strata of Ramsar area in north Iran is mostly composed of poorly graded clean sand and the
19 ground water table is found at shallow depths, it is highly susceptible to liquefaction. In this study,
20 a series of isotropic and anisotropic consolidated undrained triaxial tests are performed on
21 reconstituted specimens of Ramsar sand to identify the liquefaction potential of the area. The
22 specimens are consolidated isotropically to simulate the level ground condition, and anisotropically
23 to simulate the soil condition on a slope and/ or under a structure. The various states of soil behavior
24 are studied by preparing specimens at different initial relative densities and applying different
25 levels of effective stress. The critical state soil mechanics approach for identifying the liquefaction
26 susceptibility is adopted and the observed phenomena are further explained in relation to the micro-
27 mechanical behavior. As only four among the 27 conducted tests did not exhibit liquefactive
28 behavior, Ramsar sand can be qualified as strongly susceptible to liquefaction. Furthermore, it is
29 observed that the pore pressure ratio is a good indication of the liquefaction susceptibility

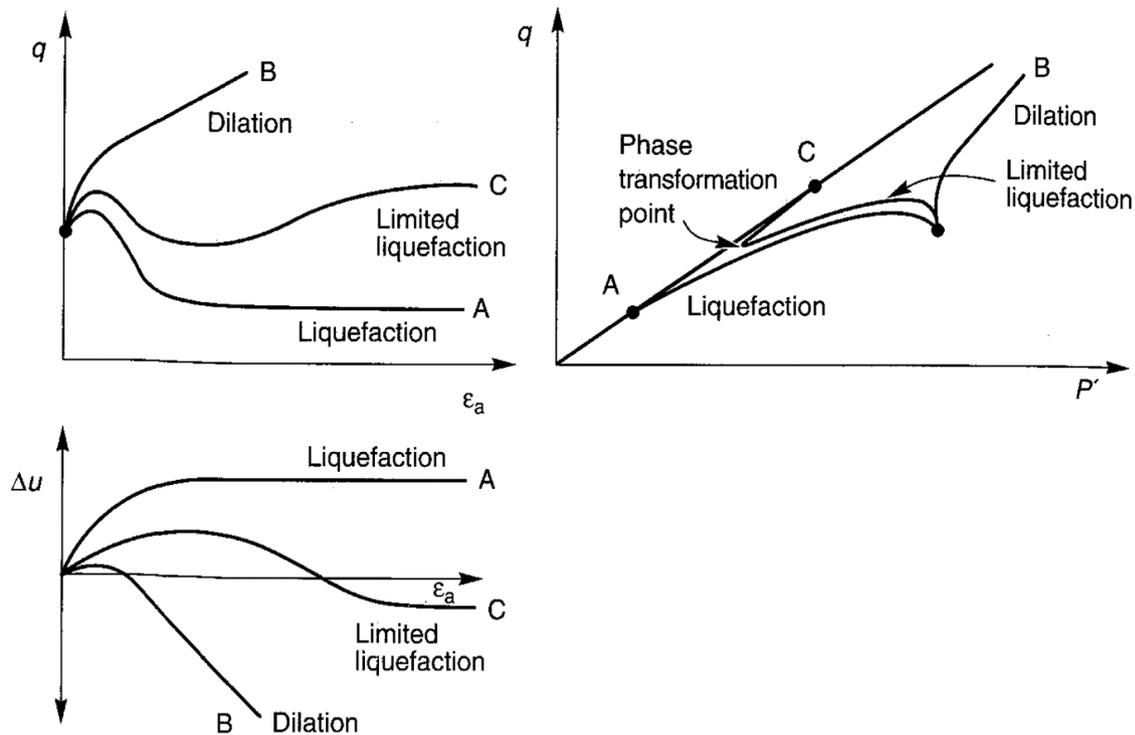
30 **Keywords:** Anisotropic Triaxial test; Initial shear stress; Pore water pressure ratio; Static
31 liquefaction; Ramsar sand.

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33 some 1. Introduction

34 Soil liquefaction is a phenomenon in which soil loses its bearing capacity and behaves like a
35 liquid. After Marcuson [1], Youd et al. [2] defined liquefaction as “the act or process of transforming
36 any substance into a liquid”. This phenomenon can damage a broad range of constructions such as
37 dams, roads, and embankments. The study of liquefaction to develop susceptibility assessment
38 approaches can enable the construction of safer structures, saving money and lives. The Niigata
39 earthquake (1964) accelerated intense research on liquefaction. Experimental work on static
40 liquefaction was originally performed by Castro [3], and Castro and Poulos [4]. Their work on static
41 liquefaction using a triaxial apparatus provided a better perception of the liquefaction mechanism
42 and its controlling parameters. The application of initial shear stress during sample consolidation is
43 a method for studying the treatment of anisotropically consolidated samples. Jafarian et al. [5]
44 observed that this method plays a significant role in stimulating the liquefaction susceptibility of the
45 soil condition on a slope subjected to high shear strain or under a structure that can tolerate high

46 shear stresses. Castro [3] performed several static tests on anisotropically and isotropically
 47 consolidated undrained samples and distinguished three different types of behavior for sands, as
 48 shown in Figure 1.



49

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Figure 1. Liquefaction, limited liquefaction and dilation in static loading tests [3].

51 Numerous studies [4,6–12] have concluded that the initial state expressed in terms the initial
 52 void ratio e_0 as well as the initial effective mean stress p'_0 significantly affect undrained soil response.
 53 The influence of the initial shear stress on the liquefaction susceptibility has been investigated in
 54 recent decades. Kramer and Seed [13] observed that in samples consolidated to principal effective
 55 stress ratios (K') of 1.5, 2.0, and 2.25, the increase in deviator stress under undrained conditions
 56 required to initiate liquefaction were approximately 0.6, 0.25, and 0.13 ksc (59, 25, and 13 kPa),
 57 respectively. They reported that the resistance to static liquefaction in these samples decreased
 58 significantly as the initial shear stress level increased. Later contributions by Harder and Boulanger
 59 [14], and Seed and Harder [15] demonstrated that the presence of the initial shear stress ratio
 60 improves liquefaction resistance at high relative densities (55–70%), whereas the effect is less
 61 pronounced at low relative densities (approximately 35%). According to recent research [16,17],
 62 triaxial tests performed at higher initial shear stress parameter values have a distinct effect for range
 63 of α . Alpha values could create both improving and aggravating effects on loose or very dense
 64 sands influence on the liquefaction susceptibility.

65 Soil samples under shearing up to large strains tend to reach a state of continuous deformation
 66 under constant shear (q) and normal stresses (p'), where such occurrence is known as the ultimate
 67 steady-state line (SSL). Soil at SSL exhibit a relationship between the ultimate values of the deviatoric
 68 stress and mean effective principal stress. Therefore, soil behavior can be predicted by expressing the
 69 state of the effective confining stress and defining the location of this point relative to the steady-state
 70 line. Castro and Poulos [4] observed that in addition to the steady-state line position being a unique
 71 soil property, the inclination of steady-state lines vary extensively, even for apparently similar soils.
 72 The steady-state concept and SSL were further described by other research [1,3,18]. Poulos et al. [4]
 73 systematically measured the steady strength through stress-controlled CU triaxial tests. On the other
 74 hand, Roscoe et al. [19] studied the yielding of soils and reported that when soil is subjected to shear
 75 distortion, it begins to shear at constant volume at a certain critical pressure. Similarly, according to

76 Schofield and Wroth [20], if a soil specimen is continuously distorted, it reaches steady state, i.e., flow
77 failure. Although the critical state was initially developed on clayey soils, several studies have
78 attempted to adopt this framework to granular materials [21,22]. However, Been et al. [23] stated that
79 such an attempt is challenging due to the difficulties in determining the normal consolidation line for
80 such soils. Coop [24] clarified that this phenomena involves stress formation at the particle contact
81 points, affecting the compression response of granular materials. However, the attempts of Ferreira
82 and Bica [25], Coop [26], Ekinici et al. [12], and Rezaian et al. [27] for adopting this framework to
83 granular soils was successful.

