

Article

Towards a framework for Noctilucent Cloud Analysis

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Abstract: In this paper, we present a framework to study the spatial structure of noctilucent clouds formed by ice particles in the upper atmosphere at mid and high latitude during summer. We study noctilucent cloud activity in optical images taken from three different locations and under different atmospheric conditions. In order to identify and distinguish noctilucent cloud activity from other objects in the scene, we employ linear discriminant analysis (LDA) with feature vectors ranging from simple metrics to higher-order local autocorrelation (HLAC), and histogram of oriented gradients (HOG). Finally, we propose a Convolutional Neural Networks (CNN) based method for the detection of noctilucent clouds. The results clearly indicate that the CNN based approach outperforms LDA based methods used in this article. Furthermore, we outline suggestions for future research directions to establish a framework that can be used for synchronizing the optical observations from ground based camera systems with echoes measured with radar systems like EISCAT in order to obtain independent additional information on the ice clouds.

Keywords: noctilucent clouds; linear discriminant analysis; convolutional neural networks

1. Introduction

Noctilucent Clouds (NLC) that can be seen by naked eye and Polar Mesospheric Summer Echoes (PMSE) observed with radar, display the complex dynamics of the atmosphere at approximately 80 to 90 km height [1]. PMSE and NLC display wavy structures (as shown Figure 1) around the summer mesopause, a region that is highly dynamical with turbulent vortices and waves of scales from a few km to several thousand km. Analysis of these structures in the upper Earth atmosphere gives us information on the dynamics in this region.

Both the NLC and PMSE phenomena occur in the presence of ice particles. The topic of ice particles formation and its link to climate change is currently in debate in the atmospheric community and needs further investigation. Recent model results [2] suggest a significant increase in the NLC occurrence number and NLC brightness over the period 1960-2008 and its link to the increase of water vapor as a result of the increasing methane content in the mesosphere. At the same time, actual ground-based NLC observations show about zero or small, statistically insignificant trends in the NLC occurrence frequency and brightness for the past five decades [1, 3-7]. The time-series analyses of satellite observations in combination with model calculations indicate that the cloud frequencies are influenced by factors like stratospheric temperature, volcanic activity, solar cycle [8, 9]. In this context the comparison of NLC and PMSE will also improve the understanding of their formation process.

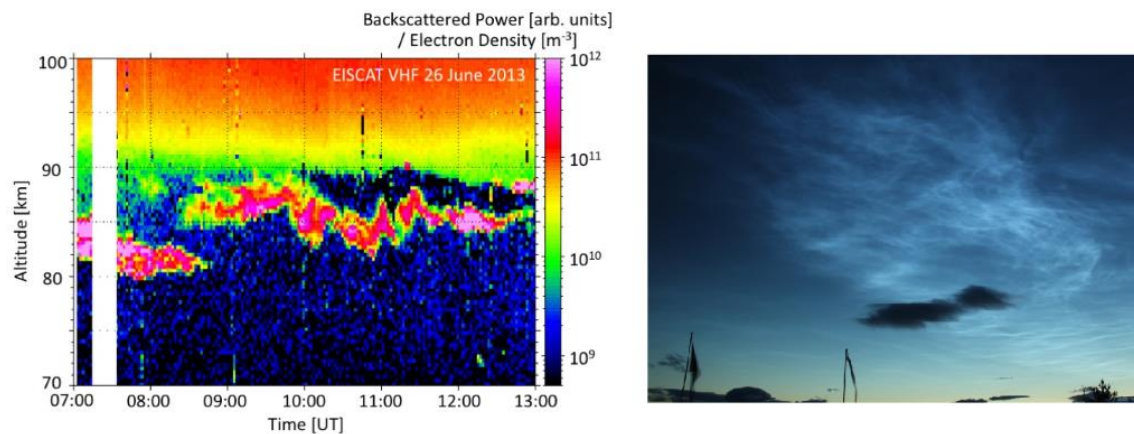


Figure 1: The PMSE Radar echoes associated with polar ice clouds on the left [10] and optical image of NLC on the right.

The morphological shape of the clouds indicates certain influence of wave propagations of various scales. Proper description and comparison of cloud structure is a step toward a detailed analysis of the role of atmospheric waves in the formation of PMSE and NLC. Both PMSE and NLC are observed during summer for several months, hence, large data sets are available for statistical analysis of the structures. A series of observations were made to collect optical images and radar data in common or overlapping volumes of the summer mesopause. So far only a few of the common volume observations were successful. In order to do a detailed analysis of the morphological shapes, advanced methods are required.

As a first step towards an integrated statistical analysis, we propose a framework for the analysis of NLC observation. The paper is organized as follows: in section 2, we discuss the theory behind the Polar Mesospheric Summer Echoes and Noctilucent Clouds, and outline our proposed framework for analysis of NLC and PMSE. Next, in Section 3, we discuss the methodology behind the analysis of noctilucent clouds, the dataset, procedure used, and the methods employed for the analysis. In Section 4, we discuss the results obtained from the comparison of different methods used in this paper. Finally, in the Section 5, we briefly discuss the results and outline strategies for future research directions.

2. Theory and Motivation

In this section, we discuss the theory behind NLC and PMSE and outline the proposed framework for their analysis.

2.1 Noctilucent Clouds and Polar Mesospheric Summer Echoes

The mesopause is the upper boundary of the mesosphere, the region of the atmosphere that is characterized by decreasing temperature with increasing altitude. The atmospheric temperature has its minimum at the mesopause and then increases with height again in the thermosphere lying above. The mesosphere and lower thermosphere are strongly influenced by atmospheric waves that couple the region to lower and higher layers. The waves determine the dynamical and thermal state of the atmosphere. They connect atmospheric regions from the ground to the lower thermosphere (0-130 km) and determine general atmospheric circulation by transferring their energy and momentum flux to the mean flow. The pronounced example of action of gravity waves (GWs) is the formation of the extremely cold polar summer mesopause (80-90 km) where the temperatures fall to the lowest values of the entire terrestrial atmosphere. Generated normally in the troposphere, gravity waves on the way up experience filtering (absorption) by zonal wind in the mesosphere [11]. The rest propagates further and grow in amplitude as atmospheric density exponentially decreases. The waves with large amplitudes break at the mesospheric altitudes or higher up and exert drag on the mean flow. This gives rise to a meridional flow from the summer to winter mesosphere. As a result, global circulation from the winter to the summer poles moves air masses downward at the winter the pole and upward

