

# Sudden variation effect of aerodynamic loads and safety analysis of running trains when entering tunnel under crosswind

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**Featured Application:** The results of this paper can provide further theoretical basis for the traffic safety command of high-speed trains in different infrastructure scenarios

**Abstract:** Sudden variation of aerodynamic loads is the potential source of safety accidents of high-speed train (HST). As a follow-up investigation on the aerodynamic response of a HST that enters a tunnel under crosswind environment, this paper focuses on the transient response of a HST's safety indices based on the train-track coupling interaction model. Firstly, a wind-train-track coupling dynamic model is proposed by introducing transient aerodynamic loads into the vehicle-track system. Secondly, the temporal evolution of safety coefficients indicates that the train's safety risk increases during tunnel entry with crosswind. Results show that the derailment coefficients and wheel load reduction rate during tunnel entry are not only larger than those in open air but also those inside the tunnel due to the sudden disappearance of wind excitation at the tunnel entrance. In addition, the characteristic wind curve, which is the wind velocity against the train speed, is presented for application based on the current specification of the safety criteria threshold. The investigation will be useful in assessing the safety risk of a running train subjected to other aerodynamic attacks, such as the coupling effect of infrastructure scenario and crosswind in windy area.

**Keywords:** tunnel entrance; crosswind; wind-train-track coupling dynamic model; transient response of aerodynamic load; sudden wind effect; traffic safety

## 1. Introduction

The flow field around a vehicle usually varies transiently when vehicles move from one infrastructure scenario to another, depending on the infrastructure scenarios, such as flat grounds [1-4], embankments [1,5,6] and viaducts [7-9], thereby resulting in the transient variation of aerodynamic force on vehicle, and even a serious overturn accident. For example, an overturn accident occurred in China's Lanzhou-Xinjiang Railway in 2007, which might be attributed to the transient variation of aerodynamic force when the train was entering wind barriers from an open air [10-14]. The transient variation effect is likely to be serious when vehicles are driven into the tunnel from a crosswind environment because the tunnel has a more considerable space closure than other infrastructure scenarios. In addition, entering/exiting a tunnel is becoming a common operation environment of a high-speed train (HST), especially in China where increasing number of cut-and-cover tunnels are designed as a windshield facility of a windy area (Figure 1).

Yang et al. [12] investigated the temporal evolution of the flow structure and conducted aerodynamic behaviour using a numerical simulation method to study the transient characteristics and main

factors of the aerodynamic loads that act on trains during tunnel entry with crosswind. The results showed that the transient variation of aerodynamic forces on train was significant and varied differently for the leading, middle and tail carriages. Although only a quantitative analysis, the train movement presents a complex dynamic response, including the lateral swing, the snake-like and pitching movements when a HST enters a tunnel in crosswind environment. The transient variation of aerodynamic load is usually a crucial source of a vehicle's safety risk associated with crosswind [7,15-18]. The flow characteristics around a HST when exiting from the tunnel under crosswind has been researched by Krajnovic [19]. The results show that the maximum yawing and rolling moments may occur when about one third of the train body is out of the tunnel. To date, although considerable attention has been given on various dynamic responses of vehicle aerodynamics, limited attention has been devoted in focusing on the transient aerodynamic response and the corresponding traffic safety of running train induced by wind effect in tunnel entrance [15,16,20-24].



**Figure 1.** Wind barriers shaped cut-and-cover tunnels for some HSR in China.

As a follow-up work of a previous study [12,25], the present work focuses on the transient aerodynamic response and the corresponding traffic safety of a running HST during tunnel entry with crosswind. Therefore, a full multi-body system (MBS) with 31 independent degrees of freedom (DOFs) of the vehicle is adopted to discuss the wheel-track dynamic response induced by the sudden extinction of wind effect on the train at the tunnel entrance. Thus, safety coefficients such as wheel load reduction rate (WRR) and derailment coefficient (DC) are obtained. Finally, the characteristic wind curve (CWC), which shows the wind velocity against the train speed, is also presented for application based on the safety criteria.

This paper is organised into six sections. Section 2 presents the wind-train-track coupling dynamic system. Section 3 proposes the approach applied to simulate the transient flow field and calculate the aerodynamic loads when HSTs enter a tunnel under crosswind. Section 4 provides the numerical demonstration and the verification. Section 5 presents the temporal evolution of aerodynamic loads and safety coefficients. Finally, Section 6 presents some conclusions and some suggestions for future work.

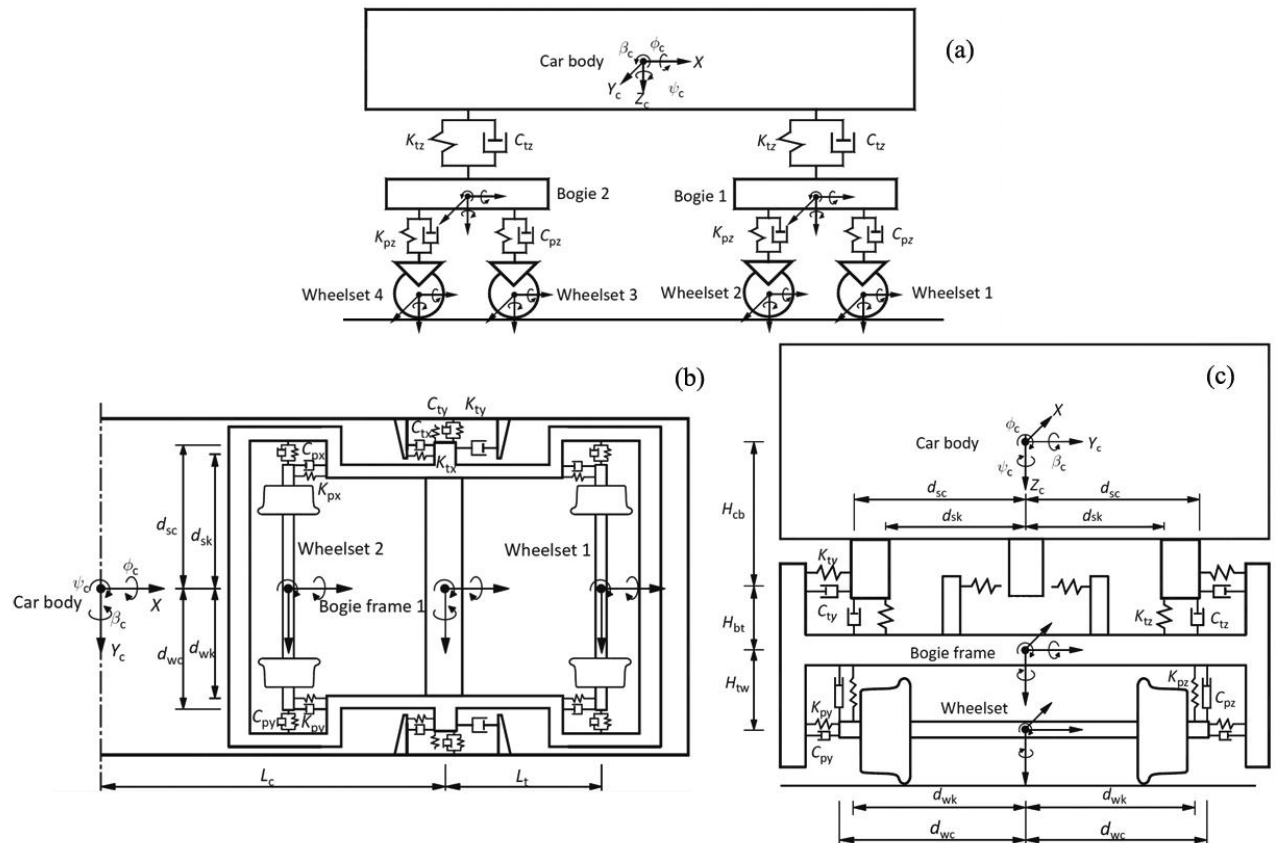
## 2. Wind-train-track coupling dynamic model

The framework of wind-vehicle interaction is divided into three main classes, that is, three simple mass models with no representation of vehicle suspension (see European standard [26]), five mass models with suspension stiffness modelled [9,27] and a full MBS based on train-track coupling interaction [28,29]. This study adopts the MBS method, which establishes the dynamic equilibrium equation of train and track subsystem components, where the wheel-rail interaction is simulated

through their geometric and mechanical compatibility. The wind data or aerodynamic loads are subsequently inputted into a sort of vehicle–track system model.

## 2.1. Modelling of train

A train usually comprises a series of carriages (e.g. 8 or 16 carriages are widely used in China). Typical carriages consist of a carriage body, suspension systems, bogies, pivots, wheelsets and other components [30]. In present study, the carriage is modelled as seven rigid bodies, i.e. one carriage body, two bogies and four wheelsets (see Figure 2). The whole carriage model has 31 independent DOFs. The response vector of a carriage is expressed as follows. The values of the main parameters in Eqs (1)–(10f) are given in Table 1 [8,10].



**Figure 2.** High-speed vehicle model: (a) side elevation, (b) plan view and (c) end view.

**Table 1.** Value of the main parameters of the CRH3 vehicle subsystem.

Notation	Value		Unit
	Head (or Rear) carriage	Middle carriage	
$m_c$	$3.96\times10^4$	$3.44\times10^4$	kg
$J_{xc}$	$1.015\times10^5$	$7.4\times10^4$	kg·m <sup>2</sup>
$J_{yc}$	$2.74\times10^6$	$2.74\times10^6$	kg·m <sup>2</sup>
$J_{zc}$	$1.0644\times10^6$	$2.74\times10^6$	kg·m <sup>2</sup>
$m_b$	$3.2\times10^3$	$2.6\times10^3$	kg
$J_{xb}$	$3.2\times10^3$	$1.6\times10^3$	kg·m <sup>2</sup>
$J_{yb}$	$8.6\times10^3$	$1.7\times10^3$	kg·m <sup>2</sup>
$J_{zb}$	$7.2\times10^3$	$1.7\times10^3$	kg·m <sup>2</sup>
$m_w$	$2.4\times10^3$	$2.4\times10^3$	kg
$J_{xw}$	$1.2\times10^3$	$1.2\times10^3$	kg·m <sup>2</sup>
$J_{yw}$	$1.2\times10^3$	$1.2\times10^3$	kg·m <sup>2</sup>
$k_{px}$	$9\times10^3$		kN/m
$k_{py}$	$1.04\times10^3$		kN/m
$k_{pz}$	$3\times10^3$		kN/m
$k_{tx}$	$2.4\times10^2$		kN/m
$k_{ty}$	$4\times10^2$		kN/m
$k_{tz}$	$2.4\times10^2$		kN/m
$c_{1x}$	5		kN·s/m
$c_{1y}$	10		kN·s/m

$c_{1z}$	5	kN·s/m
$c_{2x}$	10	kN·s/m
$c_{2y}$	10	kN·s/m
$c_{2z}$	30	kN·s/m
$d_{sk}$	0.95	m
$d_{wk}$	1	m
$l_i$	1.25	m
$l_c$	8.75	m
$H_{cb}$	0.14	m
$H_{br}$	0.14	m
$H_{rw}$	0.64	m

The matrix equation of the train motion subsystem can be expressed as

$$\mathbf{M}_v \ddot{\mathbf{X}}_v + \mathbf{C}_v \dot{\mathbf{X}}_v + \mathbf{K}_v \mathbf{X}_v = \mathbf{F}_v \quad (1)$$

where  $\mathbf{M}_v$ ,  $\mathbf{C}_v$  and  $\mathbf{K}_v$  are the mass, damping and stiffness matrices, respectively.  $\ddot{\mathbf{X}}_v$ ,  $\dot{\mathbf{X}}_v$  and  $\mathbf{X}_v$  are the acceleration, velocity and displacement vector, respectively.  $\mathbf{F}_v$  is the vector of forces on the train and can be expressed as

$$\mathbf{F}_v = [\mathbf{F}_{vc} \quad \mathbf{F}_{vb1} \quad \mathbf{F}_{vb2} \quad \mathbf{F}_{vw1} \quad \mathbf{F}_{vw2} \quad \mathbf{F}_{vw3} \quad \mathbf{F}_{vw4}]^T \quad (2)$$

where  $\mathbf{F}_{vc}$  is the vector of forces on the car body;  $\mathbf{F}_{vb1}$  and  $\mathbf{F}_{vb2}$  are the vector of forces on the first and second bogies, respectively.  $\mathbf{F}_{vw1}$ ,  $\mathbf{F}_{vw2}$ ,  $\mathbf{F}_{vw3}$  and  $\mathbf{F}_{vw4}$  are the vector of forces on the four wheelsets.

$$\mathbf{F}_{vc} = [F_{wy} \quad m_c g - F_{wz} \quad M_{wx} \quad M_{wy} \quad -M_{wz}]^T \quad (3a)$$

$$\mathbf{F}_{vb1} = \mathbf{F}_{vb2} = [0 \quad m_b g \quad 0 \quad 0 \quad 0]^T \quad (3b)$$

$$\mathbf{F}_{vwj} = [F_{yj}^{irr} \quad m_w g + F_{zj}^{irr} \quad M_{xj}^{irr} \quad M_{zj}^{irr}]^T \quad (j = 1, 2, 3, 4) \quad (3c)$$

where  $F_{wy}$ ,  $F_{wz}$ ,  $M_{wx}$ ,  $M_{wy}$  and  $M_{wz}$  are the excitations of aerodynamic loads, namely the side forces, lift forces, rolling, pitching and yawing moments on the car body, respectively (details are shown in Section 3.2);  $m_c g$ ,  $m_b g$  and  $m_w g$  are the gravity on the car body, bogies and wheelsets, respectively;  $F_y^{irr}$ ,  $F_z^{irr}$ ,  $M_x^{irr}$  and  $M_z^{irr}$  are the forces and moments induced by the track irregularity excitation (Section 2.2);  $j$  represents the serial number of the wheelset.

