

Carbon Dioxide Emission Prediction of Four CIS Countries by Applying a Correlation and GMDH Artificial Neural Network

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Abstract

Increase in the emission of Greenhouse Gases (GHS) is among the significant concerns of government, societies, and policy-makers. Due to the highest share of carbon dioxide in the produced GHGs, it is necessary to assess the factors that influence its emission. Energy systems and economic activities noticeably influence the amount of carbon dioxide production of countries. In this article, Artificial Neural Network (ANN) in addition to a linear correlation used to predict carbon dioxide emission of four CIS countries, including Turkmenistan, Uzbekistan, Kazakhstan, and Azerbaijan based the consumption of various energy sources and GDP, as the economic indicator. According to the obtained data by the proposed models, carbon dioxide emission can be estimated by utilizing the mentioned input data. Models' R-squared value are 0.9997 and 0.9999 in the cases of applying the correlation and ANN-based model. Moreover, the average absolute relative deviations by utilizing the correlation and GMDH ANN are approximately 1.05% and 0.61%, respectively. These statistical values demonstrate more proper performance of the ANN-based model compared with the applied linear correlation.

Keywords: Artificial Neural Network; Carbon dioxide; Greenhouse gases; GMDH; GDP

1. Introduction

Studies have shown that the economic activities influences on energy consumption. Also, the emission of greenhouse gases (GHGs) depends on the energy system and its features [1]. Increase in energy consumption causes a higher production of GHGs due to the noticeable share of fossil fuels in the current energy systems [2]. World energy consumption and carbon dioxide emission have significantly increased in recent decades, as illustrated in Figure 1. As it is represented, the world's total primary energy consumption increased from about 6627.1 *Mtoe* in 1980 to more than 13511 *Mtoe* in 2017. In a similar period, the carbon dioxide emission had increment form approximately 18364 *Mt* to more than 33440 *Mt*. Moreover, it can be observed that the trend of carbon dioxide emission and energy consumption is very similar to each other, which indicates their dependency. In addition to energy utilization, level of economic activities has an impact on GHGs emission.

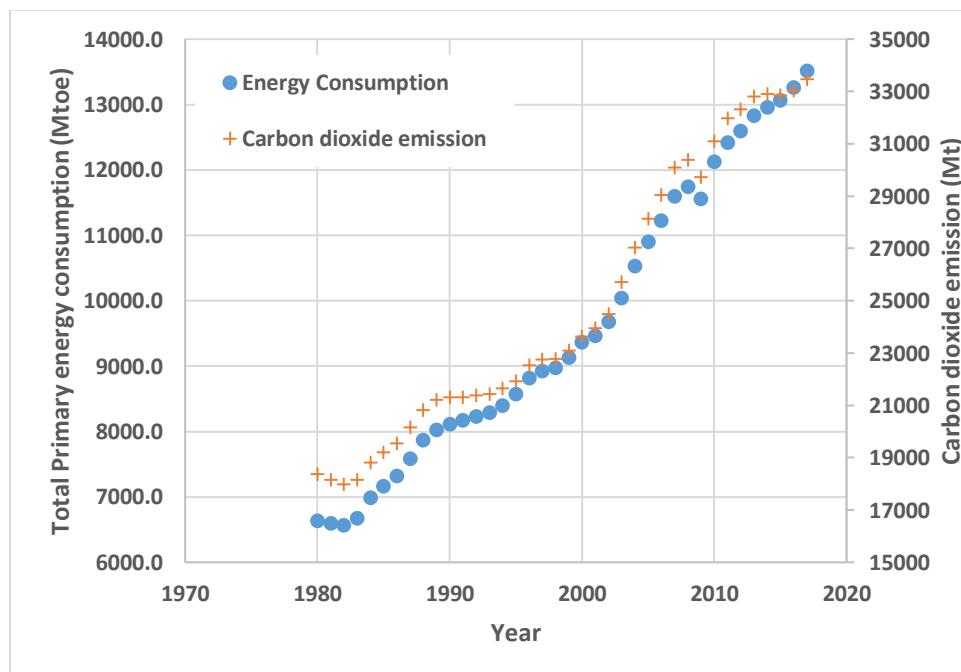


Figure 1 Total primary energy consumption and carbon dioxide emission of the world [3]

The increasing rate of energy consumption is mainly attributed to development in industrial and economic activities, increment in population, and improved quality of life. Various ways are suggested to overcome the energy-related GHG emission, such as improving the efficiency of the technologies, using renewable energy sources, energy recovery, and energy audit [4–6]. Due to the lower GHG emission of renewable energies in comparison with fossil fuels such as oil and coal [7,8], there are several worldwide renewable energy projects [9–11]. Wind and solar energy projects are among the most attractive and fast-growing types of renewable energy technologies applicable to power generation, cooling, and heating [12,13]. In order to model the energy system of a country, it is necessary to consider the share of various sources in the overall energy consumption; therefore, both renewable sources and different kinds of fossil fuels must be considered.

