1 Article

Measurement of viscoelastic properties for polymers by nanoindentation

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10 Abstract: A method for measuring the mechanical parameters of viscoelastic polymers by 11 nanoindentation technology was proposed and verified. Through the mechanical response of load-12 displacement curves at different loading rates, then creep compliances and relaxation modulus were 13 fitted. Polyimide thin film was employed in this research and experiments for five different loading 14 rates were conducted. The fitting load-displacement loading curves obtained by the inversion 15 method were identical to the experimental curves at five different loading rates, confirming the 16 validity of the method. Moreover, with the loading rates increased, the fitting curves were more 17 consistent commensurately with the nanoindentation experiment. DMA experiments were tested, 18 and the generalized Kelvin/ Maxwell model were used for fitting experiment data. Results from 19 DMA tests generally agree well with data from nanoindentation method, thereby verifying the 20 feasibility of the method. The Prony series obtained by the two methods were used to simulate the 21 creep experiments, which further verified the method.

Keywords: nanoindentation; viscoelasticity; creep compliance; relaxation modulus; Prony
 series

24

25 1. Introduction

26 With the increasing use of very small structures, nanocomposites and other micro-materials in 27 various engineering areas such as optic, mechanical, electric and micro-electromechanical systems, a 28 critical evaluation of the mechanic behavior is needed to predict the reliability of such materials [1-29 5]. Traditional mechanical testing is not suitable for small-scale or local performance testing due to 30 the limitations of sample size, experimental conditions and test resolution [6-9]. Nanoindentation 31 technology has become one of the most important methods for small-scale measurement because of 32 its advantages of high resolution, simple sample preparation and non-destructive testing [10-14]. For 33 general materials, nanoindentation technology can easily acquired hardness and elastic modulus, and 34 more importantly, in the plastic region, the inversion calculation of constitutive relation can be 35 carried out by dimensional analysis [15-17]. However, for time-dependent materials, the viscoelastic 36 parameters cannot be directly measured, and the inversion calculation method proposed by previous 37 researchers is not suitable, so how to obtain the mechanical properties of viscoelastic materials is one 38 of the emphases. Unfortunately, there are few studies on calculation of viscoelastic parameters using 39 nanoindentation.

Pal Jen Wei et al. [18] proposed the combination of one dashpot in series with one Kelvin model
and two Kelvin models with distinct time constants in series to describe the deformation of polymers
under indentation tests. A coupled experimental/numerical approach for the characterization of the
local mechanical behavior of epoxy polymer materials was proposed by M. Minervino et al. They

44 found that the pure viscoelastic constitutive law is not able to reproduce the local polymer behavior

45 and needs be enhanced by adding material softening behavior [19]. Menčík J et al. [20] proposed a 46 model consist of spring, plastic element, dashpot and two Kelvin–Voigt bodies to calculate the load 47 response of viscoelastic-plastic materials, including biological and restorative biomaterials. In 48 addition, some other models for viscoelastic polymers have been proposed as well [21-26]. Although 49 efforts have been made to explain the viscoelastic properties of polymers, the models suggested in 50 the previous studies are either very complex, resulting in time-consuming calculations or based on 51 complex input data, such as complex loading profiles. On the other hand, the parameters obtained 52 cannot be directly applied to engineering mechanical calculations, especially for simulation 53 calculations.

54 The paper will propose and validate a method to directly calculate the viscoelastic 55 parameters using nanoindentation test. The polyimide thin film (PI) was used to 56 validate this method in this paper. The method can be acquiring creep compliance 57 and relaxation modulus based on nanoindentation experiments at different loading 58 rates. Comparatively, the DMA creep experiments were carried out, and then the 59 viscoelastic parameter fitted by the generalized Kelvin/ Maxwell model, so that they 60 can be used to compare with the results of nanoindentation method. Finally, Prony 61 series calculated by the two methods are used in the creep simulation for verifying

62 the method.

