


Article

# Towards a Universal Semantic Dictionary

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**Abstract:** A novel method for finding linear mappings among word embeddings for several languages, taking as pivot a shared, universal embedding space, is proposed in this paper. Previous approaches learn translation matrices between two specific languages, but this method learn translation matrices between a given language and a shared, universal space. The system was first trained on bilingual, and later on multilingual corpora as well. In the first case two different training data were applied; Dinu's English-Italian benchmark data, and English-Italian translation pairs extracted from the PanLex database. In the second case only the PanLex database was used. The system performs on English-Italian languages with the best setting significantly better than the baseline system of Mikolov et al. [1], and it provides a comparable performance with the more sophisticated systems of Faruqui and Dyer [2] and Dinu et al. [3]. Exploiting the richness of the PanLex database, the proposed method makes it possible to learn linear mappings among an arbitrary number of languages.

**Keywords:** Natural Language Processing; Semantics; Word embeddings; Multilingual embeddings; Translation; Artificial Neural Networks

## 1. Introduction

Computer-driven natural language processing plays an increasingly important role in our everyday life. In the current digital world, using natural language for human-machine communication has become a basic requirement. In order to meet this requirement, it is inevitable to analyze human languages semantically. Nowadays, state-of-the-art systems represent word meaning with high dimensional vectors, known as word embeddings.

Current embedding models are learned from monolingual corpora, and therefore infer language dependency. But one might ask if the structure of the different embeddings, i.e. different meaning representations, are universal among all human languages. Youn et al. [4] proposed a procedure for building graphs from concepts of different languages. They found that these graphs reflected a certain structure of meaning with respect to the languages they were built of. They concluded that the structural properties of these graphs are consistent across different language groups, and largely independent of geography, environment, and the presence or absence of literary traditions. Such findings led to a new research direction within the field of computational semantics, which focuses on the construction of universal meaning representations, most of the times in the form of cross-lingual word embedding models [5]. One way to create such models is to find mappings between embeddings of different languages [1,6,7].

Our work proposes a novel procedure for learning such mappings in the form of translation matrices that serve to map each language to a universal space. The method was first tested on bilingual, and later on multilingual corpora as well. With the bilingual experiments, we obtained on Dinu's

35 benchmark data [3] a 0.377 precision@1 score for English-Italian and a 0.310 precision@1 score for  
36 Italian-English translation. These results, though, are far from the current state-of-the-art result on  
37 this dataset [7], but they are in the same order of magnitude or even better than many previous  
38 attempts [1–3]. For further bilingual and for some multilingual experiments an own dataset was  
39 created from the PanLex database [8]. We published the obtained scores of various experimental  
40 settings using this dataset [9]. Generally, bilingual experiments using only the PanLex dataset resulted  
41 in worse scores than using only Dinu’s dataset, but combining the two showed a slight improvement  
42 in the Italian-English direction. Multilingual experiments were carried out using three different  
43 languages, English, Italian, and Spanish, at the same time. The obtained pairwise precision values  
44 showed worse results, than when the system was trained in bilingual mode. However, these results  
45 are still promising considering that a completely new approach was implemented, and they showed  
46 that the system definitely learned from a data which is available for a wide range of languages.

47 Section 2 summarizes the progress made on learning translation matrices between word  
48 embeddings over the last five years. Section 3 discusses the proposed method in detail. Following  
49 that, Section 4 describes our experimental setup, and Sections 5 and 6 report and analyze the obtained  
50 results. Finally, Section 7 concludes the advantages and disadvantages of the proposed model, and  
51 also discusses some improvements for future work.

## 52 2. Related work

### 53 2.1. Word embeddings

54 One way to build semantic representations is to use distributional models. The idea is based on  
55 the observation that synonyms or words with similar meanings tend to occur in similar contexts, or as  
56 it was phrased by Firth in 1957: "You shall know a word by the company it keeps" [10]. For example,  
57 in the following two sentences "The cat is walking in the bedroom" and "A dog was running in a room"  
58 words like "dog" and "cat" have exactly the same semantic and grammatical roles, therefore we could  
59 easily imagine the two sentences in the following variations: "The dog is walking in the bedroom" and  
60 "A cat was running in a room" [11]. Based on this intuition, what distributional models are aiming to  
61 do is to compute the meaning of a word from the distribution of words around it [12]. The obtained  
62 meaning representations are usually high dimensional vectors, called word embeddings, which refer  
63 to their characteristic feature that they model a world by embedding it into a vector space.

### 64 2.2. Monolingual word embeddings

65 Mikolov et. al [13] suggested a Bag-of-words Neural Network, more specifically two architectures,  
66 for learning monolingual word embeddings. The first one, denoted as the Continuous Bag-of-Words  
67 Model (CBOW) tried to predict the current word based on the context, whereas the second one, denoted  
68 as the continuous skip-gram model tried to maximize the classification of a word based on another  
69 word in the same sentence. The CBOW turned out to be slightly better on syntactic tasks and the  
70 skip-gram on semantic tasks. Mikolov’s procedure has become known as the *word2vec*<sup>1</sup> procedure.

### 71 2.3. Multilingual word embeddings

In 2013, Mikolov et al. [1] published a simple two-step procedure for creating universal embeddings. In the first step they built monolingual models of languages using huge corpora, and in

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<sup>1</sup> <http://deeplearning4j.org/word2vec>

the second step a small bilingual dictionary was used to learn linear projection between the languages. The optimization problem was the following:

$$\min_W \sum_{i=1}^n \|Wx_i - z_i\|^2 \quad (1)$$

72 where  $W$  denotes the transformation matrix, and  $\{x_i, z_i\}_{i=1}^n$  are the continuous vector representations  
73 of word translation pairs, with  $x_i$  being in the source language space and  $z_i$  in the target language  
74 space.

