Article

Simulation of mTBI Utilizing White Matter Properties from MRE

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Version July 15, 2020 submitted to Modelling

Abstract: Tissues of the brain, especially white matter, are extremely heterogeneous - with constitutive response varying spatially. In this paper, we implement a high-resolution Finite Element (FE) head model where heterogeneities of white matter structures are introduced through Magnetic Resonance Elastography (MRE) experiments. Displacement of white matter under shear wave excitation is captured and the material properties determined though an inversion algorithm are directly used in the FE model. This approach is found to improve model predictions when compared to experimental results. In the first place, responses in the cerebrum near stiff structures such as the corpus callosum and corona radiata are markedly different compared with a homogenized material model. Additionally, the heterogeneities introduce additional attenuation of the shear wave due to wave scattering within the cerebrum.

1. Introduction

With approximately 2.8 million cases reported in the United States [1], traumatic brain injury (TBI) - commonly caused by a direct blow or impulse to the head - remains a pressing concern for study. Clinical results show that damage to the brain in blunt head injuries has a tendency to occur in regions with highly organized axon tracts such as the brainstem and corpus callosum [2–7]. These regions serve as pathways to other parts of the brain, meaning damage to them is potentially more dangerous. In this work we introduce a heterogeneous material description of white matter structures to our high-resolution Finite Element (FE) model to account for the local differences in mechanical response between different regions of the brain.

The FE method is commonly used to determine the mechanical response of brain tissue in order to develop improved diagnostic tools and protective measures to reduce the prevalence of TBI. The

accuracy of these FE models is highly dependent on the accuracy of the material model. To date, most finite element models have utilized mechanical properties averaged over large portions of the brain, as reviewed in [8], thus ignoring potentially significant effects of local structures. In actuality, the tissues of the brain are heterogeneous, their constitutive response varying from location to location. This is most noticeable for white matter due to the presence of axons with diverse orientations. Overall, the shear stiffness of white matter is 1.2-2.6 times higher than that of gray matter [9]. Locally, white matter tracts with highly oriented fibers such as the corpus callosum and corona radiata have material properties vastly different from other regions. Johnson et al. [10] determined that global white matter was softer on average than either the corpus callosum or the corona radiata. This can be explained by considering the structure of these regions. The corpus callosum provides more structural rigidity than the superficial white matter due to the presence of highly aligned fibers. The fan-like structure of the corona radiata exhibits similar behavior, but to a lesser degree as the fibers are not as highly aligned. As such the corpus callosum was found to be approximately 11% stiffer than the corona radiata. The brainstem is another structure with a high level of heterogeneity. Arbogast and Margulies [7] investigated the prevalence of trauma observed in the brainstem after head injuries. They determined that the brainstem was 80-100% stiffer than the cerebrum and concluded this regional stiffness variation is one reason for the selective vulnerability of this region to rotational motion. FE models that utilize homogenized white matter material properties have no way to resolve these local features.

A very useful tool to measure heterogeneity in-vivo is Magnetic Resonance Elastography (MRE) [11] where the head is excited with shear waves to quantitatively assess the local mechanical properties of brain tissue. This technique has been successfully applied to a variety of different applications such as decrease in whole-brain stiffness with age [12] and as a result of certain neurodegenerative diseases [13], measurement of tumor stiffness [14], as well as a marker for TBI severity [15]. MRE is applied as a three-step process beginning by first inducing shear waves in tissue with frequencies ranging from 50-500 Hz using an external driver. Second, the waves are imaged using a phase-contrast MRI pulse sequence synchronized with the frequency of the applied vibration. Finally, the mechanical properties of the tissue are estimated by inverting the observed displacements using a viscoelastic material model; such as that presented by Van Houten et al. [16].

In this work, as a steppingstone, we utilize our previously homogeneous FE model - presented and validated in our previous works [17–19] - and introduce a voxel-based heterogeneous material model using results from Johnson et al. [10]. In order to properly resolve the high-frequency waves generated during such vibrations, the finite element mesh must be properly refined, as argued in [8]. The mechanical properties used in this work are reconstructed at the same spatial resolution as the displacement data captured during the MRE process. This, in turn, generates a finite element mesh

that has more than sufficient resolution to accurately capture the dynamic shear wave propagation during impacts. To the best of our knowledge, this is the first attempt to include heterogeneity of brain tissue via MRE in a high-resolution FE model.

