

## Article

# Wave and hydrodynamic processes in the vicinity of a rubble-mound, permeable, zero-freeboard breakwater

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**Abstract:** A numerical study for the effect of crest width, breaking parameter and trunk permeability on hydrodynamics and flow behavior in the vicinity of rubble-mound, permeable, zero-freeboard breakwaters (ZFBs) is presented. The modified two dimensional Navier-Stokes equations for two-phase flows in porous media with a Smagorinsky model for the subgrid scale stresses were solved numerically. An immersed-boundary/level-set method was used. The numerical model was validated for the cases of wave propagation over a submerged impermeable trapezoidal bar and over a low-crested permeable breakwater. Five cases of breakwaters were examined, and the main results are: (a) The size of the crest width,  $B$ , does not notably affect the wave reflection, vorticity and currents in the seaward region of ZFBs, while wave transmission, currents in the leeward side, and mean overtopping discharge, all decrease with increasing  $B$ . A non-monotonic behavior of the wave setup is also observed. (b) As the breaking parameter decreases, wave reflection, transmission, currents, mean overtopping discharge, and wave setup decrease. This observation is also verified by relevant empirical formulas. (c) As the ZFB trunk permeability decreases, an increase of the wave reflection, currents, wave setup, and a decrease of wave transmission and mean overtopping discharge is observed.

**Keywords:** rubble-mound; zero-freeboard; porous-media; immersed-boundary; level-set; Smagorinsky subgrid scale model; wave reflection; wave transmission; wave overtopping; wave setup

## 1. Introduction

The role of rubble-mound low-crested breakwaters (LCBs), whose main advantage is their mild aesthetic impact on the natural environment, in coastal protection is to partially dissipate incident waves. Consequently, in the seaward region of LCBs, the most important wave processes are breaking and reflection, while in their leeward region, the most important ones are overtopping, transmission, and setup. These wave processes induce also significant flow processes in the vicinity of LCBs. The influence of the geometrical characteristics of LCBs on wave and flow processes has been studied extensively for emerged or submerged LCBs. The case of zero-freeboard breakwaters (ZFBs), where the crest level of the structure is at the still water level (SWL), is the subject of the present study. In the following literature review, the focus is on experimental and numerical (only depth-resolving flow models) studies of rubble-mound, two-dimensional vertical (2-DV) LCBs.

In terms of wave reflection in the seaward region of permeable LCBs with rock armor, Zanuttigh and Van der Meer [1] analyzed several experimental datasets and derived an empirical formula for the prediction of the reflection coefficient  $K_r$ . Specifically for ZFBs, the formula in [1] becomes

$$K_r = C \tanh \left( A_{50}^{zb} \right), \quad (1)$$

where  $A = 0.167(1 - \exp(-3.2\gamma_f))$  and  $b = 1.49(\gamma_f - 0.38)^2 + 0.86$  are calibration parameters related to the roughness factor  $\gamma_f$ ,  $C < 1$  is a reduction parameter necessary for LCBs,  $\xi_0 = \tan a(gT^2/2\pi H_i)^{1/2}$  is the breaker parameter,  $\tan a$  is the seaward slope of the ZFB,  $T$  is the wave period of the incident waves, and  $H_i$  is the wave height of the incident waves at the seaward toe of the ZFB. In terms of wave transmission in the leeward region of LCBs, empirical formulas for the prediction of the transmission coefficient,

$$K_t = \frac{H_t}{H_i}, \quad (2)$$

where  $H_t$  is the wave height at the leeward toe of the LCB, were derived in [2-5]. Specifically for ZFBs with rock armor, the corresponding empirical formulas are:

$$K_t = \begin{cases} 0.51 - 0.11 \frac{B}{d_s}, & \text{(Seelig, 1980)} \\ 1 - \exp\left(-1.09 \frac{H_i}{B}\right), & \text{(Seabrook & Hall, 1998)} \\ \left. \begin{aligned} &0.64(1 - \exp(-0.50\xi_0)) \left(\frac{B}{H_i}\right)^{-0.31}, \text{ for } B/H_i \leq 8 \\ &\text{linear interpolation}, \text{ for } 8 < B/H_i < 12 \\ &0.51(1 - \exp(-0.41\xi_0)) \left(\frac{B}{H_i}\right)^{-0.65}, \text{ for } B/H_i \geq 12 \end{aligned} \right\} & \text{(van der Meer et al., 2005)} \\ \left( \min(0.74; 0.62\xi_0^{0.17}) - 0.25 \min\left(2.2; \frac{B}{\sqrt{H_i\lambda_0}}\right) \right)^2, & \text{(Buccino & Calabrese, 2007)} \end{cases} \quad (3)$$

where  $B$  is the crest width of the ZFB,  $d_s$  is the water depth at the seaward toe of the ZFB, and  $\lambda_0 = gT^2/2\pi$  is the deep-water wavelength. The empirical formulas in [2,3] were derived using experimental datasets of LCBs with impermeable core, while the empirical formulas in [4,5] used practically the same datasets as reported in [4]. In all cases of Eq. **Error! Reference source not found.**, it is noted the important effect of  $\xi_0$  and/or  $B$  on wave transmission.

In terms of the mean overtopping discharge over rubble-mound ZFBs, the following empirical formula is suggested in EurOtop [6]

$$q = \frac{0.09}{f_q} \sqrt{gH_i^3} \quad (4)$$

where  $f_q$  is an adjustment factor that accounts for scale effect corrections. In terms of the wave setup,  $\delta$ , at the leeward toe of rubble-mound, permeable LCBs, experimental data were presented in [7,8]. In both studies several cases of ZFBs were included, and the following empirical formulas were derived

$$\delta = \begin{cases} 0.6H_i \exp(-0.7^2), & \text{(Diskin et al., 1970)} \\ \frac{B}{8gD_{50}} \left(\frac{H_i\lambda_i}{d_s T}\right)^2, & \text{(Loveless et al., 1998)} \end{cases} \quad (5)$$

where  $D_{50}$  is the mean diameter of the rubble rocks, and  $\lambda_i$  is the wavelength at the seaward toe of the ZFB. Semi-analytical models for the prediction of  $\delta$  were also presented [9,10] but they refer to submerged barriers and they are not considered here where the focus is on ZFBs.

The influence of the geometrical characteristics of rubble-mound, permeable, submerged breakwaters on wave transmission was investigated numerically (potential flow theory in the fluid region and viscous flow in the permeable trunk of the breakwater) in [11]. It was concluded that increasing the crest width and/or decreasing the crest submergence depth results into the reduction of  $K_t$ , while increasing the permeability of the breakwater, i.e. increasing the porosity or the size of the rubble rocks, results into the increase of  $K_t$  and the reduction of  $K_r$ . The Navier-Stokes equations were solved numerically in [12] in order to simulate the interaction between a solitary wave and a permeable submerged bar. It was found that the increase of porosity from 0.4 to 0.52 results into the reduction of  $K_t$ , while if the porosity is further increased up to 0.7 the transmission coefficient increases, indicating that an optimum porosity value seems to exist.

Near-field flow processes that occur due to the interaction between regular waves and rubble-mound, permeable LCBs were studied experimentally and numerically in [13]. The numerical model was based on the "Cornell Breaking Waves and Structures" (COBRAS) software [14]. In both the experiments and the simulations, a recirculation system was devised to return flow to the seaward region of the LCB in order to balance the non-realistic pilling of water in the leeward region of the LCB; this system was found to be crucial in the modeling of 2-DV LCBs. Specifically for the ZFB case in [13], it was  $\tan\alpha = 1/2$ ,  $d_s = 25$  cm,  $B = 100$  cm, while the median diameter,  $D_{50}$ , of the rocks was 4.80 cm in the armor layer and 1.47 cm in the core. Several regular wave cases were examined, which for the ZFB case corresponded to the ranges  $0.20 \leq H_i/d_s \leq 0.78$  and  $9.38 \leq \lambda_i/d_s \leq 19.63$ . It was observed that breaking waves collapsed on the seaward edge of the ZFB crest inducing a strong vortex cell in this zone, a strong mean shoreward current developed over the ZFB crest, a primary vortex cell was formed in the leeward region of the ZFB, a weak mean seaward current developed in the ZFB trunk, and a secondary vortex cell was formed near the seaward toe of the ZFB.

Losada et al. [15] focused on the submerged breakwater cases in [13] with crest height  $h_c = 25$  cm,  $d_s = 30$  cm resulting into crest elevation  $R_c = -5$  cm, and  $R_c/H_i = -0.52$ . They performed numerical simulations using the COBRAS model and found that the resulting  $K_r$  does not depend on  $B$ , while the shear stress field attains its maximum values along the armor layer of the crest. Losada et al. [15] also studied numerically a submerged breakwater case at prototype scale with  $\tan\alpha = 2/3$ ,  $d_s = 5$  m,  $B = 5$  m,  $R_c = -0.5$  m. The trunk of the breakwater was homogeneous with  $D_{50} = 1.44$  m, while the incident wave parameters at the seaward toe of the breakwater were  $H_i = 0.97$  m ( $R_c/H_i = -0.52$ ) and  $T = 6$  sec. It was found that the velocity of the flow over the crest were about one order of magnitude larger than the one in the permeable trunk of the breakwater.

