

Article

Evaluation of a mesoscale thermal actuator in open and closed operating cycles

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Abstract: Thermal-based actuators are known for generating large force and displacement strokes at mesoscale (millimeter) regime. In particular, two-phase thermal actuators are found to benefit from the scaling laws of physics at mesoscale to offer large force and displacement strokes; but they have low thermal efficiencies. As an alternative, a combustion-based thermal actuator is proposed and its performance is studied in both open and closed cycle operations. Through a physics-based lumped-parameter model, we investigate the behavior and performance of the actuator using a spring-mass-damper analogy and taking an air standard cycle approach. Three observations are reported: (1) the mesoscale actuator can generate peak forces of up to 400 N and displacement strokes of about 16 cm suitable for practical applications; (2) an increase in heat input to the actuator results in increasing the thermal efficiency of the actuator for both open and closed cycles; and (3) for a specific heat input, both the open and closed cycle operations respond differently —different stroke lengths, peak pressures, and thermal efficiencies.

Keywords: Thermal actuator, compliant architecture, open and closed operating cycles, mesoscale

1. Introduction

Mechanical actuation via thermal actuators has been a topic of interest due to their ability to generate forces $O(10^1)$ N and displacement strokes $O(10^{-4})$ m at mesoscale (millimeter) regime [1]. Most thermal actuators employ either bimorph [2], solid expansion [3], fluid expansion [4], state change (liquid-to-vapor) [5], gas expansion/compression [6], or combustion based mechanisms [7]. Among them, state change and combustion based mechanisms are found to be suitable for large displacement and force generation at mesoscale as they benefit from the scaling laws of physics [5,7]. In particular, combustion-based miniature heat engines offer high power density to weight ratio and fast response, thus making ideal for applications that require high speed, large force, and large displacement strokes. These actuators have applications in exoskeleton [8], locomotion [9], and rehabilitation [10].

Unfortunately, thermal actuators or heat engines with sliding-piston architecture at mesoscale suffer from high friction, leakage, and heat losses, resulting in poor thermal efficiencies [11,12]. A method to improve the thermal efficiency is by eliminating the crankshaft assembly and associated friction losses [7]; this can be accomplished by implementing a flexible or compliant architecture (Fig. 1) instead of a sliding-piston architecture, which also offer other advantages —no leakage losses, simpler construction, and lower fabrication costs [13,14].

Research on the fundamental design of thermal actuators (heat addition/rejection cycle [7]) or heat engines (Otto cycle) [13,14] that employ compliant architecture are being studied through models [14], prototype fabrication and experiments [13]. First-principle based mathematical models are being developed to assess the performance of the compliant actuators/engines for a range of physical and operating parameters in both open and closed cycle operations. However, it is unclear whether such a thermal actuator/heat engine be analyzed or designed to operate in an open or a closed cycle.

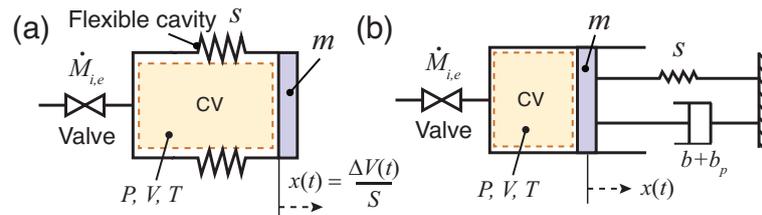


Figure 1. Proposed thermal actuator (a) schematic sketch and (b) lumped model. CV denotes the cavity or control volume with state parameters: pressure P , volume V , and temperature T at time t . The valve on the left is used for the intake or exhaust of the working fluid (air). The valve is connected to the ambient atmosphere (P_o, T_o) during the intake and exhaust processes. For the closed cycle, the valve remains closed over the entire operating cycle.

36 Our present work on thermal actuators builds on our prior physics-based modeling efforts of a
 37 resonant heat engine for portable power applications [7,13,14]. In this study, through a physics-based
 38 lumped-parameter model, similar to our previously developed models on free piston engines
 39 [15–17], we will investigate the behavior and performance of a mesoscale thermal actuator using
 40 a spring-mass-damper analogy and taking an air standard cycle approach. Here, using the model, we
 41 will predict the actuator performance for a range of operating conditions and report on the important
 42 differences between the open and closed cycle operations.