2. Model Formulation

2.1. MRE Aquisiton and Inversion

The heterogeneous properties of the white matter are taken from the work by Johnson et al. [10]. A brief overview of the acquisition and inversion is presented here. A more detailed discussion of this process can be found in [20]. Shear waves are generated at a frequency of 50Hz by placing the subject's head on a custom cradle attached to an electromagnetic shaker via a rigid rod. The actuator imparts a nodding motion to the head, while the displacement data is captured via a Siemens 3T Allegra head-only scanner (Siemens Medical Solutions; Erlangen, Germany). A multi-shot MRE sequence utilizing spiral readout gradients [21] with periods matching that of the applied shear wave was developed to reduce errors during the inversion step. In total, the imaging volume comprises twenty axial slices of 2mm thickness covering the ventricles, corpus callosum and corona radiata resulting in a $2 \times 2 \times 2mm^3$ isotropic spatial resolution for the reconstructed mechanical properties.

A non-linear inversion (NLI) algorithm [16] is applied to estimate the material properties from the measured dusplacement data. The inversion is performed by minimizing the function

$$\Phi(\theta) = \sum_{i=1}^{N} (u_i^c(\theta) - u_i^m) (u_i^c(\theta) - u_i^m)^*$$
(2.1)

by iteratively updating the material property description, given by θ . Here, u_i^m is the measured displacement amplitude at the location i; $u_i^c(\theta)$ is the computed displacement amplitude sampled at the same point; and * indicates the complex conjugate.

Following the development in [22], a Rayleigh damping model is used to represent the material response of brain tissue under time-harmonic conditions. The motion amplitude field u, is calculated from Navier's equation for an inhomogeneous, locally isotropic linear elastic medium

$$\nabla \cdot G(\nabla u + \nabla u^T) + \nabla (\lambda \nabla \cdot u) = \rho \omega^2 u, \tag{2.2}$$

where λ is the first Lamé parameter; G is the second Lamé parameter, or shear modulus; ρ is the density; and ω is the activation frequency. The Rayleigh damping model introduces the complex-valued shear modulus and density to account for attenuation related to both elastic and inertial forces - where the imaginary shear modulus includes damping effects due to inertial forces, while the imaginary part of

the density includes damping related to inertial forces. Including inertial damping effects - something that commonly used viscoelastic models do not include - allows for better characterization of material response when performing the inversion. We use the notation G' and G'' to denote the storage and loss shear moduli respectively, which are the real and imaginary part of the complex valued shear modulus

$$G = G' + iG'', \tag{2.3}$$

i being the imaginary unit. Due to the nearly incompressible nature of brain tissue, we assume that λ is very large compared to the shear modulus. The damping ratio

$$\xi := G''/2G' \tag{2.4}$$

can be determined as well, which physically describes the level of motion attenuation in the tissue.

The distribution of storage and loss moduli within the white matter in the imaging resolution $(2\times2\times2~mm^3)$ is presented in Figure 1 for the coronal, sagittal and horizontal planes. The relative stiffness of both the corpus callosum and the corona radiata can be clearly observed. The average values and the standard deviation for the global white and gray matter is presented in Table 1 as well as those for the corpus callosum and corona radiata.

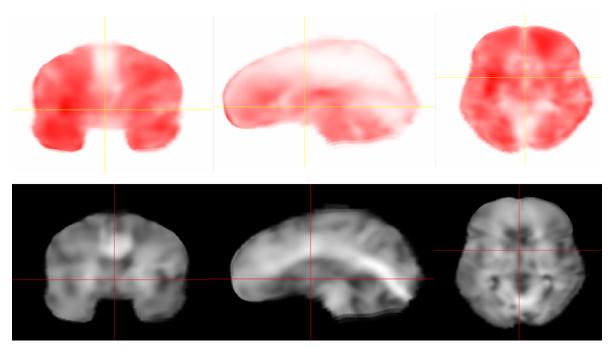


Figure 1. Distribution of Loss (top) and Storage (bottom) modulus in the FE model. Darker regions indicate higher magnitude of shear modulus.