84 To understand the critical state concept of granular materials, the microscale behavior of sandy
85 soils was investigated. Cavarretta et al. [28] studied the micromechanical behavior of coarse-grained
86 soils utilizing a new technology to compute the particle shape and surface roughness, for measuring
87 the particle contact stiffness and interparticle friction to relate the nature of fundamental particle
88 behavior with the traditional test results (triaxial and oedometer). Although a link was established
89 between the roughness of the particle surface and interparticle friction, the influence of the particle
90 shape was more noticeable. In a similar study by Senetakis et al. [29], repeated interparticle shear
91 testing showed a small decrease in the friction angle, which can be because of asperity damage during
92 initial shearing. Recently, Zhang et al. [30] investigated sands with a variety of mineralogy using
93 shape analysis, particle crush tests, and one-dimensional compression tests. Authors reported that
94 particle mineralogy could be a major factor affecting the strength or compressibility, rather than the
95 particle shape. Moreover, Zhao et al. [31] investigated the effect of the initial density of specimens in
96 one-dimensional compression to evaluate particle breakage. They stated that specimens prepared
97 with high relative density had lower probability of failure and failure modes that were less extensive
98 compared to the low-density specimens. Moreover, it was reported that the effect of the initial density
99 on the probability of particle survival reduced after significant breakage. Additionally, loose
100 specimens exhibited higher compression due to particle failure leading to more fine generation by
101 the further crushing of the existing fragments.

102 In support of the anisotropic soil condition on a slope and/ or under a structure, McDowell
103 and Bolton [32] proved that compared to isotropic or k_0 conditions, shearing was more effective at
104 breaking particles. Furthermore, Coop et al. [33] investigated particle breakage by performing ring
105 shear tests and observed that particle breakage continued up to very large strains along with
106 volumetric compression, which was observed even for tests at moderate confining stresses.
107 Accordingly, Chandler [34] stated that the observed critical state at the strain levels reached by triaxial
108 equipment was due to the counteracting dilative strains because of particle rearrangement and
109 compressive strains because of particle breakage.

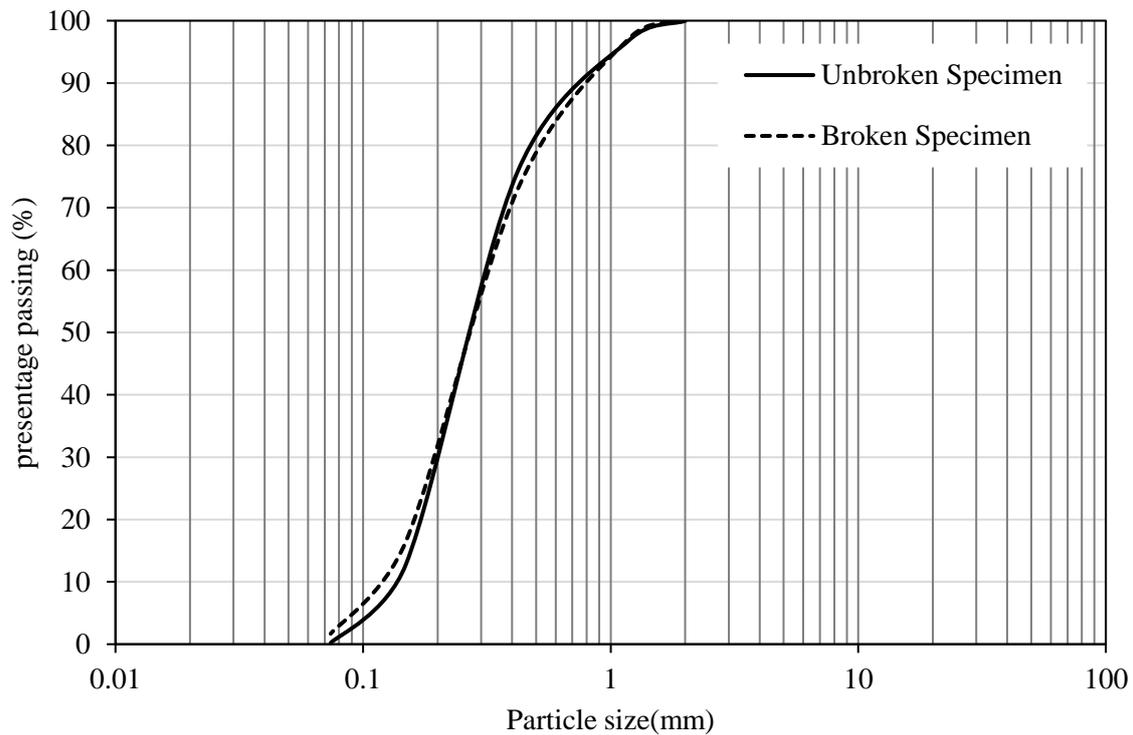
110 Liquefaction could be induced by static loading or cyclic loading. Fort Peck Dam and Nerlerk
111 Berm failures are good examples for static liquefaction. Cyclic loading may take different forms like
112 storm load, ice load and machinery load, on which Jefferies & Been [35] have given a good historical
113 summary. The most tremendous one is, undoubtedly, that caused by earthquake shaking [36] in
114 terms of the intensity of loading and extensity of damage triggered. The static loading concerned in
115 this study is primarily in relation with monotonic loading occurs due to a sudden increase of pore
116 water pressure and thus confining effective stress during an earthquake.

117 In this study, the effect of the initial shear stress ratio on the potential liquefaction susceptibility
118 is investigated through monotonic testing. This study is the first to evaluate the liquefaction
119 susceptibility by relating the pore pressure ratio (r_u) with the initial shear stress ratio (α) and explain
120 the liquefaction phenomena in relation to the particle breakage mechanism. Furthermore, the
121 adopted anisotropic testing mimics realistic scenarios such as the simulation of the soil condition on
122 a slope and/or under a structure. Compared to level ground conditions ($\alpha = 0$), only a few
123 experimental studies on the monotonic behavior of sands in sloping ground conditions ($\alpha > 0$) are
124 available. Moreover, specimen testing in undrained triaxial condition reduces the testing time.
125 Therefore, this study proposes a method for liquefaction susceptibility determination which is less
126 time consuming, and less expensive than other widespread methods just like dynamic triaxial testing
127 method.

