

Article

Determination of serviceability limits of a turboshaft engine by the criterion of blade natural frequency and stall margin

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Abstract: This paper analyses the health and performance of 12-stage axial compressor of the TV3-117VM/VMA turboshaft operated in a desert environment. The results of the dimensional control of 4,800 worn blades are analysed to model the wear process. Operational experience and numerical simulations are used to assess the effectiveness of an Inlet Particle Separator. Numerical modal analysis is performed to generate the Campbell diagram of worn blades and identify resonant blade vibration which can lead to high cycle fatigue (HCF). It is shown that the gradual loss of the stall margin over time determines the serviceability limits of compressor blades. Recommendations setting out go / no-go criteria are made to maintenance and repair organisations.

Keywords: gas-turbine performance, turboshaft, axial compressor, blade, FEM, CFD, erosion, wear, stall margin, compressor surge, brownout

1. Introduction

Long-term engine performance in adverse operating conditions is one of the main conditions for successful helicopter missions. Unlike an aeroplane, the helicopter has to hover for a long time above the ground, often raising cloud dust and causing a brownout. Therefore, the ability to conduct long-term operations at elevated dust concentrations is one of the most important features of modern helicopters. Studies on the impact of environmental particles on the efficiency of helicopter engines were already carried out during the development of the first types of helicopters [1].

The operation of a helicopter engine in a dusty environment causes contamination of the gas path [2,3]. Deposition of particles on aerofoils [4,5] and the heat exchanging surfaces of the air cooling system [6] can lead to deterioration of the aerodynamic and thermodynamic properties of these components. Moreover, given that dust particles (no matter how small they are) have abrasive properties, they also cause erosive wear of the engine components and contribute to various types of structural damage [7–9]. Erosive wear of compressor blades leads to reduction in the stall margin of the compressor, increase in the likelihood of fatigue damage of compressor blades due to changes in their natural frequencies of vibration and a decrease in the efficiency of the engine due to the wear of the gas path.

Rotating components are sensitive to mechanical damage caused by solid particles [10]. The models describing their impact and related erosive damage were proposed by many researchers, such as Finney [11], Bitter [12] and Sheldon [13], but the prediction of the actual aerofoil degradation is still difficult. The main factors affecting the magnitude of erosion consist of the angle of collision, velocity and particle size, blade surface properties, and particle concentration. Van der Walt [14] showed that the wear rate of the aerofoils is directly proportional to dust concentration. The mechanical properties of the material are also an important parameter influencing the mechanisms of erosion [15,16].

Eustyfeev [17] performed experimental and theoretical studies of compressor blades eroded by solids to determine the erosion resistance of the blade material EI-961. The limiting ratio of the particle size to their velocity of contact with the material was determined. But the experiment was performed

36 on a cut-out sample, not on a real blade, as well as on one type of material, that is EI-961 steel, while
37 most of the blades of modern compressors are made of titanium alloy.

38 Batcho [18] and Singh [19] analysed loss of performance caused both by erosion and deposition.
39 The impact of ingested particles on engine operation depends on the physical and chemical properties
40 of the dust, its composition and concentration. Particles deposited on compressor aerofoils change
41 their geometry and roughness, which leads to a decrease in the efficiency and consequently reduces
42 the pressure ratio and performance of the compressor [20].

43 The time between overhauls (TBO) of an engine operated in a highly dusty environment is much
44 less than that set by the manufacturer and is reduced by the erosion of the compressor blades. The
45 statistical analysis [21] showed that erosive wear of compressor blades was the cause of 30 - 35% of the
46 engines grounded due compressor blade damage, the largest of all causes. This is comparable to the
47 proportion of engine removals due to foreign objects ingested from the runway during take-off (25 -
48 30%). The share of aviation incidents, bird ingestion, or human errors during maintenance accounts
49 for 15 - 20%.

50 The aim of this study was to assess the serviceability limit of the blades of the axial compressor of
51 a helicopter engine operating in a dusty environment. To achieve this goal, the following tasks based
52 on the results of the dimensional control of worn blades were performed:

- 53 • establishing patterns of blade wear as a function of flight hours (FH) and dust concentration
- 54 • evaluating the increase of the natural frequency of blades by modelling the geometry of worn
55 aerofoils over the engine operating time
- 56 • development of a methodology for modelling the flow through the axial compressor
- 57 • calculating the compressor maps describing the blades with different degrees of wear

58 2. Methods

59 In this work, the compressor blades of the TV3-117 turboshafts (Figure 1) powering the Mi-8MTV
60 and Mi-24 helicopters in the desert environment of the Republic of Algeria are studied.
61 The region of North Africa and the Middle East features, in addition to extreme ambient temperatures,
62 a high concentration of dust and sand dispersing up to a height of 6000 m which is the helicopter
63 operation zone. For example, in North Sudan, the dust concentration is 1.3 g/m^3 , and in Algeria $1.3 -$
64 1.6 g/m^3 . The size of particles ingested into the gas path ranges from 0.01 to 2 mm.

65 The operation of gas-turbine engines in the regions described above, with a high content of dust
66 and sand, inevitably leads to deterioration of engine performance [22,23]. Airborne particles may
67 cause substantial erosive wear of compressor blades. A consequence of this is a widening of the tip
68 clearance and a modification of the aerofoil profile - in particular, the chord length and the blade
69 thickness appear to decrease, especially above 66% of the span (Figure 2). This leads to reduction in
70 compressor pressure ratio and ultimately a reduction in efficiency of the entire engine.

