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Highlights

- A generic numerical model for shale gas flow in tight reservoir is proposed
- A flexible open-source framework OpenShale is developed with EDFM
- EDFM can lead to large error for shale gas flow without help of grid refinement
- A new geomechanics model for hydraulic and natural fractures is proposed and evaluated
- OpenShale successfully applied in field history matching and new model evaluation

Abstract

We present a generic and open-source framework for the numerical modeling of the expected transport and storage mechanisms in unconventional gas reservoirs. These unconventional reservoirs typically contain natural fractures at multiple scales. Considering the importance of these fractures in shale gas production, we perform a rigorous study on the accuracy of different fracture models. The framework is validated against an industrial simulator and is used to perform a history-matching study on the Barnett shale. This work presents an open-source code that leverages cutting-edge numerical modeling capabilities like automatic differentiation, stochastic fracture modeling, multi-continuum modeling and other explicit and discrete fracture models. We modified the conventional mass balance equation to account for the physical mechanisms that are unique to organic-rich source rocks. Some of these include the use of an adsorption isotherm, a dynamic permeability-correction function, and an embedded discrete fracture model (EDFM) with fracture-well connectivity. We explore the accuracy of the EDFM for modeling hydraulically-fractured shale-gas wells, which could be connected to natural fractures of finite or infinite conductivity, and could deform during production. Simulation results indicates that although the EDFM provides a computationally efficient model for describing flow in natural and hydraulic fractures, it could be inaccurate under these three conditions: 1. when the fracture conductivity is very low. 2. when the fractures are not orthogonal to the underlying Cartesian grid blocks, and 3. when sharp pressure drops occur in large grid blocks with insufficient mesh refinement. Each of these results are very significant considering that most of the fluids in these ultra-low matrix permeability reservoirs get produced through the interconnected natural fractures, which are expected to have very low fracture conductivities. We also expect sharp pressure drops near the fractures in these shale gas reservoirs, and it is very unrealistic to expect the hydraulic fractures or complex fracture networks to be orthogonal to any structured grid. In conclusion, this paper presents
an open-source numerical framework to facilitate the modeling of the expected physical mechanisms in shale-gas reservoirs. The code was validated against published results and a commercial simulator. We also performed a history-matching study on a naturally-fractured Barnett shale-gas well considering adsorption, gas slippage & diffusion and fracture closure as well as proppant embedment, using the framework presented. This work provides the first open-source code that can be used to facilitate the modeling and optimization of fractured shale-gas reservoirs. To provide the numerical flexibility to accurately model stochastic natural fractures that are connected to hydraulically-fractured wells, it is built atop other related open-source codes. We also present the first rigorous study on the accuracy of using EDFM to model both hydraulic fractures and natural fractures that may or may not be interconnected.

Source code is available at https://github.com/BinWang0213/MRST_Shale

**Key words:** shale gas; MRST; embedded discrete fracture model; open-source implementation

1 **Introduction**

Unconventional gas resources gain great interest recently due to successful economic development and strong energy supply around the world. Advancement of horizontal well drilling and hydraulic fracturing technology as well as better understanding unconventional reservoirs drives substantial growth of shale gas production (Bowker, 2007). Unlike conventional reservoirs, unconventional shale gas reservoirs can be characterized by ultra-low permeability, low porosity, complex transport mechanism and multi-scale fractures (Akkutlu et al, 2018). Development of unconventional resources is more technology-demanding and expensive. Thus, accurate modeling and numerical simulation of shale gas flow is critical for evaluating, designing and managing stimulation and production processes.

Well-established flow and transport theory for conventional reservoir rocks are not directly applicable to unconventional porous media (Gensterblum et al, 2015). For decades, researchers have been investigating the storage and transport mechanisms for unconventional reservoirs, which includes gas desorption, adsorbed gas porosity, gas slippage, and Knudsen diffusion, etc (Javadpour et al, 2007; Wang and Reed, 2009; Civan et al, 2010,2011; Sakhaee and Bryant, 2012; Akkutlu and Fathi, 2012, Yu et al, 2016 and Tan et al, 2018). In addition, the fractured shale matrix is comprised of a hierarchical network of pores down to a few nanometers, cracks and micro-fractures, which makes the formation a multi-scale porous medium with large heterogeneity and anisotropy (Akkutlu et al, 2018). Hence, the complex gas transport mechanisms and multiscale fracture system (**Figs. 1-2**)}
pose a great challenge to accurately and efficiently evaluate and simulate well performance in shale gas reservoirs.

![Fig 1 – Multi-scale natural of shale gas production](image)

In recent years, significant efforts have been made to model gas flow in unconventional reservoirs. These methods can be categorized into analytical model, semi-analytical model and numerical simulations. The analytical method dates back to 1970s, where the line-source fundamental solution is derived for simple fracture geometry such as single bi-wing hydraulic fractures and pseudo-pressure is applied to linearized the non-linear real gas equation (Gringarten et al, 1974, Cinco et al, 1978 and Agarwal 1979). Recently, the analytical method is extended into semi-analytical method to consider complex fracture networks and shale gas storage mechanism based on the boundary element method (Zuo et al, 2016, Chen et al, 2015, 2016, 2017, 2018; Yang et al, 2016a, 2016b, 2017, Yu et al, 2016b, 2017 and Li et al, 2018). Although analytical-based method is fast and accurate, it is difficult to handle rock heterogeneity, multi-phase, multi-compositional and strong non-linear transport mechanisms in
shale gas flow problems (Houze et al, 2010 and Olorode et al, 2013). On the other hand, numerical simulation has been proven to be is the most general and rigorous method to account for arbitrary non-linear physics and fracture geometry for unconventional reservoirs (Olorode et al, 2013,2017 and Cipolla et al, 2012). Highly coupled non-linear physics and treatment of multi-scale fractured system are two key issues in shale gas flow simulation. Fully implicit scheme with Automatic Differentiation (AD) is a robust and generic method to solve the highly coupled non-linear problem accurately and efficiently (Zhou et al, 2011 and Krogstad et al, 2015). In terms of multi-scale fractured system, dual continuum method (Warren and Root, 1963) and discrete fracture method (Karimi-fard et al, 2004, Hoteit and Firoozabadi, 2005, Hajibeygi et al, 2011 and Moinfar et al, 2014) are generally used to model highly connected fractures and long, disconnected hydraulic/natural fractures (Fig. 1), respectively. A hierarchical method is also proposed by integrating continuum method and discrete fracture method for multi-scale fractured system where the micro-fractures are upscaled into matrix permeability tensor and hydraulic/natural fractures are modeled explicitly (Lee et al, 2001 and Karimi-Fard et al, 2006). Unstructured gridding with local grid refinement (LGR) is generally used to capture the irregular fracture geometry and sharp pressure gradient near the fractures. However, it is are still challenging to generate conforming mesh efficiently for complex fracture networks (Karimi-Fard, Durlofsky, 2016). Recently, an embedded discrete fracture model is developed to resolve the complex gridding issue. Using EDFM, the complex fractures are embedded in conventional matrix grids without conforming the matrix grids with fracture plane, thus it is more efficient for complex fracture networks. In addition, it can be easily integrated into well-established reservoir simulator without accessing the code (Xu, 2015 and Olorode et al, 2017). Table 1 shows the advantages and disadvantages of these method where unstructured grid and EDFM are the two most promising methods for generic shale gas simulation with multi-scale fractures.

