

A New Model on Cation Distribution in Cation-Disordered $\text{Li}_{1+x}\text{TM}_{1-x}\text{O}_2$ Cathodes

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Abstract

The search for new materials that could improve the energy density of Li-ion batteries (LIB) is one of today's most challenging issues. Recently, cation-disordered lithium-excess metal oxides have emerged as a promising new class of cathode materials for LIB, due to their high reversible capacities and nice structural stability. However, a full structural model of the Li-transition metal (TM) sharing sublattice and the origin of short range ordering (SRO) of cation ions requires further investigation. In this work, we put forward a Monte Carlo strategy of building a cation-disordered rocksalt material supercell model. The cation ions of $\text{Li}_{1.0}\text{Ti}_{0.5}\text{Ni}_{0.5}\text{O}_2$ (LTNO) are placed at the FCC sublattice sites with the constraint of Pauling's electroneutrality rule, instead of a random way. This constraint causes the Li-Ti and Ni-Ni clustering (the cation short range ordering). Based on this model, we discussed the relationship between the short range ordering, the local distorting, the theoretic capacity and the order-disorder strengths. A unified understanding of these factors in cation-disordered materials may enable a better design of disordered-electrode materials with high capacity and high energy density.

Keywords: cation-disordered Li-excess cathodes, short range ordering, local distorting, theoretic capacity, order-disorder strength

1. Introduction

Since the first commercial application in last century, the Li ion batteries (LIB) have been attracting the continuous attentions due to its high energy density among rechargeable batteries. There has been a continuous research effort to improve the specific energy density of LIBs for emerging applications such as electric vehicles. One

of the bottlenecks to this is developing higher capacity cathode materials which is vital to the cost, weight, and volume of a battery [1, 2]. Cathode compounds operate by reversibly releasing and reinserting lithium ions during charge and discharge, respectively. This process must be reversible and any permanent damage on the structure is undesirable to improve its cycle performance. To do this, a robust host structure is necessary which offers the accessible channels for Li intercalation and de-intercalation.

In the past decades, several kinds of cathode materials have been developed and applied in the commercial LIBs [3-5], such as LiCoO_2 which has a layered rocksalt-type structure and offers 2D slabs for Li diffusion, LiMn_2O_4 which has a spinel structure and offers 3D network tetrahedral sites for Li diffusion, LiFePO_4 which has an olivine structure and offers 1D channels for Li diffusion. In these compounds, Li and other cation ions are separated into respective sublattice and form well-ordered structures. To a general consideration, no mixing between Li and other cations is important for obtaining high-capacity cathode materials with good cycle life. In some cases, improvements in ordering have led to notable increases in power or energy density [6-8].

In recent years, Lee et al. unlocked the potential of cation-disordered oxides for rechargeable lithium batteries [9-12]. In these cathode materials, both Li and transition metal (TM) share the same sublattice which is a cubic close-packed lattice of octahedral sites, and Li diffusion proceeds by hopping from one octahedral site to another octahedral site via an intermediate tetrahedral site (o-t-o diffusion) [13]. The intermediate tetrahedral site shares faces with four octahedral sites which could be occupied by Li or TM. The migration barriers for this o-t-o hopping relates to the four face sharing cations. The ab initio calculation shows that only the intermediate tetrahedral sites involving no face-sharing TM ions (0-TM channel) allows for reasonable Li hopping rates [9,10]. To sustain macroscopic ion migration, these 0-TM diffusion channels need to span the entire structure, or in other words, the diffusion channels need to form a percolating network. Intuitively, the more number of 0-TM channels, the more likely they percolate. As the 0-TM channel is coordinated by four Li ions, the more contents of Li ions benefits the 0-TM percolating network. Using the percolation theory, Urban et al. pointed out that the necessary prerequisite for Li transport in cation-disordered oxides is an excess of Li over TM of at least 10%, in line with the general strategy to utilize Li-excess chemistries to achieve higher energy densities [9, 10]. The experimentally synthesized Li-excess cation-disordered cathodes usually have about 300 mAhg^{-1} capacities, nearly twice than those of traditional cathode materials [14-17]. Also, the cation disorder can enhance the structural stability upon Li extraction, as the Li ions are extracted uniformly from the bulk. The experimental results show that the volume changes of these materials are below about 5% during charge/discharge process [18-20]. Minimising volume fluctuations is beneficial for all electrodes, but is especially important for solid-state batteries in order to prevent fracturing of the solid electrode/electrolyte interfaces and as such cation-disordered electrodes are particularly attractive for all-solid batteries.

Despite the impressive progress in the development of disordered rock-salt

compounds, a number of key fundamental issues remain unaddressed. As stated before, Li and TM ions occupy the same sublattice in the cation-disordered materials. In regard to their concrete arrangement in the sublattice, the theoretic methodology in being just take them as in a disordered way, so no short range ordering (SRO) is considered. In fact, though the distribution of cation ions can be taken as completely disordered in the long-range scale, in the short range regarding several coordinating shells of the central cation ions, whether there exist some tendencies for outer cation coordinating is to be discussed. In practice, as chemical incompatibility (ionic radii, charge, electronic-structure et al.) between different cation ions is common, not all cation ions can be perfectly miscible and compatible in the same sublattice [21-23]. So some cation ions will 'repel' with each other and distribute themselves at a farther distance in the sublattice. Several experiments have proven this idea and show that there do exist some SRO in the synthesized cation-disorder materials [24-27]. In this paper, we focus on the SRO in the rock-salt type cation-disorder materials. We point out that the Pauling's rule of electroneutrality which constrains the assignment of cation ions in cation-ordered ones may also apply to the cation-disordered materials to some degree, resulting in the arising of SRO and clustering between cation ions. Based on our new model, we make clear the relationships between the SRO, the local distorting, the theoretic capacity and the order-disorder strengths. Our modeling methodology can be taken as an improvement of the previous theoretic treatments of sublattice-sharing crystals. Also, the design of experimental verification is direct and legible which is our focus for the next time.