71 Firstly, a statistical analysis was carried out to study the nature of compressor wear and to
72 determine its critical components. Based on the subsequent regression analysis, patterns of wear of the
73 blades of all compressor stages as a function of engine operation time and dust concentration were
74 established.

75 The obtained patterns of the chord wear of blades of the all compressor stages were used to
76 predict their geometry, depending on the engine operating time. This allowed for the modelling of
77 blade vibration, simulation of the flow through the worn compressor and a determination of the
78 serviceability limit of the blades in terms of structural integrity and the stall margin.

79 For the analysed engines, the observed impact of erosion on compressor performance was several
80 times greater than deposition, due to a high dust concentration and fair inlet protection. Moreover,
81 compressor fouling can be reversed by washing. Therefore, particle deposition is not taken into account
82 in this work.

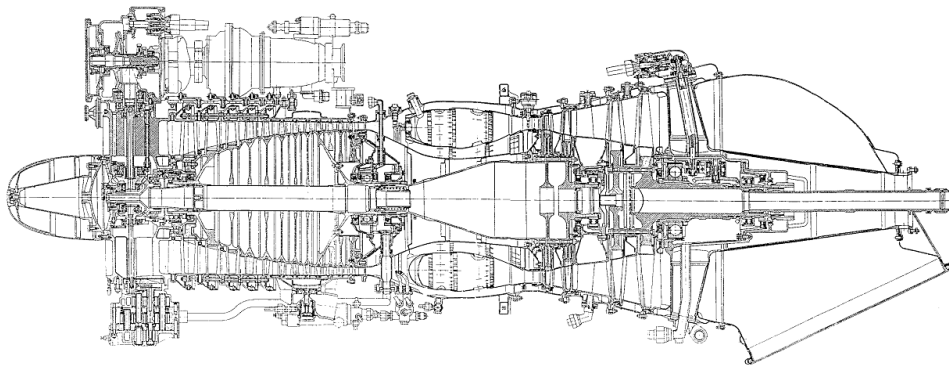


Figure 1. TV3-117 turboshaft

83 2.1. Blade inspection

84 The inspected engines were grounded and torn down for one of two reasons: either due to the
85 chord wear of the compressor blades of the first stage in the upper part exceeding 2 mm; or, due to
86 the performance parameters of the engine, such as the gas generator speed n_1 or the turbine inlet
87 temperature TIT, being outside the permissible limits.

88 The dimensional control of blade geometry was performed by measuring the chord and the
89 thickness of the profile at various sections as well as blade height. Ten blades were selected for the
90 evaluation from each stage of 40 engines [24]. In total, 4,800 blades were inspected. Statistica 12 was
91 used to analyse the results.

92 The inspected engines were initially divided into two categories. The first included those that
93 were operated without a particle separator (IPS) and the second, with an IPS.



Figure 2. Blades of a compressor of a turboshaft subjected to erosive wear

94 2.2. Structural analysis

95 Compressor blades of modern turboshafts are characterised by thin profiles and relatively low
96 stiffness, therefore forced vibration represents a notable threat to them [25,26]. The compressor blades
97 absorb intense static and dynamic loads. When rotating under large centrifugal forces, the blades
98 undergo deformation, which leads, in particular, to a decrease in their twist. The compressor blades
99 vibrate due to unsteady flow forces relative to their static deformations. The distribution of dynamic
100 stresses in blades has to be determined to ensure that they are below the fatigue limit of the material
101 [27,28].

102 The erosive wear of blades has a significant impact on their strength, which is confirmed by the
103 works of Hamed [1,29]. The properties of the blade surface and its ability to withstand erosion are one
104 of the key factors that determine the reliability of the system, since a variety of surface irregularities
105 can lead to stress concentration that increases the risk of high cycle fatigue (HCF) [30–33].

106 The main reason for the excitation of blade vibration is circumferential flow irregularity. The flow
107 is also non-uniform in the radial direction. The frequencies of the driving forces are multiples of the

108 rotor speed (engine orders) which are equal to the number of obstacles around the circumference, e.g.
109 the number of guide vanes and struts in the gas path. When the speed changes, a number of resonant
110 frequencies can be excited. To predict the frequencies of resonant vibration, a modal analysis of blades
111 and the Campbell diagram are necessary [34,35].

112 Vibration frequencies and operational deflection shapes can be determined with a certain degree
113 of accuracy by numerical methods, in particular using volumetric finite element models (FEM). At
114 present, this research method is preferred, since the complex geometry of the aerofoils is generally not
115 amenable to the analytical method of calculating frequencies and vibration modes.

116 Blade geometry was measured using 3D scanning, followed by postprocessing in the CAD system
117 ASCON KOMPAS 16.0. Geometry models of compressor blades were developed in Unigraphics
118 NX8. Compressor blades after various periods of operation in a dusty environment were described
119 using parameterized solid-state models. By varying blades height, chord length and thickness in the
120 corresponding sections of the aerofoil, several variants of blade geometry were generated.

121 The grid models of blades, developed using the ANSYS ICEM CFD grid generator, consisted of
122 15 - 18 thousand hexagonal SOLID 185 elements. The calculation of the natural vibration frequencies
123 of the blades was carried out numerically using the ANSYS 14.5 solver.

124 2.3. CFD model

125 The 3D flow calculation, with an ideal gas as the working fluid, was based on the Navier-Stokes
126 equations and the finite element method (FEM), implemented in the ANSYS CFX solver. The mesh
127 was developed in ANSYS Turbo Grid to model the operation of the compressor (Figure 3). A separate
128 mesh flow model (domain) was designed for each stage (Figures 4, 5). The domains were designed
129 taking into account the possibility of air flow to leak in the radial gap (Figure 6) by adding the interface
130 in the blade tip. The compressor model consisted of 26 domains.

