Correlation of Elastic Moduli and Serpentine Content in Ultramafic Rocks

Aida Farough 1*, Alexander Karrasch 1

1 Department of Geology, Kansas State University, Manhattan, KS

* Correspondence: afarough@ksu.edu

Abstract: Understanding the physical properties of ultramafic rocks is important for evaluating a wide variety of petrologic models of the oceanic lithosphere, particularly upper mantle and lower crust. Hydration of oceanic peridotites results in increasing serpentine content, which affects lithospheric physical properties and the global bio/geochemical cycles of various elements. In understanding tectonic, magmatic and metamorphic history of the oceanic crust, interpreting seismic velocities, rock composition and elastic moduli are of fundamental importance.

In this study we show that as serpentine content increases, density decreases linearly with a slope of 7.85. We also correlate increase in serpentine content with a linear decline in shear, bulk and Young’s moduli with slopes of 0.48, 0.77, 0.45 respectively. Our results show that increase in serpentine content of lower crust and forearc mantle could decrease elasticity of lithosphere and result in break-offs. Therefore tectonic processes at peridotite rich slow spreading ridges may be strongly affected by serpentine content, particularly serpentinization may be responsible for discontinuities in thin crust, and formation of weak fault zones.

Keywords: serpentinization; elastic moduli; density; ultramafic rocks; oceanic lithosphere

1. Introduction

Understanding the physical properties of ultramafic rocks (peridotites) is important for evaluating the wide variety of petrologic models for the Earth’s upper mantle and lower oceanic crust [1]. These properties have a key role in fluid flux and geochemical transport in magmatic system at mid oceanic ridges [e.g. 2-4] and subduction zones [e.g.5-6], as well as in enhanced geothermal systems [e.g. 7-8]. Mass, heat and chemical transport in fault zones plays a significant role in global seismicity [e.g. 9-10].

Hydration and alteration of oceanic peridotites results in increasing serpentine content and formation of serpentinites, which affects lithospheric physical properties [e.g.11-14] and the global bio/geo chemical cycles of various elements [e.g. 15-17].

In interpreting structure and seismic velocities of a region, a property of fundamental importance in understanding tectonic history is rock composition. Velocities of compressional and shear waves in ultramafic rocks decrease with increasing serpentine content [e.g. 18]. Various studies have reported seismic velocity measurements of dunites, partially serpentinized peridotites and serpentinites under pressure [e.g. 13, 19-25]. Falcon-Suarez et al., [26] analyzed seismic velocities, electrical resistivity and permeability of four serpentinized peridotite samples from the southern wall of the Atlantis Massif, Mid-Atlantic Ridge, collected during International Ocean
Discovery Program (IODP) Expedition 357. Horen et al., [27] analyzed the effect of serpentine content on seismic velocity of 6 samples from Xigaze Ophiolite and developed empirical correlations between the noted parameters, which we will use in this study to estimate seismic velocities. Ramana and Rao [28] reports density, porosity and seismic velocity of fresh (12%) to extensively altered ultramafic rocks (100%) from India.

Elastic moduli are also important in evaluating stiffness and understanding the tectonic, magmatic and metamorphic history of the oceanic crust. Evaluation of elastic moduli of oceanic rocks can be beneficial for future drilling strategies [13]. mineralogical composition, the porosity and the texture of the rocks are some of the parameter that affect elastic moduli [26, 28].

In this paper we report density, porosity and serpentine content of 8 samples of slightly to extensively serpentinized rocks and develop a linear correlation between density and serpentine content. We also use the empirical equation of Horen et al., [27], to estimate seismic velocities of the samples used in this study and develop correlation between elastic moduli and serpentine content. We produce a series of linear functions that correlate serpentine content with elastic moduli. These models can be used in understanding tectonic evolution of oceanic crust and estimating crustal weakening as a result of serpentinization.

Although the elastic thickness of the oceanic lithosphere, is estimated in the range of 2-50 km [29], serpentinization of lower crust and upper mantle can result in reduction of elasticity and weakening at much shallower depths, depending on fluid access. Serpentinization will impact onset of brittle failure or dilatancy in the lower crust and upper mantle, forming weak faults and a brittle crust, in response to bending stresses and seismicity. Serpentine content is one of the factors that affect the amount of weakening resulting from the alteration of peridotite to serpentinite [12, 30].