63 2. Theoretical background

64 The nanoindentation test can be regarded as a process in which a rigid indenter is gradually 65 pressed into an elastic half-space. For a conical indenter, the relationship between load and 66 displacement can be obtained by Sneddon contact model [27, 28].

$$P = \frac{4}{\pi (1 - \upsilon) \tan \alpha} Gh^2 \tag{1}$$

67 Similarly, according to this line of thought, when testing viscoelastic materials, the experimental 68 process can be regarded as a quasi-static boundary issue between rigid indenter and semi-infinite 69 space materials with time dependence. The difference between them is that viscoelastic materials 70 have creep or relaxation characteristics due to their time dependence properties. Therefore, how to 71 introduce time variable into contact model is a key factor. Load-displacement curve involves time 72 factors such as loading rate, holding time, unloading rate, etc. In this paper, loading rate was used to 73 express time variables.

According to Riande's research[29], the hereditary integral operator is introduced to equation(1) leads to the relationship between displacement and load:

$$h^{2}(t) = \frac{\pi (1-\nu) \tan \alpha}{4} \int_{0}^{t} J(t-\xi) [\frac{dp(\xi)}{d\xi}] d\xi$$
(2)

76 where J(t) is the creep compliance.

The indentation load could be shows as $P(t) = v_0 t H(t)$ by the constant loading rate, where v_0 being the loading rate and H(t) the Heaviside unit step function. Let substitute P(t) into equation(2), we have

$$h^{2}(t) = \frac{\pi (1-\nu)v_{0} \tan \alpha}{4} \int_{0}^{t} J(t-\xi)d\xi$$
(3)

80 Differentiating equation (3) with respect to *t*, we have

$$J(t) = \frac{8h}{\pi(1-\nu)\tan\alpha} \frac{dh}{dp}$$
(4)

81

The general representation of the creep compliance based on the Kelvin model is

$$J(t) = J_0 + \sum_{i=1}^{N} J_i (1 - e^{-t/\tau_i})$$
(5)

- 82 where $J_0, J_1, J_2, ..., J_n$ are compliance numbers, $\tau_1, \tau_2, ..., \tau_n$ are retardation times, and *N* is a 83 positive integer.
- 84 Substituting equation (5) into equation (4), we have

$$h^{2}(t) = \frac{1}{4}\pi(1-\nu)\tan\alpha[(J_{0} + \sum_{i=1}^{N}J_{i})P(t) - \sum_{i=1}^{N}J_{i}\nu_{0}\tau_{i}(1-e^{-P(t)/(\nu_{0}\tau_{i})})]$$
(6)

Equation (6) is the viscoelastic contact model based on nanoindentation technology. Apply the nanoindentation experiments at different loading rates, the relationship between loads and displacement squares can be obtained, and different creep parameters can be fitted soon. Therefore, the equation can analyze the viscoelastic relationship of time-dependent materials. According to the Laplace transformation, there is a conversion relationship between creep compliance and relaxation modulus in the Laplace domain, as shown in the equation (7), hence the relaxation modulus can be obtained by creep compliance [30].

$$E(t) = L^{-1}\{\tilde{E}(s)\} = L^{-1}(\frac{1}{s^2 \tilde{J}(s)})$$
(7)

92 where E(t) is relaxation modulus, $L\{\}$ is Laplace operator.

93 3. Experiments

A commercial polyimide thin film was adopted in our study. The polyimide precursor reacted from the pyromellitic dianhydride (PMDA) and p,p'-oxy-dianline (ODA). Specimen surface was cleaned and all specimens were aged for approximately 48 hours before nanoindentation tests. All nanoindentation tests were performed at room temperature. Nanoindentation experiments were carried out in a stress loading manner, and the constant loading is 10 mN. Five fixed loading rates of 2 mN/s, 1 mN/s, 0.5 mN/s, 0.1 mN/s and 0.05 mN/s were tested, respectively. For each sample, at least five tests were conducted to calculate the average value of the mechanical parameters.

101 Similarly, after the surface cleaning, samples were prepared by the mechanical cutting for DMA 102 creep tests. The creep tests of PI film were performed with film tension mode using DMA Q800 (TA 103 Instruments, DE, USA) dynamic mechanical analyzer. The DMA tests were performed under 104 controlled stress. In order to improve the accuracy of the tests, a preliminary test was carried out at 105 room temperature with the constant stress equal to 0.1MPa. Immediately after the preliminary test, 106 the samples were keeping 30 min at the test temperature. The initial stress was 5MPa. Therefore when 107 the stress reached the setting point, the value of strain with time change was recorded, and then the 108 creep curves were obtained.