131 The following grid parameters were considered when building the grid:

- 132 • ATM Optimized topology ensures a high quality mesh with hexahedral elements for twisted
- 133 aerofoils
- 134 • Parameter y_{\pm} size of the first wall element has a value within (80-160) units
- 135 • The ratio of the dimensions of the elements does not exceed 6.

136 First, the flow calculation was performed for two rotational speeds: 95% and 98%, where 1%
137 corresponds to 195.37 rpm. Ambient air temperature of 288 K and pressure of 101.325 kPa was assumed.
138 Each rotational speed of the compressor rotor corresponds to certain angles of variable inlet guide
139 vanes (IGV) and guided vanes of the further four stages.

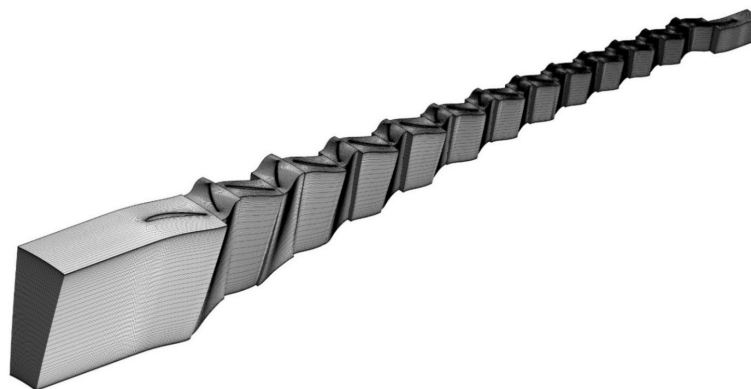


Figure 3. CFD model of the compressor

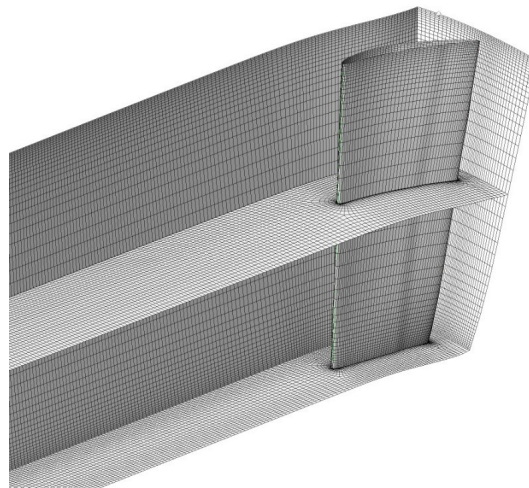


Figure 4. Mesh of inlet flow

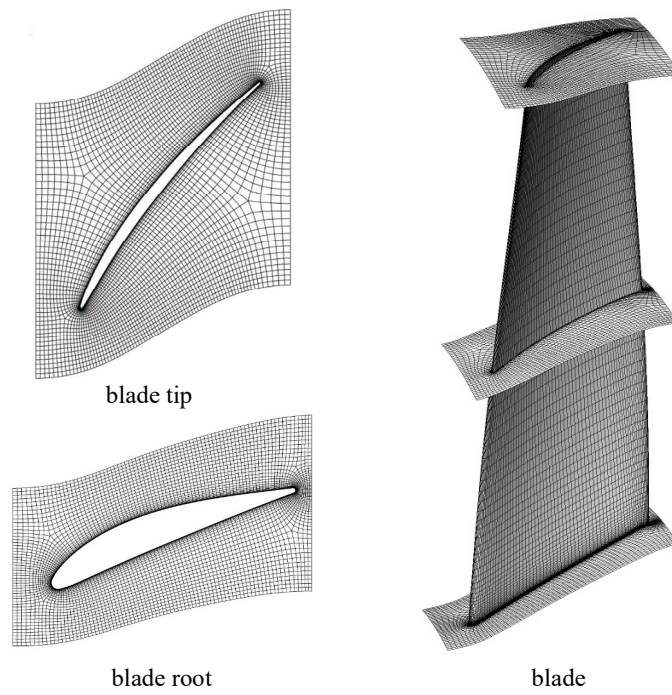


Figure 5. CFD mesh for the first stage blade

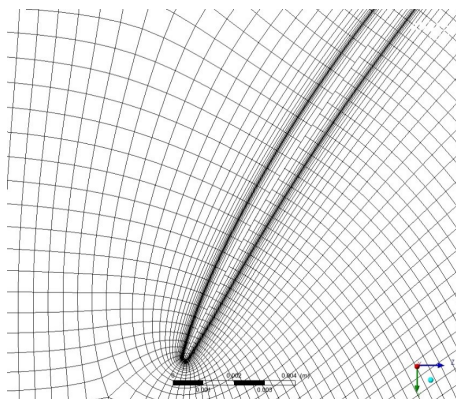


Figure 6. Mesh in the tip gap

140 To reduce the required computing power, a single blade with cyclic symmetry along the
141 lateral boundaries of the domain was modelled for each compressor stage. Stage interfaces
142 (Mizing-Plane) between fixed and rotating domains were defined, which allowed for interpolation
143 between interconnected grids, taking into account the laws of mass conservation.

144 The choice of the turbulence model depends on the nature of the turbulent flow, the required
145 accuracy, the available computational resources, and the time cost. The SST $K-\omega$ turbulence model
146 of Menter was chosen as more accurate and reliable for the class of flows with a positive pressure
147 gradient. The residual RMS error of 1×10^{-6} was assumed as the satisfactory condition of CFD
148 convergence and it was achieved after 600-870 iterations.