Lara et al. [16] exploited the capability of COBRAS to study irregular wave interaction with the submerged permeable breakwater case in [13], and they presented regular wave interaction with an LCB of permeable armor layer and less permeable core. The latter case corresponded to the LCB studied experimentally at the Maritime Engineering Laboratory of the Polytechnic University of Catalunya (Spain) as described in [17]. This LCB had  $\tan\alpha = 1/2$ ,  $h_c = 1.59$  m,  $B = 1.825$  m, while the median diameter,  $D_{50}$ , of the rocks was 10.82 cm in the armor layer and  $3 \pm 1$  cm in the core. No FZB case was considered; the only submerged case had  $R_c = -0.13$  m,  $H_i = 0.286$  cm ( $R_c/H_i = -0.45$ ) and  $T = 2.18$  sec. The transmitted wave height in the leeward region of the LCBs was, in general, under-predicted by the numerical simulations in comparison to the experimental data; this discrepancy was attributed to several factors including the inaccurate replication of the experimental LCB geometry in the numerical model.

In this paper, the interaction of regular waves with rubble-mound, permeable ZFBs was studied numerically using a two-phase flow model in the air-water region and a porous flow model in the trunk of the ZFBs. The objective was to reveal the effect of crest width and trunk permeability on the main wave (reflection, transmission and leeward setup) and flow (vortex generation, mean currents and overtopping discharge) processes for ZFBs.

## 2. Materials and Methods

### 3.1. Formulation and Numerical Implementation

The two-phase (water and air) 2-DV flow induced by regular waves in the vicinity of rubble-mound, permeable ZFBs was modeled as one-fluid flow as described in [18]. This formulation was further modified to seamlessly connect the external wave-induced flow to the porous medium flow in the permeable ZFB trunk by using the model in [19]. For the external flow, the formulation in [18] is similar to the approach in large-eddy simulation (LES) where the subgrid flow scales resulting by wave breaking are not resolved but their effect on the resolved flow scales is modeled. The resulting non-dimensional governing equations are:

$$\frac{\partial u_i}{\partial x_i} = 0 \quad (6)$$

$$\begin{aligned} \frac{1+c_A}{n} \frac{\partial u_i}{\partial t} + \frac{u_i}{n^2} \frac{\partial u_j}{\partial x_j} = & -\frac{1}{\rho} \frac{\partial P}{\partial x_i} + \frac{\delta_{ij}}{\text{Fr}^2} + \frac{1}{\text{Re}} \frac{1}{n} \frac{1}{\rho} \frac{\partial}{\partial x_j} \left( \mu \frac{\partial u_i}{\partial x_j} \right) - \frac{\partial \tau_{ij}}{\partial x_j} - \\ & a_p \frac{(1-n^2)}{n^3} \frac{\nu}{D_{50}^2} \frac{1}{\text{Re}} u_i - \beta_p \left( 1 + \frac{7.5}{\text{KC}} \right) \frac{1-n}{n^3} \frac{1}{D_{50}} u_i \sqrt{u_i u_i} + f_i \end{aligned} \quad (7)$$

where  $x_1 = x$  and  $x_2 = z$  are the streamwise and vertical coordinates, respectively,  $t$  is the time,  $u_i$  is the velocity field,  $P$  is the total pressure,  $\rho$  is the normalized fluid density,  $\mu$  is the normalized fluid dynamic viscosity,  $\text{Fr}$  is the Froude number,  $\delta_{ij}$  is the Kronecker's delta,  $\text{Re}$  is the Reynolds number,  $\tau_{ij}$  are the modeled subgrid-scale (SGS) stresses,  $c_A$  is the added mass coefficient in the form [20]

$$c_A = 0.34 \frac{1-n}{n} \quad (8)$$

$n$  is the effective porosity ( $n = 1$  in the external flow and  $n < 1$  in the ZFB trunk),  $D_{50}$  is the median diameter of the rocks forming the ZFB trunk,  $a_p$  and  $\beta_p$  are calibration constants,  $\text{KC}$  is the Keulegan-Carpenter number representing the ratio of the characteristic length scale of fluid particle motion to that of the porous media [21]

$$\text{KC} = \frac{T \sqrt{u_i u_i}}{n D_{50}} \quad (9)$$

$T$  is the characteristic wave period, and  $f_i$  is a term associated with the implementation of boundary conditions on solid surfaces using the Immersed Boundary (IB) method. The velocity components in Eqs **Error! Reference source not found.** and **Error! Reference source not found.** are the resolved ones for the external flow, based on the LES approach in [18], and the spatially-averaged ones for the porous flow in the ZFB trunk, based on the model in [19].

The SGS stresses in Eq. **Error! Reference source not found.** were modeled using the eddy-viscosity model in [22]

$$\tau_{ij} - \frac{\delta_{ij}}{2} \tau_{kk} = -2\nu_{\text{sgs}} S_{ij} = -2(C_s \Delta)^2 |S| S_{ij} \quad (10)$$

where  $C_s = 0.1$  is the model parameter,  $\Delta$  is the filter length scale of the grid, and  $|S| = (2S_{ij}S_{ij})^{1/2}$  is the magnitude of the resolved-scale, strain-rate tensor

$$S_{ij} = \frac{1}{2} \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right), \quad (11)$$

The evolution of the free surface was tracked using the signed distance function,  $\varphi$ , where  $\varphi > 0$  in the water,  $\varphi < 0$  in the air, and  $\varphi = 0$  at the water-air interface. The computation of  $\varphi$  (evolution and re-initialization) was based on the level-set method described in [18]. The normalized density, modeled with a sharp jump across the water-air interface, and the normalized viscosity, modeled with a smooth variation across the water-air interface, were defined, respectively, as

$$\rho = \frac{\rho_a + (\rho_w - \rho_a) H(\varphi)}{\rho_w}, \quad (12)$$

and

$$\mu = \frac{\mu_a + (\mu_w - \mu_a) H_\varepsilon(\varphi)}{\mu_w}, \quad (13)$$

where index 'w' corresponds to the water phase, index 'a' corresponds to the air phase,

$$H(\phi) = \begin{cases} 1, & \phi \geq 0 \\ 0, & \phi < 0 \end{cases}, \quad (14)$$

is a stepwise Heaviside function,

$$H_\varepsilon(\phi) = \begin{cases} 1, & \phi > \varepsilon \\ \frac{1}{2} \left[ 1 + \frac{\phi}{\varepsilon} + \frac{1}{\pi} \sin\left(\frac{\pi\phi}{\varepsilon}\right) \right], & |\phi| \leq \varepsilon \\ 0, & \phi < -\varepsilon \end{cases}, \quad (15)$$

is a smoothed Heaviside function, and  $\varepsilon$  is a parameter with length dimensions of order comparable to the grid cell [23]. Note that  $\rho = 1$  and  $\mu = 1$  in the water, and  $\rho = 1.2 \times 10^{-3}$  and  $\mu = 1.8 \times 10^{-2}$  in the air.

The spatial discretization of the governing equations was based on the use of finite differences on a Cartesian staggered grid where velocity components are defined at the cell edges, while  $p$  and  $\varphi$  are defined at the cell center. Therefore, the breakwater geometry, the sea bed, and the free surface do not follow grid lines but they are "immersed" in the numerical grid. For the sea bed, in particular, the implementation of the appropriate non-slip boundary conditions was based on the Immersed Boundary (IB) method in [24]. Details about the implementation are given in [18]. The main advantage of this method is the computational efficiency, since the appropriate boundary conditions on solid surfaces are imposed by only modifying the additional term  $f_i$  in Eq. **Error! Reference source not found..** This term is zero on all grid points except the so called "forcing points", which are the ones in the fluid phase that have at least one neighboring grid point in the solid phase. The value of  $f_i$  on the forcing points is computed so that it enforces the non-slip boundary condition on the sea bed.

A fractional-step method was used for the velocity-pressure coupling. First, an intermediate velocity field was computed explicitly, using an Adams-Bashforth scheme, without taking into account the pressure term of Eq. **Error! Reference source not found.**

$$\frac{u_i^* - u_i^n}{\Delta t} = \frac{3}{2} H(u_i^n, u_j^n) - \frac{1}{2} H(u_i^{n-1}, u_j^{n-1}) + f_i, \quad (16)$$

where  $H$  is a spatial operator, which includes the convective, gravity, viscous, SGS, and porous terms. The final velocity field was computed using the pressure gradient

$$u_i^{n+1} = u_i^* - \frac{\Delta t}{\rho} \frac{\partial P^{n+1}}{\partial x_i}, \quad (17)$$

which was obtained by solving the Poisson equation for the total pressure

$$\frac{\partial}{\partial x_i} \left( \frac{1}{\rho} \frac{\partial P^{n+1}}{\partial x_i} \right) = - \frac{1}{\Delta t} \frac{du_i^*}{dx_i}, \quad (18)$$

which was derived by enforcing the continuity constraint on the final velocity field. The spatial discretization of the left hand side of Eq. **Error! Reference source not found.** results into a pentadiagonal matrix, the elements of which are reconstructed at each time step due to the evolution of the free surface. The inversion of the matrix was achieved by a shared-memory multiprocessing parallel direct solver using the Intel MKL PARDISO® 11.0 library.

### 3.2. Wave Generation

In all cases examined in this paper, regular waves were generated by a piston-type wavemaker at the left boundary of the computational domain (Figs 1, 3, and 5). Using second-order theory, the imposed horizontal velocity was [25]

$$u = \frac{1}{2} S \omega \cos(\omega t - \pi/2) + \frac{1}{16} \frac{H^2}{d} \omega \left( \frac{3 \cosh(kd)}{\sinh^3(kd)} - \frac{2S}{H} \right) \cos(2\omega t - \pi), \quad (19)$$

where

$$S = H \frac{\sinh(2kd) + 2kd}{4 \sinh^2(kd)}, \quad (20)$$

is the stroke of the wavemaker,  $H$  is the height of the generated waves,  $k = 2\pi/\lambda$  is their wavenumber,  $\lambda$  is their wavelength,  $\omega = 2\pi/T$  is their radial frequency,  $T$  is their period, and  $d$  is the water depth at the wavemaker. The imposed horizontal velocity was continuously corrected to achieve zero mean mass flux. In 2D flow experiments over low-crested structures, the non-realistic wave setup in the leeward region of the structures, caused by water pilling-up due to overtopping, affects significantly the dynamics of the flow in the vicinity of the breakwaters. On the other hand, in real cases and 3D problems this water is allowed to return back offshore by the ends of the structures. In many experimental projects, recirculation systems are applied in the leeward region of the breakwaters for the prevention of this phenomenon [13]. The numerical correction of the imposed horizontal velocity applied here functions as a flow recirculation system.