43 2. Thermal Actuator: Design and Model

44 The proposed actuator is similar to a traditional internal combustion engine, where fuel-air
 45 mixture is burnt in a piston-cylinder arrangement to produce force and displacement strokes. The
 46 actuator comprises of a flexible cavity with a piston attached at one end (Fig. 1). The flexible or
 47 compliant architecture reduces the frictional losses by up to 5% [13,14]. The actuator can be operated in
 48 both open and closed cycles. The actuator when operated in the open cycle comprises of compression
 49 (1 → 2), heat addition (2 → 3), expansion (3 → 4), exhaust (4 → 5 → 6), and intake (6 → 7 → 1)
 50 processes as depicted in Fig. 2. Unlike the open cycle, the closed cycle terminates with the heat rejection
 51 process (4 → 1). In the open cycle, the actuator exchanges both heat and mass with the surroundings,
 52 while in the closed cycle only exchange of heat takes place.

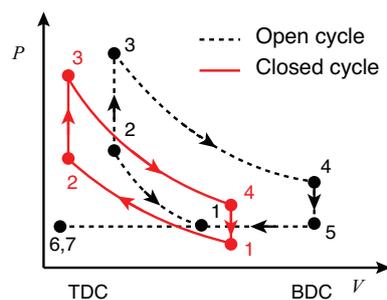


Figure 2. Ideal pressure-volume diagram of the actuator in open and closed cycle operations. Processes 1→2: Compression; 2→3: Heat addition for duration t_q ; and 3→4: Expansion. For closed cycle, process 4→1 is heat rejection for duration t_q . For open cycle, processes 4→5: Blowdown phase of exhaust; 5→6: Displacement phase of exhaust; 6→7→1: Intake. Note the piston positions at states 6 and 7 are 'Top Dead Center' (TDC) and states 4 and 5 are 'Bottom Dead Center' (BDC), respectively.

53 A physics-based model is derived to investigate the actuator behavior and performance for both
 54 the open and closed cycle operations. The actuator is modeled as a spring-mass-damper system by
 55 taking an air standard cycle approach [21] (Fig. 1b). The hollow cavity represents the control volume
 56 CV and contains the working fluid (air). The combustion process is modeled as a constant volume heat
 57 addition process to CV for a short duration $t_q \rightarrow 0$ and the heat rejection at the end of the expansion

58 process is modeled as a mass transfer process (for open cycle) or by applying a cooling pulse (for
 59 closed cycle) for a short duration $t_q \rightarrow 0$ (Fig. 3). The compliant cavity CV has a nominal volume V_o
 60 given by $V_o = LS$, where L is the nominal cavity length and S is the cross-sectional area of the cavity.
 61 The cavity has a stiffness s which allows horizontal displacement $x(t)$ of the piston m . Damper b
 62 models energy conversion which is the sum of both friction work and useful work by the actuator,
 63 and b_p (<0) models work done on the actuator during the intake process. Over an operating cycle, the
 64 working fluid temperature, $T_o + \Delta T(t)$, pressure, $P_o + \Delta P(t)$, and cavity volume, $V_o + \Delta V(t)$ undergo
 65 cyclic variation, where 'o' subscript represents nominal or ambient conditions, while Δ represents
 66 time-dependent excursion.

67 The actuator model Eqs. [1–5] is derived by employing Newton's second law, conservation of
 68 mass, conservation of energy, an ideal gas model, and a linear mass flow-rate equation.

$$\frac{m}{S^2} \Delta \ddot{V} + \frac{b + b_p}{S^2} \Delta \dot{V} + \frac{s}{S^2} \Delta V = \Delta P \quad (1)$$

$$\dot{M} = \dot{M}_i - \dot{M}_e \quad (2)$$

$$h \Delta T + \frac{d(Mc_v T)}{dt} + P \Delta \dot{V} = q + \dot{M}_i c_p T_i - \dot{M}_e c_p T \quad (3)$$

$$PV = MRT \quad (4)$$

$$\dot{M}_{i,e} = -k \Delta P \quad (5)$$

69 where M is the working fluid (air) mass, h is the total heat loss coefficient, R is the mass-specific gas
 70 constant of air, k is the mass flow rate coefficient, and c_v and c_p are the constant volume and constant
 71 pressure heat capacities of air. The overdot denotes time derivative, while the subscripts 'i' and 'e'
 72 denote intake and exhaust processes, respectively. The model Eqs. [1–5] is nondimensionalized using
 73 the scaling terms given in Eq. 6 and then written in a state space format as shown in Eqs. [7–10].