2. Materials and Methods

The measurements were performed on cubes (7.3-13.1 cm³) and mini cores (1.8-2.7 cm³) of serpentinized dunites, pyroxenites and peridotites. The major phase of each sample and serpentine content estimated through petrographic analysis is provided in Table 1. Figure (1) contains photomicrographs of each sample in plain polarized (PPL) and crossed polarized (XPL) light. Three samples, denoted by symbols TS, JC, and ND respectively, are dunites from the Twin Sisters Range in Washington (Figure 1(a), (b)), Jackson County in North Carolina (Figure 1(e), (f)), and Newdale from the Blue Ridge province in North Carolina (Figure 1(g), (h)), respectively. They contain 60-95% Mg-rich olivine, the remainder composed of serpentine and 5% of minor minerals. One sample (BC) is a pyroxenite from the Bushveld Complex, South Africa (Figure 1(c), (d)), containing more than 90% Mg-rich orthopyroxene, about 10% serpentine, and 5% other minor minerals. Four samples were selected from the Point Sal Ophiolite in California (Figure 1(i), (j), (k), (l), (m), (n), (o), (p)) with major phase of Serpentine composing 60-95% of the samples, with various other minor phases including olivine and pyroxene.

Densities were calculated from the dimensions and weights of the cubes and mini cores. Porosity of the samples were measured by saturation under vacuum conditions, with the triple weighing technique similar to the method of Saad [31]. The serpentine content was estimated by petrographic analysis.
Figure 1. Photomicrographs of the samples in the order of increasing serpentine content. PPL=Plain Polarized Light, XPL=Crossed Polarized Light. In all the images veins of serpentine in olivine and pyroxene are visible.

3. Results

3.1. Measurements of Density and Porosity

Measured bulk density $\rho$ values ranged between 2540 kg/m$^3$ for HP sample to 3200 kg/m$^3$ for TS sample. The porosity of the samples ranges between 2.1% in the WP sample to 8.4% in ND sample (Table 2). Using measurements of bulk density and porosity, the grain density was estimated to range between 2644 kg/m$^3$ for HP sample to 3328 kg/m$^3$ for TS sample, which matches with the density of serpentine and un-serpentinized dunite respectively.

3.1.1. Density Variation with Serpentine Content

To find the best fit for $\rho - \beta$ correlation, we added published data from Falcon-Suarez et al., [26], Ramana and Rao, [28] and Horen et al., [27] to our data. In all of the above studies, $\beta$ is
estimated by petrographic analysis. As shown in Figure (2) increase in $\beta$ result in linear decline in $\rho$ following equation (1):

$$\beta \times 7.85 = \rho_{\text{peridotite}} - \rho_{\text{bulk}}$$

where $\rho_{\text{peridotite}}=3300$ kg/m$^3$. The R2 for this equation is 0.82. Miller and Christensen [13] report the same correlation between $\rho$ and $\beta$ of various serpentinized harzburgites and dunites from around the world with R2=0.98.

![Graph showing the relationship between density and serpentine content.](image)

**Figure 2.** The assumptions of the linear correlation between density and serpentine content is that serpentine content of peridotite with density of 3300 kg/m$^3$ is 0 and serpentine content of serpentinite with density of 2500 kg/m$^3$ is 100%.

Porosity of the samples does not correlate systematically with serpentine content. This could be resulted from tectonic and erosional processes affecting porosity well beyond the impact of serpentinization.