The inflow region just downstream of the wavemaker had a horizontal bottom of constant water depth with length equal to about three wavelengths, in order for the generated waves to be fully developed when they reach the breakwater (Figs 1, 3, and 5). A relaxation zone of length equal to one wavelength (length decided after trial and error) was implemented just downstream of the wavemaker in order to avoid undesired wave reflections from the left boundary of the computational domain. Inside the relaxation zone, according to [26], a relaxation function was applied

$$q = a_R q_{\text{computed}} + (1 - a_R) q_{\text{target}}, \quad (21)$$

where  $q$  is either a velocity component or the level-set function,

$$a_R(l_R) = 1 - \frac{\exp(l_R^{3.5}) - 1}{\exp(1) - 1}, \quad (22)$$

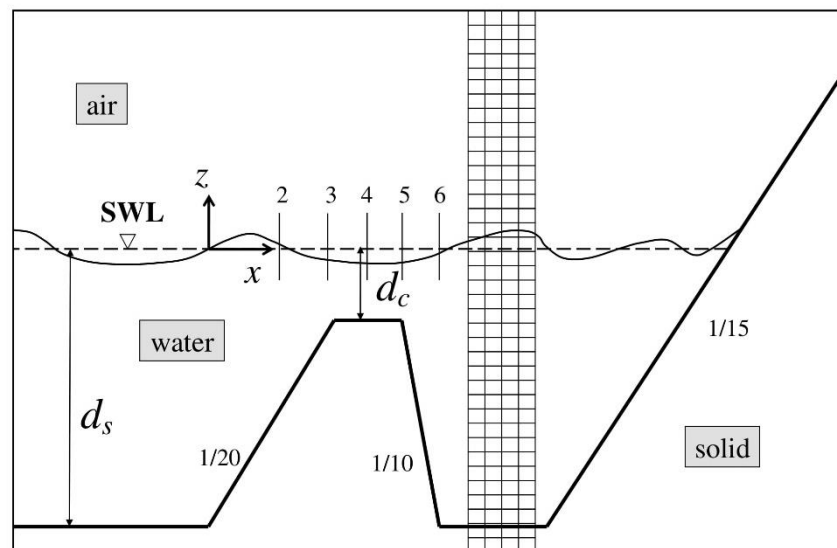


is the absorption rate, and  $l_R \in [0:1]$  is defined so that  $a_R = 0$  at the left boundary of the computational domain ( $l_R = 1$ ) and  $a_R = 1$  at the end of the relaxation zone ( $l_R = 0$ ).

### 3.3. Validation

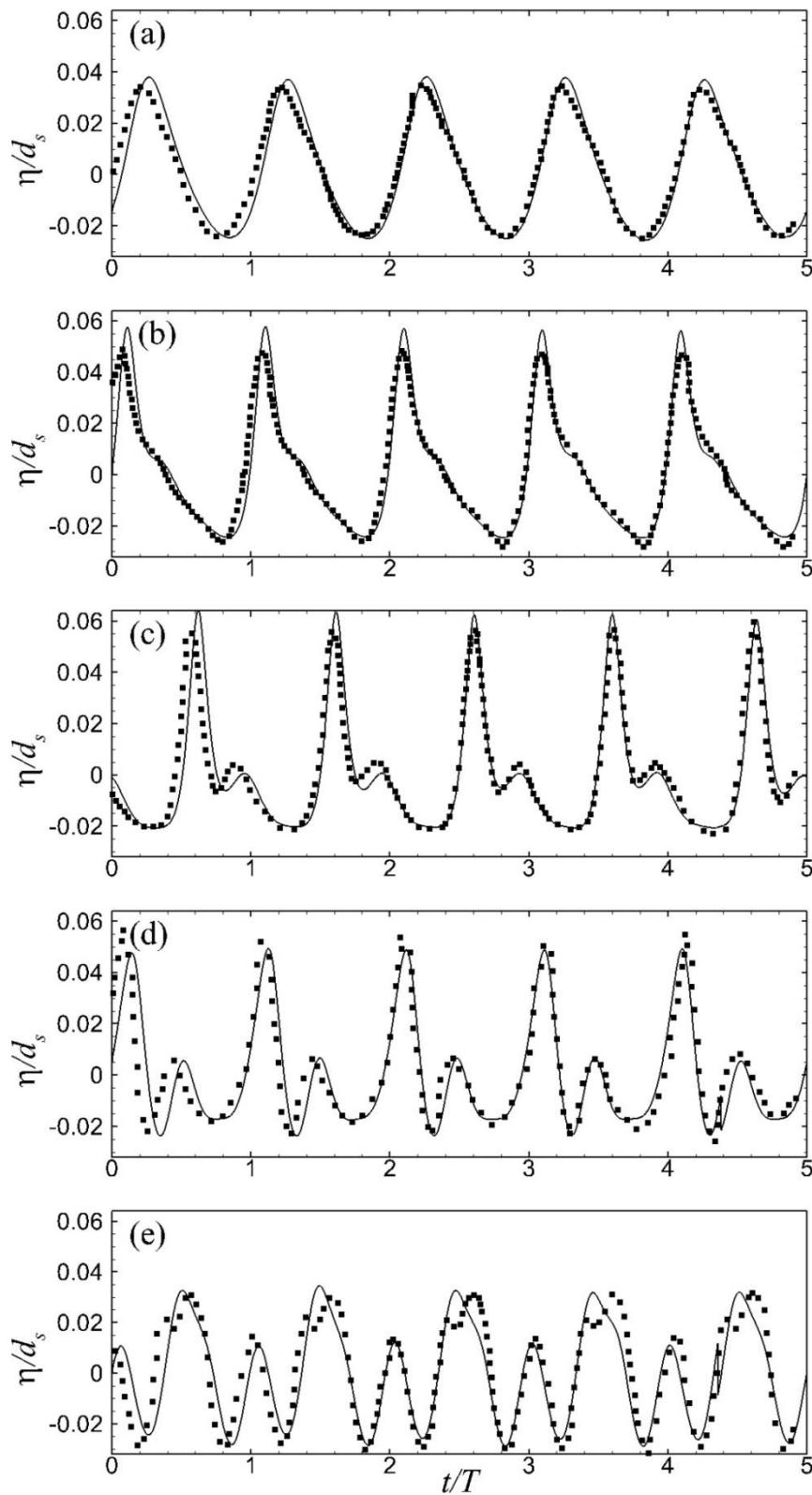
The numerical model was validated by comparison to the cases of wave propagation over a submerged impermeable trapezoidal bar and over a low-crested permeable breakwater.

The first validation case (Fig. 1) corresponds to the experiments in [27]. In these experiments, waves of height  $H = 0.02$  m and period  $T = 2$  s were generated over a region of constant water depth  $d_s = 0.4$  m before reaching the bar. The crest depth was equal to  $d_c = 0.1$  m. Using  $d_s$  as the characteristic length and  $(g/d_s)^{1/2}$  as the characteristic velocity scale, the Reynolds number was  $Re_d = 800,000$ . For the simulations (Fig. 1), in order to achieve both adequate resolution in the wall boundary layer and a reasonable computational cost the experiment was reproduced with  $d_s = 0.15$  m using Froude scaling, leading to a Reynolds number  $Re_d = 160,000$ , i.e. 5 times smaller than the one in the experiments. The computational grid had a uniform size of  $\Delta x/d_s = 0.02$  along  $x$  (460 grid points per wavelength of the incident wave), and a non-uniform size in  $z$ ;  $\Delta z/d_s = 0.005$  in the water and increasing to  $\Delta z/d_s = 0.01$  in the air. The corresponding values in the water with respect to the Stokes length,  $\delta$ , were  $\Delta x/\delta = 4.5$  and  $\Delta z/\delta = 1.13$ , which were sufficient to get a good resolution with at least 5 grid points in the wave boundary layer over the bed. The CFL (Courant-Friedrichs-Lewy) and VSL (Viscous Stability Limit) criteria were equal to  $2 \times 10^{-2}$  and  $7 \times 10^{-4}$ , respectively. In order for the flow field not to be affected by the height of the air layer in the computational domain, this was selected to be  $1.5d_s$  above the SWL (after trial and error). The trapezoidal bar was impermeable, therefore, the no-slip condition on its surface was imposed using the IB method.



**Figure 1.** Sketch of the computational domain and part of the Cartesian grid, as well as definitions of parameters for the numerical simulation of wave propagation over a submerged impermeable trapezoidal bar [27]. Note that the axes are not in scale. The distance from the wavemaker to the seaward toe of the bar is  $27d_s$ , while the distance from the leeward toe of the bar to the toe of the absorbing beach is  $5d_s$ .

Simulations were performed for 25 wave periods. Comparisons of the free-surface elevation between the numerical results and the experimental data in [27] at 5 locations (Fig.1) over the bar during the last 5 wave periods are presented in Fig. 2. A good agreement is demonstrated.