Table 1. Comparison of shale gas flow simulation methods

<table>
<thead>
<tr>
<th></th>
<th>Analytical</th>
<th>Semi-analytical</th>
<th>Structured grid</th>
<th>Unstructured grid</th>
<th>EDFM</th>
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<tr>
<td>Accuracy</td>
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<td>Nonlinear mechanisms*</td>
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<td>Rock heterogeneity</td>
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<td>Computational*** efficiency</td>
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Flow and transport theory and models for unconventional reservoir is a rapid evolving area of research, many of the existing and newly discovered phenomenon have not been completely understood. Also, the effect of these mechanism on practical well performance is not clear. To the best of our knowledge, almost all existing numerical models for shale gas reservoir are implemented in in-house simulators or commercial simulators (Jiang and Younis, 2015, Cao et al, 2016, Xu et al, 2017, Wang et al, 2017 and Akkutlu et al, 2018). Hence, it is necessary to develop a flexible and generic open-source framework to fill this gap.

In this paper, a generic numerical model is developed to simulate shale gas flow in unconventional reservoirs with multi-scaled fractures, which can be used to integrate any shale gas transport and storage mechanism for unconventional reservoirs as well as the geomechanics effect for fracture system. An efficient and flexible framework (OpenShale) is also developed using an open-source reservoir simulation toolkit (MRST) and EDFM. OpenShale can handle deterministic hydraulic fractures and stochastic natural fractures with arbitrary geometry and distribution. The framework is firstly verified against a commercial simulator and an in-house reservoir simulator that employs unstructured grid to simulate shale gas transport with non-planar hydraulic fracture, gas desorption, gas slippage & diffusion. The advantages and limitation of EDFM for shale gas flow problem is also discussed. Finally, field application of history matching and new geomechanics model evaluation are studied.

2 Mathematical equations

Considering the isothermal single-component single-phase gas flow in 2D fractured porous media with 1D fracture line without gravity effect. The general governing equation for shale gas flow in matrix ($\Omega_m$), considering storage ($m_{ad}$) and transport mechanisms ($F_{app}$), can be expressed as follows:

$$\frac{\partial}{\partial t} \left( \rho_g \phi + (1-\phi)m_{ad} \right) + \nabla \cdot \left( -\rho_g \frac{\prod F_{app}k_0}{\mu_g} \nabla p \right) = \rho_g q_w \quad \text{in} \ \Omega_m$$

Similarly, the governing equation for fracture ($\Omega_f$), only considering transport mechanisms, can be expressed as follows:
\[ \frac{\partial}{\partial t} \left( \rho_g \phi \right) + \nabla \cdot \left( -\rho_g \frac{\prod F_{app,i} k_0}{\mu_g} \nabla p \right) = \rho_g g_w \text{ in } \Omega_f \]  

(2)

Introducing inverse formation volume factor \( b_g = \rho_g / \rho_{gsc} \) (\( \rho_g = b_g \rho_{gsc} \)), the above equation can be rewritten as follows:

\[ \frac{\partial}{\partial t} \left( b_g \phi + \frac{(1-\phi) m_{ad}}{\rho_{gsc}} \right) + \nabla \cdot \left( -b_g \frac{\prod F_{app,i} k_0}{\mu_g} \nabla p \right) = b_g q_w \text{ in } \Omega_m \]  

(3)

where \( \rho_g \) is the mass density of gas, M/L^3; \( \mu_g \) is the dynamic viscosity of natural gas, N.T/L^2; \( m_{ad} \) is the accumulation term due to adsorption, M/L^3; \( \phi \) is the matrix porosity, dimensionless; \( k_0 \) is the absolute Darcy permeability of the reservoir rock, L^2. \( F_{app,i} \) is the \( i \)-th permeability correction factor for a specific shale gas transport mechanism; \( q_w \) is the volumetric sink/source term, M/L^3/T. \( k_0 \) is the absolute Darcy permeability of the reservoir rock, L^2.

2.1 Gas properties

Density: The pressure-dependent density of natural gas can be calculated by the real gas law:

\[ \rho_g = \frac{pM}{Z(p,T)RT} \]  

(4)

where \( M \) is the molecule weight of the natural gas, M/Mol; \( R \) is the Boltzmann constant, 8.314 ML^2T^{-2}/T/mole; \( T \) is the reservoir temperature, T;

The compressibility factor \( Z \) can be calculated using either implicit Peng-Robinson equation-of-state (PR-EOS) equation or empirical explicit equation. Using the empirical equation, the complex natural gas mixture can be considered as a single component with pseudo-temperature and pseudo-pressure. Mahmoud (2014) developed an explicit empirical equation for natural gas mixture as follows:

\[ Z(p,T) = 0.702 e^{-2 T_p} \cdot p_{pr}^2 - 5.524 e^{-2 T_p} \cdot p_{pr} + (0.0447 T_{pr}^2 - 0.164 T_{pr} + 1.15) \]  

(5)

where the reduced-temperature and reduced-pressure can be expressed as \( T_{pr} = T / T_c \) and \( p_{pr} = p / p_c \) , respectively. \( T_{pc} \) ands \( P_{pc} \) are the pseudo-critical pressure and pseudo-critical temperature for the shale gas mixture, respectively.

Also, for single component gas simulation, such as methane, the Z factor can be accurately
estimated by solving a cubic function of PR-EOS as follows (Lira and Elliott, 2012):

\[ Z^3 + a_2 Z^2 + a_1 Z + a_0 = 0 \]
\[ a_0(p,T) = (AB - B^2 - B^3), \quad a_1(p,T) = A - 3B^2 - 2B, \quad a_2(p,T) = B - 1 \]
\[ A = \frac{ap}{(RT)^2}, \quad B = \frac{bp}{(RT)} \]
\[ a = \frac{0.457235R^2T^2}{p_c}, \quad b = \frac{0.077961RT}{p_c} \] (6)

In this paper, an analytical solution (see details in appendix B of Lira and Elliott, 2012) is used for solving the cubic equation. For more complex natural gas mixture, it requires complex flash calculation and belongs multi-component compositional simulation which will be investigated in our future work. **Fig. 3** shows an estimation of Z-factor for methane using Eq.5 and Eq. 6, respectively.

**Fig. 3** Evaluated natural gas Z-factor for empirical and PR-EOS models with T=352 K, \( T_c=191 \) K, \( p_c=4.64 \) MPa, \( R=8.314 \) J/(K.mol)

**Fig. 4** Evaluated natural gas viscosity using Lee Lee-Gonzalez-Eakin empirical correlation with \( M=16.04 \) g/mol and \( T=633.6 \) Rankine
Viscosity: The density-dependent viscosity of natural gas can be estimated by the Lee-Gonzalez-Eakin empirical correlation (Lee et al, 1966) as follows:

\[ \mu_g = 10^{-7} K \exp(X \rho_g) \]

\[ K = \frac{(9.379 + 0.01607M)T^{1.5}}{209.2 + 19.26M + T}, \quad X = 3.448 + \frac{986.4}{T} + 0.01009M, \quad Y = 2.447 - 0.2224X \]

where the unit of \( M, T \) are g/mol and Rankine, respectively. Fig. 4 shows an estimation of viscosity for methane using Eq.7.

Noted that although the usage of pseudo-pressure equation can eliminate the nonlinearity issue introduced by pressure-dependent gas viscosity and compressibility (Eqs. 5-6), it leads to even larger errors especially for tight shale reservoirs (Houze et al, 2010). Thus, in this paper, the real-gas equation is used.