In the second section, the structure of rocksalt-type cation-disorder materials and the Pauling's rule of electroneutrality are briefly reviewed. Then we put forward a Monte Carlo method of building the $\text{Li}_{1.0}\text{Ti}_{0.5}\text{Ni}_{0.5}\text{O}_2$ (LTNO) structure with the constraints of Pauling's rule and search the final thermal equilibrium structure with an atomistic potential model. In section 3, the clustering of Li-Ti and Ni-Ni in the LTNO structure is discussed. Furthermore, we prove that this clustering has some impressive impacts on the local distorting, the theoretic capacity and the order-disorder energy.

2. Methodology

2.1 The structure of cation-disordered materials

The structure of cation-disordered are related to that of the cubic rock salt (NaCl) as shown in figure 1. The space group is Fm-3m. O ions occupy the $4b_{\text{Wyckoff}}$ sites, forming a face-centered cubic (FCC) sublattice while Li and TM ions occupy the $4a_{\text{Wyckoff}}$ sites which also form a FCC sublattice. Each cation ion is located at the center of an octahedron and coordinated by six O ions. Also, each O ion is located at the center of an octahedron and coordinated by six cation ions.

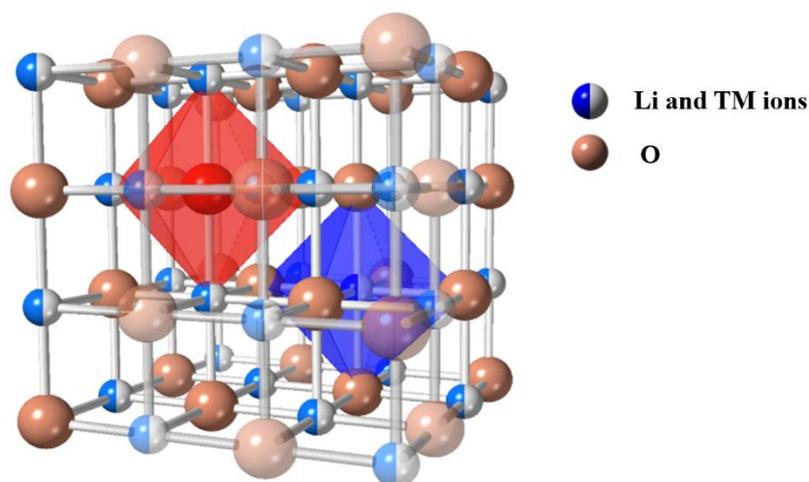


Figure 1. The structure of cation-disordered cathode materials

2.2 Pauling's rule of electroneutrality in ordered rock salt oxides

In ternary ordered rock salt oxide systems, $A_aB_bO_{a+b}$, the two cation ions, A and B, usually have different valence. However, there only exist certain combinations of A, B around O ions where Pauling's rule of electroneutrality must be followed. This rule tells that the sum of electrovalencies, z/n (z =charge, n =coordination no.) of the nearest neighbouring cation ions should equal the charge, x of O ions, i.e. $\sum z/n=x$. This occurs in the general formula ABO_2 , A_2BO_3 and A_5BO_6 , for which A is monovalent and B is tri-, tetra- and heptavalent, respectively [28].

ABO_2 has OA_3B_3 octahedra; $\sum z/n = (3 \times 1/6) + (3 \times 3/6) = 2$
 the representative ternary oxides are: $LiCoO_2$, $LiNiO_2$, $a-NaFeO_2$ et al.

A_2BO_3 has OA_4B_2 octahedra; $\sum z/n = (4 \times 1/6) + (2 \times 4/6) = 2$
 the representative ternary oxides are: Li_2MnO_3 , Li_2TiO_3 et al.

A_5BO_6 has OA_5B octahedra; $\sum z/n = (5 \times 1/6) + (1 \times 7/6) = 2$
 the representative ternary oxide is: Li_5ReO_6 et al.

2.3 Building the initial disordered structure of LTNO with the constraint of Pauling's rule.

For the disordered rocksalt-type multicomponent oxides like LTNO [29, 30], the general idea is that Li, Ti and Ni ions occupy the same sublattice and are randomly distributed on the lattice points. As far as we know, there are no theoretical model and calculations about the specific arrangements of cation ions within the sublattice. However, several works on the layered rocksalt-type Li-excess materials $xLi_2MnO_3 \cdot (1-x)LiMO_2$ ($M=Co$ or Ni) where Li, Mn and M occupy the some TM layer jointly show there exist some rules of cation arrangements rather than a fully random distribution [31, 32]. Some evidences of elemental clustering, forming local Li_2MnO_3 -like and $LiMO_2$ -like environments in the TM planes, has been reported.