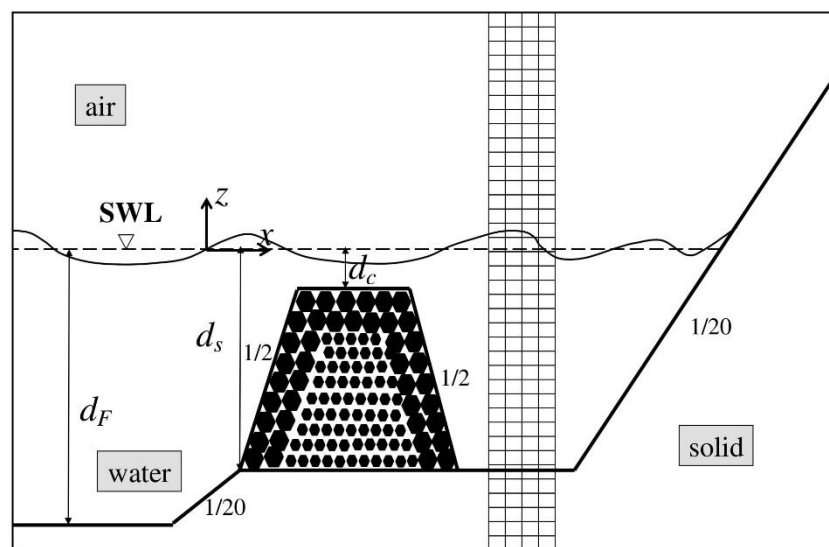


**Figure 2.** Variation of the free-surface elevation during 5 wave periods, after 20 wave periods of simulation, at five locations over a submerged permeable trapezoidal bar. These five locations correspond, respectively, to the stations 2, 3, 4, 5, and 6 of Fig. 1. The lines correspond to the present numerical results while the symbols to the experiments in [27].

The second validation case (Fig. 3) corresponds to wave transmission over the wide-crested submerged permeable breakwater in [13]. In these experiments, waves of height  $H = 0.07$  m and period  $T = 1.6$  sec were generated over a region of constant water depth  $d_F = 0.4$  m, which is followed

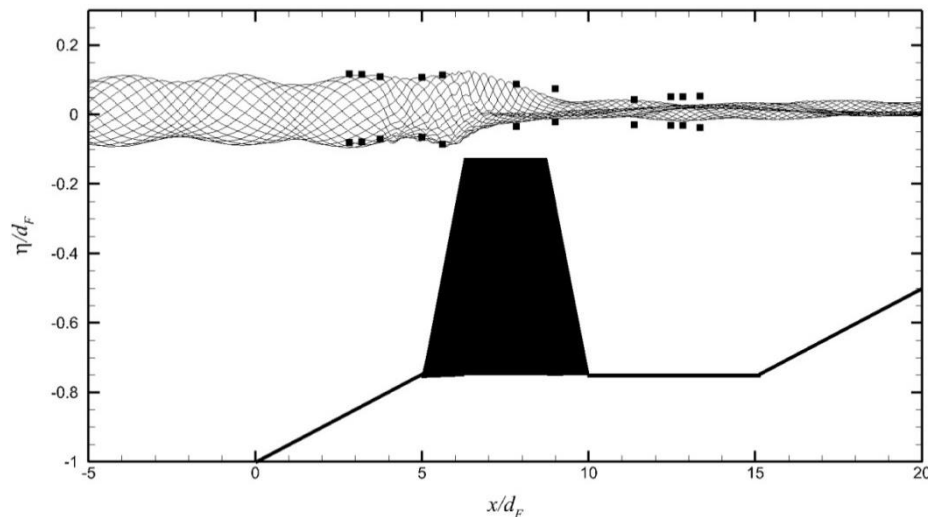


by a beach of slope  $\tan\beta = 1/20$  seawards of the breakwater. The depth at the breakwater toe was  $d_s = 0.3$  m, while the crest depth was  $d_c = 0.05$  m. As mentioned in the Introduction for these experiments, the trunk of the rubble-mound breakwater was permeable with a two-layer armor ( $D_{50} = 4.8$  cm and  $n = 0.53$ ) and a core with smaller rocks ( $D_{50} = 1.47$  cm and  $n = 0.49$ ). For the simulations (Fig. 3), in order to achieve both adequate resolution in the wall boundary layer and a reasonable computational cost the experiment was reproduced with  $d_s = 0.12$  m using Froude scaling, leading to a Reynolds number  $Re_d = 130,000$ , i.e. 6 times smaller than the one in the experiments. The computational grid had a uniform size of  $\Delta x/d_F = 0.02$  along  $x$  (355 grid points per wavelength of the incident wave), and a non-uniform size in  $z$ ;  $\Delta z/d_F = 0.005$  in the water and increasing to  $\Delta z/d_F = 0.01$  in the air. The corresponding values in the water with respect to the Stokes length,  $\delta$ , were  $\Delta x/\delta = 4.2$  and  $\Delta z/\delta = 1.06$ , which were sufficient to get a good resolution with at least 5 grid points in the wave boundary layer over the bed. The CFL and VSL criteria were equal to  $2 \times 10^{-2}$  and  $7 \times 10^{-4}$ , respectively. In order for the flow field not to be affected by the height of the air layer in the computational domain, this was selected to be  $1.5d_s$  above the SWL (after trial and error). The calibration values  $\alpha_p = 1000$  and  $\beta_p = 1.1$ , according to [19,20] were used in Eq. **Error! Reference source not found.**; the values  $\beta_p = 0.8$  in the armor layer and  $\beta_p = 1.2$  in the core were also used, according to [13], but with negligible differences in the results.



**Figure 3.** Sketch of the computational domain and part of the Cartesian grid, as well as definitions of parameters for the numerical simulation of wave propagation over a submerged permeable breakwater [13]. Note that the axes are not in scale. The distance from the wavemaker to the toe of the  $1/20$  slope is  $19.3d_F$ , while the distance from the leeward toe of the breakwater to the toe of the absorbing beach is  $4.5d_F$ .

Snapshots of the free surface elevation during 2 wave periods, after 20 wave periods of simulation, are shown in Fig. 4, and in comparison to the experimental data of crest and trough elevations in [13]. The horizontal coordinate and the free surface elevation are shown dimensionless based on  $d_F$ . The numerical model captures adequately the main characteristics of wave propagation over the submerged breakwater. More specifically, in the seaward region of the structure, the generation of a partially standing wave due to wave reflection is captured precisely by the model. In the vicinity of the crest and near the leeward region of the structure, the model captures adequately the wave dissipation due to wave breaking over the crest and due to filtration through the permeable trunk, while the wave height is under-predicted in the far leeward region. This last behavior is similar to the one observed in [16].



**Figure 4.** Envelope of the free-surface elevation of waves passing over a submerged permeable breakwater. The lines correspond to the present numerical results while the symbols to the experiments in [13].

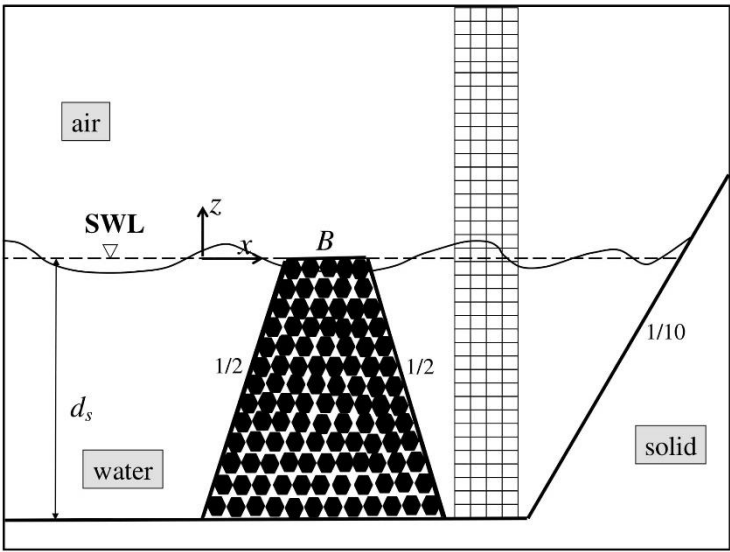
### 3. Results

This All ZFBs in the present study were rubble mound and permeable with  $\tan\alpha = 1/2$  for both seaward and leeward slopes. A sketch of the computational domain is shown in Fig. 5. First, three different setups were considered in order to examine the effect of crest width (cases 1-3 in Table 1) on the hydrodynamic processes of wave reflection, overtopping, transmission, and setup, as well as the flow behavior in the seaward and leeward regions of these structures. In cases 1-3, the ZFBs were fully-permeable (homogeneous trunk permeability), while the crest width,  $B$ , was set equal to  $d_s$ ,  $2d_s$  and  $3d_s$ , respectively, where  $d_s$  is the constant water depth between the wavemaker and the seaward ZFB toe. Then, the effect of the incident wave period (cases 1 and 4 in Table 1) and the ZFB trunk permeability (cases 1 and 5 in Table 1) were also investigated for the ZFB case with  $B = d_s$ .