Table 1. Average values and standard deviations for different tissues within the model: gray Matter (GM), White Matter (WM), Corpus Callosum (CC), Corona Radiata (CR)

	GM	WM	CC	CR
G' (kPa)	2.02 ± 0.09	2.66 ± 0.30	3.09 ± 0.39	2.78 ± 0.37
G" (kPa)	1.04 ± 0.12	1.54 ± 0.15	1.23 ± 0.26	1.97 ± 0.12
ξ	0.32 ± 0.03	0.31 ± 0.03	0.23 ± 0.07	0.37 ± 0.05

2.2. Finite Element Mesh Generation

In addition to the MRE image acquisition, T1-weighted anatomical images with a resolution of $1 \times 1 \times 1 mm^3$ are generated for the purposes of mesh segmentation. Image voxels are directly converted to eight-noded hexahedral elements through a custom code, thus preserving the same spatial resolution as the MRI scans. The resulting mesh consists of approximately 2.2 million elements. The mesh is segmented into the following tissue types: scalp, skull, cerebrospinal fluid (CSF), gray matter and white matter. Each element is assigned a different material definition based on the results of the segmentation, as detailed in section 2.3. Features that are below the imaging resolution such as membranes, blood vessels, bridging veins, and draining sinuses are excluded from the model. Since T2-weighted scans were not collected, the segmentation of the interfaces between tissue types is negatively affected. We perform a mesh smoothing operation at these interfaces to minimize this effect. We utilize a volume-preserving Laplacian smoothing algorithm as outlined in [17]. Smoothing has the added benefit of eliminating numerical artifacts that may manifest from jagged edges along interfaces. We ensure traction and displacement continuity at all material interfaces.

Our MRI voxel-based approach produces meshes which more realistically model the complicated folding structure of the cerebral cortex (i.e. gyri and sulci) as well as the differentiation of gray and white matter of brain tissues. Additionally, in order to accurately resolve the shear wave motion within the brain, the mesh must be sufficiently refined [8]. For example, using the typical speeds of shear wave propagation in brain tissue, $c_T \approx 5m/s$, and the frequency of the vibration as 50Hz, we arrive at a minimum element size of 10mm (using a conservative choice of 10 elements per wavelength [23]). For vibrations of higher frequency or more transient loading (such as the cases for impact loads), this requirement is even more stringent.

2.3. Material Properties

As discussed above, we assign different material definitions to each voxel based on the result of the mesh segmentation. Due to the presence of highly oriented tracts of myelin-sheathed axonal fibers in white matter, significant heterogeneity exist in this region, especially within the corpus callosum (CC) and corona radiata (CR). On the other hand, gray matter is made up of cell bodies and supporting vascular networks that can be assumed to be isotropic and homogeneous [10,24]. This assumption

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Table 2. Material properties of different tissues used in the FE model. For the heterogeneous white matter, only the average values of G_0 and G_∞ are presented, denoted by the "*".

Tissue	Mass Density (kg/m³)	Bulk Modulus K (Pa)	Short Term Shear Modulus G_0 (Pa)	Long Term Shear Modulus G_{∞} (Pa)	Decay Factor β (sec ⁻¹)
Skull	2070	3.61E+9	2.7E+9		N/A
gray matter	1040	2.19E+9	3.4E+4	6.4E+3	400
White matter	1040	2.19E+9	4.1E+4*	7.8E+3*	400
CSF	1004	2.19E+7	5.01	E+4	N/A

allows for the MRE imaging to be performed over a manageable acquisition volume. As such, we allow for only the white matter to have material heterogeneity whereas other tissues are assumed to be homogeneous.

For homogeneous tissues, the choice of material properties is determined from data used commonly in the literature, presented in Table 2, and is the same as that in our earlier works [17,19]. The skull is assumed to be linear elastic and modelled as a single-layer structure with homogenized properties given in [25]. We assume a linear viscoelastic material model for the shear response of the brain tissues. The standard linear solid model is chosen for its simplicity, with the shear relaxation modulus given by

$$G(t) = G_{\infty} + (G_0 - G_{\infty})e^{-\beta t}.$$
 (2.5)

Here, G_0 is the short-term shear modulus, G_∞ is the long-term shear modulus and β is the decay factor. For the white matter, we assume that only G_0 and G_∞ are heterogeneous with averages scaled to match the values taken from literature [26]. The mass density, bulk modulus and decay factor are maintained to be homogeneous. For the material model for the CSF, we have the choice of three models, previously presented in [19]: incompressible elastic, viscoelastic, and fluid-like elastic using an equation of state model. We determined that the choice of CSF affects the shear wave propagation within the brain while the peak pressure is not significantly altered. For the first iteration of our heterogeneous model, we choose the most commonly utilized model - nearly incompressible elastic model with bulk modulus to be very large compared to the shear modulus, with values taken from [27].