Reconsidering the structure of $xLi_2MnO_3 \cdot (1-x)LiMO_2$, it is clear that the Li_2MnO_3 and $LiMO_2$ components follow the Pauling's rule of electroneutrality, as the ions in Li_2MnO_3 have $O4Li^+2Mn^{+4}$ and in $LiMO_2$ have $O3Li^+3M^{3+}$ octahedral blocks.

Obviously, the maintaining of local electroneutrality is not only a strict rule in the ordered structure, in the disordered structure, the cation ions also tend to keep some degree of local electroneutrality through clustering into the ‘right’ local assignments.

As a simple generalization, we considered the electroneutrality in the cation-disordered rocksalt-type $\text{Li}_{1+x}\text{TM}_{1-x}\text{O}_2$ where Li and TM share the same FCC sublattice. This is a typical structure for layered rocksalt-type Li-excess materials where Li and TM are located at the same TM layers. We studied that if the applying of Pauling's rule to the cation-disordered rocksalt-type $\text{Li}_{1+x}\text{TM}_{1-x}\text{O}_2$ will lead to the cation clustering and SRO. For the convenience of discussion, we take LTNO as the example. In the following paragraph, the idea about building of the initial structure of LTNO by a Monte Carlo process with a constraint of the Pauling's rule is described and further discussions based on this initial structure will be presented in the following sections. All we do below can be used to study other Li-excess cation-disordered materials.

A $10 \times 10 \times 10$ supercell of LTNO is established. Initially, the O ions are placed on the $4b_{\text{Wyckoff}}$ sites to form the anion sublattice and Li, Ni and Ti on the $4a_{\text{Wyckoff}}$ sites in a random way, without any electroneutrality constraints. Then the electroneutrality is considered. We calculated the net charge of each O ion in the structure. The net charge is defined by the Pauling's rule of electroneutrality, $Q = -2 + \sum_{i=1}^6 Z_i/6$ ($Z_i = +1$ for Li, $+2$ for Ni, and $+4$ for Ti). The number of O ions with zero net charge (in electroneutrality) in the structure was counted and we found that only about 10% of O ions are with zero net charge when the cation ions are randomly distributed. Next, two of different cation ions in the structure are picked out randomly and exchange their sites. Then the proportion of O ions in electroneutrality versus the total O number (O_n) is counted. If it is larger than that before the exchange, we consider this exchange as a ‘good’ one and refresh the structure. On the other hand, if it is smaller than or equal to that before the exchange, we consider it as a ‘bad’ one and abandon this exchange. So with the exchanging process going forward, more and more O ions will be driven into electroneutrality. We set the threshold values 0.2, 0.3 and 0.4 for O_n . When the pre-set threshold is reached, the Monte Carlo procedure is stopped and the configurations with different degree of electroneutrality are generated. Figure 2 is a flow chart of our Monte Carlo strategy.

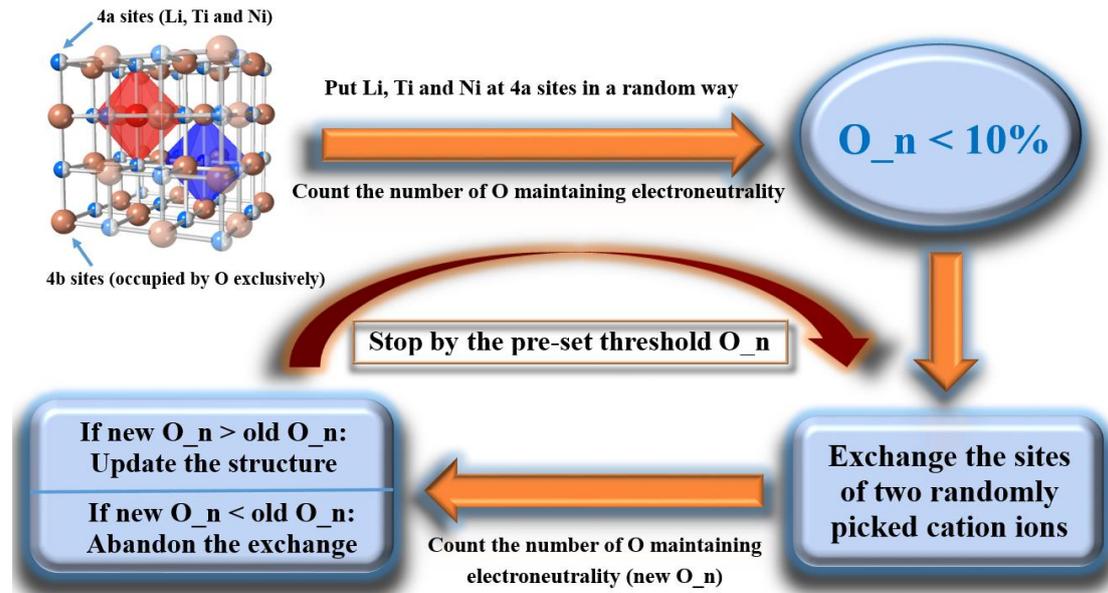


Figure 2. The detailed process of the Monte Carlo strategy establishing an initial configuration of LTNO

2.4 Search the thermal equilibrium structure with an atomistic potential model

The structures established in the last section is just a rough model for LTNO, as no interatomic interactions and thermodynamics process are considered. So they could not describe the thermal-stable structures which can be observed at laboratories. In this section, we use an atomistic model to drive the LTNO into thermal equilibrium. The structures with different levels of electroneutrality constraint established in the last section are simulated by the molecular dynamics (MD) methods which is executed on DL-POLY (Version 4.07) [33]. Periodic boundary condition were applied in all directions. Atomic motions and Coulombic interactions were calculated by the Verlet algorithm and Ewald method respectively. The time step was 1 fs. The system was relaxed for 10 ps firstly and then run for 100 ps at 300K. A Nose–Hoover thermostat was used to regulate the system's temperature at specific temperatures.