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129 **2. Materials and Methods**130 *2.1. Physical Parameters of Ramsar Sand*

131 The relative density D_r is a critical parameter that can control the stress-strain behavior or change
 132 the liquefaction susceptibility. In this study, three values of the relative density (2%, 30%, and 45%)
 133 were considered to include very loose, loose, and medium dense sand, respectively. Ramsar sand is
 134 poorly graded clean sand which is extensively found in the southern coast of the Caspian Sea and
 135 classified as SP according to USCS. The e_{max} and e_{min} values of Ramsar sand, measured according to
 136 ASTM D-4253 [37], and ASTM D-4254 [38], are 0.88 and 0.54, respectively. The grain size distribution
 137 curve of Ramsar sand is depicted in Figure 2 and its basic properties are summarized in Table 1.



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Figure 2. Grain size distribution for broken and unbroken Ramsar sand.

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Table 1. Basic properties of Ramsar sand.

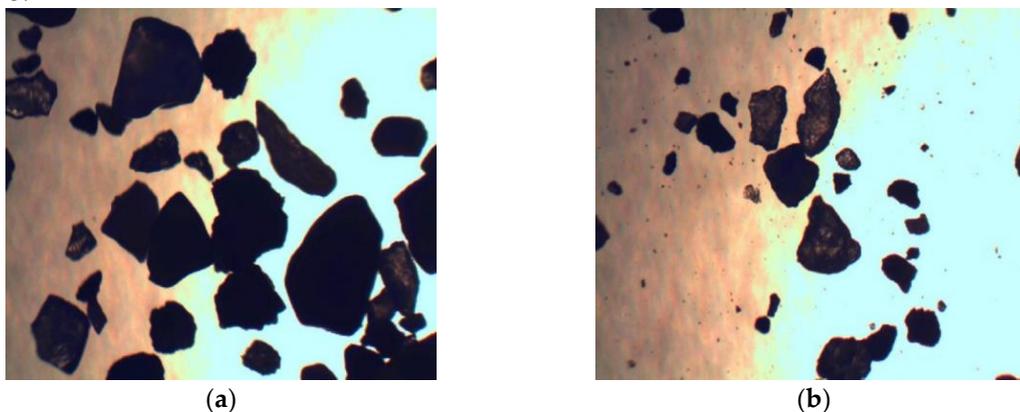
Parameters	Values
e_{max}	0.88
e_{min}	0.54
G_s	2.67
$D_{50}(mm)$	0.22
$D_{10}(mm)$	0.147
$D_{30}(mm)$	0.187
$D_{60}(mm)$	0.246
C_c	0.96

C_u	1.67
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143 The grain size distribution of the specimens after triaxial testing were investigated and plotted
 144 against sand specimens obtained at 2-m depth from a borrow pit. Figure 2 shows that sand particles
 145 around 0.6–0.8 mm are further broken because there is a reduction in this particle percentage,
 146 whereas adversely, there is an increase in the particle percentage in the 0.1– 0.2 mm particle size
 147 range. This observation reveals that after shearing, Ramsar sand particles are brittle.

148 In order to further investigate this observation, sand particles before and after the test were
 149 examined using an optical microscope. The grains of the sand in Figure 3 (a) are rounded with certain
 150 sharp ends, whereas in Figure 3(b), the edges of the parent particle appear broken. Due to extensive
 151 shearing, more rounded particles are generated with very tiny spots related to broken bits of sand
 152 grains, clearly demonstrating the inherent brittleness. Moreover, the presence of silt is obvious in
 153 Figure 3.



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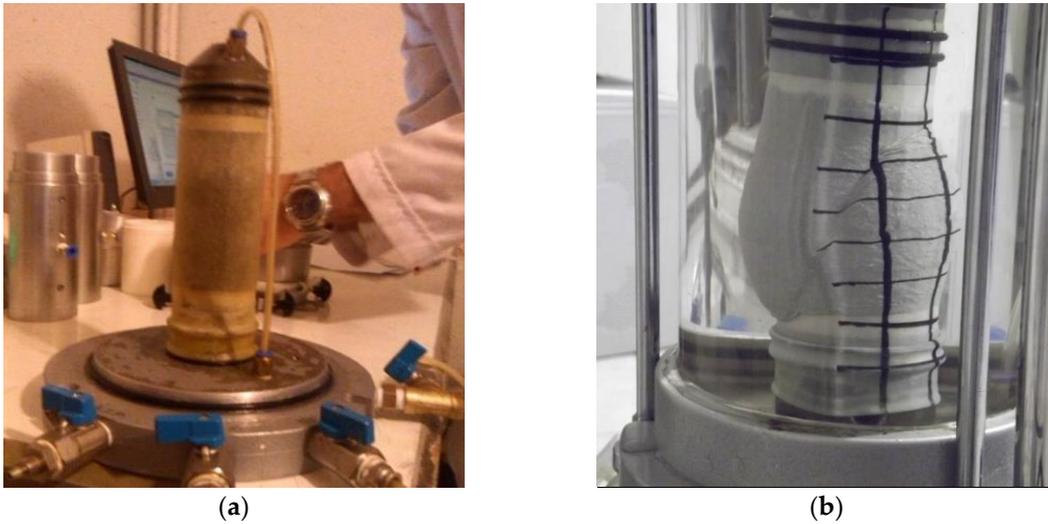
155 **Figure 3.** Microscopic view (40x) of Ramsar sand, where (a) and (b) are respectively before and after
 156 the test.

157 Furthermore, in order to assess the influence of the observed phenomenon during undrained
 158 shearing, two tests under the same confining pressure and relative density ($\sigma_{3c} = 350$ kPa and $D_{r0} =$
 159 30 %) were conducted on broken and unbroken sand. In these two tests, the ultimate deviatoric stress
 160 (q_u) for broken sand was higher (283.85 kPa) than that for the unbroken one (255.9 kPa), indicating
 161 that the former has more resistance to contractive behavior. Similar to these findings, Cavarretta et.
 162 al. [28] had reported that compared to the as supplied particles (perfectly rounded glass ballotini),
 163 crushed particles showed higher deviatoric stresses and more dilation.

164 2.2. Test Procedure

165 Moist tamping, which is the most common and valid method, was used to prepare the
 166 specimens. Sand specimens were oven-dried, mixed with 5% distilled water, and divided into five
 167 equal portions based on weight. Rubber membrane with a thickness of 0.3 mm was stretched by
 168 applying vacuum pressure. Each layer was then poured into a cylindrical split-mold, leveled with a
 169 spatula, and gently tamped. In order to improve the bonding between layers, the surface of each layer
 170 was scarified, and the same procedure was repeated for each layer. Measurement of the sample
 171 height and diameter was preceded by the application of a slight vacuum (not more than 20 kPa) on
 172 the specimen. The sample height and diameter were maintained at approximately 100 mm and 50
 173 mm, respectively. Figure 4 illustrates a prepared sample. Subsequently, the cell was installed and
 174 filled with water. The vacuum was removed, and a positive pressure of approximately 30 kPa was
 175 applied. Carbon dioxide was infused through the specimen to augment saturation (to obtain a
 176 suitable degree of saturation, the carbon dioxide infusion technique proposed by Lade and Duncan
 177 [39] was used. Deaired water was then passed into soil under a specified back pressure to achieve

178 saturation of at least 95%. After consolidation, strain-controlled undrained loading (1 mm/min) was
179 applied and continued until the occurrence of specimen failure or 30-mm axial displacement.
180 Anisotropic tests were conducted with a very-low-rate axial load applied to the sample in a drained
181 condition.