75 Faruqui and Dyer [2] proposed a procedure to obtain multilingual word embeddings by  
76 concatenating the two word vectors coming from the two languages, applying Canonical Correlation  
77 Analysis. Xing et al. [14] found that bilingual translation can be largely improved by normalizing  
78 the embeddings and by restricting the transformation matrices into orthogonal ones. Dinu et al. [3]  
79 showed that the neighborhoods of the mapped vectors are strongly polluted by hubs, which are  
80 vectors that tend to be near a high proportion of items. They proposed a method that computes  
81 hubness scores for target space vectors and penalizes those vectors that are close to many words, i.e.  
82 hubs are down-ranked in the neighboring lists. Lazaridou et al. [15] studied some theoretical and  
83 empirical properties of a general cross-space mapping function, and tested them on cross-linguistic  
84 (word translation) and cross-modal (image labelling) tasks. They also introduced the use of negative  
85 samples during the learning process. Amar et al. [16] proposed methods for estimating and evaluating  
86 embeddings of words in more than fifty languages in a single shared embedding space. Since English  
87 usually offers the largest corpora and bilingual dictionaries, they used the English embeddings to  
88 serve as the shared embedding space. Artetxe et al. [17] built a generic framework that generalizes  
89 previous works made on cross-linguistic embeddings and they concluded that the best systems  
90 were the ones with orthogonality constraint and a global pre-processing with length normalization  
91 and dimension-wise mean centering. Smith et al. [6] also proved that translation matrices should  
92 be orthogonal, for which they applied Singular Value Decomposition (SVD) on the transformation  
93 matrices. Besides, they also introduced a novel “inverted softmax” method for identifying translation  
94 pairs. All these works listed above applied supervised learning. However, in 2017 Conneau et  
95 al. [7] introduced an unsupervised way for aligning monolingual word embedding spaces between  
96 two languages without using any parallel corpora. This unsupervised procedure holds the current  
97 state-of-the-art results on Dinu’s benchmark word translation task.

### 98 3. Proposed method

99 In summary, this work proposes a novel method for learning linear mappings between word  
100 translation pairs in the form of translation matrices. These translation matrices learn to map pre-trained  
101 word embeddings into a universal vector space. During training the cosine similarity of word  
102 translation pairs is maximized, which is calculated in the universal space. After mapping the  
103 embeddings of two different languages into this universal space, the cosine similarity of the actual  
104 translation pairs should be high. At test time the system is evaluated with the precision metric,  
105 principally used for word translation tasks.

#### 106 3.1. Cosine similarity and precision

107 Cosine similarity<sup>2</sup> is a measure of similarity between two non-zero vectors. It is calculated as the  
108 normalized dot product of two vectors, as shown in Equation 2. In fact, cosine similarity is a space  
109 that measures the cosine of the angle of two vectors. It is important to note that cosine similarity is  
110 not a proper distance metric, since the triangle inequality property does not apply. In word similarity

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<sup>2</sup> [https://en.wikipedia.org/wiki/Cosine\\_similarity](https://en.wikipedia.org/wiki/Cosine_similarity)

111 tasks, however, this metric is used for measuring the similarity of two words represented as word  
 112 vectors. Although cosine similarity values by definition are in range of  $[-1, 1]$ , in word similarity tasks  
 113 it is particularly used in positive space,  $[0, 1]$ , where parallel vectors are similar and orthogonal vectors  
 114 are dissimilar.

$$\text{cos\_sim} = \cos \theta = \frac{\vec{a} \cdot \vec{b}}{\|\vec{a}\| \cdot \|\vec{b}\|} \quad (2)$$

115 Precision is a metric used for measuring the performance of translator systems, which intend to  
 116 learn to translate from a source language into a target language. On the target side a look-up space is  
 117 defined, which could, for example, correspond to the most frequent 200K words of the target language,  
 118 as in our experiments. After translating a word, the  $N$  word vectors of the look-up space that are  
 119 closest to the translated one are regarded. The Precision @ $N$  metric denotes the percentage of how  
 120 many times the real translation of a word is found among the  $N$  closest word vectors in the look-up  
 121 space. Usual  $N$  values are 1, 5, and 10.

### 122 3.2. The objective function

123 The objective of the proposed method is to learn linear mappings in the form of translation  
 124 matrices that are obtained by maximizing the cosine similarity of gold word translation pairs in a  
 125 universal space. Therefore, for each language one single translation matrix is searched that maps the  
 126 language from its original vector space to the universal one. The method tries to bring the translation  
 127 pairs close together in a shared, universal space. Therefore, it is not only applicable for language pairs  
 128 but for any number of languages as well. The main advantage is that by introducing new languages  
 129 the number of the learned parameters remains linear to the number of languages since instead of  
 130 learning pair-wise translation matrices, for each language only one matrix is learned, the one that  
 131 maps directly to this shared, universal space.