149 CFD results were used to estimate the compressor maps, as in another paper about this turboshaft
150 [36]. The mass flow rate was measured at the outlet of the compressor. Each operating point
151 corresponded to a certain mass flow, in the range from 4 to 11 kg/s.

152 2.4. Modelling two-phase flow through IPS

153 The modelling of multiphase flows presents a number of difficulties compared to single-phase
154 flows, since it is necessary to solve the equation of mass, amount of motion and energy conservation for
155 each phase separately. These equations are much more complicated than single-phase currents, since
156 they have additional terms that govern the exchange of mass and energy between phases. However,
157 due to various concomitant physical phenomena and possible changes in the flow regime, the exact
158 value of additional members is not always known.

159 In order to solve these problems, we considered multiphase dispersion flows in which there is one
160 continuous as well as one dispersion phase. The dispersed phases contained many particles distributed
161 in a continuous phase. Euler model and ANSYS CFX software were used for modelling. The equations
162 of mass, amount of motion and energy conservation were solved separately for each phase. In the
163 equations of motion, the interfacial drag force and other forces observed in multiphase dispersed
164 systems were taken into account. The calculations determined the local flow rate, temperature and
165 volume fraction of the dispersed phase. A granulation model was used to account for particle collision,
166 friction, and density of the particles.

167 To simulate two-phase flow and obtain results on the velocity of motion and distribution of dust
168 particles in the air, the following assumption were made:

- 169 • geometric model of the separator
- 170 • concentration and chemical composition of dust
- 171 • pressure and air velocity in the separator
- 172 • flow model: two-phase
- 173 • full pressure at the inlet to the engine: 101325 Pa
- 174 • exit velocity: 150 m/s
- 175 • temperature: 288 K
- 176 • turbulence model: $K-\epsilon$
- 177 • dust concentration at the inlet: 2 g/cm^2
- 178 • foreign particles material: quartz sand
- 179 • particle size: case 1) 10 - 50 μm , case 2) 50 - 100 μm

180 3. Results and discussion

181 3.1. Chord wear

182 The results of the dimensional control of the compressor blades show that the highest wear is
183 observed at the blade tip, while a much lower wear is exhibited near the root (Figure 7). The chord
184 wear of sections 2 - 4 can be expressed as a function of the wear of the tip section.

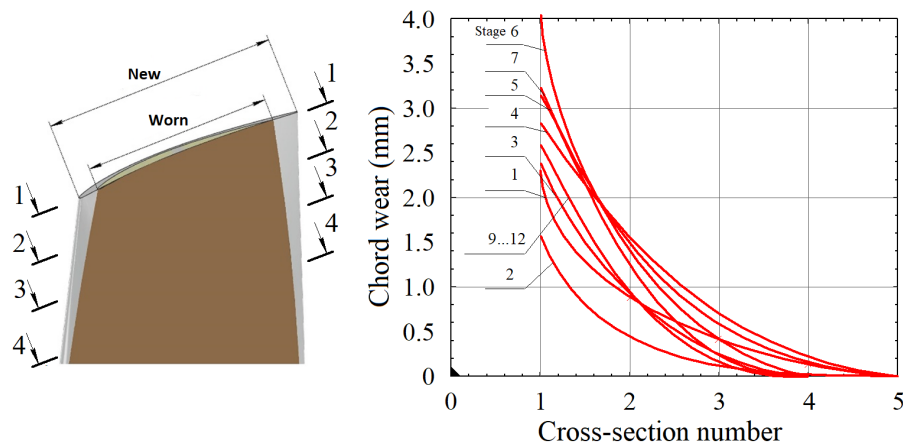


Figure 7. Chord wear of the compressor blade in specific cross-sections

185 Statistical analysis carried out for individual stages revealed the wear patterns caused by the
 186 design features of the compressor. Figure 8 shows the chord wear of the compressor blades of all the
 187 stages. For engines operated without IPS, the largest wear is observed for the first-stage blades while
 188 for engines operated with IPS, for the sixth stage blades.

189 Engines belonging to the first category, operated without IPS, were grounded in accordance with
 190 the current standards for the maximum allowable wear of the chord of the blade of the first stage of
 191 the compressor in the upper part: 2 mm. The effective TBO of the first category engines was only 150 -
 192 200 FH, provided that nominally for this type of engine is 1500 FH.

193 Engines from the second category, operated with IPS, were removed from service due to their
 194 operating parameters, such as n_1 speed and turbine inlet temperature beyond the permissible limits.
 195 The effective TBO for the second category was 600 - 650 FH which indicates a partial effectiveness of
 196 the applied IPS [37].

197 Given the close correlation ($R > 0.856$) between the wear of the blades of stages 2-12, it is possible
 198 to assess the wear of the blades of each stage based on the established regression dependencies. The
 199 chord wear of the sixth stage blades is used as the independent variable. This choice is explained by
 200 the fact that, despite the obvious advantages of using the first stage for the dimensional control of
 201 blades, which are the most convenient from the point of view of monitoring and predicting remaining
 202 useful life (RUL) without removing and disassembling the engine, it does not correlate well with the
 203 wear of the remaining stages ($R < 0.4$).