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Figure 4. Examples of (a) preparation and (b) tested triaxial sample.

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3. Results and Discussion

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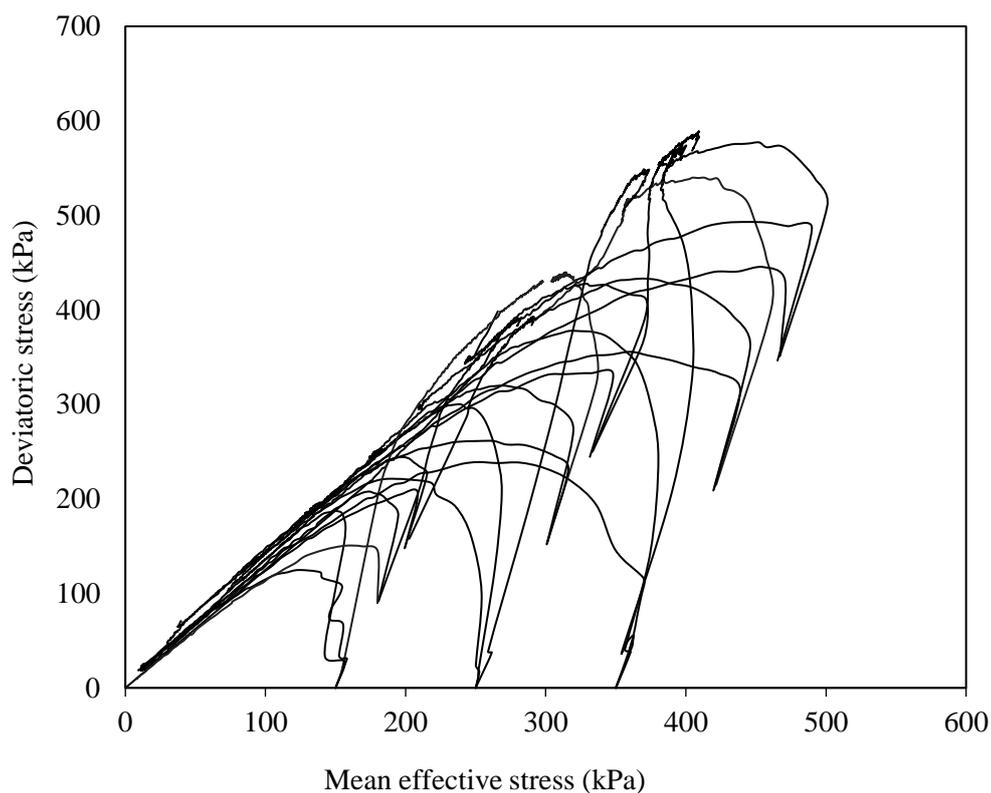
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This study is primarily concerned with the effect of the initial shear stress on the potential susceptibility to the static liquefaction of Ramsar sand. It deals with specimens prepared at relative densities of 2%, 30%, and 45%. Isotropically ($\alpha=0$) and anisotropically ($\alpha = 0.3$ and 0.5) consolidated specimens under three different confining pressure (150, 250 and 350 kPa) were tested in an undrained condition. A brief explanation of all the 27 tests is presented in Table 2. In addition, all the stress path graphs are shown in Figure 5 (ACU and ICU denote anisotropically and isotropically consolidated undrained, respectively).



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Figure 5. Steady state line in q - p' plane with all 27 stress paths

Table 2. Summary of static triaxial tests conducted during the current study.

#	Series	α	Situ	σ_{3c}	D_{r0}	D_{rc}	Result
1	(R-A) ₁	0	ICU	150	2	12.1	Liquefaction
2	(R-A) ₂	0	ICU	150	30	37.5	Liquefaction
3	(R-A) ₃	0	ICU	150	45	51.5	Dilation
4	(R-A) ₄	0	ICU	250	2	16.6	Liquefaction
5	(R-A) ₅	0	ICU	250	30	42.7	Liquefaction
6	(R-A) ₆	0	ICU	250	45	53.77	Dilation
7	(R-A) ₇	0	ICU	350	2	22.48	Liquefaction
8	(R-A) ₈	0	ICU	350	30	37.37	Liquefaction
9	(R-A) ₉	0	ICU	350	45	55.35	Limited
10	(R-B) ₁	0.3	ACU	150	2	16.6	Liquefaction
11	(R-B) ₂	0.3	ACU	150	30	38	Liquefaction
12	(R-B) ₃	0.3	ACU	150	45	52.24	Dilation
13	(R-B) ₄	0.3	ACU	250	2	20.6	Liquefaction
14	(R-B) ₅	0.3	ACU	250	30	42.25	Liquefaction
15	(R-B) ₆	0.3	ACU	250	45	54.3	Liquefaction

16	(R-B) ₇	0.3	ACU	350	2	26.7	Liquefaction
17	(R-B) ₈	0.3	ACU	350	30	44.91	Liquefaction
18	(R-B) ₉	0.3	ACU	350	45	57.16	Liquefaction
19	(R-C) ₁	0.5	ACU	150	2	18.55	Liquefaction
20	(R-C) ₂	0.5	ACU	150	30	39.9	Liquefaction
2	(R-C) ₃	0.5	ACU	150	45	53.02	Dilation
22	(R-C) ₄	0.5	ACU	250	2	24.45	Liquefaction
23	(R-C) ₅	0.5	ACU	250	30	43.7	Liquefaction
24	(R-C) ₆	0.5	ACU	250	45	54.57	Limited
25	(R-C) ₇	0.5	ACU	350	2	30.62	Liquefaction
26	(R-C) ₈	0.5	ACU	350	30	41.94	Liquefaction
27	(R-C) ₉	0.5	ACU	350	45	57.4	Liquefaction

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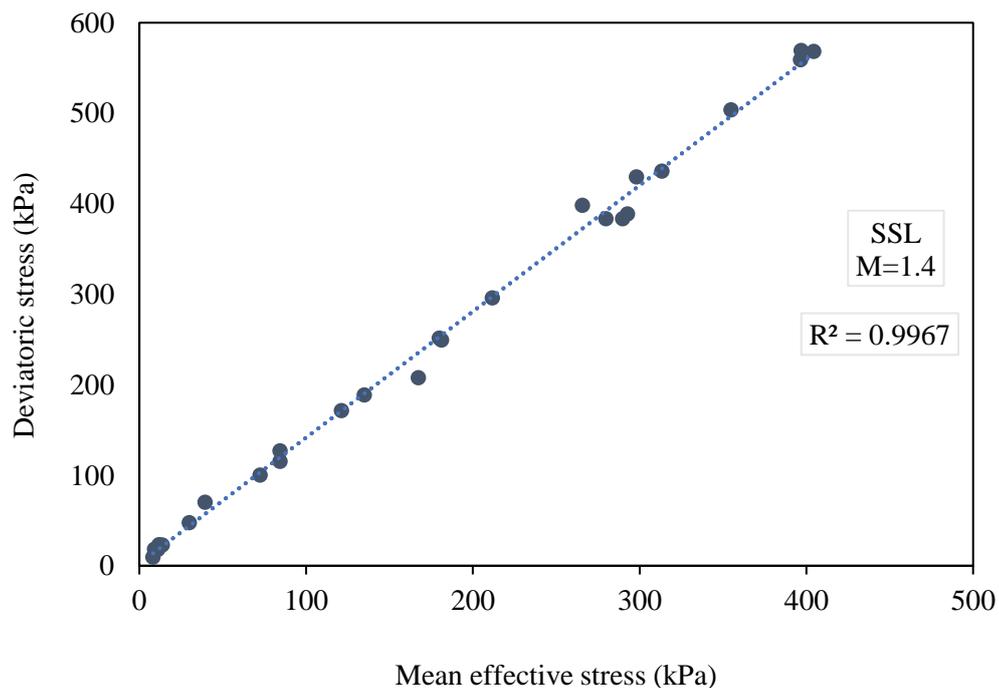
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The SSL for the 27 CU tests of Ramsar sand are displayed in Figure 6. The brittleness of the particles causes sample brakeage and fills in the available pores to bring the specimen to the same steady state as reported earlier by Cavarretta et al. [28]. Adversely, some researchers [12,40,41] had reported that poorly graded sand specimens prepared at varying relative densities had different SSLs. Ferreira and Bica [25], and Ekinici et al. [12] had tested a range of relative densities from minimum to maximum, and had managed to apply the critical state framework by grouping the relative densities and normalizing the results according to the group critical state line. Comparison of the relative densities of the specimens tested in this study with those of the study by Ekinici et al. [12] reveals that the densities of the specimens in this study falling into Group which is located at a position closest to the NCL, reach the same SSL.