Various mathematical approaches are applicable to model the systems and forecast their behavior [14–16]. Among the several methods used for system modeling, artificial neural networks (ANNs) have proved their high-level precision due to their intelligent procedure and structure [17,18]. ANNs are used for recognition of patterns and estimating the output of a system based on defined inputs [18–20]. The accuracy of the ANN-based model is highly dependent on the selection of input data. According to a study conducted by Rezaei et al. [1] employed consumptions of energy sources and GDP as input data is appropriate to accurately estimate carbon dioxide of some Nordic countries [21]. In their study, the maximum value of absolute error was lower than 4%, showing acceptable precision of the introduced model.

Since the prediction of carbon dioxide emission gets an appropriate insight into the potential ways of its reduction, it is crucial to obtain a comprehensive and precise model. In this article, GMDH ANN, as a powerful predictive approach, is used for estimating the carbon dioxide production of

four Commonwealth of Independent States (CIS) countries based on GDP, coal, oil, natural gas and renewable energies consumption as the inputs of the model. The data used for modeling are extracted from various references between 2000 and 2017 in order to have a comprehensive and reliable dataset as the inputs of the models. Details on the employed algorithm and modeling procedure explained in the following sections.

2. Method

A model is established by GMDH neural networks with the utilization of a multi-layer network structure for a complex system based on the interactions of input-output data [22,23]. This neural network is closely similar to feedforward neural networks. GMDH is a self-taught method introduced by A.G. Ivakhnenko [24], and then, it is widely used for modeling of complex systems.

Each element in a neural network is literally a nonlinear equation between two inputs and one output, and its coefficients are determined by regression methods. Useless elements are automatically removed through the network construction process as a result of the inability to specify the accurate output and beneficial connections of each hidden layer remain since they are contributed in the precise prediction of the output and increase the total network efficiency. By repeating these steps, the GMDH neural network is finally reached, with the lowest error and high predictive power in determining the correct and close outcomes.

GMDH algorithm creates a model which is a collection of neurons in various layers. In other words, this neural network is a self-organized network, consisting of several layers and several neurons in each of the layers.

The network describes the approximate function of \hat{f} with the output of \hat{y} by combining quadratic polynomial resulted from all neurons for a set of inputs, $X = x_i; i = 1,2,3, \dots, n$, with the least

error in comparison to the actual output of y . Therefore, for the M experimentally measured data comprised of n inputs and a single output, the actual results are stated as follows:

$$y_j = f(x_{j1}, x_{j2}, \dots, x_{jM}) \quad (j = 1, 2, \dots, M) \quad (1)$$

The target is to achieve a neural network that can forecast the output value of \hat{y} for any input vector of X . Hence:

$$\hat{y}_j = \hat{f}(x_{j1}, x_{j2}, \dots, x_{jM}) \quad (j = 1, 2, \dots, M) \quad (2)$$

The proposed GMDH neural network should be able to minimize the squared error between the actual and forecasted values, in other words:

$$\sum_{j=1}^M (\hat{y}_j^2 - y_j^2) \rightarrow \min \quad (3)$$

The relationship between input and output variables can be stated by using the polynomial function as follows, i.e. Ivakhnenko polynomials:

$$y = a_0 + \sum_{i=1}^n a_i x_i + \sum_{i=1}^n \sum_{j=1}^n a_{ij} x_i x_j \quad (4)$$

In many cases, the quadratic and bivariate form of this polynomial is used as follows:

$$\hat{y} = G(x_i, x_j) = a_0 + a_1 x_i + a_2 x_j + a_3 x_i^2 + a_4 x_j^2 + a_5 x_i x_j \quad (5)$$