In dimensional terms,  $d_s$  was selected to be equal to 0.4m, which corresponds to a Reynolds number  $Re_d = 800,000$ . The geometrical details and the incident wave parameters for all cases are summarized in Table 1. For all cases, the two-dimensional grid had a uniform size of  $\Delta x/d_s = 0.02$  along  $x$  (300-450 grid points per wavelength of the incident waves), and a non-uniform size in  $z$ ;  $\Delta z/d_s = 0.0025$  in the water and increasing to  $\Delta z/d_s = 0.01$  in the air. The corresponding values in the water with respect to the Stokes length,  $\delta$ , were  $\Delta x/\delta = 10.1$ -12.1 and  $\Delta z/\delta = 1.27$ -1.51 according to the wave length, which were sufficient to get a good resolution with at least 4 grid points in the wave boundary layer over the bed. The small flow scales occurring during breaking at the ZFB seaward slope are modeled by the SGS eddy-viscosity model. In all simulations, the CFL and VSL criteria were equal to  $2.0 \times 10^{-2}$  and  $5 \times 10^{-4}$ , respectively. In order for the flow field not to be affected by the height of the air layer in the computational domain, this was selected to be  $1.5d_s$  above the SWL (after trial and error). The calibration values  $\alpha_p = 1000$  and  $\beta_p = 1.1$ , according to [19,20], were used in Eq. **Error! Reference source not found.**

Typical crest and trough elevation envelopes during 10 wave periods, after 20 wave periods of simulation, are shown in Fig. 6 for case 1. From such envelope results, the breaking depth on the seaward ZFB slope and the corresponding wave height were identified at the location of the maximum wave crest elevation. In all cases, wave breaking occurred on the seaward slope and near the crest of the ZFBs; these results are summarized in Table 1. In cases 1-3, which correspond to the same incident wave and different crest width, the waveform in the seaward region of the ZFBs is similar, and a partially standing wave is generated due to reflection. On the other hand, in the leeward region of the ZFBs, the waveform is totally different between cases 1-3, as the wave height, i.e. wave energy, decreases with the increase of the crest width. In case 4, decreased wave height is observed in the seaward region, while less wave energy is transmitted to the leeward region in

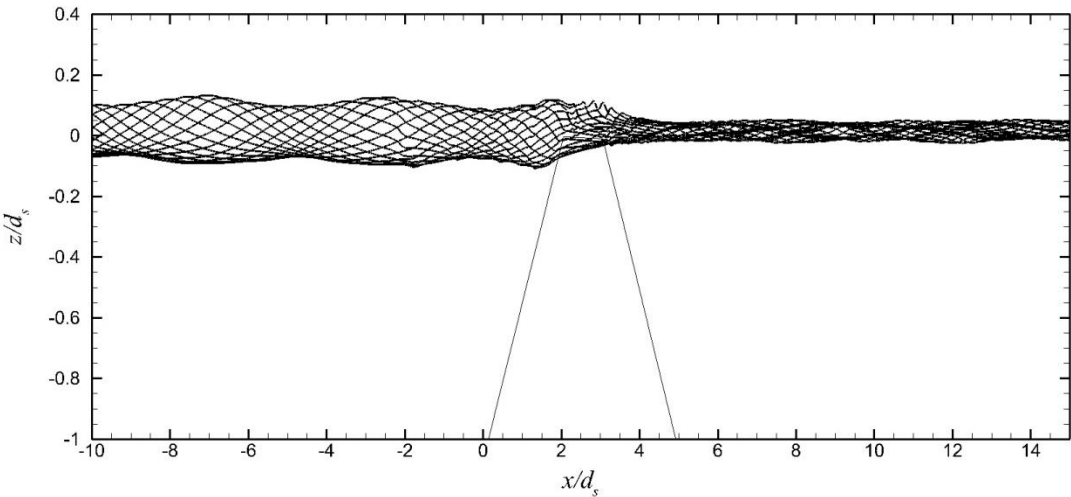
comparison to case 1, which has the same crest width but larger incident wave period, i.e. longer incident wavelength. In case 5 where the ZFB has a less permeable core, slightly increased wave height is observed in the seaward region and slightly less wave energy is transmitted to the leeward region in comparison to case 1, which has the same crest width but larger ZFB trunk permeability.



**Figure 5.** Sketch of the computational domain and part of the Cartesian grid for the permeable ZFB cases. Note that the axes are not in scale. The distance from the wavemaker to the seaward ZFB toe is  $23d_s$ , while the distance from the leeward ZFB toe to the toe of the absorbing beach is  $9d_s$ .

**Table 1.** Geometrical characteristics of the examined ZFB cases, the parameters of the incoming waves and the breaking ones on the seaward slope of the ZFB.

Case	Geometry				Incoming waves			Breaking waves on seaward ZFB slope	
	$\tan\alpha$	$B/d_s$	Armor $D_{50}/d_s$	Core $D_{50}/d_s$	$H_i/d_s$	$T(g/d_s)^{1/2}$	$\lambda/d_s$	$d_b/d_s$	$H_b/d_s$
1	1/2	1	0.31	0.31	0.2	9.8	9	0.178	0.205
2		2	0.31	0.31				0.175	0.201
3		3	0.31	0.31				0.180	0.202
4		1	0.31	0.31		6.9	6	0.179	0.197
5		1	0.31	0.031		9.8	9	0.171	0.217



**Figure 6.** The envelope of the free surface elevation of waves breaking over the ZFB case 1.

In Table 2, transmission and reflection coefficients for all ZFB cases are presented. For the reflection coefficient, surface elevation time series at three locations in the seaward region of the ZFBs were obtained, and a reflection analysis was performed using the method in Mansard and Funke (1980). For the transmission coefficient, surface elevation time series, recorded at the seaward and leeward toe of the ZFBs, were used to calculate the wave height at each position through spectral analysis. It is observed that wave transmission is decreasing, while wave reflection does not vary, with the increase of the crest width (cases 1-3) when incident wave height, incident wave period, and trunk permeability do not change. The decrease of wave transmission is attributed to the increase of wave dissipation over the ZFB crest as  $B$  increases. Decreasing the incident wave period (cases 1 and 4) results into the decrease of wave reflection and the decrease of wave transmission when crest width and trunk permeability do not change. These decreases are associated to the decrease of  $\xi_0$ . Finally, reducing trunk permeability (cases 1 and 5) also results into the increase of wave reflection and the decrease of wave transmission when crest width and incident waves do not change. Wave energy transmission is affected by both the overtopping over the ZFB crest and the porous flow in the ZFB trunk. In case 5, the less permeable ZFB trunk inhibits the transmission of kinetic energy through the trunk from the seaward to the leeward region of the ZFB in comparison to case 1, thus, the resulting reflection coefficient,  $K_r$ , is larger and the transmission coefficient,  $K_t$ , is smaller.

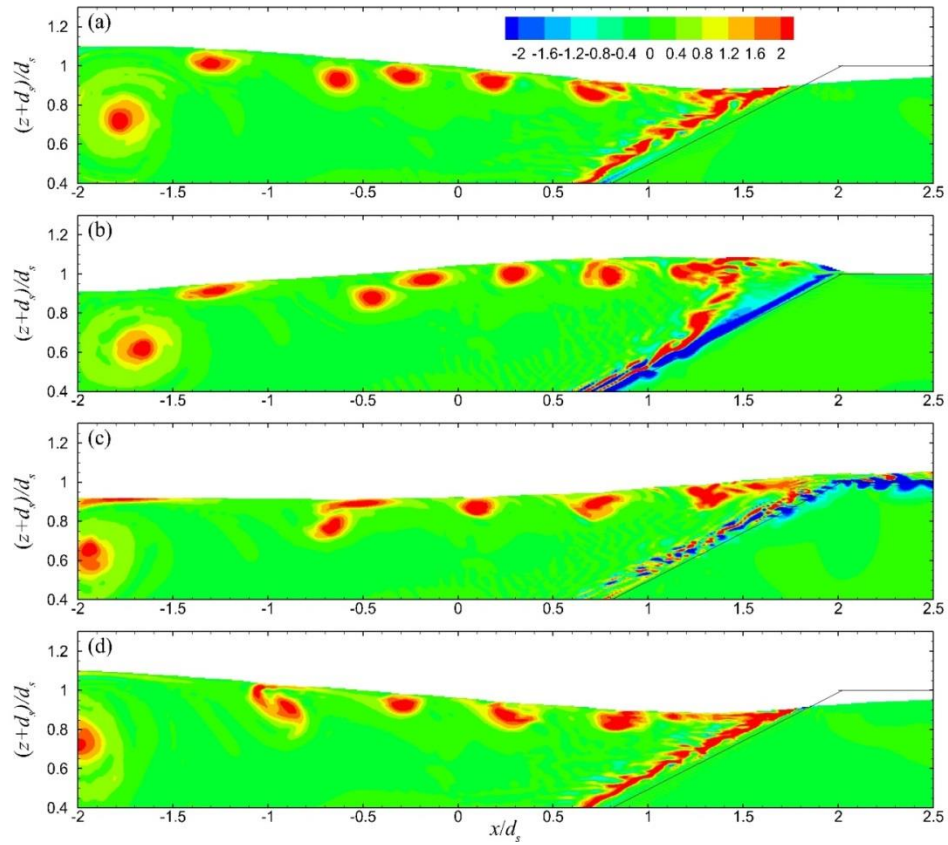
Apart from the computed reflection and transmission coefficients, the corresponding values predicted by widely used empirical formulas are also presented in Table 2. For wave reflection, the empirical formula of Eq. **Error! Reference source not found.** was used with  $\gamma_f = 0.40$ , for the fully-permeable ZFB cases 1-4, and  $\gamma_f = 0.5$ , for the partially-permeable ZFB case 5, according to [1]. To achieve the best possible agreement to the computed results, the reduction parameter was set to  $C = 0.43$  instead of the value  $C = 0.67$  suggested in [1] for ZFBs. For wave transmission, the empirical formulas of Eq. **Error! Reference source not found.** were used. The overall better prediction seems to be achieved by the empirical formula in [5].