109 4. Results and discussion

110 The experimental curves of nanoindentation are shown in Fig. 1. It is obvious that when the 111 maximum loads in the same value, different loading rates show the same trend of variation, however,

- 112 show the different maximum displacements. This indicates that polyimide film has time dependence,
- 113 so when the time for reaching the maximum load is different, causing different curve values.



114

Figure 1. The load-displacement curves for PI materials by nanoindentation under different loadingrates.

117 It is noteworthy that when the loading rate is larger, the load-displacement curves obtained by 118 the experiment basically coincide with each other. With the decrease of loading rate, the discrete 119 phenomenon of load-displacement curve begins to appear. The slower the loading rate, the more 120 obvious the discrete phenomenon of displacement curves. This is because the polyimide thin film is 121 viscoelastic material, which is time-dependent. When the loading rate is slower, thus the loading time 122 is longer. Therefore, creep phenomenon occurs during the loading process, which is consistent with 123 the research in other literature [31-33].

124 According to the nanoindentation test data and the equation (5), the relationship between $h^2(t)$ 125 and P(t) under different loading rates can be obtained, the creep compliance can be can be 126 analyzed.

127 Owing to the angle between the indenter and the measured material plane is 19.7°, the equation128 (6) can be simplified as follows

$$h^{2}(t) = 0.1883[(J_{0} + \sum_{i=1}^{N} J_{i})P(t) - \sum_{i=1}^{N} J_{i}v_{0}\tau_{i}(1 - e^{-P(t)/(v_{0}\tau_{i})})]$$
(8)

- 130 get
- 131 when the loading rate is 2 mN/s,

$$h^{2}(t) = 0.1883[0.0012953P(t) - 0.00319(1 - e^{-P(t)/18.46}) - 0.0054(1 - e^{-P(t)/172.42}) - 0.3068(1 - e^{-P(t)/2000})]$$
(9)

132 when the loading rate is 1 mN/s,

$$h^{2}(t) = 0.1883[0.0012953P(t) - 0.001596(1 - e^{-P(t)/9.32}) - 0.0027(1 - e^{-P(t)/86.21}) - 0.1534(1 - e^{-P(t)/1000})]$$
(10)

133 when the loading rate is 0.5 mN/s,

$$h^{2}(t) = 0.1883[0.0012953P(t) - 0.000798(1 - e^{-P(t)/4.66}) - 0.00135(1 - e^{-P(t)/43.105}) - 0.0766(1 - e^{-P(t)/500})]$$
(11)

134 when the loading rate is 0.1 mN/s,.

$$h^{2}(t) = 0.1883[0.0012953P(t) - 0.0001596(1 - e^{-P(t)/0.932}) - 0.00027(1 - e^{-P(t)/8.621}) - 0.01532(1 - e^{-P(t)/100})]$$
(12)

135 when the loading rate is 0.05 mN/s,

$$h^{2}(t) = 0.1883[0.0012953P(t) - 0.0000798(1 - e^{-P(t)/0.466}) - 0.000135(1 - e^{-P(t)/4.315}) - 0.00766(1 - e^{-P(t)/50})]$$
(13)

136 The fitted loading curve can be inversed by the equations (9)-(13), and then compared with the 137 loading curve of nanoindentation experiment, as shown in Fig. 2. It can be seen that the loading curve 138 under five different loading rates calculated by viscoelastic contact model of nanoindentation is 139 consistent with the nanoindentation experiment, and the value dispersion is smaller, especially in the 140 case of shallow indentation depth. It can also be seen that with the increase of the loading depth, the 141 fitting curve and the experimental curve have certain discrete deviation. However, the overall fitting 142 degree is good, which verifies the validity of the function based on nanoindentation technology. It 143 can be seen that with the increase of loading rate, the position of discrete points in the loading curve 144 is larger, which fully demonstrates the viscoelastic behavior of polyimide film. At the same time, it 145 also shows that the function proposed in this paper is applicable to the shallow loading depth 146 experiments, and with the increase of indentation depth, the error gradually appears.