132 Let  $L$  be a set of languages, and  $TP$  a set of translation pairs where each entry is a tuple of two in  
 133 the form of  $(w_1, w_2)$  where  $w_1$  is a word in language  $L_1$  and  $w_2$  is a word in language  $L_2$ , and both  $L_1$   
 134 and  $L_2$  are in  $L$ . Then, let's consider the following equation to optimize:

$$\frac{1}{|TP|} \cdot \sum_{L_1, L_2 \in L} \sum_{(w_1, w_2) \in TP} \text{cos\_sim}(w_1 \cdot T_1, w_2 \cdot T_2) \quad (3)$$

135 where  $T_1$  and  $T_2$  are translation matrices mapping  $L_1$  and  $L_2$  to the universal space. Since the equation  
 136 is normalized with the number of translation pairs in the  $TP$  set, the optimal value of this function is 1.  
 137 Off-the-shelf optimizers are programmed to find local minimum values, so during the training process  
 138 the loss function is multiplied by  $-1$ . Word vectors are always normalized, so the *cos\_sim* reduces to a  
 139 simple dot product.

140 At test time, first, both source and target language words are mapped into the universal space,  
 141 and from the most frequent 200k mapped target language words a look-up space is defined. Then, the  
 142 system is evaluated with the Precision metric, more specifically with Precision @1, @5, and @10. The  
 143 distance assigned to the word vectors when searching in the look-up space is the *cos\_sim*.

144 Previous works, such as Mikolov et al. [6] or Conneau et al. [7], suggested restricting the  
 145 transformation matrix to an orthogonal one. From an arbitrary transformation matrix  $T$  an orthogonal  
 146  $T'$  can be obtained by applying the SVD procedure. Our experiments showed that by applying SVD  
 147 on the transformation matrices the learning is significantly faster. Best results were obtained when  
 148 applying the SVD only once, at the beginning of the learning process.

## 149 4. Experimental setup

### 150 4.1. Pre-trained word embeddings

151 For pre-trained word embeddings we took the *fastText* embeddings published by Conneau et  
 152 al. [7]. These embeddings were trained by applying their novel method where words are represented as  
 153 a bag of character n-grams [18]. This model outperformed Mikolov's [13] CBOW and skipgram baseline  
 154 systems that did not take any sub-word information into account. Conneau's pre-trained word vectors  
 155 trained on Wikipedia are available for 294 languages<sup>3</sup>.

156 Some experiments were also run by using the same embedding that was used by Dinu et al. [3] in  
 157 their experiments. These word vectors were trained with *word2vec* and then the 200K most common  
 158 words in both the English and Italian corpora were extracted. The English word vectors were trained  
 159 on the WackyPedia/ukWaC and BNC corpora, while the Italian word vectors were trained on the  
 160 WackyPedia/itWaC corpus. This word embedding will be referred to as the *WaCky* embedding.

### 161 4.2. English-Italian setup of Dinu

162 Dinu et al [3] constructed an English-Italian gold dictionary split into a training and a test set  
 163 that is now being used as benchmark data for evaluating English-Italian word translation tasks. Both  
 164 training and test translation pairs were extracted from a dictionary built from Europarl Eng-Ita<sup>4</sup> [19].

165 For the test set they used 1500 English words split into 5 frequency bins, 300 randomly chosen in  
 166 each bin. The bins were defined in terms of rank in the frequency-sorted lexicon: [1-5K], [5K-20K],  
 167 [20K-50K], [50K-100K], and [100K-200K]. Some of these 1500 English words had multiple Italian  
 168 translations in the Europarl dictionary, so the resulting test set contained 1869 word pairs all together,  
 169 with 1500 different English, and with 1849 different Italian words (see Table 1).

170 For the training set, the above-mentioned Europarl dictionary was first sorted by the English  
 171 frequency. Then the top 5K entries were extracted and care was taken to avoid any overlap with the  
 172 test elements on the English side. On the Italian side, however, an overlap of 113 words was still  
 173 present. In the end, the training set contained 5K word pairs with 3442 different English, and 4549  
 174 different Italian words (see Table 1).

**Table 1.** Statistics of word counts.

Set	Language	No. words
Train (5000 word pairs)	Eng.	3442
	Ita.	4549
Test (1869 word pairs)	Eng.	1500
	Ita.	1849

### 175 4.3. The PanLex Corpus

176 PanLex [8] is a nonprofit organization that aims to build a multilingual lexical database from  
 177 available dictionaries in all languages. The name PanLex is coming from the words *panlingual* and  
 178 *lexical*, which reflect the main objective of this project. They are basically digitizing and centering the  
 179 content of different, already existing dictionaries made by domain experts. Own translations are not  
 180 accepted. To each translation pair a confidence value is assigned, which can be used for filtering the  
 181 extracted data. These confidence values are in the range of [1, 9], with 9 meaning high and 1 meaning  
 182 low confidentiality. The main purpose is to preserve the diversity of languages, so the collection

<sup>3</sup> <http://github.com/facebookresearch/fastText/blob/master/pretrained-vectors.md>

<sup>4</sup> <http://opus.lingfil.uu.se/>

Table 2. Sample of PanLex entries of the extracted tsv file.

English	Italian	Confidence values
Sarajevo	Sarajevo	9
euro	euro	9
simple	semplice	8
difficult	difficile	8
college	università	7
plausible	verisimile	7
sea	mare	6
sky	cielo	6
better	meglio	5
inform	informare	5
combustible	combustibile	4
office	ufficio	4
sorcerer	conscitore	3
it	ella	3
Great Wall of China	Grande muraglia cinese	2
factory workers	lavoratori dell'industria	2
stay	restare	1
sometimes	qualche volta	1

183 of "threatened" or "endangered" languages and dictionaries of rare language combinations are top  
 184 priority. Some examples of the English-Italian PanLex data can be seen in Table 2.

185 PanLex also exhibits different *language varieties* that include, among others, regional variations and  
 186 different writing systems. A *language variety* is denoted with a three-letter *language code*, e.g. eng for  
 187 English, and with a three-digit *variety code*, e.g. 000. To the most widely spoken variety of a language  
 188 usually the 000 *variety code* is assigned. When extracting data from the PanLex database, in all cases,  
 189 the *language variety* with the smallest *variety code* was taken.