$$\Delta \bar{V} = \frac{\Delta V}{V_o}, \quad \Delta \bar{P} = \frac{\Delta P}{P_o}, \quad \Delta \bar{T} = \frac{\Delta T}{T_o}, \quad \bar{q} = \frac{q}{q_H}, \quad \text{and} \quad \bar{t} = t\omega \quad (6)$$

$$\frac{d\Delta \bar{V}}{d\bar{t}} = \Delta \dot{\bar{V}} \quad (7)$$

$$\frac{d\Delta \dot{\bar{V}}}{d\bar{t}} = \frac{\Delta \bar{P}}{\gamma} - \frac{b + b_p}{m\omega} \Delta \dot{\bar{V}} - \frac{s}{m\omega^2} \Delta \bar{V} \quad (8)$$

$$\Delta \dot{\bar{T}} = \frac{1}{Mc_v T_o \omega} \left[q + \dot{M}_i T_o [R + c_p \Delta \bar{T}_i - c_v \Delta \bar{T}] - h T_o \Delta \bar{T} - \dot{M}_e R T_o (1 + \Delta \bar{T}) - P_o V_o \omega (1 + \Delta \bar{P}) \Delta \dot{\bar{V}} \right] \quad (9)$$

$$\Delta \dot{\bar{P}} = \frac{1}{P_o V_o \omega (1 + \Delta \bar{V})} \left[(\dot{M}_i - \dot{M}_e) R T_o (1 + \Delta \bar{T}) + M R T_o \omega \Delta \dot{\bar{T}} - P_o V_o \omega (1 + \Delta \bar{P}) \Delta \dot{\bar{V}} \right] \quad (10)$$

74 where $\omega = \sqrt{\frac{\gamma P_o S^2}{m V_o}}$ is a reference frequency and the overbar denotes a nondimensional term.

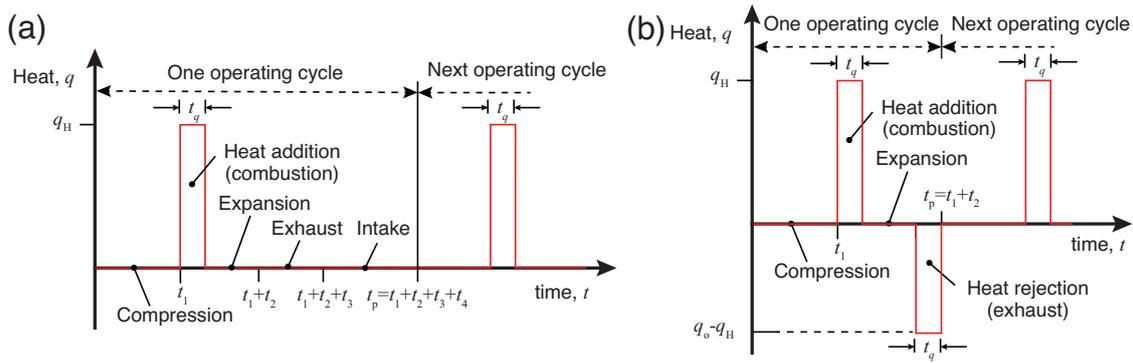


Figure 3. Heat-rate function q for modeling the (a) open and (b) closed operating cycles.