The displacement vector  $\mathbf{X}_v$  of the train is expressed as

$$\mathbf{X}_v = [\mathbf{X}_{vc} \quad \mathbf{X}_{vb1} \quad \mathbf{X}_{vb2} \quad \mathbf{X}_{vw1} \quad \mathbf{X}_{vw2} \quad \mathbf{X}_{vw3} \quad \mathbf{X}_{vw4}]^T \quad (4)$$

where  $\mathbf{X}_{vc}$ ,  $\mathbf{X}_{vb1}$ ,  $\mathbf{X}_{vb2}$ ,  $\mathbf{X}_{vw1}$ ,  $\mathbf{X}_{vw2}$ ,  $\mathbf{X}_{vw3}$  and  $\mathbf{X}_{vw4}$  are the displacement vector of the car body, the first and second bogies and the four wheelsets, respectively.

$$\mathbf{X}_{vc} = [Y_c \quad Z_c \quad \phi_c \quad \beta_c \quad \psi_c]^T \quad (5a)$$

$$\mathbf{X}_{vb1} = \mathbf{X}_{vb2} = [Y_b \quad Z_b \quad \phi_b \quad \beta_b \quad \psi_b]^T \quad (5b)$$

$$\mathbf{X}_{vw1} = \mathbf{X}_{vw2} = \mathbf{X}_{vw3} = \mathbf{X}_{vw4} = [Y_w \quad Z_w \quad \phi_w \quad \psi_w]^T \quad (5c)$$

where  $Y$  and  $Z$  are the overall translation displacement in the transverse and vertical directions, respectively;  $\phi$ ,  $\beta$  and  $\psi$  are the rolling displacements around three directions (i.e.  $x$ ,  $y$  and  $z$ ), respectively.

The quality matrix  $\mathbf{M}_v$  of the train is expressed as

$$\mathbf{M}_v = \text{diag} [\mathbf{M}_1 \quad \mathbf{M}_2 \quad \mathbf{M}_3 \quad \mathbf{M}_4 \quad \mathbf{M}_5 \quad \mathbf{M}_6 \quad \mathbf{M}_7] \quad (6)$$

where  $\mathbf{M}_1$ – $\mathbf{M}_7$  are the sub-matrices of the car body, the first and second bogies and four wheelsets, respectively.

$$\mathbf{M}_1 = \text{diag} [m_c \quad m_c \quad J_{xc} \quad J_{yc} \quad J_{zc}] \quad (7a)$$

$$\mathbf{M}_i = \text{diag} [m_b \quad m_b \quad J_{xb} \quad J_{yb} \quad J_{zb}] (i = 2, 3) \quad (7b)$$

$$\mathbf{M}_i = \text{diag} [m_w \quad m_w \quad J_{xw} \quad J_{zw}] (i = 4, 5, 6, 7) \quad (7c)$$

where  $m$  denotes the quality; and  $J_x$ ,  $J_y$  and  $J_z$  are the moments of inertia around three directions, respectively.

The stiffness matrix  $\mathbf{K}_v$  of the train is expressed as follows:

$$\mathbf{K}_v = \begin{bmatrix} \mathbf{K}_{11} & & & & & & \\ & \mathbf{K}_{21} & \mathbf{K}_{22} & & & & \\ & \mathbf{K}_{31} & 0 & \mathbf{K}_{33} & & & \\ & 0 & \mathbf{K}_{42} & 0 & \mathbf{K}_{44} & & \\ & 0 & \mathbf{K}_{52} & \mathbf{K}_{63} & 0 & \mathbf{K}_{55} & \\ & 0 & 0 & \mathbf{K}_{73} & 0 & 0 & \mathbf{K}_{66} \\ & 0 & 0 & 0 & 0 & 0 & 0 & \mathbf{K}_{77} \end{bmatrix} \quad (8)$$

where

$$\mathbf{K}_{11} = \begin{bmatrix} 4k_{ty} & & & & & & \\ 0 & 4k_{tz} & & & & & \\ & & & & & & \\ -4k_{ty}H_{cb} & 0 & 4k_{ty}H_{cb}^2 + 4k_{tz}d_{sk}^2 & & & & \\ 0 & 0 & 0 & 4k_{tx}H_{cb}^2 + 4k_{tz}d_{sk}^2 & & & \\ 0 & 0 & 0 & 0 & 4k_{tx}d_{sk}^2 + 4k_{ty}H_{cb}^2 & & \end{bmatrix} \quad (9a)$$

$$\mathbf{K}_{21} = \begin{bmatrix} -2k_{ty} & 0 & 2k_{ty}H_{cb} & 0 & 0 \\ 0 & -2k_{tz} & 0 & 2k_{tz}l_c & 0 \\ -2k_{ty}H_{bt} & 0 & 2k_{ty}H_{cb}H_{bt} - 2k_{tz}d_{sk}^2 & 0 & 0 \\ 0 & 0 & 0 & 2k_{tx}H_{cb}H_{bt} & 0 \\ 0 & 0 & 0 & 0 & -2k_{tx}d_{sk}^2 \end{bmatrix} \quad (9b)$$

$$\mathbf{K}_{22} = \mathbf{K}_{33} = \begin{bmatrix} 4k_{py} + 2k_{ty} & 0 & 4k_{pz} + 2k_{tz} & \text{symmetry} & 0 & 0 \\ 0 & 4k_{pz} + 2k_{tz} & \text{symmetry} & 0 & 0 & 0 \\ 2k_{ty}H_{bt} - 4k_{py}H_{tw} & 0 & \tilde{k}_{33} & 0 & 4k_{pz}l_t^2 + 2k_{tx}H_{bt}^2 & 0 \\ 0 & 0 & 0 & 0 & 0 & \tilde{k}_{55} \\ 0 & 0 & 0 & 0 & 0 & \tilde{k}_{55} \end{bmatrix} \quad (9c)$$

where

$$\tilde{k}_{33} = 4k_{py}H_{tw}^2 + 4k_{pz}d_{wk}^2 + 2k_{ty}H_{bt}^2 + 2k_{tz}d_{sk}^2 \quad (10a)$$

$$\tilde{k}_{55} = 4k_{px}d_{wk}^2 + 4k_{py}l_t^2 + 2k_{tx}d_{sk}^2 \quad (10b)$$

$$\mathbf{K}_{31} = \begin{bmatrix} -2k_{ty} & 0 & 2k_{ty}H_{cb} & 0 & 0 \\ 0 & -2k_{tz} & 0 & -2k_{tz}l_c & 0 \\ -2k_{ty}H_{bt} & 0 & 2k_{ty}H_{cb}H_{bt} - 2k_{tz}d_{sk}^2 & 0 & 0 \\ 0 & 0 & 0 & 2k_{tx}H_{cb}H_{bt} & 0 \\ 0 & 0 & 0 & 0 & -2k_{tx}d_{sk}^2 \end{bmatrix} \quad (10c)$$

$$\mathbf{K}_{42} = \mathbf{K}_{63} = \begin{bmatrix} -2k_{py} & 0 & 2k_{py}H_{tw} & 0 & -2k_{py}l_t \\ 0 & -2k_{pz} & 0 & 2k_{pz}l_t & 0 \\ 0 & 0 & -2k_{pz}d_{wk}^2 & 0 & 0 \\ 0 & 0 & 0 & 0 & -2k_{px}d_{wk}^2 \end{bmatrix} \quad (10d)$$

$$\mathbf{K}_{52} = \mathbf{K}_{73} = \begin{bmatrix} -2k_{py} & 0 & 2k_{py}H_{tw} & 0 & 2k_{py}l_t \\ 0 & -2k_{pz} & 0 & -2k_{pz}l_t & 0 \\ 0 & 0 & -2k_{pz}d_{wk}^2 & 0 & 0 \\ 0 & 0 & 0 & 0 & -2k_{px}d_{wk}^2 \end{bmatrix} \quad (10e)$$

$$\mathbf{K}_{44} = \mathbf{K}_{55} = \mathbf{K}_{66} = \mathbf{K}_{77} = \begin{bmatrix} 2k_{py} & 0 & 0 & 0 \\ 0 & 2k_{pz} & 0 & 0 \\ 0 & 0 & 2k_{pz}d_{wk}^2 & 0 \\ 0 & 0 & 0 & 2k_{px}d_{wk}^2 \end{bmatrix} \quad (10f)$$

where  $H_{cb}$ ,  $H_{bt}$  and  $H_{tw}$  are the distance between the gravity centre of the carriage body and the upper suspension, upper suspension and the bogie, and bogie and the wheelsets, respectively;  $l_t$  and  $l_c$  are the half width of the wheelbase and length of carriage, respectively;  $d_{wk}$  and  $d_{sk}$  are the half lateral width of the upper and lower suspensions, respectively; and  $k_{px}$ ,  $k_{py}$  and  $k_{pz}$  and  $k_{tx}$ ,

$k_{ty}$  and  $k_{tz}$  are the elasticity coefficients of the upper and lower suspensions in the three directions, respectively.

The corresponding damp matrix  $\mathbf{C}_v$  is identical with  $\mathbf{K}_v$  in terms of arrangement, except for different magnitudes.

## 2.2. Modelling of track

The ballastless track is widely used in HSR. The rail is fixed in the sleeper via fastener, which is simulated using springs and dampers (see Figure 3). The sleeper is assumed to be fully restrained. The matrix equation of the rail is identical with Eq. (1) in form [31].

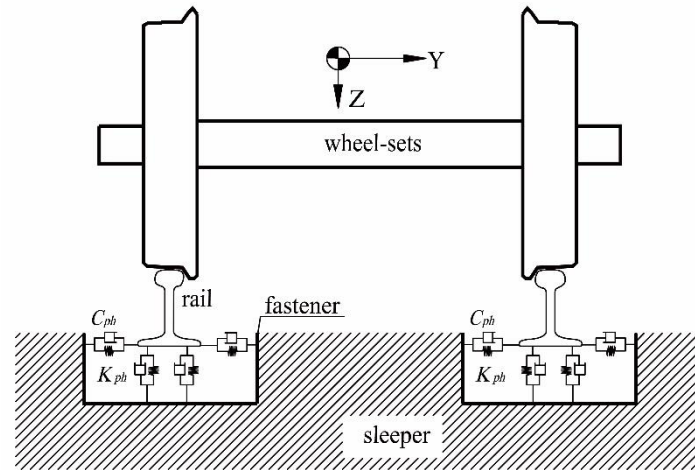


Figure 3. Model of track.