#### 190 4.4. Dataset creation from PanLex

191 The procedure applied for extracting a proper data from the PanLex database for training  
 192 multilingual embedding models roughly follows the same steps as in [3]. After extracting the raw  
 193 translation pairs from the PanLex database, a filtered version of entries was formed by dropping  
 194 translations with a confidence value below 7 and those for which no word vector was found in the  
 195 *fastText* embedding. This results in an English-Italian word translation set containing 69,623 entries.

196 For the test set 1500 English words were taken and split into 5 frequency bins, 300 randomly  
 197 assigned to each bin. The bins were defined the same way as in [3], i.e., in terms of rank in the  
 198 frequency-sorted lexicon: [1-5K], [5K-20K], [20K-50K], [50K-100K], and [100K-200K]. In [7], the word  
 199 vectors sorted by their frequency in descending order were published, and this order was used as the  
 200 source of English word frequency data. In the PanLex database it is a common issue that one English  
 201 word has sometimes as many as 10 different Italian translations. Therefore, in order to avoid having  
 202 an undesirably huge test set with many Italian synonyms only those English words were selected, for  
 203 which in the corresponding bin only one Italian translation was present. This way the obtained test set  
 204 contains exactly 1500 word pairs, which are made up of 1500 different English words and their Italian  
 205 translations.

206 For the training set, the 69,623 entries were first sorted by their English frequency, then the top 5K  
 207 entries were extracted and, as in Dinu *et al.*, care was taken to avoid any overlap with test elements on  
 208 the English side. Then, the top 5K entries were selected in three different ways:

- 209 1. Simply the first 5K entries were taken.
- 210 2. The first 5K different English words were taken with the most frequent Italian translation.
- 211 3. Only those English words were taken for which only one Italian translation was present.

#### 212 4.5. Baseline experimental setting

213 For the baseline system the *fastText* embedding was used as a pre-trained embedding and the  
 214 system was trained on Dinu's English-Italian data. For parameter adjustment Dinu's training data was  
 215 split into train and validation sets such that no overlap was present on the English side, i.e. no word  
 216 appeared in both sets; this follows Dinu's procedure of constructing their original training and test  
 217 sets. It should be noted that this does not apply for Italian words. For the word count and overlap  
 218 statistics of Dinu's original training and test sets see Table 3 and for the same statistics of the newly  
 219 produced training and validation sets see Table 4.

**Table 3.** Statistics of the original train and test split of Dinu's data.

Number of English words	train	3442
Number of Italian words		4549
Number of English words	test	1500
Number of Italian words		1849
Overlap English		0
Overlap Italian		113

**Table 4.** Statistics of the new train and validation split of Dinu's data.

Number of English words	train	3098
Number of Italian words		4129
Number of English words	valid	344
Number of Italian words		499
Overlap English		0
Overlap Italian		80

220 The system was adjusted on the previously described training and validation split. For the  
 221 optimizer the tensorflow implementation<sup>5</sup> of the Adagrad algorithm [20] was used. For evaluation the  
 222 most frequent 200K words of the target space embedding were used as look-up space for calculating  
 223 Precision @1, @5, and @10. In all cases both English-Italian and Italian-English precision scores were  
 224 observed. In addition, the average cosine similarity value of the validation set was also checked.  
 225 During training and validation as well the precision and similarity values were all calculated in the  
 226 universal space. Gold dictionaries were constructed from the input data files themselves. Following  
 227 Dinu, any word appearing in the dictionary was considered a valid translation. Various translations  
 228 may come from synonyms or different male-female forms on the Italian side.

## 229 5. Experimental results

### 230 5.1. Parameter adjustment using Dinu's data

231 First, parameter adjustment was performed using Dinu's data, which gave 0.1 as the best learning  
 232 rate and 64 as the best batch size, where batch size is equal to the number of translation pairs used in  
 233 one iteration. With applying SVD only once at the beginning the obtained results of our best system  
 234 are significantly worse than state-of-the-art results on this benchmark data, but they are comparable  
 235 with or even better than some of the previous models discussed in Section 2.

<sup>5</sup> [https://www.tensorflow.org/api\\_docs/python/tf/train/AdagradOptimizer](https://www.tensorflow.org/api_docs/python/tf/train/AdagradOptimizer)

## 236 5.2. Experimenting with SVD

237 Previous works, such as [6] or [7], suggested restricting the transformation matrix to an orthogonal  
238 one. Based on these findings this system also features a configuration option of applying an SVD.  
239 Three different SVD modes were studied:

- 240 • 0: Not using SVD at all
- 241 • 1: Using SVD after every  $n$ -th epoch
- 242 • 2: Using SVD only once, at the beginning

243 In the following experiments the same datasets were used as for parameter adjustment. Learning  
244 rate was set to 0.1 and batch size to 64 as found the best setup before. Altogether 200 epochs were done  
245 and evaluation was performed on every 10-th epoch.

### 246 5.2.1. Not using SVD

247 This experiment was carried out without applying any SVD. Translation matrices were initialized  
248 with random numbers. Figure 1 shows that similarity values are monotone increasing, meaning that  
249 the system is learning. But the learning process is relatively slow since even after 200 epochs the  
250 similarity score is still quite low, bearing in mind that the optimal value is 1.0.