2.4. Boundary Conditions

We consider two extreme assumptions for the head-neck junction, free and fixed boundary conditions mostly following previous work in [17]. The free boundary condition allows for predominantly rectilinear motion under frontal impacts while rotational motion cannot be represented. We consider the fixed boundary condition as the other extreme case where the nodes around an area of the foramen magnum are fully constrained. Research reported in [17] showed that the responses from these two boundary conditions bound the experimental response.

2.5. Experimental Verification

We use Nahum et al. linear impact experiments [28] to verify the accuracy of our model. In the typical experiment, a cylindrical impactor was launched at a seated cadaver at a constant veloctiy of 9.94m/s. The impact was along the specimen's mid-sagittal plane in an anterior-posterior direction. The skull was rotated as depicted in Figure 2a. The resultant input force time history is given in Figure 2b. Intracranial pressure history was recorded during the impact event. The results of this comparison are presented in the next section. Our homogeneous model was also verified using tagged MRI and harmonic phase (HARP) imaging analysis technique in [18] where displacement time history from head-drop experiments is compared to numerical results. Finally, we directly compare displacement data during impact utilizing experimental data from Hardy et al. brain translational motion experiment [29,30]. Brain motion was captured using neutral density targets (NDT) under linear accelerations ranging from 38 to 291g.

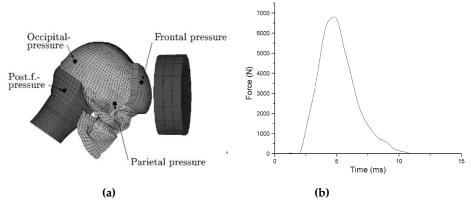


Figure 2. (a) Nahum et al.'s experimental setup depicting impactor and impact location (adapted from [31]). (b) Input force time history (adapted from [17]).

3. Results and Discussion

3.1. Simulation of Impact

The recorded impact force from the frontal cadaveric impact experiment conducted by Nahum, as discussed in the preceding section, is directly applied to the model in the form of a distributed load with the peak pressure input of 4.37 MPa on the frontal region of the skull. The impact pulse lasts about 9 ms and the simulation is run for 15 ms. Rotation of the model is permitted as we the base of the skull is not constrained. We find that this free boundary condition gives better correlation of coup pressure to experimental results [17]. The FE simulations are carried out using Abaqus/Explicit.

The pressure-time history for the Nahum loading is presented in Figure 3 at the coup impact site. We plot the results for both the homogeneous and heterogeneous model. The model predicts tensile pressure for nearly the whole duration of impact. The peak pressure predicted by the heterogeneous

material model more closely matches that from Nahum's experiments than the homogeneous model. In both cases the peak pressure occurs roughly at the same time - indicating very similar wave speeds.

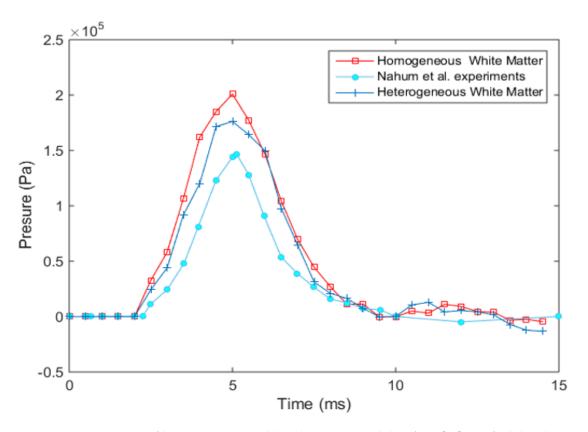


Figure 3. Comparison of heterogeneous model with experimental data from [28]. We find that the heterogeneous model exhibits response closer to the Nahum data.