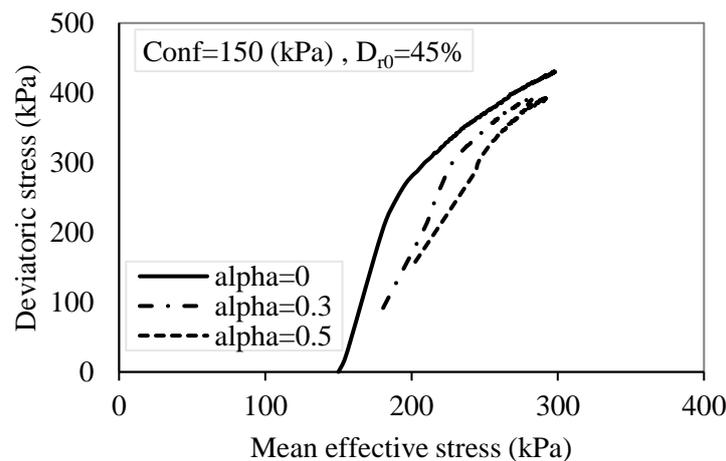
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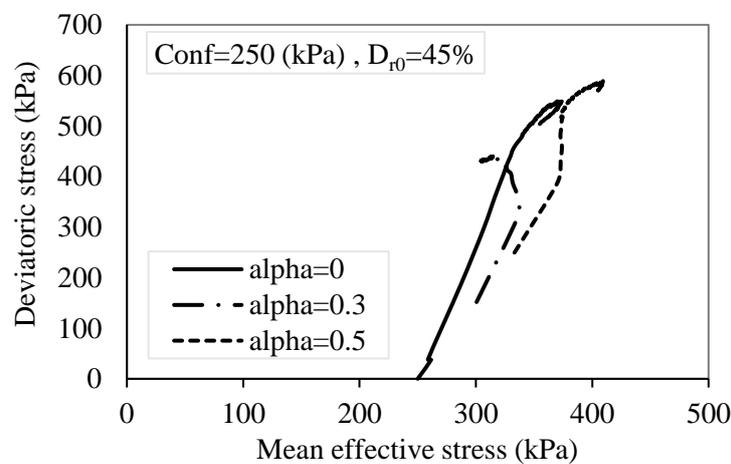
Figure 6. Steady state line in q-p' plane.

210 3.1. Effect of confining pressure on sand behavior

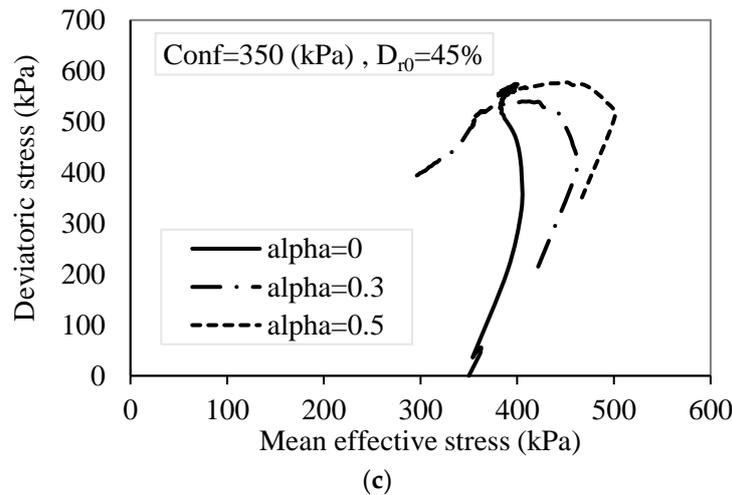
211 In this study, sand behavior was controlled by the relative density and confining pressure,
212 which, respectively, decrease and increase the liquefaction potential. Confining pressure is a
213 parameter that relates to the depth and surcharge. Figure 7 displays the effective stress paths at
214 different effective confining pressure at isotropic and anisotropic stress conditions for initial relative
215 density of the sand, $D_{r0} = 45\%$. It can be observed that on increasing the effective confining pressure,
216 the stress path tends to reach steady state, whereby there is a change in its direction indicating
217 liquefaction. As stated by Rezaian et al. [27], the increase in confinement results in increase of particle
218 breakage therefore since the particles are brittle means more breakage of particles and this leads to
219 reach to the critical state and resulting in liquefaction.
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(a)



(b)



221 **Figure 7.** Effective stress paths at different effective confining pressure a) 159 kPa, b) 250 kPa, c) 350
 222 kPa in isotropic and anisotropic stress condition for $D_{r0} = 45\%$

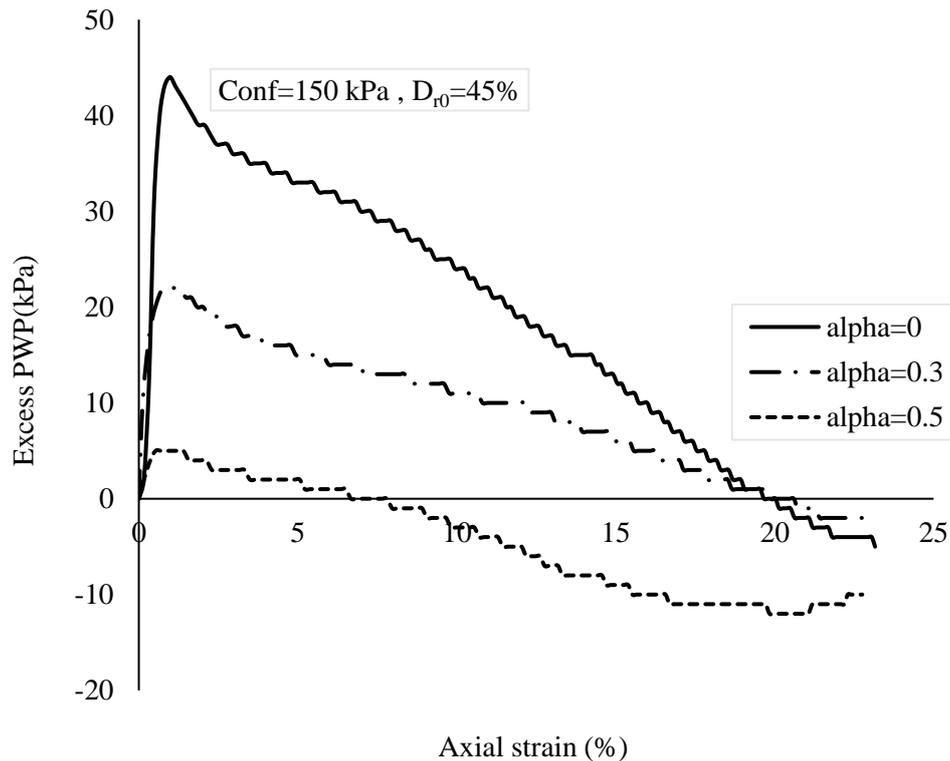
223 3.2. Initial shear stress ratio (α)