at the summer pole. Hence, adiabatic cooling lowers the mesopause temperature in summer at the mid and high latitudes [12]. There is also a strong influence of planetary waves on global scales as well as of turbulent eddies of a few meters. This dynamical forcing drives the polar summer mesosphere to around 60 degrees below radiative equilibrium temperatures. The temperature drops below the frost temperature and clouds of ice particles, Polar Mesospheric Clouds (PMC) form at heights 80 to 85 km [9]. Some of the PMC are visible to the eye after sunset when the atmosphere below is not illuminated by the Sun, those are the NLC. At similar, overlapping altitudes the PMSE are observed [13]. NLC form by light scattering at water ice particles. PMSE are influenced by neutral atmospheric dynamics, turbulence and dusty plasma effects, and their exact formation conditions are still subject to investigations [14].

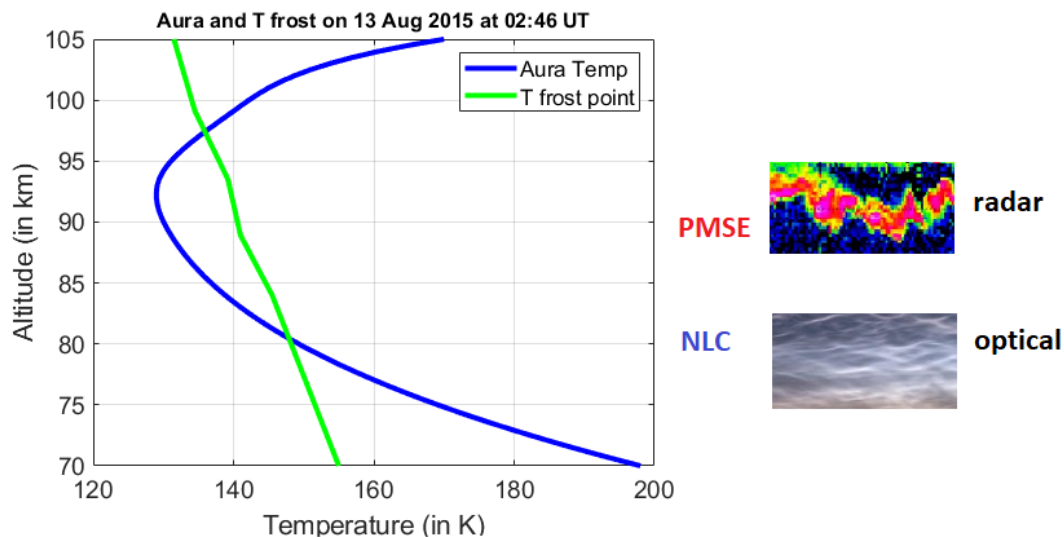


Figure 2: shows the temperature profiles (blue line) as measured by the Aura satellite [15] and frost point temperature profiles (green line) estimated using the Aura water vapor data [16]. The height ranges in which the temperature is lower than the frost point temperature indicate the regions of formation and existence of ice particles around the summer mesopause. These profiles were obtained on a day when both, PMSE and NLC were observed.

The conditions when wave dynamics cools the air down to 130 K and less so that small water-ice particles form prevail during the summer months and at high and mid latitude. PMSE ice particles are smaller in size (5-30 nm) and lighter compared to heavier NLC particles of 30-100 nm [17]. That is why a PMSE layer usually resides above an NLC layer. Ground-based optical imagers and lidars can detect an NLC layer due to Mie scattering of sunlight on larger ice particles while VHF and UHF radars can detect a PMSE layer by means of radio waves scattering from fluctuations in electron density (at half radar wavelength) that move with a neutral wind, which, in turn, can be modulated by waves. A future detailed comparison of both phenomena would provide valuable information both on the atmospheric structure and on the formation of the ice particles. It should be noted, that NLC describe the variation of the atmospheric layer on spatial horizontal scales, while PMSE observations describe the radar echoes at a given location and their time variation which further complicates the analysis. Using high-power, large-aperture radar for the PMSE observations has the advantage that those radar also measure incoherent scatter in the vicinity of the PMSE and thus provide information on the ionospheric and dusty plasma conditions [18].

2.2 Proposed Framework

EISCAT_3D is an international research infrastructure for collecting radar observations and using incoherent scatter technique for studying the atmosphere and near-Earth space environment [19]. The EISCAT_3D infrastructure is currently under development and will comprise of five phased-array antenna fields located in different locations across Finland, Norway and Sweden, each

with around 10000 dipole antenna elements [19]. One of these locations will be used to transmit radio waves at 233 MHz, and all five locations will have receivers to measure the returned radio signals [19]. As radio waves accelerate or heat electrons and ions in the upper-atmosphere, the interactions of electromagnetic waves with the atmosphere, ionosphere, and magnetosphere can be used to understand the properties of the near-Earth space environment and fundamental properties associated with plasma turbulence [20].