Figure 4 shows the schematic diagram of track irregularity. The power spectrum density (PSD) is widely used to describe track irregularities and is expressed as follows [31,32]:

$$\begin{cases} S_v(\Omega) = \frac{A_v \Omega_c^2}{(\Omega^2 + \Omega_r^2)(\Omega^2 + \Omega_c^2)} \\ S_a(\Omega) = \frac{A_a \Omega_c^2}{(\Omega^2 + \Omega_r^2)(\Omega^2 + \Omega_c^2)} \\ S_c(\Omega) = \frac{A_v b^{-2} \Omega_c^2 \Omega^2}{(\Omega^2 + \Omega_r^2)(\Omega^2 + \Omega_c^2)(\Omega^2 + \Omega_s^2)} \\ S_g(\Omega) = \frac{A_g \Omega_c^2 \Omega^2}{(\Omega^2 + \Omega_r^2)(\Omega^2 + \Omega_c^2)(\Omega^2 + \Omega_s^2)} \end{cases} \quad (11)$$

where  $S_v(\Omega)$ ,  $S_a(\Omega)$ ,  $S_c(\Omega)$  and  $S_g(\Omega)$  are the PSDs of vertical, directional, lateral and gauge irregularities, respectively.  $\Omega$  is the space frequency of the track irregularity.  $A_v$  and  $A_a$  are the roughness constants.  $A_g$  is calculated by the reference value of the roughness constants.  $\Omega_c$ ,  $\Omega_r$  and  $\Omega_s$  are the cut-off frequencies. The German low-interference track spectrum is used as the



track irregularity specimen in this simulation, where  $A_v = 4.032 \times 10^{-7}$ ,  $A_a = 2.119 \times 10^{-7}$ ,  $A_g = 5.32 \times 10^{-7}$ ,  $\Omega_c = 0.8246$ ,  $\Omega_r = 0.0206$  and  $\Omega_s = 0.438$ .

The wheel-rail contact model, which solved by the 3D space trace method, is expressed by Deng et al. [8,10].

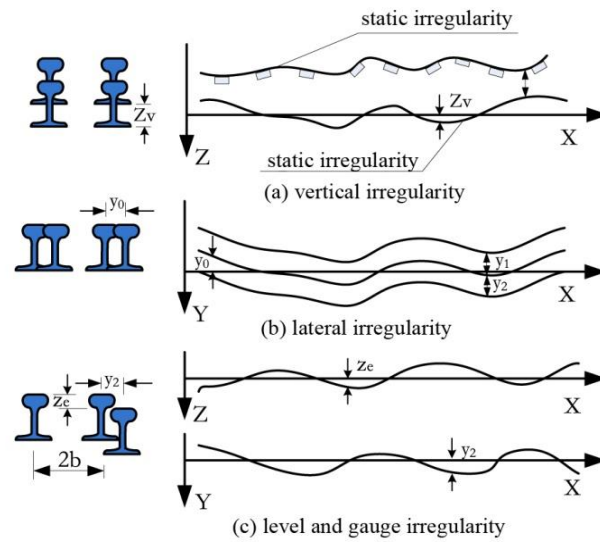


Figure 4. Schematic diagram of track irregularity.

### 3. Simulation of aerodynamic loads

#### 3.1. Governing equations for fluids

According to the engineering background of the present study, the air-flow that involves the train, tunnel and crosswind are solved by a three-dimensional, compressible, RNG  $k-\varepsilon$  turbulence model, which has been widely used in similar study [12,13,33-35]. The governing equations are as follows:

$$\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x_i} (\rho u_i) = 0 \quad (12)$$

$$\frac{\partial}{\partial t} (\rho u_i) + \frac{\partial}{\partial x_j} (\rho u_i u_j) = -\frac{\partial p}{\partial x_i} + \rho g \delta_{i3} + \frac{\partial}{\partial x_j} \left[ \mu \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) - \frac{2}{3} \delta_{ij} \frac{\partial u_l}{\partial x_l} \right] + \frac{\partial}{\partial x_j} (-\rho \overline{u_i u_j}) \quad (13)$$

where  $\rho$  represents the air density;  $p$  represents the aerodynamic pressure;  $u'$  and  $u$  are the pulsating and the average velocities, respectively;  $\mu$  represents the air dynamic (molecular) viscosity; the subscripts  $i, j=1, 2, 3$  represent the  $x, y$  and  $z$  directions, respectively;  $g$  represents the gravitational acceleration;  $\delta$  is the Kronecker delta.

#### 3.2. Aerodynamic loads

The aerodynamic forces and moments (i.e. side and lift forces and rolling, pitching and yawing moments) are defined in Eqs. (14). Here, the center of the moment is the barycenter of the carriage body, as shown in Figure 5 (take the middle carriage as an example).

$$\begin{aligned}
F_{wy} &= \sum_{i=1}^n \left( \sum_{j=1}^k (p_{i,j} \cdot S_{i,j} \cdot (\mathbf{n}_{i,j} \cdot \mathbf{y})) \right) \\
F_{wz} &= \sum_{i=1}^n \left( \sum_{j=1}^k (p_{i,j} \cdot S_{i,j} \cdot (\mathbf{n}_{i,j} \cdot \mathbf{z})) \right) \\
M_{wx} &= \sum_{i=1}^n \left( \sum_{j=1}^k (p_{i,j} \cdot S_{i,j} \cdot (\mathbf{r}_{i,j} \times \mathbf{n}_{i,j})) \right) \\
M_{wy} &= \sum_{i=1}^n \left( \sum_{j=1}^k (p_{i,j} \cdot S_{i,j} \cdot (\mathbf{n}_{i,j} \cdot \mathbf{z}) \cdot x_i) \right) \\
M_{wz} &= \sum_{i=1}^n \left( \sum_{j=1}^k (p_{i,j} \cdot S_{i,j} \cdot (\mathbf{n}_{i,j} \cdot \mathbf{y}) \cdot x_i) \right)
\end{aligned} \tag{14}$$

where, the  $k$  is the number of calculation faces along the circumferential direction;  $n$  is the segments number along the X-axis;  $\mathbf{y}$  and  $\mathbf{z}$  represent the unit vectors along the Y- and Z-axes, respectively;  $\mathbf{n}_{i,j}$  represents the unit normal vector of Surface ( $i$ th,  $j$ th);  $S_{i,j}$  represents the area of Surface ( $i$ th,  $j$ th);  $p_{i,j}$  represents the transient average pressure acting on Surface ( $i$ th,  $j$ th);  $x_i$  represents the projection length of the line between the carriage barycentre and the Surface ( $i$ th,  $j$ th) centre on the X-axis; and  $\mathbf{r}_{i,j}$  represents the moment arm vector on the  $i$ th cross section.

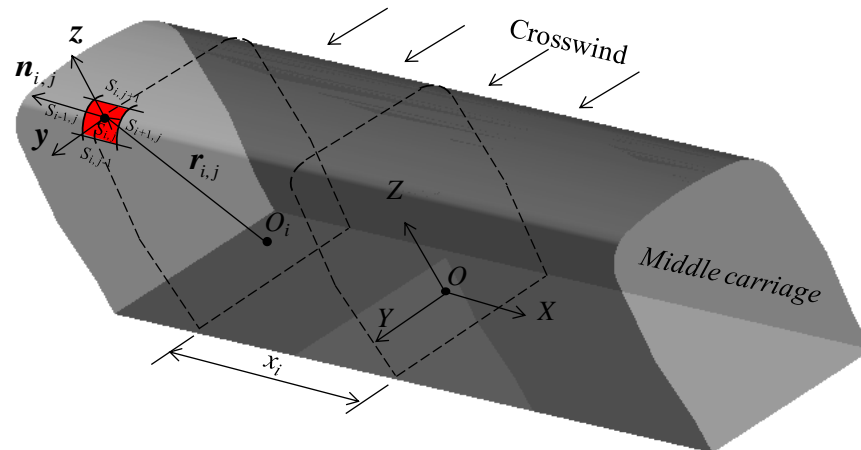


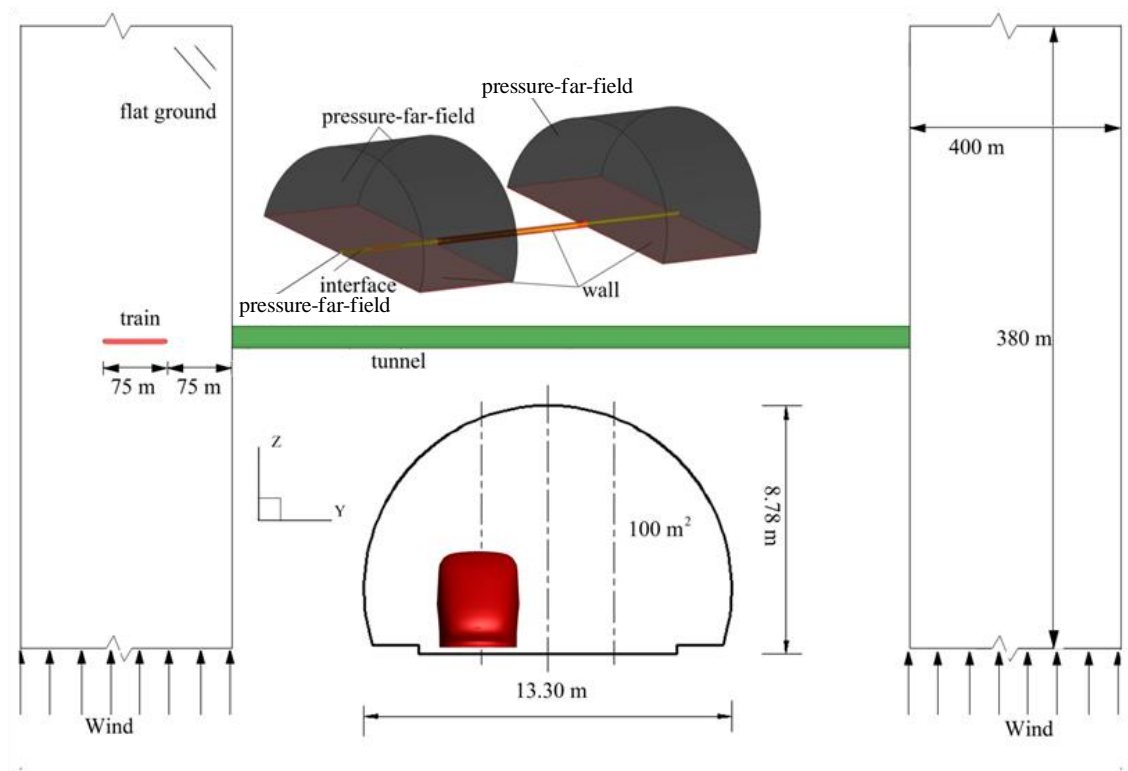
Figure 5. Calculation schematic of aerodynamic loads.

## 4. Numerical demonstration

### 4.1. Scenario prototype

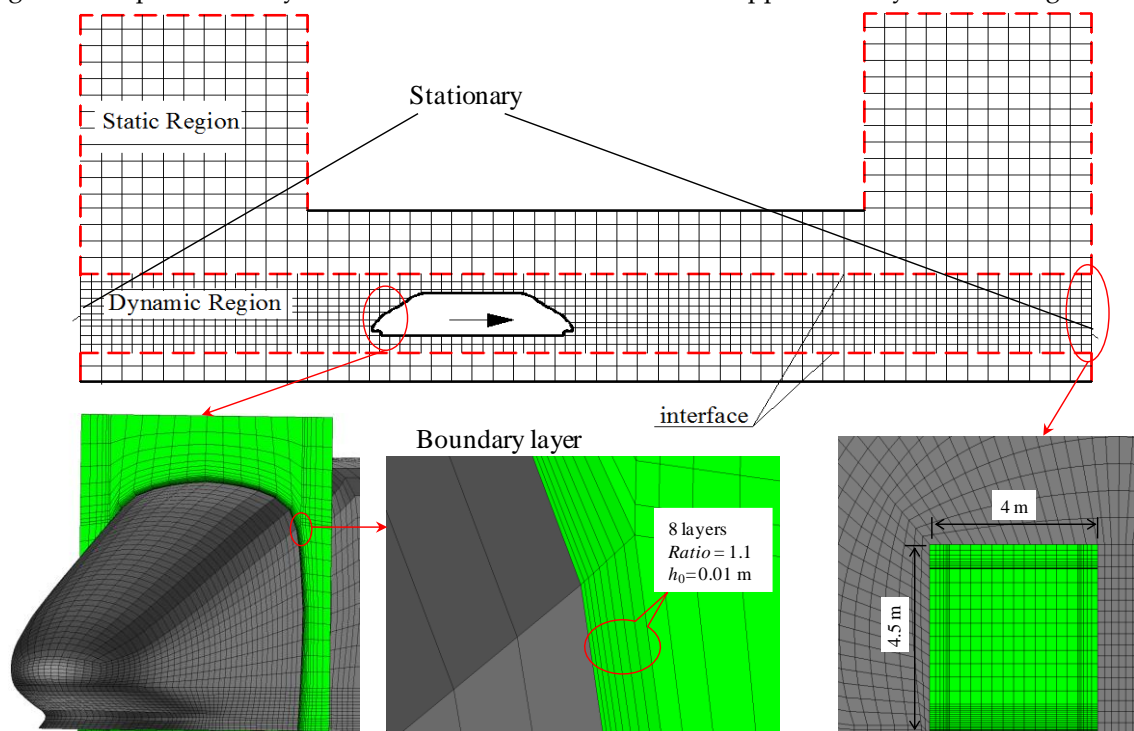
The total clear area of the prototype tunnel is 100 m<sup>2</sup>, which is used in more than 90% the operating HSR in China to date and accommodates two rails that run in opposite directions. The length of the tunnel and flat ground is 1005 m and 400 m, respectively. The train is modelled on the basis of the CRH3 prototype, designed at a maximum speed of 350 km/h. The train length is 76 m, which consists of three continuous carriages. The width and height of the train is 3.075 m and 3.89 m, respectively. The train speed is defined by the Profile function in Fluent.