The unknown coefficients of a_i in Eq. (5) are determined by the regression method so that the difference between the actual output of y and the calculated values of \hat{y} for each pair of input variables, x_i and x_j , is minimized. A set of polynomials is established by using Eq. (5). The unknown coefficients of all of these polynomials are obtained using the least squares method. For

each function of G_i (each constructed neuron), the coefficients are obtained to minimize the total neuron error in order to achieve optimal fit of the inputs with the total pair of output-input sets:

$$E = \frac{\sum_i^M (y_i - G_i)^2}{M} \rightarrow \min \quad (6)$$

In the basic methods of the GMDH algorithm, all binary compounds (neurons) are constructed by n input variables, and the unknown coefficients of the neurons are obtained using the least squares approach. Therefore, $\binom{n}{2} = \frac{n(n-1)}{2}$ neurons in the second layer are constructed as follows:

$$\{(y_j, y_{jp}, y_{jq}) | (j = 1, 2, \dots, M) \& p, q \in (1, 2, \dots, M)\} \quad (7)$$

The second-order form of the expressed function, Eq. (6), is utilized for each M triple row. These equations expressed in the following matrix form:

$$Aa = Y \quad (8)$$

Where A represents the vector of unknown coefficients of the second order equation:

$$a = \{a_0, a_1, a_2, a_3, a_4, a_5\} \quad (9)$$

$$Y = \{y_1, y_2, y_3, \dots, y_M\}^T \quad (10)$$

For M series of experimental data the vector of coefficients is determined as follows:

$$A = \begin{bmatrix} 1 & \mathcal{X}_{1p} & \mathcal{X}_{1q} & \mathcal{X}_{1p}^2 & \mathcal{X}_{1q}^2 & \mathcal{X}_{1p}\mathcal{X}_{1q} \\ 1 & \mathcal{X}_{2p} & \mathcal{X}_{2q} & \mathcal{X}_{2p}^2 & \mathcal{X}_{2q}^2 & \mathcal{X}_{2p}\mathcal{X}_{2q} \\ M & M & M & M & M & M \\ 1 & \mathcal{X}_{Mp} & \mathcal{X}_{Mq} & \mathcal{X}_{Mp}^2 & \mathcal{X}_{Mq}^2 & \mathcal{X}_{Mp}\mathcal{X}_{Mq} \end{bmatrix} \quad (11)$$

By using the least squares method with the utilization of regression analysis:

$$a = (A^T A)^{-1} A^T A \quad (12)$$

This equation gives the vector of coefficients of Eq. (6) for all M triple sets.

3. Results and discussion

In this paper, four CIS countries, including Uzbekistan, Turkmenistan, Azerbaijan and Kazakhstan, are considered as the cases of the study. CIS countries have experienced economic growth after 2000 as illustrated in Figure 2; as a consequence, due to the requirement of energy for economic and industrial activities, their overall energy consumption has increased after 2000 as shown in Figure 3. According to Figure 3, the overall primary energy consumption of these countries has increased from 104.57 *Mtoe* in 2000 to approximately 156 *Mtoe* in 2017 which indicates average annual growth rate of 2.25%. Due to the dependency of environmental issues on the economic activities of the countries and their energy consumption, it is crucial to analyze their GHG emission based on the GDP as indicator of economic activities.