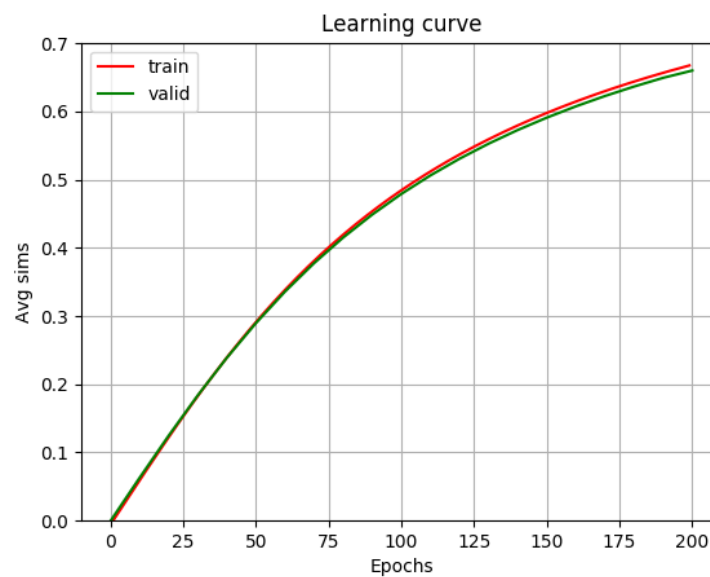
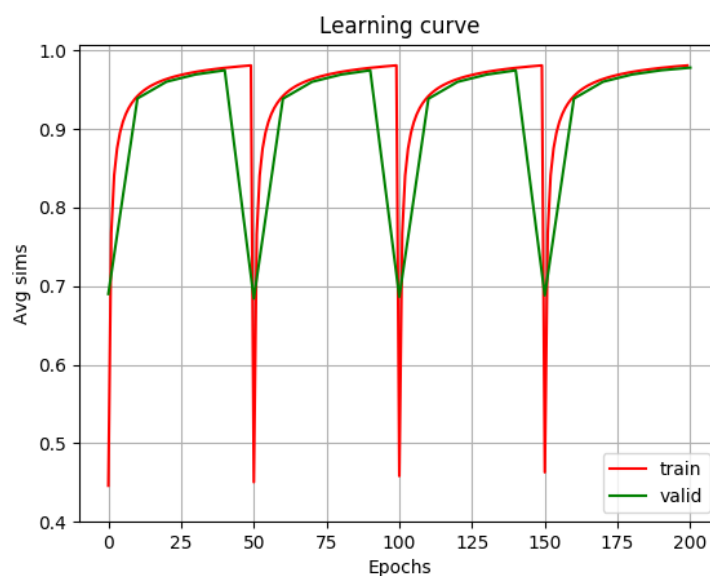


Figure 1. Learning curve of experimenting without using SVD (svd\_mode = 0).

### 251 5.2.2. SVD after every $n$ -th epoch

252 This experiment was carried out applying SVD several times over the whole learning process.  
253 SVD was made on every 50-th epoch, i.e. 4 times altogether. Figure 2 shows how the learning curve  
254 breaks down every time after applying an SVD on the translation matrices, and, also, how fast it is  
255 back once again to the previous high similarity values. Besides, this time the average cosine similarity  
256 score was higher even at the beginning than it was after 200 epochs with the previous setting, where  
257 no SVD was done. Applying SVD on the transformation matrices seems to accelerate the learning  
258 process significantly. The learning curve also shows that SVD-to-SVD fractions have exactly the same  
259 trajectory regardless of the number of previous epochs done.

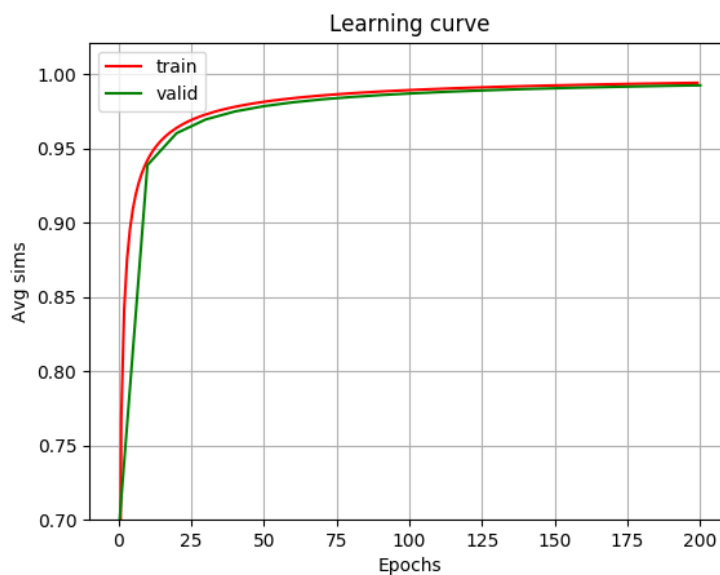




**Figure 2.** Learning curve of experimenting with SVD after every  $n$ -th epoch ( $svd\_mode = 1$ ).

### 260 5.2.3. SVD at the beginning

261 This experiment was carried out applying SVD only once, at the very beginning. This means,  
262 in simple terms, that instead of a random initial transformation matrix, the system tried to adjust an  
263 orthogonal one. Figure 3 shows that the learning curve is monotone increasing, and owing to the  
264 initial SVD it gets fairly high right at the beginning.