2.2 Transport and storage mechanism

Since rapid commercial development of unconventional tight reservoirs in recent years, many researchers spend enormous effort to understand the transport and storage mechanism of shale gas in such complex multi-scale systems (Figs. 1-2). Several key physical mechanisms (Yu et al, 2016; Klinkenberg, 1941; Florence et al, 2007; Javadpour, 2007; Civan, 2010) can be summarized as in Table 2.

In the presented open-source code, OpenShale, any storage and transport mechanisms models can be easily implemented via defining nonlinear gas storage function \( m_{ad} \) and permeability correction function \( F_{app} \). Demonstrative storage and transport models implemented in OpenShale this study are shown as follows:

Table 2. Key transport and storage mechanism for shale gas flow

<table>
<thead>
<tr>
<th>Mechanism</th>
<th>Models</th>
<th>Type</th>
<th>Continuum</th>
</tr>
</thead>
<tbody>
<tr>
<td>Adsorption</td>
<td>Langmuir, BET</td>
<td>S*</td>
<td>Matrix</td>
</tr>
<tr>
<td>Slip flow &amp; Diffusion</td>
<td>Klinkenberg, Florence, Javadpour, Civan</td>
<td>T*</td>
<td>Matrix</td>
</tr>
<tr>
<td>Non-Darcy flow</td>
<td>Darcy-Forchheimer</td>
<td>T</td>
<td>Fracture</td>
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*S-Storage mechanism, T-Transport mechanism

Adsorption: The gas molecules adsorbed in the pore wall of Kerogen in shale reservoir can be modeled using monolayer Langmuir isotherm and multiple layer BET isotherm as follows (Yu et al, 2016a):
Langmuir: \[ m_{ad} = \rho_s \rho_{gc} \frac{pV_L}{p + P_L} \] (8)

BET: \[ m_{ad} = \rho_s \rho_{gc} \frac{V_mCp_r}{1 - p_r} \left[ \frac{1 - (n + 1)p_r^n + np_r^{n+1}}{1 + (C - 1)p_r - Cp_r^{n+1}} \right] \] (9)

\[ p_r = \frac{p}{P_s}, \quad P_s = \exp(7.7437 - \frac{1306.5485}{19.4362 + T}) \]

where \( V_L \) is the Langmuir volume, \( \text{L}^3/\text{M} \). \( P_L \) is the Langmuir pressure, \( \text{M}/\text{L}/\text{T}^2 \). \( \rho_s \) is the density of rock bulk matrix \( \text{M}/\text{L}^3 \). \( V_L \) is the Langmuir volume (the maximum adsorption capacity at a given temperature), \( \text{L}^3/\text{M} \). \( P_L \) is the Langmuir pressure (the pressure at which the adsorbed gas volume is equal to \( V_L/2 \), \( \text{M}/\text{L}/\text{T}^2 \). \( V_m \) is the BET adsorption volume, \( \text{L}^3/\text{M} \). \( C \) is the BET adsorption constant, dimensionless. \( n \) is the BET adsorption molecular layers, dimensionless. \( p_r \) is the pseudo-saturation pressure, \( \text{M}/\text{L}/\text{T}^2 \). Noted that, the unit of \( P_s \) is MPa. **Fig. 5** shows an estimation of adsorption isotherm using Eq.8 and Eq. 9, respectively.

![Langmuir/BET Isotherm](image)

**Fig. 5** Langmuir and BET isotherms curve with \( V_L=0.0031 \text{ m}^3/\text{kg} \) and \( P_L=7.89 \text{ MPa} \), \( T=327.59 \text{ K} \), \( P_s=53.45 \text{ MPa} \), \( V_m=0.0015 \text{ m}^3/\text{kg} \), \( C=24.56 \) and \( n=4.46 \)

**Slippage flow & Diffusion**: Considering slippage and diffusion effect of shale gas flow in the matrix, the apparent permeability in the low-pressure region around the fracture will be increased. In the OpenShale, the Florence’s (2007) permeability correction factor (**Fig. 4**) is implemented as follows:

\[ F_{app} = (1 + \alpha K_n)(1 + \frac{4K_n}{1 + K_n}) \] (10)
where $Kn$ is the Knudsen number, dimensionless. $\alpha$ is the rarefaction parameter, dimensionless.

**Fig. 6** shows an estimation of gas slippage and diffusion permeability correction factor for methane using Eqs. 10-11.

**Non-Darcy Flow:** In case of high Forchheimer number ($F_{oc}>0.11$) in the hydraulic fractures, the linear Darcy flow is no longer applicable (Zeng and Grigg, 2006). The permeability correction factor (Barree and Conway, 2004) for Darcy-Forchheimer flow can be expressed as follows:

$$F_{app} = \frac{2}{1 + \sqrt{1 + 4 \beta \left( \frac{k_0}{\mu_g} \right)^2 |\nabla p|}}$$

**Fig. 6 – Permeability correction factor $F_{app}$ versus Knudsen number for all flow regions with methane properties in Table 2, $T=191$ K, $k_0=1 \times 10^{-10}$ and $\phi=0.1$**

where $\beta$ is the empirical Forchheimer coefficient, for propped hydraulic fractures, which can be evaluated as follows (Rubin, 2010):

$$\beta = 3.2808 \frac{1.485 \times 10^9}{(k_0 \times 10^{-15})^{0.021}}$$

**2.3 Geomechanics effect**

As shown in Fig. 2, shale reservoir has multi-scale fractures. The fracture conductivity will be decreased with increasing of production time due to the proppant embedment and fracture closure under high stress concentration near the fracture (Akkutlu et al, 2018, Hu et al, 2018a, 2018b). In this
paper, three types of fractures are defined based on their various length scales, including hydraulic fracture (half-length 50-100 meters, aperture 1 mm), natural fracture (half-length 1-20 m, aperture 0.1 mm), and micro-fracture (half-length < 1 m, aperture < 0.1 mm). A new geomechanics model is proposed herein by considering closure of micro-fracture, unpropped natural fracture and propped fractures.

To consider the micro-fracture closure, Gangi’s (1978) empirical pressure-dependent permeability reduction model can be applied as follows:

\[ k = k_0 F_{app} = k_0 \left[ 1 - \left( \frac{P_c - \alpha_B P_1}{P_1} \right)^m \right] \]  \tag{14}

Where \( \alpha_B \) is the Biot’s constant, \( P_c \) is the confining overburden pressure, \( P_1 \) is the effective stress when micro-fracture completely closed. \( m \) is a constant related to surface roughness. Fig. 7 shows an estimation of Gangi permeability correction factor for methane using Eqs. 14.

\[ F_{frac} \text{ vs. pore pressure with } m=0.5, p_1=180 \text{ MPa, } p_c=38 \text{ MPa and } \alpha=0.5 \]

To consider the closure of hydraulic and natural fractures, Alramahi and Sundberg (2012) performed experiment to measure the effect of closure pressure on propped fracture conductivity for different shale samples from stiff shale to soft shale. An empirical model of normalized fracture conductivity for propped fractures, \( F_{cd,N} \), can be fitted as follows:

- **Stiff Shale:** \( F_{cd,N}(p) = 10^{-0.00011\sigma-0.0971}, \quad R^2 = 0.961 \)
- **Medium Shale:** \( F_{cd,N}(p) = 10^{-0.00035\sigma-0.2396}, \quad R^2 = 0.996 \)
- **Soft Shale:** \( F_{cd,N}(p) = 10^{-0.00064\sigma-0.4585}, \quad R^2 = 0.987 \) \tag{15}
Wu et al (2018) performed similar experiment to investigate the effect of closure pressure on unpropped fracture conductivity. An empirical model of normalized fracture conductivity for unpropped fractures can be fitted as follows:

\[
\begin{align*}
\text{Stiff Shale: } F_{cd,N}(\sigma) &= 10^{-0.793 \ln(\sigma)+4.5618}, \quad R^2 = 0.995 \\
\text{Medium Shale: } F_{cd,N}(\sigma) &= 10^{-0.892 \ln(\sigma)+5.0725}, \quad R^2 = 0.988 \\
\text{Soft Shale: } F_{cd,N}(\sigma) &= 10^{-1.041 \ln(\sigma)+6.0216}, \quad R^2 = 0.989 
\end{align*}
\]

Where effective closure stress \(\sigma_c\) can be calculated by reservoir horizontal stress and in-situ fracture pore pressure, \(\sigma_c(p) = \sigma_h - p\). Plane direction of hydraulic fracture is normally orthogonal to the minimum horizontal stress and it support by rigid proppant, while the plane of natural fracture has stochastic orientation and lacking support from proppant. Thus, the closure stress for hydraulic fracture and natural fracture can be expressed as follows:

\[
\begin{align*}
\text{HydraulicFrac: } \sigma_{HF} &= \sigma_{h_{\text{min}}} - p \\
\text{NaturalFrac: } \sigma_{NF} &= \frac{\sigma_{h_{\text{min}}} + \sigma_{h_{\text{max}}}}{2} - p 
\end{align*}
\]

The empirical correlation between fracture conductivity and closure pressure are shown in Fig. 8. In the OpenShale, the fracture permeability can be reduced by a dynamic permeability correction factor as follows:

\[
k_f = k_0 F_{app} = k_0 \frac{F_{cd}(p)}{F_{cd}(\sigma_0)}
\]

Based on proposed empirical correlation model in Eqs. 15-16, a typical permeability correction factors for fracture closure can be shown as follows (Fig. 9):
Fig 9 – Permeability correction factor \( F_{\text{frac}} \) for hydraulic fractures and natural fractures

with \( p_o = 20.34 \text{ MPa} \) and \( p_{\text{wf}} = 34.5 \text{ MPa} \), \( \sigma_{h_{\text{min}}} = 29 \text{ MPa} \) and \( \sigma_{h_{\text{max}}} = 34 \text{ MPa} \)

3 Numerical Model

In this paper, a new shale gas simulation framework, OpenShale, is developed using the automatic differentiation module (ad-core, ad-props), black-oil module (ad-blackoil) and hierarchical fracture model (hfm) module in open-source MATLAB Reservoir Simulation Toolbox (Lie, 2012). Two-point flux approximated finite volume method (TPFA-FVM) is applied for discretizing the governing equations (Eq. 3). Time discretization is implemented using a fully implicit first-order backward scheme, where the Jacobian matrix of the nonlinear system is calculated by Automatic Differentiation. All nonlinear functions for shale gas transport and storage mechanisms as well as geomechanics effect are defined as separate function. For multi-scale fracture system, the larger fracture, such as the hydraulic fracture and natural fracture are explicitly modeled using EDFM. The micro-fractures are assumed highly connected and thus upscaled into the matrix permeability.

3.1 Numerical discretization

The discretized governing equation of Eq. 3 can be expressed as follows:

\[
\frac{\phi V}{\Delta t} \left( b_h (p^{n+1}) - b_g (p^n) \right) + \frac{(1-\phi) V}{\Delta t} \frac{1}{\rho_{\text{gc}}} \left( m_{\text{ad}}(p^{n+1}) - m_{\text{ad}}(p^n) \right) \\
- \text{div} \left( b_g (p^{n+1}) \prod_{i=1}^{l} \frac{F_{\text{app},i}(p^{n+1})}{\mu_g(p^{n+1})} T \cdot \text{grad}(p^{n+1}) \right) \\
- Vb_g (p^{n+1}) q_w (p^{n+1}) - Vb_g (p^{n+1}) \psi_{f-m}(p^{n+1}) = 0
\]  

The discretized governing equation for each 1D fracture system can be expressed as follows:
\[ \frac{\phi V}{\Delta t} \left( b_g(p^{n+1}) - b_g(p^n) \right) \]
\[ - \text{div} \left( b_g(p^{n+1}) \frac{\prod F_{\text{app},i}(p^{n+1})}{\mu_g(p^{n+1})} T \cdot \text{grad}(p^{n+1}) \right) \]
\[ - V b_g(p^{n+1}) q_w(p^{n+1}) - V b_g(p^{n+1}) \psi_{m-f}(p^{n+1}) = 0 \]

where \( V \) is the bulk volume of a grid cell. \( \psi_{f-m/m-f} \) is the flow coupling term between fracture and matrix. To simplify the implementation of governing equations (Eqs. 18-19), three discrete domain delta \( \delta \) functions for matrix (\( \Omega_m \)), hydraulic fractures (\( \Omega_{HF} \)) and natural fractures (\( \Omega_{NF} \)) can be defined as follows:

\[
\delta_m(x) = \begin{cases} 1 & x \in \Omega_m, \\ 0 & x \notin \Omega_m \end{cases}, \quad \delta_{HF}(x) = \begin{cases} 1 & x \in \Omega_{HF}, \\ 0 & x \notin \Omega_{HF} \end{cases}, \quad \delta_{NF}(x) = \begin{cases} 1 & x \in \Omega_{NF}, \\ 0 & x \notin \Omega_{NF} \end{cases}
\]

A generic numerical model for fractured reservoir considering shale gas transport and storage mechanism can be expressed as follows:

\[
\frac{\phi V}{\Delta t} \left( b_g(p^{n+1}) - b_g(p^n) \right) + \delta_m \left( 1 - \phi \right) \frac{1}{\rho_{\text{sc}}} \left( m_{ad}(p^{n+1}) - m_{ad}(p^n) \right) \]
\[ - \text{div} \left( b_g(p^{n+1}) \frac{\prod \left[ 1 + \delta_{HF/NF,j} F_{\text{app},j}(p^{n+1}) \right]}{\mu_g(p^{n+1})} T \cdot \text{grad}(p^{n+1}) \right) \]
\[ - V_{gk} b_g(p^{n+1}) q_w(p^{n+1}) - V_{gk} b_g(p^{n+1}) \psi_{f-m/m-f}(p^{n+1}) = 0 \]

Assuming vertical well fully penetrate the reservoir thickness, a semi-analytical well model (Peaceman, 1983) for a vertical well can be expressed as follows:

\[ q_w = \frac{W I}{\mu_g(p_{bh} - p)} \]

where \( p_{bh} \) is the bottom hole pressure of a wellbore, M/L/T². WI is the wellbore flow index.

The solution matrix from Eqs. 21 can be expressed as follows:

\[
\begin{bmatrix} A_{mm} & A_{mf} & A_{mw} \\ A_{fm} & A_{ff} & A_{fw} \\ A_{wm} & A_{wf} & A_{ww} \end{bmatrix} \begin{bmatrix} p_m \\ p_f \\ p_w \end{bmatrix} = \begin{bmatrix} Q_m \\ Q_f \\ Q_w \end{bmatrix}
\]

\#p_m = \# MatrixEles, \#p_f = \# FractureEles, \#p_w = \#Eles has well
Noted that the shale gas viscosity, density and permeability corrections terms are all depends on solution variables. To solve non-linear system of Eq. 23, the residual form of Newton’s iterations can be expressed as follows:

\[ J(x')(x^{i+1} - x^i) = \frac{dR}{dx}(x')(x^{i+1} - x^i) = -R(x') \]  

(25)

The Jacobian matrix \( J \) is calculated by automatic differentiation in MRST.