We next compare the displacement response to the C383-T1 impact from Hardy et al. experiments [29]. We plot the response for relative displacements for the x- and y-directions for two NDTs each in the anterior (A) and posterior (P) positions, see Figures 4 and 5. We find good agreement between our model and the experimental data as shown. Additionally, we have previously validated our homogeneous model using tagged MRI and HARP imaging analysis techniques in [18] which allows comparisons of displacement fields for the entire cerebrum *in vivo*.

We plot the contours of the von Mises stress distribution on the sagittal plane due to the frontal impact in Figure 6. The spherically convergent structure of the shear wave is clearly observed. The wave attenuates as it travels inwards and eventually dissipates. Reflections of wave due to scattering from heterogeneous white matter structures can also be observed at later times.

Next, we consider three distinct points along the sagittal plane, as depicted in Figure 7. The points are chosen within regions of strong heterogenities due to the presence of highly aligned axon tracts, such as the corpus callosum and corona radiata. The differences in mechanical properties of these regions are given in Table 3. We see that the material phases at these points are relatively stiffer than

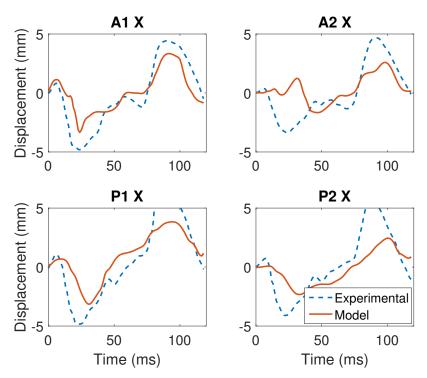


Figure 4. Comparison of displacements in the x-direction for two positions in the anterior (A) and posterior (P) to Hardy C83-T1 experiment

the corresponding points in the homogeneous model. As a result, the response in Figure 7 is affected accordingly. We find that the difference in peak pressure response is proportional to the difference in shear stiffness between the homogeneous and heterogeneous models. However, the time at which these events occur is not significantly affected. This indicates that the pressures in regions of high stiffness within the brain are over-estimated in the homogeneous models. In summary, relative to the MRI-based model, the new MRE-based heterogeneous model more accurately predicts the local response within the white matter by taking into account the differences in tissue stiffness of local white matter structures.

A few points are in order regarding the qualitative differences between the shear modulus of different regions in our model. Globally, the white matter is found to be approximately 32% stiffer than the gray matter. In general, the white matter properties in local regions differ significantly from the average ones. For instance, the storage modulus G' is significantly lower in the rest of the white matter than within the corpus callosum and the corona radiata. This is quite logical given the fact that the corpus callosum contains highly oriented, tightly packed axon tracts. The corpus callosum, in turn, is stiffer than the corona radiata, again evident from the composition of the corona radiata which contains axon fibers that fan out and are not as highly aligned as the corpus callosum.

Additionally, while both white and gray matter have similar values of damping ratio, ξ (which reflects the amount of motion attenuation within the tissue), the corpus callosum has a lower value

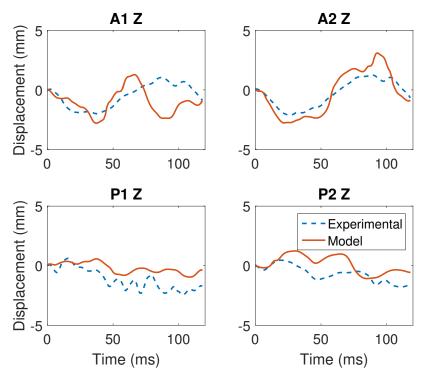


Figure 5. Comparison of displacements in the z-direction for two positions in the anterior (A) and posterior (P) to Hardy C83-T1 experiment

Table 3. Difference of material properties and peak pressure response for three distinct points (indicated in Figure 7) along the sagittal plane within the white matter.

Location	% Difference in Shear Modulus (G_{∞})	% Difference in Peak Pressure	
1	13.34	-7.86	
2	28.62	-47.25	
3	15.48	-20.75	

while the corona radiata has a higher value. This can be explained by examining the microstructure of each of these regions. Experiments by Guo et al. [32] demonstrated that the damping ratio (and thus, the attenuation) in soft tissue composites increases as the number of cross-links between fibers increases. The corona radiata consists of fibers arranged in a grid-like pattern [33] with a large number of cross-links. These crossings do not exist in the corpus callosum, offering a possible explanation for the distribution of ξ .