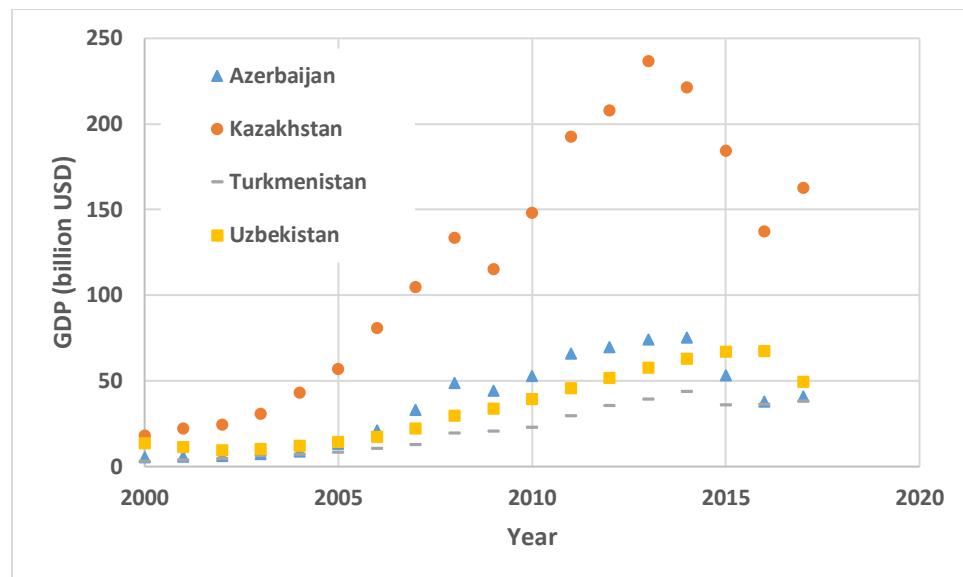


Figure 2 GDP of the investigated countries [3]

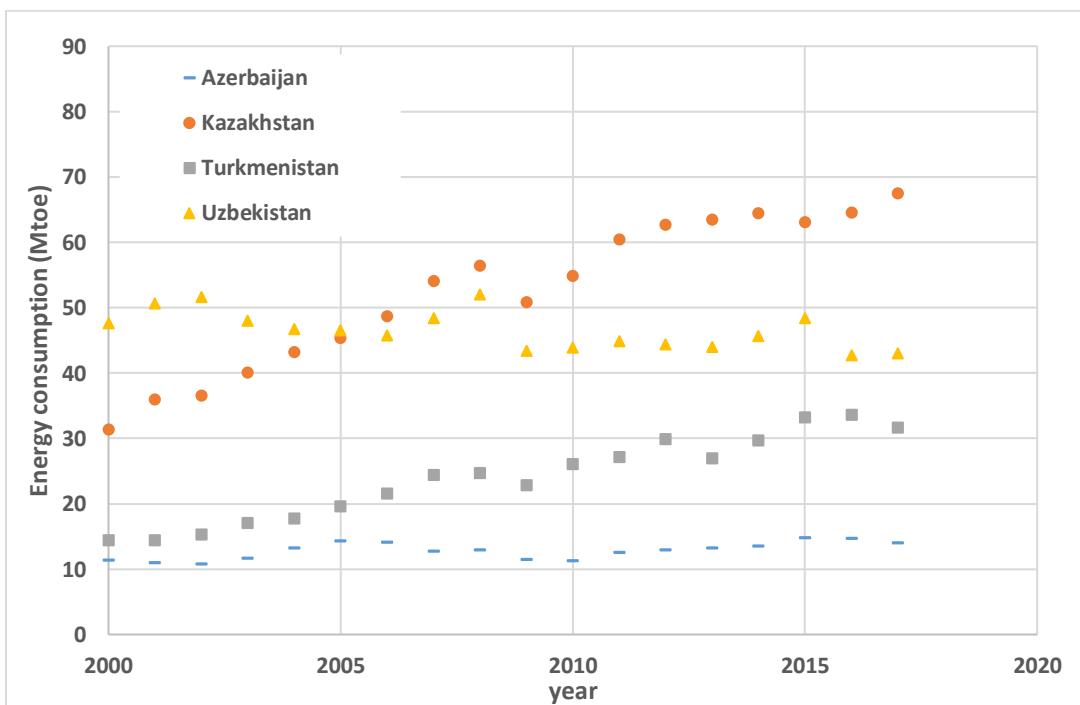


Figure 3 Total primary energy consumption of the investigated countries [3]

In addition to GDP, consumption of various conventional fuels must be used as input variables due to the dependency of production of carbon dioxide on the type of fuels. The emission of carbon dioxide from the combustion depends on their type as shown in Figure 4. Therefore, the input variables of the model used for carbon dioxide estimation of carbon dioxide production are GDP,

consumptions of oil, renewable energy sources (including hydropower and other renewable energy consumptions), natural gas and coal which are similar to the previous study [1]. All the data utilized for modeling are extracted in the period of 2000 and 2017.