For boundary conditions, the atmospheric boundaries outside the tunnel (including entrance and exit) are applied by Pressure-far-field. Crosswinds are set at the Pressure-far-field boundaries. The crosswind velocity direction is perpendicular to the running direction of the HST. Non-slip wall is applied to the flat ground, train and tunnel surfaces and two ends of the tunnel (see Figure 6).



**Figure 6.** Typical numerical configuration of plan view.

The whole computational zone is divided into static and dynamic regions by structural hexahedral grids (see Figure 7). The relative motion between the train and flat ground is realized by Layering dynamic mesh method [8,10,12,13]. Data transmission between the static and dynamic regions is implemented by Interface. The entire model contains approximately 9.5 million grids.

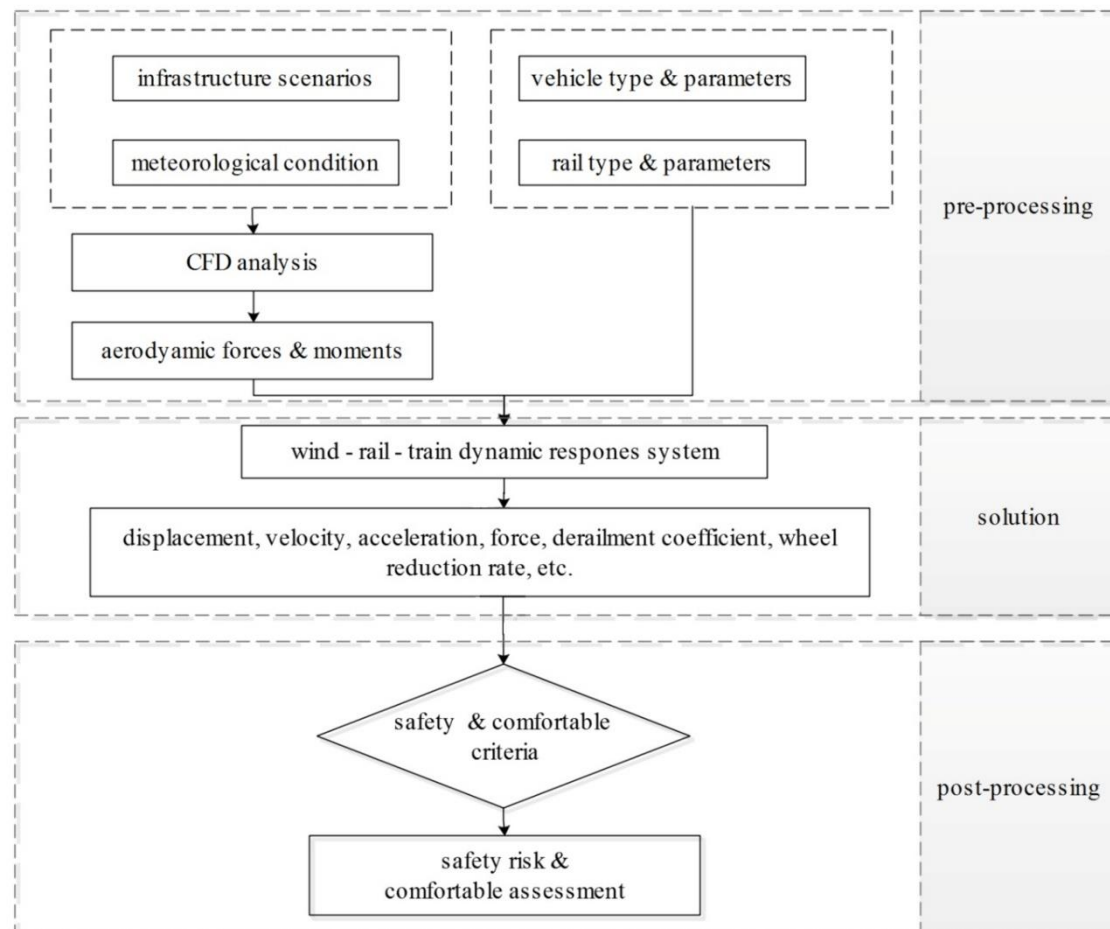


**Figure 7.** Schematic diagram of mesh model.

#### 4.2. Solving process

The safety analysis in this study follows the methodologies of CEN code [26]. The train's aerodynamic loads are obtained on the basis of CFD analysis, in which the pressure-based solver is adopted in a segregated manner to solve the unsteady flow in the process of train running. See References [12,13] for the specific solution process. The five aerodynamic loads calculated by Eqs (14) are substituted into Eq. (3a). The loading position of the aerodynamic loads is at point O in Figure 5. In the segregated algorithm, the individual governing equations for the solution variables are solved one after another. The time-step size of the CFD solution is determined to be  $1 \times 10^{-3}$  s.

A self-developed program called wind–train–rail structure (WTRSDYNA) is used to perform a case study [8,10,31]. The time-step size of the program solution is determined to be  $2 \times 10^{-4}$  s. The dynamic responses (i.e. acceleration, velocity and displacement of train and wheel), wheel–rail contact force, safety coefficients (i.e. DC and WRR) and other dynamic responses of carriages are all obtained from WTRSDYNA. Figure 8 shows the outline of the WTRSDYNA coupling solution.



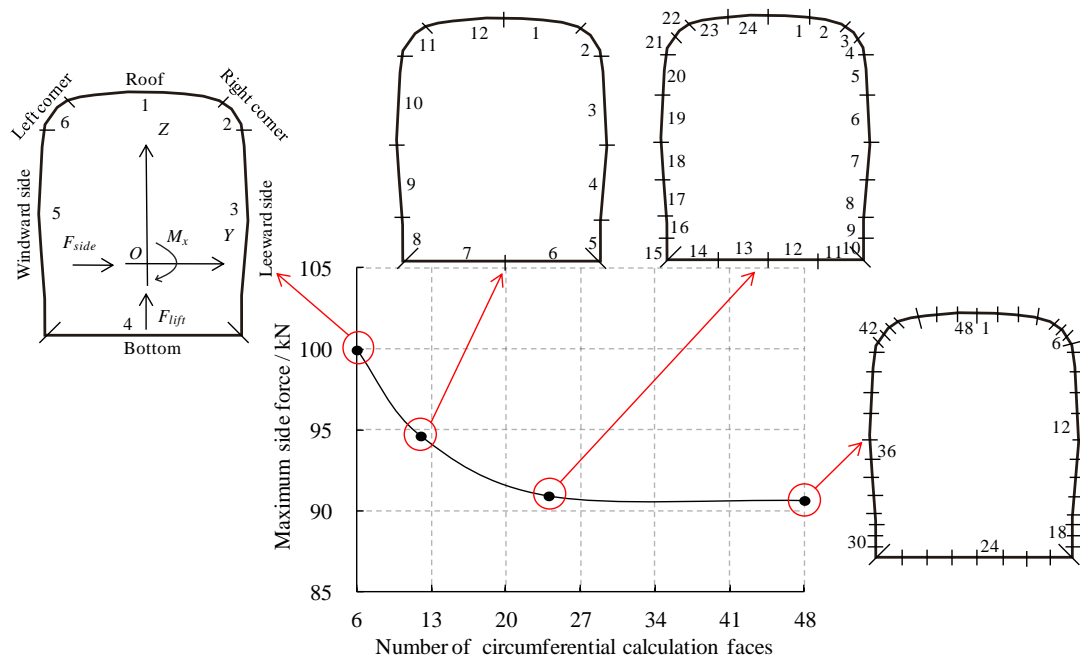
**Figure 8.** Outline of the WTRS coupling solution.

#### 4.3. Verification

##### 4.3.1. Verification of calculation scheme

The partition scheme of the calculation face may affect the calculation results of aerodynamic loads, e.g., the number of calculation faces along the circumferential direction and the number of segments along the longitudinal direction. The more the number of calculation faces, the higher the accuracy of calculation and the lower the efficiency of calculation. Assuming that the number of segments along the longitudinal direction is sufficient ( $n=20$ ), and four schemes for dividing the circumferential calculation faces are set up for comparison, as shown in Figure 9. The circumferential calculation faces are subdivided into 6, 12, 24 and 48 pieces, respectively (i.e. the  $k$  is 6, 12, 24 and 48,

respectively). The maximum side force of the head carriage when the train running in flat ground under crosswind is taken as the target indicator. The remaining conditions for the four cases are consistent. For example, the number of the longitudinal segments remains consistent, the train's running speed is 250 km/h and the crosswind velocity is 25 m/s.

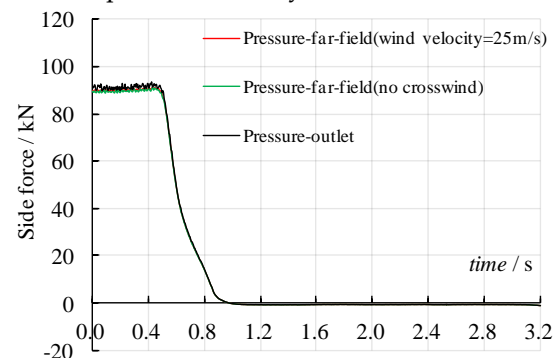


**Figure 9.** Maximum side force of head carriage under conditions of different numbers of circumferential calculation faces (train speed =250 km/h; wind velocity =25 m/s).

It is shown from Figure. 9 that the calculation result was significantly reduced when the number of circumferential calculation faces increased to 24. As the number of circumferential calculation faces continues to increase, the result will tend to be stable. It can be seen that it is appropriate to adopt the scheme of  $k = 24$  and  $n = 20$ .

#### 4.3.2. Verification of boundary condition

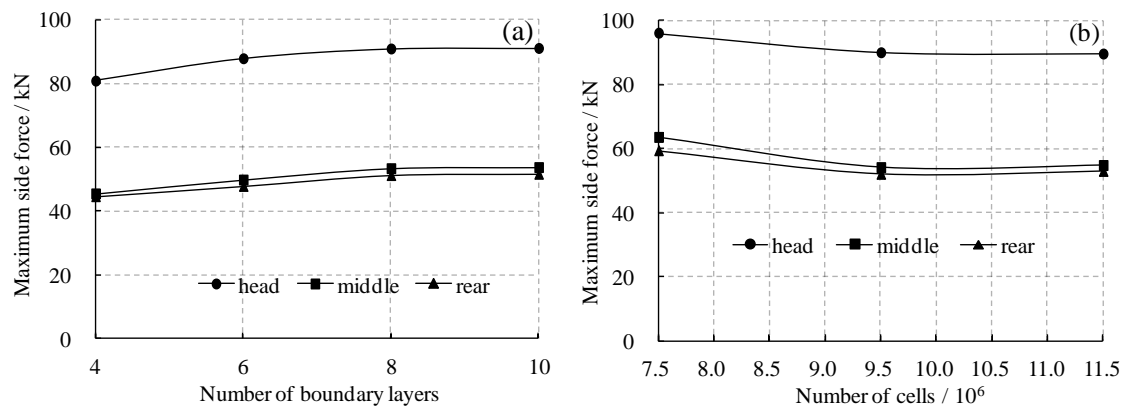
To check the influence of boundary conditions at the tunnel exit on the calculation results in present study, the atmospheric boundary at the tunnel exit is set as three conditions, i.e. Pressure-far-field boundary (crosswind velocity =25m/s ), Pressure-far-field boundary (no crosswind) and Pressure-outlet boundary. The time-history data of side force of the head carriage during the train entering tunnel is taken as target indicator. The atmospheric boundary conditions at the tunnel entrance remain unchanged (Pressure-far-field boundary with 25 m/s crosswind) and the train speed is maintained at 250 km/h in three cases. It is shown from Figure 10 that the target indicator is basically not affected by the atmospheric boundary conditions at the exit.