**Table 2.** Reflection and transmission coefficients for all the ZFB cases of Table 1.

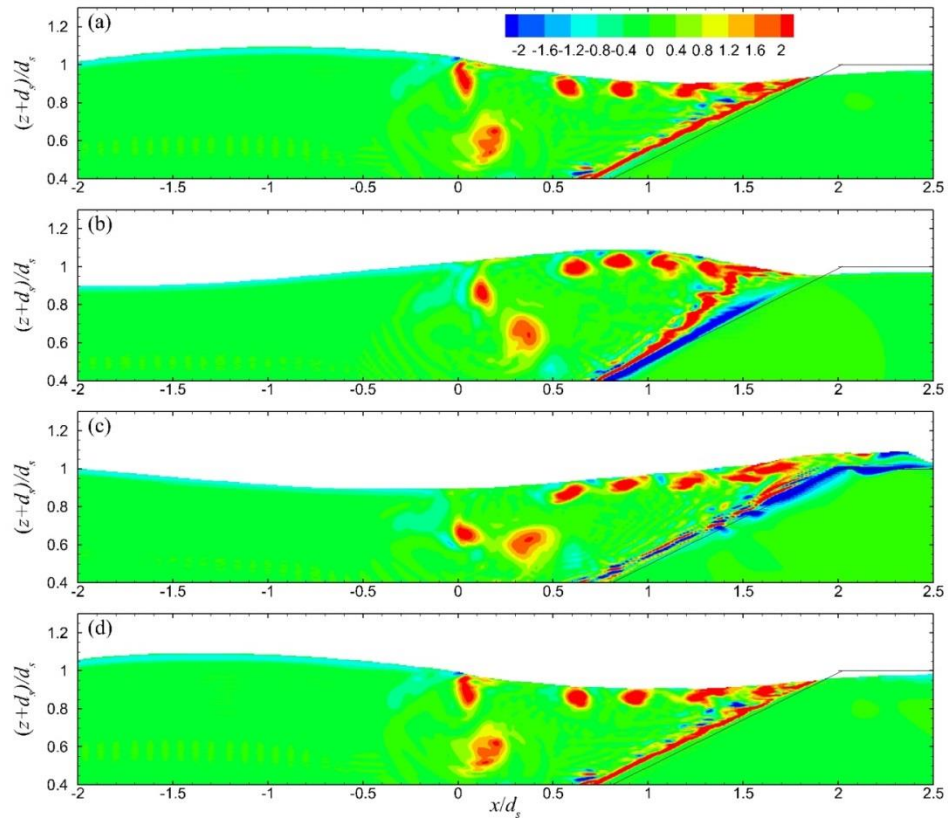
Case	$\xi_0$	$K_r$		$K_t$				
		Present	Zanuttigh and Van der Meer (2008)	Present	Seeling (1980)	Seabrook and Hall (1998)	Van der Meer et. al (2005)	Buccino and Calabrese (2007)
1	4.37	0.176	0.174	0.416	0.40	0.196	0.345	0.356
2	4.37	0.171	0.174	0.238	0.29	0.103	0.187	0.206
3	4.37	0.171	0.174	0.127	0.18	0.070	0.073	0.097
4	3.08	0.106	0.132	0.171	0.40	0.196	0.305	0.288
5	4.37	0.207	0.195	0.290	0.40	0.196	0.345	0.356

The distribution of the instantaneous vorticity field in the vicinity of the ZFB case 1, at four instances during the 30<sup>th</sup> wave period of the simulation, is presented in Fig. 7. It is shown that as the wave trough reaches the breakwater crest (down-rush flow phase), strong anti-clockwise vorticity develops near above the seaward slope of the structure. As the wave propagates and the flow reverses (up-rush flow phase), this vorticity layer is separated from the slope and vortices are generated and transported offshore, while a new vorticity layer of opposite sign (clockwise) is formed near above the slope. During the down-rush flow phase, there is no separation of this vorticity layer. In cases 2 and 3, there are no notable differences in the vorticity behavior above the seaward slope of the ZFBs. In case 4 with the shorter wavelength in comparison to case 1, the vorticity behavior is similar but the offshore transportation of the vortices is extended to a shorter distance (Fig. 8). In case 5 with the less permeable ZFB trunk in comparison to case 1, the vorticity behavior near the crest is similar, while a weak vorticity layer is generated at the interface between the armor layer and the core in the ZFB trunk (Fig. 9).

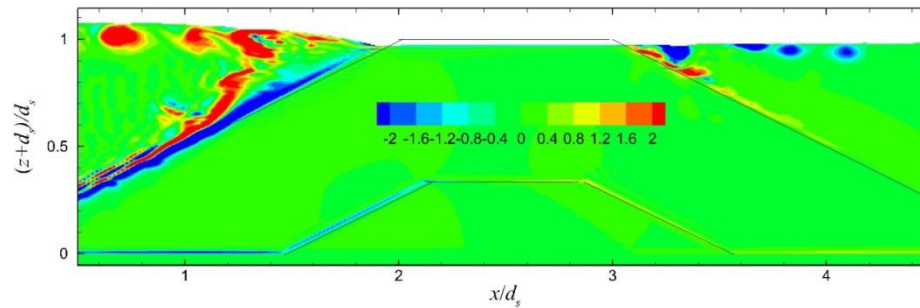




**Figure 7.** Vorticity field in the seaward region of the ZFB case 1 at four instants during the 30<sup>th</sup> wave period: (a)  $T/3$ , (b)  $3T/8$ , (c)  $5T/8$ , and (d)  $T$ .

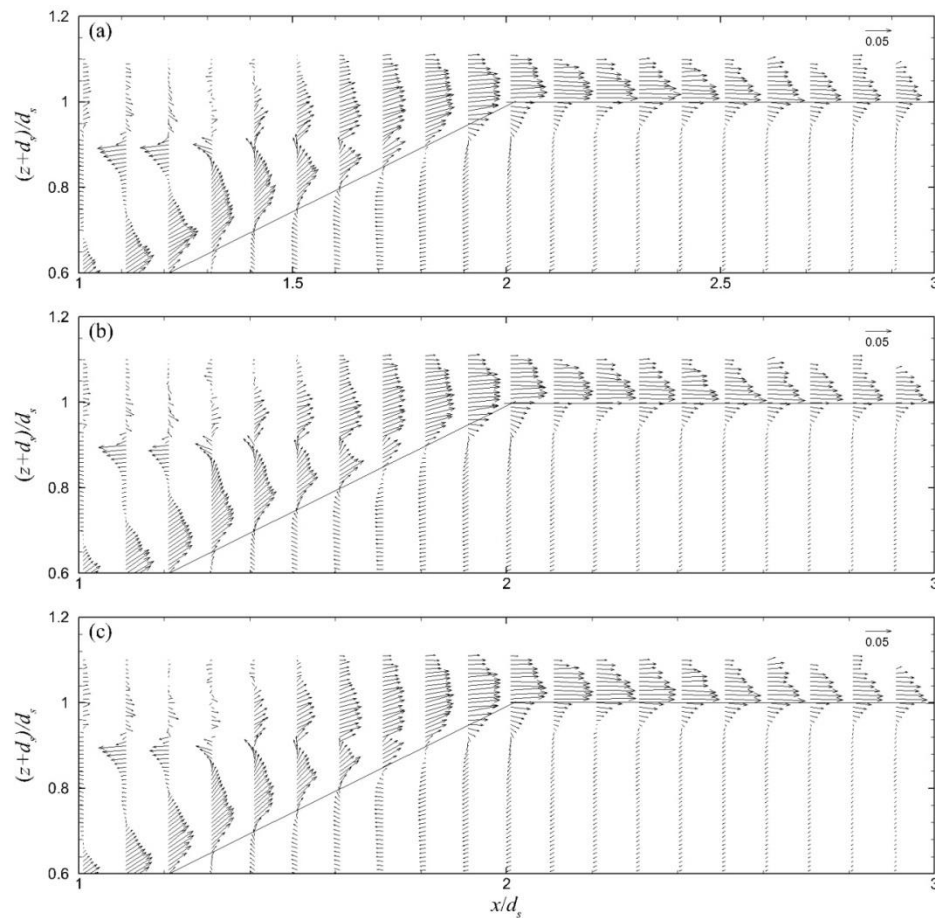


**Figure 8.** Vorticity field in the seaward region of the ZFB case 4 at four instants during the 30<sup>th</sup> wave period: (a)  $T/3$ , (b)  $3T/8$ , (c)  $5T/8$ , and (d)  $T$ .