3.2 EDFM

![Grid system in EDFM for matrix, natural fracture and hydraulic fracture](image)

**Fig. 10 – Grid system in EDFM for matrix, natural fracture and hydraulic fracture**

As shown in **Fig. 10**, EDFM adopted the concept of dual-continuum fracture modeling method, the flow coupling term \( \psi_{f-m/m-f} \) is introduced to couple the solution among matrix and fractures. Thus, the matrix grid is not necessary conforming with the fracture plane. As shown in **Fig. 11**, there are three kinds of non-neighbor connection (NNC) in EDFM formulation: 1) fracture-matrix connectivity, 2) fracture-fracture connectivity and 3) fracture-well connectivity. The general NNC model can be expressed as follows (Xu, 2015):

\[ \begin{align*}
\psi^{\text{NCC}}_{f-m} &= T^{\text{NCC}}_{f-m} (p_f^{i+1} - p_m^{i+1}) \\
\psi^{\text{NCC}}_{f-f} &= -\psi^{\text{NCC}}_{m-f}
\end{align*} \]  

(26)

**Fig. 11 – Unit EDFM NNCs of 1) fracture-matrix (i-k pair) connectivity 2) fracture-fracture (j-k pair) connectivity and 3) fracture-wellbore (well-k pair) connectivity**

**Fracture-matrix NNC:** The fracture-matrix transmissibility \( T_{f-m} \) can be expressed as follows:
\[ T_{ik}^{\text{NNC}} = \frac{k_{0,ik} A_{ik}}{\mu_{g,ik} \langle d \rangle_{ik}} \]  

(27)

where \( A_{i,k} \) is the intersection area fraction between a fracture plane and a gridblock. For 2D grid, the area is the product of intersected fracture cell length within the matrix cell and uniform formation thickness, \( DZ \). Noted that the harmonic average and upwind scheme are used for the permeability and viscosity, respectively. \( \langle d \rangle_{i,k} \) is the average normal distance between matrix cell and fracture plane, which can be calculated as follows:

\[ \langle d \rangle_{i,k} = \frac{\int d_{ik} dv}{V_i} \]  

(28)

For 2D structured grid, an analytical solution is available for the average normal distance (see Tene et al, 2016).

**Fracture-fracture NNC:** the star-delta transformation can be used to calculate the transmissibility between intersected fractures as follows (Hajibeygi et al, 2011):

\[ T_{jk}^{\text{NNC}} = \frac{t_{fk}}{\sum_{m=1}^{n_{\text{m}}} t_{m}} , \quad t_{m} = \frac{A_{f,m}}{0.5 h_{f,m}} \frac{k_{0,m}}{\mu_{g,m}} \]  

(29)

where \( A_f \) is the cross-section area of a fracture plane, for 2D cell, which can be calculated by product of fracture aperture, \( w_f \), and formation thickness. \( h_f \) is the fracture cell length.

**Fracture-well NNC:** If a well intersected with a fracture cell, the effective wellbore index (WI) and equivalent radius (\( r_e \)) can be expressed as follows (Xu, 2015):

\[ WI_f = \frac{2 \pi k_f w_f}{\ln(r_e / r_w) + s} , \quad r_e = 0.14 \sqrt{h_f^2 + DZ^2} \]  

(30)

where \( s \) is the skin factor, dimensionless, which will be used as a correction factor to correct the error introduced by EDFM when model low-permeability fractures. \( DZ \) is the formation thickness, L.

### 4 Verification

To verify the presented general shale gas model (Eq. 21), two numerical simulations are performed against a commercial simulator (CMG, 2015) and an in-house simulator with unstructured mesh (Jiang and Younis, 2015). The base model and simulation parameters for all cases as shown in Table 3:

<table>
<thead>
<tr>
<th>Table 3—Base model and simulation parameters for all cases</th>
</tr>
</thead>
<tbody>
<tr>
<td>Property</td>
</tr>
<tr>
<td>----------</td>
</tr>
</tbody>
</table>
4.1 Case 1 – Verification against commercial simulator

OpenShale is firstly verified in a simple methane production case against a commercial simulator (CMG) with a single vertical hydraulic fracture (Fig. 12). By changing the hydraulic conductivity, grid schemes and natural fractures, three subcases (Case1a, Case1b and Case1c) are investigated. The accuracy of OpenShale with explicit fracture modeling (EFM) and EDFM are systematically studied. In this simulation, only Langmuir adsorption (Eq. 8) is considered. All fluid properties and simulation parameters are the same with the commercial simulator. The compressibility factor Z and natural gas viscosity are directly interpolated from the properties table of the commercial simulator. Detailed simulation properties are shown in Table 4.

Table 4. Key reservoir and simulation parameters of Case 1

<table>
<thead>
<tr>
<th>Property</th>
<th>Unit</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Domain dimensions (x,y)</td>
<td>m</td>
<td>606.6,606.6</td>
</tr>
<tr>
<td>Grid (nx,ny)</td>
<td>-</td>
<td>201.65</td>
</tr>
<tr>
<td>Formation thickness</td>
<td>m</td>
<td>45.72</td>
</tr>
<tr>
<td>Initial reservoir pressure</td>
<td>MPa</td>
<td>34.47</td>
</tr>
<tr>
<td>Temperature</td>
<td>K</td>
<td>327.60</td>
</tr>
<tr>
<td>Langmuir pressure</td>
<td>MPa</td>
<td>8.96</td>
</tr>
<tr>
<td>Langmuir volume</td>
<td>m³/kg</td>
<td>0.0041</td>
</tr>
<tr>
<td>Matrix porosity</td>
<td></td>
<td>0.07</td>
</tr>
<tr>
<td>Matrix compressibility</td>
<td>1/Pa</td>
<td>1.45e-10</td>
</tr>
<tr>
<td>Matrix permeability</td>
<td>nD</td>
<td>500</td>
</tr>
<tr>
<td>Fracture permeability</td>
<td>mD</td>
<td>0.5-1000</td>
</tr>
<tr>
<td>Fracture width</td>
<td>m</td>
<td>0.003</td>
</tr>
<tr>
<td>Fracture half-length</td>
<td>m</td>
<td>106.68</td>
</tr>
<tr>
<td>Fracture conductivity</td>
<td>md-ft</td>
<td>5-10000</td>
</tr>
<tr>
<td>Well BHP</td>
<td>MPa</td>
<td>3.45</td>
</tr>
<tr>
<td>Production time</td>
<td>years</td>
<td>30</td>
</tr>
</tbody>
</table>
Fig. 12 Fracture map (a) and pressure contour after 30 years production (b) of Case 1a and Case 1b

Case 1a: In the first subcase, three fracture conductivities (10000 md-ft, 50 md-ft, 5 md-ft) are used to verify the accuracy of OpenShale with EFM and EDFM. Fig. 13 shows a good agreement of both gas flow rate and cumulative production between OpenShale and commercial simulator. Results show that OpenShale with EFM (dash line) always gives consistent results against commercial simulator. But OpenShale with EDFM (solid) has significant error (up to 10.92%) when fracture conductivity is low (5 md-ft). Fig. 12a shows that OpenShale EDFM only converges to reference solution under infinite fracture conductivity (10000 md-ft). This is observation matches Tene (2017)’s conclusion that EDFM can not handle the fracture with low permeability.