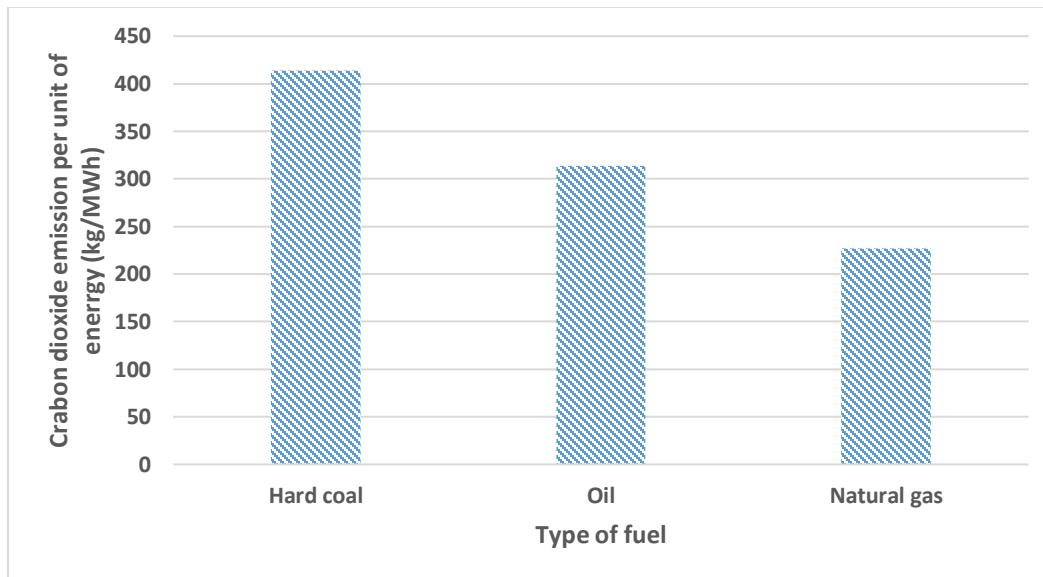


Figure 4 Carbon dioxide emission of various fuels [25]

In the first step, a linear correlation is used to find the correlation between the inputs and output. The obtained correlation by considering the mentioned data is:

$$\text{Carbon Dioxide emission} = -0.00283 * x_1 + 2.860766 * x_2 + 4.051923 * x_3 + 2.382961 * x_4 - 1.67667 * x_5 - 0.32311$$

Where x_1 , x_2 , x_3 , x_4 , and x_5 denote GDP, oil, coal, natural gas, and renewable energies consumptions. Based on the calculated coefficients of the correlation, coal has the most significant effect on the emission of CO_2 . In addition, since the coefficient of renewable energy is negative, it can be concluded that development in the renewable energy systems leads to reduced GHG emission. The actual outputs and the corresponded correlation values are represented in Figure 5. As it is represented, the R-squared value by using the correlation is equal to 0.9997.

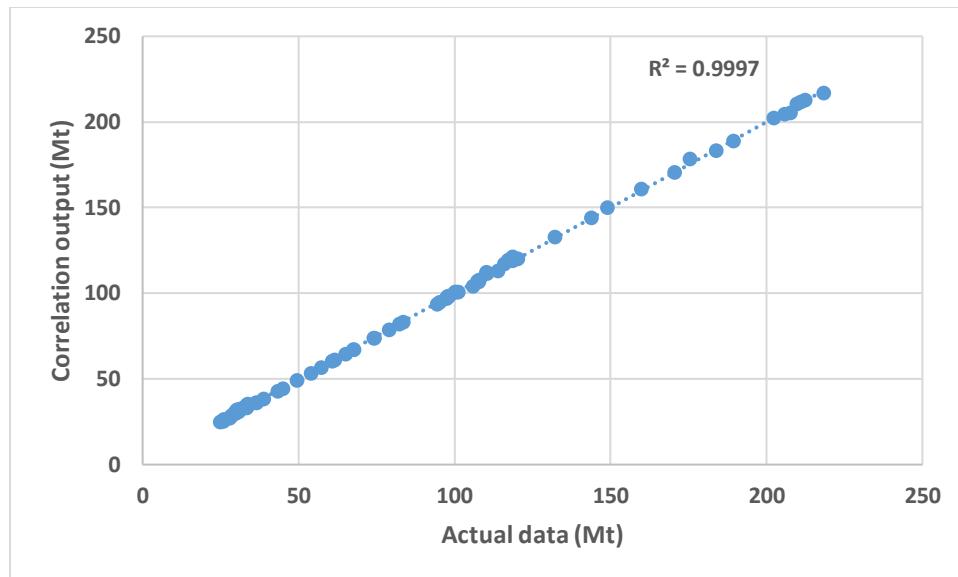


Figure 5 Actual data vs model's outputs in the case of applying linear correlation

In Figure 6, the relative deviation for each data index is represented. According to the comparison between the correlation output and actual data, the highest absolute relative deviation is approximately 5.01%. This value demonstrates acceptable accuracy of the correlation as a predictive tool. The average absolute relative deviation of the proposed correlation is about 1.05%.