224 The initial shear load parameter α obtained by anisotropically consolidating the specimens can
 225 differ according to certain soil parameters. Compared to level ground conditions ($\alpha = 0$), only a few
 226 experimental studies on the monotonic behavior of sands in sloping ground conditions ($\alpha > 0$) are
 227 available, where the shear component is also present during the initial static condition. Therefore,
 228 this study (18 tests) includes anisotropically consolidated specimens prepared with initial axial
 229 loading in a drained condition. The initial shear stress ratio α is defined as the ratio of the initial axial
 230 stress (q_s) divided by twice the effective confining stress (σ_{3c}).

231 For example, when $\alpha = 0.5$ and $\sigma_{3c} = 150$ kPa, the load will be 0.29 kN, and for $\sigma_{3c} = 250$ kPa, the
 232 specimens will undergo a 0.49-kN load. Equation (1) indicates that the initial static shear stress level
 233 increases with the increase in α values, and the limiting case of $\alpha = 0$ represents level ground
 234 conditions without the initial static shear stress. Depending on the density of soil and the initial
 235 effective stress level, the presence of initial static shear stress may have either have an improving or
 236 aggravating impact on the resistance to liquefaction.

$$237 \alpha = \frac{\tau}{\sigma'_{3c}} = \frac{q_s}{2\sigma'_{3c}} = \frac{\sigma'_{1c} - \sigma'_{3c}}{\sigma'_{1c} + \sigma'_{3c}}, \quad (1)$$

239 The excess pore water pressure (PWP) buildup of three specimens with a relative density of 45%,
 240 confining pressure of 150 kPa, and different initial shear stress ($\alpha = 0, 0.3, \text{ and } 0.5$) are shown in Figure
 241 8. All the samples in these three tests exhibit dilative behaviors because of the high relative densities,
 242 whereas their PWP intensities differ depending on the initial shear stress ratio. In addition, on
 243 increasing the initial shear stress, the PWP peak declines and subsequently, the intensity of dilation
 244 increases. Due to the reduction in the excess pore pressure, the particle contact friction increases and
 245 causes resistance to liquefaction.



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Figure 8. Comparative curvature for (R-A)₃, (R-B)₃ and (R-C)₃ in u - ϵ % plane.

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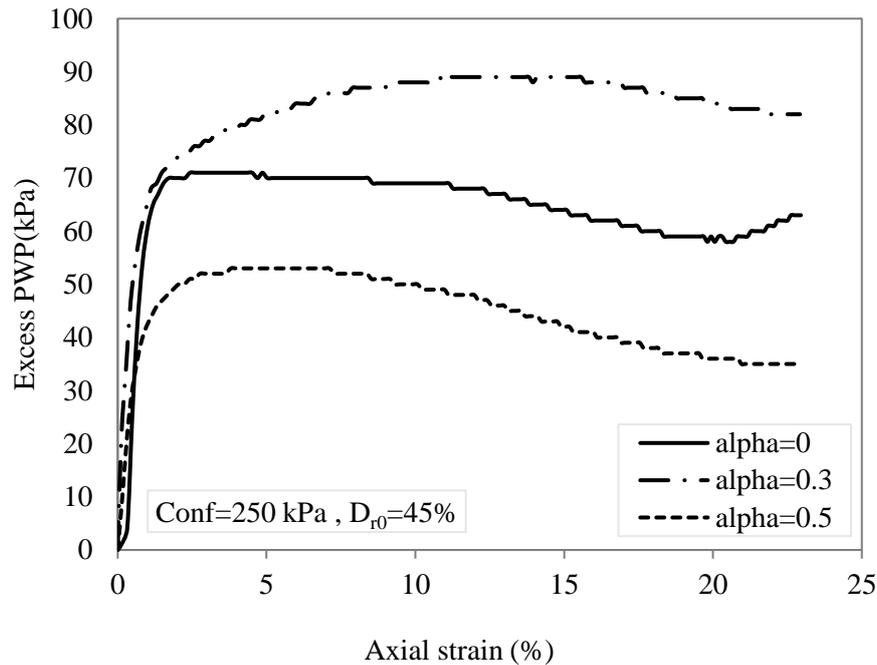
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Figure 9 displays different initial shear stress with higher confinement (250 kPa) compared to Figure 8. It can be seen that the initial shear stress not only changes the behavior intensity, but also the entire behavior to dilation in (R-A)₆, liquefaction in (R-B)₆ and limited liquefaction in (R-C)₆, where the initial shear stress ratios are 0, 0.3, and 0.5, respectively. This result is completely different from those observed in the specimens in Figure 8, where the excess PWP buildup is considerably more and has been preserved up to high strain levels. The increase in PWP reduces the effective stress, which is the particle skeleton strength (reduction in the particle contact friction); therefore, such reduction leads to liquefaction. This may also show the inverse dependency of α on the effective confining pressure.



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Figure 9. comparative curvatures for (R-A)₆, (R-B)₆ and (R-C)₆ in u-ε% plane.

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3.3. Pore water pressure ratio (r_u)

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The observations in Figures 8 and 9 regarding the effect of confinement on the excess pore pressure, on varying the initial shear stress ratios, can be a criterion for liquefaction susceptibility. From equation 2, it can be observed that the criterion for liquefaction susceptibility pore water pressure ratio (r_u) is the variation of the pore water pressure at failure to the initial effective confining pressure.