2.1. Solving the open cycle model

To generate a pressure-volume diagram, the model Eqs. [7–10] is numerically integrated in the order $1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \rightarrow 1$ (Fig. 2) starting with state 1: $\Delta \bar{V}_1, \Delta \bar{P}_1, \Delta \bar{T}_1, \Delta \dot{V}_1 = 0$. The resulting volume $\Delta \bar{V}_2$, pressure $\Delta \bar{P}_2$, and temperature $\Delta \bar{T}_2$ from the compression process, $1 \rightarrow 2$ is computed by integrating Eqs. [7–10] from the initial condition $\Delta \bar{V}_1, \Delta \bar{P}_1, \Delta \bar{T}_1, \Delta \dot{V}_1 = 0$ for a time \bar{t}_1 such that the piston velocity $\dot{V}_2 = 0$. The resulting volume $\Delta \bar{V}_3$, pressure $\Delta \bar{P}_3$, and temperature $\Delta \bar{T}_3$ during the heat addition process, $2 \rightarrow 3$ is computed from Eqs. 8 and 9 by assuming it to be instantaneous ($\Delta \bar{V}_3 = \Delta \bar{V}_2$ and $\Delta \dot{V}_3 = \Delta \dot{V}_2$). The volumes, pressures, and temperatures $\Delta \bar{V}_4, \Delta \bar{P}_4, \Delta \bar{T}_4$; $\Delta \bar{V}_6, \Delta \bar{P}_6, \Delta \bar{T}_6$; and $\Delta \bar{V}_1, \Delta \bar{P}_1, \Delta \bar{T}_1$ from the expansion $3 \rightarrow 4$, exhaust (displacement phase) $5 \rightarrow 6$, and intake processes $6 \rightarrow 7 \rightarrow 1$ are computed by integrating Eqs. [7–10] from the initial conditions $\Delta \bar{V}_3, \Delta \bar{P}_3, \Delta \bar{T}_3, \Delta \dot{V}_3 = 0$; $\Delta \bar{V}_5, \Delta \bar{P}_5, \Delta \bar{T}_5, \Delta \dot{V}_5 = 0$; and $\Delta \bar{V}_6, \Delta \bar{P}_6, \Delta \bar{T}_6, \Delta \dot{V}_6 = 0$ for times \bar{t}_2, \bar{t}_3 , and \bar{t}_4 respectively such that the piston velocity $\Delta \dot{V}_4 = \Delta \dot{V}_5 = 0$ and $\Delta \dot{V}_6 = \Delta \dot{V}_7 = 0$. The times $\bar{t}_1, \bar{t}_2, \bar{t}_3$, and \bar{t}_4 are unknowns and are determined during the process of integration. The blowdown process $4 \rightarrow 5$ is assumed instantaneous, isentropic, and occurs at zero piston velocity ($\Delta \dot{V}_4 = \Delta \dot{V}_5 = 0$) and ambient pressure ($\Delta \bar{P}_5 = 0$). The working fluid temperature at state 5, $\Delta \bar{T}_5$ is determined using the adiabatic relation:

$$\Delta \bar{T}_5 = (1 + \Delta \bar{T}_4) \left(\frac{1 + \Delta \bar{P}_4}{1 + \Delta \bar{P}_5} \right)^{\frac{1-\gamma}{\gamma}} - 1 \quad (11)$$

2.2. Solving the closed cycle model

To generate a pressure-volume diagram, the model Eqs. [7–10] is numerically integrated in the order $1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 1$ (Fig. 2) starting with state 1: $\Delta \bar{V}_1, \Delta \bar{P}_1, \Delta \bar{T}_1, \Delta \dot{V}_1 = 0$. The resulting volume $\Delta \bar{V}_2$, pressure $\Delta \bar{P}_2$, and temperature $\Delta \bar{T}_2$ from the compression process, $1 \rightarrow 2$ is computed by integrating Eqs. [7–10] from the initial condition $\Delta \bar{V}_1, \Delta \bar{P}_1, \Delta \bar{T}_1, \Delta \dot{V}_1 = 0$ for a time \bar{t}_1 such that the piston velocity $\dot{V}_2 = 0$. The resulting volume $\Delta \bar{V}_3$, pressure $\Delta \bar{P}_3$, and temperature $\Delta \bar{T}_3$ during the heat addition process ($2 \rightarrow 3$) is computed from equations 8 and 9 by assuming it to be instantaneous ($\Delta \bar{V}_3 = \Delta \bar{V}_2$ and $\Delta \dot{V}_3 = \Delta \dot{V}_2$). The volume, pressure, and temperature $\Delta \bar{V}_4, \Delta \bar{P}_4, \Delta \bar{T}_4$ from the expansion process $3 \rightarrow 4$ is computed by integrating Eqs. [7–10] from the initial conditions $\Delta \bar{V}_3, \Delta \bar{P}_3, \Delta \bar{T}_3, \Delta \dot{V}_3 = 0$ for time \bar{t}_2 such that the piston velocity $\Delta \dot{V}_4 = \Delta \dot{V}_1 = 0$. The times \bar{t}_1 and \bar{t}_2 are unknowns and are determined during the process of integration. The heat rejection process $4 \rightarrow 1$ is assumed to be instantaneous and occurs at zero piston velocity ($\Delta \dot{V}_4 = \Delta \dot{V}_1 = 0$).