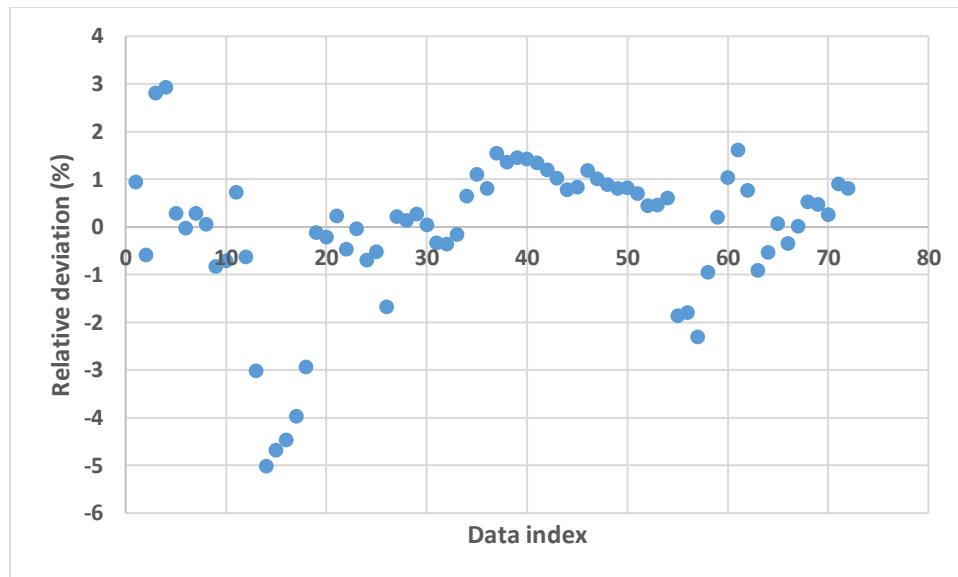


Figure 6 Relative deviation of model's outputs in the case of applying linear correlation

In Figure 7, the actual data and the corresponded calculated value by the correlation are represented. Comparing the values, both actual ones and correlation outputs, reveals the precision of the correlation in estimating CO_2 emission of the investigated countries.



Figure 7 Figure 10 Comparison between model outputs and actual data in the case of applying linear correlation

In addition to correlation, an ANN-based model is proposed to compare the results. The schematic of the model is shown in Figure 8.

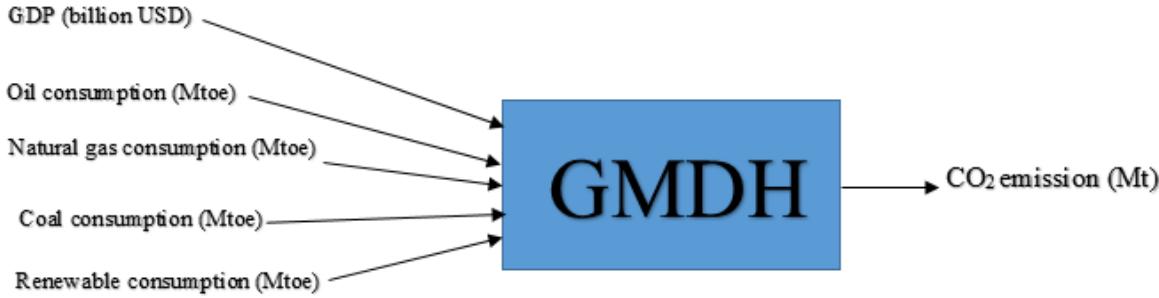


Figure 8 Schematic of the model

As it was indicated, GMDH ANN is employed for estimating the carbon dioxide emission. In order to train and evaluate the model, the data are divided into two subsets. The first subset includes 80% of data used for training the network while the remained ones utilized for testing the trained model. It should be mentioned that the data used for training and test are selected randomly. The obtained model based on the applied method and considered variables is:

$$\begin{aligned}
 \text{Carbon Dioxide emission} = & 61.3782 + (\sqrt[3]{x_4})^2 * 20.0219 + \sqrt[3]{x_4} * (-45.6416) + x_2 * 5.14946 + \\
 & (\sqrt[3]{x_1})^2 * (-0.173833) + x_3 * (\sqrt[3]{x_4})^2 * 0.107793 + x_3 * 4.18515 + \sqrt[3]{x_1} * \sqrt[3]{x_5} * 0.380529 + \sqrt[3]{x_2} * (- \\
 & 24.137) + x_2 * \sqrt[3]{x_1} * 0.24157 + x_2 * \sqrt[3]{x_3} * (-0.276629) + x_4 * \sqrt[3]{x_1} * (-0.05225) + x_4 * \sqrt[3]{x_2} * (-0.182136) \\
 & + x_2 * x_3 * (-0.0266378)
 \end{aligned}$$

Where x_1 , x_2 , x_3 , x_4 , and x_5 denote GDP, oil, coal, natural gas, and renewable energies consumptions. In order to assess the model's precision, some statistical criteria are used [26]. In the first step, the model is evaluated on the basis of R-squared value. As illustrated in Figure 9,

comparing the actual data and the outputs of the obtained model reveals that this value is 0.9999.

This value is very close to 1, which means high accuracy of the proposed regression.

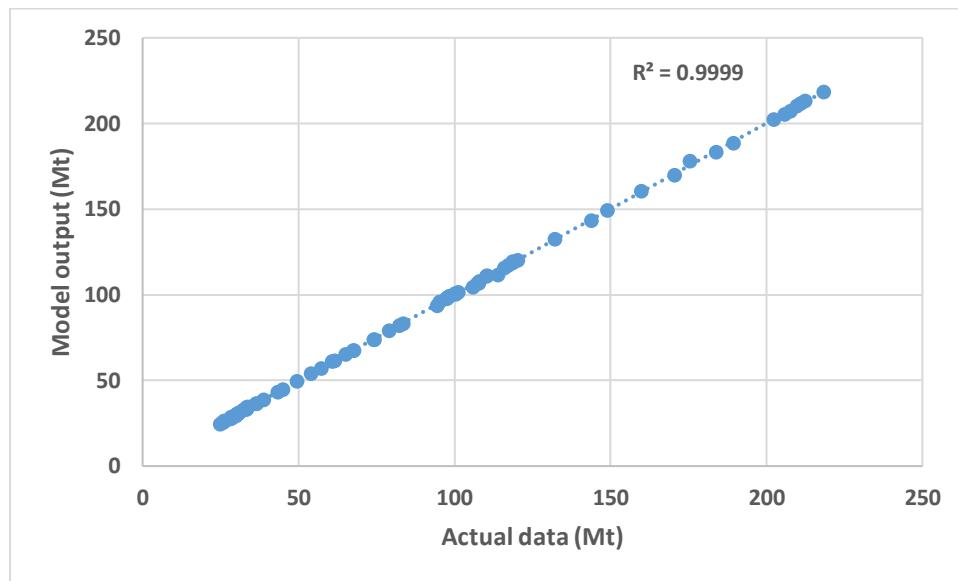


Figure 9 Actual data vs model's outputs in the case of applying GMDH

Another criterion used for evaluation is the absolute relative deviation. Based on this criterion, the model can accurately forecast the emission of carbon dioxide, which can be attributed to both model ability and appropriateness of the selected input variables. According to Figure 10, the highest absolute relative deviation of the obtained model is approximately 2.81%, which is another indicator of the model's acceptable accuracy. Moreover, the average absolute relative deviation of this model is about 0.61%. It should be mentioned that since the data are divided into two subsets in the case of using ANN, which are randomly used for train the network and test, the data indexes are different from the correlation.