Fig. 13 Comparison of gas flow rate (a) and cumulative production (b) for Case 1a between OpenShale EDFM (solid line), OpenShale EFM (dash line) and a commercial
simulator (dots) with respect to fracture conductivities of 5 md-ft (green lines), 50 md-ft (blue lines) and 10000 md-ft (red lines)

Case1b: For unconventional tight reservoir, LGR is usually required to capture the transient flow behavior and sharp pressure gradient near the hydraulic fractures. In the second subcase, the effect of grid schemes on accuracy of OpenShale with EFM and EDFM are investigated. In this case, the fracture conductivity is set as 10000 md-ft to eliminate the EDFM error mentioned in Case1a. All other parameter is the same with Case1a. As shown in Fig. 14, three grid schemes are investigated, where LGR scheme with logarithmic refinement that is solved by OpenShale EFM; EDFM scheme is the standard EDFM grid scheme (Xu et al, 2017 and Tene et al, 2017) with uniform grid that is solved by EDFM; EDFM+LGR scheme is the same grid scheme as LGR scheme that an additional EDFM fracture cell is added and that is solved by EDFM. Noted that all grid scheme has the same grid dimension (nx,ny) of 499x61.

Fig. 14 EFM and EDFM Grid schemes for Case1b, fracture cell is shown 10 times larger than the real size, where logarithmic refinement and uniform used in LGR and EDFM scheme, respectively.

Figs. 15-16 shows a good agreement of gas flow rate and cumulative production between OpenShale and commercial simulator with respect to high fracture conductivity and low fracture conductivity. OpenShale with EFM again gives consistent results against commercial simulator for all grid schemes. However, the standard EDFM grid scheme can introduce an error of 3.31% for high fracture conductivity and 1.11% for low fracture conductivity. The error is measured by the difference of cumulative production between grid schemes of LGR+EDFM and EDFM. This
benchmark case demonstrates that EDFM cannot capture transient flow behavior and sharp pressure
gradient near the hydraulic fracture without helping of LGR.

![Log-log gas flow rate](image1)

**Fig. 15** Comparison of gas flow rate (a) and cumulative production (b) for Case 1b with high fracture conductivity of 10000 md-ft between OpenShale and a commercial simulator (dots).

![Log-log gas flow rate](image2)

**Fig. 16** Comparison of gas flow rate (a) and cumulative production (b) for Case 1b with low fracture conductivity of 5 md-ft between OpenShale and a commercial simulator (dots).

**Case 1c**: As mentioned in Case 1a and Case 1b, EDFM cannot handle low-permeability fracture and hydraulic fractures with sharp pressure gradient. But modeling of natural fracture network is quite challenge for the EFM. In this subcase, the effect of different grid schemes of natural fractures on accuracy for OpenShale with EDFM is also investigated. As shown in **Fig. 17**, six natural fractures with the same length of 116.74 m are added based on the Case 1a. The well performance of two grid schemes with and without LGR for natural fractures are studied. Fracture conductivity for
hydraulic fracture and natural fractures are set as 10000 md-ft and 5 md-ft, respectively. All other parameters are the same with Table 3.

![Grid schemes of Case 1c](image)

**Fig. 17** Grid schemes of Case 1c, number of grids are shown 20 times coarser than the real scheme. LGR scheme with LGR for natural fractures, EDFM scheme without LGR for natural fractures

**Fig. 18** demonstrates that OpenShale with EDFM can lead to a significant error (up to 16.99%) for the case where low-permeability natural fractures connected with high-permeability hydraulic fractures. Also, EDFM without LGR for natural fractures tends to underestimate the well performance (error of 3.4% for six natural fractures). This benchmark case indicates that EDFM is not capable to accurately model well performance of shale gas flow in ultra-tight reservoir due to the errors introduced by low-permeability fracture and grid refinement.

![Comparison of gas flow rate](image)  ![Normalized cumulative production](image)

**Fig. 18** Comparison of gas flow rate (a) and normalized cumulative production by NFs (b) for Case 1c between different grid scheme for natural fractures
In sum, this case study shows that OpenShale with EFM always give consistence results against commercial simulator, while OpenShale with EDFM only converge to the reference solution at infinite fracture conductivity (Case1a). Also, OpenShale with EDFM cannot handle low-permeability fracture (Case1b) and cannot capture transient behavior and sharp gradient without LGR (Case1c). OpenShale with EDFM can model complex and irregular natural fractures accurately and efficiently. Thus, in the following simulations, an empirical skin-factor and uniform grid refinement are adopted to relieve the limitations of EDFM. More advanced projected EDFM (Tene et al, 2017) and adaptively grid refinement will be implemented in our future work.

4.2 Case 2 – Verification against in-house simulator

OpenShale is further verified against an in-house simulator (Jiang and Younis, 2015) by considering more comprehensive state-of-art transport mechanisms and fracture geometries. For the reference solution, it used fully unstructured mesh with LGR to capture the complex fracture geometries as well as the sharp pressure gradient near the fracture. In this case, the gas rate solution of two sub-case are investigated. In the first sub-case (Case2a), the well performance with and without storage (Eq. 8) and transport mechanism (Eq. 10) is considered. In the second sub-case (Case2b), the irregular fracture geometry is considered. The fracture map of Case2a is shown in Fig. 19. Detailed simulation parameters for Case 2 are elaborated in Table 4.

![Fracture Map](image)

**Fig. 19 Fracture map and EDFM grid of Case 2**

**Table 4. Key reservoir and simulation parameters of Case 2**

<table>
<thead>
<tr>
<th>Property</th>
<th>Unit</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Domain dimensions (x,y)</td>
<td>m</td>
<td>200,140</td>
</tr>
<tr>
<td>Formation thickness,</td>
<td>m</td>
<td>10</td>
</tr>
<tr>
<td>Initial reservoir pressure</td>
<td>MPa</td>
<td>16</td>
</tr>
<tr>
<td>Temperature</td>
<td>K</td>
<td>343.15</td>
</tr>
<tr>
<td>Langmuir pressure</td>
<td>MPa</td>
<td>4</td>
</tr>
</tbody>
</table>
Langmuir volume $m^3/kg$ 0.018
Matrix porosity 0.1
Matrix compressibility $1/Pa$ $1.0e^{-9}$
Fracture porosity 1.0
Matrix permeability $nD$ 100
Fracture permeability $D$ 1
Fracture width $m$ $1e^{-3}$
Well BHP $MPa$ 4
Correction skin factor - 43
Production time $days$ 10000

Other parameters are the same as in Table 2.

**Fig. 20** shows pressure contour after 2500 days of production for Case 2 with and without transport mechanisms. It can be observed that the sub-case with full mechanism has better pressure depletion (dark blue region) than one without any mechanism. **Fig. 21** shows a good agreement between gas flow rate between OpenShale and an in-house simulator, where demonstrates that the both adsorption and gas slippage and diffusion effect increase the gas production significantly. In tight unconventional reservoirs, smaller pore-throat and lower bottom-hole pressure can lead to higher production due to gas slippage flow and releasing adsorbed gas.

**Fig. 20 Pressure contour with and without full shale gas transport mechanism @ 2500 days of Case 2**
In the previous sections, OpenShale shows it capability to handle arbitrary transport and storage mechanism and fracture geometries. To further illustrate the applicability of OpenShale in practical problems, two case studies of OpenShale in realistic unconventional reservoirs with complex fracture network are presented.