3. Results and Discussion

The actuator with $h=0$ W/K, $b=21.5$ N-s/m, $k=6.8 \times 10^{-7}$ kg/s-Pa $\pm 20\%$, $V_0=21.8$ cc, $s=3050$ N/m, $m=0.18$ kg, and clearance volume $V_c=0.01V_0$ are treated as the reference. These numerical values are experimentally determined [13]. $T_0=295$ K and $P_0=93.4$ kPa are the ambient and standard conditions.

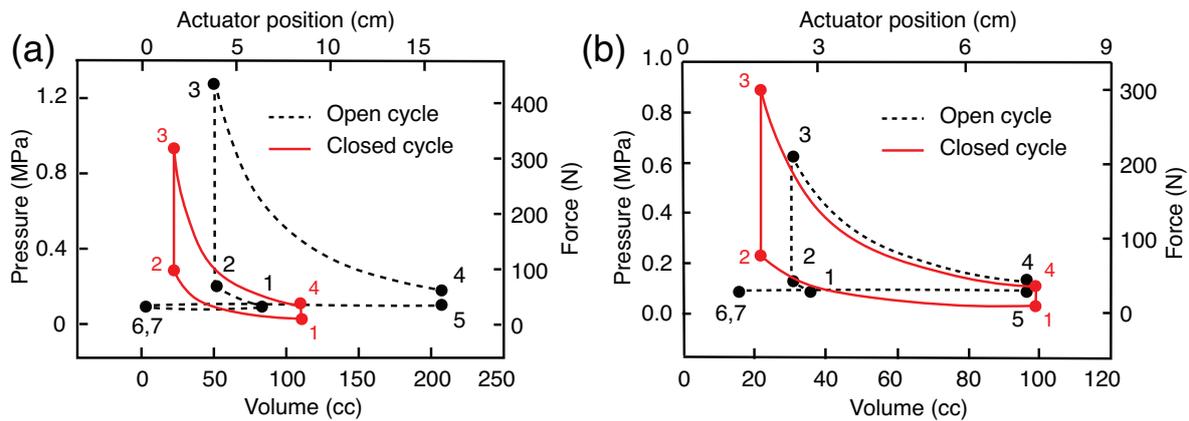


Figure 4. Open and closed cycle pressure-volume and force-displacement diagrams for (a) the reference actuator (b) an actuator with $b=27.5$ N-s/m, $b_p=-40$ N-s/m and $\phi=0.51$.

106 3.1. Pressure-Volume and Force-Displacement diagrams

107 The PV diagrams for both the open and closed cycles shown in Fig. 4 are generated by applying a
 108 heat pulse that corresponds to lean combustion (equivalence ratio $\phi=0.51$ [20]) of octane in the actuator
 109 (Fig. 3). The peak pressure P_3 in the actuator for the open and closed cycles are off by a factor of
 110 1.3 (Fig. 4a). Note that the temperature rise in both the cycles are equal ($\Delta T_{23}=2064$ K) because the
 111 equivalence ratio for both the cycles are equal ($\phi=0.51$). Also, note that the pressure rise ΔP_{23} among
 112 the cycles is different, as the density of air at the thermodynamic state 2 in both the cycles are unequal
 113 —for the closed cycle, the density at state 2 is 1.10 kg/m³, while for the open cycle, the density at state
 114 2 is 1.87 kg/m³. The actuator pressure at the end of heat rejection or blow down process is ambient
 115 pressure ($P_5=0$ kPa gage) and below the ambient pressure ($P_5=-11$ kPa gage) for the open and closed
 116 cycles, respectively. This is because the open cycle interacts with the surroundings via mass transfer
 117 that allows the actuator pressure to quickly equilibrate to the ambient conditions, while in the closed
 118 cycle there is no mechanism, that is, no mass transfer or heat transfer $h=0$ W/K to equilibrate the
 119 actuator pressure to the ambient conditions.

120 In the context of force and displacement generated, the actuator produces a peak force of up to
 121 400 N and displacement stroke of up to 16 cm (Fig. 4a). Note that the force generated is not uniform
 122 over the displacement range, but reduces in magnitude with the displacement.