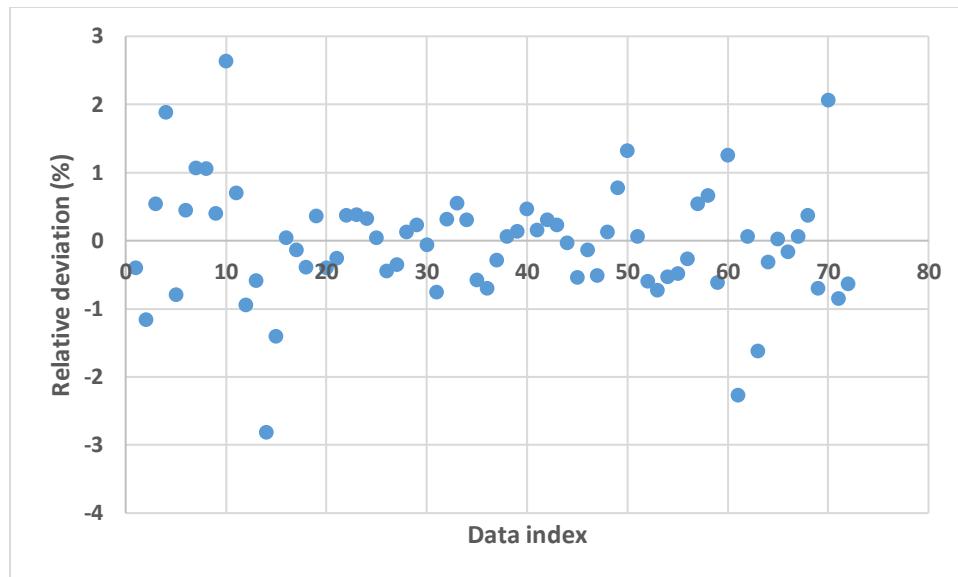


Figure 10 Relative deviation of model's outputs in the case of applying GMDH

In order to gain more appropriate insight into the model outputs, the actual data and corresponded model outputs are compared in Figure 11. As it can be observed, the data are in the close vicinity of each other. In the majority of the cases, the data obtained by the regression and actual data are approximately equal. Therefore, it can be concluded the model is very reliable to predict carbon dioxide emission and analyze the share of each input variable on it. By applying this model, production of carbon dioxide in the investigated countries can be accurately estimated for different scenarios in future years.

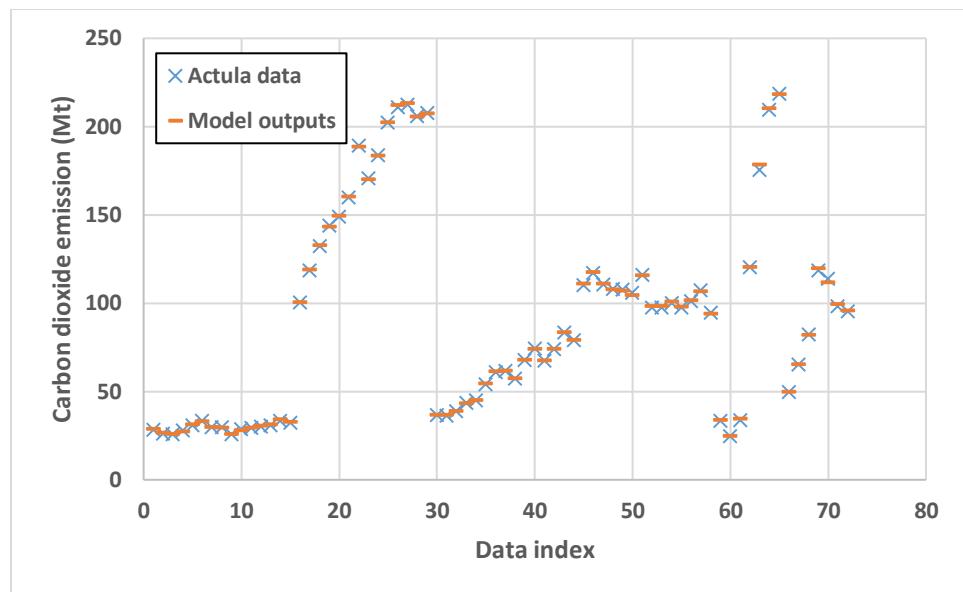


Figure 11 Comparison between model outputs and actual data in the case of applying GMDH

4. Conclusion

The emission of carbon dioxide depends on several factors such as share of energy sources in total primary energy consumption and the economic activities. In this paper, four CIS countries including Uzbekistan, Turkmenistan, Azerbaijan and Kazakhstan, are considered as cases of the study to model the carbon dioxide production on the basis of GDP, as an economic indicator, and consumption of various fuels and renewable energies. The employed methods for modeling are linear correlation and GMDH ANN. The R-squared values obtained by the correlation and ANN-based model are 0.9997 and 0.9999, respectively. In addition, the average absolute relative deviations in out the cases of using the correlation and GMDH are about 1.05% and 0.61%, respectively. It is concluded that using GMDH in modeling the emission of carbon dioxide results in more precise estimation.

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