The chord wear of the compressor stages 2-12 correlates with the wear of the sixth-stage blades
 and can be estimated using the linear regression.

$$c_i = a_i c_6 + b_i \quad (1)$$

204 The dependence of the chord wear on the compressor blades on the engine operating time in a dusty
 205 environment can be satisfactorily described by a second-order curve (Figure 9).

$$c_6 = (4.69 \times 10^{-6} t + 1.25 \times 10^{-3}) t \delta \quad (2)$$

where δ is the dust concentration in g/m^3 . For the analysed fleet, the average concentration
 $\delta = 1.6 \text{ g}/\text{m}^3$ can be assumed:

$$c_6 = 7.5 \times 10^{-6} t^2 + 0.02t \quad (3)$$

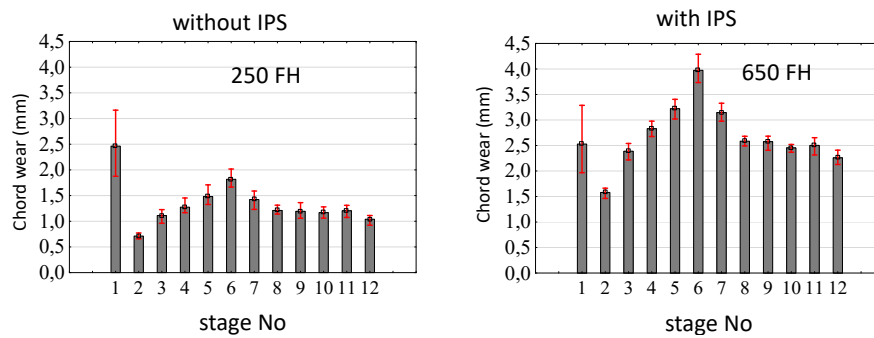


Figure 8. Average chord wear of individual compressor stages, for an engine operated without IPS or with IPS

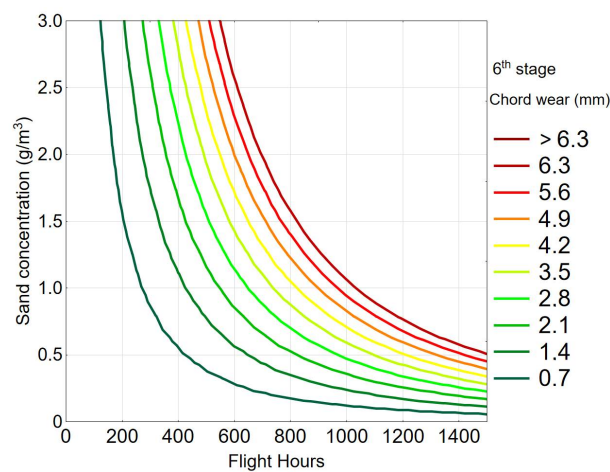


Figure 9. Chord wear of sixth-stage blades in function of flight hours

206 3.2. Modal analysis of blades

207 To assess the effect of wear on the natural frequency of the vibration, a modal analysis was
 208 performed (Figure 10). For each stage, an individual Campbell diagram was developed taking into
 209 account the nominal and worn profile of the aerofoil. Erosion significantly increases the natural
 210 frequencies of the blades. The analysis reveals several resonances excited by engine orders. Some
 211 stages were identified for which there is a risk of resonance in the operating speed range (Figure 11).

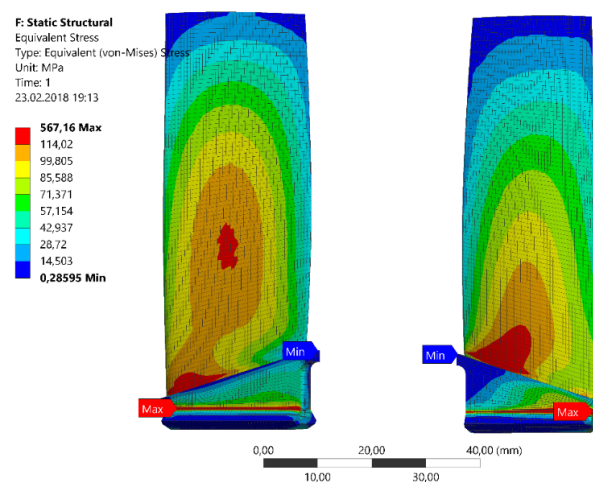


Figure 10. Modal and kinetostatic stresses of the first-stage blade with a nominal (left) and worn aerofoil (right) for $n_1 = 100\%$

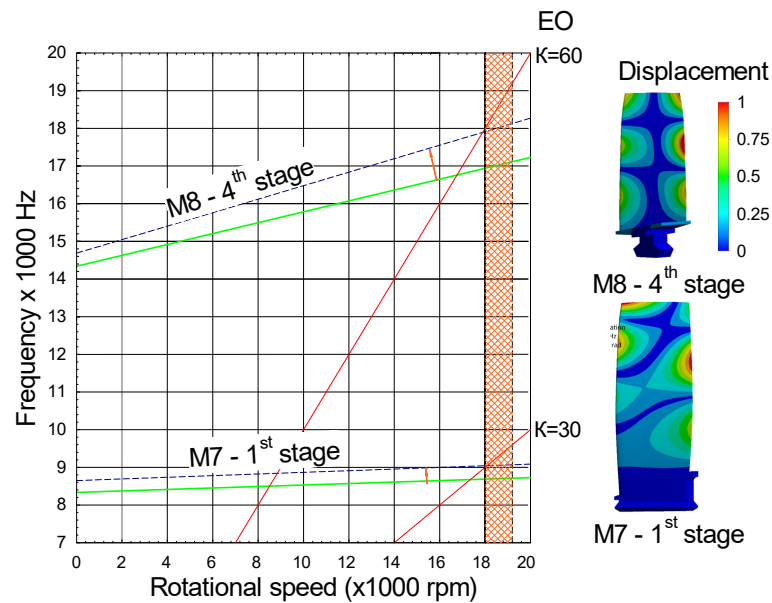


Figure 11. Impact of erosion on the Campbell diagram for critical modes and stages