**Figure 10.** Time-history of side force of head carriage during train entering tunnel under three boundary conditions (train speed =250 km/h).

#### 4.3.3. Analysis of mesh sensitivity

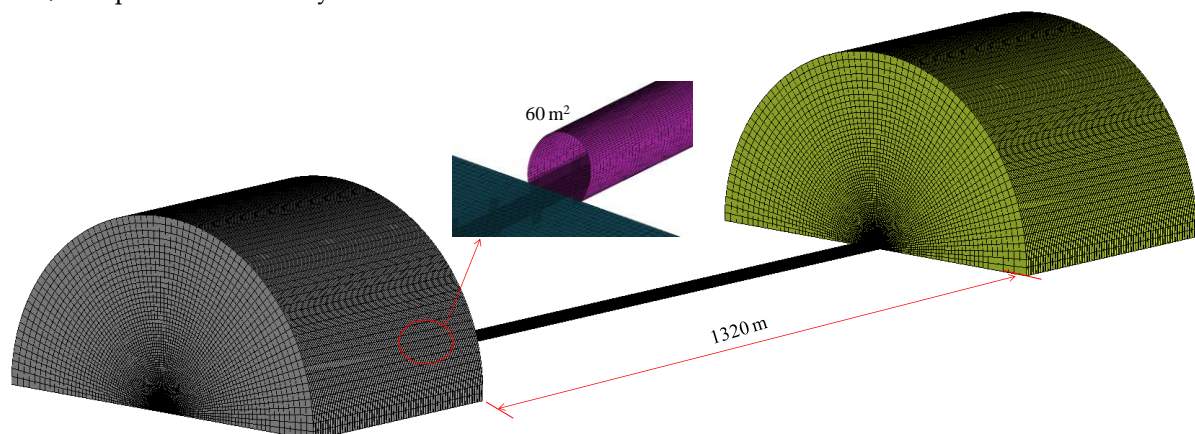
In this section, the mesh sensitivity of the present model will be checked from two aspects, i.e. the number of boundary layers and grid elements. The target indicators are the maximum side force of head, middle and rear carriages during the train running in flat ground under crosswind. First, the calculation results of four models with different number of boundary layers are compared, as shown in Figure 11(a). In each case, the height of the first layer and the entire boundary layer remains constant (see Figure 7). The crosswind velocity and the train speed remain at 25 m/s and 250 km/h, respectively. It can be seen from Figure 11(a) that the target indicators remain constant when the number of boundary layers increases to 8. Then, the number of grid elements of the whole model is set to 7.5, 9.5 and 11.5 millions, as shown in Figure 11(b). The number of boundary layers for each model remains at 8. As indicated in Figure 11(b), the target indicators tend to stabilise when the number of cells increases to  $9.5 \times 10^6$ . Therefore, it can be considered that the scheme of grid size adopted in present study is reasonable.



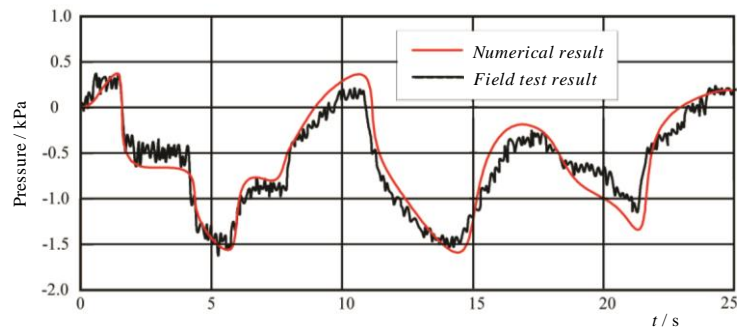
**Figure 11.** Maximum side force of three carriages under conditions of (a) different boundary layer densities and (b) mesh element numbers (train speed =250 km/h; wind velocity =25 m/s).

#### 4.3.4. Verification of aerodynamic pressure

The transient pressure calculated by the present numerical algorithm is compared with that obtained by the corresponding field test [36,37] to verify the accuracy of the adopted algorithm in this simulation. The length and clearance area of the test tunnel are 1320 m and 60 m<sup>2</sup>, respectively. A ground–tunnel–ground numerical model with the same tunnel is established to ensure the validity of the verification (Figure 12). The geometric shapes of the train (CRH3) and tunnel in the numerical model are consistent with the field test prototypes. The train speed in this test is approximately 200 km/h, and wind velocity ( $V_w$ ) is ignored. The monitoring point is located on the outside of the front side window on the head carriage. Figure 13 shows the comparison of the time-history data between the numerical simulation and field test. The waveform shows a remarkable correlation between the two, except for minimal asynchronous time.





**Figure 12.** The numerical model corresponding to the field test.**Figure 13.** Comparison of the time history of pressure on the train surface between the field test and the present numerical simulation (train speed =200 km/h; wind velocity =0 m/s).

## 5. Aerodynamic loads and safety analysis

### 5.1. Flow structure and aerodynamic loads

Figure 14 shows the variations of the pressure and flow structure around the train when approximately half of the middle carriage reaches the tunnel entrance for train speed of 250 km/h and crosswind speed of 15 m/s, and those at 25 m/s are shown in Figure 15.

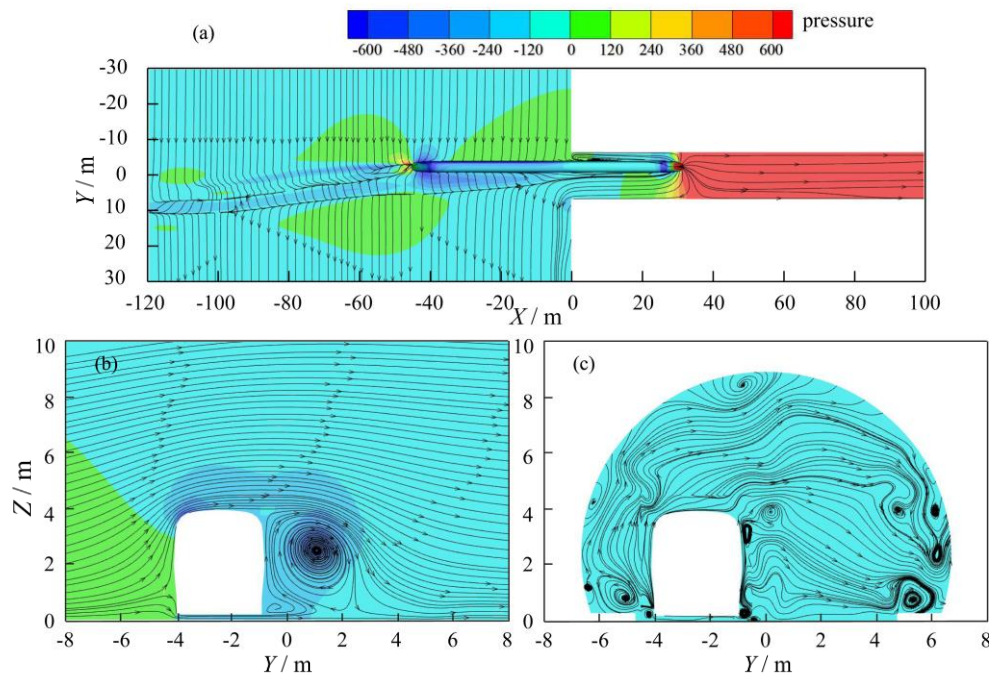
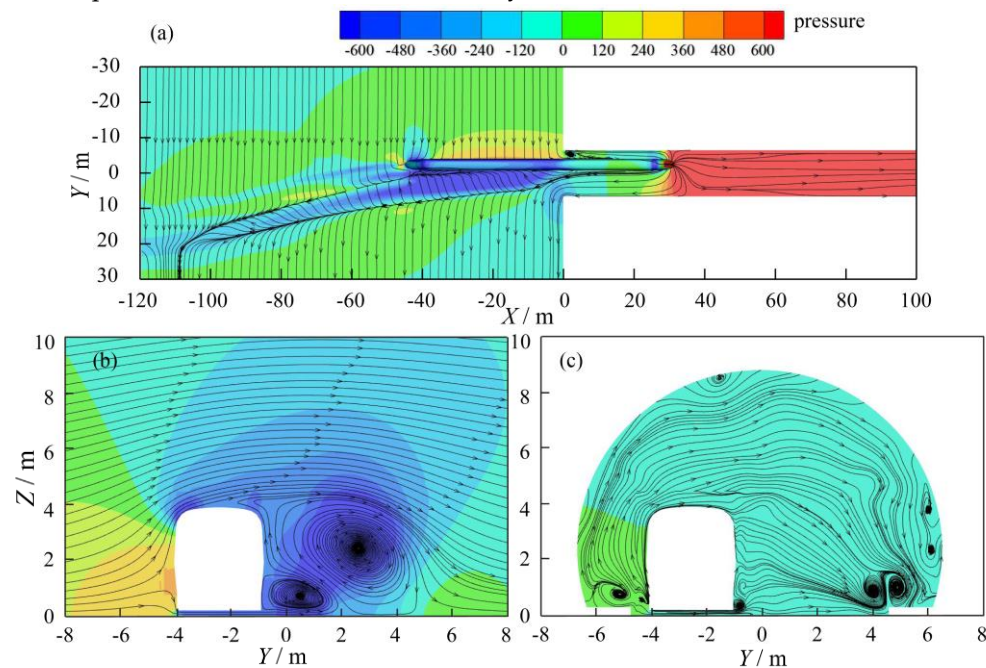
**Figure 14.** Pressure and flow distribution for train speed =250 km/h, crosswind velocity = 15 m/s, (a)  $z = 1.55$  m from top of rail, (b) 10 m outside tunnel entrance, and (c) 10m inside tunnel entrance.

Figure 14 shows that in open air, the flow structure shows remarkable asymmetry where crosswind is applied to the train. A series of vortices considerably originate from the tunnel entrance and stretch to the train tail along the leeward side. The vortices originate from the tip of the head carriage and stretch behind far away the tip of the rear carriage when the train running completely outside the tunnel. The vortices gradually retreat from the entrance as the train goes on. In open air, the pressure on the train shows the positive values at the windward side and negative values at the leeward side because of crosswind. Relatively, inside the tunnel, the vortex around the carriage rapidly disappears, and pressure in both sides of the train shows a basic symmetry. Sudden variations

along the longitudinal of flow structures around the train at the tunnel entrance were discovered. During these instances, such a difference of the flow fields between inside and outside the tunnel entrance can explain the sudden variation of aerodynamic forces and moments on the train.