5.1 Case 3: History matching and production forecast

To further verify the applicability of the OpenShale. A history matching with field production data on a Barnett shale has performed. The field production and simulation data are adopted from literature (Cao, Liu and Leong, 2016; Yu and Kamy Sepehrnoori, 2014). The detailed reservoir and fluid parameters are shown as in Fig. 22 and Table 5.
Table 5. Key reservoir and simulation parameters of Barnett shale for Case 3 (Cao, 2016)

<table>
<thead>
<tr>
<th>Property</th>
<th>Unit</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Domain dimensions (x,y)</td>
<td>m</td>
<td>1200,300</td>
</tr>
<tr>
<td>Depth</td>
<td>m</td>
<td>5463</td>
</tr>
<tr>
<td>Formation thickness</td>
<td>m</td>
<td>90</td>
</tr>
<tr>
<td>Initial reservoir pressure</td>
<td>MPa</td>
<td>20.34</td>
</tr>
<tr>
<td>Temperature</td>
<td>K</td>
<td>352</td>
</tr>
<tr>
<td>Rock density</td>
<td>kg/m³</td>
<td>2500</td>
</tr>
<tr>
<td>Langmuir pressure</td>
<td>MPa</td>
<td>4.47</td>
</tr>
<tr>
<td>Langmuir volume</td>
<td>m³/kg</td>
<td>0.00272</td>
</tr>
<tr>
<td>Matrix porosity</td>
<td></td>
<td>0.03</td>
</tr>
<tr>
<td>Matrix compressibility</td>
<td>1/Pa</td>
<td>1.5e-10</td>
</tr>
<tr>
<td>Fracture compressibility</td>
<td>1/Pa</td>
<td>1.0e-8</td>
</tr>
<tr>
<td>Matrix permeability</td>
<td>nD</td>
<td>200</td>
</tr>
<tr>
<td>Fracture permeability</td>
<td>mD</td>
<td>100</td>
</tr>
<tr>
<td>Fracture width</td>
<td>m</td>
<td>0.003</td>
</tr>
<tr>
<td>Fracture spacing</td>
<td>m</td>
<td>30.5</td>
</tr>
<tr>
<td>Fracture half-length</td>
<td>m</td>
<td>47.2</td>
</tr>
<tr>
<td>Fracture conductivity</td>
<td>md-ft</td>
<td>1</td>
</tr>
<tr>
<td>Well BHP</td>
<td>MPa</td>
<td>3.69</td>
</tr>
<tr>
<td>Correction skin factor</td>
<td>-</td>
<td>19</td>
</tr>
<tr>
<td>Production time</td>
<td>days</td>
<td>1600</td>
</tr>
</tbody>
</table>

Other parameters are the same as in Table 2.

In this simulation, a rectangle reservoir with dimension of 1100 × 290 × 90 m was discretized by 148 × 39 × 1 grids. 28 stages hydraulic fractures in the center of domain with the half-length of 47.2 m and the fracture spacing of 30.5 m. The fractures are assumed have constant aperture of 0.003 m and permeability of 100 md. Only shale gas storage mechanism of Langmuir adsorption (Eq. 8) is considered. Fig. 23 shows the pressure contour at different production time (400 days and 1600 days). Fig. 24 shows the comparison of production rate between OpenShale and field data which
shows good agreements with the field production data. Based on matched simulation parameters, the production forecast can be easily performed as in Fig. 21.

![Figure 23 Pressure contour after 1600 days production for Barnett shale reservoir (Case 3)](image)

**Figure 23** Pressure contour after 1600 days production for Barnett shale reservoir (Case 3)

![Fig. 24 History matching (a) and production forecast (b) of a Barnett shale well (Case 3)](image)

**(a)** *(left)* and *(b)* *(right)*

**Fig. 24** History matching (a) and production forecast (b) of a Barnett shale well (Case 3)

### 5.2 Case 4: New model evaluation

To illustrate the capability of modular design and rapid prototyping of OpenShale, a new shale gas model considering geomechanics effect (Eqs. 15-17) for multi-scale fractured network is implemented and evaluated using OpenShale. In this section, the influence of multi-scale fracture network and geomechanics effect on shale gas production performance will be investigated.

![Fig. 25 Fracture map with 28 non-planar hydraulic fractures and 248 natural fractures of Case 4](image)

**Fig. 25** Fracture map with 28 non-planar hydraulic fractures and 248 natural fractures of Case 4
In this case, all the simulation parameters are the same with Case 3 of Barnett shale reservoir. The total length of non-planar hydraulic fractures (blue lines in Fig. 25) is the same as planar fractures used in Case 3 (blue lines in Fig. 14). Natural fractures are stochastically generated by an open-source fracture generator ADFNE (Alghalandis, 2017). The geomechanics parameters for shale reservoir are assumed (Wasaki and Akkutlu, 2015) as follows (Table 5):

Table 5. Geomechanics parameters of Barnet shale for Case 4

<table>
<thead>
<tr>
<th>Property</th>
<th>Unit</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Biot constant, $\alpha$</td>
<td>-</td>
<td>0.5</td>
</tr>
<tr>
<td>Overburden confining stress, $p_c$</td>
<td>MPa</td>
<td>38</td>
</tr>
<tr>
<td>Maximum horizontal stress, $s_{hmax}$</td>
<td>MPa</td>
<td>34</td>
</tr>
<tr>
<td>Minimum horizontal stress, $s_{hmin}$</td>
<td>MPa</td>
<td>29</td>
</tr>
<tr>
<td>Maximum closure stress for micro-fracture, $p_1$</td>
<td>MPa</td>
<td>180</td>
</tr>
<tr>
<td>Gangi exponential constant, $m$</td>
<td>-</td>
<td>0.5</td>
</tr>
<tr>
<td>Natural fractures permeability, $md$</td>
<td></td>
<td>10</td>
</tr>
</tbody>
</table>

Other parameters are the same as in Tables 2-3

Fig. 26 Pressure contour at the 3.75 years for Barnett shale reservoir with Non-planar fracture geometries and natural fractures (case 4)
Firstly, the effect of complex fracture network on well performance is studied. **Fig. 26** shows the pressure contour for the non-planar fractures with and without the natural fractures. Obviously, the case of natural fractures has larger and better stimulated reservoir volume (SRV). Thus, as shown in **Fig. 27**, the cumulative gas production of non-planar case with natural fracture has much higher value (14.56% improvements) than the planar case in the Case 3. While in the case of same total length, the non-planar fracture geometries will slightly degenerate the well performance (-5.69% reduction).

**Fig. 27 Comparison of gas flow rate (a) and cumulative production (b) between Planar, Non-planar and Non-planar & natural fractures cases**

The influence of geomechanics effect with fracture closure on well performance is further investigated by implementing Eqs. 15-17. **Fig. 28** shows the pressure contour at the 3.75 years for the planar case (Fig. 20a) and realistic case (Fig. 20b) with non-planar hydraulic fracture, natural fractures and geomechanics effect. As shown in **Fig. 29**, at the earlier production period, even realistic case has lower production than simple planar case due to geomechanics effect. But in the
later production time, the contribution of natural fractures makes identical well performance between realistic case and simple planar case. Thus, the modeling of natural fractures and geomechanics effect is important for long-term production evaluation.