212 Stages and the modes for which the risk of resonance is identified:

- 213 • M7 of the first stage resonates with the EO30 due to the number of the inlet guide vanes. This
- 214 resonance is possible at 4 mm chord wear in the upper part
- 215 • M8 of the fourth stage resonates with the EO60 due to the number of the guide vanes of this stage.
- 216 Resonance occurs when the chord wear equals 6.3 mm

217 3.3. Particle Separator

218 A particle separator cleans the air entering the engine from dust, sand, dry twigs, leaves and
 219 other foreign objects during taxiing, take-off and landing from unpaved runways or landing areas
 220 [38]. When IPS is turned on, with the engine running, hot air from the compressor enters the dust
 221 ejector nozzle. At the same time, due to centrifugal forces, part of the airflow entering the engine is
 222 pressed to the rear of the central fairing and enters the separator inlet. Most of the cleaned air passes
 223 through a separator to the engine inlet. Contaminated air, including foreign particles, passes into the
 224 dust exhaust pipe, in which a vacuum is created due to the operation of the ejector. Thus, particles are
 225 expelled into the atmosphere.

226 The results of modelling the speed and trajectory of foreign particles of various sizes flowing in
 227 the gas path showed that most of the particles are separated along the internal curved surface of the
 228 IPS under the action of centrifugal forces. However, experience from the operation of helicopters in a
 229 dusty environment shows that the use of this type of particle separator does not eliminate the problem
 230 of erosive wear of compressor aerofoils [37].

231 IPS is effective at separating large fractions of particles ranging in size from 50 to 100 μm , almost
 232 completely cleaning the air supplied to the engine compressor (Figure 12). If the particle size is
 233 relatively small - from 10 to 50 μm , about 20% of the particles enter the engine compressor bypassing
 234 the IPS separator under the influence of viscous forces following the flow. (Figure 13).

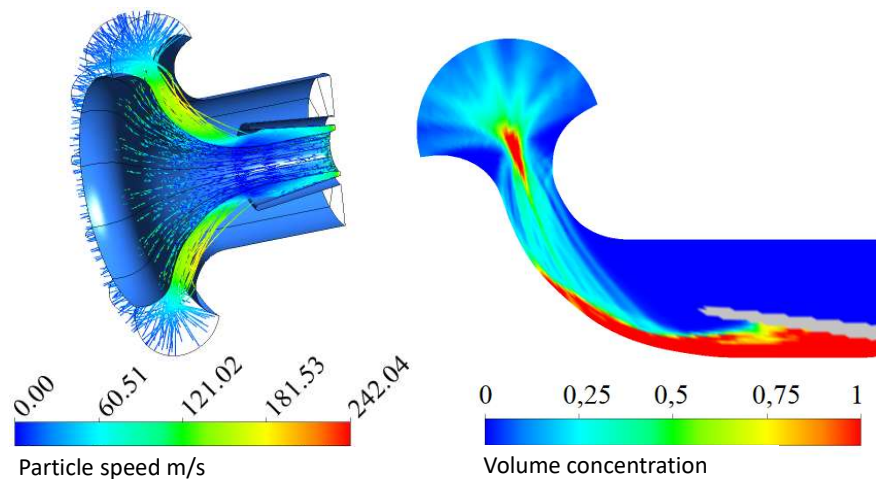


Figure 12. Velocity and concentration of large particles in the inlet of the turboshaft with IPS; particle size 50 - 100 μm

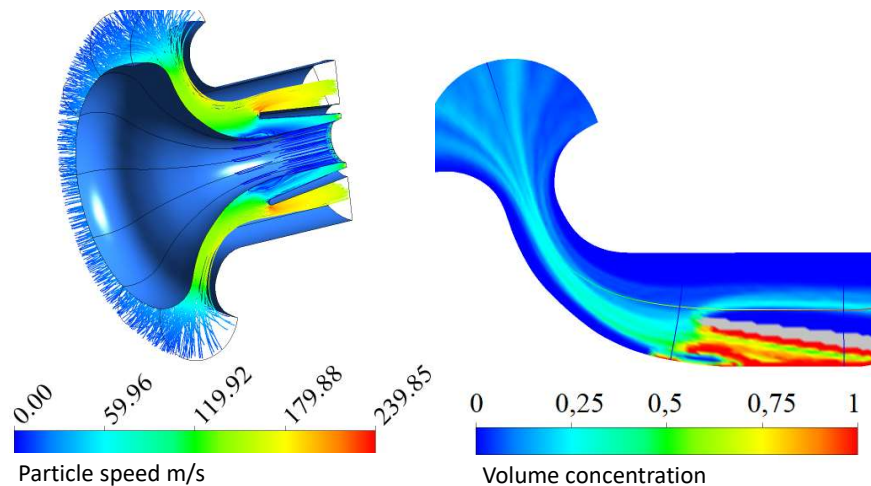


Figure 13. Velocity and concentration of small particles in the inlet of the turboshaft with IPS; particle size 10 - 50 μm

235 3.4. Stall margin analysis

236 To assess the effect of erosion on the compressor performance, the flow was calculated for the
 237 nominal (initial) geometry of the blades, as well as the geometry corresponding to the engine operating
 238 time of 200, 400, 600, and 800 FH [24].

Compressor pressure maps (Figure 14) and efficiency maps (Figure 15) calculated as a function of flight hours show that with increasing intensity of blade wear, the pressure ratio and its efficiency decreases. Consequently, the stall margin (SM) is also reduced (Figure 14). It was calculated using the following formula:

$$SM = 100\% \left(\frac{\pi_{stall} / \dot{m}_{stall}}{\pi_{ss} / \dot{m}_{ss}} - 1 \right) \quad (4)$$

239 where π_{stall} is the pressure ratio for the stall line, and π_{ss} is the pressure ratio for the steady state line.