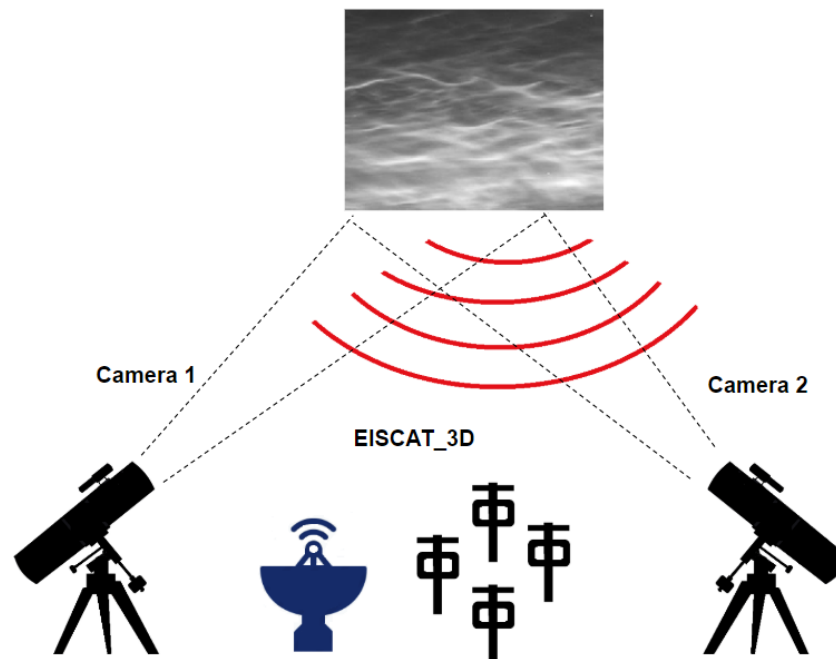


Figure 3: Framework for the analysis

In the proposed framework as shown in Figure 3, the main idea is to use cameras to detect noctilucent cloud activity in the atmosphere and use the associated time stamps to synchronize the optical observations with that of radar data obtained by using EISCAT_3D. By synchronizing the radar data with optical images we can get a detailed understanding of the conditions leading to the formation of noctilucent clouds, and their propagation and dynamics in 3D space.

As an example, it is possible to carry out summer observations campaigns to study PMSE and NLC activity in the common volume of the atmosphere above the Tromsø EISCAT station. As EISCAT_3D radars are operating at Tromsø, two optical automated cameras, located at Kiruna (Sweden) and Nikkaluokta (Sweden), can register potential occurrence of NLCs above the radar site. Both locations of the NLC cameras are about 200 km south of Tromsø, which permits making NLC triangulation measurements and hence estimating NLC height and dynamics in 3D space. After that, the observations pertaining to PMSE layers can be compared to those of the NLC to estimate characteristics of the gravity waves.

3. Methodology

In this section, we specify the dataset used for our experiments, discuss the procedure used for the analysis of the dataset and elaborate on the different methods used for the analysis.

3.1. Dataset

The dataset comprises of images captured from three different locations: Kiruna, Sweden (67.84°N, 20.41°E), Nikkaluokta, Sweden (67.85°N, 19.01°E), and Moscow, Russia (56.02°N, 37.48°E), during NLC activity. The images reflect the different conditions: low contrast or faint NLC activity, strong NLC activity, tropospheric clouds, and a combination of these conditions.

3.2 Procedure

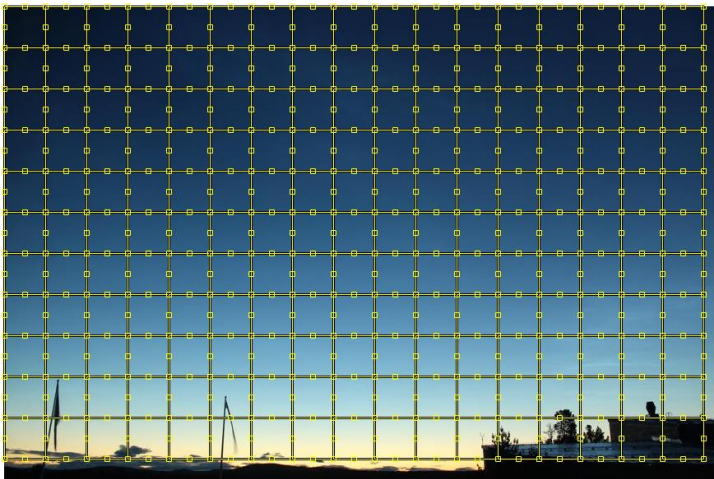


Figure 4: Resized image divided into blocks of size N-by-N pixels.

First, an input image (typically of size 3456 by 2304 pixels) is resized to one-quarter of the original size. Downsampling an image helps to reduce the computational complexity of analysis.

Second, as NLC activity is spatially localized in a given image, the resized image is divided into image blocks of size N-by-N pixels each as shown in Figure 1, for our experiments we used N=50 pixels. Image regions along the right and the bottom edges of the images are quite small in size and hence not considered.

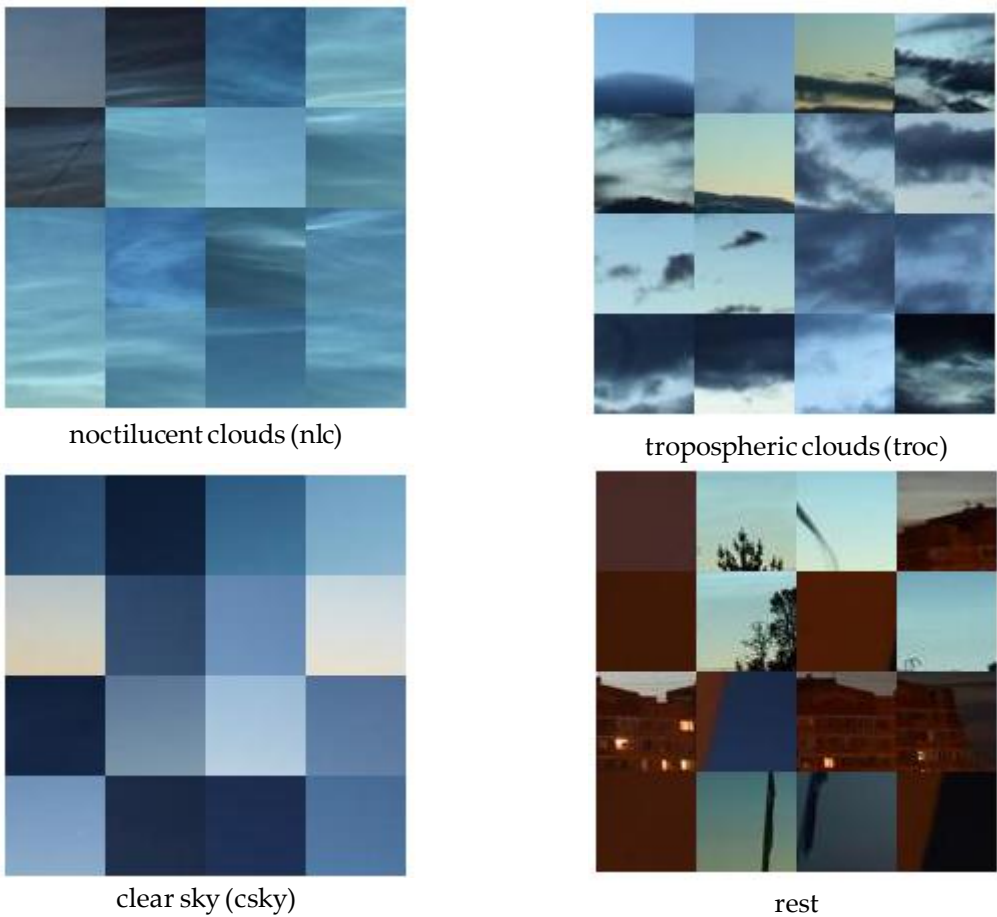


Figure 5: Samples randomly selected from the four categories.