### 3.2. Estimating Seismic Velocities

Various previous studies have proven a linear correlation between seismic velocities and serpentine content [13, 20, 25]. The empirical correlation between Compressional Velocity $V_p$ and Shear Velocity $V_s$ with serpentine content developed in Horen et al., [27]:

$$V_p = (7922 - 32.5\beta) \text{ m/s}$$
$$V_s = (4371 - 21.8\beta) \text{ m/s}$$

where $\beta$ refers to serpentine content. $V_p$ and $V_s$ values of the samples in this study were estimated in range of 4834.5-7759.5 m/s for $V_p$ and 2300-4262 m/s for $V_s$ of HP and TS samples respectively.
(Table 3). Based on the data published in Christensen [1], the VP/Vs ratio is showing that most samples are possibly rich in Lizardite serpentine (Table 3). Previous studies show serpentinized peridotites of Point Sal have compressional velocities around 5.5 km/s [18], which agrees with our estimates.

3.3. Estimating Elastic Moduli and Poisson’s Ratio

Elastic moduli are correlated with seismic velocities, based on equations below:

$$\mu = \rho V_s^2$$ \hspace{1cm} (4)
$$K = \rho V_p^2 - 1.33\mu$$ \hspace{1cm} (5)
$$E = \rho (V_p^2 - 2V_s^2)$$ \hspace{1cm} (6)
$$\nu = \frac{\nu_s^2 - \nu_p^2}{2(\nu_s^2 - \nu_p^2)}$$ \hspace{1cm} (7)

where $\mu$ is shear modulus or rigidity, $K$ is bulk modulus or incompressibility, $E$ is Young’s modulus and $\nu$ is Poisson’s ratio. By incorporating results of equations (2) and (3) into (4), (5), (6) and (7), $\mu$ is estimated between 13.4-58.1 GPa, $K$ is estimated between 41.5-115 GPa, and $E$ is estimated between 32.5-76.4 GPa for HP and TS samples respectively. Estimated values of $\nu$ ranges from 0.28 for the TS sample to 0.35 for the HP sample (Table 3). High $\nu$ is as a result of low shear wave velocities in serpentinized ultramafic rocks, which agrees with previous studies [1, 32].

3.3.1. Elastic Moduli Variation with Serpentine Content

As shown in Figure 3 with increase in serpentine content, $\mu$, $K$ and $E$ will decrease linearly following equations (8), (9) and (10):

$$\mu = -0.48\beta + \mu_0$$ \hspace{1cm} (8)
$$K = -0.77\beta + K_0$$ \hspace{1cm} (9)
$$E = -0.45\beta + E_0$$ \hspace{1cm} (10)

where subscript 0 refers to a fresh peridotite where $\beta = 0$, $\mu_0 = 57.6$, $K_0 = 115$ and $E_0 = 76.6$. $\mu_0$ and $K_0$ values are in agreement with reported values in Christensen [19], Christensen and Shaw [34], Christensen [20] and Turcotte and Schubert, [35]. The R2 of equations (8), (9) and (10) is 0.98.
Figure 3. Shows the trend of Elastic Moduli ($\mu$, $K$ and $E$) with serpentine content

The standard deviation of $\mu$, $K$ and $E$ (Table 4, Figure 4) was calculated by estimating the elastic moduli of Horen et al., [27] samples using the measured seismic velocities in comparison to estimating the equations above.

Figure 4. The bars show the mean value of elastic moduli from Table 4 and the error bars represent the standard deviation (STD) from Table 4 for Horen et al., [27] samples.

4. Discussion

Our results show that increase in serpentine content will result in a linear decrease in density, and elastic moduli, which is in agreement with results of Christensen [19]. Our calculated elastic moduli of HP samples which is 95% serpentinized, is in great agreement with that for serpentinites
reported in Christensen [1972] and Carlson [36]. This agreement is slightly weaker between our freshest sample, TS, which is a slightly serpentinized dunite compared to estimates of fresh oceanic peridotite of Christensen [20], as a result of compositional difference between serpentinized dunite and oceanic peridotite.

Our results show that increase in serpentine content of lower crust and forearc mantle could decrease elasticity of lithosphere and result in break-offs [e.g. 12, 30, 33, 37].

Therefore tectonic processes at peridotite rich slow spreading ridges may be strongly affected by serpentine content, particularly serpentinization may be responsible for observed discontinuities in thin crust, and formation of weak fault zones [e.g. 12, 38, 39, 40].