**Figure 3.** Learning curve of experimenting with SVD at the beginning ( $svd\_mode = 2$ ).

### 265 5.3. Experiments with the PanLex data

#### 266 5.3.1. Comparing different dataset construction methods

267 Tables 5 and 6 compare the results of different dataset construction methods. It is important  
 268 to note that in the first case the English word of the 5000-th translation pair is only the 845-th most  
 269 frequent English word, meaning that there is only 845 different English words in the training set and  
 270 that, on average, there is 5-6 different Italian translations to each of them. In the second case, where  
 271 every English word is kept but only with the most frequent Italian translation, this number is 9007.  
 272 In the last case, however, the 5000-th entry is made up of the 39426-th most frequent English and the  
 273 31543-th most frequent Italian words. Still, this last training set provides the best results, so for further  
 274 experiment this construction method was applied.

**Table 5.** English-Italian precision values with the different training sets.

<b>Precision</b>	<b>@1</b>	<b>@5</b>	<b>@10</b>
First 5K entry	0.0093	0.0253	0.0367
First 5K English words with retaining one translation	0.1120	0.2073	0.2427
First 5K English words with one translation	<b>0.1960</b>	<b>0.3087</b>	<b>0.3440</b>

**Table 6.** Italian-English precision values with the different training sets.

<b>Precision</b>	<b>@1</b>	<b>@5</b>	<b>@10</b>
First 5K entry	0.0000	0.0007	0.0007
First 5K English words with retaining one translation	0.1114	0.2052	0.2440
First 5K English words with one translation	<b>0.1838</b>	<b>0.3059</b>	<b>0.3443</b>

#### 275 5.3.2. Experimenting with different training set sizes

276 Table 7 summarizes the results of experiments with different training set sizes. The 3K dataset  
 277 proved to be the best on the English-Italian translation, but on the Italian-English it is only slightly  
 278 better, than the 5K dataset. This behaviour of performing better on the smaller training sets is fairly  
 279 understandable since as a consequence of the way the training set was constructed, as we are taking in  
 280 more and more entries, we are actually taking in less and less frequent English words and their Italian  
 281 translations, for which words neither the embedding nor the translations are precise enough. Since  
 282 Dinu's benchmark data contains 5K entries in the training set, despite the slightly worse performance  
 283 we kept using the 5K dataset for the sake of comparability with other result.

**Table 7.** Experiments with different training set sizes

Prec.	<b>Eng-Ita</b>			<b>Ita-Eng</b>		
	<b>@1</b>	<b>@5</b>	<b>@10</b>	<b>@1</b>	<b>@5</b>	<b>@10</b>
1K	0.1500	0.2847	0.3340	0.1391	0.2761	0.3256
3K	<b>0.2127</b>	<b>0.3473</b>	<b>0.3933</b>	<b>0.2232</b>	<b>0.3650</b>	<b>0.4152</b>
5K	0.1980	0.3193	0.3620	0.2212	0.3555	0.4030
10K	0.1613	0.2807	0.3227	0.1879	0.3012	0.3372

#### 284 5.4. Comparison of systems trained on Dinu's and PanLex data

285 In the next step, some experiments were made to determine which data is more apt for learning  
 286 linear mappings between embeddings. In order to compare all the experiments objectively subsets  
 287 of the original test sets were created. These subsets do not contain any English word present either  
 288 in the Dinu training set or in the PanLex training set. Table 8 summarizes the number of word  
 289 pairs in the old and the new test sets. It should be noted that by this reduction mainly the most

290 common English words are affected, and therefore worse scores are expected compared to the previous  
 291 train-on-Dinu-test-on-Dinu, or train-on-PanLex-test-on-PanLex top results. Scores on Dinu's test set  
 292 are shown in Table 9 and on the PanLex data in Table 10. The obtained results show that training on the  
 293 PanLex data cannot beat the system trained on Dinu's data, which performs better both on Dinu's and  
 294 on the PanLex test sets. Not even combining the two training sets succeeds in achieving significantly  
 295 better results, although on the PanLex test set it does improve the scores in the Italian-English direction.

**Table 8.** Word reduction of the new test sets

Test set	No. word pairs in old	No. word pairs in new
Dinu	1869	1455
PanLex	1500	1242

**Table 9.** Comparing Dinu's and PanLex data on Dinu's test set

Precision	Eng-Ita			Ita-Eng		
	@1	@5	@10	@1	@5	@10
Train:Dinu - Test:old	0.3770	0.5647	0.6245	0.3103	0.5018	0.5474
Train:Dinu - Test:new	<b>0.3560</b>	<b>0.5407</b>	<b>0.5978</b>	<b>0.2917</b>	<b>0.4792</b>	<b>0.5215</b>
Train:PanLex - Test:new	0.1360	0.2309	0.2594	0.1361	0.2556	0.2965
Train:Dinu+PanLex - Test:new	0.2930	0.4349	0.4861	0.2910	0.4556	0.5090

**Table 10.** Comparing Dinu's and PanLex data on the PanLex test set

Precision	Eng-Ita			Ita-Eng		
	@1	@5	@10	@1	@5	@10
Train:PanLex - Test:old	0.1960	0.3087	0.3440	0.1838	0.3059	0.3443
Train:PanLex - Test:new	0.1812	0.2858	0.3196	0.1668	0.2835	0.3213
Train:Dinu - Test:new	<b>0.2295</b>	<b>0.4171</b>	<b>0.4839</b>	0.2227	0.3763	0.4199
Train:Dinu+PanLex - Test:new	0.2295	0.3712	0.4275	<b>0.2498</b>	<b>0.4026</b>	<b>0.4495</b>

### 296 5.5. Continuing the training with PanLex data

297 Another experiment was conducted to continue the baseline system trained on Dinu's data with  
 298 the PanLex data. In other words, it is the same as initializing the translation matrices of the PanLex  
 299 training process with previously learned ones. The baseline system reaches its best performance  
 300 between 2000 and 4000 epochs, depending on which precision value is regarded. Table 11 shows that  
 301 on the English-Italian task there is no improvement at all, while on the Italian-English task with the  
 302 best setting slightly better scores are achieved on precision @1 and @10 values.