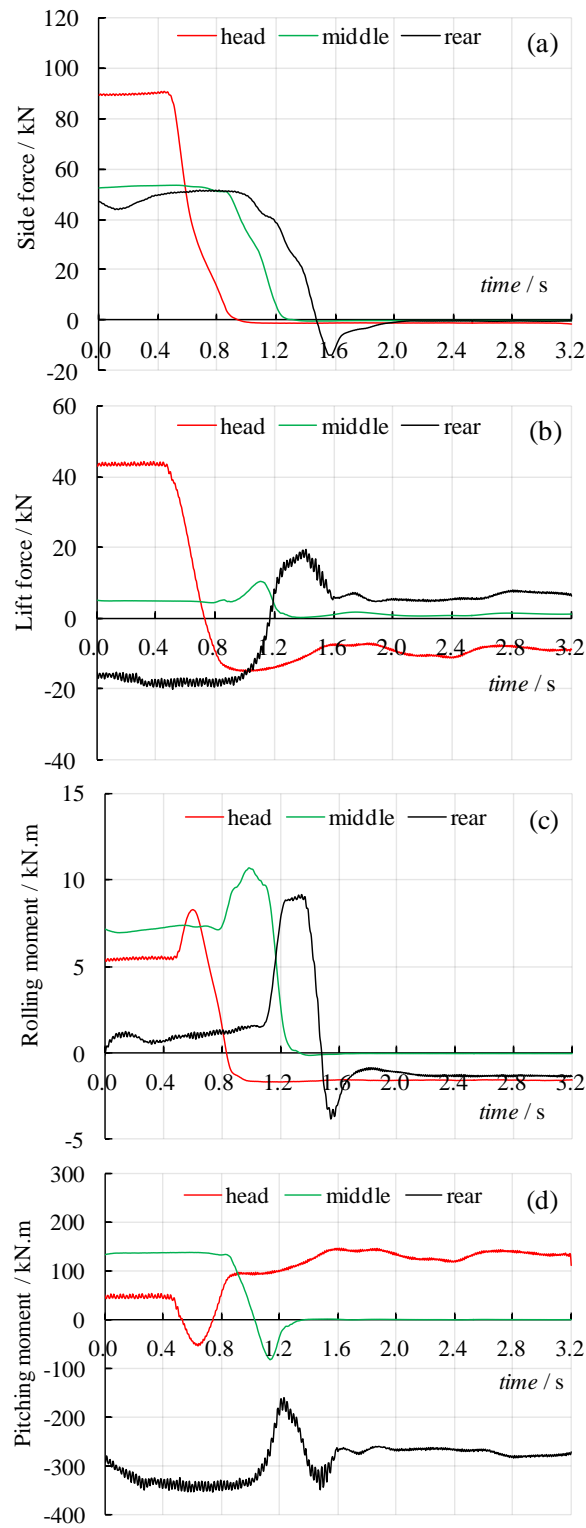
**Figure 15.** Pressure and flow distribution for train speed =250 km/h, crosswind velocity = 25 m/s, (a)  $z = 1.55$  m from top of rail, (b) 10 m outside tunnel entrance, and (c) 10m inside tunnel entrance.

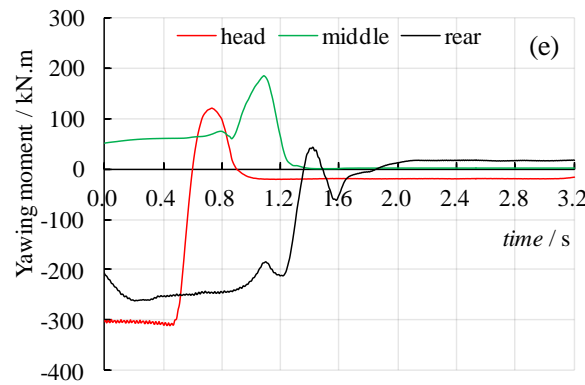
According to the Figure 15, the difference of flow fields between the leeward and windward sides of the train outside the tunnel becomes considerable as the wind speed increases. Figure 15(b) shows that the two larger vortexes in the leeward side and the pressure difference on both sides of the train increases outside the tunnel. Nevertheless, compared with Figure 14(c), there is no substantial change in the flow structure and pressure around the train inside the tunnel (see Figure 15(c)). Thus, the sudden variation of the aerodynamic forces and moments under condition of higher crosswind velocity may be remarkable.

Figures. 16(a)–(e) show the time-histories of the five aerodynamic loads (i.e. side and lift forces and rolling, pitching and yawing moments, respectively) during the train entering tunnel under conditions of train speed =250 km/h and crosswind velocity = 25 m/s. The red, green and black lines represent the head, middle and rear carriages, respectively.

Figure 16 shows that the five aerodynamic loads of the three carriages all characterise a sudden variation when entering tunnel. For example, the side force, regardless whether the head, middle and rear carriages, show a dramatic decrease (see Figure 16(a)). For the lift force, except for the head carriage, both the middle and rear carriages are showing an upward shock (see Figure 16(b)). This phenomenon may be attributed to the jet flow, which is exhausted outside the entrance along the hoop space between the train body and the tunnel. The hoop space, which is larger in the train top side than the bottom, is asymmetrical in the vertical direction, thereby causing the aerodynamic pressure on the bottom of the train to be larger than that on the top. Such a phenomenon mainly occurs in open air approximately 20 m away from the tunnel entrance. Therefore, the impact caused by the jet flow will not affect the side and lift forces of the head carriage.







**Figure 16.** Evolution of five aerodynamic loads with respect to time during train entering tunnel, train speed =250 km/h, crosswind velocity = 25 m/s.

For the aerodynamic moments, the variation characteristic of the rolling moment is similar to that of yawing moment. Once the corresponding carriages enter the tunnel, they will all have a positive peak (see Figures. 16(c) and (e)). The reason for the overshoot of the yawing moment is the pressure difference on both sides of the train changes significantly along longitudinal as the part of the carriage is shielded from the crosswind by the tunnel. While the overshoot of the rolling moment may also be attributed to the jet flow. The double-track tunnel adopted in the simulation causes the centre of the train not to coincide with that of the tunnel. The aerodynamic impact pressure caused by jet flow in the near-wall side is larger than that in the tunnel centre side. In addition, the flow structure of jet flow presents a laminar flow on the tunnel wall side and turbulent flow on the tunnel centre side. The pitching moment of the head and middle carriages present a downward pulse successively when entering the tunnel. (see Figure 16(e)). While in the corresponding process, the pitching moment of the rear carriage appears upward and downward pulses successively in the time interval of about 0.3 s.

To sum up, except for the side and lift forces of the head carriage, the remaining aerodynamic loads all show upward or downward impulse when entering the tunnel, which may be a key factor threatening the safety of the train traffic. However, the variation amplitudes of aerodynamic side force, lift force and yawing moment of the head carriage are greater than those of middle and rear carriages. The safety risks of the three carriages still need further discussion in the next section.

## 5.2. Safety analysis

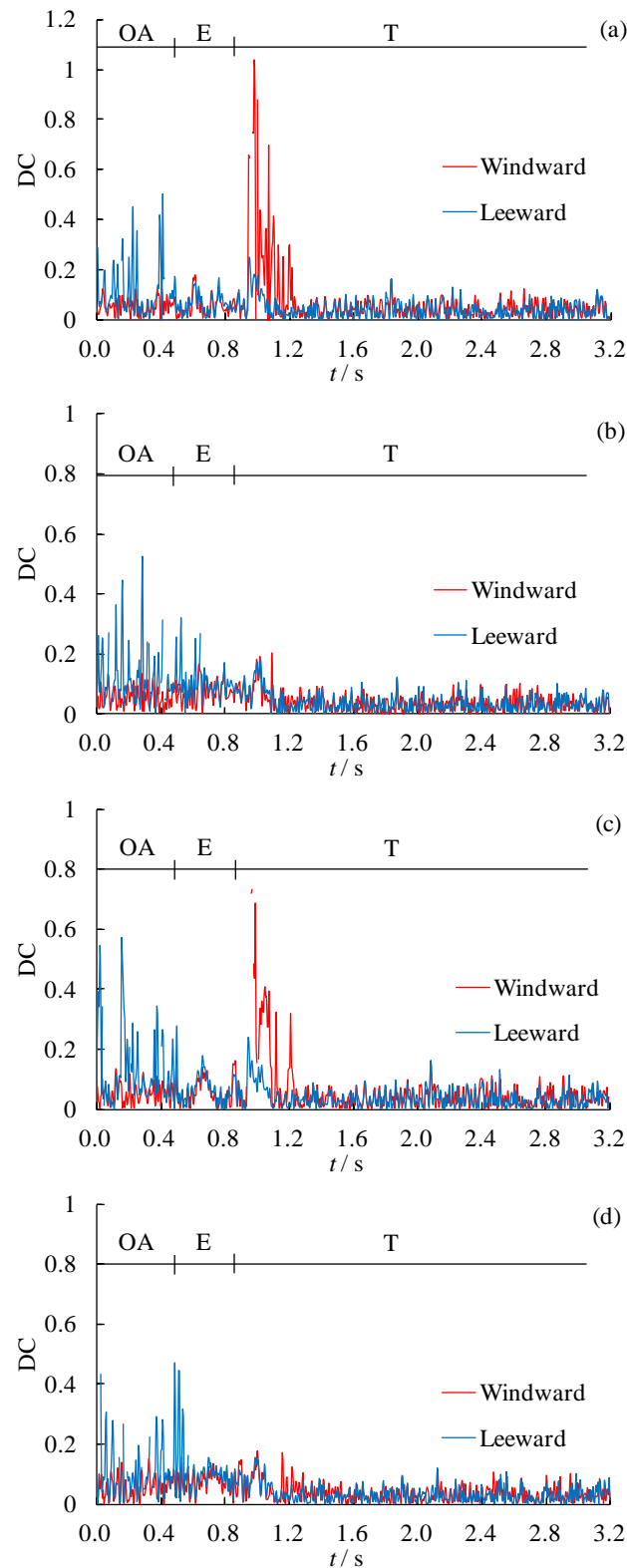
### 5.2.1. Derailment coefficient

The rollover accident will occur when the side contact force exceeds the vertical contact force to a certain extent. The rollover accident is discerned with DCs, which is defined as follow [38]:

$$DC = Q/P \quad (15)$$

where  $Q$  and  $P$  are the side and vertical contact forces, respectively.

Figure 17 demonstrates the evolution of DCs with respect to the time of the head carriage wheelsets during the train entering tunnel under conditions of train speed =250 km/h and crosswind velocity = 15 m/s. The value of DCs is removed when the value of the vertical contact force is zero. In this moment, the wheel tread has been detached from the rail top and the DCs are meaningless. Section 5.2.3 will discuss the safety assessment of the sudden separation of the wheel and rail.

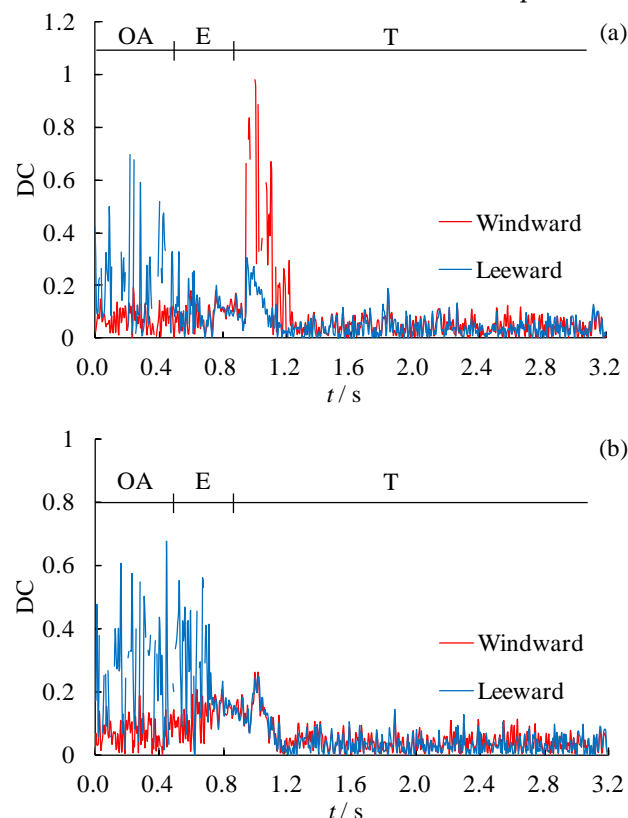


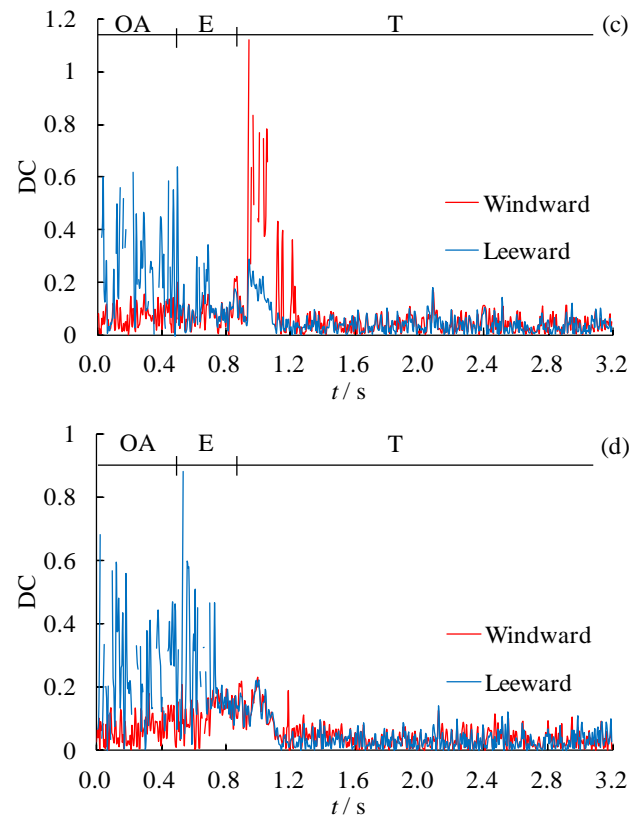
**Figure 17.** Time-history of head carriage DC conditioned train speed 250 km/h, crosswind velocity 15m/s , (a) 1st wheelset, (b) 2nd wheelset, (c) 3rd wheelset, (d) 4th wheelset (“OA” for open air, “E” for entering entrance, “T” for tunnel).