Third, image blocks from the whole dataset are divided into four different categories namely, noctilucent clouds, tropospheric clouds, clear sky, and rest that includes all objects that appear in the

background of an image. 6000 samples for each category are randomly selected from the dataset. The labelling of image blocks is done manually. 60 percent of the total number of samples are used for training, 20 percent are used for testing the performance of the different methods, and in case of CNN, rest 20 percent are used for validation.

3.3 Methods

3.3.1 Linear Discriminant Analysis

In literature Linear Discriminant Analysis (LDA) is also known as Fischer Discriminant Analysis. For two different classes with means μ_1, μ_2 and covariances Σ_1, Σ_2 , the Fischer linear discriminant is defined as a vector w which maximizes [21]:

$$J(w) = \frac{w^T S_B w}{w^T S_W w},$$

where

$$S_B = (\mu_1 - \mu_2)(\mu_1 - \mu_2)^T, \\ S_W = (\Sigma_1 + \Sigma_2),$$

are the between and within class scatter matrices. Here, the main idea is to reduce the dimensions by projecting the data along a vector w that preserves as much of the class discriminatory information as possible. This is achieved by estimating an optimal line w that maximizes the class means (numerator) and minimizes the class variances (denominator). LDA can be also extended to construct a discriminant function for problems with more than two classes. For details, please see [22].

3.3.2 Feature vectors for LDA

For LDA, we employed a range of feature vectors with simple features such as: mean (μ), standard deviation (σ), max and min, and more complex feature vectors such as: higher order local autocorrelation and histogram of oriented gradients.

Higher-order local autocorrelation (HLAC) is feature descriptor proposed by Otsu [23] that can be used for image recognition. In a recent study by [24], it has been used for object detection in satellite images. HLAC features are calculated by adding the product of intensity of a reference point $r = (x, y)$ and local displacement vectors $a = (\Delta x, \Delta y)$ within local neighbors [24]. Higher order autocorrelation is defined by

$$X_N(a_1, \dots, a_N) = \sum f(r)f(r + a_1) \dots f(r + a_N),$$

Where $f(r)$ represents the intensity level at location r of the image. An increase in the order N also increase the number of autocorrelation functions to be computed, therefore, to enable practical use N is restricted to second order ($N = 0, 1, 2$) and the range of displacements is restricted to 3 by 3 with its center as the reference. 35 displacement masks as shown in Figure 6, are convolved with the image and resulting values pertaining to each pattern are accumulated. In each mask, the values represent the reference locations used in multiplying with the image intensities and * represents don't care locations [24]. In this manner, a set of 35-dimensional HLAC vectors are generated from an intensity image at a given resolution. HLAC feature extraction is also performed for lower resolutions. For our calculations, we used only one resolution of the 50 by 50 pixels image block and three color channels resulting in a feature vector of size 105.

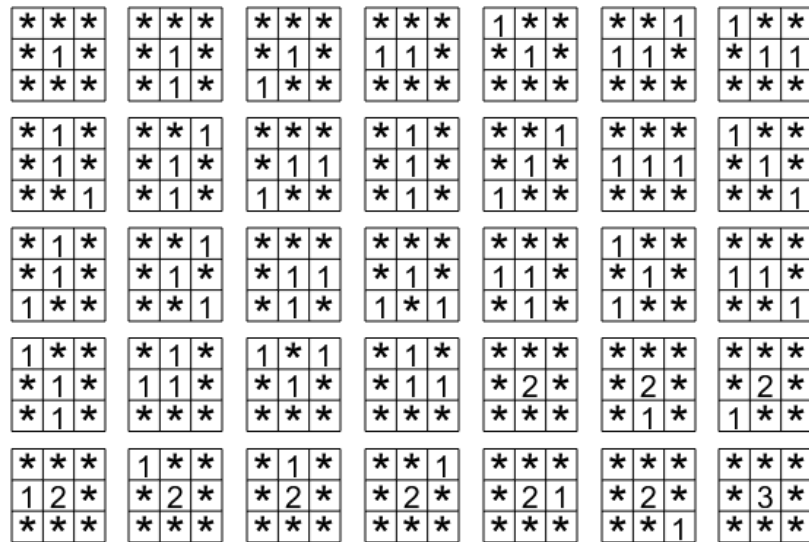


Figure 6: 35 displacement masks used for calculating HLAC feature descriptor. In each mask, the values represent the reference locations used in multiplying with the image intensities and * represents don't care locations [24].

Histogram of oriented gradients (HOG) is a feature descriptor used for object detection. The main idea behind HOG is that an object's appearance and shape can be represented by the distribution of intensity gradients or edge directions [25]. HOG is invariant to local geometric and photometric transformations [25]. In the implementation of HOG [25], first, a given image is divided into small spatial regions called cells and their gradient values are calculated. Second, for each cell a histogram of gradient directions or edge orientations is computed. In order to account for illumination and contrast changes, the gradient values are normalized over larger spatially connected cell regions called blocks. Finally, the HOG descriptor is obtained by concatenating the components of the normalized cell histograms from all of the block regions. For our calculations, we used a cell size of 8 by 8 pixels across three RGB color channels for each input image block, resulting in a feature vector of size 2700.

3.3.3 Convolutional Neural Network

Convolutional neural network (CNN) is a class of deep neural networks commonly used for image analysis. As compared to traditional neural networks, a CNN is both computationally and statistically efficient. In part, this is due to small kernel sizes used for extracting meaningful features, which leads to fewer connections and fewer parameters to be stored in the memory [26].