5. Conclusions

In this study we show that as serpentine content increases, density decreases linearly with a slope of 7.85. We also correlate increase in serpentine content with a linear decline in shear, bulk and Young’s moduli with slopes of 0.48, 0.77, 0.45 respectively. Compositional variations with lower serpentine content ultramafic rocks, can result in variation of elastic moduli.

Our results show that increase in serpentine content of lower crust and forearc mantle could decrease elasticity of lithosphere and result in break-offs. Therefore tectonic processes at peridotite rich slow spreading ridges may be strongly affected by serpentine content, particularly serpentinization may be responsible for formation of discontinuities in thin crust, and weak fault zones.

Tables

<table>
<thead>
<tr>
<th>Table 1. Description of the samples used for the experiments.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Name</td>
</tr>
<tr>
<td>Twin Sisters dunite</td>
</tr>
<tr>
<td>Bushveld Complex pyroxenite</td>
</tr>
<tr>
<td>Jackson County dunite</td>
</tr>
<tr>
<td>Newdale dunite</td>
</tr>
<tr>
<td>Point Sal sample 1</td>
</tr>
<tr>
<td>Point Sal sample 2</td>
</tr>
<tr>
<td>Point Sal sample 3</td>
</tr>
<tr>
<td>Point Sal sample 4</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Table 2. Measurements of density and porosity and estimates of grain density.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sample</td>
</tr>
<tr>
<td>---------</td>
</tr>
<tr>
<td>TS</td>
</tr>
<tr>
<td>BC</td>
</tr>
<tr>
<td>JC</td>
</tr>
<tr>
<td>ND</td>
</tr>
<tr>
<td>CP</td>
</tr>
<tr>
<td>OP</td>
</tr>
<tr>
<td>WP</td>
</tr>
</tbody>
</table>
Table 3. Calculated seismic velocities and elastic moduli. Seismic velocities are calculated based on equations (1) and (2) for Vp and Vs and elastic moduli are calculated based on equations (3), (4), (5) and (6) for $\mu$, $K$ and $E$ and $\nu$ respectively.

<table>
<thead>
<tr>
<th>Sample</th>
<th>Vp (m/s)</th>
<th>Vs (m/s)</th>
<th>Vp/Vs</th>
<th>$\mu$ (GPa)</th>
<th>$K$ (GPa)</th>
<th>$E$ (GPa)</th>
<th>$\nu$</th>
</tr>
</thead>
<tbody>
<tr>
<td>TS</td>
<td>7759.5</td>
<td>4262</td>
<td>1.82</td>
<td>58.1</td>
<td>115</td>
<td>76.4</td>
<td>0.28</td>
</tr>
<tr>
<td>BC</td>
<td>7597</td>
<td>4153</td>
<td>1.83</td>
<td>53.1</td>
<td>107</td>
<td>71.5</td>
<td>0.28</td>
</tr>
<tr>
<td>JC</td>
<td>6947</td>
<td>3717</td>
<td>1.87</td>
<td>42.4</td>
<td>91.6</td>
<td>63.3</td>
<td>0.29</td>
</tr>
<tr>
<td>ND</td>
<td>6622</td>
<td>3499</td>
<td>1.89</td>
<td>34.2</td>
<td>76.8</td>
<td>54.03</td>
<td>0.30</td>
</tr>
<tr>
<td>CP</td>
<td>5972</td>
<td>3063</td>
<td>1.95</td>
<td>28.4</td>
<td>70.2</td>
<td>51.2</td>
<td>0.32</td>
</tr>
<tr>
<td>OP</td>
<td>5484.5</td>
<td>2736</td>
<td>2.00</td>
<td>21.0</td>
<td>56.3</td>
<td>42.3</td>
<td>0.33</td>
</tr>
<tr>
<td>WP</td>
<td>5159.5</td>
<td>2518</td>
<td>2.05</td>
<td>17.9</td>
<td>51.2</td>
<td>39.3</td>
<td>0.34</td>
</tr>
<tr>
<td>HP</td>
<td>4834.5</td>
<td>2300</td>
<td>2.10</td>
<td>13.4</td>
<td>41.5</td>
<td>32.5</td>
<td>0.35</td>
</tr>
</tbody>
</table>