The Morse function is used here to represent the short range repulsion and partial charges are set to each ion to include the Coulomb interactions. The mathematic expression of our potential model is shown in below equation (1).

$$U(r) = \frac{Z_i Z_j e^2}{r} + D_{ij} \left[\left\{ 1 - e^{-a_{ij} \cdot (r - r_0)} \right\}^2 - 1 \right] \quad (1)$$

in which D_{ij} is the bond dissociation energy, a_{ij} is a function of the slope of the potential energy well, and r_0 is the equilibrium bond distance. Z_i is the partial charge of ions.

The potential parameters are listed in table 1. The original data of the potential parameters is from the work of Alfonso Pedone [34], which is established for binary oxides and fits the experimentally measured structural and mechanical properties very well. To make a better description of our ternary oxides system, we optimized the

parameters slightly, which can make a better fitting of the experimental structures of Li_2TiO_3 (C2/c, $a=5.2189\text{\AA}$, $b=8.6686\text{\AA}$, $c=5.0865\text{\AA}$) and NiO (Fm-3m, $a=b=c=4.2043\text{\AA}$). Relaxing the Li_2TiO_3 and NiO unit cell with this set of optimized potential parameters, the structural parameters of the relaxed unit cell accords well with the experimentally measured ones within error $< 4\%$, proving their suitability for our work.

Table 1 Potential parameters used in this article, terms not listed are set to zero.

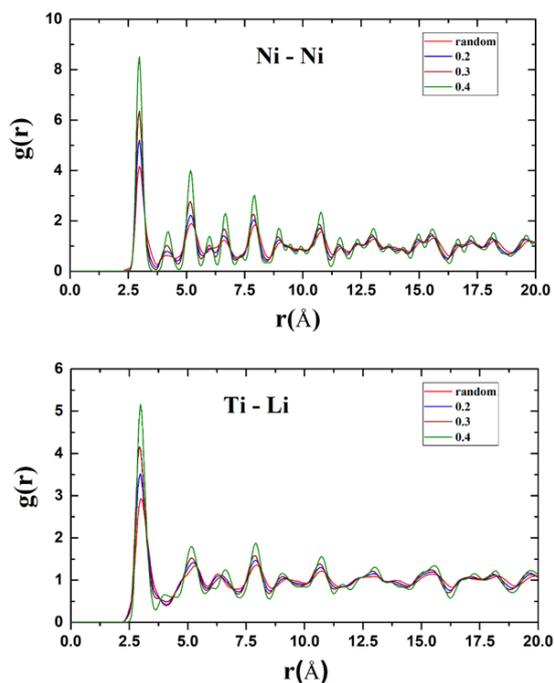
interaction	$D_{ij}(\text{eV})$	$a_{ij}(\text{\AA}^2)$	$r_0(\text{\AA})$
$\text{Li}^{+0.6}-\text{O}^{-1.2}$	0.001114	3.629506	2.701360
$\text{O}^{-1.2}-\text{O}^{-1.2}$	0.042395	2.579316	3.108701
$\text{Ti}^{+2.4}-\text{O}^{-1.2}$	0.024235	2.254704	2.808943
$\text{Ni}^{+1.2}-\text{O}^{-1.2}$	0.029356	2.679137	2.530754

3. Results and discussion

3.1 The short range ordering and phase segregation

We firstly investigate the local cation environments with different constraints of electroneutrality (O_n). To study the coordination relations between cation ions in a clear and statistic way, we calculated the atomic pair distribution function $g(r)$ between individual cation ions which counts the probability of the coordinating ion appearing at a certain distance from the center ion.

Figure 3 shows the $g(r)$ function of Ti-Li and Ni-Ni. Firstly, the peaks arising regularly spanning to the whole displaying r space (to 20\AA) proves the suitability of our potential field model, as it indicates the completeness of the periodic crystal structures after driven into equilibrium by MD. Noticing the first few peaks of Ti-Li and Ni-Ni, it is clear that with a more strict constraint (higher value of O_n), the peak values get higher which means stronger coordinating between Ti-Li and Ni-Ni. Considering that a random distribution of cation ions means a 'uniform' distribution which brings no coordinating tendency to cation ions, from our model it can be inferred that the constraints of Pauli's electroneutrality rule applying to the disordering system results in the SRO of cation arrangements.



Recalling the details of Pauling's rule which infers a charge balance between each O ion and its first shell coordinating cation ions, only O4Li2Ti and O6Ni units stratify the electroneutrality. With the increasing number of O ions in electroneutrality, more and more O4Li2Ti and O6Ni units are built in the system, leading to the clustering of Li-Ti and Ni-Ni. In other words, the phase segregation of Li₂TiO₃ and NiO arises in the system.