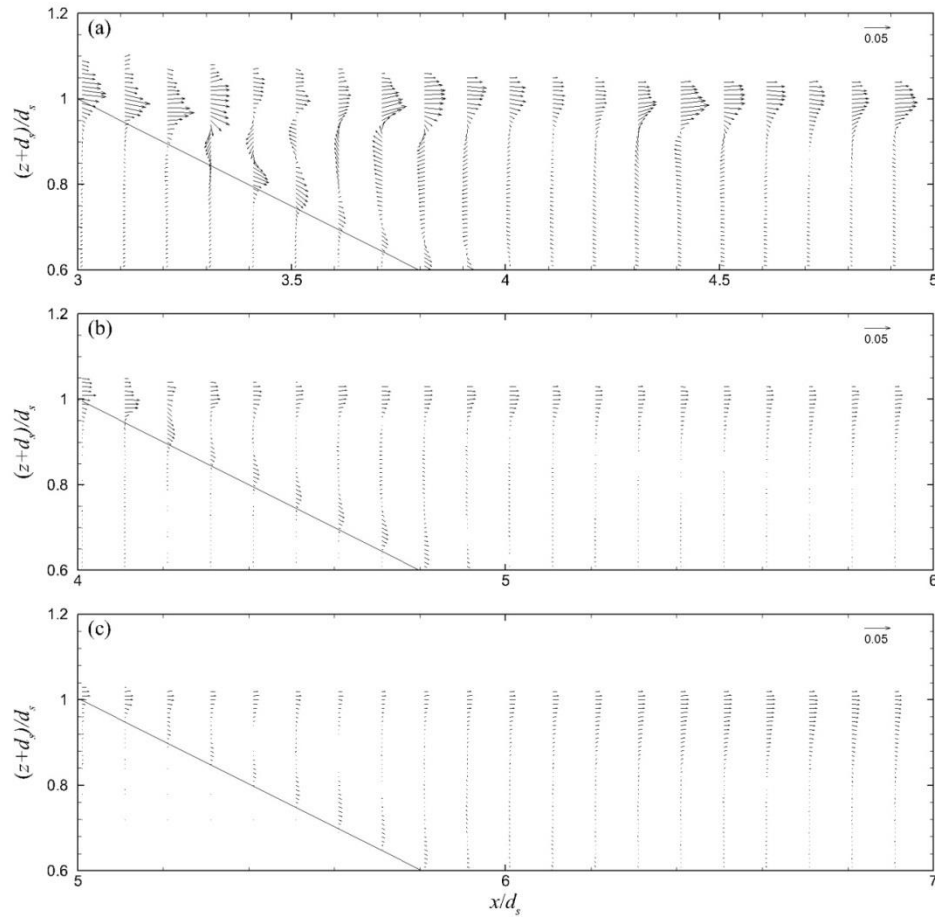
**Figure 9.** Vorticity field near the crest and in the ZFB trunk (case 5) at one instant ( $T/8$ ) during the 30<sup>th</sup> wave period.

The period-mean velocity field (of 10 wave periods after 20 wave periods of simulation) in the seaward region of the ZFBs in cases 1-3 is presented in Fig. 10. It is highlighted that in these cases, the generated currents above the ZFB seaward slope and crest are directed onshore due to wave overtopping, while the currents in the ZFB trunk are weaker and directed offshore. In the leeward region of these ZFBs, the period-mean velocity field is presented in Fig. 11. It is shown that as the crest width increases, the magnitude of the velocities becomes weaker. The period-mean velocity in the seaward and leeward regions of the ZFB case 4 is presented in Fig. 12. The direction of the currents in the seaward and leeward regions of the ZFB follows the same pattern as in case 1 but their magnitude is smaller in both regions due to the lower energy transmission onshore. The period-mean velocity field for the ZFB case 5 is presented in Fig. 13. The magnitude of the currents in the seaward and leeward regions and in the ZFB trunk is slightly larger in comparison to case 1.

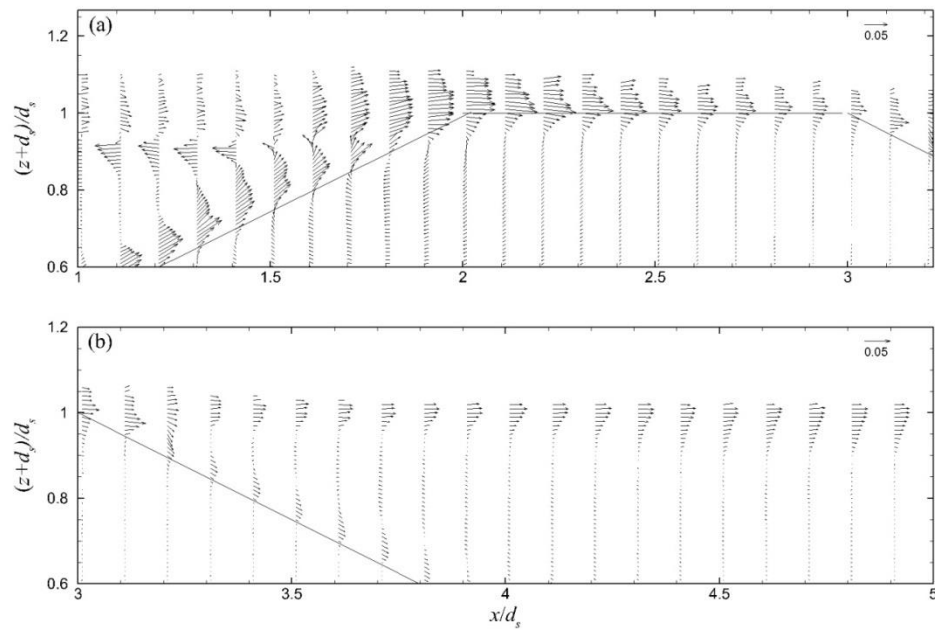


**Figure 10.** Period-mean velocity field in the seaward region of the ZFBs in cases: (a) 1, (b) 2, and (c) 3. Velocity vectors are shown non-dimensionalized by  $(g d_s)^{1/2}$  in the water phase under the wave crest envelope.

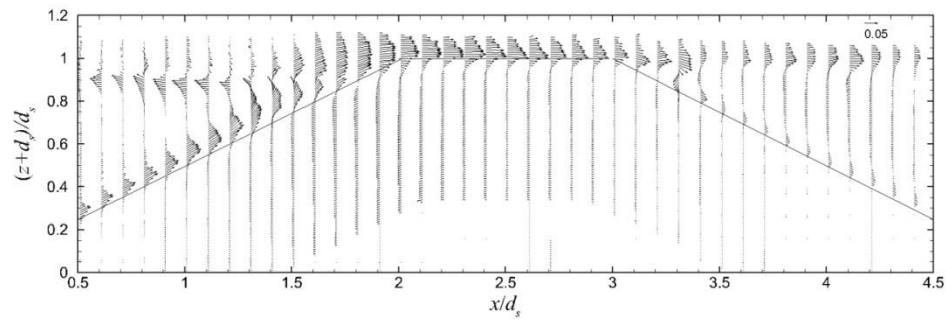




**Figure 11.** Period-mean velocity field in the leeward region of the ZFBs in cases: (a) 1, (b) 2, and (c) 3. Velocity vectors are shown non-dimensionalized by  $(gd_s)^{1/2}$  in the water phase under the wave crest envelope.

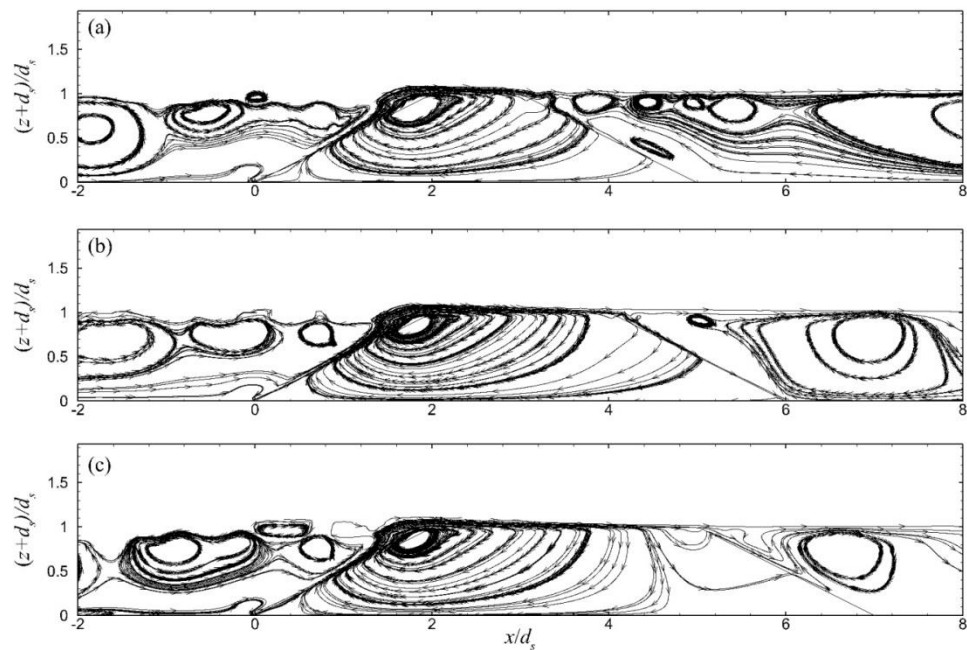


**Figure 12.** Period-mean velocity field for the ZFB case 4 in: (a) the seaward region, and (b) the leeward region. Velocity vectors are shown non-dimensionalized by  $(gd_s)^{1/2}$  in the water phase under the wave crest envelope.

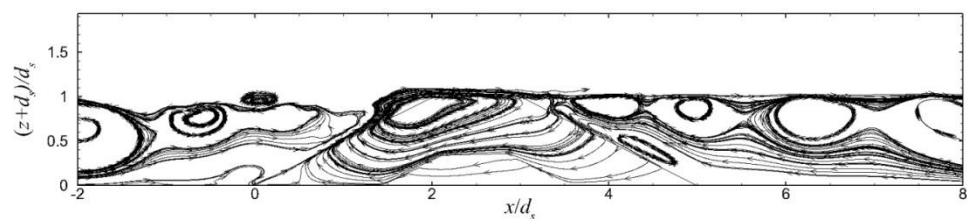


**Figure 13.** Period-mean velocity field for the ZFB case 5. Velocity vectors are shown non-dimensionalized by  $(gd_s)^{1/2}$  in the water phase under the wave crest envelope.