Table 1. Comparison of the performance metrics for the reference actuator in closed and open cycles with equivalence ratio $\phi=0.51$.

Performance Parameter	Closed cycle	Open cycle
Indicated thermal efficiency (%)	47.66	38.41
Brake thermal efficiency (%)	44.33	34.64
Heat added per cycle (J/cycle)	35.6	138.5
Cycle frequency (Hz)	37.03	13.37
Compression ratio, CR	5.05	1.76
Expansion ratio, ER	5.05	4.13
Average piston speed (m/s)	4.75	4.77
Power output (W)	584.7	641.6
Mass of air in cylinder (kg/cycle)	2.41×10^{-5}	9.28×10^{-5}

123 The work done by the reference actuator in both the closed and open cycles for $\phi = 0.51$ are found
 124 to be 16.96 J and 53.19 J. These correspond to indicated thermal efficiencies of 47.66% and 38.41%,

125 respectively. The CR and ER for the closed cycle are equal to 5.05, while the CR and ER for the open
 126 cycle are found to be 1.76 and 4.13, respectively (Table 1). This result indicates that despite the same
 127 equivalence ratio ϕ the open and closed cycles respond differently with different performance metrics
 128 quantified in terms of stroke lengths, peak pressures, and indicated work.

129 For the reference actuator, the addition of extra load (an increment by 1.5 N-s/m), results in
 130 shorter displacement strokes, and the addition of external work modeled by $b_p = -40$ N-s/m during
 131 the intake process $7 \rightarrow 1$ results in significantly altering the PV diagram for the open cycle (comparing
 132 Fig. 4a and 4b). The actuator performance metrics for the open and closed cycles are given in Table 1.

133 3.2. Equivalence ratio and heat input relationship

134 For a specific fuel, an equivalence ratio is dependent on the mass of fuel injected (or associated
 135 heat input) and the mass of air inducted into the actuator [21]. Fig. 5 graphically shows the relation
 136 between heat input and corresponding equivalence ratio ϕ for the reference actuator in open and
 137 closed cycles. Each plot in the figure is obtained by supplying the actuator with varying heat, and
 138 the corresponding equivalence ratios are calculated based on the mass of air in the cavity CV at state
 139 1. It is clear from the figure that for a fixed equivalence ratio, the amount of heat added per cycle is
 140 higher for open cycle operation compared to a closed cycle operation. Furthermore, from the figure,
 141 the closed cycle operation holds a linear relationship between the equivalence ratio and heat input,
 142 while the open cycle holds a nonlinear linear for low ϕ (< 0.23) and eventually transmutes to linear
 143 higher ϕ (> 0.23). A similar observation has been reported in Ref. [14].

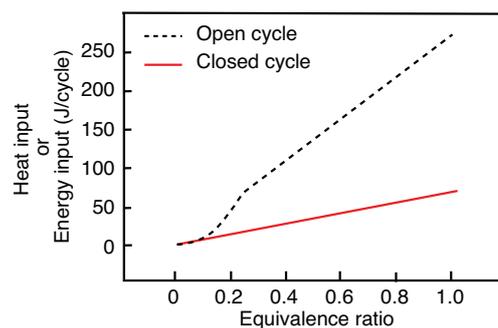


Figure 5. Relationship between the heat input and equivalence ratio for the reference actuator for open and closed cycle operations.

144 3.3. Efficiency and volume ratios

145 For a fixed equivalence ratio (say $\phi=0.5$), a difference of about 10% in indicated thermal efficiency
 146 is observed between the open and closed cycles (Fig. 6). The higher efficiencies of the closed cycle
 147 operations are because of ignoring the pumping losses in the actuator associated with the exhaust and
 148 intake processes. Furthermore, as can be seen in figure, an increase in the heat input or equivalence
 149 ratio ϕ increases the volume ratio (ER or CR). This is because a higher heat input or equivalence ratio ϕ
 150 will result in the higher pressure at the thermodynamic state 3 (Fig. 4), resulting in pushing the piston
 151 further outward and causing higher volume ratios.