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$$r_u = \frac{u_{\text{excess at failure}}}{\sigma_{3c}}, \quad (2)$$

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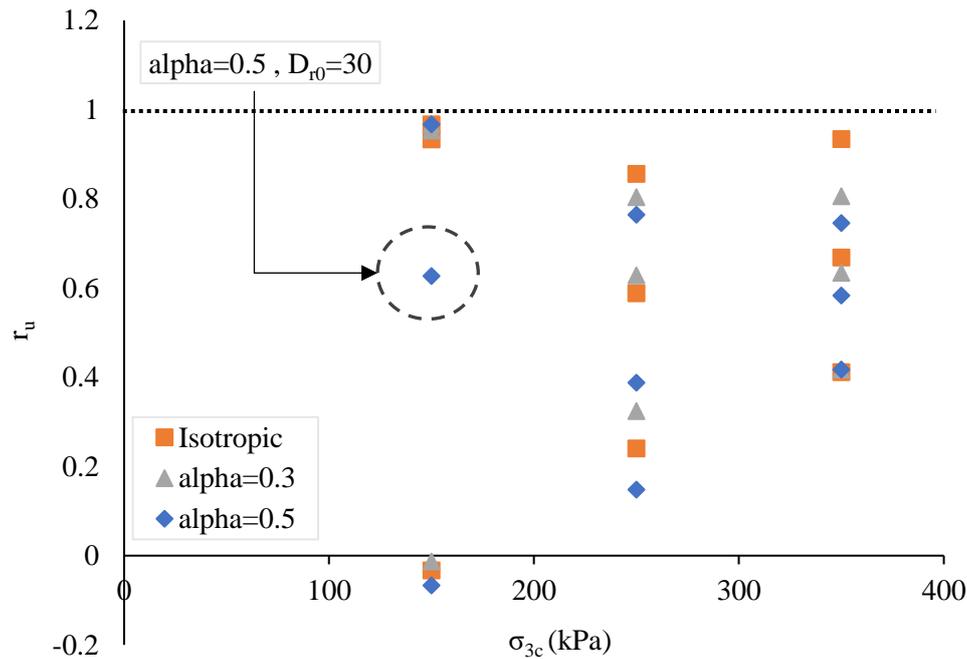
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The susceptibility ranges from 0–1, when r_u approximates unity, and the liquefaction potential increases. Jafarian et al. [5] had also stated that it is common to have lower r_u within the liquefaction phenomenon, termed as susceptible to liquefaction. Figure 10 presents the liquefaction susceptibility for isotropic and anisotropic specimens; the pore water pressure ratio (r_u) is plotted against the mean effective pressure at failure (Figure10). It can be seen that most specimens are susceptible to liquefaction, while three of them show a negative value indicating that they have no liquefaction potential. In this study, the r_u values range from -0.06–0.97. However, 21 out of the 24 tests show a positive value of r_u indicating liquefaction behavior.



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Figure 10. Pore water pressure ratio versus mean effective stress and effective confining pressure in isotropic and anisotropic stress condition.

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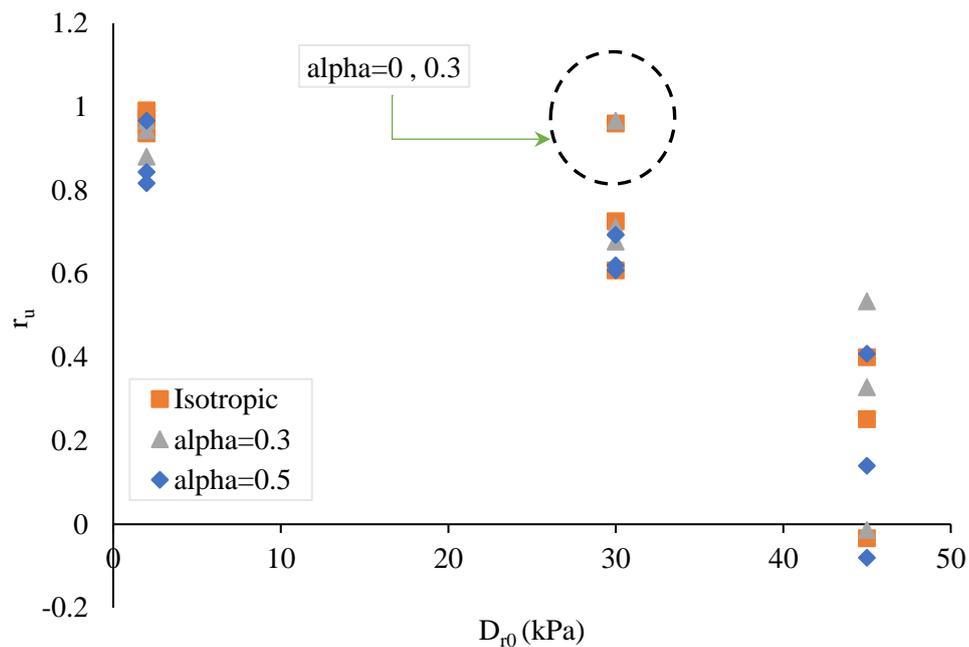
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In Figure 10, the scattered pattern of points shows that r_u is related to the relative density (D_r) because on increasing the effective confining pressure from 150 kPa to 350 kPa, the dispersion decreases. The dispersion in tests with $\sigma_{3c} = 150$ kPa reveals that except for one of the tests (R-C)₂, which may be an outlier, the outcomes of the other tests fall into two main opposing groups (phases): 1-highly susceptible and 2- completely nonsusceptible to liquefaction.

As observed from the r_u values plotted against the initial relative densities and from the point dispersion comparison shown in Figure 11, specimens with low D_{r0} exhibit almost the same behavior, whereas for those with high D_{r0} , the tests results differ to a certain extent from each other. For medium D_{r0} , two distinguishable points, (R-A)₂ and (R-B)₂, indicate the commencement of dispersion. It is clear from Figure 11 that the increase in relative density reduces the liquefaction susceptibility. As stated by Zhao et al. [31], specimens with high relative density have lower particle failure probability and less extensive failure modes than loose specimens. Additionally, loose specimens exhibit higher compression due to particle failure leading to more fine generation by the further crushing of existing fragments, and as stated earlier, reach the critical state, resulting in liquefaction.



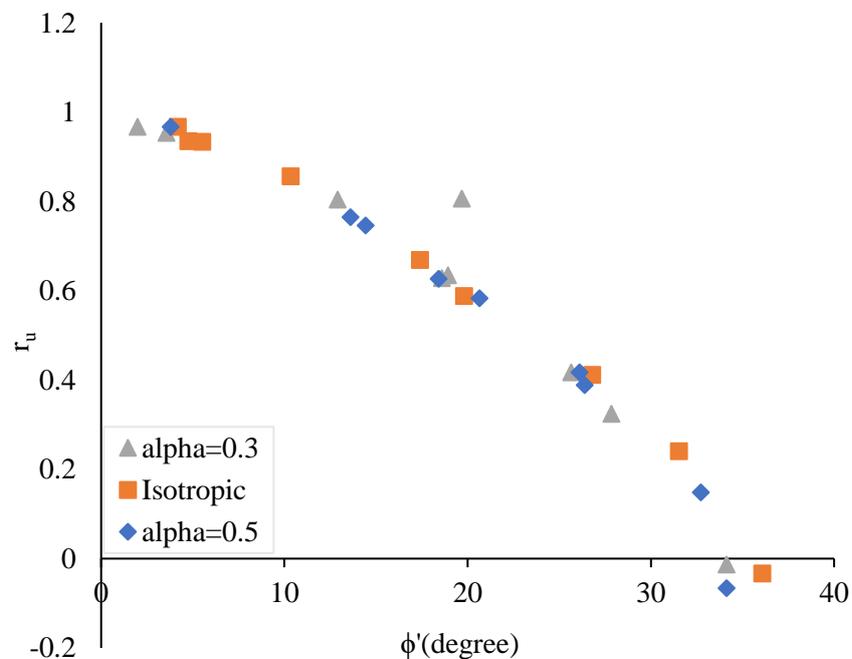
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Figure 11. Pore water pressure ratio versus mean effective stress and effective confining pressure in isotropic and anisotropic stress conditions.