A convolutional neural network comprises of an input layer, followed by multiple hidden layers and finally an output layer. Each hidden layer usually consists of three stages [26], in the first stage a convolutional layer produces a set of linear activations. In the second stage, these linear activations then run through a nonlinear function such as rectified linear unit function (RELU). In the third stage, a pooling function is used to modify the output, for instance, max pooling (MaxPool) operation selects the maximum output from the local neighborhood.

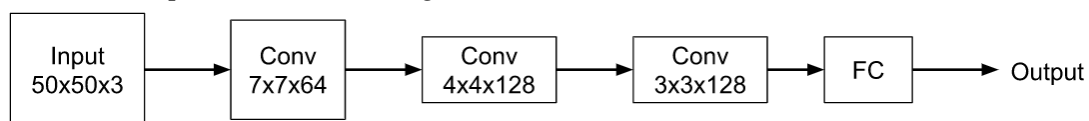


Figure 7: The proposed CNN algorithm.

In the proposed CNN algorithm, the first layer allows inputs of size 50x50x3 pixels. It is followed by a three convolutional layers of size 7x7x64, 4x4x128, and 3x3x128 respectively, where the size and the number of channels for the three layers were chosen based on the performance. For details, please

see Appendix A. Each convolutional layer is followed by a batch normalization, RELU, and MaxPool layer respectively. The fully connected layer is followed by a softmax layer which enables the outputs of the layer to be interpreted as probabilities and assigning a relevant class label.

4. Results

In this section, we compare the results obtained by using LDA for different feature vectors and the proposed CNN method. In the end, we visualize the performance of the CNN algorithm for a few test images.

4.1 Comparison of different methods

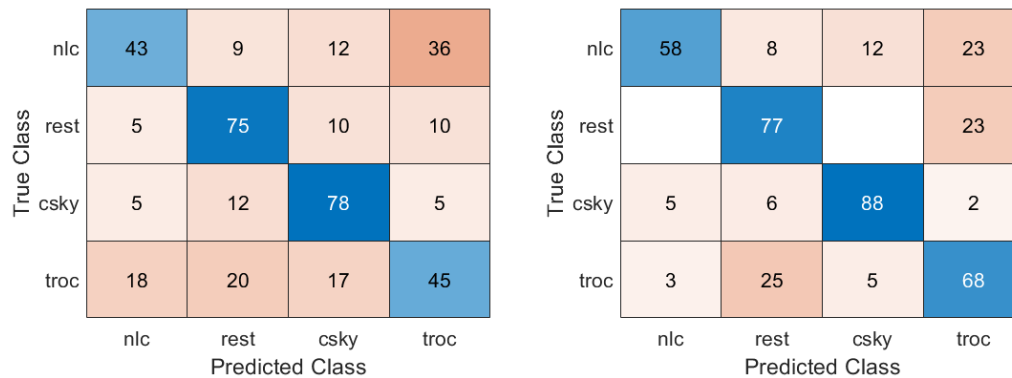


Figure 8: Confusion matrices for the four categories when using mean only (on the left) and using mean and standard deviation (on the right).

The average accuracy for the case when we use only the mean value of the image blocks for LDA is 60.19 percent. Here we define accuracy as the percentage of correct number of classifications to the total number of classifications across the four different categories. Figure 8 (left) shows the percentage of correct classifications associated with the four classes in the form of a confusion matrix. We can see that for the categories: rest and clear sky, the performances are moderate with correct classifications percentages to be 75 and 78 respectively. On the other hand, the categories: nlc and tropospheric clouds the performances are poor with correct classification percentages to be 43 and 45. When using mean and standard deviation values for LDA the average performance is improved to 72.6 percent, please see Figure 8 (right). This is also visible in the four categories in Figure 1, where the number of correct classifications improve across all four categories. However, still a significant percentage of tropospheric clouds are misclassified as rest and vice-versa, and nearly 23 percent of noctilucent clouds are misclassified as tropospheric clouds.

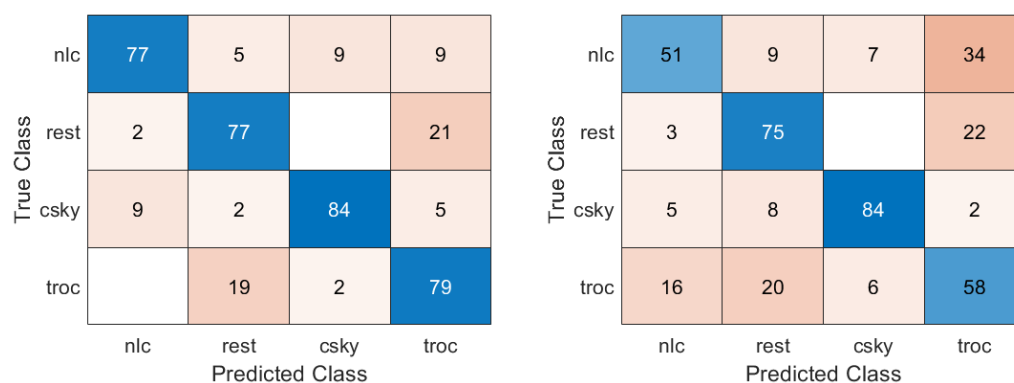


Figure 9: Confusion matrices for the four categories when using mean, standard deviation, min and max values (on the left) and using HLAC (on the right).

When using mean, standard deviation, minimum and maximum values of the image regions, we observe that the performance of the discrimination across the four categories improves to 79.21 percent, please see Figure 9 (left). Using HLAC as a metric for LDA decreases the average performance across the four categories to 67.08 percent. As shown in Figure 9 (right), this is especially visible in the observed prediction rates of 51 and 58 for the noctilucent and tropospheric cloud classes respectively, which are affected the most.