Figure 3. up: the $g(r)$ function of Ni and Ni. down: the $g(r)$ function of Ti and Li. Different colors for different constraints of electroneutrality.

3.2 The local distortion

In an ordered structure, the cation ions usually have a single or a few local high-symmetry environments, whereas in a disordered structure there exist a large number of distinct low-symmetry environments. The inhomogeneity of local chemical environments will cause microscopic strains on the ions located at the ideal positions. To relax the strains, the ions would deviate from the ideal positions, resulting in local distortions. This is predicted by the *ab initio* calculation [35]. The local distortions do exist in cation-disordered Li-TM oxides, and take much larger magnitudes than that in ordered ones on average.

Here, we also inspect the local distortion phenomenon in LTNO driven into equilibration states by MD simulation. The figure 4 shows the final structure in thermal equilibration where cation ions are distributed randomly in the initial model (left) and with an electroneutrality constraint of 0.4 in O_n (right). The anions and the cations are still located at the vicinity of the lattice points and keep the completeness of the crystal structure. As expected, the local distortions are observed. Some cation ions located at 4a sites (the center of octahedron) in the initial structure 'slide' to the 8c sites (the center of tetrahedron) during the thermodynamics process. On the other hand, this 'slide' phenomenon is not observed in the arrangements of O ions, proving the toughness of the anion sublattice. The complex local chemical environments resulting from the cation disorder do have some influence on the final stable structure. The energy hypersurfaces at some 4a sites are raised and at some 8c sites are lowered, so the cation ions slide to the 8c sites along the energy hypersurfaces.

The final structure with a constraint of electroneutrality (O_n = 4) shows a much more 'clean' cation sublattice, indicating it helps to reduce the local distortion. We counted the ratios of Li, Ni and Ti at 8c to their total numbers under the four electroneutrality constraints (averaged for the ten simulated structures in each one) as

shown in figure 5. Two obvious features can be seen in the data. The first is that the ratio of Ni at 8c sites are significantly less than those of Li and Ti, only about half of them. This result is supported by the ab initio calculation, which shows that TM cations with d^0 electronic structure (Ti^{4+}) accommodate large site distortions allowing the Ni^{2+} sites to remain close to their preferred geometry [35]. Another distinct feature is that the degree of local distortion decreases with the increasing O_n in the configuration, dropping to just 2% with the O_n value 0.4. As discussed in last section, the increasing of O_n results in the clustering of Li_2TiO_3 phases and NiO phases, which means the degree of ordering phase in the system is increased, so reducing the local distortion.

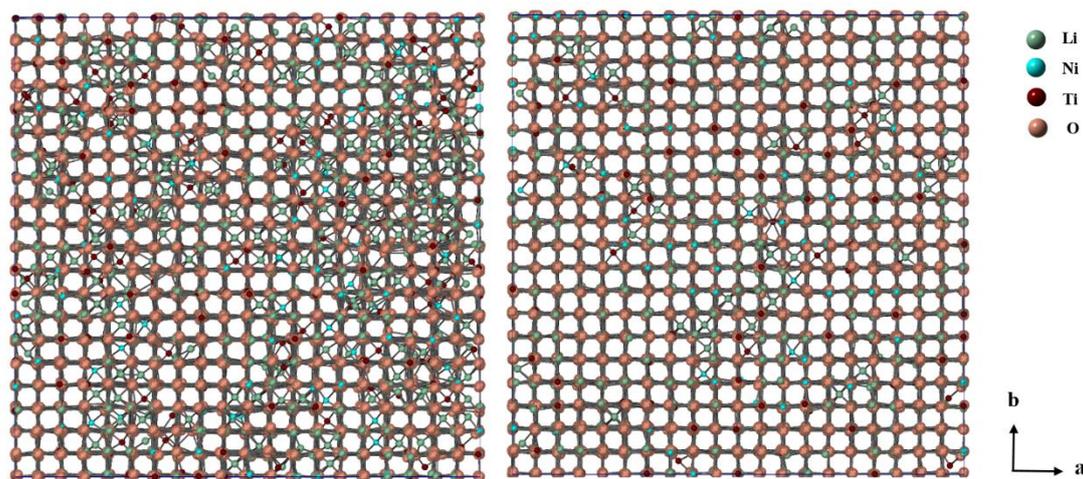


Figure 4. The MD simulated structure of LTNO. Left: The cation ions are distributed in a random way in the initial configuration. Right: The cation ions are distributed with a constraint of $O_n = 0.4$ in the initial configuration.

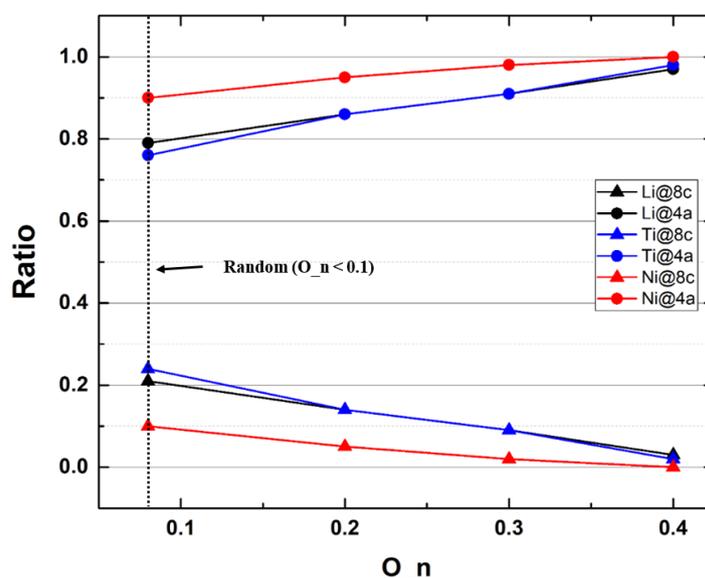


Figure 5 The contents of cation ions at octahedral (8c) and tetrahedral (4c) sites varying with the electroneutrality constraint (O_n)