152 3.4. Operating frequency and power output

153 It is evident from Fig. 7 that the operating frequency and output power from the actuator depends
 154 on the equivalence ratio. For the closed cycle, the operating frequency decreases monotonically
 155 with increasing equivalence ratio. On the contrary, for the open cycle, the operating frequency
 156 first decreases and later increases. This is because the actuator at state 6 (Fig. 2) reaches its lower
 157 displacement limit with a nonzero piston velocity—resulting in an abrupt changes the direction of

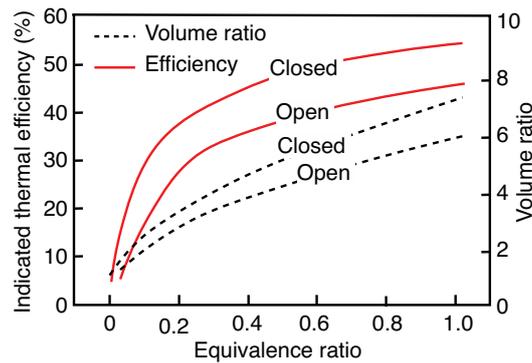


Figure 6. Efficiency and volume ratios for the reference actuator for open and closed cycles.

158 actuator motion—reducing the travel distance and time period or increasing the operating frequency
 159 of the operating cycle. For the reference actuator, the operating frequency for a closed cycle is 37.03 Hz
 160 while for an open cycle is 13.37 Hz. The operating frequency depends predominantly on the number
 161 of strokes involved in an operating cycle, higher the number of strokes lower is operating frequency.
 162 For instance, a closed cycle has two strokes, while an open cycle has four strokes.

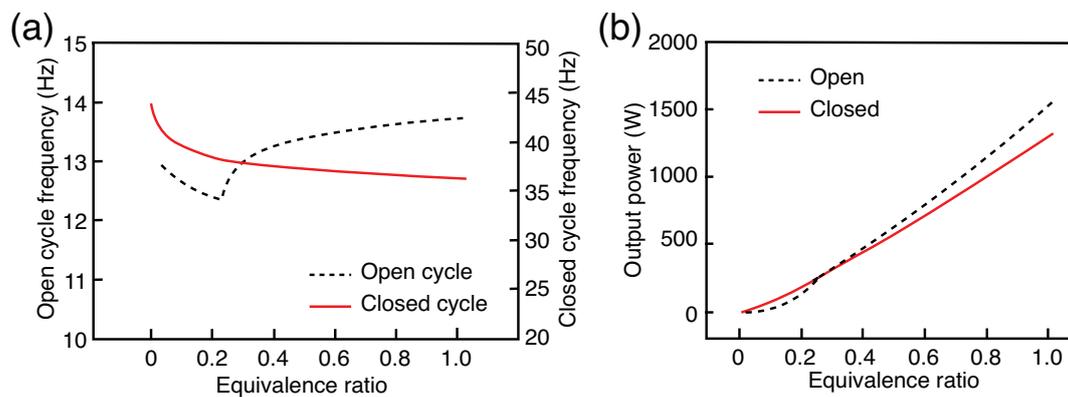


Figure 7. Performance metrics of the reference actuator in open and closed operating cycles: (a) Operating frequency and (b) Power output.

163 In the context of power output, the actuator produces a peak output power of up to 1500 W for
 164 an equivalence ratio of $\phi=1$ (Fig. 7b). The power output is a product of energy output and operating
 165 frequency of the actuator. Despite the operating frequency moderately increasing or decreasing, the
 166 trend in output power is fairly increasing —because the efficiency of the actuator and the energy input
 167 or output increases with the equivalence ratio ϕ (Figs. 5 and 6).

168 4. Conclusions

169 This work describes the difference in the behavior and performance of a mesoscale thermal
 170 actuator in both open and closed operating cycles. For this, a physics-based lumped parameter model
 171 of the actuator is derived using a spring-mass-damper analogy and taking an air standard cycle
 172 approach. Three observations are reported: (1) the mesoscale actuator can generate peak forces of up to
 173 400 N and displacement strokes of about 16 cm suitable for practical applications; (2) an increase in heat
 174 input to the actuator results in increasing the thermal efficiency of both open and closed cycles; and
 175 (3) for a specific heat input, both the open and closed cycle operations respond differently —different
 176 stroke lengths, peak pressures, and thermal efficiencies.

177 **Conflicts of Interest:** The author declares no conflict of interest.

178 Abbreviations

179 The following abbreviations are used in this manuscript:

180

ER	Expansion Ratio
CR	Compression Ratio
181 CV	Control Volume or Cavity
TDC	Top Dead Center
BDC	Bottom Dead Center

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