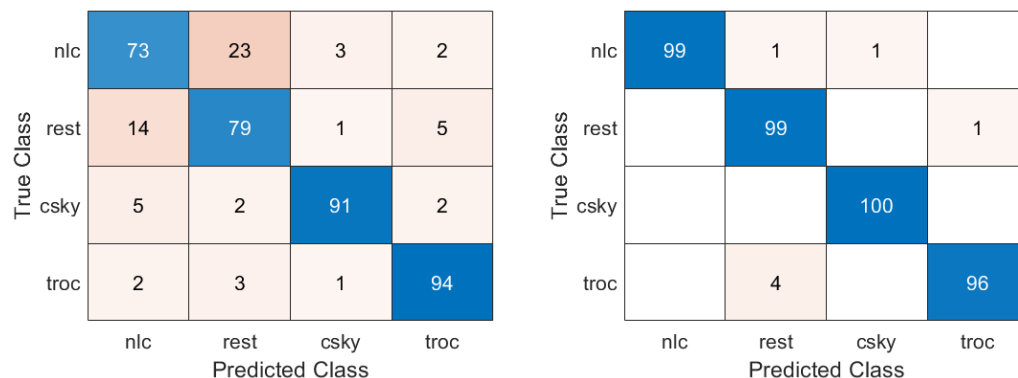


Figure 10: Confusion matrices for the four categories using HOG (on the left) and when using the proposed CNN based approach (on the right).

The classification scores for the four categories using HOG for LDA improve the performance to 84.27 percent. As shown in Figure 10 (left), the prediction rates for clear sky and tropospheric clouds improve to 91 and 94 percent respectively, however, still a significant 23 percent of noctilucent clouds and misclassified as rest. Finally, as shown in Figure 10 (right) the results obtained from the proposed CNN based approach indicates good classification scores across all four categories with approx. 99 percent for noctilucent, 99 percent for rest, 100 percent for clear sky and 96 percent for tropospheric clouds.

A summary of average classification scores for the LDA method with different metrics and CNN is shown in Table 1. We can clearly see that the CNN method with a score of 98.27 percent clearly outperforms the LDA based approaches.

Table 1: Average classification scores for LDA with different metrics and CNN

Method	Average Classification Score (in percent)
LDA using mean	60.19
LDA using mean and standard deviation	72.6
LDA using mean, standard deviation, min and max values	79.21
LDA using HLAC	67.08
LDA using HOG	84.27
CNN	98.27

For visualization of the performance of the proposed CNN algorithm, we select 5 images from the three different datasets for which the CNN algorithm was not trained. As shown in Figure 11, we can see that a majority of the noctilucent cloud activity is correctly detected by the proposed CNN algorithm. There are a few false detections in the lower left part of the image where tropospheric clouds and clear sky are predicted as noctilucent clouds. Next in Figure 12, we can observe that a majority of the noctilucent activity including faint or low contrast noctilucent clouds are correctly predicted by the algorithm. After that in Figure 13, we can see that very faint or low contrast activity is correctly predicted by the algorithm. Furthermore, the regions belonging to the categories such as clear sky and rest are correctly detected. In Figure 14, we can observe a challenging scenario where noctilucent cloud activity is happening in the presence of large number of tropospheric clouds. We

can see that while noctilucent cloud activity is correctly predicted, a number of tropospheric clouds regions are incorrectly classified as noctilucent clouds. Finally, in Figure 15, we present a challenging scenario which does not have any noctilucent cloud activity, here we can see that the tropospheric clouds are incorrectly predicted as noctilucent clouds. To address the issue of misclassification, we outline a few suggestions in the next section.

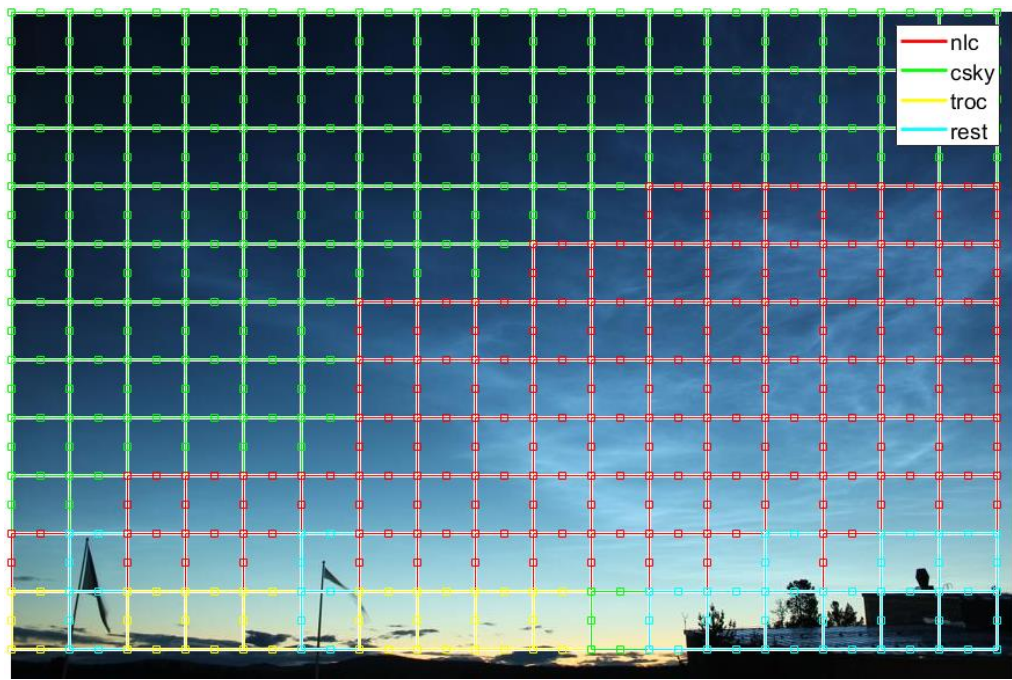


Figure 11: Majority of the noctilucent cloud activity is correctly predicted by the CNN algorithm.