3.3 The theoretic capacity and the percolation threshold

In the previous sections, we stated that only those Li ions connected to the 0-TM channels can hop to the nearby vacancies through the tetrahedral sites. So the theoretic capacity is limited by the number of 0-TM channels in the system. Here, we calculated the number of 0-TM channels with different electroneutrality constraints.

Figure 5 displays the number of 0-TM and 1-TM channels varying with the O_n in the initial MC building models. The 1-TM(Ni) and 1-TM(Ti) indicate the tetrahedral channels coordinating by one Ni or one Ti TM ion. With a more strict electroneutrality constraints, the numbers of 0-TM and 1-TM(Ni) decrease while the number of 1-TM(Ti) increases. As discussed before, the electroneutrality constraint leads to the clustering of Li-Ti and Ni-Ni. For the 0-TM and 1-TM(Ni) channel, they are coordinated by four Li ions and three Li ions, one Ni ion respectively. So the enhancing of Li-Ti and Ni-Ni coordinating should limit the number of 0-TM and 1-TM(Ni) channels. On the other hand, the 1-TM(Ti) channel is coordinated by three Li ions and one Ti ion. So the clustering of Li-Ti is preferred for them. In all, we can say with an electroneutrality constraint, the 0-TM channel which is favorable to the Li migration is limited and the number of active Li ions which can be de-intercalated from the bulk material decreases. As a result, the SRO reduces the theory capacity.

Then we consider the influence of SRO on the percolation threshold. Intuitively, since the electroneutrality constraint limits the 0-TM channels, it should decrease the percolating probability of 0-TM network in the system and raise the percolating thresholds. Here we calculate the percolating probability (P_w) of LTNO under different O_n values and see if it is. To be noted, pentavalent Mo is added to keep the overall electroneutrality of the system as an excess of Li is added. Figure 6 shows the final results. It can be seen that the percolating probability (P_w) varies steeply with the increase of Li content. In fact, it should be a step function with a discontinuity at the critical threshold x_c ($P_w = 1$ for $x_{Li} > x_c$, $P_w = 0$ for $x_{Li} < x_c$). Here, we calculate P_w in a $12 \times 12 \times 12$ supercell, it converges to a step function with much larger supercells [10]. However, the percolation threshold is always indicated by the center of the slopes (which are remarked by the vertical lines in the figure). We can see that in a random distribution hypothesis, the percolation threshold is about 1.1 which accords with that of previous calculation. However, with a more strict electroneutrality constraint (larger O_n value), the percolation threshold gradually increases. With $O_n = 0.4$, the calculated percolation threshold is even larger than 1.2 Li ions per formula unit. It is interesting that though the general guideline for designing 0-TM network percolating cation-disordered cathode materials is adding excess of Li content which is no less than about 1.1 Li atoms per formula unit, our result shows that this guideline depends. In a high-electroneutrality system, the actual percolation threshold for Li excess may larger than the general idea. In fact, we have noticed that someone synthesized some Li-excess ($x_{Li}=1.2$ per formula unit) cation-disordered cathode materials failing to show the percolating features in the electrochemical measurements [27, 36]. Our results may throw some inspiration on their problem.

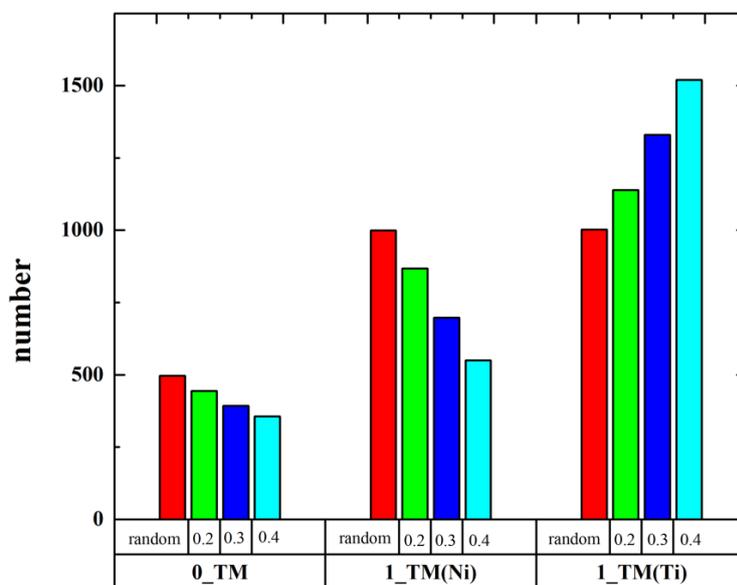


Figure 5 the number of 0-TM, 1-TM(Ni) and 1-TM(Ti) channels in the LTNO with different electroneutrality constraints