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The friction angle at the failure point and r_u have a negative correlation, as depicted in Figure 12. The friction angle ranges from 2–36 in this study, and $\phi'_{(\text{deg})} = 2$ and $\phi'_{(\text{deg})} = 36$ are related to specimens with high and low susceptibility to liquefaction, respectively. Low friction angle is a result of excess pore water pressure, causing loss of contact between particles which in turn results in interparticle friction loss.



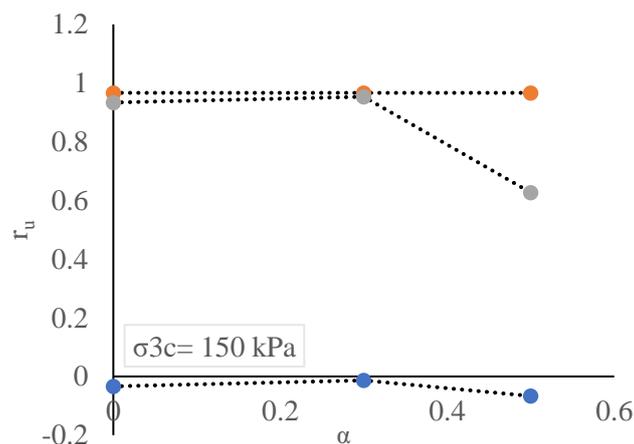
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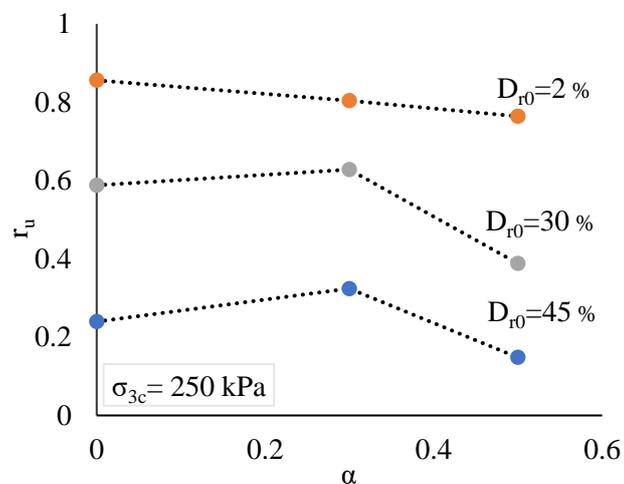
Figure 12. Pore water pressure ratio versus friction angle at failure in isotropic and anisotropic stress.

3.4. Pore water pressure ratio versus the initial shear stress ratio

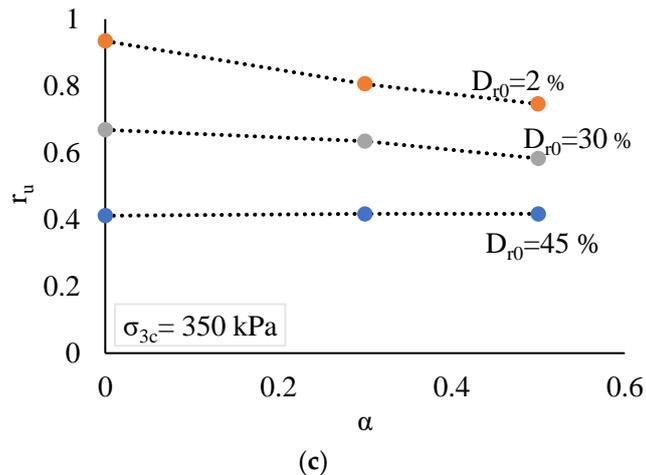
Figure 13 displays the relationship between r_u and α in three charts, whose effective confining pressures are different. It is obvious from the charts that on increasing the relative density, the liquefaction susceptibility reduces regardless of whether α and σ_{3c} increase or decrease. This indicates that the relative density is much more effective than α and σ_{3c} . Figure 13(a) shows that the initial shear stress is not effective in loose sand (2%), whereas it influences semi-dense and dense specimens. In Figure 13(b), this pattern slightly changes because the relative density after consolidation increases, which is strongly related to the effective confining pressure for loose sand. For example, as shown in Table 2, the relative density increases from 2% to approximately 23% after consolidation in sample (R-A)₇, whereas this growth is approximately 12% in sample (R-A)₁. This increment was calculated using the amount of water raised up during volume change in the consolidation process. The specimen became denser due to the increase in σ_{3c} from 150 to 250 kPa, and this pattern continued, when the effective confining pressure was increased from 250 to 350 kPa (Figure 13(c)). For the other relative densities, except for specimens with $\sigma_{3c} = 350$ kPa, all the functions initially increased to $\alpha=0.3$ and then decreased to $\alpha=0.5$ which can indicate a lesser decreasing effect for higher values of α than for the medium values, for susceptibility under medium effective confining pressure. This phenomenon is also shown in Figure 10 by the change in test result from liquefaction to quasi-limited liquefaction, when α is increased from 0.3 to 0.5. In Figure 13(c), when $\sigma_{3c} = 350$ kPa, the pattern remains unchanged for $\alpha > 0$. Moreover, the functions hardly change.



(a)



(b)



322 **Figure 13.** Pore water pressure ratio versus initial shear stress ratio at a) 159 kPa, b) 250 kPa and c)
 323 350 kPa effective confining pressure.

324

325 4. Conclusions

326 In this study, 27 isotropic and anisotropic monotonic undrained triaxial tests were performed to
 327 investigate the liquefaction susceptibility in relation to the critical state soil mechanics and
 328 micromechanical behavior. It was observed that Ramsar sand can experience all the possible
 329 behaviors of liquefiable soils, namely, flow failure, limited liquefaction, and dilation. In addition,
 330 Ramsar sand is highly susceptible to liquefaction because 21 out of the 27 tests showed flow
 331 liquefaction. Among the other six tests, two showed limited liquefaction and only four showed
 332 dilation. Another important result was that the grains of Ramsar sand are brittle, which is responsible
 333 for its high susceptibility to liquefaction because a crushed specimen becomes more resistant to
 334 liquefaction (q_u -before = 255.9 kPa and q_u -after = 283.85 kPa). The initial shear stress α is a critical
 335 parameter for studying soil behavior on a slope and/or under a structure. Although it has limited
 336 impact on loose sand, it can be an improving or aggravating factor depending on the effective
 337 confining pressure and relative density levels. The liquefaction susceptibility increased for an α range
 338 of 0–0.3 and reduced for a range of 0.3–0.5 under medium effective confining pressure and lower.
 339 However, at high effective confining pressure, r_u values barely reduces as a result of increasing the
 340 initial shear stress ratio.

341 The pore water pressure ratio r_u is a key parameter for evaluating sand behavior. In the
 342 conducted tests, even though only six tests did not result in liquefaction, only three of them showed
 343 negative r_u values. For the other three tests with positive values of r_u , the susceptibility to liquefaction
 344 despite showing dilation or limited liquefaction is not surprising. Furthermore, a similar study is
 345 recommended to evaluate the findings of this study by investigating the varying particle mineralogy
 346 and percentage of fine generation due to particle breakage after shearing at various testing
 347 conditions.

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 349 the experimental study. AE was responsible for structure interpretation. SS and AI wrote the first draft of the
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