240 A decrease in the stall margin of the compressor by 15% causes the appearance of a surge during
 241 test-cell testing of TV3-117 engines. The analysis of the mass flow in the high speed region for a
 242 compressor with blades with different degrees of wear showed that due to erosive wear in the upper
 243 parts of the blades of stages 6-9, the compressor develops a stall, leading to surge. The reason for this
 244 phenomenon was a decrease in the chord of the blades and an increase in the radial clearance. For that

245 reason, the compressor operated in a dusty environment reaches its serviceability limit after 730 - 750
 246 FH (Figure 16).

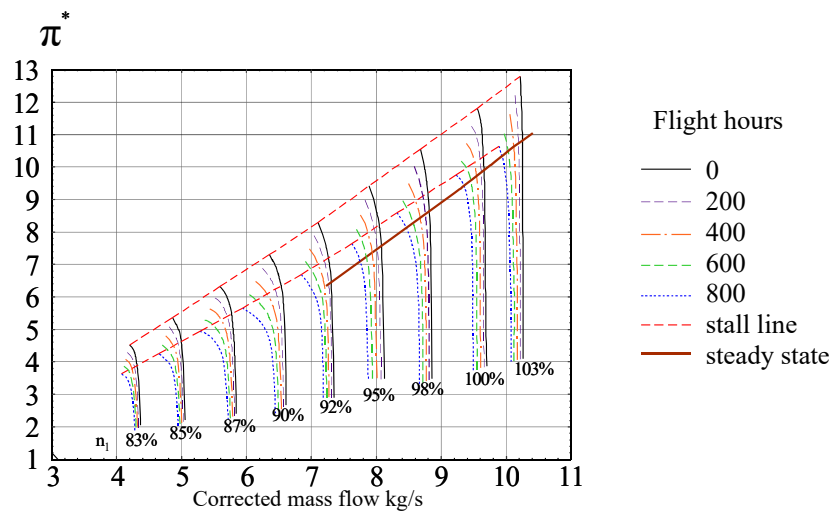


Figure 14. Dependence of the pressure compressor maps on the operating time in a dusty environment

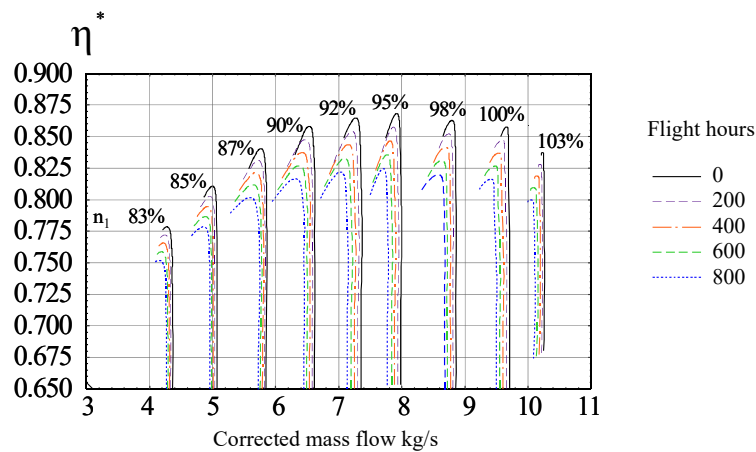


Figure 15. Compressor efficiency versus operating time in a dusty environment

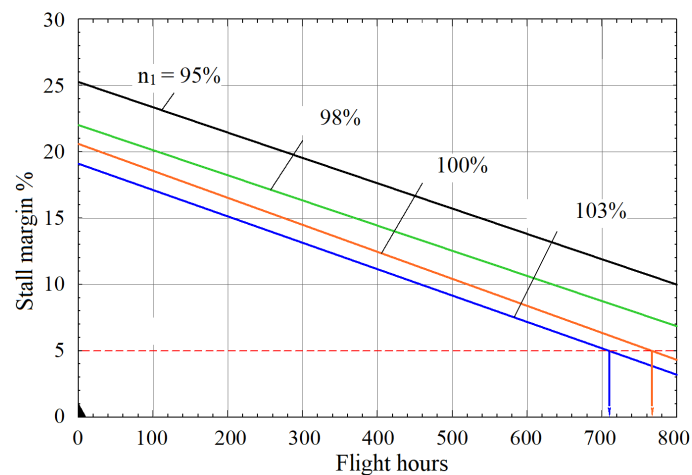


Figure 16. Stall margin of the compressor versus operating time in a dusty environment