Since mechanical measures from MRE and diffusivity measures from diffuse tensor imaging (DTI) are essentially measures of the distribution of axon tracts within the white matter, a natural question arises here: What is the difference between our heterogeneous (yet isotropic) model and the more common anisotropic FE models where fiber anisotropy is determined from DTI scans? Many such examples of the latter exist in the literature: for instance in [34–37]. Johnson et al. [10] performed both MRE and DTI measurements on a group of seven volunteers to determine the correlation of mechanical and diffusivity measures within the corpus callosum and corona radiata. They determined that MRE

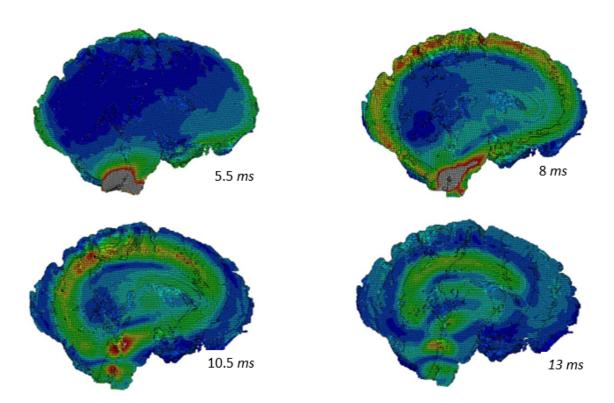


Figure 6. Shear wave propagation due to frontal impact. Notice the attenuation of the wavefront as time progresses.

and DTI measures correlate well with each other within the corpus callosum - not surprising since they are both sensitive to the underlying tissue microstructure. They hypothesize that these measures are highly dependent on axon diameter since larger axons provide greater structural rigidity to the tissue [38]. Within the corona radiata, however, the correlation is not as significant. The corona radiata comprises fiber tracts that fan towards the cortex and contain numerous crossings [33] which are not captured well by DTI [39]. This has been hypothesized as the reason for the poor correlation within the corona radiata. More work is needed to determine the differences between these two methods when used within FE models.

3.2. Stochastic Wave Propagation

The highly heterogeneous structure of the brain tissue introduces wave scattering that competes with wave amplification due to spherically convergent implosion. Following the development in [40], we investigate this effect by considering the theory of wavefronts. For the case of one-dimensional wave motion, we assume that a compressive load produces a shock wavefront that propagates from a disturbed domain to an undisturbed one with a speed c_T . The initial conditions can be given as $u(x,0) = u_t(x,0) = 0$; $\tau(0,t) = -\tau_0 H(t)$ where H is the Heaviside function.

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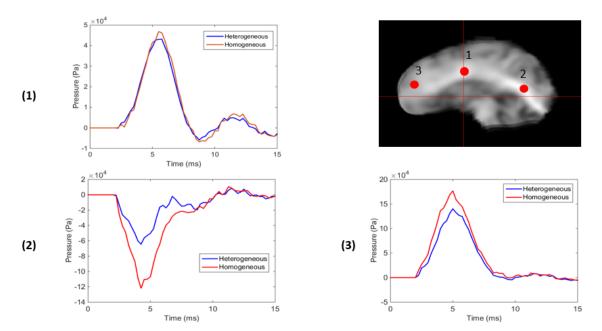


Figure 7. Comparison of pressure at three points on the sagittal plane. The difference in the heterogeneous and homogeneous models is most evident in regions of high relative stiffness.