<table>
<thead>
<tr>
<th>Horen et al., [27] samples</th>
<th>$V_p$ (m/s)</th>
<th>$V_s$ (m/s)</th>
<th>$\mu^*$ (Gpa)</th>
<th>$\mu^{**}$ (Gpa)</th>
<th>mean</th>
<th>STD</th>
<th>$K^*$ (Gpa)</th>
<th>$K^{**}$ (Gpa)</th>
<th>mean</th>
<th>STD</th>
<th>$E^*$ (Gpa)</th>
<th>$E^{**}$ (Gpa)</th>
<th>mean</th>
<th>STD</th>
</tr>
</thead>
<tbody>
<tr>
<td>PF1</td>
<td>7759</td>
<td>4353</td>
<td>61.77</td>
<td>56.15</td>
<td>58.96</td>
<td>3.98</td>
<td>113.90</td>
<td>112.72</td>
<td>113.31</td>
<td>0.83</td>
<td>72.71</td>
<td>75.28</td>
<td>61.20</td>
<td>1.81</td>
</tr>
<tr>
<td>PF2</td>
<td>7346</td>
<td>4172</td>
<td>55.70</td>
<td>50.38</td>
<td>53.04</td>
<td>3.76</td>
<td>98.42</td>
<td>103.40</td>
<td>100.91</td>
<td>3.52</td>
<td>61.29</td>
<td>69.80</td>
<td>56.94</td>
<td>6.02</td>
</tr>
<tr>
<td>PS2</td>
<td>6722</td>
<td>3552</td>
<td>37.85</td>
<td>40.77</td>
<td>39.31</td>
<td>2.07</td>
<td>85.09</td>
<td>87.86</td>
<td>86.47</td>
<td>1.96</td>
<td>59.86</td>
<td>60.67</td>
<td>50.62</td>
<td>0.58</td>
</tr>
<tr>
<td>PS1</td>
<td>6788</td>
<td>3579</td>
<td>39.20</td>
<td>40.77</td>
<td>39.98</td>
<td>1.11</td>
<td>88.73</td>
<td>87.86</td>
<td>88.30</td>
<td>0.62</td>
<td>62.60</td>
<td>60.67</td>
<td>46.59</td>
<td>1.37</td>
</tr>
<tr>
<td>PS3</td>
<td>6355</td>
<td>3333</td>
<td>32.55</td>
<td>35.97</td>
<td>34.26</td>
<td>2.42</td>
<td>74.93</td>
<td>80.09</td>
<td>77.51</td>
<td>3.65</td>
<td>53.23</td>
<td>56.10</td>
<td>42.71</td>
<td>2.03</td>
</tr>
<tr>
<td>PS4</td>
<td>5864</td>
<td>3081</td>
<td>25.72</td>
<td>23.95</td>
<td>24.84</td>
<td>1.25</td>
<td>58.89</td>
<td>60.67</td>
<td>59.78</td>
<td>1.26</td>
<td>41.74</td>
<td>44.69</td>
<td>39.28</td>
<td>2.09</td>
</tr>
</tbody>
</table>

1) $\mu^*$, $K^*$ and $E^*$ are calculated using $V_p$ and $V_s$ based on equations (4), (5), (6) respectively
2) $\mu^{**}$, $K^{**}$ and $E^{**}$ are calculated using equations (8), (9) and (10) respectively
Author Contributions: conceptualization, A.F.; methodology, A.F.; formal analysis, A.F.; investigation, A.K.; resources, A.F.; data curation, A.K.; writing—original draft preparation, A.F.; writing—review and editing, A.F.; visualization, A.F.; supervision, A.F.; project administration, A.F.

Acknowledgments: All the data are provided in Tables section of this manuscript. The authors would like to thank Kayleigh Rogers for help with petrographic analysis. We are also thankful to William Dinklage for providing the Point Sal samples. Authors would also like to acknowledge help and support from Dr. Robert P. Lowell (deceased) on earlier versions of this manuscript.

Conflicts of Interest: The authors declare no conflict of interest.
References