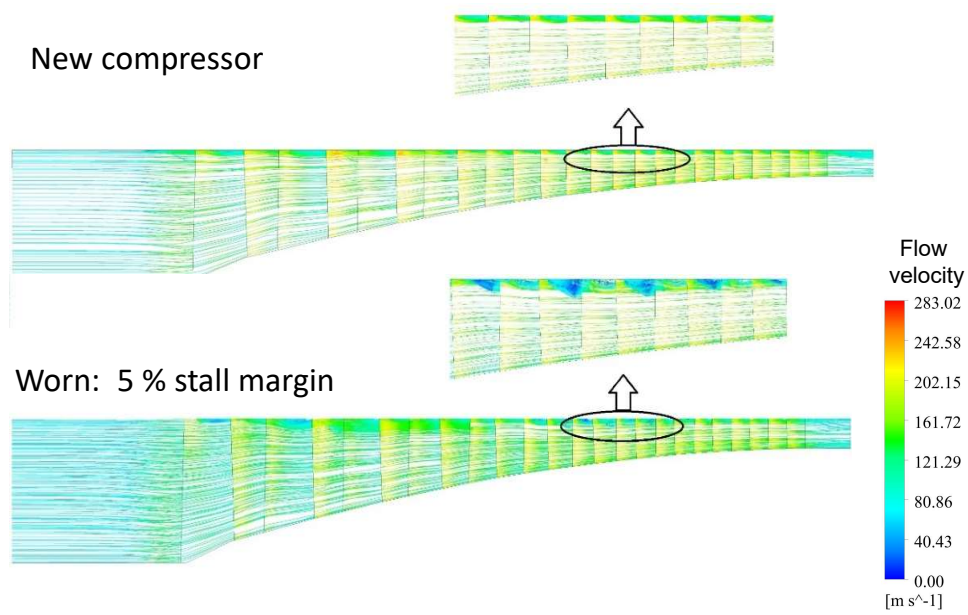


Figure 17. Flow velocity in the upper region of the flow part of the new and worn compressor

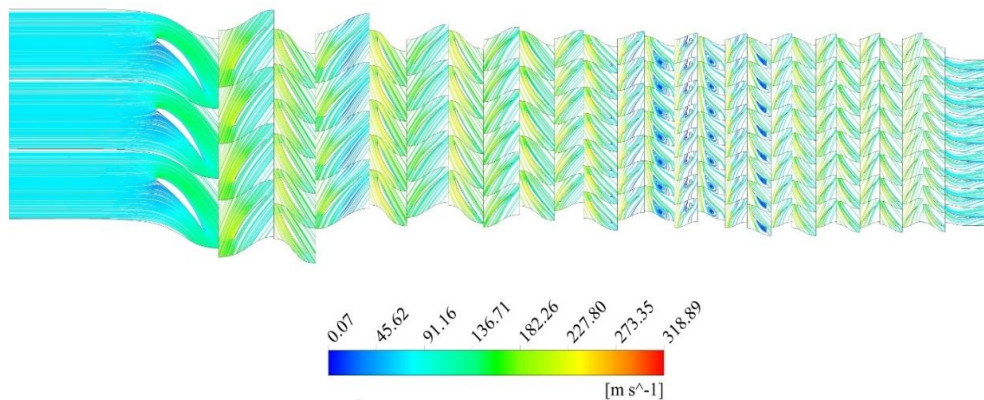


Figure 18. Flow velocity at 90% blade span

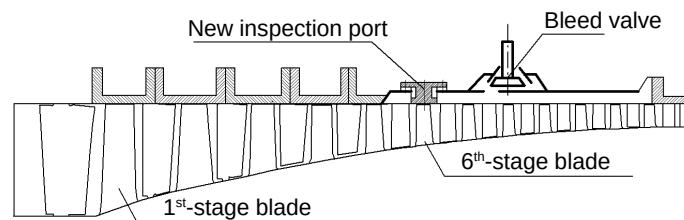


Figure 19. New slot designed to inspect the sixth stage

247 4. Conclusions

248 Based on the analysis of the geometry of the compressor blades of the TV3-117 engines operated
 249 in a dusty environment it was found that the wear of the blades of all the compressor stages occurs
 250 uniformly. When the particle separator is used, the largest wear is observed for the blades of stages 1-6.

251 It is also established that there is a close correlation between the wear of the blades of the sixth stage
252 and the stages 2-12.

253 An original method was developed to assess the influence of erosive wear of the blades and vanes
254 on the compressor performance by modelling three-dimensional flow for various degrees of wear on
255 the blades of all stages. The methodology for measuring the chord wear of the blades, calculating the
256 natural frequencies of vibration taking into account the aerofoil wear, numerical calculation of the
257 compressor flow and analysing the onset of stall, the use of which, in combination with established
258 patterns of chord wear over engine operating time allowed for the assessment of the serviceability
259 limits of the blades.

260 On the basis of a modal analysis of compressor blades with different operating times, the
261 dependency of blade vibration frequency on the chord wear for all the stages was established. It was
262 found that when the chord of the first-stage blades is worn more than 4 mm, the M7E030 resonance
263 can occur. Similarly, chord wear of the forth-stage blades higher than 5.1 mm causes M8E060 vibration.
264 The HCF risk for the remaining stages is negligible.

265 The values of the maximum permissible chord wear of the blades of all stages are determined by
266 the criterion of stall margin of the TV3-117 turboshaft. The chord wear of the sixth-stage blades equal
267 6.19 mm is critical because it is accompanied by a decrease in the stall margin of the compressor by
268 15-17% which indicates the appearance of a permanent stall at 770-790 FH. An additional slot for the
269 optical inspection of the sixth stage was designed to allow for field maintenance (Figure 19).

270 The standards applicable today determine the maximum chord wear of blade in its upper section
271 at the level of 2 mm, regardless of the use of particle separators. The criteria established in terms
272 of natural vibration frequency and the margin of stall margin allow for increasing the time between
273 overhauls (TBO) by 200 FH. The defined serviceability limits of the blades enable helicopter users
274 to significantly reduce operating costs by extending the RUL of the engines operated in a desert
275 environment.

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277 analysed the data; Y.D. and D.P. developed FEM and CFD models; D.P. and R. Przysowa verified and evaluated
278 the results. Y.D. and R.P. drew conclusions and produced the paper.

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284 execution, interpretation, or writing the study. The views, information, or opinions expressed herein are solely
285 those of the authors and do not necessarily represent the position of any organisation.

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