The period-mean flow pattern in the vicinity of the ZFBs for cases 1-3 is illustrated through streamlines in Fig. 14. It is clearly demonstrated that in the ZFB trunk, the flow is directed offshore in all cases. Part of the flow that overtops the crest of the ZFBs is returning offshore through the ZFB trunk; as a result the renewal of the ZFB leeward region water is facilitated. This process is obvious in cases 1 and 2. Further increase of the crest width though (case 3) results into the limitation of the flow circulation cell in the ZFB trunk and the interruption of the renewal of the ZFB leeward region water through the ZFB trunk. The pattern of the streamlines in ZFB case 4 does not differ in comparison to the one in case 1, and it is not shown. For the ZFB case 5, the return flow from the leeward to the seaward region through the ZFB trunk is inhibited by the presence of the less permeable core than in case 1.



**Figure 14.** Streamlines in the vicinity of the ZFBs in cases: (a) 1, (b) 2, and (c) 3.



**Figure 15.** Streamlines in the vicinity of the ZFB case 5.

The mean overtopping discharge,  $q$ , over and through the ZFBs, and the wave setup,  $\delta$ , in the leeward region of the ZFBs are shown in Table 3. The overtopping discharge was computed as the period-mean (of 10 wave periods after 20 wave periods of simulation) flux through the vertical cross-section at the leeward end of the ZFB crest. The instantaneous flux is

$$q_{lc}(t) = \int_0^{d_{lc}} u_{lc}(z, t) dz, \quad (23)$$

where  $d_{lc}(t)$  is the instantaneous water level at the leeward end of the ZFB crest. The mean overtopping discharge comprises the discharge through the part of the cross-section in the ZFB trunk and the one above it. The corresponding results are also shown in Table 3. The wave setup,  $\delta$ , was computed as the period-mean (of 10 wave periods after 20 wave periods of simulation) free-surface level over the SWL at the leeward ZFB toe.

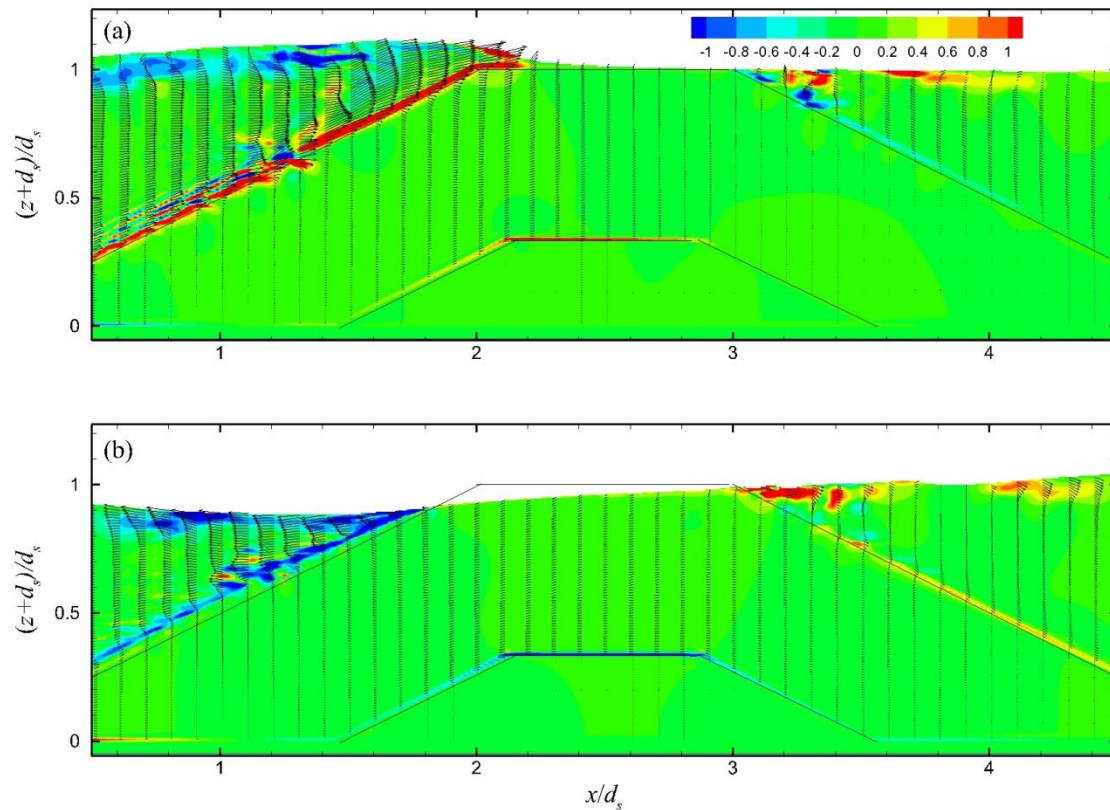
For ZFB case 1, the trunk discharge is in the offshore direction (negative), while the one over the crest is in the onshore direction (positive). As  $B$  increases, for ZFB cases 2-3, the negative trunk discharge weakens and even turns positive in case 3, while the one over the crest weakens as well but remains positive. The overall mean overtopping discharge is always onshore and it decreases albeit weakly with the increase of the ZFB crest width. The decrease of  $\xi_0$  in ZFB case 4, in comparison to case 1, also results into the weak decrease of the mean overtopping discharge. In ZFB case 5, both the trunk discharge and the one over the crest strengthen, in comparison to the ones in case 1, but the mean overtopping discharge decreases. To apply Eq. **Error! Reference source not found.** in the present cases, which are laboratory scale ones since  $d_s = 0.4$  m, an adjustment factor of  $f_q = 8.2$ , which is lower than the maximum value of 11 suggested in EurOtop [6] for  $\tan \alpha = 1/2$ . The mean overtopping discharge predicted by Eq. **Error! Reference source not found.** is constant for all ZFB cases, as shown in Table 3, reflecting the strong dependence of  $q$  on  $H_i$  but not the one on  $B$ ,  $\xi_0$ , and permeability as the present results suggest.

The wave setup increases with increasing  $B$ , for ZFB cases 1-2, but it decreases again for ZFB case 3 despite the further increase of  $B$  because of the interruption of the flow circulation cell in the ZFB trunk for case 3 as shown in Fig. 13c. The decrease of  $\xi_0$  in ZFB case 4, in comparison to case 1, results into the decrease of wave setup, while the decrease of permeability in ZFB case 5 results into the increase of wave setup. The corresponding wave setup predicted by the empirical formulas of Eq. **Error! Reference source not found.** overestimate  $\delta$  (Table 3) since they were both based on experiments without the recirculation system described in the Wave Generation subsection.

**Table 3.** Mean overtopping discharge and wave setup for all the ZFB cases (Table 1).

Case	$q/(g/d_s^3)^{1/2}$				$\delta/d_s$		
	Trunk discharge	Crest discharge	Overtopping discharge	EurOtop (2018)	Present	Diskin (1970)	Loveless (1998)
1	-0.0015	0.002580	0.001080	0.000976	0.01466	0.0735	0.0393
2	-0.000035	0.000989	0.000954	0.000976	0.01629	0.0735	0.0785
3	0.00052	0.000377	0.000897	0.000976	0.01427	0.0735	0.1178
4	-0.00032	0.001308	0.000988	0.000976	0.01002	0.0735	0.0194
5	-0.00219	0.003055	0.000865	0.000976	0.02346	0.0735	0.0393

Finally, the instantaneous shear stress field for the ZFB case 5 at two instants during the 30<sup>th</sup> wave period of the simulation is presented in Fig. 16. During the up-rush flow phase and as the wave crest approaches the breakwater crest, significant positive shear stress is observed near the seaward slope of the structure, while a positive layer is also developed in between the two different materials inside the porous media. A shear stress of opposite sign is developed in the same areas during the down rush flow phase. As expected, the seaward slope of the ZFB is the most crucial part of the structure in terms of hydraulic stability, as it experiences the larger values of the developing shear stress, i.e. destabilizing force due to wave breaking.



**Figure 16.** Shear stress at two instant during the wave period ( $T/2$  and  $T$ ) for the case 5.

#### 4. Discussion

In the present work, the effect of ZFB crest width, breaking parameter, and ZFB trunk permeability on wave reflection, crest overtopping, wave transmission, wave setup, and wave-generated currents was studied numerically.

The results indicate that the size of the crest width,  $B$ , does not notably affect wave (reflection coefficient) and flow (instantaneous vorticity and period-mean currents) processes in the seaward region of ZFBs. The processes in the leeward region of ZFBs though are significantly affected by  $B$ ; wave transmission, and magnitude of currents decrease with increasing  $B$ . In addition, the mean overtopping discharge heading onshore decreases albeit weakly with increasing  $B$ . The effect of  $B$  on wave setup is not monotonic as it depends on the pattern of the flow circulation in the ZFB trunk but eventually also decreases with increasing  $B$ . The effect of the breaking parameter,  $\xi_0$ , and the ZFB trunk permeability on wave and flow processes is significant both in the seaward and leeward regions of ZFBs. As  $\xi_0$  decreases, wave reflection, wave transmission, magnitude of currents, mean overtopping discharge, and wave setup all decrease; this observation is in accordance to the relevant empirical formulas (Tables 2 and 3) considered in this study. Finally, decreasing the ZFB trunk permeability leads to the increase of wave reflection, magnitude of currents, and wave setup, but the decrease of wave transmission and mean overtopping discharge.

Therefore, for the design of ZFBs, decreasing trunk permeability is equivalent to increasing crest width in terms of the wave and hydrodynamic processes in the leeward region of ZFBs as far as wave transmission and mean overtopping discharge are concerned but not equivalent for wave setup and magnitude of currents. If the latter parameters are not critical, decreasing the ZFB trunk permeability is a more economical option compared to the increase of crest width highlighted.

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