Figure 17(a) shows that the global maximum of the DCs is likely to happen when the train arrives at the tunnel entrance. When the time is less than approximately 0.5 s, the entire carriage runs in open air, the train withstands the side force from the crosswind and the rail in the leeward side is pressed by the edge of the wheel. This phenomenon is the reason why the DCs in the leeward side are larger

and easier to fluctuate than those in the other side. Therefore, the maximum DC in the leeward and windward sides is 0.56 and 0.15, respectively. When the carriage has completely entered the tunnel, the side force in the windward suddenly revokes at this moment (approximately 1.1 s), thereby causing the sudden reverse rotation of the carriage around the longitudinal axis. The vertical contact force of the wheel in the windward side suddenly increases, thereby shocking the DCs in the windward side upwards. The shielding effects of the aerodynamic loads induced by the tunnel is intensely sudden, such that the global maximum of the DCs is presented (e.g. approximately 1.04 for the first wheelset, nearly 2 times than the maximum DCs in the open air). Finally, the DCs at both sides decrease to less than 0.2 when the carriage enters the tunnel (after 1.1 s).

Notably, the sudden variation of the DCs due to the shielding effect of the tunnel in the lateral direction mainly occurs in the first and third wheels of windward side when the train is entering the tunnel (Figures. 17(a) and (c)). Furthermore, the DC of the second and fourth wheels in the windward side remains relatively stable (Figures. 17(b) and (d), respectively). The coupling effect of the aerodynamic loads shielded in the first wheel is probably larger than those of the others, and the suspension system of the train automatically adjusts the influence of aerodynamic unloading. For example, the safety risk of the third wheel in the windward side will increase with the wind speed. Figure 18 presents the evolution of DCs with respect to the time of the head carriage wheelsets under the conditions of train speed= 250 km/h and crosswind velocity= 25 m/s. It can be seen that the position where the maximum DC occurs shifted from the first wheel to the third wheel. This phenomenon may be caused by the pitching movement of the leading carriage. The pitching moment increases with the wind speed in open air. When the pitching moment of the carriage increases, the contact between the wheel tread of the rear bogie and rail top becomes closer. Thus, the position where the maximum DC occurs will move backward as the wind speed increases.

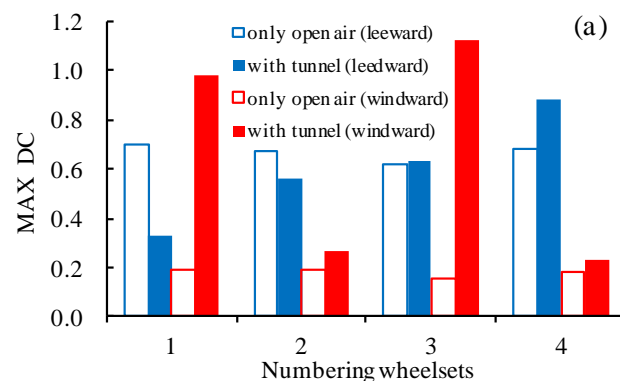


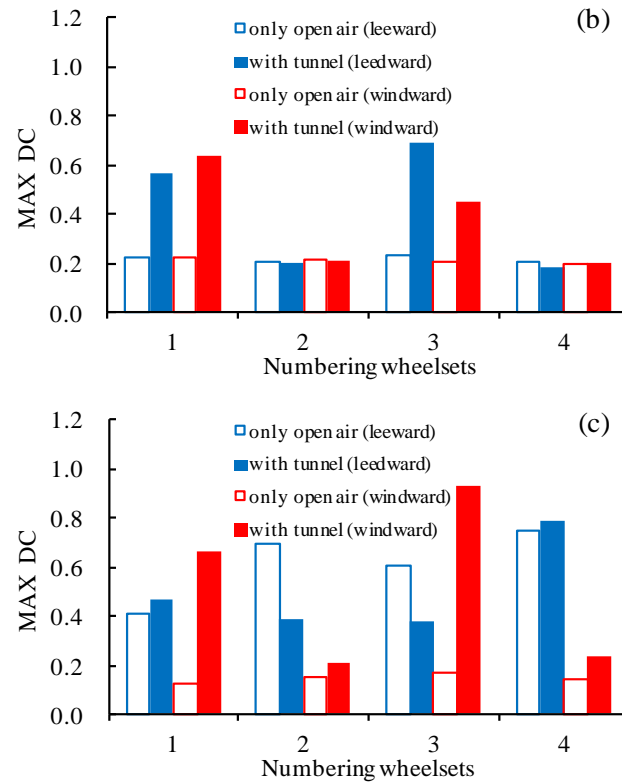


**Figure 18.** Time-history of head carriage DC conditioned train speed 250 km/h, crosswind velocity 25m/s, (a) 1st wheelset, (b) 2nd wheelset, (c) 3rd wheelset, (d) 4th wheelset (“OA” for open air, “E” for entering entrance, “T” for tunnel).

Figure 19 presents the comparison of all wheel’s maximum DC values amongst the head, middle and rear carriages during the two processes (i.e. only in open air and entering tunnel) under conditions of train speed =250 km/h and crosswind velocity = 25 m/s to discuss the influence of the aerodynamic variation on the train running safety.

It can be seen from Figure 19 that the maximum DC value of the rear carriage characterises similarly to that of the head carriage. At the third wheel in the windward side of rear carriage, the DC is approximately 0.17 and 0.93 when this carriage runs in open air and in the process of entry, respectively. The DC of third wheel for the windward side of rear carriage is larger than the others when entering the tunnel. The global maximum of DCs is slightly less than that of the head carriage. The reason for this phenomenon may be that the aerodynamic loads of the rear carriage are slightly lower than those of the head carriage (Figure 16). No significant difference of DCs is observed amongst the four wheelsets of the middle carriage when running in the crosswind environment completely. The maximum DC (0.69) of the middle carriage when it enters the tunnel is the minimum among the three carriages (Figure 19(b)).





**Figure 19.** Contrast of global maximum derailment coefficients conditioned train speed 250 km/h, crosswind velocity 25m/s: (a) head, (b) middle and (c) rear carriages.

Therefore, entering the tunnel from the crosswind environment will be more dangerous for the running train than running in crosswind completely, especially to the first and third wheels of the head and rear carriages in the windward side. The safety risk is more likely to happen in the third wheel in the windward side as the wind speed increases.

### 5.2.2. Wheel load reduction rate

When the vertical contact force of a wheel exceeds its original static wheel load, the wheel will be lifted, and the wheel unloading accident is likely to happen. The corresponding safety coefficient WRR [39] is defined as:

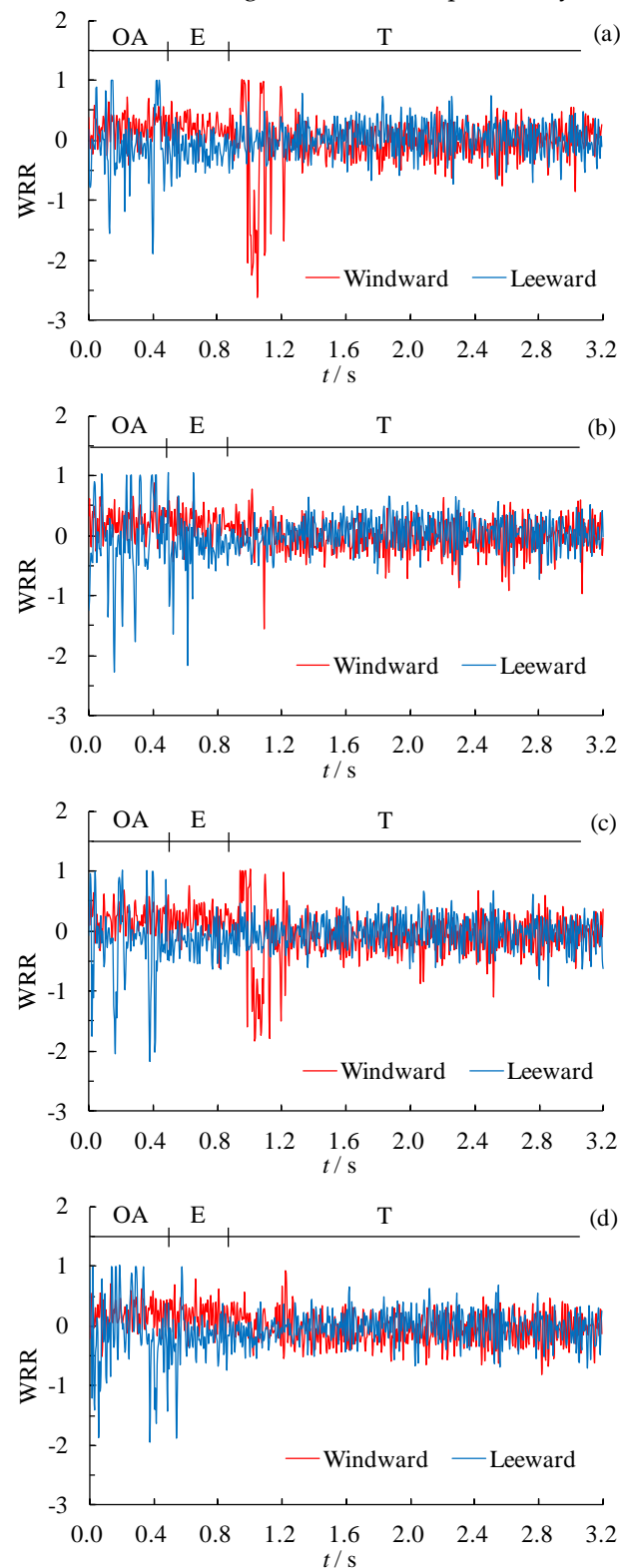
$$WRR = \Delta P / \bar{P} \quad (16)$$

where  $\Delta P$  represents the reduction amount of wheel load in one wheel, which is + for reducing and - for the increase of the vertical contact force.  $\bar{P}$  represents the load that the total train static self-weight equally distributes on each wheel.

Figure 20 demonstrates the time-history of WRR of the head carriage wheelsets during the train entering tunnel under the conditions of train speed= 250 km/h and crosswind velocity= 15 m/s.