![Comparison of gas flow rate and cumulative production between planar hydraulic fracture case and realistic case with non-planar, natural fractures and geomechanics effect](image)

Fig. 29 Comparison of gas flow rate (a) and cumulative production (b) between planar hydraulic fracture case and realistic case with non-planar, natural fractures and geomechanics effect

6 Conclusion

In this work, A generic numerical model and an open-source framework OpenShale are developed for shale gas simulation with state-of-art flow and storage mechanisms. It is verified against commercial and in-house reservoir simulators. The limitation of EDFM are also investigated quantality. Also, a field application of history matching and new model evaluation of geomechanics effect are successful performed. Several conclusions can be drawn as follows:

1. A generic shale gas numerical model is developed which can be used to model any state-of-art storage and transport mechanisms, including gas adsorption, gas slippage & diffusion, non-Darcy flow as well as geomechanics effect by considering complex multi-scale fracture geometries.

2. A general and open-source framework, OpenShale is developed and verified. With the help of the EDFM, Automatic Differentiation, and object-designed framework of OpenShale, one can easily use and extend OpenShale to simulate practical shale gas problem with arbitrary fracture geometries and new storage and transport mechanisms.

3. EDFM can efficiently and accurately model irregular fracture geometry and complex fracture
networks. However, it cannot accurately model low-permeability fracture (error of 12.22%) and hydraulic fractures without help of LGR where have strong transient behavior and sharp gradient (error of 2.84%). Thus, projected EDFM and adaptively grid refinement will be implemented and tested in our future work.

(4) Shale gas transport and storage mechanisms, such as gas desorption and gas slippage & diffusion flow gas, are the most significant impact on well performance, follow by natural fractures, geomechanics effect and fracture geometry.

(5) OpenShale is capable of serving as an efficient, flexible research tool to evaluate new models with arbitrary non-linearity and fracture complexity. It can serve as a bridge between mechanism study and field scale engineering application.

Nomenclature

\[ \rho_g = \text{mass density of natural gas, kg/m}^3 \]
\[ \phi = \text{absolute rock porosity, dimensionless} \]
\[ \Omega_m = \text{matrix domain} \]
\[ \Omega_f = \text{fracture domain} \]
\[ m_{ad} = \text{storage mechanism term, kg/m}^3 \]
\[ F_{app} = \text{transport mechanism term, dimensionless} \]
\[ k_0 = \text{absolute Darcy rock permeability, m}^2 \]
\[ \mu_g = \text{viscosity of natural gas, Pa} \cdot \text{s} \]
\[ p = \text{pore pressure, Pa} \]
\[ q_w = \text{volumetric sink/source term, m}^3/\text{day} \]
\[ b_g = \text{inverse formation volume factor, dimensionless} \]
\[ M = \text{molecular weight of natural gas, kg/mol} \]
\[ Z = \text{compressibility factor of natural gas, dimensionless} \]
\[ R = \text{ideal gas constant, 8.314 J/(mol} \cdot \text{K)} \]
\[ T = \text{reservoir temperature, K} \]
\[ T_{pr} = \text{pseudo-temperature for natural gas, dimensionless} \]
\[ T_c = \text{critical-temperature for natural gas, K} \]
\[ p_{pr} = \text{pseudo-pressure for natural gas, dimensionless} \]
\[ p_c = \text{critical-pressure for natural gas, Pa} \]
\[ a_{0,1,2} = \text{constants for Peng-Robinson equation of state, dimensionless} \]
\[ a,b = \text{constants for Peng-Robinson equation of state, dimensionless} \]
\[ A,B = \text{constants for Peng-Robinson equation of state, dimensionless} \]
\[ K,X,Y = \text{constants for Lee-Conzalez-Eakin natural gas viscosity, dimensionless} \]
\[ \rho_s = \text{mass density of bulk matrix, kg/m}^3 \]
\[ \rho_{gsc} = \text{mass density of natural gas at the standard condition, kg/m}^3 \]
\[ V_L = \text{Langmuir volume, m}^3/\text{kg} \]
1. \( P_L \) = Langmuir pressure, Pa
2. \( V_m \) = BET volume, \( m^3/kg \)
3. \( P_s \) = BET pseudo-saturation pressure, Pa
4. \( p_r \) = pseudo-pressure for BET isotherm, dimensionless
5. \( C \) = constant for BET isotherm, dimensionless
6. \( n \) = constant for BET isotherm, dimensionless
7. \( \alpha \) = rarefaction coefficient for gas slippage flow, dimensionless
8. \( K_n \) = Knudsen number, dimensionless
9. \( \beta \) = Darcy-Forchheimer coefficient, dimensionless
10. \( \alpha_B \) = Biot’s coefficient, dimensionless
11. \( P_c \) = reservoir confining overburden pressure, Pa
12. \( P_l \) = reservoir effective stress when micro-fracture completely closed, Pa
13. \( m \) = constant for the Gangi’s model, Pa
14. \( F_{cd} \) = fracture conductivity, \( md\cdot ft \)
15. \( p_0 \) = initial reservoir pressure, m
16. \( \sigma \) = effective fracture closure stress, Pa
17. \( \sigma_{hf} \) = effective closure stress for hydraulic fracture, Pa
18. \( \sigma_{nf} \) = effective closure stress for natural fracture, Pa
19. \( \sigma_h \) = reservoir horizontal principle stress, Pa
20. \( \sigma_{hmin} \) = minimum reservoir horizontal principle stress, Pa
21. \( \sigma_{hmax} \) = maximum reservoir horizontal principle stress, Pa
22. \( k_f \) = absolute Darcy permeability of fracture, \( m^2 \)
23. \( w_f \) = fracture width, m
24. \( V \) = bulk volume of a grid cell, m
25. \( \delta \) = discrete domain delta function, dimensionless
26. \( \Delta t \) = solution time-step, day
27. \( \psi_{fm} \) = mass coupling term for matrix, dimensionless
28. \( \psi_{mf} \) = mass coupling term for fracture, dimensionless
29. \( p_{bh} \) = wellbore bottom hole pressure, Pa
30. \( k_{11} \) = absolute Darcy rock permeability in x-direction, \( m^2 \)
31. \( k_{22} \) = absolute Darcy rock permeability in y-direction, \( m^2 \)
32. \( r_e \) = equivalent radius for wellbore model, m
33. \( r_w \) = wellbore radius, m
34. \( s \) = wellbore skin factor, dimensionless
35. \( \Delta x \) = grid cell size in x-direction, m
36. \( \Delta y \) = grid cell size in y-direction, m
37. \( \Delta z \) = grid cell size in z-direction, m
38. \( WI \) = wellbore index, dimensionless
39. \( x \) = Unknown vector, -
40. \( J \) = Jacobian matrix, -
41. \( R \) = Residual vector, -
42. \( WI \) = wellbore index, dimensionless
43. \( p_f \) = pore pressure at the fracture domain, Pa
44. \( p_m \) = pore pressure at matrix domain, Pa
\[ T = \text{transmissibility, dimensionless} \]
\[ A = \text{intersection area among fracture and matrix, m}^2 \]
\[ d = \text{average normal distance among fracture and matrix, m} \]
\[ h_f = \text{length of a fracture cell, m} \]
\[ t = \text{fracture transmissibility for fracture-fracture NNC, dimensionless} \]

Subscripts:
\[ NF = \text{natural fracture} \]
\[ HF = \text{hydraulic fracture} \]
\[ m = \text{matrix} \]
\[ f = \text{fracture} \]
\[ g = \text{gas} \]
\[ w = \text{well} \]

References


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