**Table 11.** Continuing the baseline system with the PanLex data.

Precision	Eng-Ita			Ita-Eng		
	@1	@5	@10	@1	@5	@10
Original	<b>0.3770</b>	<b>0.5647</b>	<b>0.6245</b>	0.3103	<b>0.5018</b>	0.5474
Cont. from 2000	0.3426	0.5256	0.5802	<b>0.3229</b>	0.4882	<b>0.5535</b>
Cont. from 3000	0.3535	0.5416	0.5970	0.3229	0.4840	0.5465
Cont. from 4000	0.3510	0.5273	0.5911	0.3118	0.4701	0.5243

### 303 5.6. Experiments using three languages

304 Finally, a multilingual experiment was carried out where the system was trained on three  
 305 languages - English, Italian, and Spanish - at the same time. During training the system learns  
 306 three different translation matrices, one for English-universal, one for Italian-universal, and one for  
 307 Spanish-universal space mapping. For example, in order to learn the English-universal translation

matrix, both the English-Italian and the English-Spanish dictionaries are used, according to Equation (3). Batches are homogeneous, but two following batches are always different in terms of the language origins of the contained data. That is, first an English-Italian batch is fed to the system, then an English-Spanish batch, after that an Italian-Spanish batch, and so on. First, bilingual models were trained in order to compare them later with the multilingual system. The results of the bilingual models are summarized in Table 12. Results are best on the Italian-Spanish task. Next, the system was trained using all the three languages at the same time. During the training process the model was evaluated on the bilingual test datasets of which the results are shown in Table 13. The obtained results show that no advantage was achieved by extending the number of languages, since the multilingual model performs worse than any of the pairwise bilingual models.

**Table 12.** Results of bilingual models trained pairwise on the three different languages.

Precision	L1-L2			L2-L1		
	@1	@5	@10	@1	@5	@10
Eng-Ita	0.2080	0.3280	0.3687	0.2082	0.3386	0.3904
Eng-Spa	0.2840	0.4320	0.4800	0.2883	0.4331	0.4836
Spa-Ita	0.3920	0.5340	0.5813	0.3655	0.5291	0.5750

**Table 13.** Bilingual results of the multilingual model trained using three different languages at the same time.

Precision	L1-L2			L2-L1		
	@1	@5	@10	@1	@5	@10
Eng-Ita	0.1573	0.2667	0.3127	0.1638	0.2942	0.3386
Eng-Spa	0.1947	0.2973	0.3447	0.2350	0.3538	0.4064
Spa-Ita	0.2520	0.3640	0.4160	0.2568	0.3723	0.4162

## 6. Comparison of the experiments

Tables 14 and 15 show our results on Dinu's dataset compared to other published works. Our results are worse than those current state-of-the-art, but they are still comparable or even better than several of previous attempts. The advantage of the proposed method compared to other procedures is that it is applicable for an arbitrary number of languages at the same time. Though the multilingual experiments on the PanLex dataset showed worse results than the bilingual ones, they are still showing convergence and can serve as a baseline for future multilingual experiments.

**Table 14.** Comparing English-Italian results on Dinu's data.

Eng-Ita	@1	@5	@10
Mikolov et al. (2013) [1]	0.338	0.483	0.539
Faruqui et al. (2014) [2]	0.361	0.527	0.581
Dinu et al. (2014) [3]	0.385	0.564	0.639
Smith et al. (2017) [6]	0.431	0.607	0.651
Conneau et al. (2017) [7]	0.662	0.804	0.834
Proposed method	0.377	0.565	0.625

**Table 15.** Comparing Italian-English results on Dinu's data.

Ita-Eng	@1	@5	@10
Mikolov et al. (2013) [1]	0.249	0.410	0.474
Faruqui et al. (2014) [2]	0.310	0.499	0.570
Dinu et al. (2014) [3]	0.246	0.454	0.541
Smith et al. (2017) [6]	0.380	0.585	0.636
Conneau et al. (2017) [7]	0.587	0.765	0.809
Proposed method	0.310	0.502	0.547

## 325 7. Conclusions and future work

326 This paper proposes a novel method for finding linear mappings between word embeddings in  
 327 different languages. As a proof of concept a framework was developed which enabled basic parameter  
 328 adjustments and flexible configuration for initial experimentation.

329 An interesting finding was that the system learned much faster when an initial SVD was applied  
 330 on the translation matrices. Results obtained with these settings on Dinu's data showed that the  
 331 proposed model did learn from the data. The obtained precision scores, though, were far from current  
 332 state-of-the-art results on this benchmark data, they were comparable with results of previous attempts.  
 333 The proposed model performed much better using the *fastText* embeddings [7], than using Dinu's  
 334 WaCky embeddings [3].

335 Thereafter, an English-Italian dataset was extracted from the PanLex database, from which training  
 336 and test datasets were constructed roughly following the same steps that Dinu et al. [3] took. The  
 337 system was trained and tested on both Dinu's and PanLex test sets, and in both cases the matrices  
 338 trained on Dinu's data were the ones reaching higher scores. On the PanLex data experiments with  
 339 different training set sizes were executed, out of which the 3K training set gave the best results.  
 340 Continuing the training of the matrices obtained by using Dinu's data with the PanLex dataset brought  
 341 a slight improvement on the Italian-English scores, but English-Italian scores only got worse.