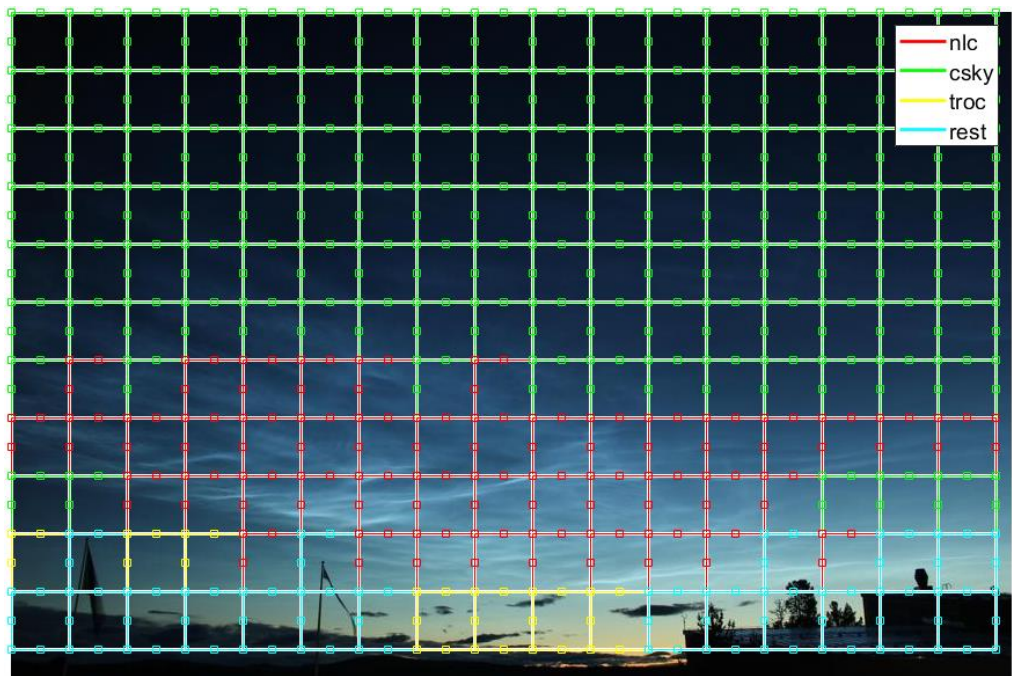


Figure 12: Majority of the noctilucent cloud activity is correctly predicted by the CNN algorithm.

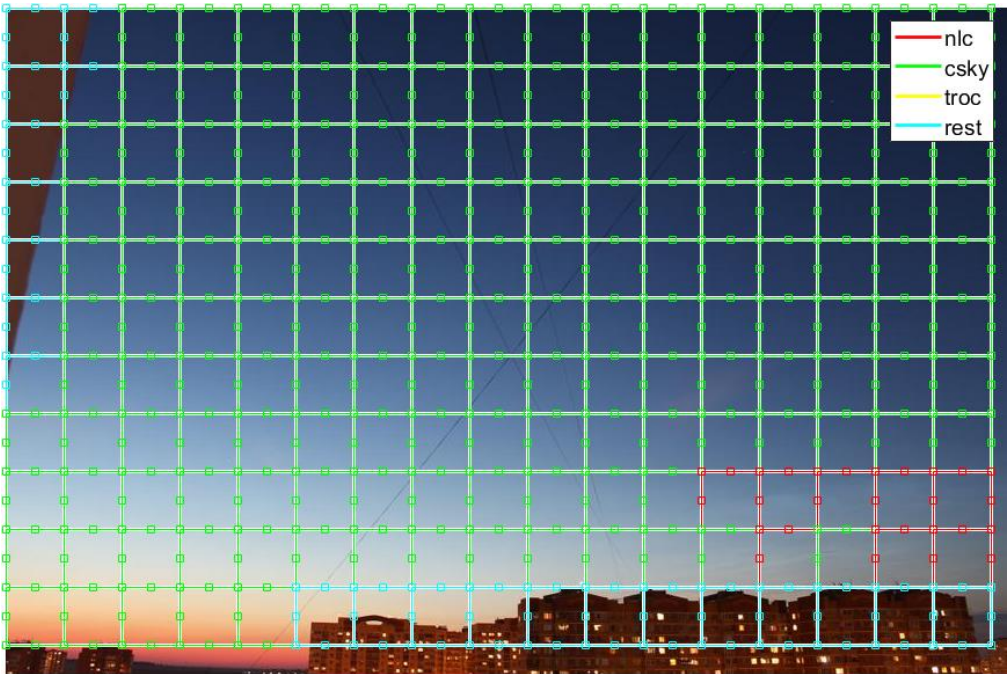


Figure 13: Very faint or low contrast noctilucent activity by the CNN algorithm.

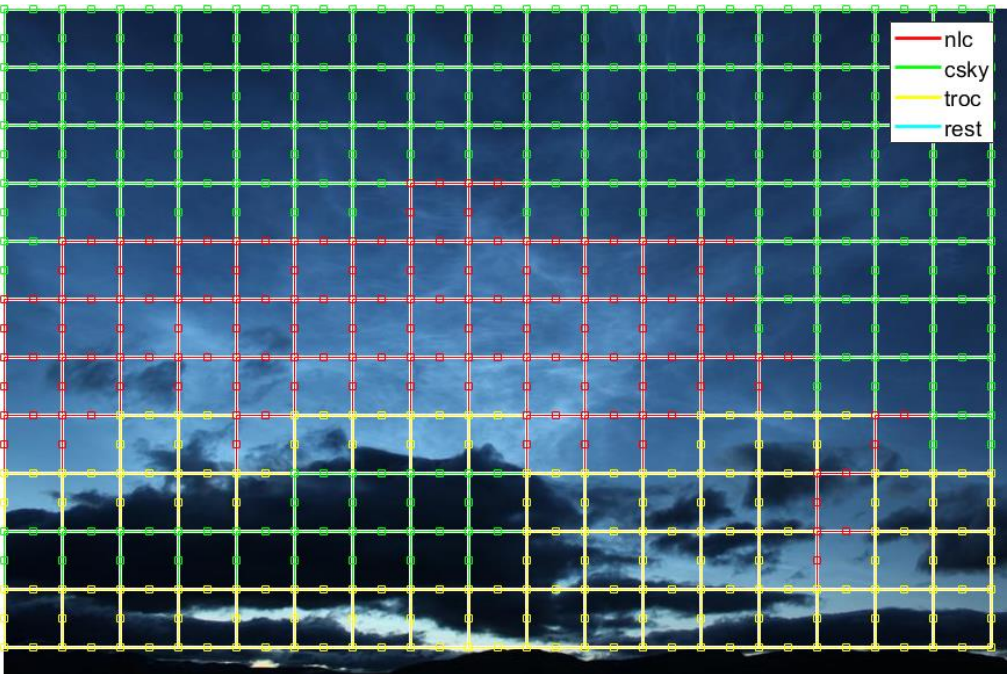


Figure 14: Noctilucent activity along with tropospheric clouds by the CNN algorithm.