Assuming a plane wave in a homogeneous medium, we have the dynamic compatibility condition $[\tau] = -\rho c_T[u_{,t}]$ in the (x,t) - plane, where $[\cdot]$ denotes the discontinuity in a function across the boundary of two materials, σ is the shear stress, ρ is the mass density, u is the displacement normal to the direction of wave motion, and c_T is the transverse wave speed. The linear viscoelastic stress-strain relation for a process that started at time $t=t_0^+$ is

$$\tau(t) = G(0)\varepsilon(t) + \int_{t_0^+}^t G_{,t}(t-s)\varepsilon(s)ds = G(0)\frac{1}{c_1}u_{,x}(t) + \int_{t_0^+}^t G_{,t}(t-s)\frac{1}{c_1}u_{,x}(s)ds, \tag{3.1}$$

where ε is the shear strain. We can derive the relationship for the wavespeed as $c_T = \sqrt{G(0)/\rho}$, where G(0) is the glassy modulus. Following the derivation in [40], we obtain the equation governing the evolution of the discontinuity of τ at the wavefront as:

$$\frac{d_T}{dt}[\tau] = \frac{1}{2} \frac{G_{,t}(0)}{G(0)}[\tau]. \tag{3.2}$$

On account of the initial conditions above, the solution of equation 3.2 is

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$$[\tau] = -\tau_0 \exp\left[\frac{1}{2} \frac{G_{,t}(0)}{G(0)} [\tau]\right]. \tag{3.3}$$

Given that $G_{,t}(0) \le 0$, and G(0) > 0, the stress jump exhibits exponential attenuation and has a tendency for blow-up as $r \to 0$. As our simulations here and in [19] demonstrate, the attenuation is

sufficiently strong so that the imploding waves generated from transient impacts do not blow up into a singularity at the head center.

The impact results not only in a fast pressure wave, but also in a slower shear wave. Due to its relatively low shear modulus, brain tissue deforms much more easily in shear than in dilatation mode. Thus, the shear wave is potentially more damaging. Recall that the spherically convergent shear wave patterns are observed even in the case of homogeneous material description, c.f. [17]. The attenuations of pressure along the sagittal plane for both the homogeneous and heterogeneous models are presented in Figure 8. It is clear that the attenuation is greater in the heterogeneous model as predicted. This is consistent with studies of transient wave propagation in elastodynamics of random media [41,42].

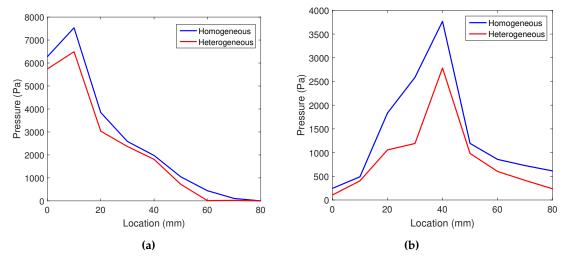


Figure 8. Comparison of attenuation of pressure wave along the sagittal plane between homogeneous and heterogeneous model. (a) At 3ms and (b) at 7ms.

3.3. Limitations

This section discusses a few limitations of our methodology, some of which are likely to be improved in future works. First, features that are below the imaging resolution such as membranes (in particular, the falx cerebri and tentorium), bridging veins and blood vessels are excluded from the current model. However, we argue that the inclusion of heterogeneous MRE-derived parameters in white matter tissue alleviates some of the drawbacks of excluding these features. Additionally, since the MRE inversion was performed assuming locally linear viscoelastic material model, we have chosen to utilize linear viscoelasticity for white and grey matter. Research has shown [43] that the the shear modulus of the brain tissue is much lower than that used in this work. We aim to perform an optimization study to tune the values chosen here to better match experimental results.

4. Conclusion

Our high resolution FE head model now includes heterogeneities of white matter structures improving the ability to capture wave dynamics during highly transient impact events. Heterogeneous shear modulus is determined using a nonlinear inversion technique from MRE experiments performed by [10]. While many FE models employ homogenized or averaged, mechanical properties to approximate constitutive relations of brain tissues, our approach allows us to investigate response due to local structures within the white matter. We note that both the corpus callosum and corona radiata are significantly stiffer than overall white matter, with the corpus callosum exhibiting greater stiffness and less viscous damping than the corona radiata. These differences are explained by examining the organizational and compositional characteristics of each structure. Incorporating this heterogeneity in our model affects wave propagation within the cerebrum and yields results that more closely match experimental results. We find that local variations in stiffness affect the local mechanical response for instance, intracranial pressure magnitude following an impact is lower in regions of high local stiffness. Finally, shear wave attenuation is observed to be more pronounced in the heterogeneous material model and this aspect introduces extra shear wave scattering in addition to the damping effect of tissue viscoelasticity.

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