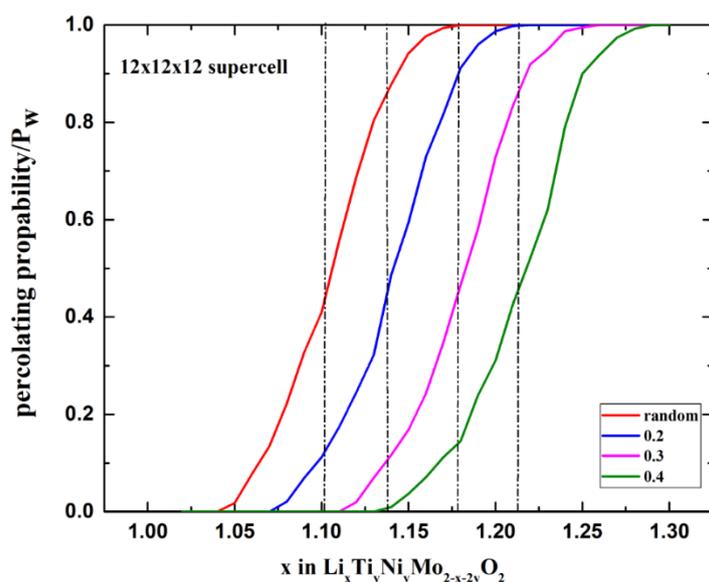


Figure 6 the percolating probability of $\text{Li}_x\text{Ti}_y\text{Ni}_y\text{Mo}_{2-x-2y}\text{O}_2$ with different electroneutrality.

3.4 The order-disorder energy

The theoretical calculation and practical application of Li-excess cation-disordered oxides as cathode materials has opened the vast configurational space of rocksalt-type oxides for designing new high-energy-density Li-ion batteries. Compared to the ordered phases of lithium metal oxides which are limited by several structures and several kinds of TM ions, any kinds of TM ions in the compositional space can be cooperated into the cation sublattices of cation-disordered oxide only if it keeps the electric neutrality in whole.

For a pre-designing purpose, it is important to know the cation-disordering strength for different kinds of alternative TM ions. Someone introduces the temperature of the

configurational order–disorder phase transition (T_{OD}) and the energy difference between the disordered state and the ordered state (E_{OD}) for measuring intrinsic cation-ordering strength [37]. They are quite useful guidelines for selecting the appropriate candidates when synthesizing the cation-disordered oxides in labs. But we noticed that these results are based on the hypothesis that cation ions are distributed randomly on the FCC sublattice. This ignores the intermediate configurations where the cation arrangement is partially disordered and the SRO exists. This condition is important as the SRO of cation ions generally inhabits in the synthesized materials so the guidelines based on random distribution of cation ions may overstate the cation-disordering strength in the materials.

We calculated the E_{OD} of $\text{LiTi}_{0.5}\text{Ni}_{0.5}\text{O}_2$ by including the configurations containing different levels of SRO which is controlled by the electroneutrality O ions (O_n).

$$E_{OD}(O_n) = E_{\text{Li}_{1.0}\text{Ti}_{0.5}\text{Ni}_{0.5}\text{O}_2}(O_n) - 0.5E_{\text{Li}_2\text{TiO}_3} - 0.5E_{\text{NiO}} \quad (1)$$

Here, we considered Li_2TiO_3 and NiO as the precursors. So the energy difference E_{OD} indicates the formation energy of $\text{LiTi}_{0.5}\text{Ni}_{0.5}\text{O}_2$ with different levels of SRO synthesized in labs. Also, E is the enthalpy of $\text{LiTi}_{0.5}\text{Ni}_{0.5}\text{O}_2$, Li_2TiO_3 and NiO from the MD calculation in the previous section and normalized to eV per formula. As in the sections above, four different kinds of configurations are explored (random distribution and $O_n < 0.1$, $O_n = 0.2$, $O_n = 0.3$ and $O_n = 0.4$). The final results are presented in table 3 below.

Table 2. the order-disorder energy (E_{OD}) for different levels of electroneutrality (O_n)

O_n	E_{OD} (ev/f.u.)
random	0.390
0.2	0.330
0.3	0.271
0.4	0.190

As expected, the order-disorder energy for all the disordered configurations take positive values. This indicates that the disordered configurations possess higher energy states in the configuration space respect to the ordered one. To drive the cation disordering, the system energy must be compensated from the outside environment. Furthermore, the configurations with larger disordering arrangements of cations (smaller O_n) take larger order-disorder energy. As discussed before, the stronger local electroneutrality environments means the segregation of Li_2TiO_3 and NiO clusters. So the energy should approach asymptotically that of $0.5\text{Li}_2\text{TiO}_3 \cdot 0.5\text{NiO}$ with the increasing of O_n . Ultimately, this helps to reduce the overall energy of the system and overcome the configuration entropy contribution that serves to randomize the distribution of cations in these oxides

3.5 Discussions

In the previous sections, we discussed the SRO, the local distortion, the capacity and the order-disorder energy based on our MC models. Here, we will make a summary further and try to elucidate their relationships in a clear way.