Figures. 20(a)–(d) show that the carriage deflects to the leeward side, the vertical contact force decreases in the windward side, and WRR stabilized at a higher level in the windward side when the train runs in crosswind environment completely. While, the variation amplitude of the WRR in leeward side wheel is remarkably larger than that of the opposite side because the wheel tread on the leeward side is close contact with the rail top. When the train in the process of entry, the carriage turns aside towards the windward side due to the sudden disappearance of wind excitation. As shown in Figure 20(a), the WRR in the windward side decreases to -2.63 (the lowest value among the four wheelsets), whereas that in the leeward side increases to 0.64 instantaneously because of self-weight. Then, the WRR in the windward side rises to its global maximum of 1.0, indicating that the

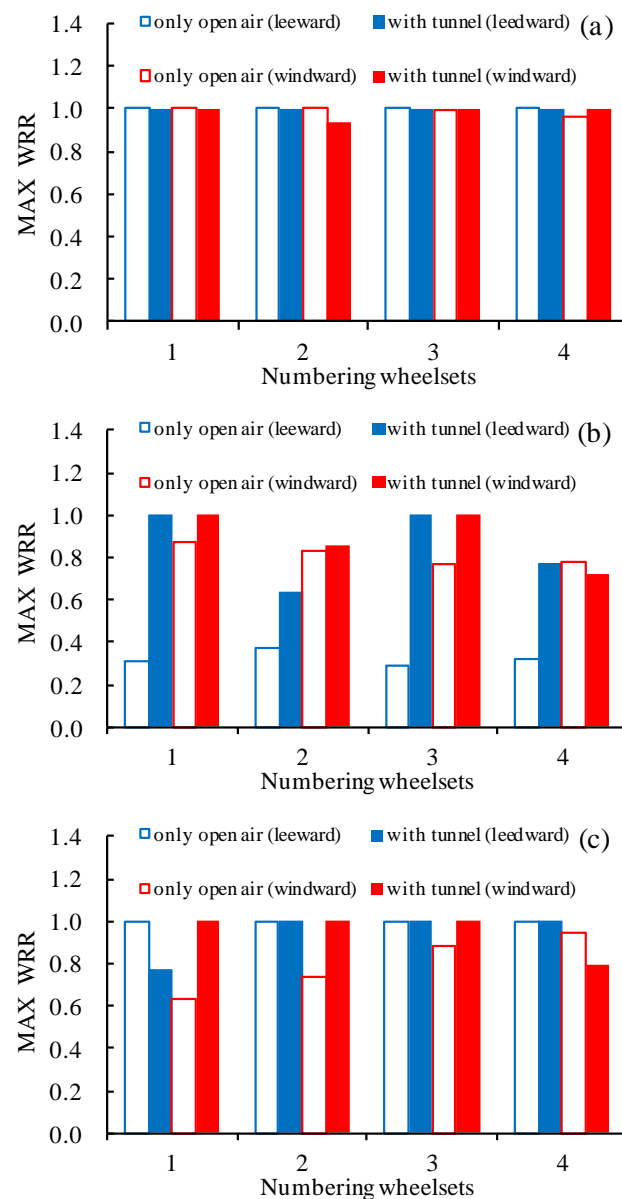
wheel has been detached from the rail. Finally, the WRRs in both sides rapidly decrease when the train entering the tunnel due to the buffering effect of the suspension system.



**Figure 20.** Time-history of head carriage WRR conditioned train speed 250 km/h, crosswind velocity 15m/s, (a) 1st wheelset, (b) 2nd wheelset, (c) 3rd wheelset, (d) 4th wheelset (“OA” for open air, “E” for entering entrance, “T” for tunnel).

Similar to DC, the variation amplitude of WRR of the first and third wheels in the windward side is larger than those of the other wheels and occurs instantaneously when the train entering

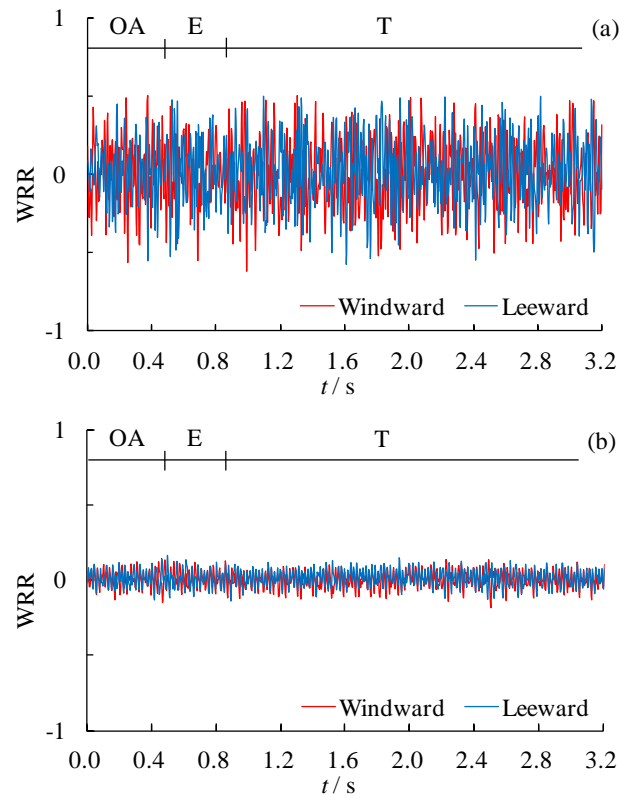
tunnel. Figure 21 presents the comparison of all wheel's maximum WRR values amongst the head, middle and rear carriages during the two processes (i.e. only in open air and entering tunnel) under conditions of train speed =250 km/h and crosswind velocity = 25 m/s. Safety risk is likely to be observed in the head carriage based on the discussion of the DCs and WRRs.



**Figure 21.** Contrast of global maximum wheel reduction rate conditioned train speed 250 km/h, crosswind velocity 25m/s: (a) head, (b) middle and (c) rear carriages.

To verify the effectiveness of the track irregularity spectrum used in present study, Figure 22 shows the time-history of the WRR in the first wheelset of head carriage during the train entering tunnel at speed of 250 km/h (no crosswind) under the track spectrum condition in this paper and the corresponding result under the condition of Chinese track spectrum [40], respectively. It is shown from Figure 22 that the WRRs of wheels on both sides fluctuate at the same level basically due to the absence of crosswind. The maximum WRR value in the Figures. 22(a) and (b) is 0.51 and 0.17, respectively. Both are significantly smaller than the corresponding result shown in Figure 20(a). Therefore, the track irregularity spectrum adopted in present study is effective and conservative.





**Figure 22.** Time-history of WRR in 1st wheelset of head carriage under conditions of different track irregularity spectrum, (a) present study, (b) Chinese code (“OA” for open air, “E” for entering entrance, “T” for tunnel, train speed= 250km/h, no crosswind).

### 5.2.3. Safety criteria

#### (1) DC grade

The safety grade of DC is proposed further in the code TB/T 2360-1993 [38] (see Table 2).

#### (2) WRR grade

$$\text{First limit: } \Delta P / \bar{P} \leq 0.65 \quad (17)$$

$$\text{Second limit: } \Delta P / \bar{P} \leq 0.60 \quad (18)$$

**Table 2.** Safety limits of DC.

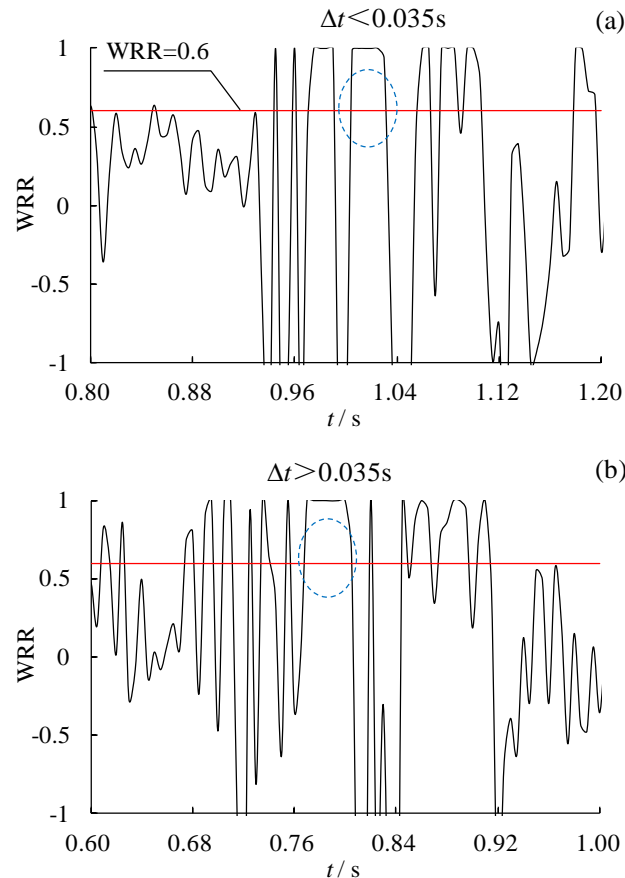
Safety grade	Superior	Good	Qualified
DC	$\leq 0.6$	$\leq 0.8$	$\leq 0.9$

Although WRR exceeds the second limit in some conditions, its safety limit value is strict because the running train has no safety issue since the opening of the Beijing–Shanghai HSR [32]. Therefore, Zhai et al. [41] proposed a new criterion of WRR, and many field tests that are widely adopted in the safety assessment of train traffic in Chinese HSR are based on the reported issue.

$$\begin{cases} \Delta P/\bar{P} \leq 0.60 \\ \Delta t < \Delta t_0, \Delta P/\bar{P} > 0.60 \end{cases} \quad (19)$$

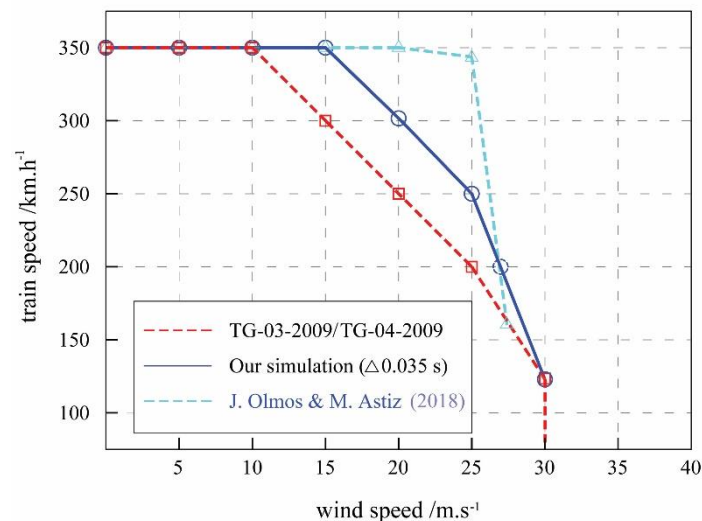
where  $t$  is the time interval when the WRR continues to exceed 0.6; and  $\Delta t$  is the maximum allowable time interval,  $\Delta t = 0.035$  s.

Figure 23 presents the partial magnification of the WRR at third wheel of windward side of head carriage when train travels at the speed of 250 km/h and 300 km/h and the crosswind velocity outside the tunnel is 25 m/s. In this study, safety is considered safe and unsafe when a train runs in the speed of 250 km/h and 300 km/h because  $\Delta t < 0.035$  s and  $\Delta t > 0.035$  s, respectively.



**Figure 23.** Partial magnification of the wheel reduction rate at 3rd wheel of windward side of head carriage: (a) train speed = 250 km/h and (b) train speed = 300 km/h.

Figure 24 presents the CWCs or the wind speed against the train speed for applications based on the safety criteria, where the wind speed is constant velocity. The allowable speed of Chinese regulations [42,43] when crosswind are involved and the results of other studies found in the scientific Literature [44] are presented for comparison. The present investigation shows that in terms of safety, an HST is allowed to enter a tunnel with crosswind at 350 km/h when the crosswind velocity is less than 15 m/s, which is looser than the national regulations but more conservative than that of Olmos et al. [44]. The literature results are deduced from the wind–train–viaduct interaction. The CWC comparison implies that the transient wind effect at the tunnel entrance might not be neglected.



**Figure 24.** Safety domain when high-speed train enters tunnel from crosswind.

## 6. Conclusions

This study presents a wind–train–track dynamic model to analyse the sudden variation of aerodynamic force and assess the operation safety of trains. Specific observations are summarised as follows.

- When a train enters tunnels with crosswind, the difference of flow field and pressure between inside and outside the tunnel causes sudden variation in the five aerodynamic load components with respect to time at the same instance. The five aerodynamic load components contribute to the safety risk of the running train.
- The global maximum of DCs and WRR of trains is likely to be achieved during tunnel entry with crosswind than in a crosswind environment due to the sudden disappearance of wind excitation when other conditions remain the same.
- The safety risk of the head carriage is higher than that of the rear carriage and even more than the middle carriage because of the transient aerodynamic effect on the head and rear carriages at the tunnel entrance. This finding is consistent with the actual situation of the rollover accident of a running train that occurred in Xinjiang, China in 2007.

The sudden variation of aerodynamic load is an important potential source of vehicle safety accidents, such as when a train enters a tunnel with crosswind, which is discussed in this study. The results show that the sudden wind excitation in the tunnel entrance and corresponding safety risks should not be neglected. However, proposing a practicable CWCs curve based on simulation and theoretical analysis is difficult. Therefore, further investigation, especially in the related field test, is needed in the future.

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