342 Finally, the system was trained on three different languages at the same time. The obtained  
 343 pairwise precision values are proved to be worse than the results obtained when the system was  
 344 trained in bilingual mode. However, these results are still promising considering that a completely  
 345 new approach was implemented, and they showed that the system definitely learned from a data  
 346 which is available for a wide range of languages.

347 The approach is quite promising but in order to reach state-of-the-art performance the system  
 348 has to deal with some mathematical issues, for example dimension reduction in the universal space.  
 349 Further experimentation in multilingual mode with an extended number of languages could also  
 350 provide meaningful outputs. By involving expert linguistic knowledge various sets of languages could  
 351 be constructed using either only very close languages, or, on the contrary, using very distant languages.  
 352 Thanks to the PanLex database, bilingual dictionaries can easily be extracted, which can, then, be  
 353 directly used for multilingual experiments.

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 357 publish the results.

## 358 Abbreviations

359 The following abbreviations are used in this manuscript:

360

361 SVD Singular Value Decomposition

362 **References**

- 363 1. Mikolov, T.; Le, Q.V.; Sutskever, I. Exploiting similarities among languages for machine translation. *arXiv preprint arXiv:1309.4168* **2013**.
- 364
- 365 2. Faruqui, M.; Dyer, C. Improving vector space word representations using multilingual correlation. Proceedings of the 14th Conference of the European Chapter of the Association for Computational Linguistics, 2014, pp. 462–471.
- 366
- 367
- 368 3. Dinu, G.; Lazaridou, A.; Baroni, M. Improving zero-shot learning by mitigating the hubness problem. *arXiv preprint arXiv:1412.6568* **2014**.
- 369
- 370 4. Youn, H.; Sutton, L.; Smith, E.; Moore, C.; Wilkins, J.F.; Maddieson, I.; Croft, W.; Bhattacharya, T. On the universal structure of human lexical semantics. *Proceedings of the National Academy of Sciences* **2016**, *113*, 1766–1771.
- 371
- 372
- 373 5. Ruder, S.; Vulić, I.; Søgaard, A. A survey of cross-lingual word embedding models. *arXiv preprint arXiv:1706.04902* **2017**.
- 374
- 375 6. Smith, S.L.; Turban, D.H.; Hamblin, S.; Hammerla, N.Y. Offline bilingual word vectors, orthogonal transformations and the inverted softmax. *arXiv preprint arXiv:1702.03859 (published at ICRL2017)* **2017**.
- 376
- 377 7. Conneau, A.; Lample, G.; Ranzato, M.; Denoyer, L.; Jégou, H. Word translation without parallel data. *arXiv preprint arXiv:1710.04087* **2017**.
- 378
- 379 8. Kamholz, D.; Pool, J.; Colowick, S.M. PanLex: Building a Resource for Panlingual Lexical Translation. LREC, 2014, pp. 3145–3150.
- 380
- 381 9. Eszter, I.; Recski, G.; Borbély, G.; Castro-Bleda, M.J. Building a global dictionary for semantic technologies. Proc. Iberspeech, 2018, pp. 286–290. doi:10.21437/IberSPEECH.2018-60.
- 382
- 383 10. Firth, J.R. A synopsis of linguistic theory, 1930-1955. *Studies in linguistic analysis* **1957**.
- 384
- 385 11. Bengio, Y.; Ducharme, R.; Vincent, P.; Jauvin, C. A neural probabilistic language model. *Journal of machine learning research* **2003**, *3*, 1137–1155.
- 386
- 387 12. Jurafsky, D.; Martin, J.H. *Speech and language processing*; Pearson London, 2017.
- 388
- 389 13. Mikolov, T.; Chen, K.; Corrado, G.; Dean, J. Efficient estimation of word representations in vector space. *arXiv preprint arXiv:1301.3781* **2013**.
- 390
- 391 14. Xing, C.; Wang, D.; Liu, C.; Lin, Y. Normalized word embedding and orthogonal transform for bilingual word translation. Proceedings of the 2015 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, 2015, pp. 1006–1011.
- 392
- 393 15. Lazaridou, A.; Dinu, G.; Baroni, M. Hubness and pollution: Delving into cross-space mapping for zero-shot learning. Proceedings of the 53rd Annual Meeting of the Association for Computational Linguistics and the 7th International Joint Conference on Natural Language Processing (Volume 1: Long Papers), 2015, Vol. 1, pp. 270–280.
- 394
- 395
- 396 16. Ammar, W.; Mulcaire, G.; Tsvetkov, Y.; Lample, G.; Dyer, C.; Smith, N.A. Massively multilingual word embeddings. *arXiv preprint arXiv:1602.01925* **2016**.
- 397
- 398 17. Artetxe, M.; Labaka, G.; Agirre, E. Learning principled bilingual mappings of word embeddings while preserving monolingual invariance. Proceedings of the 2016 Conference on Empirical Methods in Natural Language Processing, 2016, pp. 2289–2294.
- 399
- 400
- 401 18. Bojanowski, P.; Grave, E.; Joulin, A.; Mikolov, T. Enriching word vectors with subword information. *arXiv preprint arXiv:1607.04606* **2016**.
- 402
- 403 19. Tiedemann, J. Parallel Data, Tools and Interfaces in OPUS. LREC, 2012, pp. 2214–2218.
- 404
- 405 20. Duchi, J.; Hazan, E.; Singer, Y. Adaptive subgradient methods for online learning and stochastic optimization. *Journal of Machine Learning Research* **2011**, *12*, 2121–2159.