In Figure 7, we print all the correlatives in our model. A two dimensional coordinate

space is established where the abscissa represents the contents of O ions in electroneutrality (O_n) and the ordinate represents the energy. The energy varies with O_n in an inverse way as indicated by the parabola. The increase of O_n leads more O ions to keep in local electroneutrality and the phase segregation of Li_2TiO_3 and NiO . This will lower the energy of the whole system. To be noted, the points on the parabola indicate the structures with perfect lattice and all the cation ions located at the 4a sublattice. However, these configurations are not stable in thermodynamics and they will ‘slide’ to the local energy minimum nearby by relaxing the cation ions to 8c sites which are indicated by the valleys connected to the parabola. Also, the increase of O_n can reduce this distortion, so the depth of the four valleys gets smaller to the higher end of the O_n axis. In the extreme cases, the Li_2TiO_3 and NiO will be separated out totally. The system arrives to the global energy minimum in this case. However, the phase segregation of Li_2TiO_3 and NiO will break down the local Li excess environment and decrease the content of 0-TM channels which benefits the Li transports. So the amount of accessible Li ions which are connected with the 0-TM network will decrease with a higher O_n value. This goes against the final electrochemical performance as it lowers the theoretic capacity. To this point, we expect that the cation ions should be distributed in a more ‘disordering’ way, lowering the phase segregation and improving the capacity. As the sketch indicates, the more disordering configurations are located at higher energy states. This puts forward a more severe requirement when synthesizing the Li-excess cation-disorder materials in labs. In fact, we have noticed that some cathode materials synthesized at low sintering temperatures (from 750 °C to 800 °C) sometimes fail to meet the percolating capacity as the theory expects [27,36,38] while those synthesized at high sintering temperatures (around 1000-1100°C) always show high percolating capacities as expected[25, 39]. There is a more obvious comparison when synthesizing the same Li-excess cation-disorder material at different sintering temperatures and measuring their respective capacities by electrochemical methods [38] or reheating the materials and inspect the cation re-distribution by STEM/EDX mapping [40].

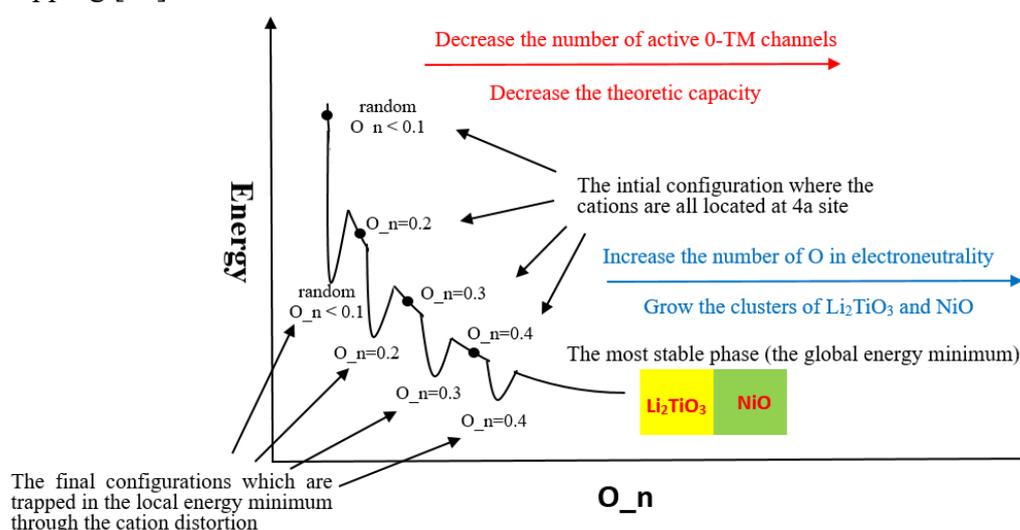


Figure 7. A sketch that interprets the relationships between the short-range ordering, the local distortion, the capacity and the energy and the local electroneutrality environments.

4. Conclusion

In this article, we focused on the cation arrangements in cation-disordered rock-salt type oxides. With the $\text{Li}_{1.0}\text{Ti}_{0.5}\text{Ni}_{0.5}\text{O}_2$ model applied with Pauling's rule of electroneutrality, the local electroneutrality demands for O ions result in the SRO of cation ions (enforce the Li-Ti and Ni-Ni coordination) and the phase segregation of Li_2TiO_3 and NiO.

Based on this model, we discussed the local distortion, the theoretic capacity and the percolation threshold, the order-disorder strengths. As the cation disordering exists, the complex local chemical environment causes the un-stabilization of cation ions at 4a sites which is the center of O octahedron. At the thermodynamics equilibrium condition, some cation ions will 'slide' to the 8c sites which is the center of O tetrahedron, leading to the local distortion arises and destroying the integrality of the rock-salt type lattice. However, when the electroneutrality constraints is applied, the phase segregation of Li_2TiO_3 and NiO will stabilize the cation ions at the 4a sites and reduce the local distortion. Also, the reinforced Li-Ti coordination destroys the local Li excess environment, reducing the content of O-TM channels in the sytem. This condition is detrimental for the theoretic capacity and a higher Li content is required for the O-TM network percolating if SRO is considered. Finally, the order-disorder energy is calculated for configurations with different levels of SRO. The results indicate that the SRO lowers the system energies. To get more cation-disordered structures with lager theoretic capacities, the materials should be sintering at a high enough temperature to overcome the high enthalpy.

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