147



Figure 2. Fitting curves and discrete points at different loading rates. (a)2mN/s, (b)1mN/s ,(c)0.5mN/s, (d)0.1mN/s ,(e)0.05mN/s, (f) discrete points at different loading rates



$$J(t) = 0.0009397 + 0.0001712(1 - e^{-t/9.23}) + 0.00003104(1 - e^{-t/86.21})$$

+0.0001534(1 - e^{-t/1000}) (14)

Fig.3 is the creep compliance curves comparison obtained between the inversion of viscoelastic contact model based on nanoindentation technology and DMA creep experiments. It can be

153 concluded that the two curves have the same development trend, less discrete in creep compliance

154 values and in good fitting degree with the increase of time. These proved that the viscoelastic contact

model based on nanoindentation technology is reasonable, and the creep compliance calculation

156 method based on nanoindentation experiment is feasible.

157



158 Figure 3. Creep compliance comparisons between derived from nanoindentation experiment and159 DMA test.

According to the equation (7), the calculated creep compliance can be converted into relaxationmodulus, and it can be concluded that:

$$E(t) = 775 + 104.4e^{-t/20} + 40.85e^{-t/200} + 76.44e^{-t/1200}$$
(15)

Similarly, the creep compliance calculated by DMA experiment can transformed for relaxation
 modulus. By introducing the parameters into the 3-element generalized Maxwell model (Supporting
 Information), the equation can be obtained:

$$E(t) = 771.4 + 45.93e^{-t/20} + 45.58e^{-t/300} + 76.67e^{-t/1200}$$
(16)

Fig.4 is the comparison of relaxation modulus between the transformed of DMA creep experiment, fitted by 3-element Maxwell model and calculated by viscoelastic contact model based on nanoindentation. It can be concluded that the three types of data have good fitting degree, which indicates that the results from the viscoelastic contact model is consistent with those from the traditional viscoelastic model, and verified the method.



170



173 To be concluded, the viscoelastic model based on nanoindentation technology can calculate both 174 the relaxation modulus and creep compliance. The calculated results are basically consistent with the 175 traditional experiments, so it provided a new method to acquire viscoelastic properties.

176 5. FEM simulation

177 In order to further verify the viscoelastic parameters obtained by nanoindentation, the FEM is 178 used to simulate creep test. The same size as the DMA test sample is selected to establish the 179 geometric model, as shown in Fig.5. In this model, three-dimensional C3D8R element and hexahedral 180 mesh are used. One end of the finite element geometric model is fully constrained and the opposite 181 side is imposed with initial stress without constraint for other aspects.



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183

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Figure 5. The simulation geometric model of PI thin film.

184 The simulation is carried out in two steps. The first step is quasi-static loading with the purpose 185 to exert the initial stress; the second step is viscous loading, keeping the initial stress for 30 min, and 186 observing the occurrence of creep phenomena in this time range. The parameters input to the model 187 are Prony series converted by the creep compliance, as shown in Table 1.

Prony series	DMA test	Nanoindentation
G1=K1	0.0489	0.1047

Table 1. Prony series under two methods.

G2=K2	0.0485	0.0410
G3=K3	0.0816	0.0767

189 Fig.6 is the comparison of the creep results between the input two types of Prony series and 190 experiment. It can be seen that the simulation curves obtained by the two methods are well consistent 191 with the experimental curves of DMA. The experimental data curves are slightly lower than the 192 simulated data curves, but the overall error is small, which verifies the accuracy of the method. It is 193

proved that the viscoelastic model based on nanoindentation can be applied to polyimide materials,

194 and it also provides a calculation method for other viscoelastic polymers.



195



Figure 6. The comparison of simulation results under three types of viscoelastic parameter.

197 6. Conclution

198 A contact model for measuring viscoelastic parameters based on nanoindentation was proposed 199 and validated. The viscoelastic mechanical response of load-displacement curve was achieved by 200 nanoindentation experiments at different loading rates. The fitted viscoelastic parameters of the 201 polyimide film were identical to the values fitted by traditional DMA experiments, confirming the 202 rationality of the method. The fitting loading curves at five different rates were obtained by the 203 inversion method, which were nearly the same as the loading curves of nanoindentation experiments. 204 Moreover, the fitting curves were more consistent with the bigger loading rates. Based on the Prony 205 series of the generalized Kelvin model, the finite element numerical simulation was conducted, 206 further confirming the feasibility of this method and providing a new idea for viscoelastic polymer 207 materials which in small scale.

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