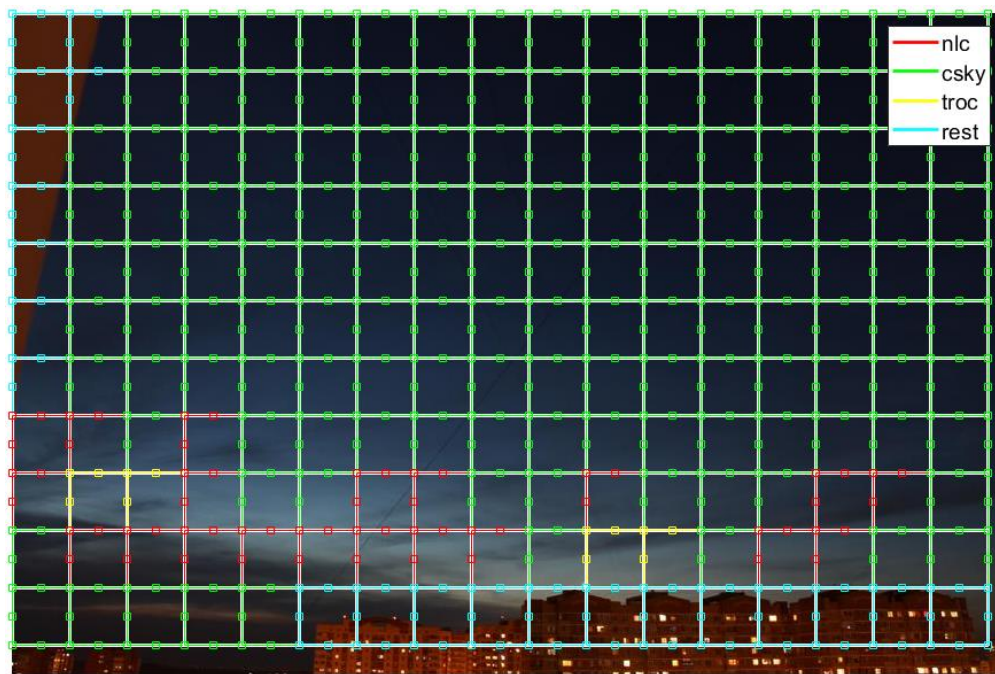


Figure 15: An example of false positive detections by the CNN algorithm.

5. Discussion

In order to investigate if noctilucent clouds can be identified from tropospheric clouds, clear sky, and rest of the objects, first, we employ LDA. For LDA, feature vectors with simple features such as: mean, standard deviation, max and min, and more complex feature vectors such as: HLAC and HOG are used. The results from LDA show that first, LDA using mean, standard deviation, max and min values as feature vectors performs better than LDA approaches using mean only, LDA using mean and standard deviation, and LDA using HLAC. Second, LDA using HOG as feature vectors outperforms all other LDA based approaches. This implies that HOG descriptor is relatively good at capturing the features associated with noctilucent clouds that enable their discrimination from other classes. Third, as the average classification score for LDA using HOG is 84.27 percent, it is clear that other approaches can be used to further improve the performance of classification. For this, we propose a CNN based method with three convolutional layers. Our results indicate that the performance of CNN based approach exceeds that of the LDA based approaches used in this paper. Four, a visual evaluation of the CNN algorithm for challenging cases pertaining to untested images indicates misclassifications for NLC activity.

In order to reduce the number of misclassifications associated with noctilucent cloud activity a number of possible approaches can be used: first, noctilucent clouds propagate in the mesosphere, which means that there is a temporal component linked to their start and end sequence in a scene. By employing recurrent neural network, we can include the time component of the activity, thereby, leading to possible improvement in their prediction. As the proposed CNN algorithm would enable us to collect more data associated with noctilucent cloud activity, including the temporal component of the image sequence would be possible in future studies.

Second, to overcome the drawbacks of region based approaches where each pixel in the region is assigned the label of the object or class in the region, a fully convolutional neural network [27] can be employed to train and predict all the pixels associated with a scene. Fully convolutional neural networks have shown significant improvements in the state of the art pertaining to image segmentation [27]. This approach requires a significant amount of fully labeled image data which can be mitigated by using semi-supervised learning approaches [28]. This is something that we plan to address in the future.

6. Conclusions and future work

In this paper, we outline a framework to study noctilucent cloud activity for an image dataset associated with three different locations and different atmospheric conditions. For the analysis, we employ two methods: linear discriminant analysis (LDA) with feature vectors (ranging from simple metrics to HLAC, and HOG), and Convolutional Neural Networks (CNN). Our results imply that the CNN based approach outperforms LDA based methods used in this paper. As a future research direction, this work can form the basis for synchronizing the optical observations from ground based camera system with radar echoes from EISCAT_3D incoherent scatter radar system. While present radar observations provide limited information of the motion of the ice clouds [10], this will be significantly improved with the new volumetric radar system EISCAT_3D [29].

Author Contributions: Sharma, Dalin, and Mann contributed towards the conceptualization and methodology of the problem. Dalin provided the image data for the analysis. Sharma performed the investigation and proposed the methods used in the paper. Sharma, Dalin, and Mann contributed towards the writing, editing, and review.

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Conflicts of Interest: The authors declare no conflict of interest

Appendix A

Different combinations of the size and number of channels for the three convolutional layers (shown in Table 1) were tested. For the first convolutional layer, sizes in the range [3, 10] and number of channels (16, 32, and 64) were tested. For the second convolutional layer, sizes in the range [3, 5] and number of channels (32, 64, and 128) were tried. For the third, convolutional layer was fixed to a size of 3 and number of channels (16, 32, 64, 128, and 256) were tested. The set of three convolutional layers that gave the best correct predictions is shown in Table 2.

Table 2: CNN algorithm layers

Input layer 50x50x3
Conv 7x7x64
BatchNorm
RELU
MaxPool 2x2
Conv 4x4x128
BatchNorm
RELU
MaxPool 2x2
Conv 3x3x128
BatchNorm
RELU
MaxPool 2x2
fullyConnected
Softmax
Classification

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